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J. B LIPPINCOTT & CO. PHILADELPHIA.

POCKET-BOOK

OF

MECHANICS

AND

ENGINEERING.

CONTAINING

A MEMORANDUM OF FACTS AND CONNECTION

OF

PRACTICE AND THEORY.

RV

JOHN W. NYSTROM, C.E.

SEVENTEENTH EDITION REVISED AND GREATLY ENLARGED

WITH

ORIGINAL M

TTER.

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J. B. LIPPINCOTT & CO.

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PREFACE.

Every Engineer should make his own Pocket-Book, as he proceeds in study and practice, to suit his particular business. The present work has been accumulated in that way during the author's professional career. It was originally not intended for publication, but grew too large for the pocket in form of manuscript, which circumstance, combined with repeated requests to publish it, first placed it before the public in the year 1854.

The author claims to have given a goodly share of original matter, and has spent much labor and money in experiments on

subjects requiring elucidation.

The authors consulted are distinguished experimenters, such as Dalton, on air and heat; Regnault, on steam; Kopp, on the expansion of water; Morin, on friction and strength of materials; Joule, on the mechanical equivalent of heat; the Franklin Institute, on the strength of iron and copper at different temperatures; the Royal Technological Institute, Stockholm, on dynamics; and various others of equal authority; but these savans are not responsible for the formulas and tables which are herein deduced from their experiments.

The solution of mathematical formulas leads to powerful presumptions in the revelation of physical laws, which could never be attained or realized from mere observation of facts in experiments and practice. All observation and contemplation which involves mind, involves theory, which is the foundation of our practice

and progress.

A knowledge of algebra is not necessary for the use of the formulas, and it is satisfactory to know that most engineers who are not versed in mathematics have acquired the very important habit of inserting numerical values for the corresponding letters, which they prefer to cumbrous written rules, which are impracticable in extensive problems. If all the formulas herein were explained in words, the book would exceed in volume Webster's unabbreviated Dictionary, and the matter would be only so much the more complicated. The algebraical formulas herein are solved into all their functions, ready to receive what is given and refund what is required. They not only tell what is to be done, but at a glance impress the mind with the complete operation.

JOHN W. NYSTROM.

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INTRODUCTION.

Quantity is that which can be increased or diminished by augments or abatements of homogeneous parts. Quantities are of two essential kinds, Geometrical and Physical.

1st, Geometrical quantities are those which occupy space; as lines, surfaces.

solids, liquids, gases, &c.

2nd, Physical quantities are those which exist in the time but occupy no space, they are known by their character and action upon geometrical quantities; as

attraction, light, heat, electricity and magnetism, colours, force, power, &c., &c.

To obtain the magnitude of a quantity we compare it with a part of the same, this part is imprinted in our mind as a unit, by which the whole is measured and conceived. No quantity can be measured by a quantity of another kind, but any quantity can be compared with any other quantity, and by such comparison arises what we call calculation or Mathematics.

MATHEMATICS.

Mathematics is a science by which the comparative value of quantities are investigated; it is divided into:

1st, Arithmetic,—that branch of Mathematics, which treats of the nature and property of numbers; it is subdivided into Addition, Subtraction, Multiplica-

tion, Division, Involution, Evolution and Logarithms.

2nd, Algebra,—that branch of Mathematics which employs letters to represent quantities, and by that means performs solutions without knowing or noticing the value of the quantities. The subdivisions of Algebra are the same as in Arithmetic.

3rd, Geometry,—that branch of Mathematics which investigates the relative property of quantities that occupies space; its subdivisions are Longimetry, Planemetry, Stereometry, Trigonometry, and Conic Sections.

4th, Differential-calculus, - that branch of Mathematics, which ascer-

tains the mean effect, produced by group of continued variable causes.

5th, Integral-calculus,—the contrary of Differential, or that branch of Mathematics which investigates the nature of a continued variable cause, that has produced a known effect.

ARITHMETIC.

The art of manæuvering numbers, and to investigate the relationship of quantities.

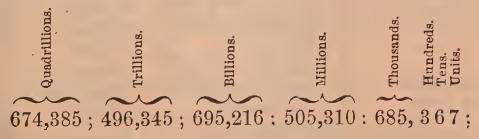
Figures-1, 2, 3, 4, 5, 6, 7, 8, 9. Arabic digits, about nine hundred years old. Ciphers-0, 0, 0. Sometimes called noughts, it is the beginning of figures and things.

Number is the expression of one or more figures and ciphers.

Integer is a whole number or unit.

Fraction is a part of a number or unit.

When figures are joined together in a number, the relative dignity expressed ly each figure, depends upon its position to the others. Thus,



ROMAN NOTATION.

The Romans expressed their numbers by various repetitions and combinations of seven letters in the alphabet; as,

1 = I. 2 = II. 3 = III. 4 = IV.5 = V. 6 = VI. 7 = VII.8 = VIII.9 = IX. 10 = X. 20 = XX30 = XXX. $40 = XI_{1}$. 50 = L. 60 = LX70 = LXX. 80 = LXXX. 90 = XC.100 = C.

EXAMPLES.—1872.—MDCCCLXXII.

500 = D, or LO. 1,000 = M, or CO. 2,000 = MM, or IIOOO. 5,000 = V, or LOO. 6,000 = VI, or MMM $10,000 = \overline{X}$, or COO. $50,000 = \overline{L}$, or LOOO. $60,000 = \overline{LX}$, or MMMO. $100,000 = \overline{C}$, or COOO. $1,000,000 = \overline{M}, \text{ or COOOO}.$ $2,000,000 = \overline{MM}$, or MMOOO.

A bar, thus, — over any number, increases it 1000 times.

524,365, DXXIVCCCLXV.

An imperfection in the Roman Notation consists in the fact that there is no signification for the cipher, as in the Arabic Notation.

Signification of Characters.

= Equality, as 6 = 6, reads 6 is equal to 6. + Plus, Addition, 3+6=9- Minus, Subtraction, 6-2=4 \times Multiplication, . $3 \times 4 = 12$ \div or: Division, . . 15:5=3 $\sqrt{\text{Square root}}, \dots \sqrt{9} = 3$ $\sqrt[3]{}$ Cube root, ... $\sqrt[3]{}8=2$ > Greater, 8>4 < Less, 6<9 ∞ Infinite, . . .

f. Integral, . . . f dy = y. dy Differential, . . dy = dx + .3/4 Fraction, . . M Ship sign, dead flat, Furnace fire-grate. O Boiler heating-surface. # Sharp. High. b Flat. Low. π Periphery.

Astronomical Characters.

Planets.

- O The Sun.
- C The Moon.
- o Mercury,
- Q Venus,
- 1 The Earth.
- d Mars.
- Q Ceres.
- ♀ Pallas.
- Duno.
- † Vesta.
- 4 Jupiter.
- h Saturn.
- H Uranus.
- W Neptune.

- d Conjunction in the same degree or sign, or having the same longitude or Right Ascension.
- X Sextile, when two signs distant, or differing 60° in longitude or Right Ascension.
- ☐ Quartile, when three signs distant, or differing 90° in Longitude or Right Ascension.
- 8 Opposition, when six signs distant, or differing 180° in Longitude or Right Ascension.
- Ascending Node. Descending Node.
- R. A. Right Ascension.

Signs of the Zodiac.

- TAries, 8 Taurus, □ Gemini, . ⊆ Cancer,
- Ω Leo, .
- M Virgo, . ← Libra,
- M Scorpio, . . # Sagittarius,
- V> Capricornus,
- 🐃 Aquarius, .
- → Pisces, . .

ALGEBRA.

In Algebra we employ certain characters or letters to represent quantities. These characters are separated by signs, which describe the operations; and by

that means, simplify the solution.

1. Whatever the value of any quantity may be, it can be represented by a character, as a. Another quantity of the same kind, but of different value, being represented by b. The sum of these two quantities is of the same kind but of different value.

For Addition we have the algebraical sign +, (plus) which, when placed

between quantities, denotes they shall be added; as a+b, reads in the algebraical language, "a plus b," or a is to be added to b.

Another algebraical sign =, (Equal) denotes that quantities which are placed on each side of this sign, are equal. Let the sum of a and b be denoted by the letter c; then we have,

a+b=c.

This composition is called an algebraical equation. The quantity on each side of the equal sign is called a member, as a+b, is one member, and c, the other. When one of the members contains only one quantity, that member is generally placed on the first side of the equal sign, and its value commonly unknown; but the value of the quantities in the other member being given, as a=4, and b=5, then the practical mode, to insert numerical values in algebraical equations, will appear; as,

> Equation, c=a+b, 4+5=9, the value of c.

2. The sum of three quantities a, b, and c, is equal to d, then

Equation, d=a+b+c, 4+5+9=18, the value of d.

3. For Subtraction we have the algebraical sign, -, (minus) which, when placed before a quantity, denotes it is to be subtracted as, a-b, reads in the algebraical language "a minus b," or from a, subtract b. Let the difference be denoted by the letter c; and a=8. b=3

> Equation, c=a-b, 8-3=5, the value of c.

4. From the sum of a and b, subtract c, and the result will be d; then,

Equation, d=a+b-c, 8+3-5=6, the value of d.

5. When two equal quantities are to be added, as a+a it is the same as to take one of them twice, and is marked thus 2a. The number 2 is called the coefficient of the quantity a. If there are more than two equal quantities to be added, the coefficient denotes how many there are of them; as, 333

- - a+a=2a, Equation, • 'd: 8, a + a + a = 3aa + a + a + a = 4adc., dc.

When the quantities are separated by the signs, plus, or minus, they are called terms.

6. **Multiplication.**—When a quantity a, is to be multiplied by another quantity b, then a and b are called factors; and separated by no sign as ab; which denotes that a is to be multiplied by b; but when the values of a and b are expressed by numbers, they are separated by the sign \times (Multiplication); the result from Multiplication is called the product. Let a=8, and b=6, and the product of a and b to be a, then duct of a and b, to be c, then,

Equation, c=ab, $8 \times 6 = 48$, the value of c.

7. The product of a and b, is to be multiplied by c, and the latter product will be equal to d; then,

Equation, d=abc, $8\times6\times48=2304$, the value of d. 8. The sum of a and b, is to be multiplied by c, and the product will be d; then,

Equation,
$$d=c$$
 $(a+b)$,
48 $(8+6)=672$ the value of d .

When the sum of two or more quantities is to be multiplied by another quantity, the sum is to be enclosed in parentheses, and denotes itself to be one factor. The other factor is to be placed on the outside of the parentheses, as seen in the preceding example.

9. To the product of a and c, add b, and the result will be d; then,

Equation,
$$d = ac + b$$
, $8 \times 48 + 6 = 390$ the value of d.

Be particular to distinguish the two Examples 8, and 9.

10. The sum of a and b, to be multiplied by the sum of a and c; the product will be d; then,

Equation,
$$d = (a+b) (a+c),$$
 (8+6) (8+48) = 784.

11. The sum of c and b, to be multiplied by the difference of c and a; the result will be d; then,

Equation,
$$d = (c+b)(c-a)$$
, $(48+6)(48-8) = 2160$.

12. **Division.**—When a quantity a, is to be separated into b equal parts, the numbers of parts or b, is called the *divisor*, and the value of each part, is called the *quotient*. The sum of the parts or the whole quantity a, is called the *dividend*; a and b, is separated by the sign: (Division); as a:b, reads in the algebraical language, "a divided by b." Let the *quotient* be denoted by the letter c; and a=18, b=6, then,

Equation,
$$c = a : b$$
,
 $18 : 6 = 3$ the quotient c .

In Algebra it is found more convenient to set up Division as a fraction, then it will appear as,

13. Divide a, by c, and the quotient will be b. Then,

Equation,
$$b = \frac{a}{c}$$
, $\frac{18}{3} = 6$ the quotient b.

14. The product of a and b, to be divided by c; and the product will be d. Then,

Equation,
$$d = \frac{ab}{c}$$
,
$$\frac{18 \times 6}{3} = 36.$$

15. The sum of d and b, to be multiplied by c, and the product divided by a; then the result will be c.

Equation,
$$e = \frac{c (d+b)}{a}$$
, $\frac{3 (36+6)}{18} = 7$.

16. From the product of a and c, subtract 3b; divide the remainder by the difference of a, and c; the result will be h.

Equation,
$$h = \frac{ac - 3b}{a - c}$$
, $\frac{18 \times 3 - 3 \times 6}{18 - 3} = 2.4$.

An old man said to a smart boy, "How old are you?" to which he replied .-"To seven times my father's age add yours, divide the sum by double the difference of yours and his, and the result will be my age."

Letters will denote, a =the old man's age, b =the father's age, c = the boy's age. Then,

Equation,
$$c = \frac{7b + a}{2(a-b)}$$
 the boy's age.

Now for any number of years of the old man and the father, will be a corresponding age of the boy; suppose,

a = 73 years the age of the old man, b = 57 years the father's age. Require the boy's age.

$$c = \frac{7 \times 57 + 73}{2(73 - 57)} = 143$$
 years.

PROPORTION.

THE relative value of two quantities, is obtained by dividing one into the other, and the quotient is called the ratio of their relationship. If the ratio of two quantities is equal to the ratio of two other quantities, they are said to be in the same proportion; as, a:b=c:d,

reads in the algebraical language "a is to b as c is to d."—a, b, c, and d, are callreads in the algebraical language "a is to b as c is to a."—a, b, c, and a, are called et terms, of which a is the first, b the second, c the third, and d the fourth term. The first and fourth are called "the outer terms," and the second and third, "the inner terms." The whole is called an "analogue." A property in the nature of analogies is, that the product of the outer terms ad, is equal to the product of the inner bc. Suppose a = 4, b = 9, c = 12,

d - 27.

$$ad=bc, 4 \times 27 = 9 \times 12.$$

If any one of the four quantities are unknown, its value can be calculated by the other three; as,

$$a = \frac{bc}{d} = \frac{9 \times 12}{27} = 4,$$

$$b = \frac{ad}{c} = \frac{4 \times 27}{12} = 9,$$

$$c = \frac{ad}{b} = \frac{4 \times 27}{9} = 12.$$

$$d = \frac{bc}{a} = \frac{9 \times 12}{4} = 27.$$

SIMPLE INTEREST.

Interest is a profit on money which is lent for a certain time.

Letters will denote.

c == the standing capital, or lent money.

r =interest on the capital c,

p = per cent. on 100 in the certain time.

Analogy,

$$c: r = 100: p.$$

If p is the per cent. on 100, in one year, then t =time in years for the standing capital c, and the interest r.

Analogy,

$$c: r = 100: pt.$$

From this analogy we obtain the equations,

Interest,
$$r=\frac{cpt}{100}$$
, -1 , $p=\frac{100 \ r}{tc}$, -2 ,

Now for any question in Simple Interest, there is one equation which gives the answer. If the time is given in months, weeks, or days, multiply the 100 correspondingly by 12, 52, 365.

Example 1. What is the interest on \$3789.35, for 3 years and five months, at 6 per cent. per annum?

 $\dot{t} = 3 \times 12 + 5 = 41$ months, from the Equation 1, we have,

Interest,
$$r = \frac{3789.35 \times 6 \times 41}{12 \times 100} = 776.81$$
 Dollars.

Example 2. A capital c = \$469.78, gave an interest r = 150.72 dollars, in a time t = 4 years and 7 months. Require the per centage per annum? $t = 4 \times 12 + 7 = 55$ months, from Equation 2, we have,

Per cent.,
$$p = \frac{12 \times 100 \times 150.72}{469.78 \times 55} = 7$$
 per cent.

Example 3. What capital is required to give an interest r=345 Dollars in 6 years, at 5 per cent. per annum? From the Equation 3, we have,

Capital,
$$c = \frac{100 \times 345}{5 \times 6} = $1150.$$

Example 4. A capital c = \$2365 shall stand until the interest will be r = 550 Dollars, at p = 6 per cent. per annum. How long must the capital stand? From the Equation 4, we have,

Time,
$$t = \frac{100 \times 550}{2365 \times 6} = 3.876 \text{ years.}$$

 $12\times0.876=10.512$ months, $4\times0.512=2.048$ weeks, the time t=3 years, 10 months, and 2 weeks.

REBATE OR DISCOUNT.

Rebate or **Discount** is an allowance on money which is paid before due. a = amount of money to be paid in the time t. By agreement the amount is paid with a capital c, at the beginning of the time t, but discounted a Rebate r, at p per cent., so that the interest on the capital c, at p per cent., should be equal to the Rebate r, in the time t. a = c + r.

Rebate,
$$r = \frac{a p t}{100 + pt}$$
. 5. Time, $t = \frac{100(a - c)}{c p}$. 8. Capital, $c = \frac{100a}{100 + p t}$. 6. Amount, $a = \frac{c}{100}(100 + p t)$. 9. Per cent., $p = \frac{100(a - c)}{c t}$. 7. Amount, $a = \frac{r}{p t}(100 + p t)$. 10.

Now, for any question in Rebate or Discount, there is one equation that will give the answer.

Example 5. A sum of money, a = 78460 dollars, is to be paid after 3 years and 6 months, but by agreement payment is to be made at the present time. What will be the Rebate, at 7 per cent.?

Rebate,
$$r = \frac{78460 \times 7 \times 3.5}{100 + 7 \times 3.5} = $15439.91.$$

FELLOWSHIP.

Fellowship or Partnership is a rule by which companies ascertain each fellow's profit or loss by their stock. Each fellow's part in the stock is called his share. The sum of shares is called the stock.

Fellowships are of two kinds, Simple and Double.

Simple Fellowship, when there is no regard to the time, the shares or stock is employed.

Letters will denote,

A = share of either one fellow. a = profit or loss on the share A. S = stock or the sum of the shares. s = gain or loss on the stock S. Then, A : a = S : s.

Example 1. A person had invested A = \$11645 in a stock S = \$64800, which gave a gain of s = \$13864. What will be the profit of the person's share?

Profit,
$$\alpha = \frac{11645 \times 13864}{64800} = $2491.45.$$

Double Fellowship. When the different shares are employed at a different length of time, each share is multiplied by its time employed, and the product is the *effect* of the share.

Letters will denote,

t = time for the employed share A. T = mean time for the employed stock S. e = effect of the share A. a = 1 E = 6 a = 1

a = profit of the effect e. E = effect of the stock. s = gain of the effect E.

Then, e:a=E:s.

Formulas for Double Fellowship.

Example 2. A canal is to be dug, and requires an effect E=76850 (men and days) to be accomplished; after that it will give a gain s=12390 dollars. An employer has A = 168 laborers. How many days must those laborers be employed at the canal, that the employer will obtain a profit a = 5000 dollars?

Time,
$$t = \frac{5000 \times 76850}{168 \times 12390} = 184.6 \text{ days.}$$

PERMUTATION.

Permutation is to arrange a number of things in every possible position. It is commonly used in games.

Example 1. How many different values can be written by the three figures 1, 2, 3.

1, 2, 3. 3 = 6 different values, namely, 123, 132, 213, 231, 312, 321. With any three different figures can be written six different values. Any three things can be placed in 6 different positions.

Example 2. How many names can be written by the three syllables, mo, ta, la? The answer is, Motala, Molata, Tamola, Talamo, Lamota, Latamo.

Example 3. How many words can be written by the five syllables, mul, tip, li, ca, tion?

 $1 \times 2 \times 3 \times 4 \times 5 = 120$ words, the answer.

COMBINATION.

Combination is to arrange a less number of things out of a greater in every possible position. It is commonly used in games.

Example 1. How many different numbers can be set up by the nine figures, 1, 2, 3, 4, 5, 6, 7, 8, 9, and three figures in each number?

$$\frac{9 \times 8 \times 7}{1 \times 2 \times 3} = 84 \text{ different numbers.}$$

Example 2. How many different variations can a player obtain his cards, when the set contains 52 cards, of which he receives 8 at a time?

$$\frac{52\times51\times50\times49\times48\times47\times46\times45}{1\times2\times3\times4\times5\times6\times7\times8} = 752538150 \text{ variations.}$$

If there are four players, and p r. 4 = 24, they can play $24 \times 752538150 =$ 18,060,915,600 different plays.

If it takes half an hour for each play, and they play 8 hours per day, it will take

$$\frac{18060915600}{2 \times 8} = 1128807225 \text{ days} = 3092622 \text{ years.}$$

ALLIGATION.

Alligation is to mix together a number of different things of different price or value, and ascertain the mean value of the mixture; or from a given mean value of a mixture ascertain the proportion and value of each ingredient.

Let the different things be a, b, c and d, etc., their respective price or value per

unit, z, y, x and w, etc.

A = a + b + c + d, etc., the sum of the things.

P = mean value or price per unit of A.

Then,
$$A P = a z + b y + c x + d w +, \text{ etc.} \qquad . \qquad . \qquad 1.$$

and
$$P = \frac{az + by + cx + dw + cx}{A}$$
, etc.

Example 1. If 3 gallons of wine, at \$1.37 per gallon, 2, at \$2.18, and 5, at \$1.75, be mixed together, what is a gallon worth of the mixture?

$$A = 3 + 2 + 5 = 10$$
 gallons.
 $P = \frac{3 \times 1.37 + 2 \times 2.18 + 5 \times 1.75}{10} = 1.72 per gallon.

Alligation of two ingredients, a and b, with their respective prices or value per $z > P > y. \qquad A = a + b.$ unit, z and y.

$$a:b=(P-y):(z-P)$$
. 3. $a=\frac{b(P-y)}{(z-P)}$, and $a=\frac{A(P-y)}{(z-y)}$. . . 4 & 5.

Example 2. A silversmith will mix two sorts of silver, one at 54 and one at 64 cents per ounce. How much must be taken of each sort to make the mixture worth 60 cents per ounce? (Formula 3.) P = 60. x = 54. y = 64.

$$a:b=(60-54):(64-60)=6:4$$
, or

4 ounces, at 54 cents, and 6 ounces, at 64 cents.

Alligation of three ingredients, a, b and c, with their prices or value per unit, z, y and x.

Example 3. A farmer will mix wheat, at 94 cents per bushel, with barley, at 72 cents, rye, at 64 cents per bushel. How much of each sort must be taken to make the mixture worth 80 cents per bushel?

(Formula 6.) z = 94, y = 72, x = 64, and P = 80.

$$a': c' = (80 - 64): (94 - 80) = 16: 14.$$

 $a': b = (80 - 72): (94 - 80) = 8: 14.$

The wheat a = 16 + 8 = 24 bushels, at 94 cents per bushel.

The wheat
$$a = 16 + 8 = 24$$
 bushels, at 94 cents per "barley $b = 14$ " "72" " $c = 14$ " "64" "

Alligation of four ingredients a, b, c and d, respective prices or value per unit. z, y, x and w.

$$\begin{array}{ll} a:d = (P-w):(z-P) \\ b:c = (P-y):(x-P) \\ when \ z > y > P > x > w > \begin{cases} 9, \\ 10, \\ 11, \\ 12, \\ 13, \\ 13, \\ 12, \\ 13, \\ 13, \\ 14, \\ 15, \\ 16$$

In the same manner, formulæ can be set up for any number of ingredients.

ARITHMETICAL PROGRESSION.

Arithmetical Progression is a series of numbers, as 2, 4, 6, 8, 10, 12, &c., or 18, 15, 12, 9, 6, 3, in which every successive term is increased or diminished by a constant number.

Letters will denote,

a = the first term of the series.

b =any other term whose number from a is n.

n = number of terms within a and b.

 δ = the difference between the terms.

S =the sum of all the terms.

In the series, 2, 5, 8, 11, $\alpha = 2$, b = 11, n = 4, $\delta = 3$, and S = 26.

When the series is decreasing, take the first term = b and the last term = a.

The accompanying Table contains all the formulas or questions in Arithmetical Progressions, and the nature of the question will tell which formula is to be used.

Formulas for Arithmetical Progressions.

$$a = b - \delta (n - 1), \qquad 1, \qquad \delta = \frac{b - a}{n - 1}, \qquad 9,$$

$$a = \frac{2S}{n} - b, \qquad 2, \qquad \delta = \frac{(b + a)(b - a)}{2S - a - b}, \qquad 10,$$

$$a = \frac{S}{n} - \frac{\delta}{2}(n - 1), \qquad 3, \qquad \delta = \frac{2(S - an)}{n(n - 1)}, \qquad 11,$$

$$b = a + \delta (n - 1), \qquad 4, \qquad \delta = \frac{2(b - an)}{n(n - 1)}, \qquad 11,$$

$$b = \frac{2S}{n} - a, \qquad 5, \qquad \delta = \frac{2(b - an)}{n(n - 1)}, \qquad 12,$$

$$b = \frac{S}{n} + \frac{\delta}{2}(n - 1), \qquad 6, \qquad S = \frac{a(a + b)(b + \delta - a)}{2S}, \qquad 13,$$

$$b = \frac{S}{n} + \frac{\delta}{2}(n - 1), \qquad 6, \qquad S = n\left[a + \frac{\delta}{2}(n - 1)\right] \qquad 15,$$

$$a = \frac{2S}{a + b}, \qquad 8, \qquad S = n\left[b - \frac{\delta}{2}(n - 1)\right] \qquad 16,$$

$$a = \frac{\delta}{2} + \sqrt{\left(b + \frac{\delta}{2}\right)^2 - 2SS}, \qquad 17,$$

$$b = \frac{\delta}{2} + \sqrt{\left(a - \frac{\delta}{2}\right)^2 + 2SS}, \qquad 18,$$

$$n = \frac{1}{2} - \frac{a}{\delta} + \sqrt{\left(\frac{1}{2} - \frac{\delta}{\delta}\right)^2 + \frac{2S}{\delta}}, \qquad 19,$$

$$a = \frac{1}{2} + \frac{b}{\delta} + \sqrt{\left(\frac{1}{2} + \frac{b}{\delta}\right)^2 - \frac{2S}{\delta}}, \qquad 20.$$

Example 1. A man was engaged to dig a well at one dollar (\$1) for the first foot of the depth of the well, \$1.84 for the second, and 84 cents more per every successive foot in depth, until he reached the water, which was found at a depth of 25 feet. How much money is due to the man?

This will be answered by the formula 15, in which a=1, d=0.84, and n=25, then the sum,

$$S = 25 \left[1 + \frac{0.84}{2} (25 - 1) \right] = $277 \text{ the answer.}$$

Example 2. A Propeller ship which is to run between Philadelphia and Charleston, cost \$116500, of which the company agreed to pay on account \$14075 at her first trip to Charleston; and per every successive trip, they paid \$650 less than the former. How many trips must the vessel make until she is fully paid?

This will be answered by the formula 20, in which b = \$14075, d = 650, and

S = 116500.

$$n = \frac{1}{2} + \frac{14075}{650} - \sqrt{\left(\frac{14075}{650} + \frac{1}{2}\right)^2 - \frac{2 \times 116500}{650}} = 10.6 \text{ or } 11 \text{ trips.}$$

Arithmetical Progressions of a Higher Order.

Arithmetical Progressions are of the first order, when the difference δ is a constant number, but when the difference δ progresses itself with a constant number, the Progression is of the second order.

When the difference δ progresses in a second order, the Progression is of the third order, &c., &c., and is thus explained:

Here you will discover that the sum of n terms in one order, is equal to the same nth term in the next higher order. Arithmetical Progressions of the first, second, and third orders, are applied to

PILES OF BALLS AND SHELLS.

Triangular Piling.

Example 1. A complete triangular pile of balls has n = 12 balls in each side. Require how many balls in the base, and how many in the whole pile?

In the base,
$$=\frac{12(12+1)}{2}=78$$
 balls, $=2d$. order.

Whole pile, $=\frac{12(12+1)(12+2)}{2\times 3}=364$ balls, $=3d$. order.

Square Piling.

1, 4, 9, 16, 25, 36, $=2d$. order.

1, 5, 14, 30, 55, 91, $=2d$. order.

[See Examples 2 and 3 on page 23]

GEOMETRICAL PROGRESSION.

Geometrical Progression is a series of numbers, as 2:4:8:16:32:&c., or 729.243:81:27:9: &c., in which every successive term is multiplied or divided by a constant factor.

Letters will denote,

a = the first term of the series.

b =any other term whose number from a is n.

n = number of terms within a and b.

r = ratio, or the factor by which the terms are multiplied or divided.

S = Sum of the terms.

In the series 1:3:9:27: a=1, b=27, n=4, r=3, S=40.

The accompanying Table contains all the formulas or questions in Geometrical Progressions. The nature of the question will tell which formula is to be used.

Formulas for Geometrical Progressions.

$$a = \frac{b}{r^{n-1}}, \qquad 1, \qquad r = \sqrt[n-1]{\frac{b}{a}}, \qquad 7,$$

$$a = S - r(S - b), \qquad 2, \qquad r = \frac{S - a}{S - b}, \qquad 8,$$

$$a = S \frac{r - 1}{r^{n-1}}, \qquad 3, \qquad ar^{n} + S - rS - a = 0, \qquad 9,$$

$$b = ar^{n-1}, \qquad 4, \qquad S = \frac{br - a}{r - 1}, \qquad 10,$$

$$b = S - \frac{S - a}{r}, \qquad 5, \qquad S = \frac{a(r^{n} - 1)}{r - 1}, \qquad 11,$$

$$b = S(\frac{r - 1}{r^{n} - 1})r^{n-1}, \qquad 6, \qquad S = \frac{b(r^{n} - 1)}{(r - 1)r^{n-1}}, \qquad 12,$$

$$n = 1 + \frac{\log b - \log a}{\log r},$$

$$18,$$

$$n = 1 + \frac{\log b - \log a}{\log (S+a) - \log (S-b)},$$

$$14,$$

$$n = \frac{\log [a+S(r-1)] - \log a}{\log r},$$

$$15,$$

$$n = 1 + \frac{\log b - \log [br - S(r-1)]}{\log r},$$

$$16,$$

$$S = \frac{b^{n-1}\sqrt{b} - a^{n-1}\sqrt{a}}{b^{n-1}\sqrt{b} - a^{n-1}\sqrt{a}},$$

$$17,$$

Example 1. Required the 10th term in the Geometrical Progression 4:12:3t....? Given a = 4, n = 10, and r = 3. We have,

Formula 4. $b = ar^{n-1} = 4 \times 3^9 = 78732$, the tenth term.

Example 2. Required the sum of the 10 terms in the preceding example?

Formula 11,
$$S = \frac{a(r-1)}{r-1} = \frac{4(3^{10}-1)}{2} = 118096$$
, the sum.

Example 3. Insert 6 proportional terms between 3 and 384? Given a = 3, b = 384, and n = 6+2 = 8.

Formula 7,

$$r = \sqrt[n-1]{\frac{b}{a}} = \sqrt[7]{\frac{384}{3}} = 2,$$

then

3:6:12:24:48:96:192:384, the answer.

Example 4. A man had 16 twenty dollar gold pieces, which he agreed to exchange for copper in such a way, that he gets one cent on the first \$20, two on the second, four on the third, and eight on the fourth, &c., &c.; until the sixteen \$20 pieces were covered. How many cents will come on the sixteenth gold piece, and what will be the whole amount of copper on the gold?

In the progression 1:2:4:8:&c., we have, Given n=16, r=2, and a=1, then,

Formula 4.
$$b = 1 \times 2^{16-1} = \frac{2^{16}}{2} = \frac{4^8}{2} = \frac{16^4}{2} = \frac{256^9}{2} = 32768$$
 cents, on the

sixteenth piece.

The total sum of cents will be found by the

Formula 10.
$$S = \frac{32768 \times 2 - 1}{2 - 1} = 65535 \text{ cents} = $655.35.$$

Piling of Balls and Shells .- [From page 21.]

Example 2. How many balls are contained in a complete square pile, n = 10 rows?

$$\frac{10(10+1)(2\times10+1)}{2\times3} = \frac{10\times11\times21}{6} = 385 \text{ balls.}$$

Rectangular Piling.

Let m be the number of balls on the top of the complete pile, and n = number of rows in the same, then the number of balls in the whole pile will be,

$$\frac{n(n+1)(2n+3m-2)}{2\times 3}$$
, • • 3d. order.

The number of balls in the longest bottom side will be = m+n-1.

Example 3. The rectangular pile having 15 rows and 23 balls on the the top, how many in the whole pile?

$$\frac{15(15+1)(2\times15+3\times23-2)}{2\times3} = \frac{15\times16\times67}{6} = 2680 \text{ balls.}$$

COMPOUND INTEREST.

Compound Interest is when the interest is added to the capital for each year, and the sum is the capital for the following year.

Amount,
$$a = c(1+p)^n$$
. 1. Percentage, $p = \sqrt[n]{\frac{a}{c}} - 1$. 3. Capital, $c = \frac{a}{(1+p)^n}$. 2. Number of years, $n = \frac{\log a - \log c}{\log (1+p)}$. 4.

In these formulas p must be expressed in a fraction of 100.

Example 1. A capital c = 8650 standing with compound interest, at p = 5 per cent. What will it amount to in n = 9 years?

Amount $a = 8650 (1.05)^9 = 13419$ dollars.

Example 2. A man commenced business with c = 300 dollars; after n = 5 years he had a = 6875 dollars. At what rate did his money increase, and how soon will he have a fortune of 50000 dollars?

The first question, or the percentage, will be answered by the formula 3.

$$p = \sqrt[5]{\frac{6875}{300}} - 1 = \sqrt[5]{22.9166} - 1 = 0.87$$
, or 87 per cent.

The time from the commencement of business until the fortune is completed will be answered from the formula 4.

$$n = \frac{log.50000 - log.300}{log.1.87} = \frac{4.69897 - 2.47712}{0.2720048} = 8.169 \text{ years},$$

or 8 years and 2 months.

Compound Interest Table, CALCULATED FROM FORMULA 1.

This table shows the value

	1			This table shows the value of one unit of			
n	COMPOUND INTEREST.			money at the rates of 5, 6 and 7 per cent. per			
Years.	5 per ct.	6 per ct.	7 per ct.	annum, compound interest, up to 60 years. Example 1. What is the amount of 864 pounds			
1	1.0500	1.0600	1.0700	stepling for 10 years at 6 per cent correspond			
2	1.1025	1.1236	1.1449	sterling for 12 years, at 6 per cent. compound interest?			
3	1.1576	1.1910	1.2250				
4	1.2155	1.2625	1.3108	Table, $2.01219 \times 864 = 1738.53216$, or £1738 $10 \text{ s. } 7.7 \text{ d.}$			
5	1.2770	1.3382	1.4025				
6	1.3400	1.4185	1.5007	Example 2. What is the amount of 3450 dollars			
7	1.4071	1.5036	1.6058	for 18 years, at 5 per cent. compound interest?			
8	1.4774	1.5938	1.7182	Table, $2.40661 \times 3450 = 8302.80$ dollars.			
9	1.5513	1.6895	1.8385	When the interest is compounded in more or			
10	1.6289	1.7908	1.9671	less than one year, at the rate of interest per			
11	1.7103	1.8983	2.1048	year, and $m =$ the number of months in which			
12	1.7958	2.0122	2.2522	the interest is compounded;			
13	1.8856	2.1329	2.4098	Then, instead of p in the formulas, put $\frac{m}{12}$,			
14	1.9799	2.2609	2.5785	and instead of n , put $\frac{12n}{n}$.			
15	2.0789	2.3965	2.7599	and instead of n, put			
16	2.1829	2.5403	2.9522	Example 3. A capital of 500 dollars bears			
17	2,2920	2.6928	3.1588	compound interest semi-annually, at 5 per cent.			
18	2,4066	2.8543	3.3799	per annum; what will it amount to in 10 years?			
19	2,5269	3.0256	3.6165	$m n 6 \times 0.05$			
20	2.6533	3.2071	3.8697	$m = 6$ months, $p = \frac{m p}{12} = \frac{6 \times 0.05}{12} = 0.025$,			
21	2.7859	3.3995	4.1406	12 12			
22	2.9252	3.6035	4.4304	and $n = \frac{12 \times 10}{6} = 20$,			
23	3.0715	3.8197	4.7405	6 .			
24	3.2251	4.0487	5.0724	then, $a = c(1+p)^n = 500(1+0.025)^{20} =$			
25	3.3864	4.2919	5.4274	8193.11 dollars, the answer.			
30	4.3219	5.7435	7.6123	log.(1 + 0.025) = 0.0107239			
35	5.5166	7.6861	10.6766	20			
40	7.0400	10.2858	14.9745				
45	8.9850	13.7646	21.0025	0.2144780			
50	11.6792	18.4190	29 4570	log. 500 = 2.6989700			
60	18.6792	32.9878	57.9466	Amount, 8193.11 = 2.9134480			

ANNUITIES.

Annuity is a certain sum of money to be paid at regular intervals.

A yearly payment or annuity b is standing for n years; to find the whole amount a, at p per cent. interest.

Amount,
$$a = b n \left[1 + \frac{p}{2}(n+1) \right]$$
 Simple Int. . . . 1.

Amount, $a = \frac{b}{p} \left[(1+p)^n - 1 \right]$ Comp. Int. 2.

A yearly payment or annuity b is to be paid for n years; to find the present worth, or the amount a, which would pay it in full at the heginning of the time n, deducting p per cent. interest.

Amount,
$$a = bn \left[1 - \frac{p}{2} \left(\frac{n+1}{1+p} n \right) \right]$$
 Simple Int. . . . 3.

Amount, $a = \frac{b}{p} \left[1 - \frac{1}{(1+p)^n} \right]$ Comp. Int. 4.

A debt D, standing for interest, is diminished yearly by a sum b; to find the debt d after n years, and the time n when it is fully paid?

The debt d after n years will be—

The time n until fully paid will be-

If b = D p, then $n = \infty$, or the debt D will never be paid. If b < D p, the debt D will be increased.

To find the yearly annuity b which will pay a debt D in n years, at p per cent. compound interest?

Annuity Table,

Showing the present worth of an annuity or rent of one unit of money, at 5, 6 and 7 per cent. compound interest for years up to 60, calculated from formula 4.

Years.	5 per ct.	6 per ct.	7 per ct.	Years.	5 per ct.	6 per ct.	7 per ct.
1	0.9524	0.9434	0.9345	17	11.2741	10.4772	9.7632
$ar{2}$	1.8594	1.8333	1.8080	18	11.6896	10.8276	10.0591
3	2,7232	2.6730	2.6243	19	12.0853	11.1581	10.3356
4.	3.5459	3.4651	3.3872	20	12.4622	11.4699	10.5940
5	4.3295	4.2123	4.1001	21	12.8211	11.7641	10.8355
6	5.0757	4.9173	4.7665	22	13.1630	12.0416	11.0612
7	5.7864	5.5824	5.3892	23	13.4881	12.3034	11.2722
8	6.4632	6.2098	5.9712	24	13.7986	12.5503	11.4693
9	7.1078	6.8017	6.5152	25	14.0939	12.7833	11.6536
10	7.7217	7.3601	7.0235	30	15.3724	13.7648	12,4 090
11	8.3064	7.8868	7.4986	35	16.3742	14.4982	12.9476
12	8.8632	8.3838	7.9426	. 40	17.1591	15.04 63	13,3317
13	9.3936	8.8527	8.3576	45	17.7741	15.4558	13.6055
14	9.8986	9.2950	8.7454	50	18.2559	15.7618	13.8007
15	10.3796	9.7122	9.1079	55	18.6334	1 5.9905	1 3.9399
16	10.8378	10.1059	9.4466	60	18,9292	16.1614	14.0389

By the Differential Calculus we ascertain the simultaneous progress By the Differential Calculus we ascertain the simultaneous progress of variable quantities depending on one another. The variable quantities are designated by the last letters u, v, x, y, z, and the constant quantities by the first, a, b, c, e, f, of the alphabet. The letter d is placed before variables to denote the instantaneous progress of that quantity, as dx, and called the differential of x. d reads differential. Let the side of a square be denoted by x and the area by z; when x increases uniformly, z will increase more rapidly. When x=1, z=1, but when x=2, z=4. When we know the instantaneous increase of x, what will be that of z? If we add, say only a point to the side x, there will be added two lines or 2x to the square. We know that $z=x^2$, the d or increment of the square will be $dz=2x\,dx$, of which dx is the point added to x and of the square will be dz = 2x dx, of which dx is the point added to x and 2x is the two lines added to the square, called the differential coefficient. Let v denote the volume of a cube, and x its side, we have $v = x^3$ and $dv = 3x^2dx$, which shows that if a point dx is added to x there will be $3x^2$

or three squares added to the cube.

The d of any power of a variable is equal to the power diminished by 1, multiplied by the primitive exponent and the product by the d of the variable. The d of a constant is = o. When the constant is a factor to the variable it appear unchanged in the d coefficient, but when a term it discapage.

it disappears.

I. The d of length u of any line defined by a formula of rectangular co-ordinates x and y, is $du = \sqrt{dx^2 + dy^2}$. II. The d of area z of any plan figure bounded by a curved line and rectangular co-ordinates is dz = y dx, y = ordinate, x = abscissa. III. The d of solidity v of any figure bounded by a plan rotating round its abscissa x, is $dv = \pi y^2 dx$, y = ordinate of the outer line of the plan. IV. The d of surface z of any solid bounded by a plan rotating round its abscissa x, is $dz = 2\pi y du$, in which u = length of the outer edge of the plan.

Successive d is when the first d coeff. is considered a function of a new function

new function.

$$u = a x^4$$
. 1st. d · coeff. $\frac{du}{dx} = 4 a x^3$, 2nd. d · coeff. $d\left(\frac{du}{dx}\right) = \frac{d^2u}{dx^2} = 12 a x^2$, 3d. d · coeff. $d\left(\frac{d^2u}{dx^2}\right) = \frac{d^3u}{dx^3} = 24 a x$, etc., etc.

 d^2u means the second, d^3u the third d^2u coefficient of u. dx^2 means the

square of the d of x, etc.

Example 1. The diameter of a sphere increases at a rate of dx = 2.31inches per second, when x = 9.5 inches, at what rate (dv = ?) does the volume v increase? $v = \frac{\pi x^3}{6} = 0.523 x^3$. $dv = 0.523 \times 3 x^2 dx = 1.569 \times 2.31$

= 327.1 cubic inches, the answer. Example 2. It is found that the displacement of a ship increases as $x^{1.5}$ the draft of water. At the load draft a=18 feet the displacement is T=2000 tons. Required the displacement (t=?) when x=12 ft. and how much (dt.?) can the vessel be loaded per dx = 1 inch or 1-12 foot, at that draft.

$$t = \frac{x^{1.5} T}{a^{1.5}} = \frac{12^{1.5} \times 2000}{18^{1.5}} = 1088.6 \text{ tons, at } x = 12 \text{ feet draft.}$$

$$dt = \frac{1.5 T}{a^{1.5}} = \frac{1.5 \times 2000 \times \sqrt{12}}{18^{1.5} \times 12 \text{ in.}} 11.34 \text{ tons per inch.}$$

The following page contains the differentials of formulas and trigonometrical functions. l means the Naperian logarithm. The common logarithm log. multiplied by 2.302585 gives the Naperian logarithm l.

FORMULAS.		DIFFERENTIALS.		FORMULAS.	1	DIFFERENTIALS	l.,
y=x		dy=dx,	1	a^x	=	$a^x l \cdot a dx$,	21
$y=ax^2$		dy = 2 a x dx	2	$d \cdot l \cdot x$	=	$\frac{dx}{x}$	22
$y=x^n$		$dy = n x^{n-1} dx$,	3	$x l \cdot x$	==	$(1+l\cdot x)dx,$	28
3 a b x*	=	$9abx^2dx,$	4	$\frac{l \cdot x}{x^n}$	=	$(\frac{1-l\cdot x)dx,}{x^{n+1}}$	24
$4 a b^2 x^n$	=	$4 n a b^2 x^{n-1} dx,$	5	$\frac{x}{l \cdot x}$	==	$\frac{(l\cdot x-1)\cdot dx}{(l\cdot x)^2}$	25
a- -x³		$3x^2dx$	6	$\frac{ay}{\sqrt{x^2+y^2}}$	==	$\frac{a y x dx - a x^2 dy}{\sqrt{(x^2 + y^2)^3}}$	26
(a- -b)x ²	300	2x(a+b)dx,	7	$\frac{a-2bx}{(a+bx)^2}$	22	$\frac{2b^2xdx}{(a+bx)^3}$	27
$6a b^4 x^3 - c$	=	$18 a b^4 x^2 dx,$	8	$\sqrt{x=x^{\frac{1}{2}}}$	==	$\frac{dx}{2\sqrt{x}}$	28
$x+3z^2-v$	==	dx+6zdz-dv	9	$(ax+x^2)^n = n($	a x-	$+x^{2}$) ⁿ⁻¹ (a+2x)dx	29
$6x^3 + 4a^{x^2} - 3x$	<u>—</u> (1	$18x^2 + 8ax - 3)dx$	10	$\sqrt{a^2+bx^2}$	===	$\frac{b x d x}{\sqrt{a^2 + b x^2}}$	30
$x v^2$	4	v dx + 2 x v dv	11	$d^{\cdot 2}(a x^3)$	==	6 a x dx*,	31
xvz =	= <i>x</i>	$v z \left(\frac{dx}{x} + \frac{dv}{v} + \frac{dz}{z} \right)$	12	$d^3(a x^3)$	==	$6 a dx^3$,	32
$x(x^2-xb^2)$	=	$(3 x^2 - b^2 x) dx,$	13	$d^4(a x^3)$	==	$obax^{\circ-1}dx^{4}=o,$	33
$\frac{x^9}{v}$	=	$\frac{2 x v dx - x^2 dv}{v^2},$	14	$\sin.v$	==-	$+\cos v dv$,	34
$\frac{a}{x}$	=	$\frac{adx}{x^2}$	15	cas. v	==	$-\sin v dv$	35
$\frac{a}{x^n}$	=	$\frac{n a x^{n-1} dx}{x^{2n}}$	16	tan. v	=	$+\frac{dv}{\cos^2 v}$	36
$(a+\sqrt{x})^3$	=	$\frac{3(a+\sqrt{x})^2dx}{2\sqrt{x}}$	17	cot. v	=	$-\frac{dv}{\sin^2 v}$	37
$(a+\sqrt[n]{x})^m =$	m (e	$(x+\sqrt[n]{x})^{n-1}\frac{1}{n}x^{n-1}$	l lx.	sec. v	-	$+ \frac{\cos v dv}{\cos^2 v}$	38
$\frac{1}{4(a-x)}$	-	$\frac{dx}{(a-x)^{n+1}}$	19			$-\frac{\cos vdv}{\sin^2 v}.$	39
$\frac{2\sqrt{2a}x-x^2}{x}$	==	$\frac{2 a dx}{x \sqrt{2 ax - x^2}}$	20	Tant. for any	cur	$ve t = y \sqrt{1 + \frac{dx^2}{dy^2}}$	40

The Integral Calculus is the reverse of the Differential, or to find the original formula of a given differential. The symbol f is placed before the d to denote that the integral is to be taken out of it, or that the original formula is to be found.

The d of $a x^3 = 3 a x^2 dx$, and $\int 3 a x^3 dx = \frac{3 a x^2 + 1}{3} = a x^3$.

Rule to find the integral. Add 1 to the exponent of the variable x in the d, divide the d by the new exponent, dx will disappear, and the quotient is the integral. The integral f does not effect a constant. A constant term in a formula disappears in its de, consequently any integral may have a constant term, whose value is determined by making the variable in the integral = o, when the first member in the formula will be a constant. It is therefore customary to add a constant C to the integral. When it is known that the first member is = o at the same time the variable in the f is = o, then C = o. When a differential is to be integrated between two limits of the invariable, say x = a and x = b, it is indicated by \int_{a}^{b} or $\int_{a}^{b} 3 c x^{2} dx = c(b^{3}-a^{6})$.

Successive differentials are accompanied with the same order of inte-

grals, as $ff = 6x dx^2 = f = 3x^2 dx = x^3$.

The integrals of the differentials gives the formula for the problem.

Example 3. It is required to find by the calculus a formula for the area z of a rightangled triangle. Proposition II, page 78. dz = y dx, the formula for the hypothenuse is y = ax, dz = ax dx, $z = \int ax dx = \frac{ax^2}{2} \frac{yx}{2}$ or the area z is half the rectangle of the sides x and y.

Example 4. Find a formula for the convex surface z of a cone, whose side is \hat{u} , and r = radius of the base? Prop. IV, page 78. $dz = 2 \pi r du$, and $z = \int 2 \pi r du = \pi r u$, the answer.

Example 5. Find a formula for the area z of a circle, when it is known that the circumference $y = 2\pi x$? Prop. II, page 78. $dz = y dx = 2\pi x dx$,

and $z = \int 2 \pi x \, dx = \pi x^2$ the answer, x = radius of the circle.

Example 6. Find a formula for the area z of a parabola of x = abscissa or height, and y = ordinate, or half the base? Formula for a parabola $y = \sqrt{p \ x}$, in which p = the constant parametric diameter, or $p = \frac{y^2}{x}$. $x = \frac{y^2}{p}$, $dx = \frac{2y}{p} \frac{dy}{p}$. Prop. II, $dz = y dx = \frac{2y^2 dy}{p}$ and $z = \int \frac{2y^2 dy}{p} = \frac{2y^2}{3p} = \frac{2y^2}{3p}$

 $\frac{2 \times y}{3}$, the answer, or the area of a parabola is % of the base by the height. Example 7. Find a formula for the volume v of a paraboloid? Prop. III. $dv = \pi y^3 dx = \frac{2 \pi y^3 dy}{p}$, and $v = \int \frac{2 \pi y^3 dy}{p} = \frac{\pi y^4}{2p}$, but $p = \frac{y^2}{x}$ and $v = \int \frac{2 \pi y^3 dy}{p} = \frac{\pi y^4}{2p}$.

 $\frac{\pi}{2}y^2x$, the answer.

V. The center of gravity s from the origin of x, of any plan figure bounded by a curved line and rectangular co-ordinates is $s = \frac{\int x y \, dx}{\sqrt{1 + (1 + x)^2 + (1 + x)^2}}$ when z area of the plan.

VI. The center of gravity s from the origin of x of any solid figure is $s = \frac{\int xz \, dx}{v}$, when z = ordinate cross section and v volume of the same.

Example 8. Find a formula for the centre of gravity (s = ?) of a cone. The ordinate cross-section $z = \pi y^2$, and $v = \frac{\pi}{3} y^2 x$, when x = height andy radius of the base of the cone. Prop. VI. $s = \frac{\int x z \, dx}{v} = \frac{3 \int \pi x \, y^3 \, dx}{\pi y^2 \, x}$ As the center of gravity is not influenced by the proportion of x and y, we can make y = x, when $s = \frac{3 f \pi x^3 dx}{\pi x^3} = \frac{3 \pi x^4}{4 \pi x^3} = \frac{3}{4} x$, from the top.

DIFFERENTIALS. $\int x \, dx = \frac{x^2}{2} + C$, 1 $\int 4 \, a \, x^3 \, dx = 4 \, a \, \int x^3 \, dx = a \, x^4 + C,$ $\int x^n dx, \qquad = \qquad \frac{x^{n+1}}{n+1} + C,$ $f\sqrt{x}\,dx fx^{\frac{1}{2}}dx = \frac{2x^{\frac{1}{2}}}{3} + C,$ $\int \frac{dx}{\sqrt{x}} = \int x^{-1/2} dx = 2\sqrt{x} + C,$ $\int \frac{dx}{x} = \int \bar{x}^1 dx = l \cdot x + C, \qquad 6$ $\int \frac{dx}{x^2} = \int x^{-2} dx = -\frac{1}{x} + C, \qquad 7$ $\int \frac{dx}{x^3} = \int x^3 dx = -\frac{1}{2x^2} + C, \quad 8$ $\int \left(a x^{3} + \frac{b}{2\sqrt{x}} \right) dx = \frac{a x^{4}}{4} + b\sqrt{x} + C, 9$ $\int \frac{a \, dx}{x} = a \, l \cdot x + C,$ $\int axdx + 3x^2dx - b^2dx = \frac{ax^2}{2} + x^3 - b^2x + C, \quad \int f \sin x \cos x \, dx = \frac{1}{2} \sin^2 x + C, \quad 33$ $f(a^2+b^2) dx = x(a^2+b^2)+C, \quad 14 \left| \int \frac{\sin b x}{x} dx \right| =$ $\int (ax-2x^2)^2 dx = x^3 \left(\frac{a^2}{3}-ax+\frac{4x^2}{5}\right) + C, \int \frac{\cos bx}{x} dx =$ $\int 3(ax-x^2)^2(a-2x)dx = (ax-x^2)^3 + C$, $\int \frac{dt}{1+t^2} = \text{circle arc of which } t = t \text{ant.}$ $\int_{a^2 - x^2}^{2a \, dx} = l \cdot \frac{a + x}{a - x} + C, \quad 18$ $\int \sqrt{a^2 + x^2} \, dx = \frac{x}{2} \sqrt{a^2 + x^2} + \frac{a^2}{2} l \cdot (x + \frac{1}{\sqrt{a^2 + x^2}}), \qquad (a+b) \, dx^2 = (a+b) x^2 + c, \quad 39$ $f\sqrt{a+bx}dx = \frac{2}{3}b(\sqrt{a+bx})^3 + C$, 20 $\int f\sqrt{2}v^2 dx^2 + 8vx dx dv + 2x^2 dv^2 = xv^2$, 40

DIFFERENTIALS. $\int \frac{dx}{\sqrt{a^2+x^2}} = l(x+\sqrt{a^2+x^2}),$ $\int_{0}^{b} 3 \, m \, x^{2} \, dx = m \, b^{3} - m \, a^{2},$ 22 $\int_{a}^{b} m \, x \, dx = \frac{m}{2} (b^2 - a^2),$ 23 $\int_{0}^{\infty} \frac{dx}{a^2 + x^2} = \frac{\pi}{2 a'}$ 24 $\int_{\sqrt{a^2-x^2}}^{a} = \frac{\pi}{2},$ 25 $\int_{a}^{b} = -\int_{b}^{a} \qquad \int_{a}^{c} = \int_{a}^{b} + \int_{c}^{c}$ 26 27 $f\cos x dx = \sin x + C$ 28 $f \tan x \, dx = -l \cos x + C,$ 29 $f \cot x \, dx = -l \sin x + C$ 30 $\int \frac{b \, dx}{a+x} = b \, l \cdot (a+x) + C, \quad 11 \quad \int \frac{dx}{\sin x} = l \cdot \tan \frac{x}{2} + C, \quad 31$ $\int \frac{3 a x^{2} dx}{b + a x^{3}} = l \cdot (b + a x^{3}) + C, \quad 12 \quad \int \frac{dx}{\cos x} = l \cdot \tan \left(\frac{\pi}{4} + \frac{x}{2}\right) + C, \quad 32$ $\int \frac{n(x^{n-1}dx)}{\sqrt{a+x^n}} = \sqrt{a^2+x^n}+C, \quad 17 \left| \int \frac{dx}{\sqrt{2x-x^2}} = \text{ circle arc of which } x = \sin x \text{ ersus. 37} \right|$ $\iiint 6adx^3 = \iint 6axdx^2 = \iint 3ax^2dx = ax^3 + C$

Two variable quantities x and y depended on one another, to find the value of one, when the other is a maxima or minima.

$$\begin{cases} x \\ \text{is a maxima or minima when its} \\ y \end{cases} \begin{cases} \frac{dx}{dy} = o. \\ \frac{dy}{dx} = o. \end{cases}$$

When the second d coef. $\frac{d^2y}{dx^2}$ is positive, y is a minimum, and when negative y is a maximum. The variables may have both maximums and minimums, as formulas will indicate.

Example 1. Find the value of x when y is a maximum or minimum, in the formula $y = x^3 - 12x + 22$? $dy = (3x^2 - 12) dx$, $\frac{dy}{dx} = 3x^2 - 12 = 0$.

Of which $x = \sqrt{\frac{12}{3}} = 2$ the answer. $\frac{d^2y}{dx^2} = 6x$, which is positive, consequently $y=2^3-12\times 2+22=6$, a minimum, when x=2.

Example 2. It is required to cut out the strongest possible beam of height h and breadth b, from a log of diameter D, fig. 221 page 174? The

strength of a beam is in proportion to bh^2 which is to be a maximum. $D^2 = b^2 + h^2, \quad h^2 = D^2 - b^2, \quad b h^3 = b (D^2 - h^2), \quad d(bh^3) = (D^2 - 3b^2) db.$ $\frac{d(bh^2)}{db} = D^2 - 3b^2 = 0$, of which the breadth $b = D\sqrt{\frac{1}{3}} = 0.577$ D, and height $h = \sqrt{D^2 - \frac{1}{3}} = D\sqrt{0.6666} = 0.8164$ D, the answer. The second d coef. $\frac{d^2(b\,h^2)}{d\,b^2} = -6\,b$, which is negative, and therefore $b\,h^2$ is a maximum when b = 0.577 D.

Example 3. It is required to know the proportion of heighth h and diameter D of a cylinder, having the greatest cubic containt v, with the smallest surface z including top and bottom? $z = \frac{\pi D^2}{2} + \pi D h = \frac{2v}{h} + \pi D h$, which is to be a minimum. Set v=1 and D=1, then $z=\frac{z}{h}+\pi h$, and $dz = \left(\pi - \frac{4}{h^2}\right)dh$, $\frac{dz}{dh} = \pi - \frac{4}{h^2} = 0$, when $h = \sqrt{\frac{4}{\pi}} = 1.1284D$, the answer. The second $d \cdot \operatorname{coef.} \frac{d^2z}{dh^2} = +\frac{4\times 2}{h^4}$ which is positive, and z a minimum when

h = 1.1284 D.

Maclaurin's Theorem.

Maclaurin's Theorem, explains how to develop into a series a function

with one variable, as
$$u = (u) + \frac{x}{1} \left(\frac{du}{dx}\right) + \frac{x^2}{2} \left(\frac{d^2u}{dx^2}\right) + \frac{x^3}{2 \times 3} \left(\frac{d^3u}{dx^3}\right) \dots + \frac{x^n}{2 \times 3 \times \dots n} \left(\frac{d^nu}{dx^n}\right) \text{ etc.}$$

where the factors in the parenthesis is that which it assumes when x=0.

The function $u = \frac{1}{a+x}$ developed into a series will be $\frac{1}{a+x} = \frac{1}{a} - \frac{x}{a^3} + \frac{x^3}{a^3} - \frac{x^3}{a^4} \cdot ... \frac{x^n}{a^{n+1}} \cdot \text{etc.}$

$$\frac{1}{a+x} = \frac{1}{a} - \frac{x}{a^2} + \frac{x^3}{a^3} - \frac{x^3}{a^4} - \frac{x^n}{a^{n+1}} \cdot \text{etc.}$$

Taylor's Theorem.

Taylor's Theorem, explains how to develop into a series a function of

the sum or difference of two variable as $u = x \pm y$. $\mathbf{F}(x \pm y) = u \pm \frac{du}{dx}y + \frac{d^2u}{dx^2} \cdot \frac{y^2}{2} \pm \frac{d^3u}{dx^3} \cdot \frac{y^3}{2 \times 3} + \dots \frac{d^2u}{dx^2} \cdot \frac{y^4}{2 \times 3} \dots \times \mathbf{n}$ where u represents the value of the function when $y = \mathbf{o}$.

Interpolation is to insert numerical values between given data, for constructing tables or empirical formulas expressing the probable relative variation of quantities. Let x and y be two variable quantities depending on one another and measured in simultaneous stages of their progress, as

We have
$$y = Ay_1 + By_2 + Cy_3 + Dy_4 + Ey_5 + &c. - - 1$$

$$A = \frac{(x - x_2) (x - x_3) (x - x_4) (x - x_5)}{(x_1 - x_2) (x_1 - x_3) (x_1 - x_4) (x_1 - x_5)}$$

$$B = \frac{(x - x_1) (x - x_3) (x - x_4) (x - x_5)}{(x_2 - x_1) (x_2 - x_3) (x_2 - x_4) (x_2 - x_5)}$$

$$C = \frac{(x - x_1) (x - x_2) (x - x_4) (x - x_5)}{(x_3 - x_1) (x_3 - x_2) (x_3 - x_4) (x_3 - x_5)}$$

$$D = \frac{(x - x_1) (x - x_2) (x - x_3) (x - x_6)}{(x_4 - x_1) (x_4 - x_2) (x_4 - x_3) (x_4 - x_5)}$$

$$E = \frac{(x - x_1) (x - x_2) (x - x_3) (x - x_4)}{(x_5 - x_1) (x_5 - x_2) (x_5 - x_3) (x_5 - x_4)}$$

The values of the coefficients A, B, C, D, and E, with their given—data, inserted in formula 1 gives an empirical formula for the variation of x and y. The number of observations or given—data of x and y should be one more than the order of progression. In arithmetical progression two observations are sufficient for a correct formula. For all curves in the conic sections, or others which are of the second order, there should be at least three observations. Pressure of steam progresses with the temperature in the 6th order, for which requires seven observations to make a correct formula. When the order of progression is not known, the more observations gives the most correct result.

Example. Let y represent the boiling-point of salt water and x the percentage of salt in solution. It is found in three experiments,

that
$$x_1 = 3$$
, $x_2 = 18$, $x_3 = 36$ per cent. salt. when $y_1 = 213 \cdot 2$ $y_2 = 219^\circ$, $y_3 = 226^\circ$ beginng-point.

Find a formula that will give any intermediate value of x and y?

$$A = \frac{(x-18)(x-36)}{(3-18)(3-36)}, \quad B = \frac{(x-3)(x-36)}{(18-3)(18-36)}, \quad C = \frac{(x-3)(x-18)}{(36-3)(36-18)},$$
$$y = 213 \cdot 2 A + 219 B + 226 C, \quad y = 0 \cdot 4x + 212$$

UNITED STATES' STANDARD MEASURES AND WEIGHTS.

MEASURE OF LENGTH.

The Standard Measure of Length is a brass rod = 1 yard at the temperature of 32° Fahrenheit. The length of a pendulum vibrating seconds in vacuo, at Philadelphia is 1.08614 yards, at + 32° Fahrenheit.

The Surveying Chain is = 22 yards = 66 feet. It consists of 100 links, and each link = 7.92 inches.

ROPES AND CABLES.

1 Cable length = 120 fathoms = 720 feet.

1 fathom = 6 feet.

GEOGRAPHICAL AND NAUTICAL MEASURES.

1 Degree of the great circle of the Earth round the Equator = 69.032 statute miles = 60 Nautical miles.

1 Statute mile = 5280 feet = 0.86875 Nautical miles.

1 Nautical mile = 6037.424 = 1.150 Statute miles.

LOG LINE.

The **Log Line** should be about 150 fathoms long, and 10 fathoms from the Log to the first knot on the line. If half a minute glass is used, it will be 51 feet between each succeeding knot. For 28 seconds glass it will be 47.6 feet = 7.93 fathoms per knot. This is the length of knot by calculation, but practically it is shortened to 7.5 fathoms per knot for 28 seconds glass.

MEASURE OF CAPACITY.

Gallon. The standard Gallon measures 231 cubic inches, and contains 8.3388822 pounds Avoirdupois = 58372.1757 grains Troy, of distilled water, at its maximum density 39.83° Fahrenheit, and 30 inches barometer height.

Bushel. The standard Bushel measures $2150 \cdot 42$ cubic inches = $77 \cdot 627413$ pounds Avoirdupois of distilled water at $39 \cdot 83^{\circ}$ Fahrenheit, barometer 30 inches. Its dimensions are $18\frac{1}{2}$ inches inside diameter, $19\frac{1}{2}$ inches outside, and 8 inches deep; and when heaped, the cone must not be less than 6 inches high, equal $2747 \cdot 70$ cubic inches for a true cone.

Pound. The standard Pound Avoirdupois is the weight of 27.7015 cubic inches of distilled water, at 39.83° Fahrenheit, barometer 30 inches, and weighed in the air.

MEASURE OF LENGTH.

Miles.	Furlongs.	Chains.	Rods.	Yards.	Feet.	Inches.
1	8	80	320	1760	5280	63360
0.125	1,	10	40	220	660	7920
0.0125	0.1	1	4	22	66	792
0.003125	0.025	0.25	1	5.5	16.5	198
0.00056818	0.0045454	0.045454	0.181818	1	3	36
0.00018939	0.00151515	0.01515151	0.0606060	0.33333	1 1	12
0 000015783		0.001262626	0.00505050	0.0277777	0.083333	1

MEASURE OF SURFACE.

Sq. Miles.	Acres	S.Chains.	Sq. Rods.	Sq. Yards.	Sq. Feet.	Sq. Inches.
0.000000323	0·0002066 0·00002296	0.0002296		3097600 4840 484 30·25 1 0·1111111 20·0007716	27878400 43560 4356 272:25 9 1 0:006944	4014489600 6272640 627264 39204 1296 144

MEASURE OF CAPACITY.

Cub. Yard.	Bushel.	Cub. Feet.	Pecks.	Gallons.	Cub. inch.				
1	21.6962	27	100.987	201.974	46656				
0.03961	1	1.24445	4	9.30918	2150.42				
0.037037	0.803564	1	3.21425	7.4805	1728				
0.009259	0.25	0.31114	1	2:32729	537.605				
	0.107421	0.133681	0.429684	1	231				
		0.000547	0.001860	0.004329	1				
		4							

MEASURE OF LIQUIDS.

Gallon.	Quarts.	Pints.	Gills.	Cub. inch.
1	4	8	32	231
0.25	1	2	8	57.75
0.125	0.5	1	4	28.875
0.03125	0.125	0.25	1	7.21875
0.004329	0.017315	0.03463	0.13858	1

MEASURES OF WEIGHTS.

AVOIRDUPOIS.

Ton.	Cwt.	Pounds.	Ounces.	Drams.
1	20	2240	35840	57344 0
0.05	1	. 112	1792	28672
0.00044642	0.0089285	1 .	16	256
0.00002790	0.000558	0.0625	1	16
0.00000174	0.0000348	0.0016	0.0625	1

TROY.

Pounds.	Ounces.	Dwt.	Grains.	Pound Avoir.
1	12	240	5760	0.822861
0.083333	1	20	480	0.068571
0.004166	0.05000	1	24	0.0034285
0.0001736	0.002083333	0.0416666	1	0.00014285
1.215275	14.58333	291.6666	7000	1

APOTHECARIES.

Pounds.	Ounces.	Drams.	Scruples.	Grains.
• 1	12	96	288	5760
0.08333	1	8	24	480
0.01041666	0.125	1	3	60
0.0034722	0.0416666	0.3333	1	20
0.00017361	0.0020833	0.016666	0.02	1

MONEY AND COINS OF THE UNITED STATES.

10 mills = 1 cent. 10 cents = 1 dimes = 1 dollar. 10 dollars = 1 eagle.

The standard gold and silver coins contain 900 parts of pure metal and 100 parts of base metal in 1000 parts of the alloy.

The remedy of the Mint is the allowance for deviation from the exact standard fineness and weight of coins.

The nickel cent contains 88 parts of copper and 12 of nickel.

The new bronze cent contains 95 parts of copper and 5 of tin and zinc.

Pure gold, 23.22 grains = \$1, or \$20.67.183 = 1 ounce. Pure silver, 357.03 grains = \$1, or \$1.36.166 = 1 ounce.

Silver coins of less value than one dollar are issued at the rate of 384 grains to the dollar.

Standard alloyed gold = \$18.60.465, and silver = \$1.22.5 per ounce.

Gold coins.	Grains.	Silver coins.	Grains.	Copper coins.	Grains.
Double eagle, .	. 516.	One dollar, .	. 412.5	Cent (old), .	. 168.
Eagle,	. 258.			Cent (new),	. 72.
Dollar,	. 25.8	Twenty-five cen	its, 96.	Cent (bronze),	. 48.
For silver and	aldet blon	000 paner aez			

WEIGHT AND FINENESS OF DIFFERENT COINS, AND THEIR VALUE IN AMERICAN MONEY.

			Fineness	Fine	UNITED
Country.	Piece and Divisions.	Weight.	in 1000.	metal.	STATES.
Country.	1 tees with Divisions.	Grains.	111 1000.	Grains.	\$ Cts.
	Crown,	171.36	900.	154.22	6.64.19
Austria,	Florins,	190.56	900.	171.5	0.48.63
Baden,	Ducat.	47.5	987.	46.9	2.00.70
Belgium, .	Ducat,	121.92	899.	109.6	4.72.03
Brazil,	2000 Reis,	393.6	918.5	361.5	1.02.53
Canada,	2000 Reis, 20 Cents, 1851,	96.0	925.	88.8	0.18.87
China,	Tael,				1.43.00
The state of the s	Tael, ∫ 10 Pesos, 1855,	236.16	900.	212.5	9.15.35
Chili,	1 Peso, 1854-6,	384.48	900.5	346.2	0.98.17
Denmark,	2 Rix dollars,	444.96	877.	390.2	1.10.65
England, .	Pound sterling $= 20 \text{ shillings},$	123.21	916.5	112.9	4.86.34
East Indies,	Company's Rupee,	180.	892.	16.5	5.10.49
France,	Napoleon, 20 Francs,	99.5	898.	87.4	3.85.00
Greece, .	20 Drachins,	88.8	900.	80.9	3.44.29
Hamburg, .	RIX Dollar,	450.	860.	397.5	1.17.66
Holland, .	{Ducat,	53.75	982.	52.77	2.29.7
	(Florin,	50.	787.	39.32	1.69.30
Italy,	20 Lire,	99.36	898.	89.22	3.84.26
Mexico, .	S Doubloon = 8 Escudos, .	416.4	870.5	362.5	15.61.05
	Peso = 8 Reals,	415.68	901.	374.5	1.06.20
Norway,	2 Rigsdaler,	444.96	877.	390.2	1.10.65
Peru,	1 Sol = 100 Centavos,	$385.82 \\ 147.84$	900. 912.	347.24 134.8	0.95.41
Portugal, .	Corona (Crown), 1838, .	45.6	912.	41.6	5.80.66
Prussia, .	1000 Reis,	268.46	912.	243.6	$1.18.00 \\ 0.72.89$
Rome,	Thaler, 2.5 Scudi = 250 Bajochi,	67.2	900.	60.5	2.60.47
,	(Imperial = 5 Roubles,	100.8	916.	92.3	3.97.64
Russia, .	Rouble silver = 100 Copecks,	320.16	875.	286.8	0.79.44
~ .	100 Reals,	128.64	896.	115.2	4.96.39
Spain,	80 Reals = 4 Dollars,	103.2	869.5	89.73	3.86.44
a 1	Ducat	53.	979.	51.9	2.23.50
Sweden, .	Sucat, Rix Dollar = 100 Ore,	112.3	873.	97.15	0.26.10
Turkey,	Piastres, 1845,	110.88	900.	99.79	4.36.93
	, , , , , , , , , , , , , , , , , , , ,		7		

THE CURRENCY OF DIFFERENT COUNTRIES COMPARED WITH ENGLISH AND AMERICAN MONEY.

En	gl'ı	nd.		ice. gi'm.	P	russi	a.		stria.	Sweden.		er- ny.		ssia.		am-	U. S.
£ 0	s. 0 0	d. 1 2	Frs.	Cts. $10\frac{1}{2}$	Th. 0	Sgr.	10	F1.	Kr. 5	Rix. Ore. 0.07	F1.	3	0	Kop.	Mrk 0	Sch.	\$ Cts. 0.02
0 0 0	0	3 4	0 0	21 32 42	0 0	$\frac{1}{2}$	8 6 4	0 0	$ \begin{array}{c} 10 \\ 16 \\ 21\frac{1}{2} \end{array} $	$0.14 \\ 0.21 \\ 0.28$	0 0	6 9 12	0 0	5 8 12	0 0	$\frac{2}{2\frac{3}{4}}$ $2\frac{1}{2}$	0.04 0.06 0.08
0	0	5	0	53	0	4	2	0	27	0.36	0	15	0	16	0	41	0.10
0	0	6	0 0	64 74	0	5 5	1 11	0	31 36‡	$0.44 \\ 0.51$	0	18 21	0	19 22	0	$\frac{5\frac{1}{4}}{6\frac{1}{4}}$	0.12
0	0	8	0	85 96	0	6 7	10	0	$42\frac{1}{2}$ $47\frac{1}{2}$	0.59 0.66	0	24 27	0	26 27	0	7 · 8	0.16 0.18
0	0	10	_1	6	0	8	6	0	53	0.73	0	30	0	33	0	83	0.18
0	0	11	1 1	16 27	0	9 10	5 3	0	$57\frac{1}{2}$ 62	0.80 0.89	0	3 1 36	0	36 39	0	9 <u>₹</u> 11	$0.22 \\ 0.24$
0	1 2 3	0	$\frac{1}{2}$	55 82	0	20	6 9	1 1	25	1.78	1	13	0	79	1	6	0.48
0	4	0	5	10	1	10	11	$\frac{1}{2}$	87 50	2.67 3.56	$\begin{bmatrix} 1 \\ 2 \end{bmatrix}$	49 24	1 1	18 58	$\frac{2}{2}$	$\frac{1}{12}$	0.72 0.96
0	5 6	0	6 7	36 64	1 2	$\frac{21}{1}$	3 6	3	$\frac{12}{74}$	4.45 5.34	$\frac{2}{3}$	59 38	$\frac{1}{2}$	97 37	3 4	$\frac{7}{2}$	1.21 1.45
0	7 8	0	8	92	2	11	9	4	36	6.23	4	12	2	77	4	12	1.69
0	9	0	10 11	20 46	3	22 2	0	4 5	95 58	7.12 8.09	4 5	$\frac{47}{22}$	3 3	18 58	5 6	$\frac{7}{2\frac{1}{2}}$	1.93 2.18
0	10 11	0	12 13	72 99	3	12 22	4	6	25 87	8.90 9.79	5 6	58 34	3 4	94 38	6 7	$13\frac{1}{2}$ $8\frac{1}{2}$	2.42 2.66
0	12	0	15	27	4	2	9	7	49	10.68	7	11	4	75	8	$3\frac{1}{2}$	2.90
0	13 14	0	16 17	55 84	4 4	13 23	$\begin{array}{c} 0 \\ 3 \end{array}$	8 8	12 75	11.57 12.66	7 8	$\frac{46}{24}$	5 5	15 55	8 9	$\frac{14\frac{1}{2}}{9\frac{1}{2}}$	3.14 3.39
0	15 16	0	19 20	8 40	5 5	3 13	5 8	9	37 0	13.45 14.2 4	8 9	57 33	5 6	96 35	10 10	$\frac{4\frac{1}{2}}{15\frac{1}{2}}$	3.63
0	17	0	21	66	5	23	11	10	65	15.13	10	9	6	74	11	$10^{\frac{1}{2}}$	3.87 3.12
	18 19	0	$\begin{array}{c} 22 \\ 24 \end{array}$	92 18	6	4 14	$\frac{2}{4}$	11 11	28 88	16.02 17.01	10 11	46 21	7 7	14 44	12 13	$\frac{5\frac{1}{2}}{0\frac{1}{2}}$	4.36 4.60
$\frac{1}{2}$	0	0	25 50	45 90	6	24 19	6	12 25	50	17.80 35.60	11 23	57 54	7 15	88 77	13 27	9	4.84
3	0	0	76	35	20	13	0 6	37	0 50	53.40	35	51	23	65	40	11	$9.68 \\ 14.52$
4 5	0	0	$101 \\ 127$	80 25	27 34	8 3	0	50 62	0 50	71.20 89.00	47 59	48 46	31 39	54 42	54 67	4 11	17.36 24.20
6	0	0	$\overline{152}$	70	40	27	6	75	0	106.80	71	42	47	31	81	4	29.04
7 8	0	0	178 202	15 60	47 54	22 16	6 6	87 100	50	124.60 142.40	83 95	39 36	55 63	20 9	94 108	13 6	33.88 38.72
9	0	0	229 254	5 50	61 68	11 6	6	$\begin{array}{c} 112 \\ 125 \end{array}$	50	160.20 178.00	107 119	34 30	70 78	96 84	121 135	15 8	43.56 48.40
_			1 -0 -							270.00							10110

The mark of Finland is equal to the French franc.

DIAMOND.

Carat.	Grain.	Parts.	Grains (Troy).			
1.	4.	64	3.2			
0.25	1.	16	ე.8			
0.015625	0.0625	1	0 05			
0.3125	12.5	20	1.			

Convention	o.f	Tmobos	and	Tichthe	into	Decimals	of	Q	Foot
Conversion	01	Inches	SCHACE	Eligitudis	11110	Decimals	OT	at	T. OOF.

Inches. 0 $\frac{1}{8}$ $\frac{1}{4}$ $\frac{3}{8}$ $\frac{1}{2}$ $\frac{5}{8}$ $\frac{3}{4}$	7 8
Inches. $0 \frac{1}{8} \frac{1}{4} \frac{3}{8} \frac{1}{2} \frac{5}{8} \frac{3}{4}$	8
	1
0 .0000 .01041 .02083 .03125 .04166 .05208 .0625	.07291
1 .08333 .09375 .10416 .11458 .125 .13541 .14588	.15639
2 .16666 .17707 .1875 .19792 .20832 .21873 .22914	.23965
3 .25 .26041 .270 .28125 .29166 .30208 .3125	.32291
4 .33333 .34375 .35416 .364 .375 .38541 .39588	.40639
5 .41666 .42707 .437 .44792 .45832 .46873 .47914	.48965
6 .5 .51041 .520 .53125 .54166 .55208 .5625	.57291
7 .58333 .59375 .60416 .614 .625 .63541 .64588	.65639
8 .66666 .67707 .685 .69792 .70832 .71773 .72914	.73965
9 .75 .76041 .770 .78125 .79169 .80208 .8425	.82291
10 .83333 .84375 .85416 .864 .875 .88541 .89588	.90639
11 .91666 .92707 .937 .94792 .95832 .96873 .97914	.98965
12 1 foot. foot. foot. foot. foot. foot.	foot.

 $\frac{1}{16}$ in. = 0.005208 ft.; $\frac{1}{32}$ in. = 0.00265 ft.; $\frac{1}{64}$ in. = 0.001375 ft.

Angle Measurement by the Opening of a Two-foot Rule.

0pening			Fr	FRACTIONS OF AN INCH.							
Rule.	0	1/8	1/4	3/8	$\frac{1}{2}$	5 8	$\frac{3}{4}$	7 8			
Inch's.	0 /	0 '	0 /	0 /	0 /	0 1	0 /	0 /			
0	00 00	0 36	1 12	1 47	2 23	2 59	3 35	4 11			
1	4 46	5 22	5 59	6 34	7 10	7 46	8 22	8 58			
2	9 34	10 10	10 46	11 22	11 58	12 34	13 10	13 46			
3	14 22	14 58	15 34	16 10	16 46	17 22	17 59	18 35			
4	19 12	19 48	20 24	21 0	21 37	22 13	22 50	23 27			
5	24 3	24 39	25 16	25 53	26 30	27 7	27 44	28 21			
6	28 58	29 35	30 12	30 49	31 26	32 3	32 40	33 17			
7	33 54	34 33	35 8	35 46	36 25	37 3	37 40	38 18			
8	38 56	39 34	40 12	40 50	41 29	42 7	42 46	43 24			
9	44 4	44 42	45 21	45 59	46 38	47 17	47 56	48 35			
10	49 15	49 54	50 34	51 13	51 53	52 33	53 13	53 53			
11	54 34	55 14	55 55	56 35	57 16	57 57	58 38	59 19			
12	60 0	60 41	61 23	62 5	62 47	63 28	64 10	64 52			
13	65 35	66 18	67 1	67 44	68 28	69 12	69 55	70 38			
14	71 20	72 6	72 51	73 35	74 21	75 6	75 51	76 36			
15	77 20	78 8	78 54	79 40	80.27	81 14	82 1	82 49			
16	83 38	84 26	85 14	86 3	86 52	87 41	88 31	89 21			
17	90 12	91 3	91 55	92 41	93 39	94 31	95 34	96 17			
18	97 11	98 5	99 0	99 55	100 51	101 47	102 44	103 42			
19	104 40	105 39	105 39	107 40	108 41	109 43	110 46	111 49			
20	112 53	113 58	115 4	116 11	117 20	118 30	119 41	120 53			
	a			70.7							

Conversion of Vulgar Fractions into Decimals.

•								
l		Decimals.			Fract'ns.	Decimals.	Fract'ns.	Decimals.
ı	1:2	.5	1:16	.0625	1:32	.03125	1:64	.015625
ı	1:3	.33333	3:16	.1875	3:32	.09375	3:64	.046875
ı	2:3	.66666	5:16	.3125	5:32	.15625	5:64	.078125
ı	1:4	.25	7:16	.4375	7:32	.21875	7:64	.109375
ı	3:4	.75	9:16	.5625	9:32	.28125	9:64	.140625
1	1:5	.2	11:16	.6875	11:32	.34375	11:64	.171875
ı	3:5	.6	13:16	.8125	13:32	.40625	15:64	.234375
Į	1:6	.16666	15:16	.9375	15:32	.46875	19:64	.296875
ł	5:6	.83333	1:24	.04166	17:32	.53125	23:64	.359375
1	1:8	.125	5:24	.20833	19:32	.59375	27:64	.421875
1	3:8	.375	7:24	.29166	21:32	.65625	31:64	.484375
١	5:8	.625	11:24	.45833	23:32	.71875	35:64	.546875
ı	7:8	.875	13:24	.54166	25:32	.78125	39:64	.609375
ı	5:12	.41666	17:24	.70833	27:32	.84375	43:64	.671875
ı	7:12	.58333	19:24	.79166	39:32	.98625	57:64	.891625
ı	11:12	.925	23:24	.95833	31:32	.96875	61:64	.953125

To Determine an Angle by the Aid of a Two-foot Rule.

b = opening of the rule in inches; v = angle formed by the rule; Sin. $\frac{1}{2}v = \frac{b}{24}$; and $b = 24 \sin \frac{1}{2}v$.

Example 1. How much (b=?) must a two-foot rule be opened to form an angle of 48° 40'?

 $b = 24 + \sin 24^{\circ} 20' = 24 \times 0.412 = 9.888$ inches.

Example 2. A two-foot rule is opened to b = 8 inches. Required the angle formed by the rule.

Sin. $\frac{1}{2}v = \frac{8}{21} = 0.3333 = \sin 19^{\circ} 30^{\circ}$, and $v = 39^{\circ}$.

THE FRENCH METRICAL SYSTEM.

The French units of weight, measure and coin are arranged into a perfect decimal system, except those of time and the circle. The division and multiplication of the units are expressed by Latin and Greek names, as follow:

Latin, Division. Greek, Multiplication. Milli = 1000th of the unit. Deca $= 1^{i}$ times the unit. Centi = 100th of the unit. Hecato = 100 times the unit.Deci = 10th of the unit. Kilio = 1000 times the unit. Metre, Litre, Stere, Are, Franc, Gramme. | Myrio = 10000 times the unit.

French Measure of Length.

= 0.03937079 inches. 1 Metre (unit) = 1 Millimetre 3.280899 feet. 1 Decametre = 32.80899 feet. 1 Hectometre = 328.0899 feet 1 Centimetre = 0.3937079 inches. = 3.937079 inches. 1 Decimetre 1 Metre (unit) = 39.37079 inches. 1 Kilometre = 3280.899 ft. : 40.621381 Sca mile or = 1.8472 kilometre. mile. 1 Statute mile = 1.609315 kilometres. 1 Kilometre = 0.541343 sea miles. 1 Kilometre =

French Measure of Surface.

49.7106 chains.

= 1076.43 square feet. 1 Sq. metre = 10.7643 square feet. 1 Are = 107.643 square feet. = 100 square metres. 1 Decare 1 Are 1 Decare = 10 ares. 1 Hectare = 2.47114 Eng. acres. 1 Hectare = 100 ares. 1 Sq. mile = 258.989 hectares.

French Measure of Volume.

1 Stere (cubic = 10 decasteres. metre) 1 Stere = 35.3166 Eng. cubic feet. 1 Litre = 61.0271 Eng. cubic inches. 1 Gallon = 3.7852 litres.= 1000 litres. 1 Stere 1 Decistere = 2.84 bushels. = 1 cubic decimetre. 1 Litre 1 Decistere = 3.53166 cubic feet.

French Measure of Weight.

= 10 decigrammes. 1 Ton = 1 cubic metre dis- | 1 Gramme 1 Decigramme = 10 centigrammes. tilled water. 1 Centigramme = 10 milligrammes. = 1000 kilogrammes. 1 Ton 1 Kilogramme = 2.2047 pounds avoir-1 Kilogramme = 1000 grammes. 1 Hectogramme = 100 grammes. dupois. 1 Eng. pound = 0.45358 kilogrammes. $= 10 \, \text{grammes}.$ 1 Decagraninie 1 Gramme = 1 cubic centimetre = 15.43315 grains troy. 1 Gramme distilled water. 1 English ton = 1.01598 French tons. = 0.984274 Eng. tons. 1 French ton

French Coin.

1 Franc 100 centimes = 19.06 cents of an American dollar.

			-		
A	- 6	77 72-7-	T oll - on	24-	Continantana
Conversion	α	EUTISH	A BRCHROS	11110	Centimetres.
COLLINICIA			MAL WAL CO	-110	0 02201

Inch's	0	1	2	3	4	5	6	7	8	9
	Ct.mt.									
0	0.000	2.540	5.080	7.620	10.16	12.70	15.24	17.78	20.32	22.86
10	25.40	27.94	30.48	33.02	35.56	38.10	40.64	43.18	45.72	48.26
20	50.80	53.34	55.88	58.42	60.96	63.50	66.04	68.58	71.12	73.66
30	76.20	78.74	81.28	83.82	86.36	88.90	91.44	93.98	96.52	99.06
40	101.60	104.14	106.68	109.22	111.76	114.30	116.84	119.38	121.92	124.46
50	127.00	129.54	132.08	134.62	137.16	139.70	142.24	144.78	147.32	149.86
60	152.40	154.94	157.48	160.02	162.56	165.10	167.64	170.18	172.72	175.26
70	177.80	180.34	182.88	185.42	187.96	190.50	193.04	195.58	198.12	200.96
80	203.20	205.74	208.28	210.82	213.36	215.90	218.44	220.98	223.52	226.06
90	228.60	231.14	233.68	236.22	238.76	241.30	243.84	246.38	248.92	251.46
100	254.00	256.54	259.08	261.62	264.16	266.70	269.24	271.78	274.32	276.85

Conversion of Centimetres into English Inches.

Ct. mt.	0	1	2	3	4	5	6	7	8	9
	Inches.									
0	0.000	0.394	0.787	1.181	1.575	1.969	2.362	2.756	3.150	3.543
10	3.937	4.331	4.742	5.118	5.512	5.906	6.299	6.693	7.087	7.480
20	7.874	8.268	8.662	9,055	9.449	9.843	10.236	10.630	11.024	11.418
30	11.811	12.205	12.599	12.992	13.386	13.780	14.173	14.567	14.961	15.355
40	15.748	16.142	16.536	16.929	17.323	17.717	18.111	18.504	18.898	19.292
50	19.685	20 079	20.473	20.867	21.260	21.654	22.048	22.441	22.835	23.229
60	23.622	24.016	24.410	24.804	25.197	25.591	25.985	26.378	26.772	27.166
70	27.560	27.953	28.347	28.741	29.134	29.528	29.922	30.316	30.709	31.103
80	31.497	31.890	32.284	32.678	33.071	33.465	33.859	34.253	34.646	35.040.
90	35.434	35.827	36.221	36.615	37.009	37.402	37.796	38.190	38.583	38.977
100	39.370	39.764	40.158	40.552	40.945	41.339	41.733	42.126	42.520	42.914

Conversion of English Feet into Metres.

Feet.	0	_1_	2_	3	4	_5_	6	7	8	9
	Met.									
0	0.000	0.3048	0.6096	0.9144	1.2192	1.5239	1.8287	2.1335	2.4383	2.7431
10	3.0479	3.3527	3,6575	3,9623	4.2671	4.5719	4.8767	5.1815	5.4863	5.7911
20	6.0359	6.4006	6.7055	7.0102	7.3150	7.6198	7.9246	8.2294	8.5342	8.8390
30	9.1438	9.4486	9.7534	10.058	10.363	10.668	10.972	11.277	11.582	11.887
40	12.192	12.496	12.801	13.106	13.411	13.716	14.020	14.325	14.630	14.935
50	15.239	15.544	15.849	16.154	16.459	16.763	17.068	17.373	17.678	17,983
60	18 287	18.592	18.897	19.202	19.507	19.811	20.116	20.421	20.726	21.031
70	21.335	21.640	21.945	22.250	22.555	22.859	23.164	23.469	23.774	24.079
80	24.383	24.688	24.993	25.298	25.602	25.907	26.212	26.517	26.822	27.126
90	27.431	27.736	28.041	28.346	28.651	28.955	29.260	29.565	29.870	30.174
100	30.479	30.784	31.089	31.394	31.698	32.003	32.308	32.613	32.918	33.222

Conversion of Metres into English Feet.

Metres.	0	1	2	3	4	5	6	7	8	9
0 10 20 30 40 50 60	Feet. 0.000 32.809 65.618 98.427 131.24 164.04 196.85	Feet. 3.2809 36.090 68.899 101.71 134.52 167.33 200.13	Feet. 6.5618 39.371 72.179 104.99 137.80 170.61 203.42			Feet. 16.404 49.213 82.022 114.83 147.64 180.45 213 26	Feet. 19.685 52.494 85.303 118.11 150.92 183.73 216.54	121.39 154.20 187.01	Feet. 26.247 59.056 91.865 124.67 157.48 190.29 223.10	Feet. 29.528 62.337 95.146 127.96 160.76 193.57 226.38
70 80 90 100	229.66 262.47 295.28 328.09	232.94 265.75 298.56 331.37		239.51 272.31 305.12 337.93	242.79 275.60 308.40 341.21	246.07 278.88 311.69 344.49	314.97	252.63 285.44 318.25 351.06	321.53	259.19 292.00 324.81 357.62

Conversion of English Statute-miles into Kilometres.

Miles.	0	1	2	3	4	5	6	7	8	9
	Kilom.	Kilom.	Kilom.	Kilom.	Kilom.	Kilom.	Kilom.	Kilom.	Kilom.	Kilom,
0	0.0000	1.6093	3.2186	4.8279	6.4372	8.0465	9.6558	11.2652	12.8745	14.4848
10	16.093	17.702	19.312	20.921	22.530	24.139	25.749	27.358	28.967	30.577
20	32.186	33.795	35.405	37.014	38.623	40.232	41.842	43.451	45.060	46.670
30	48.279	49.888	51.498	53.107	54.716	56.325	57.935	59.544	61.153	62.763
40	64.372	65.981	67.591	69.200	70.809	72.418	74.028	75.637	77.246	78.856
50	80.465	82.074	83.684	85.293	86.902	88.511	90.121	91.730	93.339	94.949
60	96.558	98.167	.99.777	101.39	102.99	104.60	106.21	107.82	109.43	111.04
70	112.65	114.26	115.87	117.48	119.08	120.69	122.30	123.91	125.52	127.13
80	128.74	130.35	131.96	133.57	135.17	136.78	138.39	140.00	141.61	143.22
90	144.85	146.44	148.05	149.66	151.26	152.87	154.48	156.09	157.70	159.31
100	160.93	162.53	164.14	165.75	167.35	168.96	170.57	172.18	173.79	175.40

Conversion of Kilometres into English Statute-miles.

Kilom.	0	1.	2	3	4	5	6	12	8	9		
	Miles.	Miles.	Miles.	Miles.	Miles.	Miles.	Miles.	Miles.	Miles.	Miles.		
0	0.0000	0.6214	1.2427	1.8641	2.4855	3.1069	3.7282	4.3497	4.9711	5.5924		
10	6.2138	6.8352	7.4565	8.0780	8.6994	9.3208	9.9421	10.562	11.185	11.805		
20	12.427	13.049	13.670	14.292	14.913	15.534	16.156	16.776	17.399	18.019		
30	18.641	19. 263	19.884	20.506	21.127	21.748	22.370	22.990	23.613	24,233		
40	24.855	25.477	26.098	26.720	27.341	27.962	28.584	29.204	29.827	30.447		
50	31.069	31.690	32.311	32.933	33.554	34.175	34.797	35.417	36.040	36.660		
60	37.282	37.904	38.525	39.147	39.768	40.389	41.011	41.631	42.254	42.874		
70	43.497	44.118	44.739	45.361	45.982	46.603	47.225	47.845	48.468	49.088		
80	49.711	50.332	50.953	51.575	52.196	52.817	53.439	54.059	54.682	55.302		
90	55.924	56.545	57.166	57.788	58.409	59.030	59.652	60.272	60.895	61.515		
100	62.138	62.759	63.380	64.002	64.623	65.244	65.866	66.486	67.109	67.729		

Conversion of Sea-miles, Knots or Minutes into Kilometres.

Knots.	0	1	2	3	4	5	6	17	8	9
	Kilom.									
0	0.0000	1.8472	3.6944	5.5416	7.3888	9.2361	11.083	12.930	14.777	16.625
10	18.472	20.319	22.166	24.013	25.861	27.708	29.555	31.402	33.249	35.097
20	36.944	38.791	40.638	42.485	44.333	46.180	48.027	49.874	51.721	53.569
30	55.416	57.263	59.110	60.957	62.805	64.652	66.499	68.346	70.193	72.041
4 0	73.888	75.735	77.582	79.429	81.277	83.124	84.971	86.818	88.665	90.513
50	92.361	94.207	96.054			101.59				20000
60	110.83	112.68	114.53	116.37	118.22	120.06	121.91	123.76	125.61	127.45
70	129.30	131.15	133.00	134.84	136.70	138.54	140.39	142.24	144.09	145.94
80	147.77	149.62	151.47	153.31	155.18	157.02	158.87	160.72	162.57	164.43
90	166.25	168.09	169.94	171.78	173.65	175.49	177.34	179.19	181.04	182.90
100	184.72	186.56	188.41	190.25	192.12	193.96	195.81	198.66	199.51	201.37

Conversion of Kilometres into Sea-miles, Knots or Minutes.

Kilom.	0	1	2	3	4	5	6	7	8	9
	Knots.									
0	0.0000	0.5413	1.0827	1.6240	2.1653	2.7066	3.2480	3.7894	4.3307	4.8721
10	5.4134	5.9547	6.4961	7.0374	7.5787	8.1200	8.6614	9.2028	9.7441	10.285
20	10.827	11.368	11.909	12.451	12.992	13.533	14.075	14.616	15.157	15.702
30	16.24	16.781	17.322	17.864	18.406	18.946	19.488	20.029	20.570	21.115
40	21.653	22.194	22.735	23.277	23.819	24.359	24.901	25.442	25.983	26.528
50	27.066	27.607	28.148	28.690	29.232	29.772	30.314	30.855	31.396	31.941
60	32.480	33.020	33.561	34.103	34.645	35.185	35.727	36.268	36.809	37.364
70	37.894	38.433	38.974	39.516	40.058	40.598	41.140	41.681	42.222	42.777
80	43.307	43.846	44.387	44.929	45.471	46.011	46.553	47.094	47.635	48.190
90	48.721	49.259	49.800	50.342	50.884	51.424	51.966	52.507	53.048	54.603
100	54.134	54.672	55.213	55.755	56.297	56.837	57.379	57.920	58.461	60.016

Comparison between Foot-measures of Different Nations.

LINEAR FEET.								
English.	Metre.	Prussia.	Saxony.	Baden.	Austria.	Hanover	Sweden.	
1	0.3048	0.9711	1.0763	1.0160	0.9642	1.0435	1.0265	
3.2809	1	3.1862	3.5312	3.3333	3,1634	3,4235	3.3678	
1.0297	0.3138	1	1.1083	1.0462	0.9929	1.0745	1.0572	
0.9291	0.2832	0.9023	1	0.9440	0.8959	0.9695	0.9538	
0.9843	0.3000	0.9559	1.0594	1	0.9490	1.0271	1.0164	
1.0371	0.3161	1.0072	1.1163	1.0537	1	1.0822	1.0963	
0.9583	0.2921	0.9307	1.0314	0.9736	0.9240	1	0.9838	
0.9741	0.2969	0.9459	1.0484	0.9838	0.9122	1.0165	1	
			SQUARE F	EET.		>		
1	0.0929	0.9431	1.1584	1.0322	0.9297	1.0888	1.0537	
10.764	1	10.152	12.469	11.111	10.007	11.721	11.342	
1.0603	0.0985	1	1.2283	1.0945	0.9858	1.1545	1.1130	
0.8603	0.0802	0.8141	1	0.8911	0.8026	0.9400	0.9097	
0.9688	0.0900	0.9137	1.1222	1	0.9007	1.0549	1.0330	
1.0756	0.0999	1.0144	1.2460	1.1103	1	1.1712	1.2019	
0.9184	0.0853	0.8661	1.0639	0.9480	0.8538	1.	0.9679	
0.9489	0.0881	0.8947	1.0941	0.9679	0.8321	1.0331	1	
			CUBIC FE	ET.				

1	0.0283	0.9159	1.2468	1.0487	0.8964	1.1362	1.1018
35.316	1	32.346	44.032	37.037	31.658	40.126	38.198
1.0918	0.0309	1.	1.3613	1.1450	0.9787	1.2405	1.1816
0.8021	0.0227	0.7346	1	0.8411	0.7190	0.9113	0.8677
0.9535	0.0270	0.8733	1.1889	1	0.8548	1.0834	1.0501
1.0756	0.0999	1.0144	1.2460	1.1103	1	1.1712	1.3176
0.8801	0.0249	0.8061	1.0973	0.9230	0.7890	1	0.9522
0.9243	0.0262	0.8483	1.1444	0.9522	0.7590	1.0501	1

Conversion of Pounds of Different Nations.

Eng. av.	Kilogram.	Prussia.	Austria.	Spain.	Hanover	Russia.	Sweden.
1	0.4536	0.9072	0.8110	0.9839	${0.9320}$	1.1076	1.0664
2.2046	1	2.0000	1.7857	2.1692	1.9842	2.4419	2.3511
1.1023	0.5000	1	0.8929	1.0857	1.0271	1.2209	1.1755
1.2346	0.5600	1.1200	1	1.2132	1.1490	1.3675	1.3166
1.0164	0.4610	0.9211	0.8243	1	0.9470	1.1257	1.0839
1.0730	0.4696	0.9752	0.8596	1.0557	1	1.1884	1.1442
0.9028	0.4095	0.8190	0.7313	0.8883	0.8414	1	0.9628
0.9377	0.4253	0.8508	0.7595	0.9226	0.8738	1.0386	1

Ancient Measures of Length.

Scripture.	Feet.	Inches.	Hebrew.	Feet.	Inches.
Digit,		0.912	Cubit,	1	9.868
Palm = 4 Digits, .		3.648	Sabbath day's journey,	3648	
Span = 3 Palms,		10.94	Mile = 4000 Cubits,	7296	
Cubit = 2 Spans, .	1	9.888	Day's journey $= 33.164 \text{ mi.}$		}
Fathon $= 3.46$ Cubits, .	7	3.552	Sacred Cubit,	2	0.24
Egyptian. Finger,		.7374	Roman.		
Nahud Cubit,	1	5.71	Digit,		.7257
Royal Cubit,	1	8.66	Uncia (Inch),		.967
Grecian.			Pes (foot) = 12 Uncias, .	• • •	11.60
Digit,		0.754	Cubit = 24 Digits,	1	5.406
Pous = 16 Digits, .		.0875	Passus = 3.33 Cubits, .	4	10.02
Cubit,	Î	1.598	Millarium (mile),	4842	
Stadium,	604	4.5	Arabian. Foot, .	1	1.14
Mile = 8 Stadiums, .	4835]	Babylonian. Foot,	1	1.68

Foreign Measures of Length Compared with American.

Places.	Meusures.	Inches.	Places.	Measures.	Inches.
Amsterdam, Antwerp, Bavaria, Berlin, Bremen, Brussels, China, " " Copenhagen, Dresden, England, Florence, France, " Geneva, Genoa,	Foot. "" "" "mathematic, "bnilder's, "tradesman's, "surveyor's "" "" Braccio. Pied de Roi, Metre, Foot, Palmo,	11·14 11·24 11·42 12·19 11·38 11·45 13·12 12·71 13·32 12·58 11·34 12·00 21·69 12·79 39.381 19·20 9·72	Malta, Moscow, Naples, Prussia, Rhineland, Riga, Rome, Russia, Sardinia, Sicily, Spain, " " Strasburg, Sweden, Turin, Venice,	Foot, Palmo, Foot, Arish, Foot, " " " Toesas, Palmo, Foot, " " " " " " " " " " " " "	11·17 13·17 10·38 12·36 38·27 12·35 10·79 11·60 13·75 9·78 9·53 11·03 66·72 8·64 11·39 11·69 12·72 13·40
Hamburg, Hanover, Leipsic, Lisbon,	Foot, " Palmo,	11·29 11·45 11·11 12·96 8·64	Vienna, . Zurich, . Utrecht, . Warsaw, .	66	13:40 12:45 11:81 10:74 14:03

Foreign Road Measures Compared with American.

Places.	Measures.	Yards.	Places.	Measures.	Yards.
Arabia,	Mile,	2148	Hungary, .	Mile,	9113
Bohemia, .	66	10137	Ireland, .	66	3038
China,	Li,	629	Netherlands,	• • • • •	1093
Denmark,	Mile,	8244	Persia,	Parasang, .	6086
England, .	" statute, .	1760	Poland, .	Mile, long,	8101
66	" geographical,	2025	Portugal, .	League,	6760
Flanders, .	66	6869	Prussia, .	Mile,	8468
France, .	League, marine,	6075	Rome,		2025
	" common,.	4861	Russia, .	Verst,	1167
66	" post, .	4264	Scotland, .	Mile,	1984
Germany, .	Mile, long,	10126	Spain,	League, common,	7416
Hamburg,		8244	Sweden, .	Mile,	11700
Hanover, .		11559	Switzerland,	• •	9153
Holland,.		6395	Turkey,	Berri,	1826

Foreign Measures of Surface Compared with American.

Places.	Measures.	Sq. Yds.	Places.	Measures.	Sq. Yds.
Amsterdam, Berlin, Canary Isles, England, . Geneva, Hamburg, Hanover, Ireland, Naples,	Morgen, " great, " small, Fanegada, Acre, Arpent, Morgen, " Acre, Moggia,.	9722 6786 3054 2422 4840 6179 11545 3100 7840 3998	Portugal, . Prussia, . Rome, . Russia, . Scotland, . Spain, . Sweden, . Switzerland, Vienna, . Zurich, .	Geira, Morgen, Pezza, Dessetina, Acre, Fanegada, Tunneland, Faux, Joch, Common acre,	6970 3053 3158 13066·6 6150 5500 5900 7855 6889 3875·0

Foreign Liquid Measures Compared with American.

Places.	Measures.	Cub. In.	Places.	Measures.	Cub. In.
Amsterdam,	Anker,	2331	Naples,	Wine Barille,	2544
"	Stoop,	146	-"	Oil Stajo, .	1133
Antwerp,	""	194	Oporto,	Almude,	1555
Bordeaux,	Barrique,	14033	Rome, .	Wine Barille,	2560
Bremen,	Stubgens,	194.5			2240
Canaries,	Arrobas, .	949	66	Boccali,	80
Constantinople,	Almud,	319	Russia,	Weddras, .	752
Copenhagen, .	Anker,	2355	66	Kunkas	94
Florence,	Oil Barille, .	1946	Scotland, .	Pint,	103.5
• •	Wine ".	2427	Sicily, .	Oil Caffiri, .	662
France,	Litre,	61.07	Spain,	Azumbras, .	22.5
Geneva,	Setier,	2760	"	Quartillos, '.	30.5
Genoa,	Wine Barille,	4530	Sweden, .	Eimer,	4794
"	Pinte,	90.5		Kanna,	159.57
Hamburg,	Stubgen, .	221	Trieste,	Orne,	4007
Hanover,	"	231	Tripoli, .	Mattari,	1376
Hungary,	Eimer,	4474	Tunis,	Oil "	1157
Leghorn,	Oil Barille, .	1942	Venice, .		628
Lisbon,	Almude, .	1040	Vienna, .	Eimer,	3452
Malta,	Caffiri,	1270	"	Maas,	86.33

Foreign Dry Measures Compared with American

Foreign Dry Measures Compared with American.							
Places.	Measures.	Cub. In.	Places.	Measures.	Cub. In.		
Alexandria,	Rebele,	9587	Malta,	Salme,	16930		
• "	Kislos,	10418	Marseilles,	Charge,	9411		
Algiers,	Tarrie,	1219	Milan,	Moggi,	8444		
Amsterdam, .	Mudde,	6596	Naples, .	Temoli,	3122		
	Sack,	4947	Oporto,	Alquiere,	1051		
Antwerp,	Viertel,	4705	Persia, .	Artaba	4013		
Azores,	Alquiere,	731	Poland,	Zorzec,	3120		
Berlin,	Scheffel	3180	Riga,	Loop,	39 78		
Bremen,	"	4339	Rome,	Rubbio,	16904		
Candia,	Charge,	9288	"	Quarti,	4226		
Constantinople,	Kislos,	2023	Rotterdam,	Sach,	6361		
Copenhagen, .	Toende,	8489	Russia,	Clietwert, .	12448		
Corsica,	Stajo,	6014	Sardinia,	Starelli,	2988		
Florence,	Stari,	1449	Scotland, .	Firlot,	2197		
Geneva,	Coupes,	4739	Sicily, .	Salme gros, .	• 21014		
Geuoa,	Mina,	7382	66	" generale,	16886		
Greece,	Medimni,	2390	Smyrna, .	Kislos,	2141		
Hamburg,	Scheffel, .	6426	Spain,	Catrize,	41269		
Hanover,	Malter,	6868	Sweden, .	Tunna,	8940		
Leghorn	Stajo,	1501	Trieste,	Stari,	4521		
"	Sacco,	4503	Tripoli, .	Caffiri,	19780		
Lisbon,	Alquiere, .	817	Tunis,		21855		
	Fanega, .	3268	Venice	Stajo,	4945		
Madeira,	Alquiere, ,	684	Vienna,	Metzen,	3753		
Malaga,	Fanaga,	3783					

English Measures of Capacity.

The Imperial gallon measures 277.274 cubic inches, containing 10 lbs. Avoirdupois of distilled water, weighed in air, at the temperature of 62°, the barometer at 30 inches.

For Grain. 8 bushels = 1 quarter.

1 quarter = 10.2694 cubic feet.

3 bushels = 1 sack.Coal, or heaped measure. 12 sacks = 1 chaldron.

Imperial bushel = 2218.192 cubic inches. * $Heaped\ bushel$, $19\frac{1}{2}$ ins. diam., cone 6 ins. high = $2812\cdot4872$ cubic ins. 1 chaldron = $58\cdot658$ cubic feet, and weighs 3136 pounds.

1 chaldron (Newcastle) = 5936 pounds.

Foreign Weights Compared with American.

-	*** * * * *	Lbs. per			Lbs. per
Places.	Weights.	100 avoir.	Places.	Weights.	100 avoir.
Aleppo,	Rottoli,	20.46	Hanover,	Pound,	93.20
"	Oke,	35.80	Japan,	Catty,	76.92
Alexandria, .	Rottoli,	107.	Leghorn,	Pound,	133.56
Algiers,	66	84.	Leipsic,	" (common)	
Amsterdam, .	Pound,	91.8	Lyons,	" (silk), .	98.81
Antwerp, .	46	96.75	Madeira, .	"	143.20
Barcelona,	66	112.6	Mocha,	Maund,	33.33
Batavia,	Catty,	76.78	Morea,	Pound,	90.79
Bengal,	Seer,	53.57	Naples,	Rottoli,	50.91
Berlin,	Pound,	96.8	Rome,	Pound,	133.69
Bologna,		125.3	Rotterdam, .	"	91.80
Bremen,	66	90.93	Russia,		110.86
Brunswick, .	"	97.14	Sicily,	"	142.85
Cairo,	Rottoli,	105.	Smyrna, .	Oke,	36,51
Candia,		85.9	Sumatra,	Catty,	35.56
China,	Catty,	75.45	Sweden,	Pound,	106.67
Constantinople		35.55	• •	" (miner's),	120.68
Copenhagen,	Pound,	90.80	Tangiers, .	" "	94.27
Corsica,	"	131.72	Tripoli,	Rottoli,	89.28
Cyprus,	Rottoli,	19.07	Tunis,		90.09
Damascus,		25.28	Venice,	Pound (heavy)	94.74
Florence,	Pound,	133.56	"	" (light)	150.
Geneva,	" (heavy),		Vienna,		81.
Genoa,	" "	92.86	Warsaw, .	"	112.25
Hamburgh, .	66 \$6	93.63	1		

A Uniform System of Metrology much Needed.

The preceding variety of tables of weights, measures and coins shows the great need of a uniform system of metrology throughout the world.

The French are the first in adopting a uniform decimal system of metrology, and an International Decimal Association has been formed for the special purpose of advocating the introduction of the French system into other countries, which Association has now labored on that subject for some twenty years with but little success. Only Belgium, Switzerland, Germany and Italy have adopted and enforced the French metrical system. It has been made legal in some other countries, but not enforced.

The principal difficulties in the way appear to be prejudices and jealousy. It must be admitted that the introduction of a new system of metrology causes some temporary inconveniences, but the objection is only temporary. Some few countries have decimated their old units in preference to adopting the French system.

One difficulty of the decimal system is, that the base 10 docs not admit of more than one binary division without fraction. See A New System of Arithmetic, page 44.

A NEW SYSTEM OF ARITHMETIC: WEIGHTS, MEASURES AND COINS.

The discordance among nations in adopting a uniform system of weights, measures and coins is caused by the base of our decimal arithmetic not being well suited for that purpose. In the shop and market it is desired to divide the units into binary fractions, which cannot be accommodated by the base 10 without cumberous decimal fractions, and the ordinary vulgar fractions are difficult to use in arithmetical calculations.

The best system of metrology yet devised for decimal arithmetics is the French Metric System, which has been adopted by most civilized nations, but not by the most practical nations—namely, those who speak the English language. The practical difficulty with the metric system is due to the arithmetic base 10 not admitting binary and trinary divisions without fractions, and that system is therefore inapplicable to the division of the circle and time, and can consequently not be used in navigation, geography and astronomy. These incurable defects of the metric system can never make it stable, but its abolishment is a mere question of time.

With the steady and unabated progress of sciences our descendants will not be contented with an incomplete system of metrology, but will devise a system that will accommodate the shop and market as well as geography and astronomy. The metric system is, however, far superior to the cumberous English metrology, and there is yet a chance for the English-speaking nations to devise and adopt a system of metrology that would be acceptable all over the world. Those who are thoroughly conversant with this subject seem to agree that the number 12 is the best suited as base for metrology, for the reason that it can be divided by 2, 3, 4 and 6 without leaving fractions, which is of great importance for the shop and market, and particularly so for mental calculations.

A committee of the English Parliament, appointed for investigating the feasibility of adopting the metric system, reported that 12 as a base of metrology would be much better for the shop and market than the metric system.

A writer in the *Edinburgh Review*, January, 1807, advocated very strongly the adoption of 12 as the base not only for metrology, but also for arithmetic. This writer hoped that the wisdom of the English-speaking nations will soon come up to the level of this species of reform—namely, to adopt the number 12 as the base for all measurements. But such important improvements are not thought of in the ordinary course of human affairs.

The Latin name for "twelve" is duodeni, and any system of metrology or arithmetic which is based on 12 is called the duodenal system.

A full description of duodenal systems of arithmetic and metrology will be found in Nystrom's "Elements of Mechanics," and also in Nystrom's "French Metric System."

The duodenal metrology with the present English units should be introduced first, and worked with decimal arithmetic until its utility is well understood, after which it would become very easy to introduce the duodenal arithmetic.

The duodenal arithmetic is as much better than decimal arithmetic as decimal arithmetic is better than the Roman notation.

The duodenal system has all the advantages and none of the disadvantages of the decimal system.

The English-speaking nations are behind the other civilized nations in two particular things—namely, in metrology and phonetic orthography. The removal of these two defects would save at least one half of the time, labor and expense now consumed in education.

Our present systems of metrology and orthography are great burdens upon children to learn; in fact, they can never learn them so as to be remembered, whilst the study of natural systems would be entertaining and never forgotten.

GEOMETRY.

DEFINITIONS.

Demonstration is a course of reasoning by which a truth is established. It consists of,

Thesis, the truth to be established, and,

Hypothesis, the foundation for the demonstration.

Axiom is that which is self-evident and requires no demonstration.

Theorem is something to be proved by demonstration.

Postulate is something to be done, but is self evident and requires no demonstration.

Problem is something proposed to be done, and requires demonstration.

Proposition is either a Theorem or a Problem.

Corolary is an obvious consequence deduced from something that has gone

Scolium is a remark on preceding propositions, commonly demonstrated by algebraical formulæ.

Lemma is something premised for a following demonstration.

Geometrical Quantities.

Point is a position, but no magnitude.

A Line is length, without breadth or thickness.

A Straight Line is the shortest distance between two points.

Curved line is a length which in every point changes its direction.

Superficies, Surface, Area, is that which has length and breadth, but no

Plane surface is a plane which coincides with a straight line in every direction

tion.

Curved surface is a plane which coincides with a curved line. Solid has length, breadth and thickness.

Circle.

Circle, Cirumference, Periphery, is a curved line drawn on a plane surface, and bounded at a common distance from one point in the plane, (centre.)

Radius is a line* drawn from the centre in a circle to the periphery.

Diameter is a line drawn through the centre to the periphery, or the longest

Chord is any line extending its both ends to the periphery of a circle, and does

not go through the centre.

Arc is a part of a periphery. Circle plane, is a plane surface bounded within a circumference.

Sector is a part of a circle-plane bounded within an arc and two radii. Segment is a part of a circle plane bounded within a chord and an arc.

Zone is a part of a circle included between two parallel chords.

Lune is the space between the intersecting arcs of two eccentric circles.

Oval is a round figure having one long and one short diameter at right angles to one another.

Semicircle is a half circle.

Quadrant is a quarter of a circle.

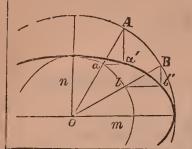
Angles.

Angle is the opening or inclination of two lines which meet in one point. If two radii being drawn from the extremities of a circle arc, to the centre; the arc, is a measure of the angle at the centre. Right angle is when the opening is a quarter of a circle.

Acute angle is less than a right angle.

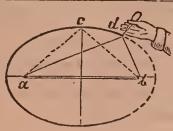
Obtuse angle is greater than a right angle.

• Line by itself means a straight line.



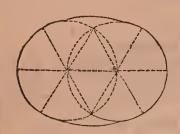
To construct an ellipse.

With o as a centre, draw two concentric circles with diameters equal to the long and short axes of the desired ellipse. Draw from o any number of radii, A, B, &c. Draw the line B b' parallel to n and b b' parallel to m, then b' is a point in the desired ellipse.



2. To draw an ellipse with a string.

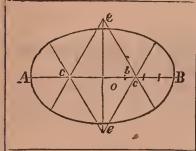
Having given the two axes, set off from c half the great axis at a and b, which are the two focuses in the ellipse. Take an endless string as long as the three sides in the triangle a, b, c, fix two pins or nails in the focuses one in a, and one in b, lay the string round a, and b, stretch it with a pencil d, which then will describe the desired ellipse.



3.

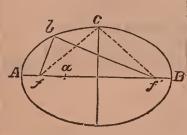
To draw an ellipse by circle arcs.

Divide the long axis into three equal parts, draw the two circles and where they intersect one another are the centres for the tangent arcs of the ellipse as shown by the figure.



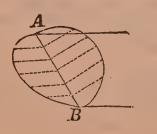
4. To draw an ellipse by circle arcs.

Given the two axes, set off the short axis from A to b, divide b B into three equal parts, set off two of these parts from o towards c and c which are the centres for the ends of the ellipse. Make equilateral triangles on c c, when e e will be the centres for the sides of the ellipse. If the long axis is more than twice the short one, this construction will not make a good ellipse.



To construct an ellipse.

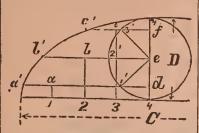
Given the two axes, set off half the long axis from c to f f, which will be the two focuses in the ellipse. Divide the long axis into any number of parts, say a to be a division point. Take A a as radius and f as centre and describe a circle are about b, take a B as radius and f as centre describe another circle are about b, then the intersection b is a point in the ellipse, and so the whole ellipse can be constructed.



B

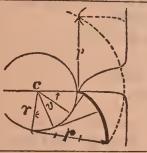
To draw an ellipse that will tangent two parallel lines in A and B.

Draw a semicircle on A B, draw ordinates in the circle at right angle to A B, the corresponding and equal ordinates for the ellipse to be drawn parallel to the lines, and thus the elliptic curve is obtained as shown by the figure.



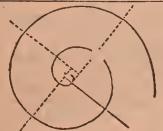
7. To construct a cycloid.

The circumference $C=3\cdot14$ D. Divide the rolling circle and base line C into a number of equal parts, draw through the division point the ordinates and abscissas, make $a\,a'=1'\,d$, $b\,b'=2'\,e$, $c\,c'=3'\,f$, then $a'\,b'$ and c' are points in the cycloid. In the Epicycloid and Hypocycloid the abscissas are circles and the ordinates are radii to one common centre.



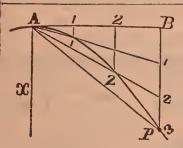
8. Evolute of a circle.

Given the pitch p, the angle v, and radius r. Divide the angle v into a number of equal parts, draw the radii and tangents for each part, divide the pitch p into an equal number of equal parts, then the first tangent will be one part, second two parts, third three parts, &c., and so the *Evolute* is traced.



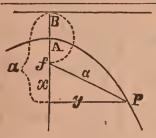
9. To construct a spiral with compasses and four centres.

Given the pitch of the spiral, construct a square about the centre, with the four sides together equal to the pitch. Prolong the sides in one direction as shown by the figure, the corners are the centres for each arc of the external angles.



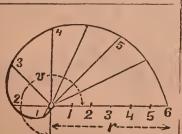
10. To construct a Parabola.

Given the vertex A, axis x, and a point P. Draw A B at right angle to x, and B P parallel to x, divide A B and B P into an equal number of equal parts. From the vertex A draw lines to the divisions on B P, from the divisions on A B draw the ordinates parallel to x, the corresponding intersections are points in the parabola.



11. To construct a Parabola.

Given the axis of ordinate B, and vertex A. Take A as a centre and describe a semicircle from B which gives the focus of the parabola at f. Draw any ordinate g at right angle to the abscissa A g, take g as radius and the focus g as a centre, then intersect the ordinate g, by a circle-arc in g which will be a point in the parabola. In the same manner the whole Parabola is constructed.



12.

To draw an arithmetic spiral.

Given the pitch p and angle v, divide them into an equal number of equal parts say 6. make 01=01, 02=02, 03=03, 04=04, 05=05, and 06=the pitch p; then join the points 1, 2, 3, 4, 5, and 6, which will form the spiral required.

THE CIRCLE.

Notation of Letters.

d = diameter of the circle.

r = radius of the circle.

p = periphery or circumfer-

a = area of a circle or part thereof.

b = length of a circle-arc.

c =chord of a segment, length of.

h = height of a segment.

s = side of a regular polygon.

v =centre angle.

w = polygon angle.

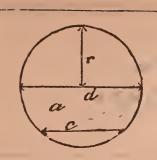
All measures must be expressed by the same unit.

Formulas for the Circle.

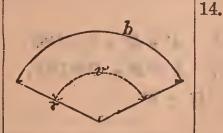
Periphery or Circum-	Diameter and Radius.	Area of the Circle.
ference.	$d = \frac{p}{\pi} = \frac{p}{3.14}$	$a = \frac{\pi d^2}{4} = 0.785d^2$.
$p = \pi d = 3.14d.$		7
$p = 2\pi r = 6.28r$.	$r = \frac{p}{2\pi} = \frac{p}{6.28}$	$a = \pi r^2 = 3.14r^2$.
$p = 2\sqrt{\pi a} =$	$d=2\sqrt{\frac{a}{\pi}}=1.128\sqrt{a}$.	$a = \frac{p^2}{2} = \frac{p^2}{2}$
$3.54\sqrt{a}$.	$a=2\sqrt{\pi}=1.128 \gamma a.$	4π 12.56
$p = \frac{2a}{r} = \frac{4a}{d}.$	$r = \sqrt{\frac{a}{\pi}} = 0.564\sqrt{a}.$	$a = \frac{pr}{r} = \frac{pd}{r}$
r d	$\sqrt{\pi}$	2 4

$\pi = 3.141592653589793238462643383279502884197169399$

$2\pi = 6.283185$	$\frac{1}{4}\pi = 0.785398$	$\frac{1}{\pi}$ =0.318310	$\frac{360}{\pi}$ =114.5915
$3\pi = 9.424778$	$\frac{1}{3}\pi$ =1.047197	$\frac{1}{\pi}$ =0.636619	$\pi^2 = 9.869650$
$4\pi = 12.566370$	$\frac{1}{2}\pi = 1.570796$	$\frac{3}{\pi}$ =0.954929	$\sqrt{\pi}$ =1.772453
$5\pi = 15.707963$	$\frac{1}{8}\pi = 0.392699$	$\frac{4}{\pi}$ =1.273239	$\sqrt{\frac{1}{\pi}}$ =0.564189
$6\pi = 18.849556$	$\frac{1}{6}\pi = 0.523599$	$\frac{6}{\pi}$ =1.909859	$\sqrt{\frac{\pi}{2}}$ =1.253314
$7\pi = 21.991148$	$\frac{1}{12}\pi = 0.261799$	**	-
$8\pi = 25.132741$	$\frac{2}{3}\pi = 2.094394$	$\frac{8}{\pi}$ =2.546478	$\sqrt{\frac{2}{\pi}}$ =0.797884
$9\tau = 28.274334$	$\left \frac{1}{360}\pi = 0.008726 \right $	$\frac{12}{\pi}$ = 3.819718	Log. $\pi = 0.49714987$

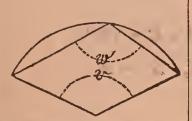


The periphery of a Circle is commonly expressed by the *Greek* letter $\pi=3.14$ when the diameter d=1 or the unit. For any other value of the diameter d, we will denote the periphery by the letter p, r= radius, and a= area of the circle. The periphery of a circle is equal to $3\frac{14}{100}$ times its diameter, c= chord.



 $b = \frac{\pi r v}{180} = 0.0175 r v,$

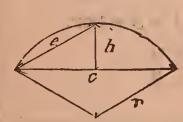
$$v = \frac{180b}{\pi r} = 57.296 \frac{b}{r}.$$



15.

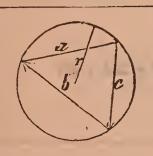
$$w = 180 - \frac{v}{2},$$

 $v = 2(180^{\circ} - w).$



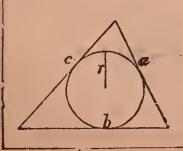
16.

$$r = \frac{c^2 + 4h^2}{8h} = \frac{e^2}{2h},$$
 $c = 2\sqrt{2hr - h^2}.$



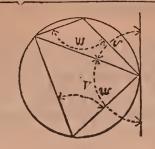
17.

$$r = \frac{ac}{2\sqrt{a^2 - (\frac{a^2 + b^2 - c^2}{2b})^2}}$$



18.

$$r = \frac{b\sqrt{a^2 - \left(\frac{a^2 + b^2 - c^2}{2b}\right)^2}}{a + b + \epsilon}$$



20.

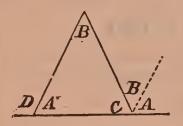
21.

22.

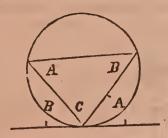
23.

24.

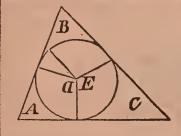
$$v = v, \quad w = w,$$
 $w + v = 180^{\circ}, w > v.$



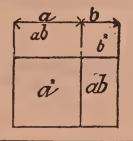
D = B + C, $A' + B' + C = 180^{\circ}$, B = D - C, $A + B + C = 180^{\circ}$, A' = A, B' = B'.



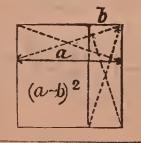
 $A + B + C = 180^{\circ},$ A' = A, B' = B.



 $E + C = A + D = 180^{\circ},$ D = B + c, E = A + B.



 $(a+b)^3 = a^3 + 2ab + b^2$.



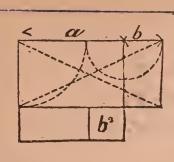
 $(a-b)^2 = a^2 - 2ab + b^2.$

26.

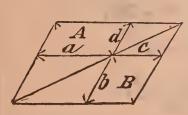
27.

28.

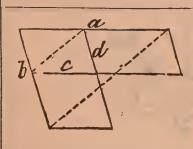
29.



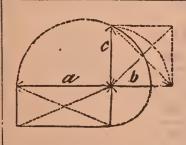
 $(a+b)(a-b)=a^a-b^a.$



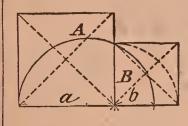
a:b=c:d, ad=bc, A=B.



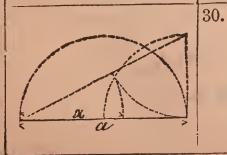
a:b=c:d, ad=bc.



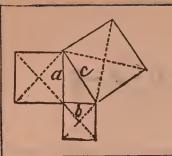
a: c = c: b, $ab = c^{2},$ $c = \sqrt{ab}.$



A:B=a:b.

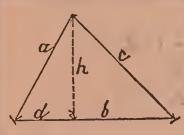


a: x = x: a - x, $x = \sqrt{a^2 + \left(\frac{a}{2}\right)^2 - \frac{a}{2}}$



$$c^{2} = a^{2} + b^{2},$$

 $a^{2} = c^{2} - b^{2},$
 $b^{2} = c^{2} - a^{2}.$

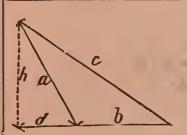


32.

$$c^{2} = a^{2} + b^{2} - 2bd,$$

$$h = \sqrt{a^{2} - d^{2}}.$$

$$d = \frac{a^{2} + b^{2} - c^{2}}{2b}.$$

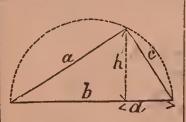


33. .

$$c^{2} = a^{2} + b^{2} + 2bd,$$

$$h^{2} = \sqrt{a^{2} - d^{2}},$$

$$d = \frac{c^{2} - a^{2} - b^{2}}{2b}.$$

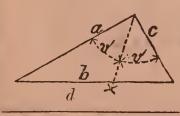


34.

$$a: b = h: c,$$

$$h = \frac{ac}{b} = \frac{ad}{c},$$

$$d = \frac{c^2}{b} = \frac{ch}{a}.$$

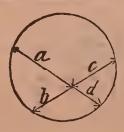


35.

$$a: c = d: (b - d),$$

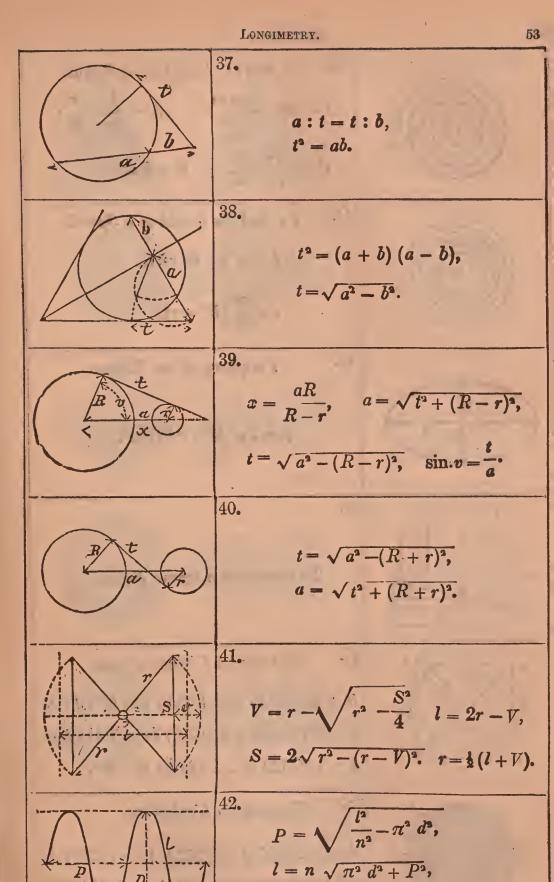
$$d = \frac{ab}{c + a},$$

$$v = v.$$



36.

$$a: c = b: d$$
, $ad = bc$.



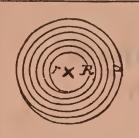
 $n=\sqrt{\pi^3 d^2+P}.$



43. To find the length of a Spiral.

$$l = \pi r n = \frac{\pi r^2}{P}, \qquad n = \frac{l}{\pi r} = \frac{r}{P},$$

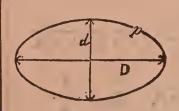
$$P = \frac{\pi r_2}{l} = \frac{r}{n}. \qquad P = Pitch.$$



44. To find the length of a Spiral.

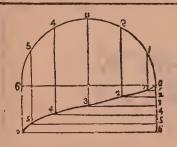
$$l=\pi n (R+r),$$

$$l=\frac{\pi}{P}(R^2-r^2).$$



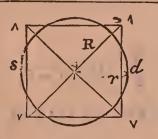
45. Periphery of an Ellipse.

$$p = 2\sqrt{D^2 + 1.4674d^2}$$



46.

To construct a screw Helix.

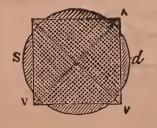


47. To square a Circumference.

R = 0.555355 d = 1.1107 r = 0.7071 S.

S = 0.785398 d = 1.57079 r = 1.4142 R.

d = 1.27322 S = 1.79740 R = 2 r.

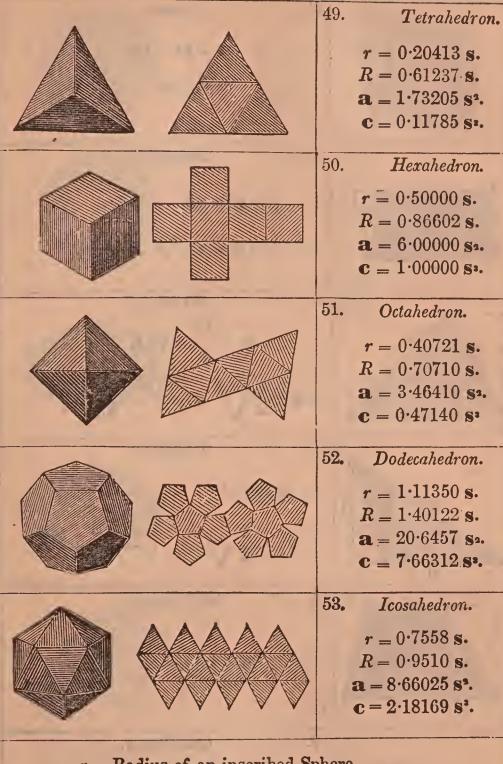


48. To square a Circleplane.

 $R = 0.626657 \ d = 1.253314 \ r = 0.7071 \ S.$

 $S = 0.886226 \ d = 1.77245 \ r = 1.4142 \ R$

d = 1.12838 S = 1.5367 R = 2 r.



r =Radius of an inscribed Sphere.

R =Radius of circumscribed Sphere.

a = Area of the Polyhedrons.

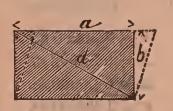
c = Cubic contents of the Polyhedrons.

s = Side or edge of the Polyhedrons.



1. Square.
$$\mathbf{a} = \mathbf{s}^2 = \mathbf{4}b^2.$$

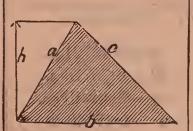
$$\mathbf{a} = 0.5d^2$$



55. Rectangle.

$$\mathbf{a} = a b$$
,

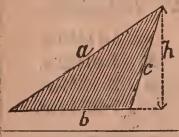
$$\mathbf{a} = b \sqrt{d^2 - b_2}$$



Triangle. 56.

$$\mathbf{a} = \frac{b h}{2} = \frac{1}{2}b h,$$

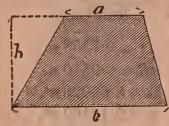
$$a = \frac{b}{2} \sqrt{a^2 - \left(\frac{a^2 + b^2 - c^2}{2b}\right)^2}$$



57. Triangle.

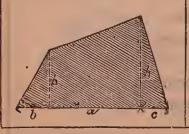
$$\mathbf{a} = \frac{1}{2}b h,$$

$$\mathbf{a} = -\frac{b}{2} \sqrt{a^2 - \left(\frac{c^2 - a^2 - b^2}{2b}\right)^2}$$



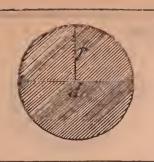
58. Quadrangle.

$$\mathbf{a} = \frac{1}{2}h(a+b).$$



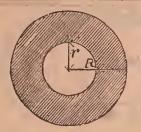
59. Quadrangle.

$$a = \frac{1}{2}(a[h+h'] + bh' + ch).$$



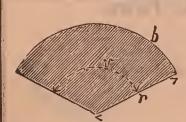
60. Circle Plane.

$$\mathbf{a} = \pi r^2 = 0.785 d^4,$$
 $\mathbf{a} = \frac{p r}{2} = 0.0796 P^2.$



61. Circle Ring.

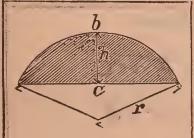
$$\mathbf{a} = \pi(R^2 - r^2) = \pi(R + r)(R - r),$$
 $\mathbf{a} = 0.785(D^2 - d^2).$



62. Sector.

$$\mathbf{a} = \frac{1}{2}b \, r,$$

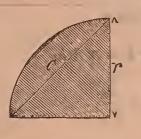
$$\mathbf{a} = \frac{\pi \, r^2 \, v}{360} = \frac{r_2 \, v}{114 \cdot 5}.$$



63. Segment.

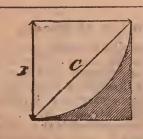
$$\mathbf{a} = \frac{1}{2} [b \, r - c \, (r - h)],$$

$$\mathbf{a} = \frac{\pi \, r^2 \, v}{360} + \frac{c}{2} (r - h).$$



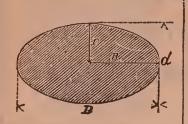
64. Quadrant.

$$\mathbf{a} = 0.785 \ r^2 = 0.3927 \ c^2.$$



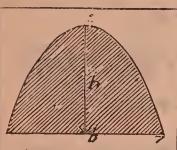
65.

$$\mathbf{a} = 0.215 \ r^* = 0.1075 \ c^*$$
.



Ellipse.

$$a = \pi R r = 0.785 D d.$$



67.

Parabola.

$$\mathbf{a} = \frac{2}{3} \ b \ h = \frac{1}{6} \ b^2,$$

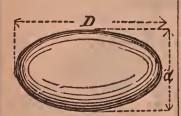
$$\mathbf{a} = \frac{2}{3} \, h \sqrt{p \, h}.$$



68.

Irregular Figure.

$$\mathbf{a} = b(h + h' + h'').$$

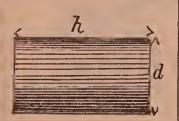


69.

Ellipsoid.

$$a = 8.88 r \sqrt{R^2 + r^2}$$

$$a = 2.22 d \sqrt{D^2 + d^2}$$
.

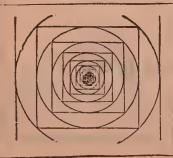


70.

Cylinder.

$$\mathbf{a} = 2 \pi r h = \pi d h,$$

$$h = \frac{\mathbf{a}}{2\pi r} = \frac{\mathbf{a}}{\pi d}.$$



71. The road to Extremity of Space.

1st. Draw a Circle and inscribe a Square, and in that Square a Circle, &c., &c., &c..... The last figure that can be drawn, is one extremity of Space Required if the last one is a Circle or a Square?

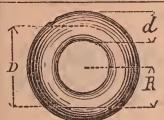
2nd. Draw a Circle and circumscribe a Square, and around that Square a Circle, &c., &c., &c. ... The last one that can be circumscribed is the other extremity of space. Required if the last figure is a Circle or a Square?

75.



Sphere.

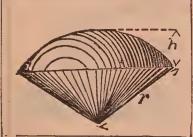
$$\mathbf{a} = 4 \pi r^2 = 12.56 r^2 = \pi d^3.$$



73. Forus.

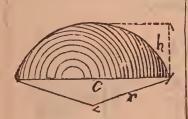
$$\mathbf{a} = 4 \, \pi^2 \, R \, r = 39.44 \, R \, r$$

$$a = 9.86 D d.$$



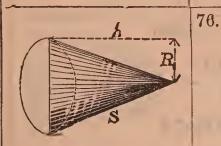
74. Sphere Sector.

$$\mathbf{a} = \frac{\pi r}{2} (4 h + c).$$



Circle Zone.

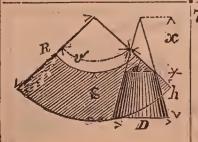
$$\mathbf{a} = 2 \pi r h = \frac{\pi}{4} (c^2 + 4 h^2)$$



Cone.

$$\mathbf{a} = \pi R s$$
,

$$\mathbf{a} = \pi R \sqrt{R^2 + h^2}.$$



Cone. $x = \frac{dh}{D-d}, \quad R = s + \frac{ds}{D-d},$

$$\mathbf{a} = \frac{\pi s}{2}(D+d),$$

$$v = \frac{180 D}{R} = \frac{180(D-d)}{s}$$
.



78. Sphere.

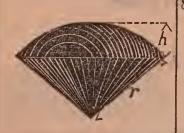
$$\mathbf{c} = \frac{4 \pi r^3}{3} = 4.189 \, \mathbf{r}^3,$$

$$\mathbf{c} = \frac{\pi d^3}{6} = 0.523 \, \mathbf{d}^3.$$



79. Forus.

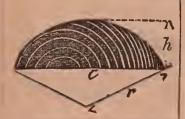
$$\mathbf{c} = 2 \pi_2 R r^2 = 19.74 R r^2,$$
 $\mathbf{c} = 2.463 D d^2.$



80. Sphere Sector.

$$\mathbf{C} = \frac{2}{3} \pi r^2 h = 2.0944 r^2 h,$$

$$\mathbf{C} = \frac{2}{3} \pi r^2 (r - \sqrt{r^2 - \frac{1}{4} c^2}).$$



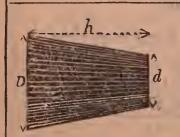
$$\mathbf{C} = \pi \ h^{2}(r - \frac{1}{3} \ h),$$

$$\mathbf{C} = \pi \ h^{2}(\frac{c^{3} + 4h^{2}}{8 \ h} - \frac{1}{3} \ h).$$



82. Cone.

$$\mathbf{c} = \frac{\pi r^2 h}{3} = 1.047 r^2 h,$$
 $\mathbf{c} = 0.2618 d^2 h.$



83. Conic Frustum.

$$\mathbf{C} = \frac{1}{3} \pi h(R^2 + R r + r^2),$$

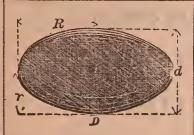
$$\mathbf{C} = \frac{1}{12} \pi h(D^2 + D d + d^2)$$



. Cylinder.

$$\mathbf{c} = \pi \, r^2 \, h = 0.785 \, d^2 \, h,$$

$$\mathbf{c} = \frac{p^2 h}{4 \pi} = 0.0796 p^2 h.$$

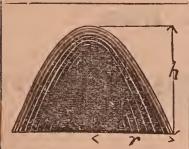


85.

Ellipsoid.

$$\mathbf{c} = 0.424 \ \pi^2 \ R \, r^2 = 4.1847 \ R \, r^3$$

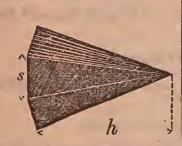
$$\mathbf{C} = 0.053 \, \pi^2 \, D \, d^2 = 0.5231 \, D \, d^2$$



86.

Paraboloid.

$$\mathbf{c} = \frac{1}{2} \pi r^2 h = 1.5707 r^2 h.$$

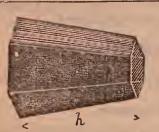


87.

Pyramid.

$$\mathbf{c} = \frac{1}{6} \mathbf{a} h,$$

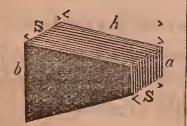
$$\mathbb{C} = \frac{n \, s \, h}{6} \sqrt{r^2 - \frac{s^2}{4}}$$



88.

Pyramidic Frustum.

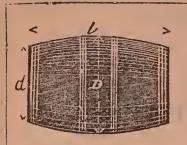
$$\mathbf{c} = \frac{h}{3}(A + \mathbf{a} + \sqrt{A\mathbf{a}}).$$



89.

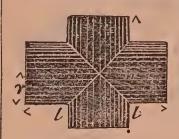
Wedge Frustum.

$$\mathbf{c}=\frac{h\,s}{2}(a+b).$$



$$c = 1.0453 l(0.4 D^2 + 0.2 D d + 0.15 d^3),$$

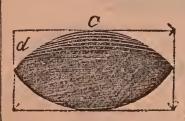
Gallon =
$$\frac{l}{2200} (4 D^2 + 2 Dd + 1.5 d^2)$$
.



91. Cylinder Sections.

$$\mathbf{c} = \pi r^2 (l + l' - \frac{2}{3} r),$$

$$\mathbf{c} = \pi \ r^2(l+l') - 2 \cdot 1 \ r^2$$
.



92. Circular Spindle.

$$c = \pi(\frac{1}{6} c^3 - 0.2 d[c + \frac{2}{3} \sqrt{c^2 + d^2}] \sqrt{d^2 + c^2})$$

Example 1. Fig. 56. The base of a Triangle is b=8 feet, 3 inches, and the height, h=5 feet, 6 inches. What is the area a=?

$$\mathbf{a} = \frac{b \ h}{2} = \frac{8.25 \times 5.5}{2} = 22.6875 \text{ square feet.}$$

Example 2. Fig. 62. A Circle Sector having an angle $v = 39^{\circ}$ and the radius $r = 67\frac{3}{4}$ inches. What is the area of the sector a = ?

$$\mathbf{a} = \frac{\pi r^2 v}{360} = \frac{3.14 \times 67.75^2 \times 39^\circ}{360} = 1562.1 \text{ square feet.}$$

Example 3. Fig. 75. A Spherical Zone having its diameter $c = 18\frac{1}{8}$ inches and height $h = 7\frac{3}{4}$ inches. What is the convex surface of the Zone?

$$\mathbf{a} = \frac{\pi}{4} (c^2 + h^2) = \frac{3.14}{4} (18.5^2 + 7.75^2) = 315.96 \text{ square inches.}$$

Example 4. Fig. 52. Require the radius R of a Sphere that will circumscribe a Dodecahedron with the side s=9 inches.

$$R = 1.36428 \times 9 = 12.27852$$
 inches, the answer.

Example 5. Fig. 89. A Frustrum of a Cone having its bottom diameter D=13 inches, the top diameter $d=5\frac{1}{4}$ inches, and the height h=25 inches. What is the cubic contents $\mathbf{c}=?$

 $\mathbf{c} = \frac{1}{10} \pi h (D^2 + Dd + d^2) = 0.2618 \times 25 (13^2 + 13 \times 5.25 + 5.25^2) = 20995$ cubic inches.

Example 6. Fig. 90. A Cask having its bung diameter D=36 inches, head diameter d=28 inches, and length l=56 inches, (inside measurement) how many gallons of liquid can be contained in the cask? (The gallon = 231 cub. il..)

Gallon =
$$\frac{56}{2200}$$
 $\left(4 \times 36^{\circ} + 2 \times 36 \times 28 + 1.5 \times 28^{\circ}\right) = 214$ gallons.

Example 7. Fig. 14. Require the length of the circle-arc b, when the angle $v = 42^{\circ}$, and the radius r = 4 feet, 3 inches?

$$b = \frac{\pi r v}{180} = \frac{3.14 \times 4.25 \times 42}{180} = 3.113$$
 feet.

Example 8. Fig. 16. Require the radius of a circle-arc, whose chord is 9 feet, 4 inches, and height, h = 1 foot, 8 inches?

$$r = \frac{c^2 + 4h^2}{8h} = \frac{9.33^2 + 4 \times 1.66^2}{8 \times 1.66} = \frac{98.0711}{13.28} = 7.384 \text{ feet.}$$

Example 9. Fig. 32. The three sides in a triangle being, a = 6.42, b = 7.75, and c = 8.66 feet. How high is the triangle over the base b?

$$d = \frac{a^2 + b^2 - c^2}{2b} = \frac{6 \cdot 42^2 + 7 \cdot 75^2 - 8 \cdot 66^2}{2 \times 8 \cdot 66} = 1 \cdot 5175 \text{ feet,}$$

the height $h = \sqrt{a^2 - d^2} = \sqrt{6.42^2 - 1.5175^2} = 6.24$ feet, the answer.

Example 10. Fig. 41. The radius of a walking beam is, r = 8.36 feet, the stroke S = 5.5 feet. How much is the vibration V = ?

Vibration,
$$V = r - \sqrt{r^2 - \frac{S^2}{4}} = 8.36 - \sqrt{8.36^2 - \frac{5.5^2}{4}}$$

=0.471 feet = 5.65 inches = $5 \cdot \frac{21}{20}$, the answer.

TABLE OF POLYGONS.

	-	Centre	Polygon	Side	Area	Apotem	Side	Area				
Number	- {	Angle w.	Angle v.	= h R.	$= \lambda S^{2}$.	== h R.	= h r.	$= h r^2.$				
of sides					~							
in the Polygon.							\triangle					
201,502.		1										
				5	S							
	- 5	1000	000	1.732	0.4220	0.5000	2.4047	F-1001				
Trigon.	3		60°		0.4330		3.4641	5.1961				
Tetragon.	4		900	1.4142	1.0000	0.7071	2.0000	4.0000				
Pentagon.	5	72°	108°	1.1755	1.7205	0.8090	1.4536	3.6327				
Hexagon.	6	600	120°	1.0000	2.5980	0.8660	1.1547	3.4640				
Heptagon.	7	51°43′	128°17′	0.8677	3.6339	0.9009	0.9631	3.3710				
Octagon.	8	450	135°	0.7653	4.8284	0.9238	0.8284	3.3130				
Nonagon.	9	400	140°	0.6840	6.1820	0.9396	0.7279	3.2750				
Decagon.	10	360	1440	0.6180	7.6942	0.9510	0.6498	3.2490				
Undecagon.	11	32°13′	147°47′	0.5634	9.3656	0.9595	0.5872	3.2290				
Dodecagon.	12	300	150°	0.5176	11.196	0.9659	0.5359	3.2152				
	14	25°43′	154017'	0.4450	15.334	0.9762	0.4562	3.1935				
_	15	240	156°	0.4158	17.642	0.9781	0.4250	3.1882				
	16	22°30′	157°30′	0.3900	20.128	0.9807	0.4068	3.1824				
	18	20°	160°	0.3472	25.534	0.9848	0.3526	3.1737				
	20	18°	162°	0.3130	40.634	0.9877	0.3166	3.1676				
	24	150	165°	0.2610	45.593	0.9914	0.2632	3.1596				

Explanation of the Table for Polygons.

The number of sides in the polygon is noted in the first column. k = tabular coefficient, to be multiplied as noted on the top of the columns. Example 1. How long is the side of an inscribed Pentagon, when the radius of the circle is 3 feet, and 4 inches? (4 inches = 0.333 feet.) $3.333 \times 1.1755 = 3.9179$ feet, the answer.

Example 2. What is the area of a Heptagon when one of its sides is 13.75 inches

13.752×3.6339=687.02 square inches.

	Circum.	Amaa						
		Area.		Circum.	Area.		Circum.	Area.
Diam.			Diam-			Diam-		
eter.			eter.			eter.		
1	3.1416	0.7854	51.	160.22	2042.8	101	317.30	8011.9
2	6.2832	3.1416	52	163.36	2123.7	102	320.44	8171.3
3	9.4248	7.0686	53	166.50	2206.2	103	323.58	8332.3
4	12.566	12.5664	54	169.65	2290.2	104	326.73	8494.9
5	15.708	19.6350	55	172.79	2375.8	105	329.87	8659.0
6	18.850	28.2743	56	175.93	2463.0	106	333.01	8824.7
7	21.991	38.4845	57	179.07	2551.8	107	336.15	8992.0
8	25.133	50.2655	58	182.21	. 2642.1	108	339.29	9160.9
9	28.274	63.6173	59	185.35	2734.0	109	342.43	9331.3
10	31.416	78.54	60	188.50	2827.4	110	345.58	9503.3
11	34.558	95.03	61	191.64	2922.5	111	348.72	9676.9
12	37.699	113.10	62	194.78	3019.1	112	351.86	9852.0
13	40.841	132.73	63	197.92	3117.2	113	355.00	10028.8
14	43.982	153.94	64	201.06	3217.0	114	358.14	10207.0
15	47.124	176.71	65	204.20	3318.3	115	361.28	10386.9
16	50.265	201.06	66	207.35	3421.2	116	364.42	10568.3
17	53.407	226.98	67	210.49	3525.7	117	367.57	10751.3
18	56.549	254.47	68	213.63	3631.7	118	370.71	10935.9
19	59.690	283.53	69	216.77	3739.3	$\begin{array}{ c c }\hline 119\\120\\ \end{array}$	373.85	11122.0
20 21	62.832	314.16	70 71	219.91 - 223.05	3848.5	121	376·99 380.13	11310 11499
$\begin{vmatrix} 21\\22 \end{vmatrix}$	65·973 69·115	346.36	72	226.19	3959·2 4071.5	122	383.27	11499
$\begin{bmatrix} 22 \\ 23 \end{bmatrix}$	72.257	380.13	73	229.34	4185.4	123	386.42	11882
24	75.398	415·48 452·39	74	232.48	4300.8	124	389.56	12076
25	78.540	490.87	75	235.62	4417.9	125	392.70	$\begin{array}{c} 12070 \\ 12272 \end{array}$
26	81.681	530.93	76	238.76	4536.5	126	395.84	12469
27	84.823	572.56	77	241.90	4656.6	127	398.98	12668
28	87.965	615.75	78	245.04	4778.4	128	402.12	12868
29	91.106	660.52	79	248.19	4901.7	129	405.27	13070
30	94.248	706.86	80	251.33	5026.6	130	408.41	13273
31	97.389	754.77	81	254.47	5153.0	131	411.55	13478
32	100.53	804.25	82	257.61	5281.0	132	414.69	13685
33	103.67	855.30	83	260.75	5410.6	133	417.83	13893
34	106.81	907.92	84	263.89	5541.8	134	420.97	14103
35	109.96	962.11	85	267.04	5674.5	135	424.12	14314
36	113.10	1017.88	86	270.18	5808.8	136	427.26	14527
37	116.24	1075.21	87	273.32	5944.7	137	430.40	14741
38	119.38	1134.11	88	276.46	6082.1	138	433.54	14957
39	122.52	1194.59	89	279.60	6221.1	139	436.68	15175
40	125.66	1256.63	90	282.74	6361.7	140	439.82	15394
41	128.81	1320.25	91 92	285.88	6503.9	$\begin{array}{c c} 141 \\ 142 \end{array}$	442.96	15615
42 43	131·95 135·09	1385.44	92	289·03 292·17	6647.6	143	446.11 449.25	15837
44	138.23	$1452 \cdot 20 \mid 1520 \cdot 52 \mid$	94	295.31	6939.8	144	452.39	16061 16286
45	141.37	1590.43	95	298.45	7088.2	145	452.39	16513
46	144.51	1661.90	96	301.59	7238.2	146	458.67	16742
47	147.65	1734.94	97	304.73	7389.8	147	461.81	16972
48	150.80	1809.55	98	307.88	7543.0	148	464.96	17203
49	153.94	1885.74	99	311.02	7697.7	149	468.10	17437
50	157.08	1963.5	100	314.16	7854.0		471.24	17671
	'							_

	Circum.	Area.	11 1	Cinama	Amaa	(1	0	1 4
		ATEM.		Circum.	Area.		Circum.	Area.
Diam- eter.			Diam- eter.			Diam- eter.		
151	474.38	17908	201	631.46	31731	251	788.54	49481
152	477.52	18146	202	634.60	32047	252	791.68	49876
153	480.66	18385	203	637.74	32365	253	794.82	50273
154	483.81	18627	204	640.89	32685	254	797.96	50671
155	486.95	18869	205	644.03.	33006	255	801.11	51071
156	490.09	19113	206	647.17	33329	256	804.25	51472
157	493.23	19359	207	650.31	33654	257	807.39	51875
158	496.37	19607	208	653.45	33979	258	810.53	52279
159	499.51	19856	209	656.59	34307	259	813.67	52685
160	502.65	20106	210	659.73	34636	260	816.81	53093
161 162	505.80	$20358 \\ 20612$	$\begin{array}{ c c c }\hline 211\\212\\\end{array}$	662.88	34967	261	819.96	53502
163	508·94 512·08	20812	$\begin{vmatrix} 212\\213\end{vmatrix}$	666.02	35299	262	823.10	53913
164	515.22	21124	214	$669 \cdot 16$ $672 \cdot 30$	35633 35968	$\begin{array}{ c c c c }\hline 263 \\ 264 \\ \hline \end{array}$	\$26.24 \$29.38	54325
165	518.36	21382	215	675.44	36305	265	832.52	54739 55155
166	521.50	21642	216	678.58	36644	266	835.66	55572
167	524.65	21904	217	681.73	36984	267	838.81	55990
168	527.79	22167	218	684.87	37325	268	841.95	56410
169	530.93	22432	219	688.01	37668	269	845.09	56832
170	534.07	22698	220	691.15	38013	270	848.23	57256
171	537.21	22966	221	694.29	38360	271	851.37	57680
172	540.35	23235	222	697.43	38708	272	854.51	58107
173	543.50	23506	223	700.58	39057	273	857.66	58535
174	546.64	23779	224	703.72	39408	274	860.80	58965
175	549.78	24053	225	706.86	39761	275	863.94	59396
176	552.92	24328	$\begin{bmatrix} 226 \\ 227 \end{bmatrix}$	710.00	40115	276	867.08	59828
177 178	556·06 559·20	$24606 \\ 24885$	228	713.14 716.28	40471 40828	277 278	870·22 873·36	60263 60699
179	562.35	25165	$\begin{vmatrix} 220 \\ 229 \end{vmatrix}$	719.42	41187	279	876.50	61136
180	565.49	25447	230	722.57	41548	280	879.65	61575
181	568.63	25730	231	725.71	41910	281	882.79	62016
182	571.77	26016	232	728.85	42273	282	885.93	62458
183	574.91	26302	233	731.99	42638	283	889.07	62902
184	578.05	26590	234	735.13	43005	284	892.21	63347
185	581.19	26880	235	738-27	43374	285	895.35	63794
186	584.34	27172	236	741.42	43744	286	898.50	64242
187	587.48	27465	237	744.56	44115	287	901.64	64692
188	590.62	27759	238	747.70	44488	288	904.78	65144
189	593.76	$28055 \\ 28353$	$\begin{bmatrix} 239 \\ 240 \end{bmatrix}$	750·84 753·98	44863	289	907.92	65597
190	$\begin{bmatrix} 596.90 \\ 600.04 \end{bmatrix}$	28652	241	757.12	45239 45617	$\begin{array}{ c c c c c c c c c c c c c c c c c c c$	$911.06 \\ 914.20$	$66052 \\ 66508$
191	603.19	28953	242	760.27	45996	292	914.20	66966
193	606.33	29255	243	763.41	46377	$\begin{bmatrix} 292 \\ 293 \end{bmatrix}$	920.49	67426
194	609.47	29559	244	766.55	46759	294	923.63	67887
195	612.61	29865	245	769.69	47144	295	926.77	68349
196	615.75	30172	246	772.83	47529	296	929.91	68813
197	618.89	30481	247	775.97	47916	297	933.05	69279
198	622.04	30791	248	779-12	48305	298	936.19	69747
199	625.18	31103	249	782.26	48695	299	939.34	70215
200	628.32	31416	250	785.40	49087	300	942.48	70686

66	6 CIRCUMFERENCE AND AREA OF CIRCLES.							
	Circum.	Area.	11	Circum.	Area.	11	Circum.	Area.
Diam- eter.			Diam- eter.			Diam- eter.		
301	945.62	71158	351	1102.70	96762	401	1259.78	126293
302	948.76	71631	352	1105.84	97314	402	1262.92	126923
303	951.90	72107	353	1108.98	97868	403	1266.06	127556
304	955.04	72583	354	1112.12	98423	404	1269.20	128190
305	958.19	73062	355	1115.27	98980	405	1272:35	128825
306	961.33	73542	356	1118.41	99538	406	1275.49	129462
307	964.47	74023	357	1121.55	100098	407	1278.63	130100
308	967.61	74506	358	1124.69	100660	408	1281.77	130741
309	970.75	74991	359	1127.83	101223	409	1284.91	131382
310	973.89	75477	360	1130.97	101788	410.	1288.05	132025
311	977.04	75964	361	1134.11	102354	411	1291.19	132670
312	980.18	76454	362	1137.26	102922	412	1294.34	133317
313	983.32	76945	363	1140.40	103491	413	1297.48	$133965 \\ 134614$
314	986.46	77437	364	1143.54	$oxed{104062}{104635}$	414	1300·62 1303·76	134014 135265
315 316	989·60 992·74	77931 78427	365	1146·68 1149·82	$104035 \\ 105209$	$\begin{array}{ c c c }\hline 415 \\ 416 \\ \end{array}$	1306.90	135205 135918
317	995.88	78924	367	1149.82	105205	$\frac{410}{417}$	1310.04	136572
318	999.03	79423	368	1156.11	106362	418	1313.19	137228
319	1002.17	79923	369	1159.25	106941	419	1316.33	137885
320	1005.31	80425	370	1162.39	107521	$ \frac{410}{420} $	1319.47	138544
321	1008.45	80928	371	1165.53	108103	421	1322.61	139205
322	1011.59	81433	372	1168.67	108687	422	1325.75	139867
323	1014.73	81940	373	1171.81	109272	423	1328.89	140531
324	1017.88	82448	374	1174.96	109858	424	1332.04	141196
325	1021.02	82958	375	1178.10	110447	425	1335.18	141863
326	1024.16	83469	376	1181.24	111036	426	1338.32	142531
327	1027.30	83982	377	1184.38	111628	427	1341.46	143201
328	1030.44	84496	378	1187.52	112221	428	1344.60	143872
329	1033.58	85012	379	1190.66	112815	429	1347.74	144545
330	1036.73	85530	380	1193.81	113411	430	1350.88	145220
331	1039.87	86049	381	1196.95	114009	431	1354.03	145896
332	1043.01	86570	382	1200.09	114608	432	1357.17	146574
333	1046.15	87092	383	1203.23	115209	433	1360.31	147254
334 335	1049.29	87616	384	1206.37	115812	434	1363.45	147934
336	1052·43 1055·58	88141 88668	385 386	1209.51 1212.65	$egin{array}{c c} 116416 & \\ 117021 & \\ \end{array}$	435	1366·59 1369·73	$148617 \\ 149301$
337	1053.33 1058.72	89197	387	1212 03	117628	437	1372.88	149987
338	1061.86	89727	388	1213.30	118237	438	1376.02	150674
339	1065.00	90259	389	1210.04 1222.08	118847	439	1379.16	151363
340	1068.14	90792	390	1225.22	119459	440	1382.30	152053
341	1071.28	91327	391	1228.36	120072	441	1385.44	152745
342	1074.42	91863	392	1231.50	120687	442	1388.58	153439
343	1077.57	92401	393	1234.65	121304	443	1391.73	154134
344	1080.71	92941	394	1237.79	121922	444	1394.87	154830
345	1083.85	93482	395	1240.93	122542	445	1398.01	155528
346	1086.99	94025	396	1244.07	123163	446	1401.15	156228
347	1090.13	94569	397	1247.21	123786	447	1404.29	156930
348	$1093 \cdot 27$	95115	398	1250.35	124410	448	1407.43	157633
349	1096.42	95662	399	1253.50	125036	449	1410.58	158337
350	1099.56	96211	400	1256.64	125664	450	1413.72	159043

CIRCUMFERENCE ANI					AREA OF	OIRCLE	ss.	6
	Circum.	Area.	1	Circum.	Area.	{	Circum.	Area.
Diam-			D.		Million			dilling
eter.			Diam- eter.			Diam- eter.		
			0001			0001.		
451	1416.86	750757	FOT	1550.04	102100		7507.00	2112
		159751	501	1573.94	197136	551	1731.02	238448
452	1420.00	160460	502	1577.08	197923	552	1734.16	239314
453	1423.14	161171	503	1580.22	198713	553	1737.30	240182
454	1426.28	161883	504	1583.36	199504	554	1740.44	241051
455	1429.42	162597	505	1586.50	200296	555	1743.58	241922
456	1432.57	163313	506	1589.65	201090	556	1746.73	242795
457	1435.71	164030	507	1592.79	201886	557	1749.87	243669
458	1438.85	164748	508	1595.93	202683	558	1753.01	244545
459	1441.99	165468	509	1599.07	203482	559	1756.15	245422
460	1445.13	166190	510	1602.21	204282	560	$1759 \cdot 29$	246301
461	1448.27	166914	511	1605.35	205084	561	1762.43	247181
462	1451.42	167639	512	1608.50	205887	562	1765.58	248063
463	1454.56	168365	513	1611.64	206692	563	1768.72	248947
464	1457.70	169093	514	1614.78	207499	564	1771.86	249832
465	1460.84	169823	515	1617.92	208307	565	1775.00	250719
466	1463.98	170554	516	1621.06	209117	566	1778.14	251607
467	1467.12	171287	517	1624.20	209928	567	1781.28	252497
468	1470.27	172021	518	1627.35	210741	568	1784.42	253388
469	1473.41	172757	519	1630.49	211556	569	1787.57	254281
470	1476.55	173494	520	1633.63	212372	570	1790.71	255176
471	1479.69	174234	521	1636.77	213189	571	1793.85	256072
472	1482.83	174974	522	1639.91	214008	572	1796.99	256970
473	1485.97	175716	523	1643.05	214829	573	1800.13	257869
474	1489.11	176460	524	1646.20	215651	574	1803.27	258770
475	1492.26	177205	525	1649.34	216475	575	1806.42	259672
476	1495.40	177952	526	1652.48	217301	576	1809.56	260576
477	1498.54	178701	527	1655.62	218128	577	1812.70	261482
478	1501.68	179451	528	1658.76	218956	578	1815.84	262389
479	1504.82	180203	529	1661.90	219787	579	1818.98	263298
480	1507.96	180956	530	1665.04	220618	580	1822.12	264208
481	1511.11	181711	531	1668.19	221452	581	1825.27	265120
482	1514.25	1.82467	532	1671.33	222287	582	1828.41	266033
483	1517.39	183225	533	1674.47	223123	583	1831.55	266948
484	1520.53	183984	534	1677.61	223961	584	1834.69	267865
485	1523.67	184745	535	1680.75	224801	585	1837.83	268783
486	1526.81	185508	536	1683.89	225642	586	1840.97	269702
487	1529.96	186272	537	1687.04	226484	587	1844-11	270624
488	1533.10	187038	538	1690.18	227329	588	1847.26	271547
489	1536.24	187805	539	1693.32	228175	589	1850.40	272471
490	1539.38	188574	540	1696.46	229022	590	.1853.54	273397
491	1542.52	189345	541	1699.60	229871	591	1856.68	274325
492	1545.66	190117	542	1702.74	230722	592	1859.82	275254
493	1548.81	190890	543	1705.88	231574	593	1862.96	276184
494	1551.95	191665	544	1709.03	232428	594	1866.11	277117
495	1555.09	192442	545	1712.17	233283	595	1869.25	278051
496	1558.23	1932442 193221	546	1715.31	234140	596	1872.39	278986
497	1560.25 1561.37	$\begin{vmatrix} 193221 \\ 194000 \end{vmatrix}$	547	1718.45	234998	597	1875:53	279923
498	1564.51	194782	548	171343 1721.59	235858	598	1878.67	280862
499	1564.65	195565	549	1721.33 1724.73	$\frac{235333}{236720}$	599	1881.81	281802
500	1507.03	196350	550		237583	600	1884.96	282743
300	1910.00	1.00000	000	1121 00	201000	000	1001 00	202130

68	CIRCUMFERENCE AND AREA OF CIRCLES.							
	Circum.	Area.	!	Circum.	Area.		Circum.	Area.
Diam- eter.			Diam- eter.			Diam- eter.		
601	1888.10	283687	651	2045.18	332853	701	2202.26	385945
602	1891.24	284631	652	2048.32	333876	702	2205.40	387047
603	1894.38	285578	653	2051.46	334901	703	2208.54	388151
604	1897.52	286526	654	2054.60	335927	704	2211.68	389256
605	1900.66	287475	655	2057.74	.336955	705	2214.82	390363
606	1903.81	288426	656	2060.88	337985	706	2217.96	391471
607	1906.95	289379	657	2064.03	339016	707	2221.11	392580
608	1910.09	290333	658	2067.17	340049	708	2224.25	393692
609	1913·23 1916·37	291289	659	2070·31 2073·45	$\begin{vmatrix} 341083 \\ 342119 \end{vmatrix}$	709	2227·39 2230·53	394805 395919
610	1910.57 1919.51	$\begin{vmatrix} 292247 \\ 293206 \end{vmatrix}$	660	2076.59	343157	$\begin{vmatrix} 710 \\ 711 \end{vmatrix}$	2233.67	397035
612	1922.65	$\begin{vmatrix} 293200 \\ 294166 \end{vmatrix}$	662	2079.73	344196	711	2236.81	398153
613	1925.80	$\begin{vmatrix} 294100 \\ 295128 \end{vmatrix}$	663	2082.88	345237	$\begin{vmatrix} 712 \\ 713 \end{vmatrix}$	2239.96	399272
614	1928.94	296092	$\frac{664}{664}$	2086.02	346279	714	2243.10	400393
615	1932.08	297057	665	2089.16	347323	715	2246.24	401515
616	1935.22	298024	666	2092.30	348368	716	2249.38	402639
617	1938-36	298992	667	2095.44	349415	717	2252.52	403765
618	1941.50	299962	668	2098.58	350464	718	2255.66	404892
619	1944.65	300934	669	2101.73	351514	719	2258.81	406020
620	1947.79	301907	670	2104.87	352565	720	2261.95	407150
621	1950.93	302882	671	2108.01	353618	721	2265.09	408282
622	1954.07	303858	672	2111.15	354673	722	2268.23	409416
623	1957.21	304836	673	2114.29	355730	723	. 2271.37	410550
624	1960.35	305815	674	2117.43	356788	724	2274.51	411687
625	1963.50	306796	675	2120.58	357847	725	2277.65	412825
626	1966·64 1969·78	307779	676	2123.72	358908	726	2280.80	413965
627	1909.78 1972.92	308763 309748	677	2126·86 2130·00	$\begin{vmatrix} 359971 \\ 361035 \end{vmatrix}$	$\begin{array}{c} 727 \\ 1728 \end{array}$	$2283.94 \ 2287.08$	415106 416248
629	1976.06	310736	679	2133.14	$\frac{361035}{362101}$	729	2290.22	417393
630	$1979 \cdot 20$	311725	680	2136.28	363168	730	2293.36	418539
631	1982.35	312715	681	2139.42	364237	731	2296.50	419686
632	1985.49	313707	682	2142.57	365308	732	2299.65	420835
633	1988.63	314700	683	2145.71	366380	733	2302.79	421986
634	1991.77	315696	684	2148.85	367453	734	2305.93	423139
635	1994.91	316692	685	2151.99	368528	735	2309.07	424292
636	1998.05	317690	686	2155.13	369605	736	2312.21	425447
637	2001.19	318690	687	2158.27	370684	737	2315:35	426604
638	2004:34	319692	688	2161.42	371764	738	2318.50	427762
639	2007.48	320695	689	2164.56	372845	739	2321.64	428922
640	2010.62	321699	690	2167.70	373928	740	2324.78	430084
641 642	$2013.67 \\ 2016.90$	$\begin{vmatrix} 322705 \\ 323713 \end{vmatrix}$	691	$2170.84 \ 2173.98$	$\begin{array}{c c} 375013 \\ 376099 \end{array}$	741	2327.92	431247
643	$2010 \cdot 30$ $2020 \cdot 04$	$\frac{323713}{324722}$	$\begin{bmatrix} 692 \\ 693 \end{bmatrix}$	2175.98	377187	742 743	$\begin{bmatrix} 2331.06 \\ 2334.30 \end{bmatrix}$	432412 433578
614	2023-19	325733	694	$\frac{217712}{2180\cdot 27}$	378276	744	2337.34	434746
645	$2026 \cdot 33$	$\frac{323733}{326745}$	695	2183.41	379367	745	2340.49	435916
646	2029.47	327759	696	2186.55	380459	746	2343.63	437087
647	2032.61	328775	697	2189.69	381554	747	2346.77	438259
648	2035.75	329792	698	2192.83	382649	748	2349.91	439433
649	2038.89	330810	699	2195.97	383746	749	2353.05	440609
650	2042.04	331831	700	2199.11	384845	750	2356.19	441786

		OTROOM	I EILE.	NCE AND F	TREA OF	JIKCLIF	43.	0
	Circum.	Area.	1	Circum.	Area.	11	Circum.	Area.
Diam-			Diam		COUNTY OF THE PARTY OF THE PART			COUNTY OF THE PARTY OF THE PART
eter.			Diam- eter.			Diam- eter.		
751	2359.34	442965	801	2516.42	503912	051	2673.50	50000
752	2362.48	444146	802	2519.56	505171	851		568786
753	2365.62	445328	1			852	2676.64	570124
754	2368.76	445525	803	2522.70	506432	853	2679.78	571463
755	2371.90	447697	804	2525.84	507694	854	2682.92	572803
756	2375.04		805	2528.98	508958	855	2686.06	574146
757	2378.19	448883	806	2532.12	510223	856	2689.20	575490
758	2381.33	450072	807	2535.27	511490	857	2692.34	576835
759	2384.47	451262	808	2538.41	512758	858	2695.49	578182
760	2387.61	452453	809	2541.55	514028	859	2698.63	579530
761	$\frac{258701}{2390.75}$	453646	810	2544.69	515300	860	2701.77	580880
762	2393.89	454841	311	2547.83	516573	861	2704.91	582232
763	2395.89	456037	812	2550.97	517848	862	2708.05	583585
764		457234	813	2554.11	519124	863	2711.19	584940
765	2400.18	458434	814	2557.26	520402	864	2714.34	586297
766	2403·32 2406·46	459635	815	2560.40	521681	865	2717.48	587655
767	2400.40 2409.60	460837	816	2563.54	522962	866	2720.62	589014
768		462041	817	2566.68	524245	867	2723.76	590375
769	2412:74 2415:88	463247	818	2569.82	525529	868	2726.90	591738
770	2419.03	464454	819	2572.96	526814	869	2730.04	593102
771	2419 03	465663	820	2576.11	528102 529391	870	$2733 \cdot 19$ $2736 \cdot 33$	594468
772	2425.31	466873 468085	821 822	2579·25 2582·39	530681	$\begin{bmatrix} 871 \\ 872 \end{bmatrix}$	2739.47	595835
773	2423 31 2428 45	469298	823	2585.53	531973	873	2739.47 2742.61	597204
774	2431.59	470513	$\begin{vmatrix} 825 \\ 824 \end{vmatrix}$	2588.67	533267	874	2745.75	598575 599947
775	2434.73	471730	825	2591.81	534562	875	2748.89	601320
776	2437.88	472948	826	2594.96	535858	876	2752.04	602696
777	2441.02	474168	827	2598.10	537157	877	2755.18	604073
778	2444.16	475389	828	2601.24	538456	878	2758.32	605451
779	2447:30	476612	829	2604.38	539758	879	2761.46	606831
780	2450.44	477836	830	2607.52	541061	880	2764.60	608212
781	2453.58	479062	831	2610.66	542365	881	2767.74	609595
782	2456.73	480290	832	2613.81	543671	882	2770.88	610980
783	2459.87	481519	833	2616.95	544979	883	2774.03	612366
784	2463.01	482750	834	2620.09	546288	884	2777.17	613754
785	2466.15	483982	835	2623.23	547599	885	2780.31	615143
786	2469.29	485216	836	2626.37	548912	886	2783.45	. 616534
787	2472.43	486451	837	2629.51	550226	887	2786.59	617927
788	2475.58	487688	838	2632.65	551541	888	2789.73	619321
789	2478.72	488927	839	2635.80	552858	889	2792.88	620717
790	2481.86	490167	840	2638.94	554177	890	2796.02	622114
791	2485.00	491409	841	2642.08	555497	891	2799.16	623513
792	2488.14	492652	842	2645.22	556819	892	$2802 \cdot 30$	624913
793	2491.28	493897	843	2648:36	558142	893	2805.44	626315
794	2494.42	495143	844	2651.50	559467	894	2808.58	627718
795	2497.57	496391	845	2654.65	560794	895	2811.73	629124
796	2500.71	497641	846	2657.79	562122	896	2814.87	630530
797	2503.85	498892	847	2660.93	563452	897	2818.01	631938
798	2506.99	500145	848	2664.07	564783	898	2821.15	633348
799	2510.13	501399	849	2667.21	566116	899	2824.29	634760
800	2513.27	502655	850	2670.35	567450	900	2827.43	636173

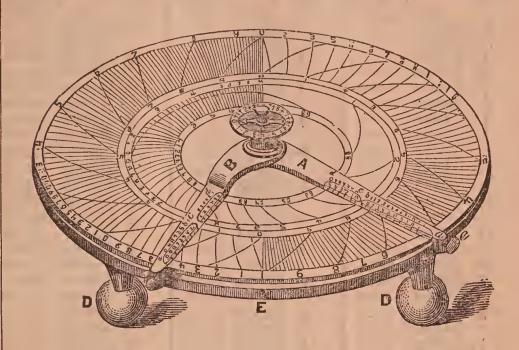
	Circum.	Area.	1 1	Circum.	Area.	11	Circum.	Area.
	Circum.	Alex.		On Cuin.	ATTON.			Allein
Diam-			Diam-			Diam- eter.		
eter.			eter.			Coci.		
901	2830.58	637587	934	2934.25	685147	967	3037.92	734417
901	2833.72	639003	935	$2934 29$ $2937 \cdot 39$	686615	968	3041.06	735937
902	2836.86	$\begin{bmatrix} 639003 \\ 640421 \end{bmatrix}$	936	2940.53	688084	969	3044.20	737458
904	2840.00	641840	937	2943.67	689555	970	3047.34	738981
905	2843.14	643261	938	2946.81	691028	971	3050.49	740506
906	2846.28	644683	939	2949.96	692502	972	3053.63	742032
907	2849.42	646107	$ \frac{933}{940} $	2953.10	693978	973	3056.77	743559
908	2852.57	647533	941	2956.24	695455	974	3059.91	745088
909	2855.71	648960	942	2959.38	696934	975	3063.05	746619
910	2858.85	650388	943	2962.52	698415	976	3066.19	748151
911	2861.99	651818	944	2965.66	699897	977	3069.34	749685
912	2865.13	653250	945	2968.81	701380	978	3072.48	751221
913	2868.27	654684	946	2971.95	702865	979	3075.62	752758
914	2871.42	656118	947	2975.09	704352	980	3078.76	754296
915	2874.56	657555	948	2978.23	705840	981	3081.90	755837
916	2877.70	658993	949	2981.37	707330	982	3085.04	757378
917	2880.84	660433	950	2984.51	708822	983	3088.19	758922
918	2883.98	661874	951	2987.65	710315	984	3091.33	760466
919	2887:12	663317	952	2990.80	711809	985	3094.47	762013
920	2890.27	664761	953	2993.94	713307	986	3097.61	763561
921	2893.41	666207	954	2997.08	714803	987	3100.75	765111
922	2896.55	667654	955	3000.22	716303	988	3103.89	766662
923	2899.69	669103	956	3003.36	717804	989	3107.04	768215
924	2902.83	670554	957	3006.50	719306	990	3110.18	769769
925	2905.97	672006	958	3009.65	720810	991	3113.32	771325
926	2909.11	673460	959	3012.79	722316	992	3116.46	772882
927	2912.26	674915	960	3015.93	723823	993	3119.60	774441
928	2915.40	676372	961	3019.07	725332	994	3122.74	776002
929	2918.54	677831	962	3022.21	726842	995	3125.88	777564
930	2921.68	679291	963	3025.35	728354	996	3129.03	779128
931	2924.82	680752	964	3028.50	729867	997	3132.17	780693
932	2927.96	682216	965	3031.64	731382	998	3135.31	782260
933	2931.11	683680	1 966	3034.78	732899	999	3138.45	783828

Explanation of the Preceding Table.

When the diameter is expressed in more or less units than in the table, add or subtract so many figures more in the circumference; add or subtract twice as many in the area.

Examples.	
Circumference.	Area.
29436.7	68955500
294.367	6895.55
29.4367	68.9555
2.94367	0.689555
	$29436.7 \\ 294.367 \\ 29.4367$

NYSTROM'S CALCULATOR.



ALL calculations in this POCKET BOOK have been computed by this Instrument. It consists of a silvered brass plate on which are fixed two moveable arms, extending from the centre to the periphery. On the plate are engraved a number of curved lines in such form and divisions, that by their intersection with the arms, numbers are read and problems solved.

The arrangement for trigonometrical calculations is such that it is not necessary to notice sine, cosine, tan, &c., &c., operating only by the angles themselves expressed in degrees and minutes. This makes trigonometrical solutions so easy, that any one who understands Simple Arithmetic, will be able to solve trigonometrical questions.

Calculations are performed by it almost instantly, no matter how complicated they may be, while there is nothing intricate or difficult in its use. The author of this book, who is the inventor, has thoroughly tested its practical utility. Without this instrument not one-tenth of the calculations and tables which he is continually bringing out, could be produced.

ADVERTISEMENT.

THE attention of Engineers, Ship builders, and all whose business requires frequent and extensive calculations, is called to Nystrom's Calculator. *Price* \$30. To be obtained with description by applying to John W. Nystrom, Philadelphia.

Communications will be promptly attended to.

This Calculator received the First Premium at the Franklin Institute Exhibition.

WM. J. YOUNG,

Mathematical, Optical, and Calculating Machine Manufacturer, 43 N. 7th St., Philadelphia.

Circ.	Area.		Circ.	Area	Circ.	Area
Iriame-	- Million	Diame		OTATION.	Diame-	
ter. (- <i>((((((((((((((((((((((((((((((((((((</i>	Diame- ter.			ter.	
1 .0001	•00076	=	75.70	70.025	11 24 55	95.033
$\frac{1}{3}\frac{1}{2}$ 0981 1963	.00306	5-	15.70 16.10	19.635 20.629	$\begin{array}{ c c c c c c c c c c c c c c c c c c c$	97.205
1903	01227	긫 -	16.49	20.025 21.647	35.34	99.402
$\frac{1}{8}$ 3926 5890	.02761	4	16.88	$\begin{vmatrix} 21.047 \\ 22.690 \end{vmatrix}$	35.73	101.62
₹	.04908	$\frac{1}{2}$	17.27	23.758	$\frac{1}{2}$ $\frac{36.12}{36.12}$	103.86
16 -9817	.07669	í	17.67	24.850	36.52	106.13
₹ - 1·178	.1104	<u> </u>	18.06	25.967	36.91	108.43
16 1.374	·1503		18.45	27.108	37.30	110.75
1.570 1.67	•1963	6-	18.84	28.274	12-137.69	113.09
1.767	•2485		19.24	29.464	38.09	115.46
\$ + 1.963	*3067	14 -	19.63	30.679	1 - 38.48	117.85
18 2.159	•3712	,	20.02	31.919	H 38·87	120.27
$\frac{3}{4}$ $ 2.356$ 2.552	•4417	1/2	20.42	33.183	$\frac{1}{2} - \frac{39.27}{39.33}$	122.71
18 2·552	•5184	3	20.81	34.471	39.66	125.18
$\frac{7}{8}$ + 2.748	·6013 ·6902	3 ~	21.20	35.784	40.05	127.67
$\begin{array}{c c} 15 \\ \hline 16 \\ \hline 1 \\ \hline \end{array}$ $\begin{array}{c c} 2.945 \\ 3.141 \\ \end{array}$	·7854	7_	-21.57 -21.99	37·122 38·484	13-40.44	130·19 132·73
3.534	•9940		22.38	39.871	41.23	135.29
3.927	1.227	1 -	22.77	41.282	1 - 41.62	137.89
4.319	1.484	*	23.16	42.718	42.01	140.50
$\frac{1}{2} - \frac{1}{4.712}$	1.767	1/2-	23.56	44.178	$\frac{1}{2} - \frac{1}{42.41}$	143.13
5.105	2.073	_	23.95	45.663	42.80	145.80
₹ + 5.497	2.405	3 -	24.34	47.173	₹ + 43·19	148.48
5.890	2.761		24.74	48.707	43.58	151.20
2 —6·283	3.141	8	25.13	50.265	14-143.98	153.93
6.675	3.546	,	25.52	51.848	44.37	156.69
1 - 7·068	3.976	1 -	-25.91	53.456	1 - 44.76	159.48
7.461	4.430	1	26.31	55.088	1 +45.16	162.29
7.854	4·908 5·411	1/2-	-26.70	56.745	$\frac{1}{2}$ - $\frac{1}{45.55}$	165.13
3 - 8·246 8·639	5.939	3 4 -	$\frac{27.09}{27.48}$	58·426 60·132	45·94 46·33	167·98 170·87
9.032	6.491	4	27.88	61.862	46.73	173.78
39.424	7.068	9	28.27	63.617	15 - 47.12	176.71
9.817	7.669		28.66	65.396	47.51	179.67
1 - 10.21	8.295	1 -	29.05	67.200	± +47.90	182.65
10.60	8.946		29.45	69.029	48.30	185.66
$\frac{1}{2}$ 10.99	9.621	1/2-	29.84	70.882	$\frac{1}{2}$ 48.69	188.69;
11.38	10.320		-30.23	72.759	49.08	191.74
₹ - 11·78	11.044	3 -	30.63	74.662	₹ + 49.48	194.82
H12·17	11.793	10	31.02	76.588	49.87	197.93
4-112.56	12.566	10	31.41	78.539	16	201.06
1 12.95	13.364 14.186	1	31.80	80.515	1 50.65	204.21
13·35 13·74	15.033	1 -	$\frac{32.20}{32.59}$	\$2.516 \$4.540	\$ -151.05	207.39
14.13	15.904	1 _	$\frac{32.99}{32.98}$	86.590	$\frac{1}{2}$ $\frac{51.44}{51.83}$	$\begin{vmatrix} 210.59 \\ 213.82 \end{vmatrix}$
14.52	16.800	2-	33.37	88.664	52.22	$\begin{vmatrix} 213.82 \\ 217.07 \end{vmatrix}$
₹ 114·92	17.720	3 4	33.77	90.762	3 + 52.62	220.35
15.31	18.665			92.885		223.65
		•			110001	

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17-153.40	226.98	23 72.25	415-17	29-1191.10	660.62
53.79	230.33	72.64	420.00	91.49	666.22
1 54.19	233.70	£ 173.04	424.55	4 31.80	671.95
64.68	237-10	73:43	429-13	92.28	677.71
2 54.97	240.52	73.82	433.73	3 92.67	683.49
55.37	243·97 247·45	2 74·21 74·61	438.30	93.06	689.29
\$ - 55.76	250.94	76.	447.69	2 - 93·46 93·85	700.98
18 66.64	264.46	24 75.39	462.39	30- 94.24	706.86
56.94	258.01	76.79	457.11	94.64	712.76
1 57.33	261.68	1 - 76-18	461.86	4 - 95.03	718.69
57.72	265.18	76.57	466.63	95.42	724.64
58.11	268.80	1 76.96	471.43	3 95.81	730.61
58.51	1272:44	77.36	176.26	96.21	736.61
2 58.00	276-11	2 - 77.75	481.10	2 96.60	742.64
59.29	279.81	78.14	485.97	96-99	748-69
19 69.69	283.52	25 78.54	490.87	31 97.38	754.76
50.03	287-27	78.93	496.79	97.78	760.86
1 160.47	291.03	1 79.32	500.74	1 - 98-17	766.99
60.86	294.83	79.71	605.71	98.56	773-14
3 61.26	298-64	₹ \\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\	510.70	3 98.96	779.31
161.65	302.48	80.20	515.72	99.36	785.51
2 - 62.04	306.35	2 - 80.89	520.70	至 - 99.74	791.73
62.43	310.24	81.28	525.83	100-1	797:97
20 62.83	314.16	26-181.68	530.03	32 100.5	804.24
63.22	318.09	82.07	536.04	100.9	810.64
\$ 63.61	322.06	1 - 82.46	541.18	1 101.3	816.86
164.01	326.05	32·85 -83·25	551.54	101.7	823·21 829·57
\$ 64.40 +64.79	334·10	3 - 83·25 83·64	556.76	102·1 102·4	835.97
2 - 35.18	338-16	2 - 84.03	562.00	2 - 102.8	842:39
35.68	342.25	84.43	567.26	103.2	848.83
21 65.97	346-36	2784.82	572.55	33 103.6	855:30
66:36	350.49	85.21	577.87	104	861-79
1 - 66.75	354-65	\$ - 85.60	583:20	3 - 104.4	868-30
67.15	358.84	86.	588.57	104.8	874.84
1 57.54	363-05	3 86.39	593.95	105.2	881.41
67.93	367-28	86.78	599.37	105.6	888.00
2 68.32	371.54	2 - 87.17	604.80	\$ · 106.	894-61
68.72	375.32	87.67	610.26	106.4	901-25
22 - 69.11	380-13	28 37.96	615.75	84 106.8	907.92
69.50	384.46	88.35	621.26	107.2	914.61
1 - 69.90	383.8%	1 88.75	626.79	1 107 6	921.32
-70-29	393.20	89.14	632.35	107.9	928.06
2 70.68	397.60	3 89.63	637-94	108.3	934.82
71.07	402.03	89.92	643-54	108.7	941.60
2 171.47	406.49	\$ 190.32	649-18	2 100.5	948-41
71.86	410.97	1390.71	654.83	1 109.6	900.70
1					

		1	1.4	Oi	Area.
Circ.	Area.	Circ.	Area.	Circ.	Area.
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					15040
35 - 109.9	962.11	41 - 128.8	1320.2	47-[147.6	1734.9
110.3	968.99	129.1	1328.3	148.	1744.1
1 110.7	975.90	½ † 129·5	1336.4	148.4	1753.4
H 111·1	982.84	129.9	1344.5	148.8	1762.7
111.5	989.80	$\frac{1}{2}$ 130·3	1352.6	$\frac{1}{2}$ 149.2	1772.0
H111·9	996.78	H 130·7	1360.8	149.6	1781.3
3 - 112.3	1003.7	₹ + 131·1	1369.0	₹ 150·	1790.7
1112.7	1010.8	131.5	1377.2	150.4	1800.1
36-1113	1017.8	42-131.9	1385.4	48-150.7	1809.5
113.4	1024.9	132.3	1393.7	H 150·1	1818.9
1 113.8	1032.0	1 132.7	1401.9	₹ 1 151·5	1828.4
H114·2	1039.1	133.1	1410.2	151.9	1837.9
$\frac{1}{2}$ 114.6	1046.3	$\frac{1}{2}$ 133.5	1418.6	$\frac{1}{2}$ - 152·3	1847.4
115.	1053.5	133.9	1426.9	H 152·7	1856.9
3 - 115.4	1060.7	₹ - 134·3	1435.3	₹ 153.1	1866.5
1115.8	1067.9	134.6	1443.7	153.5	1876.1
37 116.2	1075.2	43-135.	1452.2	49 - 153.9	1885.7
116.6	1082.4	H135·4	1460.6	154.3	1895.3
‡ · 117·	1089.7	1 135.8	1469.1	$\frac{1}{4} + 154.7$	1905.0
117.4	1097.1	H _{136·2}	1477.6	H155·1	1914.7
117.8	1104.4	136.6	1486.1	$\frac{1}{2}$ - $ 155.5$	1924.4
1118.2	11111.8	H137·	1494.7	155.9	1934.1
3 - 118.6	1119.2	₹ + 137·4	1503.3	$\frac{3}{4} + 156.2$	1943.9
1118.9	1126.6	H137·8	1511.9	156.6	1953.6
38 - 119.3	1134.1	44 138.2	1520.5	50-157.	1963.5
119.7	1141.5	138.6	1529.1	157.4	1973.3
120.1	1149.0	1 - 139·	1537.8	157.8	1983.1
120.5	1156.6	139.4	1546.5	H158·2	1993.0
$\frac{1}{2}$ 120.9	1164.1	139.8	1555.2	$\frac{1}{2}$ - $\frac{1}{158.6}$	2002.9
	1171.7	H140·1	1564.0	159.	2012.8
3 - 121.7	1179.3	$\frac{3}{4} - 140.5$	1572.8	$\frac{3}{4} + 159.4$	2022.8
122.1	1186.9	H140.9	1581.6	159.8	2032.8
39 122.5	1194.5	45-141.3	1590.4	5 1 - 160·2	2042.8
122.9	1202.2	141.7	1599.2	160.6	2052.8
1 123.3	1209.9	\frac{1}{4} \cdot \frac{1}{142 \cdot 1}	1608.1	<u>1</u> + 161⋅	2062.9
123.7	1217.6	142.5	1617.0	161.3	2072.9
124.	1225.4	$\frac{1}{2}$ 142.9	1625.9	$\frac{1}{2}$ + 161.7	2083.0
124.4	1233.1	143.3	1634.9	162.1	2093.2
₹ 124·8	1240.9	3 - 143.7	1643.8	3 - 162.5	2103.3
125.2	1248.7	H144·1	1652.8	H 162.9	2113.5
40-125.6	1256.6	46-144.5	1661.9	52 - 163·3	2123.7
126.	1264.5	H144·9	1670.9	163.7	2133.9
1 126.4	1272.3	145.2	1680.0	164.1	2144.1
126.8	1280.3	145.6	1689.1	164.5	2154.4
127.2	1288.2	1 146·	1698.2	1 164·9	2164.7
127.6	1296.2	1146.4	1707.3	165.3	2175.0
128.	1304.2	3 + 146.8	1716.5	₹ 1 165·7	2185.4
128.4	1312.2	147.2	1725.7	166.1	2195.7
	4			المسا	-

	Circ.	Area.		Circ.	Area.		Circ.	Area.
	One.	Million.		One.	Alea.		One.	Mea.
Diame-			Diame-		<i>\(\(\(\(\)\\\\\\\\\\\\\\\\\\\\\\\\\\\\</i>	Diame-		
ter.			ter.			ter.		
E9	166.5	2206.1	50	185.3	2733.9	65	1204.2	3318.3
53	166.8	2216.6	59 -			05		1
, ,			, [185.7	2745.5	7	204.5	3331.0
1 +	167.2	2227.0	1 +	186.1	2757.1	4 -	204.9	3343.8
, ,	167.6	2237.5		186.5	2768.8	,	205.3	3356.7
1/2	168.	2248.0	1/2	186.9	2780.5	12-	205.7	3369.5
	168.4	2258.5		187.3	2792.2		206.1	3382.4
2 -	168.8	2269.0	34	187.7	2803.9	<u> </u>	206.5	3395.3
	169.2	2279.6	20	188.1	2815.6	0.0	206.9	3408.2
54-	169.6	2290.2	60-	188.4	2827.4	66—	207.3	3421.2
, [170.	2300.8		188.8	2839.2	, ,	207.7	3434.1
1 +	170.4	2311.4	1 1	189.2	2851.0	1 -	208.1	3447.1
, [170.8	2322.1	,	189.6	2862.8	, ,	208.5	3460.1
1/2-	171.2	2332.8	1/2	190.	2874.7	1/2-	208.9	3473.2
	171.6	2343.5	9	190.4	2886.6	3	209.3	3486.3
34	172.	2354.2	2 +	190.8	2898.5	34	209.7	3499.3
	172.3	2365.0	0.7	191.2	2910.5	07	210	3512.5
55	172.7	2375.8	61-	191.6	2922.4	67—	210.4	3525.6
1	173.1	2386.6	, [192.	2934.4	,	210.8	3538.8
4 -	173.5	2397.4	1 +	192.4	2946.4	1 -	211.2	3552.0
	173.9	2408.3	,	192.8	2958.5	,	211.6	3565.2
1/2-	174.3	2419.2	1/2	193.2	2970.5	1/2	212.	3578.4
2	174.7	2430.1	2	193.6	2982.6	3 -	212.4	3591.7
3 -	175.1	2441.0	- 2 +	193.9	2994.7	4	212.8	3605.0
50	175.5	2452.0	60-	194.3	3006.9	68-	$-213.2 \\ -213.6$	3618.3
56	175.9	$\begin{vmatrix} 2463.0 \\ 2474.0 \end{vmatrix}$	62	194.7	3019.0	00-	214	3631.6
,	176.3		, _[195.1	3031.2	1	1	3645·0 3658·4
1 -	176.7	$\begin{vmatrix} 2485.0 \\ 2496.1 \end{vmatrix}$	4 -	195.5	3043.4	1 -	214.4	3671.8
, 1	177.5	2507.1	, ,	195.9	3055.7	1_	215.1	3685.2
12-	177.8		1 2	196.3	3067.9	12-	215.5	3698.7
R	178.2	$\begin{vmatrix} 2518 \cdot 2 \\ 2529 \cdot 4 \end{vmatrix}$	<u> </u>	196·7 197·1	$3080 \cdot 2 \\ 3092 \cdot 5$	3 -	-215.9	3712.2
3 -	178.6	2540.5	4	197.5	3104.8	4.	-216.3	3725.7
57	179.	2551.7	63	197.9	3117.2	69—	216.7	3739.2
31-	179.4	2562.9	05-	198.3	3129.6	00-	217.1	3752.8
1 -	179.8	2574.1	1 +	198.7	3149.0	1 -	10	3766.4
4	180.2	2585.4	4	199.	3154.4	4	-217.9	3780.0
1	180.6	2596.7	1-	199.4	3166.9	<u>1</u>	218.3	3793.6
2	181.	2608.0	2	199.8	3179.4	2	218.7	3807.3
3 -	181.4	2619.3	3 -	200.2	3191.9	3 -		3821.0
4 7	181.8	2630.7	4	200.6	3204.4	4	-219.5	3834.7
58-	182.2	2642.0	64-	201	3216.9	70-		3848.4
30-	182.6	2653.4	0.1	201.4	3229.5		220.3	3862.2
1 -	182.9	2664.9	1 -		3242.1	1 -		3875.9
4	183.3	2676.3	4	202.2	3254.8	4	221.	3889 8
1/2	183.7	2687.8	1/2-	202.6	3267.4	1/2-	221.4	3903.6
2	184.1	2699.3	2	203	3280.1		221.8	3917.4
3	184.5	2710.8	3 -	203.4	3292.8	身 -	222.2	3931.3
	184.9	2722.4		203.8	3305.5		2 2 2·6	3945.2
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89 —	279.6	6221.1		93 -	292.1	6792.9	97-	-1304.7	7389.8
	279.9	6238.6			292.5	6811.1		-305.1	7408.8
1 -	280.3	6256.1		4	292.9	6829.4	1 4	305.5	7427.9
	280.7	6273.6			293.3	6847.8		-305.9	7447.0
1/2-	281.1	6291.2	1.	1/2	293.7	6866.1	1 2-1	306.3	7466.2
	281.5	6308.8			-294.1	6884.5		306.6	7485.3
3 -	281.9	6326.4	ì	$\frac{3}{4}$ -	294.5	6902.9	34 -	307	7504.5
	282.3	6344.0	-		294.9	6921.3		307.4	7523.7
90-	282.7	6361.7		94-	295.3	6939.7	98—	307.8	7542.9
	283.1	6379.4			295.7	6958.2		308.2	7562.2
4 -	283:5	6397.1		4 -	- 296	6976.7	1 -	308.6	7581.5
, ,	283.9	6414.8		, 1	296.4	6995.2		309.0	7600-8
1/2	284-3	6432.6		12-	296.8	7013.8	$\frac{1}{2}$ -	309.4	7620-1
,	284.7	6450.4			297.2	7032.3		309.8	7639.4
3 -	285.1	6468.2		34 -	297.6	7050.9	34	310.2	7658.8
0.1	285.4	6486 0	ļ	0-	298	7069.5		310.6	7678.2
91-	285.8	6503.8		95-	298.4	7088-2	99 —	311.0	7697.7
7	286.2	6521.7		,	298.8	7106.9	,	311.4	7717.1
1 -	286.6	6539.6		4 -	299.2	7125.5	1 -	311.8	7736.6
7	287.	6557.6		,]	-1299·6 300·	7144.3	,	312.1	7756.1
1/2	287.4	6575.5		1/2	-300.4	7163.0	$\frac{1}{2}$ -	312.5	7775.6
3	287.8	6593.5		9	300.4	7181·8 7200·5	9	312.9	7795·2 7814·7
3 -	$288.2 \\ 288.6$	$6611.5 \\ 6629.5$		34	$\frac{300.8}{301.2}$	7200.5	3 -	313.3	7834.3
92	289	6647.6		96	301.5	7238.2	100	313·7 314·1	7853.9
54-	289.4	6665.7		90	301.9	7257.1	100	314.1	7853.6
1 -	289.8	6683·8		, ,	302.3	7275.9	1 -	314.9	7893.3
4	$\begin{bmatrix} 239 & 3 \\ 290 & 2 \end{bmatrix}$	6701.9		1 -	302.7	7294.9	3 -	315.3	7913.1
12-	290.5	6720.0		1/2	303.1	7313·S	1/2-	315.7	7932.7
2	290.9	6738.2		2	303.5	7332·S	2	316.0	7942.4
3 -	291.3	6756.4		3 -	303.9	7351.7	3 -	316.4	7972.2
4	291.7	6776.4		4	304.3	7370.7	4	316.8	7991.9
	1202				10010	10101		0100	

EXPLANATION OF THE TABLE FOR SEGMENTS, &c.

The chord divided by the height is the gauge in the Table, the quotient in the first column.

k = tabular coefficient, always to be multiplied by the chord.

To find the angle of an arc of a circle.

RULE. Divide the base (chord) of the arc by its height, (sine verse) and find the quotient in the first column. The corresponding number in the second column is the angle of the arc in degrees of the circle.

To find the radius of an arc of a circle.

RULE. Divide the chord of the arc by its height, and find the quotient in the first column. The corresponding number in the third column, multiplied by the chord, is the radius of the arc.

78		TABLE FO	e Segmen	T3 &c., of	A CIRCLE.			
Chord div.	Centre	Radius .	Cir. Arc.	Area Seg.	Surface	Solidity	Chord	
by height.	Angle v.	r = k c.	b = k c	a = h c2	$a = k c^2.$		$c = \lambda r$.	
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\ \ \		V	\\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\					
458.08	1	. 57.296	1.0000	•01091	.78539	00085	.01744	
229.18	2	28.649	1.0000	00218	•78549	.00172	.03490	
152.77	3	19.101	1.0000	.00327	1.78462	.00255	.05234	ı
114.57	4	14.327	1.0000	.00436	.78574	•00310	.06978	ı
84.747	5	11.462	1.0001	.00647	.78586	.00401	.08722	-
76.375	6	9.5530	1.0003	.00741	•78599	.00514	10466	1
65.943	7	8.1902	1.0004	.00910	.78621	.00592	·12208	1
57.273	8	7.1678	1.0006	01089	.78630	.00686	13950	1
50.902	. 9	6.3728	1.0008	01254	.78665	.00772	•15690	1
45.807	10	5.7368	1.0011	.01407	.78695	.00857	·17430	l
41.203	11	5.2167	1.0013	.01552	•78730	.00964	·19168	ı
38.133	12	4.7834	1.0016	01695	•78725	.01031	•20904	ł
35.221	13	4.4168	1.0019	01841	.78794	.01114	.22640	ı
32.742	14	4.1027	1.0023	.02000	.78832	·01199	.24372	ı
30.514	15	3.8307	1.0027	.02157	.78889	.01288	26104	
28.601	16	3.5927	1.0029	.02269	.78909	.01375	27834	
26.915	17	3.3827	1.0034	.02434	.78969	.01462	·295 6 0	
25.412	18	3.1962	1.0039	.02592	.79028	.01542	·31286	
24.068	19	3.0293	1.0044	.02744	.79084	.01635	·33008	
22.860	$\frac{10}{20}$	2.8793	1.0048	.02878	.79140	01722	•34728	
21.760	$\frac{20}{21}$	2.7440	1.0054	•03040	.79234	.01802	.36446	
20.777	$\frac{21}{22}$	2.6222	1.0059	•03178	.79300	01897	38160	
19.362	23	2.5080	1.0066	03173	.79340	.01984	.39872	
19.028	24	2.4050	1.0072	.03493	.79416	01004	.41582	
18.261	$\frac{21}{25}$	2.3101	1.0078	•03639	.79486	.02159	•43286	
17.553	26	2.2233	1.0084	•03784	.79530	02133	•44990	
16.970	27	2.1418	1.0091	03734	.79639	02248	46688	
16.288	28	$\frac{2.1413}{2.0673}$	1.0101	03370	.79748	02424	·483S4	
15.721	29	1.9969	1.0105	.04230	.79811	02424	.50076	
15.191	30	1.9319	1.0113	.04385	.79907	.02600	.51762	
14.970	31	1.8710	1.0121	.04476	.78530	.02692	.53446	
14.230	32	1.8140	1.0129	.04710	80098	.02778	.55126	
13.796	33	1.7605	1.0138	.04842	·S0181	.02866	·56802	
13.382	34	1.7102	1.0146	.04989	80300	02956	.58479	
12.994	35	1.6628	1.0155	04939	80405	02330	60140	
12.733	36	1.6184	1.0167	.05311	80531	.03137	.61802	
12.473	37	1.5758	1.0174	.05401	80622	03226	.63460	
11.931	38	1.5358	1.0184	.05628	·S0713	.03328	.65112	
11.621	39	1.4979	1.0194	05755	80850	.03418	.66760	
11.342	40	1.4619	1.0204	.05899			68404	
11.060	41	1.4266	1.0207	.06001			.70040	
10.791	42	1.3952	1.0226	.06196			.71672	
10.534	43	1.3643	1.0237	.06359			.73300	
10.289	44		1.0248	.06574			.74920	
10.043	45		1.0260	.06628	1		.76536	
9.8303	46		1.0272				.78146	
9.6153	47		1.0290				•79748	
9.4092	48		1.0297	.09138			81346	
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r				- DEGME	115 00., 02	A CIRCLE.		79
l	Chord div	Centre	Radius	Cir. Arc.	Area Sag.	Surface	Solidity	Chord
۱	by height.	Angle v.	r = k c.	b = k c.	$a = k e^{9}$.	$a = k c^2.$	$\mathbf{c} = k c^3$.	c = h r.
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Ì	\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\		1		1	\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\	-	No.
l	9.2113	49	1.2057	1.0309	.07290	.82244	.04330	·82938
١	9.0214	50	1.1831	1.0323	.07453	.82384	.04424	·84522
l	8.8387	51	1.1614	1.0336	07433	82562	.04519	
ł	8.6629	52		1.0349	•			*86102
1		53	1.1406		.07758	*82729	.04614	*87674
١	8.4462		1.1206	1.0364	•07959	*83363	.04685	•89238
	8.3306	54	1.1014	1.0378	.08083	*83072	.04805	•90798
l	8 1733	55	1.0828	1.0393	.08246	.83249	.04901	•92348
١	8.0215	56	1.0650	1.0407	.08400	*83422	.05002	•93894
ı	7.8750	57	1.0478	1.0422	.08579	*83602	.05098	•95430
ı	7.7334	58	1.0313	1.0431	.08680	·8379 6	.05191	.96960
ı	7.5895	59	1.0154	1.0454	08891	·84064	.05299	.98484
ı	7.4565	60	1.0000	1.0470	.09106	*84266	.05400	1.0000
ı	7.3358	61	•98515	1.0486	.09209	•84380	·054f6	1.0150
ı	7.2118	62	•97080	1.0503	.09375	*84581	.05583	1.0300
ł	7.0914	63	.95694	1.0520	.09540	.84791	.05684	1.0450
I	6.9748	64	•94352	1.0537	.09697	·84996	.05784	1.0598
l	6.8616	65	•93058	1.0555	.09865	·85215	.05885	1.0746
I	6.7512	66	•91804	1.0573	.10036	.85441	.05987	1.0892
ı	6.6453	67	•90590	1.0591	10030	·85640	.06088	1.1038
ľ	6.5469	68	·89415	1.0610	10367	·85815	.06181	1.1184
I	6.4902	69	·SS276	1.0629	10501	·85464	.06201	1.1328
Ī		70						
ľ	6.3431		.87172	1.0648	10710	*86350	06396	1.1471
Į	6.2400	71	*86102	1.0668	10887	·\$6699	.06515	1.1614
ı	6.1553	72	.85065	1.0687	•11046	*86834	.06604	1.1755
ı	6.0652	73	•84058	1.0708	•11225	.87081	.06709	1.1896
i	5.9773	74	*83082	1.0728	11385	.87935	.06815	1.2036
I	5.8918	75	*82134	1.0749	·11563	.87590	.06921	1.2175
ľ	5.8084	76	·81213	1.0770	·11736.	·87853	.07037	1.2313
	5.7271	77 .	·80319	1.0792	·11910	*88120	.07136	1.2450
ı	5.6478	78	•79449	1.0814	12072	.88389	.07244	1.2586
ı	5.5704	79	·78606	1.0836	·12281	.88677	.07352	1.2721
	5.4949	80	·77786	1.0859	12441	*88949	.07462	1.2855
-	5.4254	81	.76988	1.0882	·12660	·89161	.07512	1.2989
1	5.3492	82	.76212	1.0905	·12793	89520	.07683	1.3121
	5.2705	83	•75458	1.0920	·12958	.89958	.07819	1.3252
	5.2101	84	•74724	1.0953	·13157	90095	.07907	1.3383
ļ	5.1429	85	.74009	1.0977	·13330	.90420	.07960	1.3512
i	5.0772	86	.73314	1.1012	·13546	.90734	.08102	1.3639
ı	5.0134	87	•72637	1.1027	·13704	.91036	.08340	1.3767
	4.9501	88	.71978	1.1054	13893	.91363	.08436	1.3893
1	4.8886	89	•71336	1.1079	·14078	.91696	.08530	1.4818
1	4.8216	90	•70710	1.1105	14279	92210	.08621	1.4142
		$\begin{vmatrix} 90 \\ 91 \end{vmatrix}$.70101	1.1132	14449	92352	.08716	1.4265
-	4.7694			1.1159	14449			
1	4.7117	92	•69508			.92476	:08798	1.4387
	4.6615	93	·68930	1.1186	•14817	.92914	·08932	1.4507
I	4.5999	94	*68366	1.1211	15009	93385	.09076	1.4627
1	4.5453	95	67817	1.1242	15211	•93746	.09197	1.4745
1	4.4845	96	•67282	1.1271	•15375	•94272	•09348	1.4863
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80		TABLE P	TS ac., or	A CINCIE.			
Chord div	Centre	Radius	Cir. Arc.	Area Seg.	Surface	Solidity	Chord
by height.	Angle v.	r = k c	b = k c.	$a = k a^2$.	$a = k c^2$.	$\mathbf{c} = k c^2$.	c = k r.
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4.4398	97	•66760	1.1300	·15600	•94470	.09442	1.4979
4.3859	98	•66250	1.1329	15801	•94852	.09567	1.5094
4.3383	99	.65754	1.1359	•15995	•95236	•09693	1.5208
4.2862	190	65270	1.1382	•16180	·95682	.09831	1.5321
4.2406	101	64798	1.1420	.16393	•96011	.09856	1.5432
4.1930	102		1.1451		.96412	10076	1.5543
	102	•64338		16610	.96568	10557	1.5652
4.1570		•63889	1.1483	16925		10273	
4.1006	104	•63450	1.1515	•17001	.97246	10273	1.5760
4.0555	105	•63023	1.15.47	•17204	•97643		1.5867
4.0113	106	•62607	1.1580	•17414	•98067	10601	1.5973
3.9679	107	•62200	1.1614	•17619	•98495	10735	1.6077
3.9252	108	•61803	1.1648	•17832	•98931	10870	1.6180
3.8832	109	•61416	1.1682	•18041	•99376	•11007	1.6282
3.8419	110	•61039	1.1716	•18257	•98827	•11149	1.6383
3.8013	111	•60670	1.1752	·18472	1.0028	11284	1.6482
3.7612	112	•60325	1.1790	·18696	1.0077	·11426	1.6581
3.7221	113	•59960	1.1823	•18900	1.0122	·11566	1.6677
3.6837	114	•59618	1.1859	•19117	1.0169	11709	1.6773
3.6454	115	•59284	1.1897	•19339	1.0218	·11853	1.6867
3.6086	116	•58959	1.1934	·19559	1.0266	·11995	1.6961
3.5712	117	•58641	1.1972	·19787	1.0317	12145	1.7053
3.5349	118	•58331	1.2011	.20009	1.0368	•12294	1.7143
3.4992	119	•58030	1.2050	.20227	1.0417	.12444	1.7232
3.4641	120	•57735	1.2089	.20453	1.0472	12596	1.7320
3.4296	121	.57450	1.2130	.20678	1.0525	12748	1.7407
3.3953	122	•57168	1.2177	•20945	1.0578	12903	1.7492
3.3616	123	•56895	1.2213	•21175	1.0634	13060	1.7576
3.3285	124	•56628	1.2253	•21399	1.0690	•13218	1.7659
3.2940	125	•56370	1.2295	•21538	1.0753	•13391	1.7740
3.2637	126	•56116	1.2338	•21859	1.0803	.13558	1.7820
3.2319	127	•55870	1.2381	•22121	1.0862	·13701	1.7898
3.2006	128	•55630	1.2425	•22370	1.0921	.13866	1.7976
3.1716	129	•55396	1.2470	•22617	1.0974	14028	1.8051
3.1393	130		1.2515	22865	1.1040	14202	1.8126
3.1093	131	•54947	1.2561	•23113	1.1104	14371	1.8199
3.0805	132	•54732	1.2607	•23372	1.1164	14537	1.8271
3.0555	133	•54522	1.2654	•23603	1.1212	14676	1.8341
3.0216	134	•54318	1.2701	23892	1.1295	•14894	1.8410
2.9777	135	•54120	1.2749	•24198	1.1420	•15209	1.8477
2.9651	136	•53927	1.2798	•24364	1.1428	15253	1.8543
2.9374	137	•53740	1.2847	•24676	1.1425	•15422	1.8608
2.9115	138	•53557	1.2897	·24938	1.1558	15605	1.8671
2.8829	139	•53380	1.2948	24933	1.1634	15807	1.8733
2.8562	139	•53209	1.2948	25485	1.1705	15996	
2·8302 2·8299			1	1	1.1703		1.8794
2.8299	141	•53042 •52881	1.3051	•25759		16201	1.8853
2.7781	142		1.3065	•25936	1.1851	16381	1.8910
	143	•52724	1.3157	•26320	1.1925	16577	1.8966
2.7527	144	•52573	1.3211	•26604	1.2000	•16776	1.9021
	1						
-				-			

			TABLE FO	R SEGMENT	s ac., or	A CIRCLE.		21
Ì	Chord div.	Centre	Radius	Cir. Arc.	Area Seg.	Surface	Solidity	Chord
1	by height.	Angle v.	r = k c.	b = k c.	$a = k c^2$.	$a = k c^2.$	$c = k c^2$	c = k r
ı	-							
ı		(- AN	/一个	6		MAN OF THE PARTY O	Malle	/
Ī	C. Jan	7			Continue Course			1
į			1	~~		1,00	•	1
K	2.7276	145	•52426	1.3265	•26889	1.2077	•16965	1.9074
	2.7002	146	•52284	1.3320	•27196	1.2166	17209	1.9126
	2.6816	. 147	•52147	1.3377	.27449	1.2219	17205	1.9176
	2.6533	148	•52015	1.3433	-27772	1.2318	17605	1.9225
	2.6301	149	•51887	1.3491	.28168	1.2396	17809	1.9272
	2.6064	150	•51764	1.3549	•28369	1.2476	18023	1.9318
	2.5830	151	•51645	1.3608	.28674	1.2563	18666	1.9363
	2.5598	152	•51530	1.3668	·28983	1.2648	18751	1.9406
	2.5239	153	•51420	1.3729	•29397	1.2801	18845	1.9447
	2.5143	154	•51315	1.3790	•29607	1.2824	·18913	1.9487
	2.4919	155	•51214	1.3852	•29928	1.2914	19147	1.9526
	2.4699	156	•51117	1.3919	•30259	1.3004	19374	1.9563
	2.4478	157	•51014	1.3973	•30560	1.3094	19607	1.9598
	2.4262	158	•50936	1.4043	•30905	1.3191	•20029	1.9632
	2.4047	159	•50851	1.4109	•31239	1.3287	20095	1.9663
	2.3835	160	•50771	1.4175	•31575	1.3368	•20342	1.9696
	2.3613	161	•50695	1.4243	•31931	1.3490	20609	1.9725
	2.3417	162	•50623	1.4311	•32263	1.3583	20847	1.9753
	2.3211	163	•50555	1.4380	•32618	1.3682	•21105	1.9780
	2.3004	164	•50491	1.4450	•32969	1.3791	•21371	1.9805
	2.2805	165	•50431	1.4520	•33327	1.3895	·21634	1.9829
	2.2605	166	•50374	1.4592	•33684	1.4021	•21904	1.9851
	2.2408	167	•50323	1.4665	•34048	1.4111	•22177	1.9871
	2.2212	168	•50275	1.4739	•34422	1.4222	· 2 1946	1.9890
	2.2013	169	•50231	1.4813	•34802	1.4344	•22766	1.9908
	2.1826	170	•50191	1.4889	•35230	1.4476	•23028	1.9924
	2.1636	171	•50154	1.4966	•35563	1.4565	•23266	1.9938
	2.1447	172	•50122	1.5044	•35953	1.4684	·23650	1.9951
	2.1271	173	•50093	1.5123	•36337	1.4797	·23900	1.9962
	2.1075	174	•50068	1.5202	•36747	1.4927	•24225	1.9972
	2.0892	175	•50047	1.5283	•37152	1.5052	•24537	1.9981
	2.0710	176	•50030	1.5365	•37562	1.5179	•24856	1.9988
	2.0530	177	•50017	1.5448	•37974	1.5308	·25179	1.9993
	2.0352	178	•50007	1.5533	•38401	1.5439	·25531	1.9996
	2.0175	179	•50002	1.5618	•38828	1.5573	•25840	1.9999
	2.0000	180	•50000	1.5707	•39269	1.5708	·26179	2.0000

To find the length of an arc of a circle.

RULE. Divide the chord of the arc by its height, and find the quotient in the first column. The corresponding number in the fourth column multiplied by the chord is the length of the arc.

To find the area of a segment of a circle,

RULE. Divide the chord of the segment by its height, and find the quotient in the first column. The corresponding number in the fifth column multiplied by the square of the chord, is the area of the segment.

32 TABLE OF EQUARES, OURES, EQUARE AND COME TOOLS.									
Number.	Squares.	Cubes.	√ Roots.	³ √ Roots.	Reciprocals.				
1	1	1	1.0000000 .	1.0000000	1.00000000				
2	4	8	1.4142136	1.2599210	•50000000 0				
3	9	27	1.7320508	1.4422496	•333333333				
4	16	64	2.0000000	1.5874011	•250000000				
5	25	125	2.2360680	1.7099759	•200000000				
6	36	216	2.4494897	1.8171206	•166666667				
7	49	343	2.6457513	1.9129312	•142857143				
8	64	512	2.8284271	2.0000000	•125000000				
9	81	729	3.0000000	2.0800837	•1111111111				
10	100	1000	3.1622777	2.1544347	•100000000				
11	121	1331	3.3166248	2.2239801	•090909091				
12	144	1728	3.4641016	2.2894286	•083333333				
13	169	2197	3.6055513	2.3513347	•076923077				
14	196	2744	3.7416574	2.4101422	.071428571				
15	225	3375	3.8729833	2.4662121	•066666667				
16	256	4096	4.0000000	2.5198421	•062500000				
17	289	4913	4.1231056	2.5712816	•058823529				
18	324	5832	4.2426407	2.6207414	•05555556				
19	361	6859	4.3588989	2.6684016	.052631579				
20	400	8000	4.4721360	2.7144177	•050000000				
21	441	9261	4.5825757	2.7589243	•047619048				
22	484	10648	4.6904158	2.8020393	•045454545				
23	529	12167	4.7958315	2.8438670	•043478261				
24	576	13824	4.8989795	2.8844991	•041666667				
25	625	15625	5.0000000	2.9240177	•040000000				
26	676	17576	5.0990195	2.9624960	.038461538				
27	729	19683	5.1961524	3.0000000	•037037037				
28	784	21952	5.2915026	3.0365889	•035714286				
29	841	24389	5.3851648	3.0723168	•034482759				
30	900 9 61	$27000 \\ 29791$	5.4772256	3.1072325	•033333333 •032258065				
31 32	1024	32768	5.5677644	3.1413806 3.1748021	•031250000				
33	1024	35937	5.6568542 5.7445626	3.2075343	•031230000				
34	1156	39304	5.8309519	3.2396118	•029411765				
35	$\begin{array}{c} 1130 \\ 1225 \end{array}$	42875	5.9160798	3.2710663	•028571429				
36	1223	46656	6.0000000	3.3019272	•027777778				
37	1369	50653	6.0827625	3.3322218	•027027027				
38	1444	54872	6.1644140	3.3619754	.026315789				
39	1521	59319	6. 2449980	3.3912114	.025641026				
40	1600	64000	6.3245553	3.4199519	.025000000				
41	1681	68921	6.4031242	3.4482172	.024390244				
42	1764	74088	6.4807407	3.4760266	023809524				
43	1849	79507	6.5574385	3.5033981	•023255814				
44	1936	85184	6.6332496	3.5303483	•022727273				
45	2025	91125	6.7082039	3.5568933	•02222222				
46	2116	97336	6.7823300	3.5830479	.021739130				
47	2209	103823	6.8556546	3.6088261	.021276600				
48	2304	110592	6.9282032	3.6342411	·020833333				
49	2401	117649	7.0000000	3.6593057	.020408163				
50	2500	125000	7·0710 6 78	3.6840314	•02000000 0				
51	2601	132651	7.1414284	3.7084298	•019607843				
52	2704	140608	7·21110 26	3.7325111	•019230769				

		or equints	o, Cubro, Square	AND COME ROOT	83
Number.	Squares.	Cubes.	√ Roots.	Noots.	Reciprocals.
53	2809	148877	7.2801099	3.7562858	018867925
54	2916	157464	7.3484692	3.7797631	018518519
55	3025	166375	7.4161985	3.8029525	.018181818
56	3136	175616	7.4833148	3.8258624	•017857143
57	3249	185193	7.5498344	3.8485011	•017543860
58	3364	195112	7.6157731	3.8708766	017241379
59	3481	205379	7.6811457	3.8929965	.016949153
60	3600	216000	7.7459667	3.9148676	.016666667
61	3721	226981	7.8102497	3.9304972	016393443
62	3844	238328	7.8740079	3.9578915	.016129032
63	3969	250047	7.9372539	3.9790571	015873016
64	4096	262144	8.0000000	4.0000000	.015625000
65	4225	274625	8.0622577	4.0207256	.015384615
66	4356	287496	8.1240384	4.0412401	.015151515
67	4489	300763	8.1853528	4.0615480	.014925373
68	4624	314432	8.2462113	4.0816551	014705882
69	4761	328509	8.3066239	4.1015661	014492754
70	4900	343000	8.3666003	4.1212853	014285714
71	5041	357911	8.4261498	4.1408178	•014084517
72	5184	373248	8.4852814	4.1601676	013888889
73	5329	389017	8.5440037	4.1793390	.013698630
74	5476	405224	8.6023253	4.1983364	.013513514
75	5 625	421875	8.6602540	4.2171633	•0133333333
76	5776	438976	8.7177979	4.2358236	·01315789 5
77	5929	456533	8.7749644	4.2543210	.012987013
78	6084	474552	8.8317609	4.2726586	·0128205 13
79	6241	493039	8.8881944	4.2908404	.012658228
80	6400	512000	8.9442719	4.3088695	.012500000
81	6561	531441	9.0000000	4.3267487	.012345679
82	6724	551368	9.0553851	4.3444815	.012195122
83	6889	571787	9.1104336	4.3620707	.012048193
84	7056	592704	9.1651514	4.3795191	.011904762
85	7225	614125	9.2195445	4.3968296	.011764706
86	7396	636056	9.2736185	4.4140049	•011627907
87	7569	658503	9.3273791	4.4310476	•011494253
88	7744	681472	9.3808315	4.4479692	•011363636
89	7921	704969	9.4339811	4.4647451	•011235955
90	8100	729000	9.4868330	4.4814047	•011111111
91	8281	753571	9.5393920	4.4979414	.010989011
92	8464	778688	9.5916630	4.5143574	•010869565
93	- 8649	804357	9.6436508	4.5306549	•010752688
94	8836	830584	9.6953597	4.5468359	·010638298
95	9025	857375	9.7467943	4.5629026	.010526316
96	9216	884736	9.7979590	4.5788570	•010416667
97	9409	912673	9.8488578	4.5947009	•010309278
98	9604	941192	9.8994949	4.6104363	.010204082
99	9801	970299	9.9498744	4.6260650	.010101010
100	10000	1000000	10.0000000	4.6415888	.010000000
101	10201	1030301	10.0498756	4.6570095	.009900990
102	10404	1061208	10.0995049	4.6723287	009803922
103	10609	1092727	10.1488916	4.6875482	•009708738
104	10816	1124864	10.1980390	4.7025694	•009615385

84	AADĻ	E OF DOURIE	bb, Cubbb, Section		
Number.	Squares.	Cubes.	√ Roots.	$\sqrt[3]{\text{Roots.}}$	Reciprocals.
105	11025	1157625	10.2469508	4.7176940	•009599810
106	11236	1191016	10.2956301	4.7326235	·00943396 2
107	11449	1225043	10.3440804	4.7474594	·00934579 4
108	11664	1259712	10.3923048	4.7622032	.009259259
109	11881	1295029	10.4403065	4.7768562	.009174312
110	12100	1331000	10.4880885	4.7914199	•009090909
111	12321	1367631	10.5356538	4.8058995	•009009009
112	12544	1404928	10.5830052	4.8202845	.008928571
113	12769	1442897	10.6301458	4.8345881	.008849558
114	12996	1481544	10.6770783	4.8488076	.008771930
115	13225	1520875	10.7238053	4.8629442	·008695652
116	13456	1560896	10.7703296	4.8769990	.008620690
117	13689	1601613	10.8166538	4.8909732	.008547009
118	13924	1643032	10.8627805	4.9048681	.008474576
119	14161	1685159	10.9087121	4.9186847	.008403361
120	14400	1728000	10.9544512	4.9324242	•008333333
121	14641	1771561	11.0000000	4.9460874	.008264463
122	14884	1815848	11.0453610	4.9596757	.008196721
123	15129	1860867	11.0905365	4.9731898	•008130081
124	15376	1906624	11.1355287	4.9866310	•008064516
125	15625	1953125	11.1803399	5.0000000	.008000000
126	15876	2000376	11.2249722	5.0132979	.007936508
127	16129	2048383	11-2694277	5.0265257	.007874016
128	16384	2097152	11.3137085	5.0396842	.007812500
129	16641	2146689	11.3578167	5.0527743	.007751938
130	16900	2197000	11.4017543	5.0657970	.007692308
131	17161	2248091	11.4455231	5.0787531	.007633588
132	17424	2299968	11.4891253	5.0916434	.007575758
133	17689	2352637	11.5325626	5.1044687	•007518797
134	17956	2406104	11.5758369	5.1172299	·007462687
135	18225	2460375	11.6189500	5.1299278	.007407407
136	18496	2515456	11.6619038	5.1425632	.007352941
137	18769	2571353	11.7046999	5.1551367	.007299270
138	19044	2628072	11.7473401	5.1676493	.007246377
139	19321	2685619	11.7898261	5.1801015	.007194245
140	19600	2744000	11.8321596	5.1924941	.007142857
141	19881	2803221	11.8743421	5.2048279	.007092199
142	20164	2863288	11.9163753	5.2171034	.007042254
143	20449	2924207	11.9582607	5.2293215	•006993007
144	20736	2985984	12.0000000	5.2414828	.006944444
145	21025	3048625	12.0415946	5.2535879	.006896552
146	21316	3112136	12.0830460	5.2656374	.006849315
147	21609	3176523	12.1243557	5.2776321	.006802721
148	21904	3241792	12.1655251	5.2895725	.006756757
149	22201	3307949	12.2065556	5.3014592	.006711409
150	22500	3375000	12.2474487	5.3132928	.006666667
151	22801	3442951	12.2882057	5.3250740	.006622517
152	23104	3511008	12.3288280	5.3368033	•006578947
153	23409	3581577	12.3693169	5.3484812	•006535948
154	23716	3652264	12.4096736	5.3601084	·00649350 6
155	24025	3723875	12.4498996	5.3716854	•006451613
156	24336	3796416	12·4899960	5.3832126	·00641 0256

ı	-	TABI.	L OF DEVANE	s, Cubes, Square	AND CODE 16001	80
l	Number.	Squares.	Cubes.	√ Roots.	³ √ Roots.	Reciprocals.
I	157	24649	38698 93	12.5299641	5.3946907	·006369427
i	158	24964	3944312	12.5698051	5.4061202	.006329114
	159	25281	4019679	12.6095202	5.4175015	.006289308
	160	25600	4096000	12.6491106	5.4288352	.006250000
	161	25921	4173281	12.6885775	5.4401218	.006211180
	162	26244	4251528	12.7279221	5.4513618	.006172840
	163	26569	4330747	12.7671453	5.4625556	.006134969
	164	26896	4410944	12.8062485	5.4737037	.006097561
	165	27225	4492125	12.8452326	5.4848066	.006060606
	166	27556	4574296	12.8840987	5.4958647	.006024096
	167	27889	4657463	12.9228480	5.5068784	.005988024
	168	28224	4741632	12.9614814	5.5178484	.005952381
	169	28561	4826809	13.0000000	5.5287748	.005917160
	170	28900	4913000	13.0384048	5.5396583	.005882353
	171	29241	5000211	13.0766968	5.5504991	.005847953
	172	29584	5088448	13.1148770	5.5612978	.005813953
	173	29929	5177717	13.1529464	5.5720546	.005780347
	174	30276	5268024	13.1909060	5.5827702	.005747126
	175	30625	5359375	13.2287566	5.5934447	.005714286
	176	30976	5451776	13.2664992	5.6040787	.005681818
	177	31329	5545233	13.3041347	5.6146724	.005649718
	178	31684	5639752	13.3416641	5.6252263	.005617978
	179	32041	5735339	13.3790882	5.6357408	.005586592
	180	32400	5832000	13.4164079	5.6462162	·00555556
	181	32761	5929741		5.6566528	.005524862
	1	33124	6028568	13.4536240		•005494505
	182	33489	6128487	13.4907376	5.6670511	•005464481
	183	33856	6229504	13.5277493	5.6774114	•005434783
	184	34225	6331625	13.5646600	$5.6877340 \ 5.6980192$	•005405405
	185	34596	6434856	13.6014705	5.7082675	•005376344
	186	34969	6539203	13.6381817		.005347594
	187	35344	6644672	13.6747943	5.7184791	.005319149
	188	35721	6751269	13.7113092	5·7286543 5·738793 6	•005291005
	189	36100	6859000	13.7477271		.005263158
	190	36481	6967871	13.7840488	5.7488971	•005235602
	191	36864	7077888	13.8202750	5.7589652 5.7689982	•005208333
	192	37249	7189517	$\begin{array}{c c} 13.8564065 \\ 13.8924400 \end{array}$	5·7789966	.005181347
	193	37636	7301384		5.7889604	•005154639
	194	38025	7414875	13.9283883	5.7988900	.005128205
	195		7529536	$\begin{array}{ c c c c c c c c c c c c c c c c c c c$	5.8087857	.005123233
	196	38416			5.8186479	.005076142
	197	38809	7645373	14.0356688	5.8284867	.005050505
	198	39204	7762392	14.0712473		.005025126
	199	39601	7880599	14.1067360	5.8382725 5.8480355	.005000000
	200	40000	8000000	14.1421356		.004975124
	201	40401	8120601	14.1774469	5.8577660	•004950495
	202	40804	8242408	14.2126704	5.8674673	.004930493
	203	41209	8365427	14.2478068	$\begin{bmatrix} 5.8771307 \\ 5.8867653 \end{bmatrix}$	•004901961
	204	41616	8489664	14.2828569	5.8963685	•004878049
	205	42025	8615125	14:3178211	5.9059406	•004854369
	206	42436	8741816	14.3527001	5.9154817	.004830918
	207	42849	8869743	14.4999051	5.9249921	·004807692
	208	43264	8998912	14.4222051	0.9249921	003001091

		Labi	L OF DQUART	-	COBLO, DQUAIN		
]	Number.	Squares	Cubes.		√Roots.	% Roots.	Reciprocals.
1	209	43681	9129329		14.4568323	5.9344721	.004784689
П	210	44100	9261000		14.4913767	5.9439220	.004761905
	211	44521	9393931		14.5258390	5.9533418	.004739336
	212	44944	9528128		14.5602198	5.9627320	.004716981
	213	45369	9663597		14.5945195	5.9720926	.004694836
	214	45796	9800344		14.6287388	5.9814240	.004672897
1	215	46225	9938375		14.6628783	5.9907264	.004651163
	216	46656	10077696		14.6969385	6.0000000	.004629630
	217	47089	10218313		14.7309199	6.0092450	.004608295
	218	47524	10360232		14.7648231	6.0184617	.004587156
	219	47961	10503459		14.7986486	6.0276502	.004566210
	220	48400	10648000		14.8323970	6.0368107	.004545455
	221	48841	10793861		14.8660687	6.0459435	.004524887
	222	49284	10941048		14.8996644	6.0550489	.004504505
	223	49729	11089567		14.9331845	6.0641270	.004484305
	224	50176	11239424		14.9666295	6.0731779	.004464286
	225	50625	11390625		15.0000000	6.0824020	.004444444
	226	51076	11543176		15.0332964	6.0991994	.004424779
	227	51529	11697083		15.0665192	6.1001702	.004405286
	228	51984	11852352		15.0996689	6.1091147	.004385965
	229	52441	12008989		15.1327460	6.1180332	.004366812
	230	52900	12167000		15.1657509	6.1269257	.004347826
	231	53361	12326391		15.1986842	6.1357924	.004329004
	232	53824	12487168		15.2315462	6.1446337	.064310345
	233	54289	12649337		15.2643375	6.1534495	.004291845
	234	54756	12812904		15.2970585	6.1622401	.004273504
	235	55225	12977875		15.3297097	6.1710058	•004255319
	236	55696	13144256		15.3622915	6.1797466	.004237288
	237	56169	13312053		15.3948043	6.1884628	004219409
	238	56644	13481272		15.4272486	6.1971544	.004201681
	239	57121	13651919		15.4596248	6.2058218	·004184100
	240	57600	13824000		15.4919334	6.2144650	·004166667
	241	58081	13997521		15.5241747	6.2230843	.004149378
	242	58564	14172488		15.5563492	6.2316797	.004132231
	243	59049	14348907		15.5884573	6.2402515	.004115226
	244	59536	14526784		15.6204994	6.2487998	.004098361
	245	60025	14706125		15.6524758	6.2573248	.004081633
	246	60516	14886936		15.6843871	6.2658266	.004065041
	247	61009	15069223		15.7162336	6.2743054	.004048583
П	248	61504	15252992		15.7480157	6.2827613	.004032258
ı	249	62001	15438249		15.7797338	6.2911946	.004016064
	250	62500	15625000		15.8113883	6.2996053	.004000000
	251	63001	15813251		15.8429795	6.3079935	.003984064
	252	63504	16003008		15.8745079	6.3163596	•003968254
	253	64009	16194277		15.9059737	6·3247035 6·3330256	•003952569
	254	$\begin{array}{c} 64516 \\ 65025 \end{array}$	$\begin{vmatrix} 16387064 \\ 16581375 \end{vmatrix}$		15·9373775 15·9687194	6.3413257	•003937008
	255 256	65536	$16581375 \\ 16777216$		16.0000000	$\begin{bmatrix} 6.3413257 \\ 6.3496042 \end{bmatrix}$	•003921569
	250 257	$\begin{array}{c} 65036 \\ 66049 \end{array}$	16974593		16.0312195	6.3578611	·003906250 ·003891051
	258	66564	17173512		16.0623784	6.3660968	•003891051
	259 259	67081	17373979		16.0934769	6.3743111	003875969
	260		17576000		16.1245155	6.3825043	·003846154
	200	01000.	11010000 }		10 12 10100	0 0023010	000040104

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Number.	Squares.	Cubes.	√ Roots.	³ √ Roots.	Reciprocals.
261	68121	17779581	16.1554944	6.3906765	·003831418
262	68644	17984728	16.1864141	6.3988279	.003816794
263	69169	18191447	16.2172747	6.4069585	.003802281
264	69696	18399744	16.2480768	6.4150687	.003787879
265	70225	18609625	16.2788206	6.4231583	.003773585
266	70756	18821096	16.3095064	6.4312276	.003759398
267	71289	19034163	16.3401346	6.4392767	.003745318
268	71824	19248832	16.3707055	6.4473057	.003731343
269	72361	19465109	16.4012195	6.4553148	.003717472
270	72900	19683000	16.4316767	6.4633041	.003703704
271	73441	19902511	16.4620776	6.4712736	.003690037
272	73984	20123643	16.4924225	6.4792236	.003676471
273	74529	20125045	16.5227116	6.4871541	.003663004
274	75076	20570824	16.5529454	6.4950653	.003649635
275	7.5625	20796875	16.5831240	6.5029572	.003636364
276	76176	21024576	16.6132477	6.5108300	003630304
277	76729	21253933	16.6433170	6.5186839	.003610108
278	77284	21484952	16.6783320	6.5265189	.003597122
279	77841	21717639	16.7032931	6.5343351	003584229
280	78400	21952000	16.7332005	6.5421326	003554220 003571429
281	78961	22188041	16.7630546	6.5499116	.003558719
282	79524	22425768	16.7928556	6.5576722	.003546099
283	80089	22665187	16.8226038	6.5654144	•003533569
284	80656	22906304	16.8522995	6.5731385	.003521127
285	81225	23149125	16.8819430	6.5808443	.003508772
286	81796	23393656	16.9115345	6.5885323	.003496503
287	82369	23639903	16.9410743	6.5962023	.003484321
288	82944	23887872	16.9705627	6:6038545	.003472222
289	83521	24137569	17.0000000	6.6114890	.003460208
290	84100	24389000	17.0293864	6.6191060	.003448276
291	84681	24642171	17.0587221	6.6267054	.003436426
292	85264	24897088	17.0880075	6.6342874	•003424658
293	85849	25153757	17.1172428	6.6418522	.003412969
294	86436	25412184	17.1464282	6.6493998	•003401361
295	87025	25672375	17.1755640	6.6569302	.003389831
296	87616	25934836	17.2046505	6.6644437	•003378378
297	88209	26198073	17.2336879	6.6719403	.003367003
298	88804	26463592	17.2626765	6.6794200	•003355705
299	89401	26730899	17.2916165	6.6868831	•00334448 2
300	90000	27000000	17.3205081	6.6943295	•003333333
301	90601	27270901	17.3493516	6.7017593	.003322259
302	91204	27543608	17.3781472	6.7091729	•003311258
303	91809	27818127	17.4068952	6.7165700	•003301330
304	92416	28094464	17.4355958	6.7239508	•003289474
305	93025	28372625	17.4642492	6.7313155	·00327868 9
306	93636	28652616	17.4928557	6.7386641	.003267974
307	94249	28934443	17.5214155	6.7459967	.003257329
308	94864	29218112	17.5499288	6.7533134	•003246753
309	95481	29503609	17.5783958	6.7606143	.003236246
310	96100	29791000	17.6068169	6.7678995	•003225806
311	96721	30080231	17.6351921	6.7751690	•003215434
312	97344	30371328	17.6635217	6.7824229	·00320512 8

88	LABLI	e of Square	S, CUBES, SQUARE	AND CUBE ROOT	8.
Number.	Squares.	Cubes.	√ Roots.	³ √ Roots.	Reciprocals.
313	97969	30664297	17.6918060	6.7896613	•003194888
314	98596	30959144	17.7200451	6.7968844	•003184713
1 315	99225	31255875	17.7482393	6.8040921	.003174603
316	99856	31554496	17.7763888	6.8112847	.003164557
317	100489	31855013	17.8044938	6.8184620	.003154574
318	101124	32137432	17.8325545	6.8256242	.003144654
319	101761	32461759	17.8605711	6.8327714	.003134796
320	102400	32768000	17.8885438	6.8399037	.003125000
321	103041	33076161	17.9164729	6.8470213	.003115265
322	103684	33386248	17.9443584	6.8541240	.003105590
323	104329	33698267	17.9722008	6.8612120	.003095975
324	104976	34012224	18.00000000	6.8682855	.003086420
325	105625	34328125	18.0277564	6.8753433	.003076923
326	106276	34645976	18.0554701	6.8823888	.003067485
327	106929	34965783	18.0831413	6.8894188	.003048104
328	107584	35287552	18.1107703	6.8964345	003048780
329	108241	35611289	18.1383571	6·903435 9	.003039514
330	108900	35937000	18.1659021	6.9104232	.003030303
331	109561	36264691	18.1934054	6.9173964	.003021148
$\frac{331}{332}$	110224	36594368	18.2208672	6.9243556	.003.012048
333	110224	36926037	18.2482876	6.9313088	•003003003
334	111556	37259704	18.2756669	6.9382321	.002994012
335	112225	37595375	18.3030052	6.9451496	•002985075
336	112896	37933056	18.3303028	6.9520533	.002976190
337	113569	38272753	18.3575598	6.9589434	•002967359
338	114244	38614472	18.3847763	6.9658198	•002958580
3 39	114921	38958219	18.4119526	6.9726826	•002949853
340	115600	39304000	18.4390889	6.9795321	.002941176
341	116281	39651821	18.4661853	6.9863681	•002932551
342	116964	40001688	18.4932420	6.9931906	•002923977
343	117649	40353607	18.5202592	7.0000000	.002915452
344	118336	40707584	18.5472370	7.0067962	•002906977
345	119025	41063625	18.5741756	7.0135791	.002898551
346	119716	41421736	18.6010752	7.0203490	•002890173
347	120409	41781923	18.6279360	7.0271058	•002881844
348	121104	42144192	18.6547581	7.0338497	·002873563
349	121801	42508549	18.6815417	7.0405860	.002865330
350	122500	42875000	18.7082869	7.0472987	.002857143
351	123201	43243551	18.7349940	7.0540041	.002849003
352	123904	43614208	18.7616630	7.0606967	.002840909
353	124609	43986977	18.7882942	7.0673767	•002832861
354	125316	44361864	18.8148877	7.0740440	.002824859
3 55	126025	44738875	18.8414437	7.0806988	•002816901
356	126736	45118016	18.8679623	7.0873411	•002808989
357	127449	45499293	18.8944436	7.0939709	.002801120
358	128164	45882712	18.9208879	7.1005885	.002793296
359	128881	46268279	18.9472953	7.1071937	•002785515
360	129600	46656000	18.9736660	7.1137866	.002777778
361	130321	47045831	19.0000000	7.1203674	.002770083
362	131044	47437928	19.0262976	7.1269360	•002762431
363	131769	47832147	19.0525589	7.1334925	•002754821
364	132496	48228544	19.0787840	7.1400370	•002747253

		-	1		09
Number.	Squares:	Cubes.	√ Roots.	Noots.	Reciprocals.
365	133225	48627125	19.1049732	7.1465695	•002739726
366	133956	49027896	19.1311265	7.1530901	.002732240
367	134689	49430863	19.1572441	7.1595988	.002724796
368	135424	49836032	19.1833261	7.1660957	.002717391
369	136161	50243409	19.2093727	7.1725809	.002710027
370	136900	50653000	19.2353841	7.1790544	•002702703
371	137641	51064811	19.2613603	7.1855162	.002695418
372	138384	51478848	19.2873015	7.1919663	.002688172
373	139129	51895117	19.3132079	7.1984050	•002680965
374	139876	52313624	19.3390796	$7 \cdot 2048322$	•002673797
375	140625	52734375	19.3649167	7.2112479	.002666667
376	141376	53157376	19.3907194	7.2176522	•002659574
377	142129	53582633	19.4164878	7.2240450	•002652520
378	142884	54010152	19.4422221	7.2304268	.002645503
379	143641	54439939	19.4679223	7.2367972	•002638521
380	144400	54872000	19.4935887	7.2431565	.002631579
381	145161	55306341	19.5192213	7.2495045	•002624672
382	145924	55742968	19.5448203	7.2558415	•002617801
383	146689	56181887	19.5703858	7.2621675	•002610966
384	147456	56623104	19.5959179	7.2684824	.002604167
385	148225	57066625	19.6214169	7.2747864	•002597403
386	148996	57512456	19.6468827	7.2810794	•002590674
387	149769	57960603	19.6723156	7.2873617	•002583979
388	150544	58411072	19.6977156	7.2936330	•002577320
389	151321	58863869	19.7230829	7.2998936	•002570694
390	152100	59319000	19.7484177	7.3061436	•002564103
391	152881	59776471	19.7737199	7.3123828	002557545 002551020
392	153664	60236288	19.7989899	7.3186114	•002531020
393	154449 155236	60698457	19.8242276	7·3248295 7·3310369	•002538071
394	156025	61162984	$\begin{array}{c c} 19.8494332 \\ 19.8746069 \end{array}$	7.3372339	•002531646
395	156816	$\begin{bmatrix} 61629875 \\ 62099136 \end{bmatrix}$	19.8997487	7.3434205	002531040 002525253
396	157609	62570773	19.9248588	7.3495966	•002518892
398	158404	63044792	19.9499373	7.3557624	•002512563
399	159201	63521199	19.9749844	7.3619178	•002506266
400	160000	64000000	20.0000000	7.3680630	•002500000
401	160801	64481201	20.0249844	7.3741979	.002493766
402	161604	64964808	20.0499377	7.3803227	.002487562
403	162409	65450827	20.0748599	7.3864373	•002481390
404	163216	65939264	20.0997512	7.3925418	•002475248
405	164025	66430125	20.1246118	7.3986363	•002469136
406	164836	66923416	20.1494417	7.4047206	•002463054
407	165649	67419143	20.1742410	7.4107950	•002457002
408	166464	67917312	20.1990099	7.4168595	·002450980
409	167281	68417929	20.2237484	7.4229142	•002444988
410	168100	68921000	20.2484567	7.4289589	•002439024
411	168921	69426531	20.2731349	7.4349938	•002433090
412	169744	69934528	20.2977831	7.4410189	•002427184
413	170569	70444997	20.3224014	7.4470343	•002421308
414	171396	70957944	20.3469899	7.4530399	•002415459
415	172225	71473375	20.3715488	7.4590359	•002409639 •002406846
416	173056	71991296	20.3960781	7.4650223	002400840

50		(1	1	1
Number.	Squares.	Cubes.	√ Roots.	Roots.	Reciprocals.
417	173889	72511713	20.4205779	7.4709991	•002398082
418	174724	73034632	20.4450483	7.4769664	•002392344
419	175561	73560059	20.4694895	7.4829242	.002386635
420	176400	74088000	20.4939015	7.4888724	•002380952
421	177241	74618461	20.5182845	7.4948113	.002375297
422	178084	75151448	20.5426386	7.5007406	.002369668
423	178929	75686967	20.5669638	7.5066607	.002364066
424	179776	76225024	20.5912603	7.5125715	.002358491
425	180625	76765625	20.6155281	7.5184730	.002352941
426	181476	77308776	20.6397674	7.5243652	.002347418
427	182329	77854483	20.6639783	7.5302482	·002341920
428	183184	78402752	20.6881609	7.5361221	.002336449
429	184041	78953589	20.7123152	7.5419867	.002331002
430	184900	79507000	20.7364414	7.5478423	.002325581
431	185761	80062991	20.7605395	7.5536888	.002320186
432	186624	80621568	20.7846097	7.5595263	•002314815
433	187489	81182737	20.8086520	7.5653548	.002309469
434	188356	81746504	20.8326667	7.5711743	.002304147
435	189225	82312875	20.8566536	7.5769849	.002298851
436	190096	82881856	20.8806130	7.5827865	.002293578
437	190969	83453453	20.9045450	7.5885793	.002288330
438	191844	84027672	20.9284495	7.5943633	.002283105
439	192721	84604519	20.9523268	7.6001385	.002277904
440	193600	85184000	20.9761770	7.6059049	.002272727
441	194481	85766121	21.0000000	7.6116626	.002267574
442	195364	86350888	21.0237960	7.6174116	.002262443
443	196249	86938307	21.0475652	7.6231519	.002257336
444	197136	87528384	21.0713075	7.6288837	·002252252
445	198025	88121125	21.0950231	7.6346067	.002247191
446	198916	88716536	21.1187121	7.6403213	.002242152
447	199809	89314623	21.1423745	7.6460272	*002237136
448	200704	89915392	21.1660105	7.6517247	.002232143
449	201601	90518849	21.1896201	7.6574138	.002227171
450	202500	91125000	21.2132034	7.6630943	*002222222
451	203401	91733851	21.2367606	7.6687665	.002217295
452	204304	92345408	21.2602916	7.6744303	.002212389
453	205209	92959677	21.2837967	7.6800857	.002207506
454	206116	93576664	21.3072758	7.6857328	.002202643
455	207025	94196375	21.3307290	7.6913717	0021 7802
456	207936	94818816	21.3541565	7.6970023	.002192982
457	$208849 \\ 209764$	95443993	21.3775583	7.7026246	.002188184
458 459	210681	96071912	21.4009346	7.7082388	*002183406
460	211600	96702579	21.4242853	7.7188448	.002178649
461	212521	97336000	21.4476106	7.7194426	.002173913
462	212321	97972181	21.4709106	7.7250325	.002169197
463	214369	$oxed{98611128}{99252847}$	21.4941853	7.7306141	002164502
464	2 14309 2 15296	99252847	21.5174348	7.7361877	.002159827
465	216225	100544625	21.5406592	7.7417532	.002155172
466	217156	$100544625 \\ 101194696$	21·5638587 21·5870331	7·7473109 7·7528606	.002150538
467	218089	101194696 101847563	21.6101828	7.7528606 7.7584023	•002145923
468	219024	$\frac{101847303}{102503232}$	21.6333077	7·7584023 7·7639361	002141328 002136752
100	A10 V24	102000202	21 0000011	1 1000001 1	002180792

-		- OI Deominio	CODES, DQUARIS	AND CUBE ROOTS	• 9:
Number.	Squares.	Cubes.	√Roots.	³ √ Roots.	Reciprocals.
469	219961	103161709	21.6564078	7.7694620	.002132196
470	220900	103823000	21.6794834	7.7749801	.002127660
471	221841	104487111	21.7025344	7.7804904	.002123142
472	222784	105154048	21.7255610	7.7859928	.002118644
473	223729	105828817	21.7485632	7.7914875	.002114165
474	224676	106496424	21.7715411	7.7969745	-002109705
475	225625	107171875	21.7944947	7.8024538	.002105263
. 478	226576	107850176	21.8174242	7.8079254	.002100840
477	227529	108531333	21.8403297	7.8133892	.002096436
478	228484	109215352	21.8632111	7.8188456	.002092050
479	229441	109902239	21.8860686	7.8242942	.002087683
480	230400	110592000	21.9089023	7.8297353	.002083333
481	231361	111284641	21.9317122	7.8351688	.002079002
482	232324	111980168	21.9544984	7.8405949	.002074689
483	233289	112678587	21.9772610	7.8460134	.002070393
484	234256	113379904	22.0000000	7.8514244	.002066116
485	235225	114084125	22.0227155	7.8568281	.002061856
486	236196	114791256	22.0454077	7.8622242	.002057613
487	237169	115501303	22.0680765	7.8676130	.002053388
488	238144	116214272	22.0907220	7.8729944	.002049180
489	239121	116930169	22.1133444	7.8783684	.002044990
490	240100	117649000	22.1359436	7.8837352	.002040816
491	241081	118370771	22.1585198	7.8890946	.002036660
492	242064	119095488	22.1810730	7.8944468	.002032520
493	243049	119823157	22.2036033	7.8997917	.002028398
494	244036	120553784	22.2261108	7.9051294	.002024291
495	245025	121287375	22.2485955	7.9104599	.002020202
496	246016	122023936	22.2710575	7.9157832	.002016129
497	247009	122763473	22.2934968	7.9210994	.002012072
498		123505992	22.3159136	7.9264085	.002008032
499	249001	124251499	22.3383079	7.9317104	.002004008
500	250000	125000000	22:3606798	7.9370053	.002000000
501	251001	125751501	22.3830293	7.9422931	.001996008
502		126506008	22.4053565	7.9475739	.001992032
503		127263527	22.4276615	7.9528477	.001988072
504		128024064	22.4499443	7.9581144	.001984127
505		128787625	22.4722051	7.9633743	.001980198
506		129554216	22.4944438	7.9686271	.001976285
507		130323843	22.5166605	7.9738731	.001972387
508		131096512	22.5388553	7.9791122	.001968504
509		131872229	22.5610283	7.9843444	.001964637
510		132651000	22.5831796	7.9895697	.001960784
511	- 1	133432831	22.6053091	7.9947883	.001956947
512		134217728	22.6274170	8.0000000	•001953125
513		135005697	22.6495033	8.0052049	.001949318
514		135796744	22.6715681	8.0104032	•001945525
515		136590875	22.6936114	8.0155946	•001941748
516		137388096	22.7156334	8.0207794	•001937984
517		138188413	22.7376341	8·0259574 8·0311287	•001934236
518		138991832	22·7596134 22·7815715	8.0362935	·001930502 ·001926782
519 520		$\frac{139798359}{140608000}$	22.7813713	8.0414515	·001923077
320 1	210400	140000000	44 0000000	0 0414010	001923011

92	* ADM	d of patients,	Colles, Decrite		
Number.	Squares.	Cubes.	√Roots.	Noots.	Reciprocals.
521	271441	141420761	22.8254244	8.0466030	•001919386
522	272484	142236648	22.8473193	8.0517479	.001915709
523	273529	143055667	22.8691933	8.0568862	.001912046
524	274576	143877824	22.8910463	8.0620180	.001908397
525	275625	144703125	22.9128785	8.0671432	.001904762
526	276676	145531576	22.9346899	8.0722620	.001901141
527	277729	146363183	22.9564806	8.0773743	.001897533
		140505153 147197952	22.9782506	8.0824800	001893939
528	278784		23.0000000	8.0875794	.001890359
529	279841	148035889	23.000000	8.0926723	$[\cdot \ 001886792]$
530	280900	148877001		8.0977589	001883239
531	281961	149721291	23.0434372		001879699
532	283024	150568768	23.0651252	8.1028390	001373033
533	284089	151419437	23.0867928	8.1079128	001870173
534	285156	152273304	23.1084400	8.1129803	001872039
535	286225	153130375	23.1300670	8.1180414	
536	287296	153990656	23.1516738	8.1230962	.001865672
537	288369	154854153	23.1732605	8.1281447	*001862197
538	289444	155720872	23.1948270	8.1331870	001858736
539	290521	156590819	23.2163735	8.1382230	*001855288
540	291600	157464000	23.2379001	8.1432529	001851852
541	292681	158340421	23.2594067	8.1482765	001848429
542	293764	159220088	23.2808935	8.1532939	001845018
543	294849	160103007	23.3023604	8.1583051	.001841621
544	295936	160989184	23.3238076	8.1633102	*001838235
545	297025	161878625	23.3452351	8.1683092	001834862
546	298116	162771336	23.3666429	8.1733020	.001831502
547	299209	163667323	23.3880311	8.1782888	.001828154
548	300304	164566592	23.4093998	8.1832695	.001824818
549	301401	165469149	23.4307490	8.1882441	.001821494
550	302500	166375000	23.4520788	8.1932127	.001818182
551	303601	167284151	23.4733892	8.1981753	• •001814882
552	304704	168196608	23.4946802	8.2031319	•001811594
553	305809	169112377	23.5159520	8.2080825	.001808318
554	306916	170031464	23.5372046	8.2130271	.001805054
555	308025	170953875	23.5584380	8.2179657	.001801802
556	309136	171879616	23.5796522	8.2228985	.001798561
557	310249	172808693	23.6008474	8.2278254	.001795332
558	311364	173741112	23.6220236	8.2327463	.001792115
559	312481	174676879	23.6431808	8.2376614	.001788909
560	313600	175616000	23.6643191	8.2425706	.001785714
561	314721	176558481	23.6854386	8.2474740	•001782531
562	315844	177504328	23.7065392	8.2523715	•001779359
563	316969	178453547	23.7276210	8.2572635	.001776199
564	318096	179406144	23.7486842	8.2621492	.001773050
565	319225	180362125	23.7697286	8.2670294	.001769912
566	320356	181321496	23.7907545	8.2719039	.001766784
567	321489	182284263	23.8117618	8.2767726	.001763668
568	322624	183250432	23.8327506	8.2816255	.001760563
569	323761	184220009	23.8537209	8.2864928	•001757469
570	324900	185193000	23.8746728	8.2913444	.001754386
571	326041	186169411	23.8956063	8.2961903	•001751313
572	327184	187149248	23.9165215	8.3010304	·00174825 2
k.					

į		LADI	E OF DQUARES	, CUBES, SQUARE	AND CUBE ROOT	8. 93
	Number.	Squares.	Cubes.	√ Roots.	³ √ Roots.	Reciprocals.
-	573	328329	188132517	23.9374184	8.3058651	•001745201
	574	329476	189119224	23.9582971	8.3106941	.001742160
	575	330625	190109375	23.9791576	8.3155175	.001739130
	576	331776	191102976	24.0000000	8.3203353	.001736111
	577	332927	192100033	24.0208243	8.3251475	.001733102
	578	334084	193100552	24.0416306	8.3299542	.001730104
	579	335241	194104539	24.0624188	8.3347553	.001727116
	580	336400	195112000	24.0831891	8.3395509	.001724138
	581	337561	196122941	24.1039416	8.3443410	.001721170
	582	338724	197137368	24.1246762	8.3491256	.001718213
	583	339889	198155287	24.1453929	8.3539047	.001715266
	5 84	341056	199176704	24.1660919	8.3586784	.001712329
	5 8 5	342225	200201625	24.1867732	8.3634466	.001709402
	586	343396	201230056	24.2074369	8.3682095	.001706485
	587	344569	202262003	24.2280829	8.3729668	.001703578
	588	345744	203297472	24.2487113	8.3777188	.001700680
	589	346921	204336469	$24 \cdot 2693222$	8.3824653	.001697793
	590	348100	205379000	24.2899156	8.3872065	.001694915
	591	349281	206425071	24.3104996	8.3919428	.001692047
	592	350464	207474688	24.3310501	8.3966729	.001689189
	593	351649	208527857	24.3515913	8.4013981	.001686341
	594	352836	209584584	24:3721152	8.4061180	.001683502
	595	354025	210644875	24.3926218	8.4108326	.001680672
	596	355216	211708736	24.4131112	8.4155419	•001677852
i	597	356409	212776173	24.4335834	8.4202460	.001675042
I	598	357604	213847192	24.4540385	8.4249448	.001672241
i	599	358801	214921799	24.4744765	8.4296383	.001669449
i	600	360000	216000000	24.4948974	8.4343267	•001666667
ŀ	601	361201	217081801	24.5153013	8.4390098	.001663894
ı	602	362404	218167208	24.5356883	8.4436877	•001661130
ı	603	363609	219256227	24.5560583	8.4483605	•001658375
Į	604	364816	220348864	24.5764115	8.4530281	•001655629
	605	366025	221445125	24.5967478	8.4576906	•001652893
	606	367236	222545016	24.6170673	8.4623479	.001650165
	607	368449	223648543	24.6373700	8.4670001	.001647446
	608	369664	224755712	24.6576560	8.4716471	.001644737
	609	370881	225866529	24.6779254	8.4762892	.001642036
	610	372100	226981000	24.6981781	8.4809261	•001639344
	611	373321	228099131	24.7184142	8.4855579	•001636661
	612	374544	229220928	24.7386338	8.4901848	.001633987
	613	375769	230346397	24.7588368	8.4948065	.001631321
i	614	376996	231475544	24.7790234	8.4994233	.001628664
ł	615	378225	232608375	24.7991935	8.5040350	.001626016
Ì	616	379456	233744896	24.8193473	8.5086417	•001623377
	617	380689	234885113	24.8394847	8.5132435	*001620746
1	618	381924	236029032	24.8596058	8·5178403 8·5224331	•001618123
- Aller	619	383161	237176659	24.8797106	8.5270189	•001615509
-	620	384400	238328000	24·8997992 24·9198716	8.5316009	.001612903
-	621	385641	239483061	24.9399278	8.5361780	·001610306 ·001607717
1	622	386884	240641848 241894367	24.9399278 24.9599679	8.5407501	·001607717
	623	388129	241894367 242970624	24.9599979	8.5453173	001602564
1	624	2022101	242910024	24 010002U	0 0100110 1	001002004
1						

94	LABLE	OF DUDANTE,	CUBES, DQUARA	1110 0000 10001	oi.
Number.	Squares.	Cubes.	√ Roots.	Noots.	Reciprocals.
625	390625	244140625	25.0000000	8.5498797	.001600000
626	391876	245134376	25.0199920	8.5544372	.001597444
627	393129	246491883	25.0399681	8.5589899	•001594896
628	394384	247673152	25.0599282	8.5635377	.001592357
629	395641	248858189	25.0798724	8.5680807	•001589825
630	396900	250047000	25.0998008	8.5726189	.001587302
631	398161	251239591	25.1197134	8.5771523	.001584786
632	399424	252435968	25.1396102	8.5816809	.001582278
633	400689	253636137	25.1594913	8.5862247	•001579779
634	401956	254840104	25.1793566	8.5907238	.001577287
635	403225	256047875	25.1992063	8.5952380	•001574803
636	404496	257259456	25.2190404	8.5997476	.001572327
637	405769	258474853	25.2388589	8.6042525	.001569859
638	407044	259694072	25.2586619	8.6087526	.001567398
639	408321	260917119	25.2784493	8.6132480	.001564945
640	409600	262144000	25.2982213	8.6177388	.001562500
641	410881	263374721	25.3179778	8.6222248	.001560062
642	412164	264609288	25.3377189	8.6267063	.001557632
643	413449	265847707	25.3574447	8.6311830	.001555210
644	414736	267089984	25.3771551	8.6356551	.001552795
645	416025	268336125	25.3968502	S·6401226	.001550388
646	417316	269585136	25.416.5302	8.6445855	.001547988
647	418609	270840023	25.4361947	8.6490437	.001545595
648	419904	272097792	25.4558441	8.6534974	.001543210
649	421201	273359449	25.4754784	8.6579465	.001540832
650	422500	274625000	25.4950976	8.6623911	.001538462
651	423801	275894451	25.5147013	8.6668310	.001536098
652	425104	277167808	25.5342907	8.6712665	*001533742
653	426409	278445077	25.5538647	8.6756974	.001531394
654	427716	279726264	25.5734237	8.6801237	.001529052
655	429025	281011375	25.5929678	8.6845456	.001526718
656	430336	282300416	25.6124969	8.6889630	*001524390
657	431649	283593393	25.6320112	8.6933759	.001522070
658	432964	284890312	25.6515107	8.6977843	•001519757
659	434281	286191179	25.6709953	8.7021882	•001517451
660	435600	287496000	25.6904652	8.7065877	.001515152
661	436921	288804781	25.7099203	8.7109827	.001512859
662	438244	290117528	25.7293607	8.7153734	.001510574
663	439569	291434247	25.7487864	8.7197596	.001508296
664	440896	292754944	25.7681975	8.7241414	.001506024
665	442225	294079625	25.7875939	8.7285187	.001503759
666	443556	295408296	25.8069758	8.7328918	.001501502
667	444889	296740963	25.8263431	8.7372604	.001499250
668	446224	298077632	25.8456960	8.7416246	.001497006
669	447561	299418309	25.8650343	8.7459846	.001494768
670.	448900	300763000	25.8843582	8.7503401	*001492537
671	450241	302111711	25.9036677	8.7546913	001490313
673	451584 452929	303464448 304821217	25.9229628	8.7590383	.001488095
674	452929	304821217	25.9422435 25.9615100	8.7633809	.001485884
675	454270	307546875	25.9807621	8.7677192	·001483680 ·001481481
676		308915776		8·7720532 8·7763830	·001451451
010	1 100010	300010110	20 0000000	, 0,,,00000	001479290

			Centro, Recard		95
Number.	Squares.	Cubes.	√ Roots.	Noots.	Reciprocals.
677	458329	310288733	26.0192237	8.7807084	.001477105
678	459684	311665752	26.0384331	8.7850296	.001474926
679	461041	313046839	26.0576284	8.7893466	.001472754
680	462400	314432000	26.0768096	8.7936593	·001470588
681	463761	315821241	26.0959767	8.7979679	•001468429
682	465124	317214568	26.1151297	8.8022721	·00146627 6
683	466489	318611987	26.1342687	8.8065722	.001464129
684	467856	320013504	26.1533937	8.8108681	001461988
685	469225	321419125	26.1725047	8.8151598	.001451353
686	470596	322828856	26.1916017	8.8194474	·00145772 6
687	471969	324242703	26.2106848	8.8237307	.001457720
688	471909	325660672	26.2297541	8.8280099	•001453604
689		327082769	26.2488095	8.8322850	
690	474721 476100	328509000	26.2678511	8.8365559	·0014513 79 ·00144927 5
691		329939371	26.2868789	8.8408227	
692	477481		26.3058929	8.8450854	.001447178
ž	478864	331373888		8.8493440	.001445087
693	480249	332812557	26.3248932		.001443001
694	481636	334255384	26.3438797	8.8535985	.001440922
695	483025	335702375	26.3628527	8.8578489	.001438849
696	484416	337153536	26.3818119	8.8620952	.001436782
697	485809	338608873	26.4007576	8.8663375	•001434720
698	487204	340068392	26.4196896	8.8705757	•001432665
699	488601	341532099	26.4386081	8.8748099	•001430615
700	490000	343000000	26.4575131	8.8790400	•001428571
701	491401	344472101	26.4764046	8.8832661	.001426534
702	492804	345948408	26.4952826	8.8874882	001424501
703	494209	347428927	26·5141472 26·5329983	8·8917063 8·8959204	001422475 001420455
704	$\begin{vmatrix} 495616 \\ 497025 \end{vmatrix}$	348913664 350402625	26.5518361	8.9001304	·001420433 ·001418440
706	498436	351895816	26.5706605	8.9043366	•001416431
707	499849	353393243	26.5894716	8.9085387	.001410431
708	501264	354894912	26.6082694	8.9127369	.001412429
709	502681	356400829	26.6270539	8.9169311	001412423
710	504100	357911000	26.6458252	8.9211214	•001410451
711	505521	359425431	26.6645833	8.9253078	.001406470
712	506944	360944128	26.6833281	8.9294902	.001404494
713	508369			8.9336687	.001402525
714	509796		26.7207784	8.9378433	.001400560
715.	511225		26.7394839	8.9420140	.001398601
716	512656	1	26.7581763	8.9461809	.001396648
717	514089		26.7768557	8.9503438	.001394700
718	515524		26.7955220	8.9545029	.001392758
719	516961	371694959	26.8141754	8.9586581	.001390821
720	518400	373248000	26.8328157	8.9628095	•001388889
721	519841	374805361	26.8514432	8.9669570	.001386963
722	521284			8.9711007	.001385042
723	522729	377933067	26.8886593	8.9752406	.001383126
724	524176	379503424	26.9072481	8.9793766	.0013812!5
725	525625	381078125	26.9258240	8.9835089	.001379310
726	527076	382657176	26.944:1872	8.9876373	.001377410
727	528529	384240583	26.9629375	8.9917620	•001375516
728		385828352		8.9958899	. 001373626

48	I ADD.	E OF DOUBLESS	, COBES, ECONICE		
Number.	Squares.	Cubes.	√ Roots.	Noots.	Reciprocals.
729	531441	387420489	27.0000000	9.0000000	001371742
730	532900	389017000	27.0185122	9.0041134	•001369863
731	534361	390617891	27.0370117	9.0082229	.001367989
732	535824	392223168	27.0554985	9.0123288	.001366120
733	537289	393832837	27.0739727	9.0164309	•001364256
734	538756	395446904	27.0924344	9.0205293	.001362398
735	540225	397065375	27.1108834	9.0246239	.001360544
736	541696	398688256	27.1293199	9.0287149	•001358696
737	543169	400315553	27.1477149	9.0328021	.001356852
738	544644	401947272	27.1661554	9.0368857	.001355014
739	546121	403583419	27.1845544	9.0409655	.001353180
740	547600	405224000	27.2029140	9.0450419	·0013513 51
741	549081	406869021	$27 \cdot 2213152$	9.0491142	.001349528
742	550564	408518488	27.2396769	9.0531831	.001347709
743	552049	410172407	27.2580263	9.0572482	.001345895
744	553536	411830784	27.2763634	9 0613098	.001344086
745	555025	413493625	27.2946881	9.0653677	•001342282
746	556516	415160936	27.3130006	9.0694220	.001340483
747	558009	416832723	27:3313007	9.0734726	•001338688
748	559504	41.8508992	27.3495887	9.0775197	.001336898
749	561001	420189749	27.3678644	9.0815631	•001335113
750	562500	421875000	27.3861279	9.0856030	•001333333
751	564001	423564751	27.4043792	9.0896352	•001331558
752	565504	425259008	2 7·4226184	9.0936719	.001329787
753	567009	426957777	27.4408455	9.0977010	.001328021
754	568516	428661064	27.4590604	9.1017265	•001326260
755	570025	430368875	27.4772633	9.1057485	$ \cdot 001324503 $
756	571536	432081216	27.4954542	9.1097669	.001322751
757	573049	433798093	27.5136330	9.1137818	•001321004
758	574564	435519512	27.5317998	9.1177931	.001319261
759	576081	437245479	27.5499546	9.1218010	.001317523
760	577600	438976000	27.5680975	9.1258053	•001315789
761	579121	440711081	27.5862284	9.1298061	•001314060
762	580644	442450728	27.6043475	9.1338034	.001312336
763	582169		27.6224546	9.1377971	•001310616
764	583696	445943744	27.6405499	9.1417874	.001308901
765	585225	447697125	27.6586334	9.1457742	•001307190
766	586756	449455096	27.6767050	9.1497576	.001305483
767	588289	451217663	27.6947648	9.1537375	.001303781
768 769	589824)	27.7128129	9.1577139	.001302083
770	591361	454756609	27.7308492	9.1616869	•001300390
771	592900 594441	456533000 458314011	27·7488739 27·7668868	9.1656565 9.1696225	$001298701 \ 001297017$
772	595984	460099648	27.7848880	9.1735852	001297017
773	597529	461889917	27.8028775	9.1753852 9.1775445	001293557
774	599076	463684824	27·8208555	9.1815003	001293001 001291990
775	600625	465484375	27.8388218	9.1854527	·001291990 ·001290323
776	602176	467288576	27.8567766	9.1894018	.001288660
777	603729	469097433	27.8747197	9.1933474	001287001
778	605284		27.8926514	9.1972897	001287001
779	606841	472729139	27.9105715	9.2012286	001283697
780	608400		27.9284801	9.2051641	001282051

			- Cobib, Devine		5. 97
Number.	Squares.	Cubes.	√ Roots.	Noots.	Reciprocals.
781	609961	476379541	27.9463772	9.2090962	.001280410
782	611524	478211768	27.9642629	9.2130250	.001278772
783	613089	480048687	27.9821372	9.2169505	.001277139
784	614656	481890304	28.0000000	9.2208726	.001275510
785	616225	483736625	28.0178515	9.2247914	.001273885
786	617796	485587656	28.0356915	9.2287068	001272265
787	619369	487443403	28.0535203	9.2326189	.001270648
788	620944	489303872	28.0713377	9.2365277	.001269036
789	622521	491169069	28.0891438	9.2404333	.001267427
790	624100	493039000	28.1069386	9.2443355	.001265823
791	625681	494913671	28.1247222	9.2482344	001264223
792	627264	496793088	28.1424946	9.2521300	.001262626
793	628849	498677257	28.1602557	9.2560224	.001261034
794	630436	500566184	28.1780056	9.2599114	.001251034
795	632025	502459875	28.1957444	9.2637973	001253440
796	633616	504358336	28.2134720	9.2676798	001257802
797	635209		28.2311884	9.2715592	001253201
798	636804	508169592	28.2488938	9.2754352	•001253133
799	638401	510082399	28.2665881	9.2793081	•001251564
800	640000	512000000	28.2842712	9.2831777	•001251304
801	641601	513922401	28.3019434	9.2870444	001230000
802	643204	515849608	28.3196045	9.2909072	001246433
803	644809	517781627	28.3372546	9.2947671	00124033
804	646416	519718464	28.3548938	9.2986239	001243330
805	648025	521660125	28.3725219	9.3024775	•001243781
806	649636	523606616	28.3901391	9.3063278	.001242230
807	651249	525557943	28.4077454	9.3101750	•001239157
808	652864	527514112	28.4253408	9.3140190	•001233131
809	654481	529475129	28.4429253	9.3178599	.001237024
810	656100	531441000	28.4604989	9.3216975	.001234568
811	657721	533411731	28.4780617	9.3255320	.001233046
812	659344	535387328	28.4956137	9.3293634	.001231527
813	660969	537367797	28.5131549	9.3331916	.001230012
814	662596	539353144	28.5306852	9.3370167	.001228501
815	664225	541343375	28.5482048	9.3408386	.001226994
816	665856	543338496	28.5657137	9.3446575	.001225499
817	667489	545338513	28.5832119	9.3484731	.001223990
818	669124	547343432	28.6006993	9.3522857	.001222494
819	670761	549353259	28.6181760	9.3560952	.001221001
820	672400	551368000	28.6356421	9.3599016	.001219512
821	674041	553387661	28.6530976	9.3637049	.001218027
822	675684	555412248	28.6705424	9.3675051	.001216545
823	677329	557441767	28.6879716	9.3713022	.001215067
824	678976	559476224	28.7054002	9.3750963	.001213592
825	680625	561515625	28.7228132	9.3788873	.001212121
826	682276	563559976	28.7402157	9.3826752	.001210654
827	683929	565609283	28.7576077	9.3864600	.001209190
828	685584	567663552	28.7749891	9.3902419	.001207729
829	687241	569722789	28.7923601	9.3940206	.001206273
830	688900	571787000	28.8097206	9.3977964	.001204819
831	690561	573856191	28.8270706	9.4015691	•001203369
832	692224	575930368	28.8444102	9.4053387	.001201923

90	3.2702		CODES, Decimen		
Number.	Squares.	Cubes.	√Roots.	³ √ Roots.	Reciprocals
833	693889	578009537	28.8617394	9.4091054	.001200480
834	695556	580093704	28.8790582	9.4128690	•001199041
835	697225	582182875	28.8963666	9.4166297	•001197605
836	698896	584277056	28.9136646	9.4203873	•001196172
837	700569	586376253	28.9309523	9.4241420	.001194743
838	702244	588480472	28.9482297	9.4278936	.001193317
839	703921	590589719	28.9654967	9.4316423	.001191895
840	705600	592704000	28.9827535	9.4353800	.001190476
841	707281	594823321	29.0000000	9.4391307	•001189061
842	708964	596947688	29.0172363	9.4428704	.001187648
843	710649	599077107	29.0344623	9.4466072	.001186240
844	712336	601211584	29.0516781	9.4503410	•001184834
845	714025	603351125	29.0688837	9.4540719	.001183432
846	715716	605495736	29.0860791	9.4577999	.001182033
847	717409	607645423	29.1032644	9.4615249	•001180638
848	719104	609800192	29.1204396	9.4652470	.001179245
849	720801	611960049	29.1376046	9.4689661	.001177856
850	722500	614125000	29.1547595	9.4726824	.001176471
851	724201	616295051	29.1719043	9.4763957	.001175088
852	725904	618470208	29.1890390	9.4801061	.001173709
853	727609	620650477	29.2061637	9.4838136	•001172333
854	729316	622835864	29.2232784	9.4875182	.001170960
855	731025	625026375	29.2403830	9.4912200	.001169591
856	732736	627222016	29.2574777	9.4949188	.001168224
857	734449	629422793	29.2745623	9.4986147	•001166861
858	736164	631628712	29.2916370	9.5023078	.001165501
859	737881	633839779	29.3087018	9.5059980	.001164144
860	739600	636056000	29.3257566	9.5096854	.001162791
861	741321	638277381	29.3428015	9.5133699	•001161440
862	743044	640503928	29.3598365	9.5170515	•001160093
863	744769	642735647	29.3768616	9.5207303	•001158749
864	746496	644972544	29.3938769	9.5244063	•001157407
865	748225	647214625	29.4108823	9.5280794	•001156069
866	749956	649461896	29.4278779	9.5317497	•001154734
867	751689	651714363	29.4448637	9.5354172	•001153403
868	753424	653972032	29.4618397	9.5390818	•001152074
869	755161	656234909	29.4788059	9.5427437	•001150748
870	756900	658503000	29.4957624	9.5464027	•001149425
871	758641	660776311	29.5127091	9.5500589	•001148106
872	760384	663054848	29.5296461	9.5537123	•001146789
873	762129	665338617	29.5465734	9.5573630	001145475
874	763876	667627624	29.5634910	9.5610108	•001144165
875	765625	669921875	29.5803989	9.5646559	.001142857
876	767376	672221376	29.5972972	9.5682782	•001141553
877	769129	674526133	29.6141858	9.5719377	•001140251
878	770884	676836152	29.6310648	9.5755745	•001138952
879	772641	679151439	29.6179342	9.5792085	.001137656
880	774400	681472000	29.6647939	9.5828397	.001136364
881	776161	683797841	29.6816442	9.5864682	.001135074
882	777924	686128968	29.6984848	9.5900937	.001133787
883	779689	688465387	29.7153159	9.5937169	•001132503
884	1 781490	690807104	29.7321375	9.5973373	001131222
1					

		or Decanas	, COBES, SQUARE	AND CUBE ROUT	8. 99
Number.	Squares.	Cubes.	✓ Roots.	³ √ Roots.	Reciprocals.
885	783225	693154125	29.7489496	9.6009548	.001129944
886	784996	695506456	29.7657521	9.6045696	.001128668
887	786769	697864103	29.7825452	9.6081817	.001127396
888	788544	700227072	29.7993289	9.6117911	.001126126
889	790321	702595369	29.8161030	9.6153977	.001124859
896	792100	704969000	29.8328678	9.6190017	.001123596
891	793881	707347971	29.8496231	9.6226030	.001122334
892	795664	707932288	29.8663690	9.6262016	.001121076
893	797449	712121957	29.8831056	9.6297975	.001119821
894	799236	714516984	29.8998328	9.6333907	.001118568
895	801025	716917375	29.9165506	9.6369812	.001117818
896	802816	719323136	29.9332591	9.6405690	.001116071
897	804609	721734273	29.9499583	9.6441542	.001114827
898	806404	724150792	29.9666481	9.6477367	.001113586
899	808201	726572699	29.9833287	9.6513166	.001112347
900	810000	729000000	30.0000000	9.6548938	.001111111
901	811801	731432701	30.0166621	9.6584684	.001109878
902	813604	733870808	30.0333148	9.6620403	.001108647
903	815409	736314327	30.0499584	9.6656096	.001107420
904	817216	738763264	30.0665928	9.6691762	.001106195
905	819025	741217625	30.0832179	9.6727403	.001104972
906	820836	743677416	30.0998339	9.6763017	.001103753
907	822649	746142643	30.1164407	9.6798604	.001102536
908	824464	748613312	20.1330383	9.6834166	.001101322
909	826281	751089429	30.1496269	9.6869701	.001100110
910	828100	753571000	30.1662063	9.6905211	.001098901
911	829921	756058031	30.1827765	9.6940694	.001097695
912	831744	758550828	30.1993377	9.6976151	.001096491/
913	833569	761048497	30.2158899	9.7011583	•001095290
914	835396	763551944	30.2324329	9.7046989	.001094092
915	837225	766060875	30.2489669	9.7082369	.001092896
916	839056	768575296	30.2654919	9.7117723	.001091703
917	840889	771095213	30.2820079	9.7153051	•001090513
918	842724	773620632	30.2985148	9.7188354	•001089325
919	844561	776151559	30.3150128	9.7223631	•001088139
920	846400	778688000	30.3315018	9.7258883	•001086957
921	848241	781229961	30.3479818	9.7294109	•001085776
922	850084	783777448	30.3644529	9.7329309	•001084599
923	851929	786330467	30.3809151	9.7364484	•001083423
924	853776	788889024	30.3973683	9.7399634	.001082251
925	855625	791453125	30.4138127	9.7434758	•001081081
926	857476	794022776	30.4302481	9.7469857	.001079914
927	859329	796597983	30.4466747	9.7504930	.001078749
928	861184	799178752	30.4630924	9.7539979	•001077586
929	863041	801765089	30.4795013	9.7575002	.001076426
930	864900	804357000	30.4959014	9.7610001	.001075269
931	866761	806954491	30.5122926	9.7644974	.001074114
932	868624	809557568	30.5286750	9.7679922	.001072961
933	870489	812166237	30.5450487	9.7714845	•001071811
934	872356	814780504	30.5614136	9.7749743	•001070664
935	874225	817400375	30.5777697	9.7784616	.001069519
936	1876096	820025856	30.5941171	9.7819466	-001068376

100			Ochic, Diconius		
Number.	Squares.	Cubes.	√ Roots.	Noots.	Reciprocals.
937	877969	\$22656953	30.6104557	9.7854288	·001067236
938	379844	825293672	30.6267857	9.7889087	·001066098
939	881721	827936019	30.6431069	9.7923861	.001064963
940	883600	830584000		9.7958611	.001063830
941	885481	833237621		9.7993336	.001062699
942	887364	835896888	30.6920185	9.8028036	.001061571
943		838561807		9.8062711	.001060445
944	889249 891136	841232384	30.7245830	9.8097362	.001059322
945		843908625	30.7408523	9.8131989	001058201
946	893025	846590536	30.7571130	9.8166591	•001057082
947	894916	849278123		9.8201169	.001055966
	896809		30.7733651	9.8235723	001053500
948	898704	851971392	30.7896086	9.8270252	·001053741
949	900601	854670349	30.8058436		
950	902500	857375000	30.8220700	9.8304757	001052632 001051525
951	904401	860085351	30.8382879	9.8339238	
952	906304	862801408	30.8544972	9.8373695	•001050420
953	908209	865523177	30.8706981	9.8408127	.001049318
954	910116	868250664	30.8868904	9.8442536	•001048218
955	912025	870983875	30.9030743	9.8476920	.001047120
956	913936	873722816	30.9192477	9.8511280	•001046025
957	915849	876467493	30.9354166	9.8545617	.001044932
958	917764	879217912	30.9515751	9.8579929	.001043841
959	919681	881974079	30.9677251	9.8614218	.001042753
960	921600	884736000	30.9838668	9.8648483	•001041667
961	923521	887503681	31.0000000	9.8682724	•001040583
962	925444	890277128	31.0161248	9.8716941	•001039501
963	927369	893056347	31.0322413	9.8751135	.001038422
964	929296	895841344	31.0483494	9.8785305	•001037344
965	931225	898632125	31.0644491	9.8819451	.001036269.
966	933156	901428696	31.0805405	9.8853574	•001035197
967	935089	904231063	31.0966236	9.8887673	•001034126
968	937024	907039232	31.1126984	9.8921749	•001033058
969	938961	909853209	31.1287648	9.8955801	.001031992
970	940900	912673000	31.1448230	9.8989830	•001030928
971	942841	915498611	31.1608729	9.9023835	.001029866
972	944784	918330048	31.1769145	9.9057817	.001028807
973	946729	$\begin{array}{ c c c c c c c c c c c c c c c c c c c$	31.1929479	9.9091776	.001027749
974	948676		31.2089731	9.9125712	•001026694
975 976	950625	926859375	31.2249900	9.9159624	.001025641
977	952576	929714176 932574833	31.2409987 31.2569992	9.9193513	001024590
978	954529 956484	935441352	31.2729915	$\begin{vmatrix} 9.9227379 \\ 9.9261222 \end{vmatrix}$.001023541
979	958441	938313739	31.2889757	9.9295042	$001022495 \ 001021450$
980	960400	941192000	31.3049517	9.9328839	.001020408
981	962361		31.3209195	9.9362613	001020403
982	964324	946966168	31.3368792	9.9396363	•001019103
983	966289	949862087	31.3528308	9.9430092	·001017294
984	968256	952763904	31.3687743	9.9463797	.001017294
985	970225	955671625	31.3847097	9.9497479	.001015228
986	972196	958585256	31.4006369	9.9531138	.001013223
987	974169	961504803	31.4165561	9.9564775	.001013171
988	976144		31.4324673	9.9598389	·001012146

	,		OCBEB, DQUARE	THE COBE RECOT	11/1
Number.	Squares.	Cubes.	√ Boots.	³ √ Roots.	Reciprocals.
989	978121	967361669	31.4483704	9.9631981	·001011122
990	980100	970299000	31.4642654	9.9665549	.001010101
991	982081	973242271	31.4801525	9.9699055	.001009082
992	984064	976191488	31.4960315	9.9732619	.001008065
993	986049	979146657	31.5119025	9.9766120	.001007049
994	988036	982107784	31.5277655	9.9799599	.001006036
995	990025	985074875	31.5436206	9.9833055	.001005025
996	992016	988047936	31.5594677	9.9866488	.001004016
1 997	994009	991026973	31.5753068	9.9899900	.001003009
998	996004	994011992	31.5911380	9.9933289	.001002004
999	998001	997002999	31.6069613	9.9966656	.001001001
1000	1000000	1000000000	31.6227766	10.00000000	.0010000000
1001	1002001	1003003001	31.6385840	10.0033222	.0009990010
1002	1004004	1006012008	31.6543866	10.0066622	.0009980040
1003	1006009	1009027027	31.6701752	10.0099899	.0009970090
1004	1008016	1012048064	31.6859590	10 0133155	.0009960159
1005	1010025	1015075125	31.7017349	10.0166389	.0009950249
1006	1012036	1018108216	31.7175030	10.0199601	.0009940358
1007	1014049	1021147343	31.7332633	10.0232791	.0009930487
1008	1016064	1024192512	31.7490157	10.0265958	.0009920635
1009	1018081	1027243729	31.7647603	10.0299104	.0009910803
1010	1020100	1030301000	31.7804972	10.0332228	.0009900990
1011	1022121	1033364331	31.7962262	10.0365330	.0009891197
1012	1024144	1036433728	31.8119474	10.0398410	.0009881423
1013	1026169	1039509197	31.8276609	10.0431469	.0009871668
1014	1028196	1042590744	31.8433666	10.0464506	.0009861933
1015	1030225	1045678375	31.8590646	10.0497521	.0009852217
1016	1032256	1048772096	31.8747549	10.0530514	.0009842520
1017	1034289	1051871913	31.8904374	10.0563485	.0009832842
1018	1036324	1054977832	31.9061123	10.0596435	·0009823183
1019	1038361	1058089859	31.9217794	10.0629364	·0009813543
1020	1040400	1061208000	31.9374388	10.0662271	.0009803922
1021	1042441	1064332261	31.9530906	10.0695156	.0009794319
1022	1044484	1067462648	31.9687347	10.0728020	.0009784736
1023	1046529	1070599167	31.9843712	10.0760863	.0009775171
1024	1048576	1073741824	32.0000000	10.0793684	.0009765625
1025	1050625	1076890625	32.0156212	10.0826484	.0009756098
1026	1052676	1080045576	32.0312348	10.0859262	0009746589
1027	1054729	1083206683	32.0468407	10.0892019	.0009737098
1028	1056784	1086373952	32.0624391	10.0924755	.0009727626
1029	1058841		32.0780298	10.0957469	.0009718173
1030	1060900	1092727000	32.0936131	10.0990163	.0009708738
1031	1062961	1095912791	32.1091887	10.1022835	.0009699321
1032	1065024	1099104768	32.1247568	10.1055487	.0009689922
1033	1067089	1102302937	32.1403173	10.1188117	.0009680542
1034	1069156	1105507304	32.1558704	10.1120726	.0009671180
1035	1071225	1108717875	32.1714159	10.1153314	.0009661836
1036	1073296	1111934656	32.1869539	$\begin{array}{ c c c c c c c c c c c c c c c c c c c$	$\begin{array}{c} \cdot 0009652510 \\ \cdot 0009643202 \end{array}$
1037	1075369	1115157653	32.2024844	10.1218428 10.1250953	0009643202
1038	1077444	1118386872	$32 \cdot 2180074 \\ 32 \cdot 2335229$	10.1250955 10.1283457	0009633911
1039	1079521	1121622319 1124864000		10.1315941	·0009624039
1040	1081600	1124804000	54 4490510	10 1010941	0009010000

102	LABL	or EQUANTE,	CUBES, EQUARE	AND CODE ROOT	U
Number.	Squares.	Cubes.	√ Roots.	³ √ Roots.	Reciprocals.
1041	1083681	1128111921	32.2645316	10.1348403	•0009606148
1042	1085764	1131366088	32.2800248	10.1380845	0009596929
1043	1087849	1134626507	32.2955105	10.1413266	0009587728
1044	1089936	1137893184	32.3109888	10.1445667	0009578544
1045	1092025	1141166125	32.3264598	10.1478047	*0009569378
1046	1094116	1144445336	32.3419233	10.1510406	*0009560229
1047	1096209	1147730823	32.3573794	10.1542744	.0009551098
1048	1098304	1151022592	32.3728281	10.1575062	*0009541985
1049	1100401	1154320649	32.3882695	10.1607359	*0009532888
1050	1102500	1157625000	32.4037035	10.1639636	*0009523810
1051	1104601	1160935651	32.4191301	10.1671893	*0009514748
1052	1106704	1164252608	32.4345495	10.1704129	10009505703
1053	1108809	1167575877	32.4499615	10.1736344	*0009496676
1054	1110916	1170905464	32.4653662	10.1768539	*0009487666
1055	1113025	1174241375	32.4807635	10.1800714	0009478673
1056	1115136	1177583616	32.4961536	10.1832868	*0009469697
1057	1117249	1180932193	32.5115364	10.1865002	*0009460738
1058	1119364	1184287112	32.5269119	10.1897116	0009451796
1059	1121481	1187648379	32.5422802	10.1929209	'0009442871
1060	1123600	1191016000	32.5576412	10.1961283	*0009433962
1061	1125721	1194389981	32.5729949	10.1993336	0009425071
1062	1127844	1197770328	.32.5883415	10.2025369	'0009416196
1063	1129969	1201157047	32.6035807	10.2057382	'0009407338
1064	1132096	1204550144	32.6190129	10.2089375	*0009398496
1065	1134225	1207949625	32.6343377	10.2121347	0009389671
1066	1136356	1211355496	32.6496554	10.2153300	.0009380863
1067	1138489	1214767763	32.6649659	10.2185233	0009372071
1068	1140624	1218186432	32.6802693	10.2217146	0009363296
1069	1142761	1221611509	32.6955654	10.2249039	0009354537
1070 1071	1144900	1225043000	$32.7108544 \ 32.7261363$	$\begin{array}{c c} 10.2280912 \\ 10.2312766 \end{array}$	*0009345794
1071	$ 1147041 \\ 1149184 $	$\begin{array}{c c} 1228480911 \\ 1231925248 \end{array}$	32.7414111	10.2312766	*0009337068 *0009328358
1073	1149184	1231925248 1235376017	32.7566787	10.2376413	000932838
1073	1151329 1153476	1238833224	32.7719392	10.2408207	0009319004
1075	1155625		32.7871926	10.2439981	.0009302326
1076		1245766976	32.8024398	10.2471735	.0009293680
1077		1249243533	32.8176782	10.2503470	0009285051
1078	1162084		32.8329103	10.2535186	0009276438
1079	1164241	1256216039	32.8481354	10.2566881	.0009267841
1080	1166400		32.8633535	10.2598557	.0009259259
1081	1168561	1263214441	32.8785644	10.2630213	0009250694
1082	1170724	1266723368	32.8937684	10.2661850	0009242144
1083	1172889	1270238787	32.9039653	10.2693467	0009233610
1084	1175056	1273760704	32.9241553	10.2725065	*0009225092
1085	1177225	1277289125	3 2 ·939338 2	10.2756644	*0009216590
1086	1179396	1280824056	32.9545141	10.2788203	*0009208103
1087	1181569		32.9696830	10.2819743	*0009199632
1088	1183744	1287913472	32.9848450	10.2851264	*0009191176
1089	1185921	1291467969	33.0000000	10.2882765	.0009182736
1090		1295029000	33.0151480	10.2914247	0009174312
1091		1298596571	33.0302891	10.2945709	.0009165903
1092	1192464	1302170688	33.0454233	10.2977153	·0009157509 ¹
5					

1	,	or equilibries,	COBES, DCOARE	AND CODE TOOL	103
Number.	Squares.	Cubes.	VRoots.	3/ Roots.	Reciprocals.
1093	1194649	1305751357	33.0605505	10.3008577	.0009149131
1094	1196836	1309338584	33.0756708	10.3039982	.0009140768
1095	1199025	1312932375	33.0907842	10.3071368	.0009132420
1096	1201216	1316532736	33.1058907	10.3102735	.0009124008
1097	1203409	1320139673	33.1209903	10.3134083	.0009115770
1098	1205604	1323753192	33.1360830	10.3165411	.0009107468
1099	1207801	1327373299	33.1511689	10.3196721	.0009107408
1100	1210000			10.3190721	.0009090909
1101	1210000	1331000000	33.1662479		
1101		1334633301	33.1813200	10.3259284	.0009082652
	1214404	1338273208	33.1963853	10.3290537	.0009074410
1103	1216609	1341919727	33.2114438	10.3321770	.0009066183
1104	1218816	1345572864	33.2266955	10.3352985	.0009057971
1105	1221025	1349232625	33.2415403	10.3384181	.0009049774
1106	1223236	1352899016	33.2565783	10.3415358	.0009041591
1107	1225449	1356572043	33.2716095	10.3446517	.0009033424
1108	1227664	1360251712	33.2866339	10.3477657	.0009025271
1109	1229881	1363938029	33.3016516	10.3508778	.0009017133
1110	1232100	1367631000	33.3166625	10.3539880	.0009009009
1111	1234321	1371330631	33.3316666	10.3570964	.0009000900
1112	1236544	1375036928	33.3466640	10.3602029	.0008992806
1113	1238769	1378749897	33.3616546	10.3633076	.0008984726
1114	1240996	1382469544	33.3766385	10.3664103	.0008976661
1115	1243225	1386195875	33.3916157	10.3695113	.0008968610
1116	1245456	1389928896	33.4065862	10.3726103	.0008960753
1117	1247689	1393668613	33.4215499	10.3757076	.0008952551
1118	1249924	1397415032	33.4365070	10.3788030	.0008944544
1119	1252161	1401168159	33.4514573	10.3818965	.0008936550
1120	1252101 1254400	1404928000	33.4664011	10.3849882	0008928571
1121	1254400	1404928000	_	10.3880781	.0008960607
1122	1258884		33.4813381		·0008922656
1123	3	1412467848	33.4962684	10.3911661	
1	1261129	1416247867	33.5111921	10.3942527	.0008904720
1124	1263376	1420034624	33.5261692	10.3973366	.0008896797
1125	1265625	1423828125	33.5410196	10.4004192	.0008888889
1126	1267876	1427628376	33.5559234	10.4034999	.0008880995
1127	1270129	1431435383	33.5708206	10.4065787	.0008873114
1128	1272384	1435249152	33.5857112	10.4096557	.0008865248
1129	1274641	1439069689	33.6005952	10.4127310	.0008857396
1130	1276900	1442897000	33.6154726	10.4158044	.0008849558
1131	1279161	1446731091	33.6303434	10.4188760	.0008841733
1132	1281424	1450571968	33.6452077	10.4219458	.0008833922
1133	1283689	1454419637	33.6600653	10.4250138	.0008826125
1134	1285956	1458274104	33.6749165	10.4280800	·0008818342
1135	1288225	1462135375	33.6897610	10.4311443	·0008810573
1136	1290496	1466003456	83.7045991	10.4342069	.0008802817
1137	1292769	1469878353	33.7174306	10.4372677	.0008795075
.1138	1295044	1473760072	33.7340556	10.4403677	.0008787346
1139	1.297321	1477648619	33.7490741	10.4433839	.0008779631
1140	1299600	1481544000	33.7638860	10.4464393	.0008771930
1141	1301881	1485446221	33.7786915	10.4494929	.0008764242
1142	1304164	1489355288	33.7934905	10.4525448	.0008756567
1143	1306449	1493271207	33.8082830	10.4555948	.0008748906
1144		1497193984	33.8230691	10.4586431	.0008741259
	2000100		30 323001		
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104		of Decares,	OUBES, DQUARE		
Number.	Squares.	Cutes.	√ Roots.	3 Roots.	Reciprocals.
7145	1311025	1501123625	33.8378486	10.4616896	.0008733624
1146	1313316	1505060136	33.8526218	10.4647343	.0008726003
1147	1315609	1509003523	33.8673884	10.4677773	•0008718396
1148	1317904	1512953792	33.8821487	10.4708158	.0008710801
1149	1320201	1516910949	33.8969025	10.4738579	.0008703220
1150	1322500	1520875000	33.9116499	10.4768955	.0008695652
1151	1324801	1524845951	33.9263909	10.4799314	.0008688097
1152	1327104	1528823808	33.9411255	10.4829656	•0008680556
1153	1329409	1532808577	33.9558537	10.4859980	-0008673027
1154	1331716	1536800264	33.9705755	10.4890286	•0008665511
1155	1334025	1540798875	33.9852910	10.4920575	•0008658009
1156	1336336	1544804416	34.0000000	10.4950847	.0008650519
1157	1338649	1548816893	34.0147027	10.4981101	.0008643042
1158	1340964	1552836312	34.0293990	10.5011337	·0008635579
1159	1343281	1556862679	34.0440890	10.5041556	.0008628128
1160	1345600	1560896000	34.0587727	10.5071757	.0008620690
1161	1347921	1564936281	34.0734501	10.5101942	.0008613264
1162	1350244	1568983528	34.0881211	10.5132109	.0008605852
1163	1352569	1573037747	34.0127858	10.5162259	0008598452
1164	1354896	1577098944	34.1174442	10.5192391	.0008591065
1165	1357225	1581167125	34.1320963	10.5222506	.0008583691
1166	1359556	1585242296	34.1467422	10.5252604	0008576329
1167	1361889	1589324463	34.1613817	10.5282685	.0008568980
1168	1364224	1593413632	34.1760150	10.5312749	.0008561644
1169	1366561	1597509809	34.1906420	10.5342795	.0008554320
1170	1368900	1601613000	34.2052627	10.5372825	.0008547009
1171	1371241	1605723211	34.21987.73	10.5402837	.0008539710
1172 1173	1373584 1375929	$\frac{1609840448}{1613964717}$	34.2344855	10.5432832	0008532423 0008525149
1174	1378276	1618096024	34·2490875 34·2636834	$\frac{10.5462810}{10.5492771}$	0008525149
1175	1380625	1622234375	34.2782730	10.5522715	0008510638
1176.	1382976	1626379776	34.2928564	10.5552642	.0008503401
1177	1385329	1630532233	34.3074336	10.5582552	.0008496177
1178	1387684	1634691752	34.3220046	10.5612445	.0008488964
1179	1390041	1638858339	34.3365694	10.5642322	.0008481764
1180	1392400	1643032000	34.3511281	10.5672181	.0008471576
1181	1394761	1647212741	34.3656805	10.5702024	.0008467401
1182	1397124	1651400568	34.3802268	10.5731849	.0008460237
1183	1399489	1655595487	34.3947670	10.5761658	.0008453085
1184	1401856	1659797504	34.4093011	10.5791449	.0008445946
1185	1404225	1664006625	34.4238289	10.5821225	.0008438819
1186	1406596	1668222856	34.4383507	10.5850983	.0008431703
1187	1408969	1672446203	34.4528663	10.5880725	.0008424600
	1411344	1676676672	34.4673759	10.5910450	.0008417508
1	1413721	1680914629	34.4818793	10.5940158	.0008410429
1190	1416100	1685159000	34·496376 6	10.5969850	.0008403361
	1418481	1689410871	34.5108678	10.5999525	.0008396308
		1693669888	34.5253530	10.6029184	.0008389262
1	1423249	1697936057	34.5398321	10.6058826	.0008382320
	1425636	1702209384	34.5543051	10.6088451	.0008375209
•	1428025	1706489875	34.5687720	10.6118060	·00083682 01
2196	1430416	1710777536	34.5832329	10.6147652	.0008361204

				,	100
Number.	Squares.	Cubes.	√ Roots.	Noots.	Reciprocals.
1197	1432809	1715072373	34.5976879	10.6177228	.0008354219
1198	1435204	1719374392	34.6121366	10.6206788	•0008347245
1199	1437601	1723683599	34.6265794	10.6236331	.0008340284
1200	1440000	1728000000	34.6410162	10.6265857	*0008333333
1201	1442401	1732323601	34.6554469	10.6295367	*0008326395
1202	1444804	1736654408	34.6698716	10.6324860	•0008319468
1202			34.6842904	10.6354338	
1203	1447209	1740992427	34.6987031		*0008312552
1204	1449616	1745337664		10.6383799	*0008305648
	1452025	1749690125	34.7131099	10.6413244	.0008298755
1206	1454436	1754049816	34.7275107	10.6442672	.0008291874
1207	1456849	1758416743	34.7419055	10.6472085	*0008285004
1208	1459264	1762790912	34.7562944	10.6501480	.0008278146
1209	1461681	1767172329	34.7706773	10.6530860	.0008271299
1210	1464100	1771561000	34.7850543	10.6560223	.0008264463
1211	1466521	1775956931	34.7994253	10.6589570	0008257638
1212	1468944	1780360128	34.8137904	10.6618902	.0008250825
1213	1471369	1784770597	34.8281495	10.6648217	*0008244023
1214	1473796	1789188344	34.8425028	10.6677516	*0008237232
1215	1476225	1793613375	34.8568501	10.6706799	*0008230453
1216	1478656	1798045696	34.8711915	10.6736066	*0008223684
1217	1481089	1802485313	34.8855271	10.6765317	*0008216927
1218	1483524	1806932232	34.8998567	10.6794552	.0008210181
1219	1485961	1811386459	34.9141805	10.6823771	*0008203445
1220	1488400	1815848000	34.9284984	10.6852973	.0008196721
1221	1490841	1820316861	34.9428104	10.6882160	.0008190008
1222	1493284	1824793048	34.9571166	10.6911331	.0008183306
1223	1495729	1829276567	34.9714169	10.6940486	.0008176615
1224	1498176	1833764247	34.9857114	10.6969625	*0008169935
1225	1500625	1838265625	35.0000000	10.6998748	*0008163265
1226	1503276	1842771176	35.0142828	10.7027855	.0008156607
1227	1505529	1847284083	35.0285598	10.7056947	*0008149959
1228	1507984	1851804352	35.0428309	10.7086023	*0008143322
1229	1510441	1856331989	35.0570963	10.7115083	*0008136696
. 1230	1512900	1860867000	35.0713558	10.7144127	.0008130081
1231	1515361	1865409391	35.0856096	10.7173155	.0008123477
1232	1517824	1869959168	35.0998575	10.7202168	*0008116883
1233	1520289	1874516337	35.1140997	10.7231165	.0008110300
1234	1522756	1879080904	35.1283361	10.7260146	.0008103728
1235	1525225	1883652875	35.1425668	10.7289112	.0008097166
1236	1527696	1888232256	35.1567917	10.7318062	.0008090615
1237	1530169	1892819053	35.1710108	10.7346997	.0008084074
1238	1532644	1897413272	35.1852242	10.7375916	.0008077544
1239	1535121	1902014919	35.1994318	10.7404819	.0008071025
1240	1537600	1906624000	35.2136337	10.7433707	.0008064516
1240	1540081	1911240521	35.2278299	10.7462579	.0008058018
1242	1542564	1915864488	35.2420204	10.7491436	.0008051530
1243	1545049	1920495907	35.2562051	10.7520277	.0008045052
1244	1547536	1925134784	35.2703842	10.7549103	.0008038585
1245	1550025	1929781125	35.2845575	10.7577913	0008032129
1246	$1550025 \\ 1552516$	1934434936	35.2987252	10.7606708	0008025682
1247	1555009	1939096223	35.3128872	10.7635488	.0008019246
1		1943764992	35.3270435	10.7664252	.0008012821
1210	1001004	1010101002	00 02,0100		4

10h TABLE OF DECAMES, OUDES, DECAME AND OUDE ROOTS						
Number	Squares.	Cubes.	√Roots.	Noots.	Reciprocals.	
1249	1560001	1948441249	35.3411941	10.7693001	.0008006405	
1250	1562500	1953125000	35.3553391	10.7721735	.0008000000	
1251	1565001	1957816251	35.3694784	10.7750453	.0007993605	
1252	1567504	1962515003	35.3836120	10.7779156	.0007987220	
1253	1570009	1967221277	35.3977400	10.7807843	.0007980846	
1254	1572516	1971935064	35.4118624	10.7836516	.0007974482	
1255	1575025	1976656375	35.4259792	10.7865173	.0007968127	
1256	1577536	1981385216	35.4400903	10.7893815	.0007961783	
1257	1580049	1986121593	35.4541958	10.7922441	.0007955449	
1258	1582564	1990865512	35.4682957	10.7951053	.0007949126	
1259	1585081	1995616979	35.4823900	10.7979649	0007942812	
1260	1587600	2000376000	35.4964787	10.8008230	.0007936508	
1261	1590121	2005142581	35.5105618	10.8036797	.0007930214	
1262	1592644	2009916728	35.5246393	10.8065348	.0007923930	
1263	1595169	2014698447	35.5387113	10.8093884	.0007917656	
1264	1597696	2019487744	35.5527777	10.8122404	.0007911392	
1265	1600225	2024284625	35.5668385	10.8150909	.0007905138	
1266	1602756	2029089096	35.5808937	10.8179400	.0007898894	
1267	1605289	2033901163	35.5949434	10.8207876	.0007892660	
1268	1607824	2038720832	35.6089876	10.823633 6	.0007886435	
1269	1610361	2043548109	35.6230262	10.8264782	.0007880221	
1270	1612900	2048383000	35.6370593	10.8293213	.0007874016	
1271	1615441	2053225511	35.6510869	10.8321629	.0007867821	
1272	1617984	2058075648	35.6651090	10.8350030	•0007861635	
1273	1620529	2062933417	35.6791255	10.8378416	.0007855460	
1274	1623076	2067798824	35.6931366	10.8406788	.0007849294	
1275	1625625	2072671875	35.7071421	10.84351.44	.0007843137	
1276	1628176	2077552576	35.7211422	10.8463485	.0007836991	
1277	1630729	2082440933	35.7351367	10.8491812	•0007830854	
1278	1633284	2087336952	35.7491258	10.8520125	.0007824726	
1279	1635841	2092240639	35.7631095	10.8548422	.0007818608	
1280	1638400	2097152000	35.7770876	10.8576704	.0007812500	
1281	1640961	2102071841	35.7910603	10.8604972	.0007806401	
1282	1643524	2106997768	35.805 0276	10.8633225	.0007800312	
1283	1646089	2111932187	35.8189894	10.8661454	•0007794232	
.1284	1648656	2116874304	35.8329457	10.8689687	.0007788162	
1285	1651225	2121824125	35·846896 6	10.8717897	.0007782101	
1286	1653796	2126781656	35.8608421	10.8746091	.0007776050	
1287	1656369	2131746903	35.8747822	10.8774271	0007770008	
1288	1658944	2136719872	35.8887169	10.8802436	.0007763975	
1289	1661521	2141700569	35.9026461	10.8830587	0007757952	
1290	1664100	2146689000	35.9165699	10.8858723	.0007751938	
1291	1666681	2151685171	35.9304884	10.8886845	.0007745933	
1292	1669264	2156689088	35.9444015	10.8914952	.0007739938	
1293	1671849	2161700757	35.9583092	10.8943044	.0007733952	
$1294 \\ 1295$	1674436 1677025	2166720184	35.9722115	10.8971123	•0007727975	
$\begin{array}{c} 1295 \\ 1296 \end{array}$		2171747375	35.9861084	10.8999186 10.9027235	.0007722008	
$\begin{array}{c c} 1296 \\ 1297 \end{array}$	1679616 1682209	$\begin{bmatrix} 2176782336 \\ 2181825073 \end{bmatrix}$	36·0000000 36·0138862	10.9027235	$ \cdot 0007716049 $ $ \cdot 0007710100 $	
1297 1298	1684804	2181825073	36.0138802	10.9055269 10.9083290	.0007710100	
1298 1299	1687401	2180875592	36.0277671	10.9111296	0007704160	
1300	1690000	2197933399	36.0555128	10.9111296 10.9139287	0007698229	
1000	1 1000000	2000000	00 0000120	10 0100207	0007002000	

r	Number.	Squares.	Cubes.	Roots.	³ √. Roots.	Reciprocals.
	1301	1692601	2202073901	36.0693776	10.9167265	.0007686395
	1302	1695204	2207155608	36.0832371	10.9195228	.0007680492
	1303	1697809	2212245127	36.0970913	10.9223177	.0007674579
	1304	1700416	2217342464	36.1109402	10.9251111	.0007668712
ı	1305	1703025	2 222447625	36.1247837	10.9279031	.0007662835
	1306	1705636	2227560616	36.1386220	10.9306937	.0007656968
1	1307	1708249	2232681443	36.1524550	10.9334829	-0007651109
İ	1308	1710864	2237810112	36.1662826	10.9362706	.0007645260
١	1309	1713481	2242946629	36.1801020	10.9390569	.0007639419
	1310	1716100	2248091000	36.1939221	10.9418418	0007633588
	1311	1718721	2253243231	36.2077340	10.9446253	.0007627765
i	1312	1721344	2258403328	36.2215406	10.9475074	.0007621951
1	1313	1723969	2263571297 2268747144	36.2353419	10.9501880	.0007616446
	1314 1315	1726596	2273930875	36.2491379	10.9529673	.0007610350
	1316	1729225 1731856	2279122496	36·2626287 36·2767143	10.9557451	·0007604563 ·0007598784
1	1317	1734489	2284322013	36.2904246	10.9612965	0007593784
1	1318	1737124	2289529432	36.3042697	10.9640701	.0007587253
	1319	1739761	2294744759	36.3180396	10.9668423	.0007581501
	1320	1742400	2 299968000	36:3318042	10.9696131	.0007575758
	1321	1745041	2305199161	36.3455637	10.9723825	.0007570023
	1322	1747684	2310438248	36.3593179	10.9751505	.0007564297
	1323	1750329	2315685267	36:3730670	10.9779171	.0007558579
	1324	1752976	2320940224	36.3868108	10.9806823	.0007552870
	1325	1755625	2326203125	36.4005494	10.9834462	.0007547170
۱	1326	1758276	2331473976	36.4142829	10.9862086	.0007541478
1	1327	1760929	2336752783	36.4280112	10.9889696	.0007535795
	1328	1763584	2342039552	36.4417343	10.9917293	.0007530120
	1329	1766241	2347334289	3 6- 4554523	10.9944876	0007524454
	1330	1768900	2352637000	3 6 .4691650	10.9972445	.0007518797
۱	1331	1771561	2357947691 2363266368	36.4828727	11.00000000	.0007513148
	1332 1333	1774224	2368593037	36·4965752 36·5102725	11.0027541 11.0055069	·0007507508 ·0007501875
١	1334	1776889 1779556	2373927704	36.5239647	11.0082583	.0007301873
ı	1335	1782225		36.5376518	11:0110082	0007490232
ı	1336	1784896		36.5513388	11.0137569	.0007485030
	1337	1787569		36.5650106	11.0165041	.0007479432
	1338	1790244		36.5786823	11.0192500	.0007473842
	1339	1792921	2400721219	36.5923489	11.0219945	.0007468260
	1340	1795600	2406104000	36.6060104	11.0247377	.0007462687
	1341	1798281	2411494821	36.6196668	11.0274795	.0007457122
	1342	1800964	2416893688	36.6333181	11:0302199	.0007451565
1	1343	1803649	2422300607	36.6469144	11.0329590	.0007446016
ł	1344	1806336	2427715584	36.6606056	11.0356967	.0007440476
	1345	1809025	2433138625	36.6742416	11.0384330	.0007434944
	1346	1811716	2438569736	36.6878726	11:0411680	.0007429421
	1347	1814409	2444008923	36.7014986	11·0439017 11·0466339	0007423905 0007418398
	1348	1817104	244945619 2 245491154 9	36·7151195 36·7287353	11.0493649	0007418398
	1349 1350	1819801 1822500	245491154 9 246037500 0	36.7423461	11.0520945	0007412898
	1351	1825201	2465846551	36.7559519	11.0548227	.0007401924
	1352		2471326208	36.7695526	11.0575497	.0007396450
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Number	Squares.	Cubes.	√ Roots.	3/ Roots.	Reciprocals.
1353	1830609	2476813977	36.7831483	11.0602752	.0007390983
1354	1833316	2482309864		11.0629994	.0007385524
1355	1836025	2487813875	36.8103246	11.0657222	.0007380074
1356	1838736	2493326016	36.8239053	11.0684437	.0007374631
1357	1841449	2498846293	36.8374809	11.0711639	.0007369197
1358	1844164	2504374712	36.8510515	11.0738828	.0007363770
1359	1846881	2509911279	36.8646172	11.0766003	•0007358352
1360	1849600	2515456000	36.8781778	11.0793165	.0007352941
1361	1852321	2521008881	36.8917335	11.0820314	.0007347539
1362	1855044	2526569928	36.9052842	11.0847449	.0007342144
1363	1857769	2532139147	36.9188299	11.0874571	.0007336757
1364	1860496	2537716544	36.9323706	11:0901679	.0007331378
1365		2543302125	36.9459064	11:0928775	0007326007 0007320644
$1366 \\ 1367$	$1865956 \\ 1868689$	2548895896 2554497863	36·9594372 36·9729631	11.0955857	0007320044
1368	1871424	2560108032	36.9864840	11.1009982	0007319289
1369	1874161	2565726409	37.0000000	11.1003302	.0007304602
1370	1876900	2571353000	37.0135110	11.1064654	.0007299270
1371	1879641	2576987811	37.0270172	11.1091070	.0007293946
1372	1882384	2582630848	37.0405184	11.1118073	.0007288630
1373	1885129	2588282117	37.0540146	11.1145064	.0007283321
1374	1887876	2593941624	37.0675060	11.1172041	.0007278020
1375	1890625	2599609375	37.0899924	11.1199004	.0007272727
1376	1893376	2605285376	37.0944740	11.1225955	.0007267442
1377	1896129	2610969633	37.1079506	11.1252893	.0007262164
1378	1898884	2616662152	37.1214224	11.1279817	.0007256894
1379	1901641	2622362939	37.1348893	11.1306729	.0007251632
1380	$\frac{1904400}{1907161}$	2628072000	37.1483512	11.1333628	0007246377 0007241130
$1381 \\ 1382$	$1907101 \\ 1909924$	$2633789341 \mid 2639514968 \mid$	37.1618084 37.1752606	11·1360514 11·1387386	0007241130
1383	1903324 1912689	2645248887	37.1887079	11.1414246	0007230658
1384	1915456	2650991104	37.2021505	11.1441093	.0007225434
1385	1918225	2656741625	37.2155881	11.1467926	.0007220217
1386	1920996	2662500456	37.2290209	11.1494747	.0007215007
1387	1923769	2668267603	37.2424489	11.1521555	.0007209805
1388	1926544		37.2558720	11.1548350	.0007204611
1389	1929321	2679826869	37.2692903	11.1575133	.0007199424
1390	1932100	2685619000	37.2827037	11.1601903	.0007194245
1391	1934881	2691419471	37.2961124	11.1628659	.0007189073
1392	1937664	2697228288	37.3095162	11.1655403	.0007183908
1393	1940449	2703045457	37.3229152	11.1682134	.0007178751
1394 1395	$egin{array}{c} 1943236\ 1946025 \end{array}$	2708870984 2714704875	37·3363094 37·3496988	$oxed{11.1708852} 11.1735558$	·0007173601 ·0007168459
1396	1948816	2720547136	37.3630834	11.1762250	.0007163324
1397	1951609	2726397773	37.3764632	11.1788930	.0007158196
1398	1954404		37.3898382	11.1815598	.0007153076
1399	1957201	2738124199	37.4032084	11.1842252	.0007147963
1400	1960000	2744000000	37.4165738	11.1868894	.0007142857
1401	1962801	2749884201	37.4299345	11.1895523	.0007137759
1402	1965604	2755776808	37.4432904	11.1922139	.0007132668
1403	1968409	2761677827	37.4566416	11.1948743	.0007127584
1404	1971216	2767587264	37.4699880	11.1975334	·000712250 7

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Number.	Squares.	Cubes.	VRoots.	Noots.	Reciprocals.
1405	1974025	2773505123	37.4833296	11.2001913	.0007117438
1406	1976836	2779431416	37.4966665	11.2028479	0007112376
1407	1979649	2785366143	37.5099987	11.2055032	.0007107321
1408	1982464	2791309312	37.5233261	11.2081573	.0007102273
1409	1985281	2797260929	37:5366487	11.2108101	.0007097232
1410	1988100	2803221000	37.5499667	11.2134617	.0007092199
1411	1990921	2809189531	37.5632799	11.2161120	.0007087172
1412	1993744	2815166528	37.5765885	11.2187611	.0007082153
1413	1996569	2821151997	37.5898922	11.2214089	.0007077141
1414	1999396	2827145944	37.6031913	11.2240054	.0007072136
1415	2002225	2833148375	37.6164857	11.2267007	.0007067138
1416	2005056	2839159296	37.6297754	11.2293448	.0007062147
1417	2007889	2845178713	37.6430604	11.2319876	.0007057163
1418	2010724	2851206632	37.6563407	11.2346292	.0007052186
1419	2013561	2857243059	37.6696164	11.2372696	.0007047216
1420	2016400	2863288000	37.6828874	11.2399087	.0007042254
1421	2019241	2869341461	37·696153 6	11.2425465	.0007037298
1422	2022084	2875403448	37.7094153	11.2451831	.0007032349
1423	2024929	2881473967	37.7226722	11.2478185	.0007027407
1424	2027776	2887553024	37.7359245	11.2504527	.0007022472
1425	2030625	2893640625	37.7491722	11.2530856	.0007017544
1426	2033476	2899736776	37.7624152	11.2557173	.0007012623
1427	2036329	2905841483	37.7756535	11.2583478	-0007007708
1428	2039184	2911954752	37.7888873	11.2609770	0007002801
1429	2042041	2918076589	37.8021163	11.2636050	-0006997901
1430	2044900	2924207000	37.8153408	11.2662318	$\cdot 0006993007$
1431	2047761	2930345991	37.8285606	11.2688573	·0006988120
1432	2050624	2936493568	37.8417759	11.2714816	.0006983240
1433	2053489	2942649737	37.8549864	11.2741047	.0006978367
1434	2056356	2948814504	37.8681924	11.2767266	.0006973501
1435 1436	2059225	2954987875	37.8813938	11.2793472	.0006968641
1430	2062096 2064969	2961169856 2967360453	37.8945906	11·2819666 11·2845849	0006963788 0006958942
1438	2067844	2973559672	37·9077828 37·9209704	11.2843849	·0006954103
1439	2070721	2979767519	37.9341535	11.2898177	0000934103 0006949270
1440	2073600	2985984000	37.9473319	11.2924323	.0006944444
1441	2076481	2992209121	37.9605058	11.2950457	·0006939625
1442	2079364	2998442888	37.9736751	11.2976579	·0006934813
1443	2082249	3004685307	37.9868398	11.3002688	.0006930007
1444	2085136	3010936384	38.0000000	11.3028786	.0006925208
1445	2088025	3017196125	38.0131556	11.3054871	.0006920415
1446	2090916	3023464536	38.0263067	11.3080945	.0006915629
1447	2093809	3029741623	38.0394532	11:3107006	.0006910850
1448	2096704	3036027392	38.0525952	11:3133056	·0006906078
1449	2099601	3042321849	38.0657326	11.3159094	.0006901312
1450	2102500	3048625000	38.0788655	11.3185119	·0006896552
1451	2105401	3054936851	38.0919939	11.3211132	.0006891799
1452	2108304	3061257408	38.1051178	11.3237134	.0006887052
1453	2111209	3067586777	38.1182371	11.3263124	.0006882312
1454	2114116	3073924664	38.1313519	11.3289102	.0006877579
1455	2117025	3080271375	38.1444622	11.3315067	.0006872852
1456	2119936	3086626816	38.1575681	11.3341022	·000 6 368 132

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Number.	Squares.	Cubes.	√ Roots.	3 Roots.	Reciprocals.
1457	2122849	3092990993	38.1706693	11.3366964	.0006863412
1458	2125764	3099363912	38.1837662	11.3392894	.0006858711
1459	2128681	3.105745579	38.1963585	11.3418813	*0006854010
1460	2131600	3112136000	38.2099463	11.3444719	*0006849315
1461	2134521	3118535181	38.2230297	11.3470614	*0006844627
1462	2137444	3124943128	38.2361085	11.3496497	*0006839945
1463	2140369	3131359847	38.2491829	11.3522368	*0006835270
1464	2143296	3137785344	33.2622529	11.3548227	*0006830601
1465	2146225	3144219625	38.2753184	11.3574075	*0006825939
1466	2149156	3150662696	38.2863794	11.3599911	*0006821282
1467	2152089	3157114563	38.3014360	11.3625735	*0006816633
1468	2155024	3163575232	38.3144881	11.3651547	.0006811989
1469	2157961	3170044709	38.3275358	11.3677347	*0006807352
1470	2160900	3176523000	38.3405790	11.3703136	0006802721
1471	2163841	3183010111	38.3536178	11.3728914	*0006798097
1472	2166784	3189506048	38.3666522	11.3754679	*0006793478
1473	2169729	3196010817	38.3796821	11.3780433	*0006788866
1474	2172676	3202524424	38.3927076	11.3806175	0006784261
1475	2175625	3209046875	38.4057287	11.3831906	.0006779661
1476	2178576	3215578176	38.4187454	11.3857625	*0006775068
1477	2181529	3222118333	38.4317577	11.3883332	0006770481
1478	2184484	3228667352	38.4447656	11.3909028	*0006765900
1479	2187441	3235225239	38.4577691	11.3934712	0006761325
1480	2190400	3241792000	38.4707681	11.3960384	*0006756757
1481	2193361	3248367641	38.4837627	11.3986045	*0006752194
1482	2196324	3254952168	38.4967530	11.4011695	'0006747638
1483	2199289	3261545587	38.5097390	11.4037332	*0006743088
1484	2202256	3268147904	38.5227206	11.4062959	'0006738544
1485	2205225	3274759125	38.5356977	11.4088574	'0006734007
1486	2208196	3281379256	38.5486705	11.4114177	*0006729474
1487	2211169	3288008303	38.5616389	11.4139769	0006724950
1488	2214144	3294646272	38.5746030	11.4165349	'0006720430
1489	2217121	3301293169	38.5875627	11.4190918	0006715917
1490	2220100	3307949000	38.6005181	11.4206476	*0006711409
1491	2223081	3314613771	38.6134691	11.4242022	*0006706908
1492	2226064	3321287488	38.6264158	11.4267556	*0006702413
1493	2229049	3327970157	38.6393582	11.4293079	0006697924
1494	2232036	3334661784	38.6522962	11.4318591	0006693440
1495	2235025	3341362375	38.6652299	11.4344092	*0006688963
1496 1497	2238016	3348071936	38.6781593	11.4369581	*0006684492
1497	2241009 2244004	3354790473	38.6910843	11.4395059	·0006680027
1498	2244004 2247001	3361517992 3368254499	38·7040050 38·7169214	11.4420525 11.4445980	*0006675567 *0006671114
1500	$\frac{2247001}{2250000}$	3375000000	38.7298335	11.44471424	*0006666667
1501	$\frac{2250000}{2253001}$		38.7427412	11.4471424	*0006662225
1502	2256004	3388518008	38.7556447	11.4522278	.0006657790
1503	2259009	3395290527	38.7685439	11.4547688	*0006553360
1504	2262016	3402072064	38.7814389	11.4573087	*0006648936
1505	2265025	3408862625	38.7943294	11.4598476	0006644518
1506		3415662216	38.8072158	11.4623850	.0006640106
1507		3422470843	38.8200978	11.4649215	0006635700
1508		3429288512	38.8329757	11.4674568	.0006631300
		322020012	30 0020101	77 101 1000	30000200
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,			or Decimizes,	OUBES, EQUARE	THE CODE TOOLS	5. 111
-	Number.	Squares.	Cubes.	√Roots.	% Roots.	Reciprocals.
	1509	2277081	3436115229	38.8458491	11.4699911	·00066269 05
	1510	2280100	3442951000	38.8587184	11.4725242	.0006622517
1	1511	2283121	3449795831	38.8715834	11.4750562	.0006618134
į	1512	2286144	3456649728	38.8844442	11.4775871	.0006613757
ı	1513	2289169	3463512697	38.8973006	11.4801169	.0006609385
Į	1514	2292196	3470384744	38.9101529	11.4826455	.0006605020
ļ	1515	2295225	3477265875	38.9230009	11.4851731	.0006600660
l	1516	2298256	3484156096	38.9358447	11.4876995	.0006596306
ŀ	1517	2301289	3491055413	33.9486841	11.4902249	.0006591958
	1518	2304324	3597963832	38.9615194	11.4927491	.0006587615
i	1519	2307361	3504881359	38.9743505	11.4952722	.0006583278
	1520	2310400	3511808000	38.9871774	11.4977942	.0006578947
ı	1521	2313441	3518743761	39.0000000	11.5003151	.0006574622
l	1522	2316484	3525688648	39.0128184	11.5028348	.0006570302
	1523	2319529	3532642667	39.0256326	11.5053535	.0006565988
-	1524	2322576	3539605824	39.0384426	11.5078711	.0006561680
-	1525	2325625	3546578125	39.0512483	11.5103876	.0006557377
	1526	2328676	355355957 6	39.0640499	11.5129030	.0006553080
	1527	2331729	3560558183	39.0768473	11.5154173	.0006548788
	1528	2334784	3567549552	39.0896406	11.5179305	.0006544503
	1529	2337841	3574558889	39.1024296	11.5204425	.0006540222
	1530	2340900	3581577000	39.1152144	11.5229535	.0006535948
	1 5 31	2343961	3588604291	39.1279951	11.5254634	.0006531679
i	1532	2347024	3595640768	39.1407716	11.5279722	.0006527415
	15 33	2350089	3602686437	39.1535439	11.5304799	.0006523157
ŀ	1534	2353156	3609741304	39.1663120	11.5329865	.0006518905
i	1535	2356225	3616805375	39.1790760	11.5354920	.0006514658
ļ	1536	2359296	3623878656	39.1918359	11.5379965	.0006510417
-	15 37	2362369	3630961153	39.2045915	11.5404998	.0006506181
ŀ	1538	2365444	3638052872	39.2173431	11.5430021	.0006501951
ŀ	1539	2368521	3645153819	39.2300905	11.5455033	.0006497726
Į	1540	2371600	3652264000	39.2428337	11.5480034	.0006493506
ŀ	1541	2374681	3657983421	39.2555728	11.5505025	.0006489293
ľ	.1542	2377764	3666512088	39.2683078	11.5530004	.0006485084
	1543	2380849	3673650007	39.2810387	11.5554972	.0006480881
	1544	2383936	3680797184	39.2937654	11.5579931	.0006476684
	1545	2387025	3687953625	39.3064880	11.5604878	0006472492
1	1546	2390116	3695119336	39.3192065	11.5629815	.0006468305
-	1547	2393209	3702294323	39.3319208	11.5654740	.0006464124
	1548	2396304	3709478592	39.3446311	11.5679655	.0006459948
	1549	2399401	3716672149	39.3573373	11.5704559	.0006455778
	1550	2402500	3723875000	39.3700394	11.5729453	.0006451613
	1551	2405601	3731087151	39.3827373	11.5754336	.0006447453
	1552	2408704	3738308608	39.3954312	11.5779208	.0006443299
	1553	2411809	3745539377	39.4081210	11.5804069	.0006439150
	1554	2414916	3752779464	39.4208067	11.5828919	.0006435006
	1555	2418025	3760028875	39.4334883	11.5853759	.0006430868
1	1556	2421136	3767287616	39.4461658	11.5878588	.0006426735
1	1557	2424249	3774555693	39.4588393	11.5903407	.0006422608
	1558	2427364	3781833112	39.4715087	11.5928215	.0006418485
J	1559	2430481	3789119879	39.4841740	11.5953013	.0006414368
-	1560	2433600	3796416000	39.4968353	11.5977799	.0006410256
-						
1						

		,			
Number	Squares.	Cubes.	√ Roots.	³ √ Roots.	Reciprocals.
1561	2436721	3803721481	39.5094925	11.6002576	.0006406150
1562	2439844	3811036328	39.5221457	11.6027342	.0006402049
1563	2442969	3818360547	39.5347948	11.6052097	•0006397953
1564	2446096	3825641444	39.5474399		
				11.6076841	•0006393862
1565	2449225	3833037125	39.5600809	11.6101575	.0006389776
1566	2452356	3840389496	39.5727179	11.6126299	.0006385696
1567	2455489	3847751263	39.5853508	11.6151012	.0006381621
1568	2458624	3855123432	39.5979797	11.6175715	•0006377551
1.569	2461761	3862503009	39.6106046	11.6200407	.0006373486
1570	2464900	3869883000	39.6232255	11.6225088	.0006369427
1571	2468041	3877292411	39.6358424	11.6249759	.0006365372
1572	2471184	3884701248	39.6484552	11.6274420	.0006361323
1573	2474329	3892119157	39.6610640	11.6299070	.0006357279
1574	2477476	3899547224	39.6736688	11.6323710	.0006353240
1575	2480625	3906984375	39.6862696	11.6348339	.0006349206
1576	2480025 2483776	3914430976	39.6988665		
			39.7114593	11.6372957	.0006345178
1577	2486929	3921887033		11.6397566	.0006341154
1578	2490084	3929352552	39.7240481	11.6422164	.0006337136
1579	2493241	3936827539	39.7366329	11.6446751	.0006333122
1580	2496400	3944312000	39.7492138	11.6471329	.0006329114
1581	2499561	3951805941	39.7617907	11.6495895	.0006325111
1582	2502724	3959309368	39.7743636	11.6520452	.0006321113
1583	2505889	3966822287	39.7869325	11.6544998	.0006317119
1584	2509056	3974344704	39.7994976	11.6569534	.0006313131
1585	2512225	3981876625	39.8120585	11.6594059	.0006309148
1586	2515396	3989418056	39.8246155	11.6618574	.0006305170
1587	2518569	3996969003	39.8371686	11.6643079	.0006301197
1588	2521744	4004529472	39.8497177	11.6667574	.0006297229
1589	2524921	4012099469	39.8622628	11.6692058	.0006293266
1590	2528100	4014679000	39.8748040	11.6716532	.0006289308
1591	2531281	4027268071	39.8873413	11.6740996	.0006285355
1592	2534464	4034866688	39.8998747	11.6765449	.0006281407
1593	2537649	4042474857	39.9124041	11.6789892	.0006277464
1594	2540836	4050092584	39.9249295	11.6814325	.0006273526
1595	2544025	4057719875	39.9374511	11.6838748	.0006269592
1596	2547216	4065356736	39.9499687	11.6863161	.0006265664
1597	2550409	4073003173	39.9624824	11.6887563	0006261741
1598	2553604	4080659192	39.9749922	11.6911955	·0006257822
1599	2556801	4088324799	39.9874980	11.6936337	.0006257822
1600	25600001	4096000000	40-0000000	11.6960709	·0006253909
1000	1	20000000	20 0000000	11 0900109	1000230000
			,—		i.
N.	N^2 .	N^3 .	\sqrt{N} .	$\sqrt[3]{N}$.	17
\sqrt{N} .	AT.	$\sqrt{N^3}$.	$\sqrt[4]{N}$.	6/	1
	N.	V No.		$\sqrt[6]{N}$.	$\frac{1}{N}$.
$\sqrt[3]{N}$.	$\sqrt[3]{N^2}$.	N.	$\sqrt[6]{N}$.	$\sqrt[9]{N}$.	$\frac{1}{\sqrt[3]{N}}$
N^2 .	N^4 .	$N^6.$	N.	$\sqrt[3]{N^2}$.	$\frac{1}{N^2}$.
N^3 .	N^{6} .	N^9 .	$\sqrt{N^3}$.	N.	$\frac{1}{N^3}$.
1	1	1	$\sqrt{\frac{1}{N}}$.	$\sqrt[3]{\frac{1}{N}}$	N^3
$\frac{1}{N}$.	$\frac{1}{N^2}$	$rac{1}{N^3}$.	\sqrt{N} .	\sqrt{N}	. N.

When the number contains Integer and Decimals.

Example 5. Required the Square Root of 7845'45? In the column of Squares you will find,

When the number of ciphers in the integer is even, the number of figures taken in the Square column must also be even; but when the number of figures in the integer is odd, the number taken in the Square column must also be odd.

To find the Cube Root of Numbers exceeding 1600.

Example 6. Required the Cube Root of 5694958? In the Cube column you will find,

$$\begin{array}{c} +5735339 = 179^{3} \\ -5694958 = 178^{3} \cdots \\ \hline 40381 \ \text{divided by} \end{array} \begin{array}{c} +5735339 = 179^{3}. \\ -5639752 = 178^{3}. \\ \hline 95587 = 000 \cdot 4225, \\ \hline \sqrt[3]{5694958} = 178 \cdot 4225 \ \text{nearly.} \end{array}$$

When the number contains Integer and Decimals.

Example 7. Required the Cube Root of 4186.586? In the column of Cubes you will find,

$$\begin{array}{c} +4251 \cdot 528 = 16 \cdot 2^{3} \\ -4186 \cdot 585 = 16 \cdot 1^{3} \cdots \\ \hline 64942 & 4251 \cdot 528 = 16 \cdot 2^{3} \\ \hline 4173 \cdot 281 = 16 \cdot 1^{3} \\ \hline 78247 = 00 \cdot 083 \\ \hline \sqrt[3]{4186 \cdot 586} = 16 \cdot 183 \text{ nearly.} \end{array}$$

The following notice must be particularly attended to, when extracting Cube Root of numbers with decimals.

2 ciphers in the integer must be 5, 8, or 11 ciphers in the Cube column.

3	. '66	66	166	3, 6, or	9	66	66
4	66	66	66	4, or	7	66	66
4 5 6 7	[†] 66	66	66		8	66	66
6	166	66	66	6, or	9	66	66
7	'66	66	6.			66	66

Example 8. Required the Cube Root of 61358.75? In the Cube column and 8 figures you will find,

$$\begin{array}{c} +61629 \cdot 875 = 395^{3} \\ -61358 \cdot 750 = 3943 \cdots \\ \hline 271 \cdot 125 & \text{divided by} \end{array} \begin{array}{c} +61629875 = 39 \cdot 5^{3} \\ -61162984 = 39 \cdot 4^{3} \\ \hline 466891 = 00 \cdot 05807 \\ \hline \sqrt[3]{6135} \cdot 75 = 39 \cdot 45807. \end{array}$$

To find the Fourth Root.

Rule. Extract the Square Root of the number as before described, and of that root extract the Square Root again, then the last is the Fourth root of the number.

Example 9. Required the fourth root of 2469781?

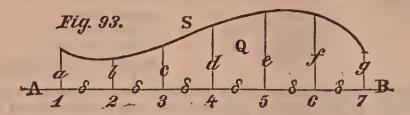
$$\sqrt[4]{2469781} = \sqrt{\sqrt{2469781}} = \sqrt{1571.4463} = 39.6467$$
, the answer.

To find the Sixth Root.

Rule. Find the Cube Root of the number as before described, and of that root extract the Square Root, and then the last is the Sixth root of the number.

To find the Area and Solidity of Irregular Figures.

Chapman's rule in the construction of ships, Stockholm, 1775.



Divide the base A B into any even number of equal parts. $\delta =$ distance between the ordinates; Q = area of the projecting figure.

$$Q = \frac{\delta}{3}(a + 4b + 2c + 4d + 2e + 4f + g). \qquad . \qquad . \qquad 1.$$

Suppose this area to revolve around the axis A B and form a solid figure like a handle, an urn or a gun; then the solidity C of the figure will be—

The practical calculation of these formulas is set up as in table for Formula 1. Suppose a = 1.25, b = 1.15, c = 1.52, d = 1.86, e = 2, f = 1.77, and g = 1.20.

The distance between the ordinates being $\delta = 2$, then the area will be, $Q = \frac{2}{3} \times 28.51 = 19$ square of

whatever measure used.

The convex surface S of the figure will be, $S=2\pi Q$ = $2 \times 3.14 \times 19 = 119.3$ square.

Ord	inates.	Mult.	Product.
a	1.25	1	1.25
b	1.15	4	4.50
C	1.52	2	3.04
\boldsymbol{d}	1.86	4	7.44
e	2.	2	4.00
f	1.77	4	7.08
g	1.20	1	1.20
Q	9.506	1/3	28.51

This rule can also be employed in calculating the cubic contents of earth-work in excavations and embankments, in which the ordinates are expressed in areas of the sections.

Suppose a = 36 square feet, yards, metres, or whatever unit of measure, b = 30, c = 42, d = 56, e = 84, f = 72, and g = 50, the distance between the sections being, say, 50 feet. The calculation is set up as in the preceding table, namely:

set up as in the preceding table, namely: Volume $C = 50 \times 323.3 = 1616.5$ cubics of what-

ever unit of measure used.

Ord	inates.	Mult.	Product.
a	36	1	36
b	30	4	120
C	42	2	84
d	56	$\frac{4}{2}$	224
e	84		168
f	72	4	288
g	50	1	50
C	323.3	1/3	970

This rule is universally employed for calculating the areas of water-lines, cross-sections and cubic contents of displacement in ships (known as Simpson's rule).

When the cubic content is required between each section, calculate it as explained in Excavation and Embankment.

Surface of Revolution.

The surface generated by a line revolving around an axis, is equal to the length of the line multiplied by the circumference of its centre of gravity.

N. B. The line, whether straight or curved, must be in the same plane as the axis.

Solidity of Revolution.

The solidity generated by a plane revolving around an axis, is equal to the area of the plane multiplied by the circumference of its centre of gravity.

N. B. The revolving plane must be in the same plane as the axis.

1000	.7.		0.73		1	47.				1
Ang		1. 7.	2. 6.	nates. 3. 5.	4, h.	Angle.	1. 7.	Ordi	nates. 3. 5 .	4. h.
	10				i					
	2	·00084 ·00191	00164	.00193	.00218		05313	08932	11063	11773
	3	.00299	00527	·00409 ·00561	00436 00659		05422	09130	11318	12003
	4	00299	.00522	00301	00839		.05531 .05646	$09308 \\ 09487$	11510	12235
	5	00382	.00818	.01023	.01091		05040	09437	11731	12466
	6	00437	.00928	01023	.01309		05700	.09853	·11950 ·12170	12698
	7	.00675	00928	.01432	01509		05989	10037	12170	·12932 ·13162
	8	.00764		.01639	.01746		03333	10037	12593	13102
	9	0.0845	.01474	.01842	.01964	61	06261	10220	12840	13631
1		00955	.01637	.02047	.02183		06331	10421	13054	·13866
l i		.01053	.01801	.02250	.02402		06451	.10781	13034	.14101
1 is			.01965	.02456	.02620		.06570	10964	13505	•14337
lî:	3		.02129	02662	.02839		.06681	11101	13765	·14573
1 4		.01284	.02271	.02861	.03058		.06805	11342	13956	.14810
11.			.02461	.03081	.03282		.06914	.11532	14181	.15048
11		.01535	.02625	.03277	.03496		.07040	.11721	•14409	15286
	7	.01630	.02789	.03484	.03715		.07168	·11912	.14637	15526
118		.01730	.02956	.03693	.03935	_	.07284	.12103	.14864	15765
1 :			.03125	.03996	.04154		.07407	·12294	15087	·16005
20	0	.01922	.03286	.04103	.04374	72	.07535	·12485	15323	.16245
2		.02022	.03453	.04309	.04594	73	.07656	·12685	15555	.16487
22		·0211 9	.03619	.04522	•04814	74	.07784	.12877	15785	·16729
	3	·0221 5	.03787	.04720	.05034	75	.07912	·13078	·16016	·16972
24		.02311	.03934	·04930	05255	76	.08040	13292	16247	·17216
2		.02413	.04117	.05138	.05475	77	.08168	13472	·16482	·17460
20		$\cdot 02508$.04283	.05346	.05696	78	.08297	13670	16716	·17706
2		.02610	.04457	.05552	.05917	79	.08426	13868	16951	·17951
28		.02708	.04621	.05761	.06139	80	.08560	.14070	17187	·18198
29		.02813	•04793	.05970	.06361	81	.08695	.14274	17423	18445
30		02911	.04970	06188	.06582	82	.08829	14477	17660	18694
3		·03005 ·03107	.05125	-06386	06804 07027	83	.08944	•14681	17901	.18943
33		03191	·05298 ·05464	·06596 ·06806	07027	84	$09105 \ 09235$	·14888 ·15120	·18140 ·18379	·19193 ·19444
34		.03310	.05637	.07016	.07477	85	09233	15120	18622	19444
3		.03412	.05804	.07424	.07695	86	.09518	15509	18865	19946
3		.03515	.05992	0.07452	.07919	88	.09660	.15756	19108	20201
3		.03616	.06147	.07646	.08143		.09780	.15931	19350	20555
38		.03718	.06327	.07858	.08367		.09944	.16144	19597	20710
39	_	.03821	.06492	.08069	.08591		.10098	·16359	19842	.20966
4	0	.03905	.06631	.08243	.08816		10240	·16575	20092	·21223
4	1	.04030	.06836	.08494	.09041		·10384	·16787	20338	·21481
4:	2	·04133	.07012	.08707	.09266	94	·10537	17005	20589	·21740
4:	3	.04241	.07182	.08920	.09492		·10692	17224	20837	·22000
4.4		.04363	07353	.09130	.09719	0 0	·10851	·17444	21091	•22262
44	_	0-522	.07531	.09346	.09945		10997	17666	.21342	.22523
4	_	.04556	.07706	.09562	.10172	00	11150	17888	21596	•22786
4		.04682	.07894	.09790	10400		11310	18111	22800	23050
48	_	.04833	08059	.09991	10627	100	11468	·18354 ·18500	22107	•23315
4 9	_	.04879	.08236	.00207	110856	TOT	·11626 ·11791	18793	22364 22623	·23596 ·23848
50		.04982	08413 08593	·00422 ·10639	11085		·11791 ·11959	19021	22876	23848
5	- /	05096 05204	·08593 ·08768	10855	·11314 ·11543	103	12116	19021	23147	·24386
5	٥	00204	00100	10000	11040	104	22110	10200	20131	27000

RAIL ROAD CURVES.

When Railroads are to be connected by curves, we commonly have given the distance (chord c,) between the two ends oo of the tracks, and the tangential By these the curve is to be constructed.

Example 1. Fig. 94. The chord C = 168 feet, and the tangential angle $v = 19^{\circ} 30'$. Required the centre angle w =, and the radius R =?

 $w = 2(19^{\circ}30') = 39^{\circ}$. $R = {}^{39}k \ c = 1.4979 \times 168 = 251.647$ feet. k = See Table for Segments, &c., of a circle.

By Tangential Angles.

The curve to be laid out by the three tangential angles ror, ron, and noo, each angle = $\frac{1}{3}v = 6^{\circ} 30'$. Required the chord r = ?

The centre angle for the chord r is

 $2 \times (6^{\circ} 30') = 13^{\circ}$, and $r = {}^{13}k R = 0.2264 \times 251.647 = 56.974$ feet.

By Angles of Deflexion.

Divide the centre angle w into an even number of parts = z. Set off at o the angle z = r o n, and bisect it into r o r and r o n,—find the chord r, and sub-chord a, and continue as shown by Figure.

Example 2. Fig. 94. The tangential angle $v = 78^{\circ}$, and the chord C = 638feet. Required the centre-angle w=? Radius R=? Chord r=? and the subchord a = ?

 $w = 2 \times 78^{\circ} = 156^{\circ}$. $R = 156 k c = 0.51117 \times 638 = 326.126$ feet.

Let the curve be laid out by 6 angles of deflexion, and $z = \frac{1}{6} \times 156^{\circ} = 26^{\circ}$, and $r = 26k R = 0.4499 \times 326.126 = 146.73$ feet.

By Ordinates.

 $a = {}^{26}k \ r = 0.4495 \times 146.73 = 66.012$ feet.

The chord C = 368 feet, and $v = 36^{\circ}$. Required the Example 3. Fig. 95. height h=?

 $h = \frac{1}{2}C(\csc v - \cot v).$

 $- \cos ec.36^{\circ} = 1.70130$ From $-\cot .36^{\circ} = 1.37638$ Subtract -

 $h = 0.32492 \times 184 = 59.785$ feet. The height

At x = 92 feet from h. Required the ordinate y?

$$\sin z = \frac{2 \times 92 \sin .36^{\circ}}{368} = 0.2938926 = \sin .17^{\circ} 6'.$$

$$y = \frac{1}{4} \times 368 \left(\frac{\cos .17^{\circ} 6'}{\sin .36^{\circ}} - \cot .36^{\circ} \right) = 45.9448 \text{ feet.}$$

By Sub-Chords.

Example 4. Fig. 96. The ends o and o of the tracks form different angles we and W to the chord C, and therefore must be connected by two curves of different radii, R and r. The chord C = 869 feet, $w = 38^{\circ}$, and $W = 86^{\circ}$. Required the distance from o to the height h, n=? sub-chord b=? sub-chord a=?radii R and r = ?

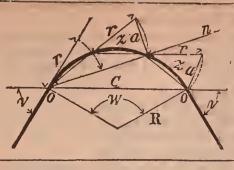
$$v = \frac{1}{8} \times 38^{\circ} = 19^{\circ}$$
, and $V = \frac{1}{8} \times 86^{\circ} = 43^{\circ}$.
 $n = \frac{869 \text{ tan.} 19^{\circ}}{\text{tan.} 19^{\circ} + \text{tan.} 43^{\circ}} = 234^{\circ}35 \text{ feet.}$

 $R = 38ka = 1.5358 \times 671.21 = 1030.2$ ft. $b = 234.35 \text{ sec.} 43^{\circ} = 320.42 \text{ feet.}$ $a = \sec .19^{\circ}(869 - 234.35) = 671.21 \text{ ft.}$ $r = 86kb = 0.73314 \times 320.42 = 234.91 \text{ ft.}$

By Eight Ordinates.

Example 5. Fig. 100. Required 8 ordinates for a curve of chord C = 710 feet and the centre angle $w = 69^{\circ}$? (See Table on the preceding page.)

1st and 7th Ordinates $0.07168 \times 710 = 50.8928$ feet. 2nd " 6th 3rd " 5th $0.11912 \times 710 = 84.5752$ 66 66 $0.14637 \times 710 = 103.9227$ $0.15526 \times 710 = 110.2346$ 66 4th or height h

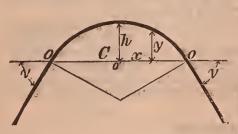


94.

By angles of deflexion.

$$w = 2v$$
, $R = {}^{w}k C = {}^{\frac{1}{2}}C$ cosec.v.

$$r = {}^{z}k R$$
, $a = {}^{z}k r = 2r \sin \frac{1}{2}z$.



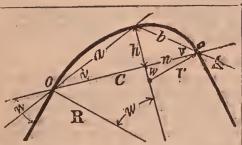
95.

By Ordinates:

$$h = \frac{1}{2}C(\csc v - \cot v).$$

$$y = \frac{1}{2}C\left(\frac{\cos z}{\sin v} - \cot v\right),\,$$

$$\sin z = \frac{2x \sin v}{C}$$



By Sub-chords. 96.

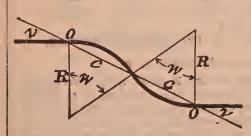
$$n = \frac{C \tan v}{\tan v + \tan v}, \quad h = n \tan v,$$

$$b = n \sec V,$$
 $w = 2v$

$$a = \sec v(C - n),$$

W = 2V'

$$a = \sec v(C - n)$$

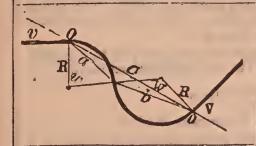


97.

Parallel tracks by a reverse curve.

Formulas same as above.

The length o o = 2c, length of a circle arc l = 0.035v R.



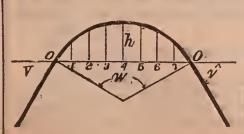
99.

The greatest radius in a reverse curve.

$$w = \frac{1}{2}(V+3v), \quad W = w+V-v,$$

$$a = {}^{w}k R, \quad b = {}^{w}k R,$$

 $R = C \sec w(\sin V - \sqrt{\sin^2 V - \cos^2 w}).$



100.

Curve by 8 Ordinates.

The ordinates are calculated in the accompanying Table, the chord C=1 or

If the angle w is large, or there be some obstacle on the chord C, find the height hand lay out the curve by two or more sets of 8 ordinates.

By Ordinates and Subchords.

Example 6. Fig. 101. The tangents t being prolonged to where they meet at a, divide that angle into two equal parts, say $W=75^{\circ}$. Required the tangents t=? external secant S=? chords C=? and the angle w=?Radius of the curve R=1500 feet.

> $t = R \cot .75^{\circ} = 1500 \times 0.26794 = 401.91 \text{ feet.}$ Centre angle $w=90-75^{\circ}=15^{\circ}$ for half the curve. $S=R (\sec .15^{\circ}-1) = 1500 (1.0352 - 1) = 52.8 \text{ feet.}$ The chords C=k $R=0.26104\times1500=391.56$ feet.

Measure off from a the tangents and the external secant.

Draw the chords CC, and divide them each into eight equal parts. In the table of ordinates under $w=15^{\circ}$ will be found the

1st. 7th. $0.01438 \times 391.56 = 5.631$, 3rd. 5th. $0.03081 \times 391.56 = 12.063$, $0.03282 \times 39.56 = 12.851$, 2nd. 6th. $0.02461 \times 391.56 = 9.636$, 4th.

Thus by only four multiplications, 16 ordinates in the curve is obtained. Should there be any obstacles for the chords C. C. as is often the case in excavations and on embankments, a line can be drawn further in on the track parallel to the chord and the ordinates obtained by subtraction, readily understood by the Engineer.

Ellipse by Ordinates.

By this arrangement ellipses can be constructed of any proportions. One of the two axes is divided into 16 equal parts. The ordinates drawn and calculated as shown by the figure 102.

Parallel Tracks by a Semi-Ellipse.

Example 7. Fig. 103. The instrument placed at b and b', divide the angles W and w each into two equal parts, prolong the chords which will meet at a, a point in the curve. Divide the chords each into eight equal parts, and draw the ordinates parallel to the tracks as shown in the figure. The grand chord C is the unit for calculating the ordinates, which latter are alike on both the chords c', c''.

5th. 1st 2nd. 3rd. 4th. 6th. 7th. 0.1795C 0.2058C0.2029 C 0·1830*C* 0·1477C 0·1091C 0.0586C.

Suppose the grand chord to be C=2050 feet.

Required the length of the 6th ordinate? 0.1091×2050-223.655 feet.

Tracks not Parallel by Elliptic, arc.

Example 8. Fig. 104. Divide the angles W and w each into two equal parts, prolong the subchords until they intersect one another at a, which is a point in the curve. Divide the chord C into eight equal parts, join a with the 4th division and draw the other ordinates parallel thereto. Suppose the angles are $W=18^{\circ}$ and $w=12^{\circ}$, the centre angle will be 30° for which the ordinates are to be calculated from the table. The chord

C=125 feet. Required the 3rd and 5th ordinates? $0.06188 \times 125 = 7.335$ feet.

Springing of Rails.

Example 9. Fig. 105. A rail of L=21 feet is to be curved to a radius of R=1250 feet. Required the spring S=1 in sixteenths of an inch.

$$S = \frac{24 \times 21^2}{1250} = 8.47$$
 sixteenths.

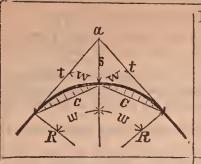
Super Elevation of the External Rail.

Example 10. Fig. 106. A train running M=30 miles per hour on a curve of R=1550 feet radii, the gauge of the track is G=5 feet. Required the angle of inclination v=? and the super elevation of the external rail $h=\overline{3}$

$$tan.v = \frac{30^2}{15 \times 1550} = 0.0387 = tan. 2^{\circ} 13'.$$

 $h=G \sin .1^{\circ} 2! = 5 \times 0.02356 = 0.1178 \text{ feet, or nearly } 1\frac{1}{6} \text{ inches.}$

It is practically impossible to lay the super elevation to suit the different speeds of trains. If a mean speed is taken, the faster passenger trains will wear the outer rail, and the slow or freight train will wear the inner rail

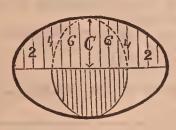


101. By ordinates and subchords.

 $t = R \cot W = R \tan w, W = 90 - w,$

S = R (sec. w - 1) = R (cosec. W - 1)

C=k R. For k, see table of segments.

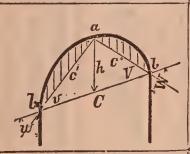


Ellipse by ordinates.

 $1 = 0.4840 C \qquad 5 = 0.9204 C$

2 = 0.6616 C * 6 = 0.9682 C3 = 0.7808 C 7 = 0.9922 C

4 = 0.8660C 8 = C the unit.



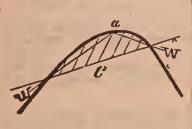
103.

Parallel tracks by elliptic curve:

 $h = \frac{1}{2} C. \quad w = 2 v. \quad W = 2 V,$

 $c' = \frac{C \sin W}{2 \sin v}, \quad c'' = \frac{C \sin W}{2 \sin V},$

See example for ordinates.



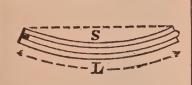
104.

102.

Tracks not parallel by elliptic arc.

Angle of the arc = W + w.

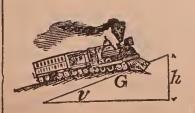
Ordinates to be calculated from the table.



Spring of Rails.

$$S = \frac{1.5 L^2}{R} = \text{spring in inches.}$$

$$S = \frac{24 L^2}{R} = 16 \text{ths of an inch.}$$



106.

100.

Inclination of tracks in curves:

$$\tan v = \frac{M^2}{15 R}, \quad \hbar = G \sin v.$$

Meaning of letters, see example.

Explanation of the Figures on the Following Page.

The most correct and positive ways of laying out railway curves are by external secant or by sinus-versus either to be employed, as the ground permits. The

operation is well understood by the figures 107 and 108.

The natural secant and sinus-versus are found in the trigonometrical tables. Subtract 1 from the natural secant, and the remainder will be the external secant. Multiply the external secant by the assumed radius, and the product is the external secant s in the same unit of measure as the radius.

The centre angle is divided by 2 and 2 as many times as may be required for

setting out the curve.

Fig. 107 is used when there are obstacles inside the curve, and Fig. 108 when the outside is inaccessible. The sinus-versus in the tables, multiplied by the assumed radius, will be the height of the curve above the chord.

When the inside of the curve is obstructed, and the point T of intersection is

also inaccessible, then the curve can be laid out as illustrated by Fig. 109.

Fig. 110 illustrates how to lay out a curve by chords of 100 feet.

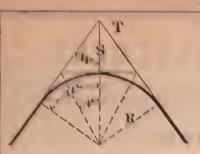
Tangential angles for a chord of c = 100 feet, and different radii R from 500 feet to 3 miles (fig. 110).

R.	tan. angle.	\parallel R.	tan. angle.	R.	tan. angle.
Feet.	0 , "	Feet.	0 , ",	Miles.	0 1 "
500	5. 43 46	3000	0 57 18	0.125	4 20 26
600	4 46 29	3500	0 49 6	0.25	2 10 13
700	4 5 33	4000	0 42 58	0.5	1 5 6
800	3 34 52	4500	0 38 12	0.75	0 43 25
900	3 10 59	5000	0 34 23	1 mile.	0 32 33
1000	2 51 53	5500	0 31 15	1.25	. 0 26 2
1100	2 36 16	6000	0 28 39	1.5	0 21: 42
1200	2 23 15	7000	0 24 34	1.75	0 18 42
1500	1 54 35	8000	0 21 30	2	0 16 17
2000	1 25 56	9000	0 19 6	21/2	0 13 1
2500	1 8 46	10000	17 12	3 -	0 10 51

Fig. 116 illustrates a section of a cut or embankment through sloping ground. The meaning of letters is the same as that on the following pages on excavation and embankment.

Fig. 117, Sidings for parallel tracks.—D = distance over tangent points; W = width between centres of tracks, and R = radius of curvature; v = angle of frogplates.

The different operations of laying out the curves are so well understood by railroad engineers that it is considered unnecessary to enter into detailed description. The formulas and figures are intended only as a memorandum.



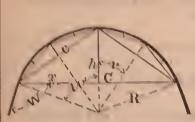
107.

By external secants.

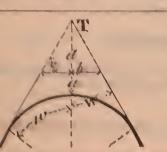
External secant $s = R(\sec w - 1)$.

W = 90 - w; w = 90 - W, w = 2v.

tangent $t = R \cot W = R \tan w$.



108. $W = 180 \frac{By \text{ sinus-versus.}}{W}. \quad c = 2R \text{ sin.w.}$ $R = \frac{C}{2 \sin w}. \quad c = 2R \sin w.$ sinus-versus $h = R \sin w.$ $x = 90 - \frac{W}{2}.$

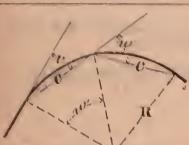


109. When the point T is inaccessible.

$$w = 90 - v. \qquad b = 2d \text{ cot.} v.$$

$$a + d = R$$
 see.w. $d = \frac{1}{2}b \tan v$.

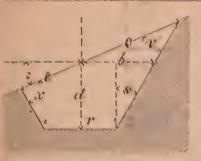
$$a = R \sec w - \frac{1}{2}b \tan v$$
.



110. Tangential angle for a chord of c = 100 feet, and different radii R from 500 feet to 3 miles.

$$w = 2v, \qquad \sin \frac{1}{2}w = \frac{c}{2R}.$$

$$R = \frac{c}{2 \sin \frac{1}{2} w}$$
. $c = 2R \sin \frac{1}{2} w$.



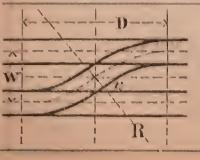
111. Railway out or embankment through side slopes.

$$b = \frac{r}{2} + d \tan s. \quad c = \frac{b \sin(90 + 2z - s)}{\sin(90 - z - s)}$$

$$x = 90 + z - s. \quad v = 90 - z - s.$$

$$b \cos s$$

$$e = \frac{\sin(90 + z - s)}{\sin(4 \sin s \sec z + r)}.$$



112. Sidings of parallel tracks.

$$D = 2\sqrt{W(R - \frac{1}{2}W)}.$$

$$R = \frac{D}{4W} + \frac{1}{2}W. \qquad \sin v = \frac{D}{2R}.$$

EXCAVATION AND EMBANKMENT.

Example 1. The Road-way of an excavated channel is r=15 feet, the depth D=9 feet, and the breadth at the top $b=46\frac{1}{6}$ feet. Require the slope S=?

Formula 6.
$$S = \frac{46.5 - 15}{2 \times 9} = 1.75 \text{ or } 1\frac{3}{4} \text{ to } 1$$

Example 2. The Road way is to be r = 15, D = 18, and the slope $S = 1\frac{1}{4}$, Require the breadth b = 2 and the cross-section A = 2

Formula 4.
$$b = 2 \times 18 \times 1.25 + 15 = 60$$
 feet.

Formula 7.
$$A = \frac{18}{2} (60 + 15) = 675 \text{ square feet.}$$

Example 3. The Road-way is to be r = 16 feet, the slope $S = \frac{1}{2}$, and the depth D = 11 feet. Required the area of Cross-section A = ?

Formula 9.
$$A = 11 (11 \times 13 + r) = 357.5$$
 square feet.

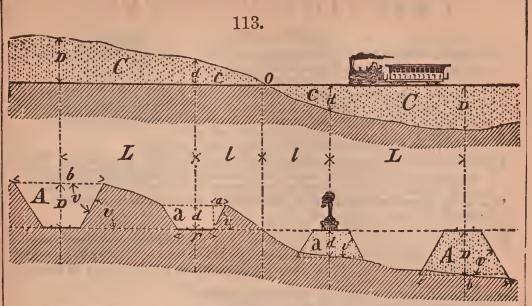
Example 4. The Road-way r = 18 feet, slope $S = 1\frac{1}{4}$, d = 14 feet 6 inches, and the length from o is l = 55 feet. Required the cubic contents $\mathbf{c} = ?$

Formula 11. $\mathbf{c} = 55 \times 14.5 \left(\frac{14.5 \times 1.25}{3} + \frac{18}{2} \right) = 11995.676$ cubic feet, divided by 27 = 444.28 cubic yards.

Example 5. The Road-way is r=16 feet, slope $S=1\frac{1}{6}$ feet, D=17.5, d=7.4 and the length L=100 feet. Required the cubic content C=?

Formula 12.
$$C = 100 \left[\frac{1}{8} \left(\frac{17.5^2 + 7.4^2 + 17.5 \times 7.4}{3} \right) + \frac{16}{2} \left(17.5 + 7.4 \right) \right]$$
 = 44445 cubic feet, or 1645.4 cubic yards,

The computation is executed thus.



Letters in the Formulas correspond with the Figure.

$$S = \cot v, -1.$$

$$a = D S, -2.$$

$$a = \frac{d}{2}(b+r), -8.$$

$$a = D \cot v, -3.$$

$$b = 2DS + r, -4.$$

$$S = \frac{a}{D}, -5.$$

$$S = \frac{b-r}{2D}, -5.$$

$$S = \frac{b-r}{2D}, -6.$$

$$A = \frac{D}{2}(b+r), -9.$$

$$A = D(DS + r), -9.$$

$$C = l d(\frac{dS}{3} + \frac{r}{2}), -11.$$

$$C = L \left[S(\frac{D^2 + d^2 + Dd}{3}) + \frac{r}{2}(D+d)\right]. -12.$$

Letters Denote,

A and a = Cross-Sections in square feet, of the excavated channel or embankment.

D and d =depth in feet, of the Sections. r =width in feet of the Road-Way.

b =Base in feet of the embankment, or top breadth of the channel.

L =length in feet, between the two Sections A and a.

l = length in feet, from the Section a to the point o where the ground is level with the road.

C = cubic contents in feet, between A and a.

c = cubic contents in feet, between a and o.

S = slope of the sides. The slope is commonly given in proportions, thus: "Slope = $1\frac{1}{2}$ to 1," which means, that the side slopes $1\frac{1}{2}$ feet horizontally for 1 fcot vertical.

v = angle of the slope.

TRACTION ON ROADS.

Letters denote.

F = tractive force in pound avoir., necessary to overcome the rolling friction, and ascending inclined plains.

M = miles per hour of the train or force F.
 T = weight of the load in tons, including the weight of the carriages.
 On rail-roads T includes the weight of the locomotive and tender.

t = weight of the locomotive resting on the driving wheels in tons.

h =vertical rise in feet per 100 of inclined roads.

b =base in feet per 100 of the inclined road or plain.

k = tractive coefficient in pound per ton of the load T, as noted in the accompanying Table, under the different conditions of the road.

A = area of one of the two cylinder pistons in a locomotive, in sq. in.

P = mean pressure of steam in lbs. per sq. in. on cylinder pistons.

S =stroke of pistons in feet.

D = diameter of driving wheel in feet.

H = actual horse power of a locomotive or the power necessary for the load. About 25 per cent. is allowed for friction and working pumps. f = adherence coefficient of the driving wheels to the rails, in pounds per ton of the weight t.

n = revolutions per minute of driving wheels.

d =continued working hours of a horse.

v =velocity in feet per second. t' =weight of a horse in pounds.

Example 11. Fig. 114: The area of one of the two cylinder pistons in a locomotive is A=314 square inches, stroke of piston P=2 feet, meanpressure P=80 lbs. per square inch. Driving wheels D=4 feet diameter. Required the tractive force F=3 of a locomotive.

$$F = \frac{314 \times 2 \times 80}{4} = 12560$$
 lbs. the answer.

The adhesive force of the driving wheels to the rails, ft, must always be greater than the retractive force of the locomotive, otherwise the

wheels will slip on the track.

Example 12. Fig. 115. A locomotive of t=15 tons on an inclined plain rising h=10 feet, and the base b=99.5 feet per 100. f=560, other dimensions being the same as in the preceding example. Required the tractive, retractive and adhesive forces?

Tractive,
$$F = \frac{314 \times 2 \times 80}{4} - 22.4 \times 15 \times 10 = 9200 \text{ lbs.}$$
Retractive, $F = 22.4 \times 15 \times 10 = 3360 \text{ lbs.}$
Adhesive, $F = \frac{560 \times 15 \times 99.5}{100} = 8358 \text{ lbs.}$

Consequently the locomotive can ascend the inclined plain with a tractive force of 8358 3360=4998 lbs., without slip in the driving wheels. Example 13. Fig. 116. A train of T=200 tons is to be drawn M=20 miles per hour on a horizontal track in good condition, k=4. Required retractive force F=?

$$F = 200 (4 + \sqrt{20}) = 1694.4 \text{ lbs. the answer.}$$

Example 14. Fig. 117. A train of T=150 tons is to be drawn up an inclined plain of h=9 feet in 100, with a speed of M=16 miles per hour, k=4. Required the necessary horse power of the locomotive H=?

$$H = \frac{16 \times 150}{375} (22.4 \times 9 + 4 + \sqrt{16}) = 1342.144 \text{ horses.}$$

Example 15. Fig. 118. Required the tractive ability F=? of a horse, running M=7 miles per hour, in d=4 continued hours.

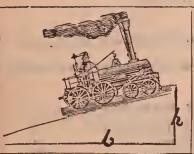
$$F = \frac{375}{7/4} = 26.8$$
 lbs. the answer.



114.

$$F = \frac{A S P}{D}, \quad n = \frac{28 M}{D},$$

$$H = \frac{A S P n}{11000} = \frac{A S P M}{376 D}.$$
Adhesive force = $f t$.



115.

$$\dot{F} = \frac{A \ S \ P}{D} - 22.4th. \quad M = \frac{D \ n}{28}$$

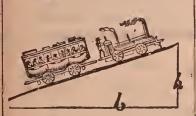
Adhesive, $\frac{ftb}{100} > 22.4th$. retractive.



116.

$$F = T(k + \sqrt{M})$$
. < $ft = Adhesive$.

$$H = \frac{MT}{375}(k + \sqrt{M}),$$



117.

$$F = T(22.4 h + k + \sqrt{M}). < \frac{f t b}{100} = Ad.$$

$$H = \frac{M T}{375} (22.4 h + k + \sqrt{M}).$$



118.

$$F = T(k + \sqrt{M}). \qquad v = 1.466 M.$$

$$F = \frac{550}{v \sqrt{d}} = \frac{375}{M\sqrt{d}}$$
 ability of a horse.



119.

$$F = T(22.4 h + k + \sqrt{M}).$$

$$F = \frac{550}{v \sqrt{d}} - \frac{t'h}{100} \quad M = 0.6821 \ v.$$

Example 16. Fig. 145. Required, the tractive force F=? of a load I=5.25 tons to be drawn h=2 miles per hour up a turnpike of h=9 feet in 100, the road being newly laid with coarse gravel k=50?

$$F = 5.25(22.4 \times 9 + 50 + \sqrt{2}) = 1328.30 \text{ lbs.}$$

Suppose a horse to weigh t' = 1000 lbs., working continually in d = 1 hour up the turnpike. Required, the tractive ability F = ? per horse?

$$F = \frac{375}{2\sqrt{1}} - \frac{1000 \times 9}{100} = 97.5 \text{ lbs.}$$

Number of horses $=\frac{1328.25}{97.5}=13.6$, say 14 horses, which will be necessary for the load under the mentioned circumstances. In these examples it is necessary to take M>1, and d>1.

. Traction Coefficient at very Slow Spec	ed.
On railroads in good condition, carriage axles well lubricated,	
On railroads under ordinary, not very good condition,	
On very smooth stone pavement,	
On ordinary street pavements in good condition,	
On street pavements and turnpikes,	
On turnpikes new laid with coarse gravel and broken stones,	
On common roads in bad condition,	. 1
On natural loose ground or sand	5
Adhamana Caaffaiant	
Adherence Coefficient.	
On rails of maximum dryness,	. 6
" very dry,	5
" under ordinary circumstances,	. 4
" in wet weather,	3
" with snow or frost	. 2

In railway curves the retractive force is augmented so many per cent. as the whole train occupies degrees in the curve.

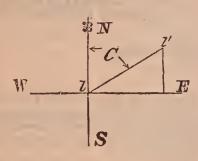
Railway Gauges. Ga	uge
The most general gauge in coal mines,	6
Rio Grande and Texas,	6
The most general gauge in the United States, England, France, Prussia, Sweden, Mexico, Chili and Peru,	81/2
The compromised gauge,	9 10
In the Southern States and in Russia,	3
Louisiana and Texas, also in Canada and India, 5	6
Great Western in England,	

Rain-fall in Inches at Different Seasons of the Year.

Locations.	Year.	Spring.	Summer.	Fall.	Winter.			
Nishny, Taguilsk, Russia,	18.26	3.35	9.28	3.70	1.93			
Tobolsk, Siberia,	17.76	2.29	9.05	4.02	2.40			
Nertchinsk, Asia,	18.13	2.32	10.5	4.96	0.35			
Yakoutsk, East Siberia,	10.25	1.46	3.35	3,59	1.85			
Peking, China,	23.88	2.17	17.7	3.50	0.51			
Macao, Quang-tong,	67.81	18.8	28.0	17.7	3.31			
Saigon, India,	62.80	5.86	28.9	28.0	0.04			
Yokohama, Japan,	35.02	7.52	12.0	15.2	0.295			
Manilla, Philip. Islands,	71.31	4.77	34.1	25.6	4.84			
For rain-fall, see page 359.								

TRAVERSE SAILING AND SURVEYING.

To navigate a vessel upon the supposition that the earth is a level plane, on which the meridians are drawn north and south, parallel with each other; and the parallels east and west, at right-angles to the former.



The line NS represents a meridian north and south, the line WE represents a parallel east and west.

A ship in l sailing in the direction of ll', and having reached l', it is required to know her position to the point l, which is measured by the line ll', and the angle Nll'; and imagined by the lines l a and a l'

While the vessel is running from l to l', the distance is measured by the log and time; and the course Nll' is measured by the compass commonly expressed in points.

These four quantities bear the following names.

 $d = l \ l'$, dislance from l to l' in miles. $C = N l \ l'$, course, or points from the meridian.

n = la, departure or difference in longitudes, in miles.

u = a l', difference in latitudes, in miles.

l = latitude in degrees.

L = difference in longitude, in degrees or time.

Traverse Formulas.

	-	1, 2, 3,	$\cos l = \frac{u \tan C}{60L}, -$	15,
$ \mathfrak{d} = \sqrt{d^2 - u^2}, u = d \cos . C, - u = \mathfrak{d} \cot . C, - $	-	4, 5, 6,	$L = \frac{\mathfrak{v}}{60 \cos l},$	16,
$u = \frac{60L \cos .l}{\tan .C},$	-	7,	$L = \frac{d \sin \cdot C}{60 \cos \cdot l}$,	17,
$u=\sqrt{d^2-\mathfrak{d}^2},$	•	8,	$L = \frac{u \tan C}{60 \cos l},$	18,
$d=\frac{v}{\sin C},$	•	9,		
$d=\frac{u}{\cos C},$	-	10,	$\cos C = \frac{u}{d}, -$	19,
$d = \frac{60L \cos l}{\sin C},$	•	11,	a a	20,
$d=\sqrt{\mathfrak{d}^2+u^2},$	-	12,	$\tan C = \frac{\sigma}{u}, -$	21,
$\cos l = \frac{\mathfrak{d}}{60L}, -$	-	13,	$\sin C = \frac{60L \cos l}{d},$	22,
$\cos l = \frac{d \sin C}{60L},$	-	14,	$\tan C = \frac{60L \cos l}{\iota}$	23,
			76	

Example 1. A vessel sails east-north-east (6 points) 236 miles. Required her departure 0, and difference in latitude u.

Formula 1. $\mathfrak{d} = d \sin C = 236 \times \sin 6$ points = 218 miles departure, and u = d $\cos c = 236 \times \cos 6$ points = 90.3 miles difference in latitude.

Example 2. A ship sails in north latitude in a course $C = ESE^{\frac{3}{4}}E = G^{\frac{3}{4}}$ points; at a distance of 132 miles she made a difference in longitude of $L=3^{\circ}$ 34'. What latitude is she in?

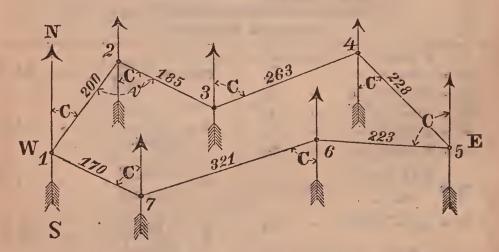
Formula 14.
$$\cos t = \frac{d \sin C}{60L} = \frac{132 \times \sin 6\frac{3}{4}}{60 \times 3 + 34} = 0.59832;$$

or $l = 53^{\circ} 15'$ the latitude.

In high latitudes and very long distances, the preceding formulas will not give such correct results as may be desired, because they are set up with the supposition that the earth is a level plane; but by the aid of spherical trigonometry we are enabled to ascertain courses and distances correctly from and between any known points on the earth. (See Spherical Trigonometry.)

LAND SURVEYING.

Application of formulas on the preceding page.



The operation is readily understood by the illustration. When only an azimuth compass is used, the course C at each station is measured from the magnetic needle or meridian to the direction of the survey. When a theodolite is employed, the course C is read as carefully as possible from the compass at the first station, but at the second station the angle v between the distances is measured, from which subtract the first course, and the remainder will be the second course. At the third station subtract the second course from the angle between the distances, and the remainder will be the third course, and so on. The calculated course is compared with that shown by the compass at each station; if a difference is observed, there may be some errors in the subtraction or angle measurement, or some local attraction of the magnetic needle, which is sometimes the case near great deposits of iron ores. The angles and courses are measured by the theodolite because they cannot be read so delicately on the compass.

At the 5th station, where the 4th and 6th stations are on the same side of the meridian and both north of 5, add the 4th course to the angle 4, 5, 6, and the sum is the new course. On return to the 1st station, where the 7th and 2d stations are both on the same side of the meridian, and one north and the other south, add the angle 2, 1, 7, to the 7th course, subtract the sum from 180°, and the remainder should be the 1st course, which shows the accuracy of the survey. If the measurements are not correct, there will be errors on return to the first station, as seen at the foot of the traverse table. The correction for varia-

tion of the compass is made on the map.

Traverse Table for the Survey.

Sta-	Course C.	Sin. or cos.	Dist.	Latit N.	ude. S.	Depa E.	rture.
1	N. 35°42′ E.,	$\begin{cases} \cos. 8121 \\ \sin. 5835 \end{cases}$	200	162.42		116.70	
2	S. 63 48 E.,	{ cos. 4415 } sin. 8972 }	185		81.68	165.98	
3	N. 68 38 E.,	$\begin{cases} \cos. 3643 \\ \sin. 9312 \end{cases}$	263	95.81	• • • .	244.90	
4	S. 42 25 E.,	{ cos. 7382 } { sin. 6747 }	228	• • • .	168.31	153.78	
5	N. 85 51 W.,	(prin. 9917)	223	16.12	• • •		222.42
6	S. 72 18 W.,	(814. 0020)	321	• • • :	97.58		305.78
7	N. 64 27 W.,	$\begin{cases} \cos. 4313 \\ \sin. 9022 \end{cases}$	170	73.32	• • •	• • •	153.37
Sum of N. S. E. and W., Subtract the smallest,				347.67	347.57	681.36	681.57
Subt	ract the smalle	st,	•	347.57			681.36
Erro	rs in the measu	rement, .	•	0.10			0.21

Find the natural sines and cosines in the trigonometrical tables.

The distance, d, multiplied by the cosine for the course C, will be the difference in latitude formula 5.

The distance, d, multiplied by the sine for the course C, will be the departure

formula 1.

The formulas and traverse table will answer for any unit of measure, but if the above traverse had been made in miles, whether on land or sea, each departure should be divided by cosine for the mean latitude between each two stations, formula 16, in order to obtain the true difference in longitude. To divide by cosine is the same as to multiply by the secant for the same angle.

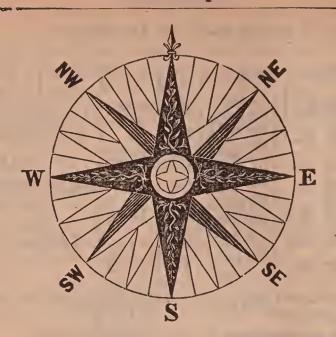
Length of a Degree in Parallel of Latitude.

Multiply the length of a degree at the equator (60 sea-miles = 69.03 statute miles = 110.83 kilometres) by cosine for the latitude, and the product will be the length of a degree in parallel of latitude.

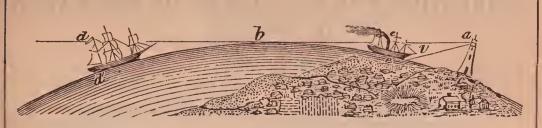
The length of a minute or second at the equator, multiplied by the cosine for the latitude, will be the corresponding length in the parallel of that latitude.

Measurement over Sloping Ground.

d = Sloping distance.	b = Base, or hori- zontal distance.	h = Difference in height.	v = Angle of the slopes.
d = h cosec. v .	$b=d\cos v$.	$h=d\sin v$.	$\sin v = \frac{h}{d}.$
d = b sec. v .	$b = h \cot v$.	h=b an. v.	$\tan v = \frac{\hbar}{b}.$



North.	South.	Points.	Degrees.	sineC.	Cos. C.	tan.C.
N.	s. {	1 2 3 4	2° 49′ 5 37 8 26	·0491 ·0979 ·1544	·9988 ·9952 ·9880	·0492 ·0983 ·1982
N. by E. and N. by W.	S. by E. and S. by W.	1 1½ 1½ 1¾	11 15 14 4 16 52 19 41	•1936 •2430 •2901 •3368	•9811 •9700 •9570 •9416	•1989 •2505 •3032 •3577
N. N. E. and N. N. W.	S. S. E. and S. S. W.	2 2½ 2½ 2½ 2¾ 2¾	22 30 25 19 28 7 30 56	·3827 ·4276 ·4713 ·5140	·9239 ·9039 ·8820 ·8577	·4142 ·4730 ·5343 ·5993
N. E. by N. and N. W. by N.	S. E. by S. and S. W. by S.	3 3½ 3½ 3¾	33 45 36 44 39 22 42 11	•5555 •5981 •6343 •6715	·8314 -8014 ·7731 ·7410	•6883 •7463 •8204 •9062
N. E. and N. W.	S. E. and S. W	4: 4: 4: 4: 4: 4:	45 0 47 49 50 37 53 26	•7071 •7410 •7731 •8014	·7071 ·6715 ·6345 ·5981	1·000 1·103 1·218 1·348
N. E. by E. and N. W. by W.	S. E. by E. and S. W. by W.	5 5½ 5½ 5¾	56 15 59 4 61 52 64 41	·8314 ·8577 ·8820 ·9039	·5555 ·5140 ·4713 4276	1·496 1·668 1·870 2·114
E. N. E and W. N. W.	E. S. E. and W. S. W.	6 6 ¹ / ₄ 6 ¹ / ₂ 6 ² / ₄	67 30 70 19 73 7 75 56	•9239 •9416 •9570 •9700	•3827 •3368 •2901 •2430	2·414 2·795 3 295 3·991
E. by N. and W. by N.	E. by S. and W. by S.	7 7 ¹ / ₄ 7 ¹ / ₂ 7 ³ / ₄	78 45 81 34 84 22 87 11	·9811 ·9880 ·9952 ·9988	·1936 ·1544 ·0979 ·0491	5·027 6·744 11·14 20·32
East or	West	8	9 0 0	1-000	0.000	œ



Distance and Dip of Horizon,

from different heights above the surface of the ocean.

Height.	Distance.	Dip.	Height.	Distance.	Dip.	Height.	Distance.	Dip.
Feet.	Miles.	1 77	Feet.	Miles.	, ,,	Feet.	Miles.	0 ' "
0.582	1 mile.	0 59	16	5.29	3 56	150	16.22	0 14 07
1*	1.31	0 59	17	5.4 5	4 03	200	18.72	0 16 18
2	1.87	1 24	18	5.61	4 11	300	22.91	0 19 56
3	2.29	1 42	19	5.77	4 17	400	26.46	0 23 03
4	2.63	1 58	20	5.92	4 24	500	29.58	0 25 46
5	2.96	2 12	25	6.61	4 55	1000	32.41	0 28 18
6	3.24	2 25	30	7.25	5 23	2000	59 20	0 51 42
7	3.49	2 36	35	7.83	5 49	3000	72.50	1 3 24
8	3.73	2 47	40	8.37	6 14	4000	83.70	1 14 15
9	3.96	2 57	45	8.67	6 36	5000	93.50	1 21 54
10	4.18	3 07	50	9.35	6 58	1 mile.	96.10	1 24 01
11	4.39	3 16	60	10.25	7 37	1 1 4 "	108.96	1 35 40
12	4.58	3 25	70	11.07	8 14	2 "	123.23	1 48 20
13	4.77	3 33	80	11.83	8 48	21/4	140.64	2 3 50
14	4.95	3 41	90	12.55	9 20	3 "	154.10	2 15 50
15	5.12	3 49	100	13.23	9 51	5 "	199.15	2 57 15
								النصحص

* For smaller heights, see Curvature of the Earth.

The refraction is included in the dip of horizon.

The distance being the tangent a b in statute miles, at the elevation a c, in feet.

Example 1. The lighthouse at a is 100 feet above the level of the sea. Required the distance a b.

Height 100 feet = 13.23 miles.

Example 2. The flag of a ship is seen from a in d. Required the distance a d, when the flag is known to be 50 feet above the level d' of the sea?

Height of the light 100 = 13.23 miles a.b., Height of the flag 50 = 9.35 " b.d., Distance to the ship = 22.58 miles a.d.

Example 3. A steamer is seen at e; the horizon b seen in the masts is assumed to be 16 feet above the level e'. Required the distance to the ship?

Height of the light 100 = 13.23 miles a b, The assumed height 16 = 5.29 " e b, Distance to the ship = 7.94 miles a e.

CORRECTION FOR CURVATURE OF THE EARTH

IN LEVELING.

Notation of letters.

D = distance in miles from the level to the stave or other object, and

d = the same distance in feet.

C =correction for curvature in feet at the stave; always negative.

c = the same correction in inches.

$$C = \frac{2D^2}{3}$$
. $D = 1.2247 \sqrt{C}$.
 $c = \frac{d^2}{3486543}$. $d = 1867.3 \sqrt{c}$.

The accompanying table gives the curvature for distances from 100 feet to 20 miles. For greater distances see table of *Distances and Dip of Horizon*.

Difference of Apparent and True Level or Curvature of the Earth, with and without Refraction.

Distance.	Curvature.	Curv. and ref.	Distance.	Curvature.	Curv. and ref.
Feet.	Inches.	Feet.	Miles.	Feet.	Feet.
100	.0028	.0002	1	0.666	0.575
200	.0115	.0008	2	2.666	2.283
300	.0258	.0018	3	6.000	5.141
400	.0489	.0033	4 5	10.675	9.150
500	.0717	.0051	5	16.675	14.291
600	.1032	.0073	6	24.083	20.583
700	.1405	.0100	7 8	32.683	28.167
800	.1835	.0130	8	42.691	36.591
900	2223	.0158	9 .	54.025	46.031
1000	.2868	.0204	10	66.700	.57.175
1500	.6453	.0459	11	80.708	69.175
2000	1.147	.0817	12	96.050	82.325
2500	1.792	.1276	13	112.716	96.616
3000	2.581	.1836	14	130.732	112.058
3500	3.513	.2500	15	150.075	126.633
4000	4,589	.372	16	170.750	147.191
4500	5.557	.396	17	192.766	165.225
5000	7.170	.5110	18	216.108	185.233
5500	8.676 .	.6185	19	240.783	206.391
6000	10.324	.7360	20	266.800	228.683

TO FIND THE DIVERGENCY OF THE PARALLEL

FROM THE PRIME VERTICAL.

Notation of letters.

l = latitude of the parallel in degrees.

 $v \Rightarrow$ distance on the prime vertical, expressed in angle of the great circle from the base-meridian.

c = divergency in feet of the parallel at the angle v.

 $c = 729000 \sin^2 \frac{1}{8} v \times l$.

The divergency is calculated in the accompanying table for distances from one second to one degree, also expressed in feet and miles on the prime vertical. The coefficient $c = 729000 \sin^2 \frac{1}{2}v$, which, multiplied by the latitude of the parallel in degrees, gives the divergency in feet.

Example 1. Suppose the distance on the prime vertical to be v = 6' = 6 miles and 4770 feet, the latitude of the parallel being 48°. Required the divergency.

From the table, $0.5551 \times 48^{\circ} = 26.6448$ feet, the divergency required.

Divergency of the Parallel from the Prime Vertical.

Seconds v. Feet. C. 1 101.25 0.00000434 2 202.5 0.00001735 3 303.75 0.00003855	Minutes v . 1 $1\frac{1}{2}$ 2 $2\frac{1}{2}$	prime vertical. Miles. Feet. 1 795 1 3832.5 2 1590	0.0154213 0.0346979
1 101.25 0.00000434	$egin{array}{c c} 1 & 1_{rac{1}{2}} \ 2 & \end{array}$	1 795 1 3832.5	0.0154213
2 202.5 0.00001735	2	1 3832.5	
0 000 88	2		
3 303.75 0.00003855			0.061685
		2 4627.5	0.0964
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	3	2 4627.5 3 2585	0.1387917
6 607.5 0.0001542	4	4 3180	0.24674
7 708.75 0.0002099	5	5 3975	0.3855
7 708.75 0.0002099 8 810 0.00027665 9 911.25 0.0003470	6	6 4770	0.55516
9 911.25 0.0003470	7	8 285	0.75564
10 1012.5 0.0004284	8 9	9 1080	0.98696
11 1113.75 0.00051833	9	10 1875	1.2491253
12 1215 0.0006168	10	11 2670	1.5420
13 1316.25 0.00072394	11	12 3465	1.865820
14 1417.50 0.0008396	12	13 4260	2.220604
15 1518.75 0.0009638	13	14 5055	2.6062
16 1620 0.0010966	14	16 570	3.02256
17 1721.25 0.0012380	15	17 1365	3.4696
18 1822.5 0.0013879	16	18 2160	3.94783
19 1923.75 0.0015464	18	20 3750	4.9965012
20 2025 0.0017135	20	23 60	6.1680
25 2531.25 0.002677	25	28 4035	9.637500
30 3037.5 0.0038553	30	34 2730	13.8785
35 3543.75 0.0052475	35	40 1425	18.8895
40 4050 0.0068539	40	45 120	24.6720
45 4 556.25 0 .0086742	45	51 4095	31.22815
50 5062.5 0.010709	50	57 2790	38.5500
55 5568.75 0.012958	55	63 1485	46.6455
60 6075 0.154213	60	69 180	55.5151

The length of minutes and seconds on the parallel is equal to that in the table, multiplied by cosine for the latitude.

These calculations are necessary in running a parallel of latitude by fore and back sighting, and also for laying out the parallels and meridians on a map.

TRIGONOMETRY.

TRIGONOMETRY is that part of Geometry which treats of triangles. It is divided

into two parts—viz., plane and spherical.

Plane Trigonometry treats of triangles which are drawn (or imagined to be) on a plane. Spherical Trigonometry treats of the triangles which are drawn (or

imagined to be) on a sphere.

A triangle contains seven quantities—namely, three sides, three angles and the surface. When any three of these quantities are given, the four remaining ones can by them be ascertained (one side or the area must be one of the given quantities), and the operation is called solving the triangle, which is only an application of arithmetic on geometrical objects.

For the foundation of the above-mentioned solution, there are assumed eight help quantities, which are called Trigonometrical functions, and are here denoted

with their names and number, corresponding with Figure 126.

Example 1. Fig. 121. An inclined plane a = 150 feet long, and c = 27 feet, the height over its base. What is the angle of inclination C=i

Formula 14.
$$\sin C = \frac{c}{a} = \frac{27}{150} = 0.18000.$$

Find 9.18000* in the table of sines, which will be found at 10°30', which is the angle C nearly.

Example 2. Fig. 122. An oblique-angled triangle has the sides c = 27.6 feet, the angle $C = 34^{\circ}10^{\circ}$, and the angle $A = 47^{\circ}40^{\circ}$. How long is the side a = ?

Formula 1.
$$a = \frac{c \sin A}{\sin C} = \frac{27.6 \times \sin .47^{\circ} 40'}{\sin .34^{\circ} 10'} = 36.33$$
 feet, the answer.

By Logarithms.
$$\log a = \log c + \log \sin A - \log \sin C$$

$$c + \log 27.6 = 1.44090$$

$$A + \log \sin 47^{\circ} 40' = 9.86878$$

$$1.30968*$$

$$C - \log \sin 34^{\circ} 10' = 9.74942$$

$$\log 36.4 = 1.56026, \text{ or } a = 36.4 \text{ feet.}$$

Example 3. Two ships of war notice a strong firing from a castle. In order to be safe, they keep themselves at a distance beyond the reach of the balls from the castle. To measure the distance from the castle, they place the vessels 800 yards from each other, and observe the angles between the castle and the vessels to be $A = 63^{\circ}45'$, $B = 75^{\circ}50'$. What will be the two distances from the castle?

$$C = 180 - 63^{\circ}45' - 75^{\circ}50' = 40^{\circ}25'$$

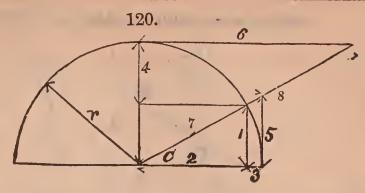
To A the distance will be,

$$b = \frac{c \sin B}{\sin C} = \frac{800 \times \sin 75^{\circ} 50'}{\sin 40^{\circ} 25'} = 1195.75 \text{ yards.}$$

To B the distance will be,

$$a = \frac{c \sin A}{\sin C} = \frac{800 \times \sin 63^{\circ} 45'}{\sin 40^{\circ} 25'} = 1106.6 \text{ yards.}$$

* The index of a logarithm for a fraction is negative; but in the logarithms for the trigonometrical functions, 10 is added to the index, for which it appears so much less than 10 as the real negative index. Therefore, when trigonometrical logarithms are added, 10's must be rejected from the sum of the index, which will be understood by the examples.



1	Sinus	abbreviated	sin.C.
2	Cosinu s	66	cos.C.
3	Sinvs-versus	16	sinv.C.
4	Cosinus-versus	66	cosv.C.
	Tangent	66	tan.C.
	Cotangent	66	cot.C.
	Secant	66	sec.C.
	Cosecant	66	cosec C

= Radius of the circle, which is the unit by which the functions are measured.

$$r^2 = \sin^2 C + \cos^2 C.$$

$$\tan C = \frac{\sin C}{\cos C},$$

$$\tan C = \frac{1}{\cot C},$$

$$\cot C = \frac{\cos C}{\sin C},$$

$$\cot C = \frac{1}{\tan C},$$

$$\sec.C = \frac{1}{\cos.C},$$

$$\csc C = \frac{1}{\sin C},$$

$$\sin v.C = 1 - \cos .C.$$

$$\cos v \cdot C = 1 - \sin \cdot C$$

$$\sin 2C \equiv 2 \sin C \cos C$$

$$\sin \frac{1}{2}C = \frac{1}{2}\sqrt{\sin^2 C + \sin^2 C},$$

$$\sin \cdot (C + B) = \sin \cdot C \cos \cdot B + \sin \cdot B \cos \cdot C$$

Positive and Negative Signs.

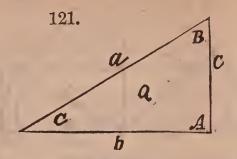
Angles.	sin.	cos.	sinv.	. co .v.	tan.	cot.	sec.	cosec.	Ì
+00	+0	+1	+0	+1	+0	+ ∞	+1	+∞	
÷90°	+1	+0	+1	+0	+∞	+0	+∞	+1	
+1800	<u>+</u> 0	-1	+2	+1	- 0	∞	<u>—</u> 1	+00	
4100		_					-	<u></u> ~	
+2700	1	+0	+1	+2	+∞	<u>+</u>	+∞	-1	
	-0		ī	1.1	<u></u>	∞	41		
+360°	+0	+1	+0	+1	7			-00	d

When a quantity has reached 0 or ∞ , it has ceased to exist, because it can not be increased or diminished.

Example. What is the length of the secant for an angle of 74° 18'?

Secant C =
$$\frac{1}{\cos 74^{\circ} 18'} = 3.695$$
.

FORMULA FOR RIGHT-ANGLED TRIANGLES.



$$a = \sqrt{b^{2}+c^{2}}, \qquad 1, \qquad Q = \frac{a^{2} \sin .2C}{4}, \qquad 10,$$

$$a = \frac{c}{\sin .C}, \qquad 2, \qquad Q = \frac{1}{2} b^{2} \tan .C, \qquad 11,$$

$$a = \frac{b}{\cos .C}, \qquad 3, \qquad Q = \frac{1}{2} c^{2} \cot .C, \qquad 12,$$

$$Q = \frac{1}{2} c \sqrt{(a+c)(a-c)} \qquad 13,$$

$$a = 2 \sqrt{\frac{Q}{\sin .2C}}, \qquad 4, \qquad \sin .C = \frac{c}{a}, \qquad 14,$$

$$b = a \cos .C, \qquad 5, \qquad \cos .C = \frac{b}{a}, \qquad 15,$$

$$b = c \cot .C, \qquad 6,$$

$$b = a \sin .B, \qquad 7,$$

$$b = c \tan .B, \qquad 8, \qquad \sin .2C = \frac{4Q}{a^{2}}, \qquad 17,$$

$$b = \sqrt{\frac{2Q}{\tan .C}}, \qquad 9, \qquad \tan .C = \frac{2Q}{b^{2}}, \qquad 18,$$

Say the angle to be $C=60^{\circ}$. In the first column of the table of sines, 60° corresponds with 0.86602 in the next column, which is the length of sin. 60° , when the radius of the circle is one, or the unit, and the expression \sin $60^{\circ} \times 36$ means $0.86602 \times 36 = 31.17672$, and likewise with all the other Trigonometrical expressions.

În a triangle the functions for an angle have a certain relation to the opposite side; it is this relationship which enables us to solve the triangle by the ap-

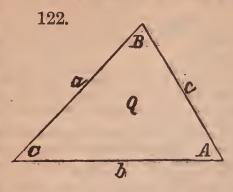
plication of Simple Arithmetic.

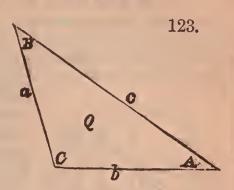
In triangles the sides are denoted by the letters a, b, and c; their respective opposite angles are denoted by A, B, and C, and the area by Q.

Example 1. Fig. 136 The side c in a right angled Triangle being 365 feet, and the angle $C = 39^{\circ}$ 20'. How long is the side a = ?

Formula 2.
$$a = \frac{c}{\sin C} = \frac{365}{\sin .39^{\circ}.20'} = \frac{365}{0.63383} = 575.86$$
 feet, the answer.

FORMULA FOR OBLIQUE-ANGLED TRIANGLES.





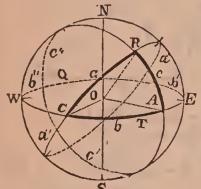
 $a:b=\sin A:\sin B$, and $b:c=\sin B:\sin C$. $a:c=\sin A:\sin C$, and $Q:ab=\sin C:2$.

$a=\frac{c\sin.A}{\sin.C},$	1,	$S = \frac{1}{2}(a+b+c)$ $\sin \frac{1}{2}A = \sqrt{\frac{(s-b)(s-c)}{bc}}$	12, ,13,
$a = \frac{c \sin A}{\sin (A+B)},$	2,	$\sin_{\frac{1}{2}}B = \sqrt{\frac{(s-a)(s-c)}{ac}},$	
$a=\frac{2Q}{b\sin.C},$	3,	$\cos_{\frac{1}{2}}A = \sqrt{\frac{s(s-a)}{bc}},$	
$b = \frac{c \sin B}{\sin C},$	4,	$\cos \frac{1}{2}B = \sqrt{\frac{s \cdot (s - b)}{ac}},$	16,
$b = \frac{2Q}{c \sin A},$	5,	$Q = \frac{bc \sin A}{2},$	17,
$\sin C = \frac{c \sin B}{b},$	6,	$Q = \frac{ao \sin . C}{2},$	18,
$\sin C = \frac{c \sin A}{a},$	7,	$Q = \frac{c^2 \sin A \sin B}{2 \sin (A+B)},$	19,
$\sin A = \frac{2Q}{bc},$	8,	$Q = \sqrt{S-a)(S-b)(S-c)}$	20,
$\sin A = \frac{a \sin C}{c},$ $\sigma = \sqrt{b^2 + c^2 - 2b c \cos A},$		$b = \sqrt{\frac{2Q \sin.(A+C)}{\sin.A \sin.C}},$	21,
$a = \sqrt{\frac{2Q \sin A}{\sin B \sin (A+B)}}$	11,	$c = \sqrt{\frac{2Q \sin . C}{\sin . A \sin . (A+C)}},$	22

SPHERICAL TRIGONOMETRY.

Spherical Trigonometry treats of triangles which are drawn (or imagined to be) on the surface of a sphere. Their sides are arcs of the great circle of the sphere, and measure by the angle of the arc. Therefore the trigonometrical functions bear quite a different relation to the sides.

Every section of a sphere cut by a plane is a circle. A line drawn through the



centre and at right angles to the sectional circle is called an axis, and the two points where the axis meets the surface of the sphere are called the poles of the sectional circle.

When the cutting plane goes through the centre of the sphere, it will pass through the great circle, and is then called the *Equator* for the poles. Axis = N.S. Equator — G.E.T.W.

Three great circle-planes, a a'a''a''', b b'b'', and c c'c'', cutting a sphere, NESW, will form a solid angle at the centre O, and a triangle ABC on the surface of the sphere, in which the arcs a, b, c, are the sides. The angles formed by each two planes are congruent to each of the appertinent angles A, B and C.

Spherical Distances.

For the spherical distances, letters will denote,

l = lower latitude, in degrees from the equator.

l' = highest latitude, "" " C = course, from the latitude l to l'.

l' to l. C' = course, from

d = shortest distance between l and l' in degrees of the great circle.

L = difference in longitude between l and l', in degrees, or time.

 $\tan m = \cot l' \cos L$.

 $n = 90 \mp l - m$.

-l, when l and l' are on one side of the equator.

+ l, when l is on one side, and l' on the other. Then

$$\cos d = \frac{\sin l' \cos n}{\cos m}, \qquad 1.$$

$$\sin C = \frac{\sin L \cos l'}{\sin d}, \qquad 2.$$

$$\sin C' = \frac{\sin L \cos l}{\sin d}, \qquad 3.$$

Example. Required the shortest distance and course from New York to Liverpool.

 $l = 40^{\circ} 42'$ N. latitude, 74° 42' W. longitude, \} New York.

 $V = 53^{\circ} 22'$ N. latitude, 2° 52' W. longitude, Liverpool.

 $L = 71^{\circ}8'$ difference in longitude.

 $\tan m = \cot .53^{\circ} 22' \times \cos .71^{\circ} 8' = 13^{\circ} 31'.$

 $n = 90^{\circ} - 13^{\circ}31' - 40^{\circ}42' = 35^{\circ}47'$

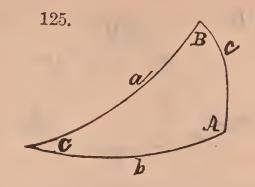
 $\cos d = \frac{\sin .53^{\circ} 22' \times \cos .35^{\circ} 47'}{47^{\circ}} = 47^{\circ} 58'.$ Formula 1. cos. 13° 31"

Shortest distance = $47^{\circ} \times 60 + 58 = 2878$ geographical miles.

$$\sin C = \frac{\sin .71^{\circ} 8' \times \cos .53^{\circ} 22'}{\sin .47^{\circ} 58'} = 49^{\circ} 23' = 4\frac{3}{6} \text{ points,}$$

course from New York NE & E.

RIGHT-ANGLED SPHERICAL TRIANGLE.



$\sin b = \sin a \sin B,$ $\tan c = \tan a \cos B,$	1, 2,	$\sin B = \frac{\sin b}{\sin a},$	12,
$\cot C = \cos a \tan B,$ $\tan c = \sin b \tan C,$	3, 4,	$\sin \cdot C = \frac{\tan \cdot b}{\tan \cdot a}$	13,
$\cos a = \cos b \cos c,$ $\cos B = \cos b \sin C,$ $\tan a = \frac{\tan b}{\tan C},$	5, 6, 7,	$\tan C = \frac{\tan c}{\sin b},$	14,
$\sin c = \frac{\tan b}{\tan B},$	8,	$\tan B = \frac{\tan b}{\sin c},$	15,
$\sin a = \frac{\sin b}{\tan B'}$	9,	$\cos c = \frac{\cos C}{\sin B},$	16,
$\sin C = \frac{\cos B}{\cos b},$	10,	$\cos b = \frac{\cos B}{\sin C},$	17,
$\cos c = \frac{\cos a}{\cos b},$	11,	$\cos a = \frac{\cot C}{\tan B},$	18.

The sum of the three angles in a spherical triangle is greater than two right angles, and less than six right angles.

By Spherical Trigonometry we ascertain distances and courses on the surface of the earth; positions and motions of the heavenly bodies, &c., &c. Examples will be furnished in Geography and Astronomy.

Example 1. Fig. 140 In a right-angled spherical triangle the side or hypothenuse $a=36^{\circ}$ 20', the angle $B=68^{\circ}$ 50'. How long is the side b=?

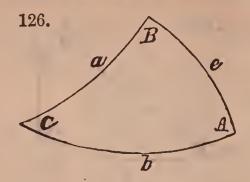
Formula 1. $\sin b = \sin a \sin B = \sin 36^{\circ}20' \times \sin 68^{\circ}60'$.

a log.sin. $36^{\circ} 20' = 9:77267$ B log.sin. $68^{\circ} 50' = 9:96966$

The answer, $\log \sin . 33^{\circ} 32' = 9.74233$

or $b = 33^{\circ} 32'$.

OBLIQUE-ANGLED SPHERICAL TRIANGLE.



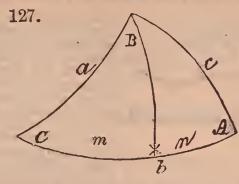
$$\begin{array}{lll}
sin.a : sin.b = sin.A : sin.B, & sin.a = \frac{\sin.b \sin.A}{\sin.B}, & 19 \\
sin.b : sin.c = sin.B : sin.C, & sin.b = \frac{\sin.c \sin.B}{\sin.C}, & 20 \\
tan.(a+b) = tan.\frac{1}{2}c \frac{\cos.\frac{1}{2}(A-B)}{\cos.\frac{1}{2}(A+B)}, & - & - & 21, \\
tan.(a-b) = tan.c \frac{\sin.\frac{1}{2}(A-B)}{\sin.\frac{1}{2}(A+B)}, & - & - & 22, \\
tan.\frac{1}{2}(A+B) = \cot.\frac{1}{2}A \frac{\cos.\frac{1}{2}(b-c)}{\cos.\frac{1}{2}(b+c)}, & - & 23, \\
tan.\frac{1}{2}(A-B) = \cot.\frac{1}{2}A \frac{\sin.\frac{1}{2}(b-c)}{\sin.\frac{1}{2}(b+c)}, & - & 24, \\
cot.\frac{1}{2}A = tan.\frac{1}{2}(B-C) \frac{\sin.\frac{1}{2}(b+c)}{\sin.\frac{1}{2}(b-c)} & - & 25, \\
tan.\frac{1}{2}c = tan.\frac{1}{2}(a-b) \frac{\sin.\frac{1}{2}(A+B)}{\sin.\frac{1}{2}(A-B)}, & - & 26, \\
\end{array}$$

Example 2. Fig. 141 Oblique angled spherical triangle. $c = 72^{\circ}30'$. $B = 17^{\circ}30'$. $C = 79^{\circ}50'$.

How long is the side b = ?Formula 20. $\sin b = \frac{\sin c \sin B}{\sin C} = \frac{\sin .72^{\circ} 30' \times \sin .17^{\circ} 30'}{\sin .79^{\circ} 50'}$ $c + \log .\sin .72^{\circ} 30' = 9:97942$ $+ \log .\sin .17^{\circ} 30' = 9:47812$ $+ \log .\sin .79^{\circ} 50' = 9:99312$

The answer $\log \sin 16^{\circ} 50' = 9.46442$ or $b = 16^{\circ} 56.'$

OBLIQUE-ANGLED SPHERICAL TRIANGLE.



$$\tan \frac{1}{2}(m+n)\tan \frac{1}{2}(m-n) = \tan \frac{1}{2}(a+c)\tan \frac{1}{2}(a-c)$$

$$\tan m = \tan c \cos A, \qquad 27,$$

$$\tan C = \frac{\sin m \tan A}{\sin (b-m)}, \qquad 28,$$

$$\cos a = \frac{\cos c \cos (b-m)}{\cos m}, \qquad 29,$$

$$\cos n = \frac{\cos a \cos m}{\cos c}, \qquad 30,$$

$$b = m+n.$$

$$\cot m = \frac{\cos c \tan A}{\tan a}, \qquad 31,$$

$$s = a+b+c \quad S = A+B+C,$$

$$\sin \frac{1}{2}A = \sqrt{\frac{\sin (s-c) \sin (s-b)}{\sin b \sin c}}, \qquad 32,$$

$$\sin \frac{1}{2}a = \sqrt{\frac{\cos S \cos (S-A)}{\sin B \sin C}}, \qquad 33,$$

To Find the Area of a Spherical Triangle.

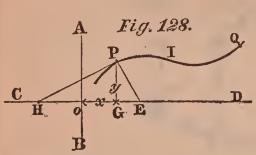
Let Q be the area of the triangle in square degrees; if R = radius of the sphere, the length of one degree will be,

the length of one degree will be,
$$= \frac{2\pi R}{360}, \text{ or one square degree} = \frac{R^2}{3285 \cdot 58}.$$

$$\cot \cdot \frac{1}{2}Q = \frac{\cot \cdot \frac{1}{2}c \cot \cdot \frac{1}{2}a + \cos \cdot B}{\sin \cdot B}, \qquad \cdot \qquad \cdot \qquad \cdot \qquad 1,$$

$$\sin \cdot \frac{1}{2}Q = \frac{\sin \cdot \frac{1}{2}c \sin \cdot \frac{1}{2}a \sin \cdot B}{\cos \cdot \frac{1}{2}b}, \qquad \cdot \qquad \cdot \qquad \cdot \qquad 2,$$

ANALYTICAL GEOMETRY AND CONIC SECTIONS.



An equation of a line is generally referred to rectangular lines, A B = axis of ordinate and CD = axis of abscissa. The position of any point P in the curved line PIQ is defined by the rectangular distances, y the ordinate and x the abscissa; x and y are variables, depending on one another. Any change in either of them will produce a change in the other, in accordance with the formulæ for the line. The position of a number of points can be determined, located and joined into the required line of the equation.

The ordinate y generally constitutes the first member of the equation, and its

value is determined by assumed values of the abscissa x.

The junction of the two axes is called origin, and denoted by o. The line will not pass through the origin when the equation has a constant term.

Properties of Lines Referred to Rectangular Co-ordinates.

The tangent of any curve, The subtangent of any curve, . . . $HG = y \frac{dx}{dy}$. .

The normal of any curve, $PE = y\sqrt{1 + \frac{dy^2}{dx^2}}$.

 $GE = y \frac{dy}{dx}$. . . The subnormal of any curve, . . .

The point of inflection, I, where convex and

concave curves tangent, or where a curve re- $\frac{d^2y}{dx^2} = 0, \text{ or } \infty. \qquad . \qquad . \qquad 5.$ verses, is when . . .

Let z denote the length of any curve, then $dz = \sqrt{dx^2 + dy^2}$.

 $R = \frac{dz^3}{dx d^2y}$. . . The radius of curvature of any curve is .

The ordinate y is a maximum or minimum when $\frac{dy}{dx} = 0$

(See Maxima and Minima.)

A curve is convex to the axis of abscissa when the ordinate and second differential coefficient have the same sign, but concave when either of them is positive and the other negative I Q is convex, and P I concave, to the abscissa C D.

A Conic Section is the section obtained when a plane cuts a cone.

The conic sections are of five different kinds, namely:

1st. Triangle. When the plane cuts the cone through its axis.

2d. Circle. When the plane cuts the cone at right angles to its axis.

3d. Ellipse. When the plane cuts the cone obliquely, passing through the two sides.

4th. Parabola. When the plane cuts the cone parallel to one side.
5th. Hyperbola. When the plane cuts the cone at an angle to the axis less than the angle of the axis and the side of the cone.

HYPERBOLIC LOGARITHMS.

Hyperbolic logarithms are used in formulas derived from the calculus when the differential cannot be integrated without the aid of hyp. logarithms. The common logarithm multiplied by 2.30258509 will be the hyperbolic logarithm, and the hyp. log. multiplied by 0.43429448 will be the common logarithm.

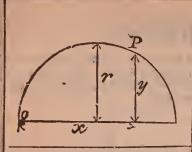
$$\int_{x_0}^{x'} \frac{dx}{x} = \text{hyp.log.} x' - \text{hyp.log.} x_0 = \text{hyp.log.} \frac{x'}{x_0}.$$

Hyperbolic Logarithms.

					0.4					
0	— ∞	- 00000	8.39056	8.79602	9.08371	9.30685	9.48918	9.64332	9.77685	9.89463
					0.33646					
										1.06473
					1.22373					
					1.48161					
					1.68633					
					1.85629					
7	1.94591	1.96006	1.97406	1.98787	2.00149	2.01490	2.02816	2.04115	2.05415	2.06690
					2.12830					
9	2.19722	2.20837	2.21932	2.23014	2.24085	2.25129	2.26191	2.27228	2.28255	2.29171

Hyperbolic Logarithms.

	Hyperbolic Logarithms.												
No. I	0	1	2	3	4	5	6	7	8	9			
10	2.30258	2.39589	2.48491	2.56494	2.63906	2.70805	2.77259	2.83321	2.89037	2.94444			
20	.99573		3.09104			3.21888			3.33220	3.36730			
30	3.40120	.43399	.46574	.49651	.52636	.55535	.58352	.61092	.63759	.66356			
40	.68888	.71357	.73767	.76120	.78419	.80666	.82864	.85015	.87120	.89182			
50	.91202	.93183	.95124	.97029	.98898	4.00733	4.02535	4.04305	4.06044	4.07754			
60	4.09434	4.11087				.17439		.20469	.21951	.23411			
70	.24849	.26268	.27667	.29046		.31749		.34380	.35671	.36945			
80	.38203	.39445		.41884		.44265		.46591	.47734	.48864			
90	.49981	.51086		.53260	.54329	55388	.56435	.57471	.58497	.59512			
100	4.60517		4.62497		4.64439	4.65396		4.67283	4 68213	4.69135			
110	.70048	.70953		.72739	.73619	.74493	.75359	.76217	.77068	.77912			
120	.78749	.79579		.81218		.82831	.83628		.85203	.85981			
1 30	.86753	.87519		.89035	.89784	.90527	.91265	.91998	.92725	.93447			
140	.94164			.96284	.96981	.97673	.98360	.99043	.99721	5.00394			
150	5.01063		5,02388		5.03695	5.04342	5.04985	5.05624	5.06259	5.06890			
160	.07517	.08140		.09375	.09986	.10594	.11199	.11799	.12396	.12990			
170	.13580	.14166		.15329	.15905	.16478	.17048	.17615	.18178	.18738			
180	.19295				.21493		.22574	.23111	.23644	.24175			
190	.24702		.25750	.26269	.26786		.27811	.28320	.28826	.29330			
200	5.29832		5.30826		5.31812		5.32787	5.33272	5.33754	5.34233			
210	.34711	.35186		.36129		.37064	.37528	.37989	.38450	.38907			
220	.39363			.40717	.41164		.42053	.42495	.42934	.43372			
230	.43808	.44242		.45104				.46806	.47227	.47646			
240	.48064			.49306			.50533	.50939	.51343	.51745			
250	5.52146						5.54517	5.54907	5.55296	5.55683			
260	.56068	.56452		.57215			.62040	.58725	.59098	.59471			
270	.59842			.60947	.61313	.61677	.65599	.62402	.62762	.63121			
280	.63479			.64544			.69036	.69373	.66296	.66642			
290	.66988			.68017	.68358	5.72031		5.72685	.69709	.70044			
300	5.70378			5.71373			.75574	.75890	5.73010 .76205				
310	.73657	.73979		.74620			.78690		.79301	.76519			
320	.76832			.77765				.82008	.82304	.79606			
330	.79909			.80814					.85220				
340	.82894	.83188	.83481	.83773	.84064					.85507			
350	10.85793	15.86078	10.86363	0.86647	0.80929	0.01212	0.01495	5.87773	[0.88093	19.00552			

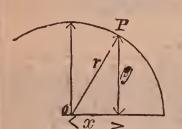


.29.	Circle.

$$y = \sqrt{2rx - x^2},$$

$$r = \frac{y^2 + x^2}{2x},$$

$$x = r + \sqrt{r^2 - y^2}.$$

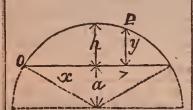


$$y = \sqrt{r^2 - x^2},$$

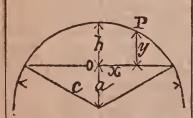
$$r = \sqrt{y^2 + x^2},$$

 $x = \sqrt{r^2 - y^2}.$

 $y = \sqrt{a^2 + cx - x^2} - a,$



$$a=\frac{c^2-4h^2}{8h}.$$



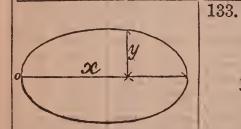
132. Circle Arc.

$$y = \sqrt{\left(\frac{c^2 + h^2}{8h}\right)^2 - x^2} - a.$$

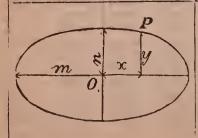
$$c^2 - 4h^2$$

$$a=\frac{c^2-4h^2}{8h}.$$

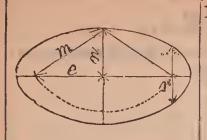
134.



$$y=\frac{n}{m}\sqrt{2mx-x^2}.$$



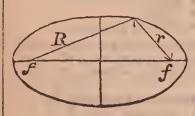
$$y = \sqrt{n^2 - \left(\frac{nx}{m}\right)^2}$$



35.	Ellipse.

$$e=\sqrt{m^2-n^2},$$

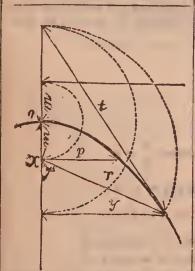
$$p=\frac{2n^2}{m}.$$



136.

$$R=2m-r,$$

$$r=2m-R$$
.



137.

$$y = \sqrt{px}, \quad p = 4m,$$

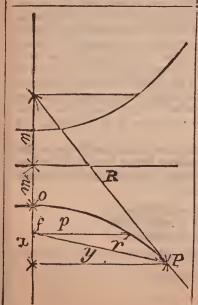
$$r = \sqrt{y^2 + (x - m)^2} = x + m,$$

$$y = \sqrt{t^2 - 4x^2}$$

$$y = 2\sqrt{x(x+m) - x^2},$$

$$t=\sqrt{4x^2+y^2},$$

$$t = 2\sqrt{x(x+m)}$$
.



138.

$$R-r=2m, e=\frac{n}{m}.$$

$$y=\frac{1}{m}\sqrt{(e^2-1)(x^2-m^2)},$$

$$b^2 = \frac{e^3 - 1}{m^2},$$

$$y = b \sqrt{\frac{(x+m)^2}{m^2} - 1}.$$

LOGARITHMS.

A Logarithm is an exponent of a power to which 10 must be raised to give a certain number, which will be understood by this

The unit of the logarithm is called the characteristic or index, and the decimal part is called the mantissa, the sum of the characteristic and mantissa is the Loga-The invariable number 10 is the base for the system of Lugarithm. rithms.

It is not necessary that the base should be 10, it can be any number, but all the tables of logarithms now in common use, are calculated with 10 to the

The nature of logarithms in connection with their numbers are such, that the index of the logarithm is always one less than the number of figures in the number, (when the base of the logarithm is 10,) as,

$$\begin{array}{l} \text{index } 5012 = 3 \\ \text{mantissa } 5012 = 0.7 \\ \text{logarithm } 5012 = 3.7. \end{array}$$

Let 10 be raised to any power x, and the power of $10^x = a$ or $\log a = x$,

the power of $10^z = b$ or $\log b = z$.

Let the product of ab = c and the quotient $\frac{a}{c} = c$.

$$10x \times 10z = 10x = ab = c or log. c = x + s.$$

$$\frac{10x}{10z} = 10x - z = \frac{a}{b} = d or log. d = x - z.$$

$$a = mz or log. m = z \times log. a.$$

$$\sqrt[3]{a} = n or log. n = log. a : 3.$$

Any number represented by the letters a, b, c, or d, can be a power of 10, which exponent is the logarithm for the number. Logarithms are calculated for every number with three figures in the accompanying Table, by which any operation in Multiplication, Division, Involution and Evolution can be performed by simple Addition or Subtraction of Logarithms. Tables of Logarithms are commonly more extensive, and calculated tor any number of four or five figures, which would occupy too much room in this book; but by the proportional parts, the logarithm can be found by this Table, to four or five figures. The index of the logarithms do not appear in the Table, only the mantissa. It is easily remembered that the index is one less, than the number of figures in the number; then when the number is only one figure, the index is 0; and when the number is a fraction, the index is negative.

When the logarithm is to be found for a fraction, we commonly have the fraction expressed in a decimal; and then the negative index is equal to the number of ciphers before the first figure, and commonly marked after the man-

tissa; thus explained in whole numbers and fractions:

In the accompanying Table of Logarithms, for the trigonometrical lines the negative index is marked thus,

 $\log \sin 35^{\circ} 40' = \log 0.58306 = 1.76572.$

To find the Logarithm of Numbers.

Example 1. Find the logarithm of 45.

To 45 in the first column of the Table, answers 65321 in the next column, which is the mantissa; index = 1 because 45 is two figures.

Then, $\log. 45 = 1.65321$, the answer.

Example 2. Find the logarithm of 768?

Opposite 76 in the first column, answers 88536 in the column marked 8 on the top or bottom. Index = 2 because 768 is three figures.

Then, $\log 768 = 2.88536$.

Example 3. Find the Logarithm of 6846?

 $\log 6846 = 3.835434$ the answer.

To find the number for a given Logarithm.

Example 1. What number answers to the logarithm 3.87157? In the Table you will find in the column of logarithms, that $\log.7440 = 3.87157$.

Example 2. What number answers to the logarithm 3.801884?

Given logarithm 3.801884, 3.801400 = log. 6330, Divided by proportional part, 69|484| ---- 7,

6337 the req. numb.

Multiplication by Logarithms.

Rule. Add together the logarithms of the factors, and the sum is the logarithm of the product.

Example 1. Multiply 425 by 48.

To log. 425 = 2.62839, Add log. 48 = 1.68124, The product, log. 20400 = 4.30963.

Example 2. Multiply 79600 by 0.435.

To $\log. 79600 = 4.90091,$ Add, $\log. 0.435 = \frac{.63848-1}{4.53939},$ The product $\log. 34690 = 4.53939.$

Division by Logarithms.

Rule. From the logarithm of the dividend subtract the logarithm of the divisor, and the difference is the logarithm of the quotient.

Example 1. Divide 43800 by 363.

From $\log. 43800 = 4.64147$, Subtract $\log. 368 = 2.56584$, The quotient $\log. 119 = 2.07563$.

Example 2. Divide 36 by 0.625.

From log. 36 = 1.55636, Subtract, log. 0.625 = .79588-1. The quotient, log. 57.6 = 1.76048.

A negative index follows an opposite operation of its mantissa, as if the mantissa is subtracted, add the negative index, and vice versa.

Envolution by Logarithms.

Rule. Multiply the logarithm of the number by its exponent, and the product is the logarithm of the power of the number.

Involution by Logarithms.

Rule. Divide the logarithm of the number by the index of the root, and the quotient is the logarithm of the root of the number.

No. 100 to 1600. Logarithms. 00000 to 20412.												
No.	0	1	2	3	4	5	6	7	8	9		4.2
100	00000	00043	00087	00130	00173	00217	00260	00303	00346	00389	11	43
101	0432	0475	0518	0561	0604	0647	0689	0732	0775	0817	$\frac{1}{2}$	9
102	0860	0903	0945	0988	1030	1072	1115	1157	1199	1242	3	13
103	1284	1326	1368	1410	1452	1494	1536	1578	1620	1662	4	17
104	1703 02119	$1745 \\ 02160$	$1787 \\ 02202$	$1828 \mid 02243 \mid$	1870 02284	1912 02325	$1953 \\ 02366$	1995 02407	2036 0244 9	2078 02490	5 6	22 26
105	2531	2572	2612	2653	2694	2735	2776	2816	2857	2898	7	30
107	2938	2979	3019	3060	3100	3141	3181	3222	3262	3302	8	34
108	3342	3383	3423	3463	3503	3543	3583	3623	3663	3703	9	39
109	3743	3782 041 7 9	3822 04218	3862 04258	$3902 \\ 04297$	3941 04336	3981 04376	$4021 \\ 04415$	$\frac{4060}{04454}$	4100 04493		41
110 111	$04139 \\ 4532$	4571	4610	4650	4689	4727	4766	4805	4844	4883	1	4
112	4922	4961	4999	5038	5077	5115	5154	5192	5231	5269	2	8 12
113	5308	5346	5385	5423	5461	5500	5538	5576	5614	5652	3 4	16
114	5690	5729	5767	5805	5843	5881	5918	5956	5994	6032	5	21
115	06070 6446	$06108 \\ 6483$	06145 6521	06183 6558	$06221 \\ 6595$	06258 6633	06296 6670	06333 6707	$06371 \\ 6744$	06408 6781	6	25
117	6819	6856	6893	6930	6967	7004	7041	7078	7115	7151	7	29
118	7188	7225	7262	7298	7335	7372	7408	7445	7482	7518	8	33 37
119	7555	7591	7628	7661	7700	7737	7773	7809	7846	7882		
120 121	07918 8279	07954 8314	07990 8350	08027 8386	08063 8422	08099 8458	08135 8493	08171 8529	08207 8565	08243 8600		39
121	8636	8672	8707	8743	8778	8814	8849	8884	8920	8955	1 2	4 8
123	8991	9026	9061	9096	9132	9167	9202	9237	9272	9307	$\frac{2}{3}$	12
124	9342	9377	9412	9447	9482	9517	9552	9587	9621	9656	4	16
125	09691	09726	09760	09795	09830	09864	09899	09934	09968	10003	5	20
126 127	$10037 \\ 0380$	10072 0415	10106 0449	10140 0483	10175 0517	10209 0551	10243 0585	10278 0619	10312 0653	0346 0687	6 7	23 27
128	0721	0755	0789	0823	0857	0890	0924	0958	0992	1025	8	31
129	1059	1093	1126	1160	1193	1227	1261	1294	1327	1361	9	35
130	11394	11428	11461	11494	11528	11561	11594	11628	11661	11694		37
131	1727 2057	1760 2090	1793 2123	1826 2156	1860 2189	1893 2222	1926 2254	1959 2287	1992 2320	$2024 \\ 2352$	11	4
133	2385	2418	2450	2483	2516	2548	2581	2613	2646	2678	2	7
134	2710	2743	2775	2808	2840	2872	2905	2937	2969	3001	3	11
135	13033	13066	13098	13130	13162	13194	13226	13258	13290	13322	4 5	15 19
136	3354 3672	3386 3704	3418 3735	3450	3481 3799	3513 3830	3545 3862	3577 3893	3609 3925	3640 3956	6	22
138	3988	4019	4051	4082	4114	4145	4176	4208	4239	4270	7	26
139	4301	4333	4364	4395	4426	4457	4489	4520	4551	4582	8	30
140	14613	14644		14706		14768	14799	14829	14860	14891	9	33
141	4922 5229	4953 5259	4983 5290	5014 5320	5045 5351	5076 5381	5106 5412	5137 5442	5168 5473	5198 5503		35
143	5534	5564	5594	5625	5655	5685	5715	5746	5776	5806	$\begin{vmatrix} 1\\2 \end{vmatrix}$	4 7
144	5836	5 866	5897	5927	5957	5987	6017	6047	6077	6107	3	11
145	16137	16167	16197	16227	16256	16286	16316	16346	16376	16406	4	14
146 147	6435	6465	6495 6791	6524 6820	6554 6850	6584	6613 6909	6643 6938	6673 6967	6702 6997	5	18
141	7026	7056	7085	7114	7143	7173	7202	7231	7260	7289	6 7	21 25
149	7319	7348	7377	7406	7435	7464	7493	7522	7551	7580	8	28
150	17609	17638	17667	17696	17725	17754	17782	17811	17840	17869	9	32
151	7898	7926 8213	7955 8241	7984 8270	8013 8298	8041 8327	8070 8355	8099 8384	8127	8156		33
152 153	8184 8469	8213	8526	8554	8583	8611	8639	8667	8412 8696	8441 8724	11	3
154	8752	8780	8808	8837	8865	8893	8921	8949	8977	9005	2	7
155	19033	19061	19089	19117	19145	19173	19201	19229	19257	19285	3 4	10 13
156	9312	9340	9368	9396	9424	9451	9479	9507	9535	9562	5	17
157 158	9590 9866	9618 9893	9645 9921	9673 9948	9700	9728	9756 20030	9783 20058	9811	9838 20112	6	20
159	20140	20167	20194	20222	20249	0276	0303	0330	0358	0385	7	23
No.		1	2	3	4	5	6.	7	8	9	8 9	26 30
		^ <u>*</u>	- And	, ,	3.				. 0		. 0	UC

N	o. 160	0 to 2	200.		Loga	rithm	s.	2	0412	to 342	42	
No.	0	1	2	3	4	5	6	7	8	9		31
160	20412	20439	20466	20493	20520	20548	20575	20602	20629	20656	1	3
161	0683	0710	0737	0763	0796	0817	0844	0871	0898	0925	2	6
162 163	0952 1219	0978 1245	$1005 \ 1272$	1032 1299	$1059 \ 1325$	$1085 \\ 1352$	1112 1378	1139 1405	1165 1431	1192 1458	3 4	$\frac{9}{12}$
164	1484	1511	1537	1564	1590	1617	1643	1669	1696	1722	5	16
165	21748	21775	21801	21827	21854	21880	21906	21932	21958	21985	6	19
166	2011	2037	2063	2089	2115	2141	2167	2194	2220	2246	7	. 22
167 168	2272 2531	2298 2557	2324 2583	2350 2608	$2376 \\ 2634$	2401 2660	2427 2686	2453 2712	2479 2737	$2505 \\ 2763$	8	25 28
169	2789	2814	2840	2866	2891	2917	2943	2968	2994	3019	91	
170	23045	23070	23096	23121	23147	23172	23198	23223	23249	23274	1	29
171	3300	3325 3578	3350 3603	3376	3401 3654	3426 3679	3452 3704	3477 3729	3502 3754	3528 3779	2	6
172 173	3553 3805	3830	3855	3629 3880	3905	3930	3955	3980	4005	4030	3	9
174	4055	4080	4105	4130	4155	4180	4204	4229	4254	4279	4 5	12 15
175	24304	24329	24353	24378	24403	24428	24452	24477	24502	24527	6	17
176 177	4551 4797	4576 4822	4601 4846	4625 4871	4650 4895	4674	4699 4944	4724 4969	4748 4993	4773 5018	7	20
178	5042	5066	5091	5115	5139	5164	5188	5212	5237	5261	8	23
179	5285	5310	5334	5358	5382	5406	5431	5455	5479	5503	9	26
180	25527	25551	25575	25600	25624	25648	25672	25696	25720	25744	٠,	27
181 182	5768 6007	5792 6031	5816 6055	58 4 0 6079	5864 6102	5888 6126	5912 6150	5935	5959 6198	5983 6221	$\begin{vmatrix} 1 \\ 2 \end{vmatrix}$	3 5
183	6245	6269	6293	6316	6340	6364	6387	6411	6435	6458	3	8
184	6482	6505	6529	6553	6576	6600	6623	6647	6670	6694	4	11
185	26717	26741	26764	26788	26811 7045	26834	26858	26881 7114	26905 7138	26928	5	14
186 187	6951 7184	6975	6998 7231	7021 7254	7277	7068 7300	7091 7323	7346	7370	7161 7393	$\begin{vmatrix} 6 \\ 7 \end{vmatrix}$	16 19
188	7416	7439	7462	7485	7508	7531	7554	7577	7600	7623	8	22
189	7646	7669	7692	7715	7738	7761	7784	7807	7830	7852	9	24
190	27875	27898 8126	27921 8149	27944	27967 8194	27989 8217	28012 8240	28035 8262	28058 8285	28081 8307		25
191	8103 8330	8353	8375	8171	8421	8443	8466	8488	8511	8533	1	3
193	8556	8578	8601	8623	8646	8668	8691	8713	8735	8758	2 3	5 8
194	8780	8803	8825	8847	8870	8892	8914	8937	8959	8981	4	10
195 196	29003 9226	29026 9248	29048 9270	29070 9292	29092 9314	29115 9336	29137 9358	29159 9380	29181 9403	29203 9425	5	13
197	9447	9469	9491	9513	9535	9557	9579	9601	9623	9645	6	15
1.98	9667	9688	9710	9732	9754	9776	9798	9820	9842	9863	7 8	18 20
199	9885	9907	9929 30146	9951	9973 30190	9994	30016	30038	30060	30081 30298	9	23
200	30103	0341	0363	30168 0384	0406	0428	0449	0471		0514		23
202	0535	0557	0578	0600	0621	0643	0664	0685	0707	0728	1	2
203	0750	0771		0814	0835	0856	0878	0899	0920	0942	2	5
204 205	0963 31175	0984 31197	1006 31218	1027 31239	1048 31260	1069 31281	1091 31302	1112 31323	1133 31345	1154 31366	3 4	7 9
206	1387	1408	1429	1450	1471	1492	1513	1534	1555	1576	5	12
207	1597	1618	1639	1660	1681	1702	1723	1744		1785	6	14
208	1805	1827	1848	1869	1890	1911	1931	1952	1973	1994 2201	7	16
209	2015 32222	2035 32243	2056 32263	$\begin{vmatrix} 2077 \\ 32284 \end{vmatrix}$	2098 32305	2118 32325	2139 32346	2160 32366	2181 32387	32408	8 9	18 21
211	2428	2449	2469	2490	2510	2531	2552	2572	2593	2613		21
212	2634	2654	2675	2695	2715	2736	2756	2777	2797	2818	1	2
213	2838	2858	2879	2899	2919 3122	2940 3143	2960 3163	2980 3183	3001	3021 3224	2	4
214 215	3041 33244	3062 3326‡	3082 33284	3102 33304	33325	33345	33365	33385	33405	33425	3	6
216	3445	3465	3486	3506	3526	3546	3566	3586	3606	3626	4 5	8
217	3646	3666		3706	3726	3746	3766	3786	3806	3826	6	13
218	3846	3866		3905 4104	3925 4124	3945 4143	3965 4163	3985 4183	4005 4203	4025 4223	7	15
219 No	4044	4061				5	6	7	8	9	8	17
No.	1 0	1	2	3	1 4) 0	, 0	1 /	, 0	J	9	19

N	o. 220	0 to 2	800.		Loga	rithm	ıs.		34242	to 447	716.
No.	0	1	2	3	4	5	6	7	8	9	20
220	34242	34262	34282	34301	34321	34341	34361	34380	34400	34420	1 2
221	4439	4459	4479	4498	4518	4537	4557	4577	4596	4616	2 4
222	4635	4655	4674	4694	4713	4733	4753	4772	4792	4811	3 6
223 224	4830	4850	4869	4889	4908	4928	4947	4967	4986	5005	4 8
225	5025 35218	5044 35 2 38	5064 35257	5083 35276	5102 35295	5122 35315	5141 35334	5160 35353	5180 35372	5199 35392	5 10 6 12
226	5411	5430	5449	5468	5488	5507	5526	5545	5564	5583	7 14
227	5603	5622	5641	5660	5679	5698	5717	5736	5755	5774	8 16
228	5793	5813	5832	5851	5870	5889	5908	5927	5946	5965	9 18
229 230	5984 36173	6003 36192	$6021 \\ 36211$	6040 36229	6059 36248	6078 36267	6097 36286	6116 36305	6135	6154 36342	19
231	6361	6380	6399	6418	6436	6455	6474	6493	36324 6511	6530	1 2
232	6549	6568	6586	6605	6624	6642	6661	6680	6698	6717	2 4
233	6736	6754	6773	6791	6810	6829	6847	6866	6884	6903	3 6
234	6922	6940	6959	6977	6996	7014	7033	7051	7070	7088	4 8 5 10
235	37107	37125	37144	37162	37181	37199	37218	37236	37254	37273	6 11
236 237	7291 7475	7310 7493	7328 7511	73 4 6 7530	7365 75 4 8	7383 7566	7401 7585	7420 7603	7438 7621	7457 7639	7 13
238	7658	7676	7694	7712	7731	7749	7767	7785	7803	7822	8 15
239	7840	7858	7876	7894	7912	7931	7949	7967	7985	8003	9 17
240	38021	38039	38057	38075	38093	38112	38130	38148	38166	38184	18
241	8202	8220	8238 8417	8256	8274	8292	8310	8328	8346	8364	1 2
242 243	8382 8561	8399 8578	8596	8435 8614	8453 8632	8471 8650	8489 8668	8507 8686	8525 8703	8543 8721	2 4
244	8739	8757	8775	8792	8810	8828	8846	8863	8881	8899	$\begin{bmatrix} 3 & 5 \\ 4 & 7 \end{bmatrix}$
245	38917	38934	38952	38970	38987	39005	39023	39041	39058	39076	5 9
246	9094	9111	9129	9146	9164	9182	9199	9217	9235	9252	6 11
247	9270	9287	9305	9322	9340	9358	9375	9393	9410	9428	7 13
248 249	9 44 5 9620	9463 9637	9480 9655	9498 9672	9515 9690	9533 9707	9550 9724	9568 9742	9585 9759	9602 9777	8 14
250	39794	39811	39829	39846	39863	39881	39898	39915	39933	39950	9 16
251	9967	9985	40002	40019	40037	40054	40071	40088	40106	40123	17
252	40140	40157	0175	0192	0209	0226	0243	0261	0278	0295	$\begin{bmatrix} 1 & 2 \\ 2 & 3 \end{bmatrix}$
253	0312	0329	0346	0364	0381	0398	0415	0432	0449	0466	3 5
254 255	$0483 \\ 40654$	0500 4 0671	40688	0535 40705	$0552 \\ 40722$	0569 407 3 9	$0586 \\ 40756$	$0603 \\ 40773$	0620 40790	0637 40807	4 7
256	0824	0841	0858	0875	0892	0909	0926	0943	0960	0976	5 9
257	0993	1010	1027	1044	1061	1078	1095	1111	1128	1145	6 10
258	1162	1179	1196	1212	1229	1246	1263	1280	1296	1313	7 12· 8 14
259 260	1330 41497	1347 41514	1363 41531	1380 41547	1397 41564	1414 41581	1430 41597	1447 41614	1 464 41631	1481 41647	9 15
261	1664	1681	1697	1714	1731	1747	1764	1780	1797	1814	16
262	1830	1847	1863	1880	1896	1913	1929	1946	1963	1979	1 2
263	1996	2012	2029	2045	2062	2078	2095	2111	2127	2144	2 3
264	2160	2177	2193	2210	2226	2243	2259	2275	2292	2308	3 5
265 266	42325 2488	$42341 \\ 2504$	42357 2521	42374 2537	42390 255 3	$\frac{42406}{2570}$	42423 2586	42439 2602	$42455 \\ 2619$	42 47 2 2635	4 6
267	2651	2667	2684	2700	2716	2732	2749	2765	2781	2797	$\begin{bmatrix} 5 & 8 \\ 6 & 10 \end{bmatrix}$
268	2813	2830	2846	2862	2878	289±	2911	2927	2943	2959	7 11
269	2975	2991	3008	3024	3040	3056	3072	3088	3104	3120	8 13
270	43136	43152	43169	43185		43217	43233	43249	43265	43281	9 14
271 272	3297 3457	3313 3473	3329 3489	33 4 5 3505	3361 3521	3377 3537	3393 3553	340 9 3569	3425 3584	3 44 1 3 6 00	15
273	3616	3632	3648	3664	3680	3696	$\frac{3553}{3712}$	3727	3743	3759	1 2
27+	3775	3791	3807	3823	3838	3854	3870	3886	3902	3917	2 3
275	43 933	43949	43965	43981	43996	44012	44028	44044	44059	44075	3 5 4 6
$\begin{vmatrix} 276 \\ 277 \end{vmatrix}$	4091	4107	4122	4138	4154	4170	4185	4201	4217	4232	5 8
278	4248 4404	4264 4420	4279 4436	4295 4451	4311 4467	4326 4483	4342 4498	4358 4514	4373 4529	4389 4545	6 9
279	4560	4576	4592	4607	4623	4638	4654	4669	4685	4700	7 11
No.		1	2	3	4	5	6	7	8	9	8 12 9 14

No. 2800 to 3400. Logarithms. 44716 to 53148.												3.
No.	()	1	2	3	4	5	(;	7	8	9		16
280	44716	44731	41717	44762	14778	14703	44869	41821	418(0	4 1855	J	2
281	4871	485.6	4902	4917	49.32	4948	4963	4979	4994	5610	2	13
282	5025 5170	5040 5194	5056 5209	5071	5086 5240	5102 5255	5117 5271	5133 5286	5148 5301	5163	3	5
281	5332	6347	5862	6378	6393	5408	6420	5139	5454	5469	13	8
285	45484	45500	45515	46630	45545	45561	45576	45591	45666	45621	6,	10
286	6637	5052	5667	6683	E6397	5712	6728	1574:3	6768	67773	7	11
287 288	6788 6989	5803 594	5818 5969	5834	6849 6000	5864	5879 6636	6045	5509 6060	6975	8 9	18
289	6090	6105	61.20	6135	6150	6165	6180	6195	6210	6225	"	7.5
2111	46240	46255	46276	46285	46300	46315	46330	46315	46059	46371		
201	6380 6538	6404	6419 6568	6431 6583	6598	6461	6627	6494	6557	6523		14 85
202	6687	6762	6716	6731	6746	6761	6776	6790	6865	6820	1	15
2114	6835	6850	6864	63874	6891	6960	63323	63338	613777	65567	2	11
295	46982	46007	47012	47026	47041	47056	47670	470%5	47100	47114	11	6
206	7129 7276	7144	71.9 7305	7173	7188 7834	7202	7217 7363	7232	7246 7352	7261	4	6 8
208	7422	7436	7451	7465	7180	7434	7500	7624	7533	7550	6	9
200	7567	7582	7596	7611	7625	7649	7664	7665	76:43	7698	7	11
300	47712	47727	47741	47756	47770	47784	47799	47 113	47828	47842	8	12
361	7867 8001	7871	78×5 8029	7900	7911 8058	7923	7943	7958 8101	7972 8116	79×6 8139	9	14
303	8111	8159	8173	8187	8202	8216	912236)	8244	1 250	8273		
301	8287	8302	8316	8330	83344	80.559	8::7:3	8387	8491	8416		
305	48430	48444	48158	42473	48487	48501	48515	18584)	48541	445564	1	14
306	8572 8714	8586 8728	8601 8742	8615 8756	8629 8770	8643 8785	2657 8799	8671	8086 8827	8766 8841	1 2	11,
308	8855	8869	8883	8897	8911	8926	8940	8954	8568	8536.Z	33	4
300	8996	9010	9021	9038	51552	\$3(3(36)	9030	5054	9168	9122	3	6
310	49136	49150	49164	49178	49192	49296 9346	49220	49234	43218	184112	5	7 %
311	9276	9290	9301	9457	9471	5485	9499	9513	5521	9511	7	10
313	9554	9668	9582	9596	9610	5024	36:12	9651	9665	36775	4	17
314	9693	9767	9721	97:A	9748	9762	9776	9790	64.50	9717	9	133
316	49831 9969	49845	49859	49872	49886	49900 56037	49914 50051	49927	49941	4/355		
317	50106	50120	59133	6147	0161	0174	6188	142542	(1215	19225		
3318	0243	(1256	0270	(1274	(1/2/37	(3311	18:25	(8:33%)	1811812	18:36%		133
319	6379	(3:3:3:3	6)4(36)	()42()	04333	(M47	0461	1M74	(MA.H.	(15/6)	2	11
3320	50515	60529	60542	6651	60569	6718	6732	(774.)	(178/1)	6772	33	1
322	0786	0799	0813	6826	6840	0853	6%66	(3/2/2/3	6893	(1.4.17	4	8,
323	()()2()	0934	6947	0961	0574	0387	1()()1	1614	16/23	1041	6	7 %
324	1055 51188	51202	51215	1095 51228	51242	51255	51268	512/2	51295	51398	7	3
325	13322	1335	1348	1::62	1875	1388	1402	1415	1428	1441	81	30
327	1455	1468	14*1	1495	150%	1521	15:34	15/4/3	1561	1574	53	12
1128	1587	1601	1614	1627	1646	1854	1687	1680	16/3/3	1766		
1320	51851	1733 51865	51878	1789 51891	1772 51901	1786 51917	51936	1812 61943	1825 51907	1838 51970		46
3331	1983	1696	2009	21/22	2635	2648	2001	2175	2088	2101	1	12
11:12	2114	2127	2110	2153	2186	2179	2192	2215	9218	241	2	2
13:37	2214	2257	2270	2284	22:97	2316	Tris Lis	Lists	243	2512	%	1
3334	2375 52501	52517	2401 52530	52543	2A 27 52556	5/2509	2453	TARKS.	2875 5524486	1/25/21	3	F) 43
336	2631	2647	2666	267:	2686	20%	2711	2741	2787	2:84)	6,	7
23:57	2760	2776	2780	27112	2815	27.27	27/30	Will.	22,856	27.75	7	7.
13:38	2832	29(35)	3046	2930	2943	2554	2565	2584 3110	2054	3135	7.	16
339	3020	(5():3:3									8	11
No.	0	1	2	3	4	5	6	7	8	9		

N	No. 3400 to 4000. Logarithms. Log. 53148 to 60206.											
No.	0	1	2	3	4	5	6	7	8	9	13	
340	53148	53161	53173	53186	53199	53212	53224	53237	53250	53263	1 1	
341	3275	3288	3301	3314	3326	3339	3352	3364	3377	3390	2 3	
342 343	3403 3529	3415 3542	3428 3555	3441	3453 3580	3466 3593	3479 3605	3491 3618	3504 3631	3517 3643	3 4 5	
344	3656	3668	3681	3694	3706	3719	3732	3744		3769	5 7	
345	53782	53794	53807	53820	53832	53845	53857	53870	53882	5 3 895	6 8	
346	3908	3920	3933	3945	3958	3970	3983	3995	4008	4020	7 9	
347 348	4033 4158	4045 4170	4058 4183	4070	4083 4208	4095 4220	4108 4233	4120 4245	4133 4258	4145 4270	8 10 9 12	
349	4283	4295	4307	4320	4332	4345	4357	4370	4382	4394	9 12	
350	54407	54419	54432	54444	54456	54469	54481	54494	54506	54518		
351	4531	4543	4555	4568	4580	4593	4605	4617	4630	4642		
352 353	4654 4777	4667 4790	4679 4802	4691 4814	4704 4827	4716 4839	4728 4851	4741 4864	4753 4876	4765 4888		
354	4900	4913	4925	4937	4949	4962	4974	4986	4998	5011		
355	55023	55035	55047	55060	55072	55084	55096	55108	55121	55133		
356	5145	5157	5169	5182	5194	5206	5218	5230	5242	5255	12	
357 358	5267 5388	5279 5400	5291 5413	5303 5425	5315 5437	5328 5449	5340 5461	5352 5473	5364	5376 5497	$\begin{vmatrix} 1 & 1 \\ 2 & 2 \end{vmatrix}$	
359	5509	5522	5534	5546	5558	5570	5582	5594	5606	5618	3 4	
360	55630	55642	55654	55666	55678	55691	55703	55715	55727	55739	4 5	
361	5751	5763	5775	5787	5799	5811	5823	5835	5847	5859	5 6	
362 363	5871 5991	5883 6003	5895 6015	5907 6027	5919 6038	5931 6050	5943 6062	5955 6074	5967 6086	5979 6098	6 7 8	
364	6110	6122	6134	6146	6158	6170	6182	6194	6205	6217	7 8 8 10	
365	56229	56241	56253	56265	56277	56289	56301	56312	56324	56336	9 11	
366	6348	6360	6372	6384	6396	6407	6419	6431	6443	6455		
367 368	6467 6585	6478 6597	6490 6608	6502 6620	6514 6632	6526 6644	6538 6656	6549 6667	6561 6679	6573 6691		
369	6703	6714	6726	6738	6750	6761	6773	6785	6797	6808		
370	56820	56832	56844	56855	56867	56879	56891	56902	56914	56926	757	
371	6937	6949	6961	6972	6984	6996	7008	7019	7031	7043		
372 373	7054 7171	7066 7183	7078 7194	7089 7206	7101 7217	7113 7229	7124	7136 7252	7148 7264	7159 7276	71.71	
374	7287	7299	7310	7322	7334	7345	7357	7368	7380	7392	11 1	
375	57403	57415	57426	57438	57449	57461	57473	57484	57496	57507	2 2	
376	7519	7530	7542	7553	7565	7576	7588	7600	7611	7623	3 3	
377 378	7634 7749	7646 7761	7657 7772	- 7669 7784	7680 7795	7692 7807	7703	7715 7830	7726 7841	7738 7852	$\begin{vmatrix} 4 & 4 \\ 5 & 6 \end{vmatrix}$	
379	7864	7875	7887	7898	7910	7921	7933	7944	7955	7967	6 7	
380	57978	57990	58001	58013	58024	58035		58058	58070	58081	7 8	
381	8092	8104	8115	8127	8138	8149	8161	8172	8184	8195	8 9	
382 383	8206 8320	8218 8331	8229 83 4 3	8240 8354	8252 8365	8263 8377	8274 8388	8286 8399	8297 8410	8309 8422	9 10	
384	8433	8444	8456	8467	8478	8490	8501	8512	8524	8535		
385	58546	58557	58569	58580	58591	58602	58614	58625	58636	58647		
386 387	8659 8771	8670 8782	8681 8794	8692 8805	8704	8715 8827	8726	8737	8749	8760		
388	8883	8894	8906	8917	8816 8928	8939	8838 8950	8850 8961	8861 8973	8872 8984		
389	8995	9006	9017	9028	9040	9051	9062	9073	9084	9095		
390	59106	59118	59129	59140	59151	59162	59173	59184	59195	59207	10	
391 392	9218 9329	9229 9340	9240 9351	9251 93 62	9262 9373	9273 9384	9284 9395	9295 9406	9306	9318 9428	$\begin{vmatrix} 1 & 1 \\ 2 & 2 \end{vmatrix}$	
393	9439	9450	9461	9472	9483	9494	9506	9517	9417 9528	9539	3 3	
394	9550	9561	9572	9583	9594	9605	9616	9627	9638	9649	4 4	
395	59660	59671	59682	59693	59704	59715	59726	59737	59748	59759	5 5	
396 397	9770 9879	9780 9890	9791 9901	9802 9912	9813 9923	98 24 993 4	9835 99 4 5	9846 9956	985 7 9966	98 6 8 9977	6 6 7	
398	9988	9999	60010	60021	60032	60043	60054	60065	60076	60086	8 8	
399	60097	60108	0119	0130	0141	0152	0163	0173	0184	0195	9 9	
No.	0	1	2	3	4	5	6	7	8	9		
									1 -			

N	No. 4000 to 4600. Logarithms. Log. 60206 to 66276.											
No.	0	1	2	3	4	5	6	7	1 8	9	1 1	1
400	60206	60217	60228	60239	60249	60260	60271	60282	60293	60304	1	1
401	0314	0325	0336	0347	0358	0369	0379	0390	0401	0412	2	2
402	0423 0531	0433 0541	0444 0552	0455 0563	0466 0574	0477 0584	0487	0498	0509 0617	0520 0627	3	3 4
404	0638	0649	0660	0670	0681	0692	0703	0713	0724	0735	4 5	6
405	60746	60756	60767	60778	60788	60799	60810	60821	60831	60842	6	7
406 407	0853 0959	0863	0874	0885	0895	0906	0917	0927	0938	0949	7	8
408	1066	0970 1077	0981	0991 1098	1002 1109	1013 1119	1023 1130	1034 1140	1045 1151	1055 1162		9
409	1172	1183	1194	1204	1215	1225	1236	1247	1257	1268	9 1	
410	61278	61289	61300	61310	61321	61331	61342	61352	61363	61374		
411	1384	1395	1405	1416	1426	1437	1448	1458	1469	1479		
412 413	1490 1595	1500 1606	1511 1616	1521 1627	1532 1637	1542 1648	1553 1658	1563 1669	1574 1679	1584 1690		
414	1700	1711	1721	1731	1742	1752	1763	1773	1784	1794		
415	61805	61815	61826	61836	61847	61857	61868	61878	61888	61899		
416	1909	1920	1930	1941	1951	1962	1972	1982	1993	2003		
418	2014 2118	2024 2128	2034 2138	2045 2149	$2055 \\ 2159$	2066 2170	2076 2180	2086 2190	2097 2201	2107 2211		
419	2221	2232	2242	2252	2263	2273	2284	2294	2304	2315		
420	62325	62335	62346	62356	62366	62377	62387	62397	62408	62418		
421 422	2428 2531	2439 2542	2449	2459	2469	2480	2490	2500	2511	2521		
423	2634	2644	2 5 52 2655	2562 2665	2572 2675	2583 2685	2593 2696	2603 2706	2613 2716	2624 2726		
424	2737	2747	2757	2767	2778	2788	2798	2808	2818	2829	-1	0
425	62839	62849	62859	62870	62880	62890	62900	62910	62921	.62931	1	1
426 427	2941 3043	2951 305 3	2961 3063	2972 3073	2982	2992 3094	3002 3104	3012	3022	3033	2	$\frac{\hat{2}}{3}$
428	3144	3155	3165	3175	3083 3185	3195	3205	3114 3215	3124 3225	3134 3236	3	3
429	3246	3256	3266	3276	3286	3296	3306	3317	3327	3337	4 5	4 5
430	63347	63357	63367	63377	63387	63397	63407	63417	63428	63438	6	6
431 432	3448 3548	3458 3558	3468 3568	3478 3579	3488 3589	3498 3599	3508 3609	3518 3619	3528 3629	3538 3639	7	7
433	3649	3659	3669	3679	3689	3699	37 09	3719	3729	3739		8
434	3749	3759	3769	3779	3789	3799	8809	3819	3829	3839	9	9
435	63849	63859	63869	63879	63889	63899	63909	63919	63929	63939		
436 437	3949 4048	3959 4058	3969 4068	3979 4078	3988 4088	3998 4098	4008 4108	4018 4118	4028 4128	4038		
438	4147	4157	4167	4177	4187	4197	4207	4217	4227	4237		
439	4246	4256	4266	4276	4286	4296	4306	4316	4326	4335		
440	64345	64355	64365	64375		64395		64414		64434		
441	4444 4542	4454 4552	4464 4562	4473	4483 4582	4493 4591	4503 4601	4513 4611	4523 4621	45 3 2 4631		
443	4640	4650	4660	4670	4680	4689	4699	4709	4719	4729		
441	4738	4748	4758	4768	4777	4787	4797	4807	4816	4826		
445 446	64836 4933	64846 4943	64856 4953	64865 4963	64875 4972	64885 4982	64895 4992	64904 5002	64914 5011	64924 5021		
447	5031	5040	5050	5060	5070	5079	5089	5099	5108	5118		
448	5128	5137	5147	5157	5167	5176	5186	5196	5205	5215		
449	5225	5234	5244	5254	5263	5273	5283	5292	5302	5312		0
450 451	6532I 5418	6533 1 5427	65341 5437	65350 5447	65360 5456	65369 5466	65379 5475	65389 5485	65398 5495	65408 5504		9
452	5514	5523	5533	5543	5552	5562	5571	5581	5591	5600	2	$2 \mid$
453	5610	5619	5629	5639	5648	5658	5667	5677	5686	5696	3	3
454	5706	5715	5725	5734	5744	5753	5763	5772	5782	5792	4	4 5
455 456	65801 5896	65811 5906	65820 5916	65830 5925	65839 5935	65849 5944	65858 5954	65868 5963	65877 5973	65887 5982	5 6	5
457	£992	6001	6011	6020	6030	6039	6049	6058	6068	6077	7	6
458	€087	6096	6106	6115	6124	6134	6143	6153	6162	6172	8	7
459	6181	6 1 91	6200	6210	8219	6229	6238	6247	6257	6266	9 8	8
No.	0	1	2	3	4	5	6	7	8	9		

	No. 4600 to 5200. Logarithms. Log. 66276 to 71600.												
No.	0	1	2	3	4	5	6	7	8	9	10		
460	66276	66285	66295	66304	66314	66323	66332	66342	66351	66361	1 1		
461	6370	6380	6389	6398	6408	6417	6427	6436	6445	6455	2 2		
462 463	6464 6558	6474 6567	6483 6577	6492 6586	6502 6596	6511 6605	6521 6614	6530 6624	6539 6 633	6549 6642	3 3 4 4		
464	6652	6661	6671	6680	6689	6699	6708	6717	6727	6736	5 5		
465	66745	66755	6676‡	66773	66783	66792	66801	66811	66820	66829	6 6		
466	6839	6848	6857	6867	6876	6885	6894	6904	6913	6922	7 7		
467	6932	6941	6950	6960	6969	6978	6987	6997	7006	7015	8 8		
468 469	7025 7117	$7034 \\ 7127$	7043 7136	7052	7062	7071	7080 7173	7089 7182	7099 7191	7108	9 9		
470	67210	67219	67228	7145 67237	7154 67247	7164 67256	67265	67274	67284	67293			
471	7302	7311	7321	7330	7339	7348	7357	7367	7376	7385			
472	7394	7403	7413	7422	7431	7440	7449	7459	7468	7477			
473	7486	7495	7504	7514	7523	7532	7541	7550	7560	7569			
474 475	7578 67669	7587	7596 67688	7605	7614	7624	763 3 67724	7642 67733	7 651 67742	7660 67752			
476	7761	67679 7770	7779	67697 7788	67706 7797	67715 7806	7815	7825	7834	7843			
477	7852	7861	7870	7879	7888	7897	7906	7916	7925	7934	11		
478	7943	7952	7961	7970	7979	7988	7997	8006	8015	8024			
479	8034	8043	8052	8061	8070	8079	8088	8097	8106	8115			
480 481	68124 8215	68133	68142 8233	68151	68160	68169	68178 8269	68187 8278	68196 8287	68205 8296			
482	8305	822 4 8314	8323	8242 8332	8251 8341	8260 8350	8359	8368	8377	8386			
483	8395	8404	8413	8422	8431	8140	8149	8458	8467	8476			
484	8485	8494	8502	8511	8520	8529	8538	8547	8556	8565	9		
485	68574	68583	68592	68601	68610	68619	68628	68637	68646	6865 5	1 1		
486	8664	8673	8681	8690	8699	8708	8717	8726	8735	8741	$\begin{bmatrix} 2 & 2 \\ 3 & 3 \end{bmatrix}$		
487 488	8753 88 42	8762 8851	8771 8860	8780 8869	8789 8878	8797 8886	8806 8895	8815 8904	882 4 8913	8833 8922	3 3		
489	8931	8940	8949	8958	8966	8975	8984	8993	9002	9011	4 4		
490	69020	69028	69037	6 9046	69055	69064	69073	69082	69090	69099	5 5 6 5		
491	9108	9117	9126	9135	9144	9152	9161	9170	9179	9188	$\begin{vmatrix} 0 & 3 \\ 7 & 6 \end{vmatrix}$		
492 493	9197 928 5	$9205 \\ 9294$	9214 9302	9223	9232	9241	9249	9258 9346	926 7 935 5	9276	8 7		
494	9373	9381	9390	93 11 9399	9320 9408	9329 9417	$9338 \\ 9425$	9434	9443	9364 94 5 2	9 8		
495	69461	69469	69478	69487	69496	69504	69513	69522	69531	69539			
496	9548	9557	9566	9574	9583	9592	9601	9609	9618	9627			
497	9636	9644	9653	9662	9671	9679	9688	9697	9705	9714	0		
498 499	9723 9810	9732 9819	9740 9827	9749 9836	9758 9845	9767 9854	9775 9862	9784 9871	9793 9880	9801 9888			
500	69897	69906	69914	69923	69932	69940	69949	69958	69966	69975			
501	9984	9992	70001	70010	70018	70027	70036	70044	70053	70062			
502	70070	70079	0088	0096	0105	0114	0122	0131	.0140	0148			
503	0157	0165	0174	0183	0191	0200	0209	0217	0226	0234			
504 505	02±3 70329	0252 70338	0260 70346	0269 70355	$0278 \\ 70364$	$0286 \\ 70372$	$0295 \\ 70381$	0303 70389	0312 70398	0321 70406			
506	0415	0424	0432	0441	0449	0458	0467	0475	0484	. 0492			
507	0501	0509	0518	0526	0535	0544	0552	0561	0569	0578			
508	0586	0595	0603	0612	0621	0629	0638	0646	0655	0563			
509	0672	0680	0689	0697	0706	0714	0723	0731	0740	0749	0		
510 511	70757 0842	70766 0851	70774	70783 0868	70791 0876	70800	70808 0893	70817 0902	70825 0910	70834 0919	8 1 1		
512	0927	0935	0944	0952	0961	0969	0978	0986	0910	1003	2 2		
513	1012	1020	1029	1037	1046	1054	1063	1071	1079	1088	3 2		
514	1096	1105	1113	1122	1130	1139	1147	1155	1164	1172	4 3		
515	71181	71189	71198	71206	71214	71223	71231	71240	71248	71257	5 4 6 5		
516 517	1265 1349	$1273 \\ 1357$	1282 1366	$1290 \ 1374$	$1299 \\ 1383$	1307 1391	1315 1399	1324 1408	1332 1416	1341 1425	6 5 7 6		
518	14 3 3	1441	1450	1458	1466	1475	1483	1403	1500	1508	8 6		
51 9	1517	1525	1533	1542	1550	1559	1567	1575	1584	1592	9 7		
OLU													

_N	No. 52	00 to 8	5800.		Loga	rithn	ıs.	Log. 7	1600	to 763	343	•
No.	0	1	2	3	1 4	5.	1 6	7	18	9	1	0
520	71600	71609	71617	71625	71634	71642	71650	71659	71667	71675	11	9
521	1684	1692	1700	1709	1717	1725	1734	1742	1750	1759		1 2 3
522	1757	1775	1784	1792	1800	1809	1817	1825	1834	1842	3	3
523	1850	1858	1867	1875	1883	1892	1900	1908	1917	1925	4	4
524	1933 72016	1941	1950	1958	1966	1975	1983	1991	1999	2008		5
525 526	2010	72024 2107	72032 2115	72041 2123	72049 2132	72057 2140	72066	72074	72082	72090		5
527	2181	2189	2198	2206	2214	2222	2148 2230	2156 2239	2165 2247	2173 2255	7 8	6
528	2263	2272	2280	2288	2296	2304	2313	2321	2329	2337	9	7 8
529	23.16	2354	2362	2370	2378	2387	2395	2403	2411	2419	-	
530	72428	72436	72444	72452	72469	72469	72477	72485	72493	72501		
531	2509	2518	2526	2534	2542	2550	2558	2567	2575	2583		
532 533	2591 2673	2599	2607	2616	2624	2632	2640	2648	2656	2665		
534	2754	2681 2762	2689 2770	2697 2779	2705 2787	2713 2795	2722 2803	2730 2811	2738 2819	2746		
535	72835	72843	72852	72860	72868	72876	72884	72892	72900	72908		
536	2916	2925	2933	2941	2949	2957	2965	2973	2981	2989		
537	2997	3006	3014	3022	3030	3038	3046	3054	3062	3070		
538	3078	3086	3094	3102	3111	3119	3127	3135	3143	3151		
539	3159	3167	3175	3183	3191	3199	3207	3215	3223	3231		
540 541	73239 3320	73247 3328	73255 3336	73263 3344	73272	73280 3360	73288 3368	73296 3376	73304	73312 3392		
542	3400	3408	3416	3424	3352 3432	34 40	3448	3456	3384 3464	3472		
543	3480	3488	34.96	3504	3512	3520	3528	3536	3544	3552		
544	3560	3568	3576	3584	3592	3600	3608	3616	3624	3632		0
545	73640	73648	73656	73664	73672	73679	73687	73695	73703	73711	7.	8
546	3719	3727	3735	3743	3751	3759	3767	3775	3783	3791	$\begin{vmatrix} 1 \\ 2 \end{vmatrix}$	2
547	3799	3807	3815	3823	3830	3838	3846	3854	3862	3870	3	2
548 549	3878 3957	3886	3894	3902 3981	3910	3918 3997	3926 4005	3933 4013	3941	3949 4028	4	3
550	74036	$\frac{3965}{74044}$	3973 7 4 052	74060	3989 74068	74076	74084	74092	4020 74099	74107	5	4
551	4115	4123	4131	4139	4147	4155	4162	4170	4178	4186	6	5
552	4194	4202	4210	4218	4225	4233	4241	4249	4257	4265	7 8	6
553	4273	4280	4288	4296	4304	4312	4320	4327	4335	4343	9	6 7
554	4351	4359	4367	4374	4382	4390	4398	4406	4414	4421	0	
555	74429	74437	74445	74453	74461	74468	74476	74484	74492	74500		
556 557	4507 4586	4515 4593	4523 4601	4531 4609	4539 4617	4547 4624	$4554 \\ 4632$	45 6 2 4640	4570 4648	4578 46 5 6		
558	4663	4671	4679	4687	4695	4702	4710	4718	4726	4733		
559	4741	4749	4757	4764	4772	4780	4788	4796	4803	4811		
500	74819	74827	74834	74842	74850	74858	74865	74873	74881	74889		
561	4896	4904	4912	4920	4927	4935	4943	4950	4958	4966		
562 563	4974	4981	4989	4997	5005	5012 5089	5020 5097	5028 5105	5035 5113	5043 5120		
564	5051 5128	5059 5136	5066 5143	5074 5151	5082 5159	5166	5174	5182	5189	5120		
565	75205	75213	75220	75228	75236	75243	75251	75259	75266	75274		
566	5282	5289	5297	5305	5312	5320	5328	5335	5343	5351		
567	5358	5366	5374	5381	5389	5397	5404	5412	5420	5427		
568	5435	5442	5450	5458	5465	5473	5481	5488	5496	5504		
569	5511	5519	5526	5534	5542	5549	5557 75633	5565	5572	5580		7
57() 571	75587 5664	75595 5671	75603 5679	75610 5686	75618 5694	75626 5702	5709	75641 5717	75648 5724	75656 5732	11	1
572	5740	5747	5755	5762	5770	5778	5785	5793	5800	5808	2	1
573	5815	5823	5831	5838	5846	5853	5861	5868	5876	5884	3	2
574	5891	5899	5906	5914	5921	5929	5937	5944	5952	5959	4	3
575	75967	75974	75982	75989	75997	76005	76012	76020	76027	76035	5	4
576	6042	6050	6057	6065	6072	6080	6087	6095	6103	6110	$\begin{vmatrix} 6 \\ 7 \end{vmatrix}$	5
577 578	6118	6125	6133	6140	6148	6155	6163	6170	6178	6185 6260	8	6
579	6193 6268	6200 6275	6208 6283	6215 6290	6223 6298	6230 6305	6238 6313	6245 6320	6253 6328	6335	9	6
No.	-							1				-1
10.	0	1 1	2	3	4	5	6	7	8	9 1		

N	No. 5800 to 6400. Logarithms. Log. 76343 to 80618.												
No.	0	1	2	3	4	5	6	7	8	9		8	
580	76343	76350	76358	76365	76373	76380	76388	76395	76403	76410	1		
581	6418	6425	6433	6440	6448	6455	6462	6470	6477	6485		1 2 2	
582	6492	6500	6507	.6515	6522	6530	6537	6545	6552	6559 6634	2	3	
583 584	6567 6641	6574 6649	6582 6656	6589	6597 6671	6604 6678	6612	6619	6626 6701	6708		3 4	
585	76716	76723	76730	76738	76745	76753	76760	76768	76775	76782	6	5	
586	6790	6797	6805	6812	6819	6827	6834	6842	6849	6856	7	6	
587	6864	6871	6879	6886	6893	6901	6908	6916	6923	6930	8	6	
588	6938	6945	6953	6960	6967	6975	6982	6989	6997	7004 7078	9	7	
589 590	7012 77085	7019 77093	7026 77100	7034 77107	7041 77115	7048	7056 77129	7063 77137	7070 77144	77151			
591	7159	7166	7173	7181	7188	7195	7203	7210	7217	7225			
592	7232	7240	7247	7254	7262	7269	7276	7283	7291	7298			
593	7305	7313	7320	7327	7335	7342	7349	.7357	736±	7371			
594	7379	7386	7393	7401	7408	7415	7422	7430	7437	7444			
595 596	77452 7525	77459	77466	77474	77481	77488	77495 7568	77503 7576	77510 7583	77517 7590			
597	7597	7532 7605	7539 7612	7546 7619	7554 7627	7561 7634	7641	7648	7656	7663			
598	7670	7677	7685	7692	7699	7706	7714	7721	7728	7735			
599	7743	7750	7757	7764	7772	7779	7786	7793	7801	7808			
600	77815	77822	77830	77837	77844	77851	77859	77866	77873	77880			
601	7887	7895	7902	7909	7916	7924	7931	7938	7945	7952			
602	7960 8032	7967 8039	7974 80 4 6	7981 8053	7988	7996	8003 8075	8010 8082	8017 8089	8025 809 7	•		
604	8104	8111	8118	8125	8061 8132	8068 8140	8147	8154	8161	8168			
605	78176	78183	78190	78197	78204	78211	78219	78226	78233	78240	71	7	
606	8247	8254	8262	8269	8276	8283	8290	8297	8305	8312	$\begin{vmatrix} 1 \\ 2 \end{vmatrix}$	1	
607	8319	8326	8333	8340	8347	8355	8362	8369	8376	8383	$\begin{vmatrix} 2 \\ 3 \end{vmatrix}$	2	
608	8390	8398	8405	8412	8419	8426	8433	8440	8447	8455	4	3	
609	8462 78533	8469 78540	8476 78547	8483 78554	8490 78561	8497 78569	8504 78576	8512 78583	8519 78590	8526 78597	5	4	
611	8604	8611	8618	8625	8633	8640	8647	8654	8661	8668	6	4	
612	8675	8682	8689	8696	8704	8711	8718	8725	8732	8739	7 8	5 6	
613	8746	8753	8760	8767	8774	8781	8789	8796	8803	8810	9	6	
614	8817 78888	8824	8831	8838	8845	8852	8859	8866	8873	8880	41		
615	8958	78895 8965	78902 8972	78909 8979	78916 8986	78923 8993	78930 9000	78937 9007	78944 9014	78951 9021			
617	9029	9036	9043	9050	9057	9064	9071	9078	9085	9092			
618	9099	9106	9113	9120	9127	9134	9141	9148	9155	9162			
619	9169	9176	9183	9190	9197	9204	9211	9218	9225	9232			
620		79246	79253	79260	79267	79274	79281	79288		79302			
621 622	9309 9379	9316 9386	93 2 3 9393	9330 9400	9337 9407	9344 9414	9351 9421	935.8 9428	9365 9435	9372 - 9442			
623	9449	9456	9463	9470	9477	9484	9491	9498	9505	9511			
€24	9518	9525	9532	9539	9546	9553	9560	9567	9574	9581			
125	79588	79595	79602	79609	79616	79623	79630	79637	79644	79650			
626	9657	9664	9671	9678	9685	9692	9699	9706	9713	9720			
627 628	9727 9796	9734	9741	9748	9754	9761	9768	9775	9782	9789			
629	9865	9803 9872	9810 9879	9817 9886	982± 9893	9831 9900	9837 9906	9844 9913	$\begin{vmatrix} 9851 \\ 9920 \end{vmatrix}$	9858 9927			
630	79934	79941	79948	79955	79962	79969	79975	79982	79989	79996		6	
631	80003	80010	80017	80024	80030	80037	80044	80051	80058	80065	1	1	
632	0072	0079	0085	0092	0099	0106	0113	0120	0127	0134	2	1	
633	0140 0209	$0147 \\ 0216$	$\begin{array}{c c} 0154 \\ 0223 \end{array}$	$0161 \\ 0229$	0168	0175	$0182 \\ 0250$	0188	0195	0202	3	2	
635	80277	80284	80291	80298	0236 80305	0243 80312	80318	0257 80325	0264 80332	0271 80339	5	$\frac{2}{3}$	
636	0346	0353	0359	0366	0373	0380	0387	0393	0400	0407	6	4	
637	0414	0421	0428	0434	0441	0448	0455	0462	0468	0475	7	4	
638	0482	0489	0496	0502	0509	0516	0523	0530	0536	0543	8	5	
6 39	0550	0557	0564	0570	0577	0584	0591	0598	0604	0611	9	5	
No.	0	1	2	3	4	5	6	7	8	9			

N	No. 6400 to 7000. Logarithms. Log. 80618 to 84510.												
No.	0	1	2	3	4	5	6	7	8	9			
640	80618	80625	80632	80638	80645	80652	80659	80665	80672	80679		17	
641	0686	0693	0699	0706	0713	0720	0726	0733	0740	0747	1	1	
642	0754	0760	0767	0774	0781	0787	0794	0801	0808	0814	2	1	
643	0821	0828	0835	0841	0848	0855	0862	0868	0875	0882	3	2	
644	0889	0895	0902	0909	0916	0922	0929	0936	0943	0949	4	3 4	
645	80956	80963	80969	80976	80983	80990	80996	81003	81010	81017	$\begin{vmatrix} 5 \\ 6 \end{vmatrix}$	4	
646	1023 1090	1030 1097	1037	1043 1111	1050	1057	1064 1131	1070 1137	1077 1144	1084 1151	7	5	
647	1158	1164	1104 1171	1178	1117 1184	1124 1191	1198	1204	1211	1218	8	6	
649	1224	1231	1238	1245	1251	1258	1265	1271	1278	1285	9	6	
650	81291	81298	81305	81311	81318	81325	81331	81338	81345	81351	-		
651	1358	1365	1371	1378	1385	1391	1398	1405	1411	1418			
652	1425	1431	1438	1445	1451	1458	1465	1471	1478	1485			
653	1491	1498	1505	.1511	1518	1525	1531	1538	1544	1551			
654	1558	1564	1571	1578	1584	1591	1598	1604	1611	1617		- 1	
655	81624 1690	81631	81637 1704	816 44 1710	81651 1717	81657 1723	81664 1730	81671 1737	81677 1743	81684 1750			
656	1757	1763	1770	1776	1783	1790	1796	1803	1809	1816			
658	1823	1829	1836	1842	1849	1856	1862	1869	1875	1882			
659	1889	1895	1902	1908	1915	1921	1928	1935	1941	1948			
660	81954	81961	81968	81974	81981	81987	81994	82000	82007	82014			
661	2020	2027	2033	2040	2046	2053	2060	2066	2073	2079			
662	2086	2092	2099	2105	2112	2119	2125	2132	2138	2145			
663	2151	2158	2164	2171	2178	2184	2:91	2197	2204	2210			
664	2217 82282	2223 82289	2230 82295	2236 82302	2243 82308	2249 82315	2256 82321	2263 82328	2269 82334	2276 82341			
665	2347	2354	2360	2367	2373	2380	2387	2393	24 00	2406			
667	2413	2419	2426	2432	2439	2445	2452	2458	2465	2471			
668	2478	2484	2491	2497	2504	2510	2517	2523	2530	2536			
669	2543	2549	2556	2562	2569	2575	2582	2588	2595	2601			
670	82607	82614	82620	82627	82633	82640	82646	82653	82659	82666			
671	2672	2679	2685	2692	2698	2705	2711	2718	2724	2730			
672	2737	2743	2750	2756	2763	2769	2776 2840	2782 2847	2789 2853	2795 2860			
673 674	2802 2866	2808 2872	2814 2879	2821 2885	2827 2892	2834 2898	2905	2911	2918	2924			
675	82930	82937	82943	82950	82956	82963	82969	82975	82982	82988			
676	2995	3001	3008	3014	3020	3027	3033	3040	3046	3052			
677	3059	3065	3072	3078	3085	3091	3097	3104	3110	3117			
678	3123	3129	3136	3142	3149	3155	3161	3168	3174	3181			
679	3187	3193	3200	3206	3213	3219	3225	3232	3238	3245			
680	83251	83257	83264	83270		83283		3359	83302 3366	83308 3372			
681 682	3315	3321	3327 3391	3334 3398	3340 3404	3347 3410	3353 3417	3423	3429	3436			
683	3378 3442	3448	3455	3461	3467	3474	3480	3487	3493	3499			
68±	3506	3512	3518	3525	3531	3537	3544	3550	3556	3563			
685	83569	83575	83582	83588	83594	83601	83607	83613	83620	83626		6	
686	3632	3639	3645	3651	3658	3664		3677	3683	3689	1	1	
687	3696	3702	3708	3715	3721	3727	3734	3740	3746	3753	2	1	
688	3759	3765	3771	3778	3784	3790	3797	3803	3809	3816	3 4	2 2	
689	3822	3828	3835	3841	3847	3853 83916	3860 83923	3866 83929	3872 83935	3879 83942	5	3	
690	83885	83891	83 897 3 960	83904 3967	83910 3973	3979	3985	3992	3998	4004	6	4	
691 692	4011	4017	4023	4029	4036	4042	4048	4055	4061	4067	7	4	
693	4073	4080	4086	4092	4098	4105	4111	4117	4123	4130	8	5	
694	4136	4142	4148	4155	4161	4167	4173	4180	4186	4192	9	5	
695	84198	84205	84211	84217	84223	84230	84236	84242	84248	84255			
696	4261	4267	4273	4280	4286	4292	4298	4305	4311	4317			
697	4323	4330	4336	4342	4348	4354	4361	4367	4373	4379			
698	4386	4392	4398	4404		4417	4423 4485	4429	4435 4497	4442 4504			
699	4448	4454	4460	4466	4473	4479	4						
No.	0	1	1 2	3	4	5	6	7	8	9	1		

	N	o. 70	00 to '	7600.		Loga	rithn	ns.	Log. 8	3 4 51 0	to 880	81.	,
	No.	0	1	2	3	14	5	6	7	18	9	1	
	700	84510	84516	84522	84528	84535	84541	84547	84553	84559	84566		7
ì	701	4572	4578	4584	4590	4597	4603		4615	4621	4628	$\begin{vmatrix} 1\\2 \end{vmatrix}$	1 1
	702	4634	4640	4646	4652	4658	4665		4677	4683	4689	3	2
	703 704	4696 4757	4702 4763	4708 4770	4714 4776	4720 4782	4726 4788	4733 4794	4739 4800	4745 4807	4751 4813	4	3
	705	84819	84825	84831	84837	84844	84850		84862	84868	84874	5	4
	706	4880	4887	4893	4899	4905	4911	4917	4924	4930	4936	6	4
	707	4942	4948	4954	4960	4967	4973	4979	4985	4991	4997	7	5
1	708	5003	5009	5016	5022	5028	5034		5046	5052	5058	8 9	6 6
Н	709 710	5065 85126	5071 S5132	5077 85138	5083	5089 85150	5095 85156	5101 85163	5107 85169	5114 85175	5120 85181	-	0
И	711	5187	5193	5199	5205	5211	5217	5224	5230	5236	5242		
	712	5248	5254	5260	5266	5272	5278	5285	5291	5297	5303		
	713	5309	5315	5321	5327	5333	5339	5345	5352	1358	5364		
1	714	5370	5376	5382	5388	5394	5400	5406	5412	5418	5425		
	715	85431	85437	85443	8544.9	85455	85461	85467	85473	85479	85485		
	716 717	5491 5552	5497 5558	5503 5564	5509 5570	5516 5576	5522 5582	5528 5588	5534 559 4	5540 5600	5546 5606		
	718	5612	5618	5625	5631	5637	5643	5649	5655	5661	5667		
1	719	5673	5679	5685	5691	5697	5703	5709	5715	5721	5727		
	720	85733	85739	85745	85751	85757	85763	85769	85775	85781	85788		
	721	5794	5800	5806	5812	5818	5824	5830	5836	5842	5848		
	722 723	5854 5914	5800 5920	5866 5926	5872 5932	5878 5938	5884 5944	5890 5950	5896 5956	5902 5962	5908 5968		
1	724	5974	5980	5986	5992	5998	6004	6010	6016	6022	6028		0
	725	86034	86040	86046	86052	86058	86064	86070	86076	86082	86088	71 1	6
	726	6094	6100	6106	6112	6118	6124	6130	6136	6141	6147	$\begin{bmatrix} 1 \\ 2 \end{bmatrix}$	1
1	727	6153	6159	6165	6171	6177	6183	6189	6195	6201	6207	$\frac{1}{3}$	2
į	728 729	6213 6273	$6219 \\ 6279$	$6225 \\ 6285$	$6231 \\ 6291$	6237 6297	6243 6303	6249 6308	$6255 \\ 6314$	$6261 \\ 6320$	$6267 \\ 6326$	4	2
	730	86332	86338	86344	86350	86356	86362	86368	86374	86380	86386	5	3
1	731	6392	6398	6404	6410	6415	6421	6427	6433	6439	6445	$\begin{vmatrix} 6 \\ 7 \end{vmatrix}$	4 4
-	732	6451	6457	6463	6469	6475	6481	6487	6493	6499	6504	8	5
	733	6510	6516	6522	6528	6534	6540	6546	6552	6558	6564	9	5
-	734 735	6570 86629	6576 86635	$6581 \\ 86641$	6587 86646	6593 86652	6599 86658	6605 86664	6611 86670	6617 86676	6623 86682		
	736	6688	6694	6700	6705	6711	6717	6723	6729	6735	6741		
	737	6747	6753	6759	6764	6770	6776	6782	67.88	6794	6800		
	738	6806	€812	6817	6823	6829	6885	6841	6847	6853	6859		
ı	739 740	6864 86923	6870 86929	6876 86935	6882 86941	6888 86947	6894 86953	6900 86958	6906 86964	6911 86970	6917 86976		- 1
	741	6982	6988	6994	6999	7005	7011	7017	7023	7029	7035		
	742	7040	7046	7052	7058	7064	7070	7075	7081	7087	7093		
	743	7099	7105	7111	7116	7122	7128	7134	7140	7146	7151		
	744	7157	7163	7169	7175	7181	7186	7192	7198	7204	7210		
1	745 746	87216 7274	872 <i>2</i> 1 7280	87227 7286	87233 7291	87239 7297	87245 7303	87251 7309	87256 7315	87262 7320	87268 7326		
1	747	7332	7338	7344	7349	7355	7361	7367	7373	7379	7384		
	748	7390	7396	7402	7408	7413	7419	7425	7431	7437	7442		
1	749	7448	7454	7460	7466	7471	7477	7483	7489	7495	7500		_
}	750	87506	87512	87518	87523	87529	87535	87541	87547	87552	87558	-1 E	5
1	751 752	7564 7622	7570 7628	7576 7633	7581 7639	7587 7645	7593 7651	7599 7656	7604 7662	7610 7668	7616 7674	$\frac{1}{2}$	1
1	753	7679	7685	7691	7697	7703	7708	7714	7720	7726	7731	3	2
	754	7737	7743	7749	7754	7760	7766	7772	7777	7783	7789	4	2
1	755	87795	87800	87806	87812	87818	87823	87829	87835	87841	87846	5	3
	756	7852	7858	7864	7869	7875	7881	7887	7892	7898	7904	6	3
	757 758	7910 7967	7915 7973	7921 7978	7927 7984	7933 7990	7938 7996	7944 8001	7950 8007	7955 8013	7961 8018	7 8	4 4
	759	8024	8030	8036	8041	8047	8053	8058	8064	8070	8076	9	5
	No.	0	1	2	3	4	5	6	7	8	9		
1		0	-	4 1	0 1	7	0 1	0 1	1 1	0 1	J		

N	No. 760	00 to 8	3200.		Loga	rithm	ıs.	Log. 8	8081	to 913	81.	
No.	0	1	2	3	4	5	6	7	8	9		
760	88081	88087	88093	88098	88104	88110	88116	88121	88127	88133	4	6
761	8138	8144	8150	8156	8161	8167	8173	8178	8184	8190	$\frac{1}{2}$	1
762	8195	8201	8207	8213	8218	8224	8230	8235	8241	8247	3	2
763 764	8252 8309	8258 8315	8264 8321	8270 8326	8275 8332	8281 8338	8287 8343	8292 8349	8298 8355	8304 8360	4	2 3
765	88366	88372	88377	88383	88389	88395	88400	88406	88412	88417	5 6	3 4
766	8423	8429	8434	440	8446	8451	8457	8463	8468	8474	7	4
767 768	8480 8536	8485 8542	8491 8547	8497 8553	8502 8559	\$508 \$564	8513 8570	8519 8576	8525 8581	8530 8537	8	5 5
769	8593	8598	8604	8610	8615	8621	8627	8632	8638	8643	9	5
770	88649	88655	88660	88666	88672	88677	88683	88689	88694	88700		
771	8705	8711	8717	8722	8728	8734	8739	8745	8750	8756		
772	8762 8818	8767 8824	8773 8829	8779 8835	878 4 88 4 0	8790 8846	8795 8852	8801 8857	8807 8863	8812 8868		
774	8574	8880	8885	8891	8897	8902	8908	8913	8919	8925		
775	85930	88936	88941	88947	88953	88958	88964	88969	88975	88981		
776	8986 9042	8992	8997	9003	9009	9014	9020	9025	9031	9037	ш	
778	9098	9048. 9104	9053 9109	9059 9115	9064 9120	9070 9126	9076 9131	9081	9087 9143	9092 9148		- 20
779	9154	9159	9165	9170	9176	9182	9187	9193	9198	9204		
780	89209	89215	89221	89226	89232	89237	89243	89248	89254	89260		
781 782	9265 9321	9271 9326	9276 9332	9282 9337	9287 9343	9293 93 4 8	9298 9354	930 4 9360	9310 9365	9315 9371	ш	
783	9376	9382	9387	9393	9398	9404	9409	9415	9421	9426		
784	9432	9437	9443	9448	9454	9459	9465	9470	9476	9481		
785	89487	89492	89498	89504	89509	89515	89520	89526	89531	89537		
786 787	9542 9597	9548 9603	9553 9€09	9559 9614	9564 9620	9570 9625	9575 9631	9581 9636	9586 9642	9592 9647		
788	9653	9658	9664	9669	9675	9680	9686	9691	9697	9702		
789	9708	9713	9719	9724	9730	9735	9741	9746	9752	9757		
790 791	89763	89768	89774	89779	89785	89790	89796	89801	89807 9862	89812		
792	9818 9873	9823 9878	9829 9883	983 4 9889	9840 9894	98 4 5 9900	9851 9905	9856 9911	9916	$9867 \\ 9922$		
793	9927	9933	9938	9944	9949	9955	9960	9966	9971	9977		
794		9988	9993	9998	90004	90009	90015	90020	90026	90031		
795 796	90037	90042 0097	90048 0102	90053	90059 0113	90064	90069 0124	$ \begin{array}{c c} 90075 \\ 0129 \end{array} $	90080 0135	90086 0140		
797	0146	0 51	0157	0162	0168	0173	0179	0184	0189	0195		
798	0200	0206	0211	0217	0222	0227	0233	0238	0244	0249		
799 800	0255 90309	0260 90314	0266 90320	0271 90325	0276 90331	0282 90336	$0287 \\ 90342$	0293 90347	0298 90352	030 4 90358		
801		0369	0374	0380	0385	0390	0396	0401	0407	0112		
802	0417	0423	0428	0434	0439	0445	0450	0455	0461	0466		
803		0477 0531	0482 0536	0488 0542	0493 0547	$0499 \\ 0553$	$0504 \\ 0558$	0509 0563	0515	0520 0574	10	
805	90580	90585	90590	90596	90601	90607	90612	90617	90623	90628		5
806	0634	0639	0644	0650	0655	0660	0666	0671	0677	0682	1	1
807	0687	0693	0698	0703	0709	0714	0720	0725	0730	0736	2	1
808	0741 0795	0747	0752 0806	0757	0763 0816	0768 0822	0773 0827	0779	0784 0838	0789 0843	3 4	2 2 3
810	90849	90854	90859	90865	90870	90875	90881	90886	90891	90897	5	
811	0902	0907	0913	0918	0924	0929	0934	0940	0945	0950	6	3
812	0956	0961	0966	0972	0977 1030	0982 1036	0988 1041	0993 1046	0998 1052	1004 1057	7 8	4 4
814	1009	1014	1020 1073	1025 1078	1084	1089	1091	1100	1105	1110	9	5
815	91116	91121	91126	91132	91137	91142	91148	91153	91158	91164	- 0	
816	1169	1174	1180	1185	1190	1196	1201	1206	1212	1217		
817	$1222 \\ 1275$	1228 1281	1233 1286	1238 1291	1243 1297	1249 1302	1254 1307	1259 1312	1265 1318	1270 1323		
819	1328	133 1	1339	1344	1350	1355	1360	1365	1371	1376		
No.	_	1	2	3	4	5	6	7	8	9		
					-							

N	No. 8200 to 8800. Logarithms. Log. 91381 to 94448.												
No.	0	1	2	3	4	5	6	7	8	9		6	
820	91381	91387	91392	91397	91403	91408	91413	91418	91424	91429	1	1	
821	1434	1440	1445	1450	1455	1461	1466	1471	1477 1529	1482 1535	2	1	
822 823	1487 1540	1492 1545	1498 1551	1503 1556	1508 1561	1514 1566	1519 1572	1524 1577	1529	1587	3	2 2	
824	1593	1598	1603	1609	1614	1619	1624	1630	1635	1640	4 5	3	
825	91645	91651	91656	91661	91666	91672	91677	91682	91687	91693	6	4	
826	1698	1703	1709	1714	1719	1724	1730	1735	1740	1745	7	4	
827	1751	1756	1761	1766	1772	1777	1782 1834	1787 1840	1793 1845	1798 1850	8	5	
828 829	1803 1855	1808 1861	1814 1866	1819 1871	1824 1876	1829 1882	1887	1892	1897	1903	9	5	
830	91908	91913	91918	91924	91929	91934	91939	91944	91950	91955			
831	1960	1965	1971	1976	1981	1986	1991	1997	2002	2007			
832	2012	2018	2023	2028	2033	2038	2044	2049	2054	2059			
833 834	2065 2117	2070 2122	2075	$2080 \\ 2132$	2085 2137	2091 2143	2096 2148	$2101 \\ 2153$	$2106 \\ 2158$	2111 2163	ш		
835	92169	92174	2127 92179	92184	92189	92195	92200	92205	92210	92215			
836	2221	2226	2231	2236	2241	2247	2252	2257	2262	2267	П.		
837	2273	2278	2283	2288	2293	2298	2304	2309	2314	2319			
838	2324	2330	2335	2340	2345	2350	2355	2361	2366	2371			
839	$2376 \\ 92428$	2381 92433	2387 92438	2392 92443	2397 92449	2402 92454	2407 92459	2412 92464	2418 92469	2423 92474			
841	2480	2485	2490	2495	2500	2505	2511	2516	2521	2526			
842	2531	2536	2542	2547	2552	2557	2562	2567	2572	2578			
843	2583	2588	2593	2598	2603	2609	2614	2619	2624	2629			
844	2634	2639	2645	2650	2655	2660	2665	2670	2675	2681		5	
845	$92686 \\ 2737$	92691 2742	92696 2747	92701 2752	92706 2758	92711 2763	$92716 \\ 2768$	$92722 \\ 2773$	92727 2778	$ \begin{array}{r} 92732 \\ 2783 \end{array} $	1	1	
847	2788	2793	2799	2804	2809	2814	2819	2824	2829	2834	2 3	1 2	
848	2840	2845	2850	2855	2860	2865	2870	2875	2881	2886	4	$\frac{2}{2}$	
849	2891	2896	2901	2906	2911	2916	2921	2927	2932	2937	5	3	
85.)	92942 2993	92947 2998	92952 3003	92957 3008	92962 3013	92967	92973 3024	92978 3029	92983 3034	92988 3039	6	3	
852	3044	3049	3054	3059	3064	3069	3075	3080	3085	3090	7	4	
853	3095	3100	3105	3110	3115	3120	3125	3131	3136	3141	8	5	
854	3146	3151	3156	3161	3166	3171	3176	3181	3186	3192			
855	93197	93202	93207	93212	93217	93222	93227	93232	93237	93242			
856	3247 3298	3252 3303	3258 3308	3263 3313	3268 3318	3273 3323	3278 3328	3283 3334	3288 3339	3293 3344			
858	3349	3354	3359	3364	3369	3374	3379	3384	3389	3394			
859	3 399	3404	3409	3414	3420	3425	3430	3435	3440	3445			
860	93450	93455		93465		93475		93485		93495			
861 862	3500 3551	3505 3556	3510 3561	3515 3566	3520 3571	3526 3576	3531 3581	3536 3586	3541 3591	3546 3596			
863	3601	3606	3611	3616	3621	3626	3631	3636	3641	3646			
864	3651	3656	3661	3666	3671	3676	3682	3687	3692	3697			
865	93702	93707	93712	93717	93722	93727	93732	93737	93742	93747			
866 867	3752	3757	3762	3767	3772	3777	3782	3787	3792	3797			
868	3892 3852	3857	3812 3862	3817 3867	3822 3872	3827 3877	3832 3882	3837 3887	3842 3892	3847 3897	1		
869	3902	3907	3912	3917	3922	3927	3932	3937	3942	3947			
870	93952	93957	93962	93967	93972	93977	93982	93987	93992	93997		4	
871	4002	4007	4012	4017	4022	4027	4032	4037	4042	4047	10	0	
872 873	4052	4057	4062 4111	4067	4072 4121	4077 4126	4082	4086	4091 4141	4096 4146	$\begin{vmatrix} 2 \\ 3 \end{vmatrix}$	1 1	
874		4156	4161	4166	4171	4176		4186	4191	4196		2	
875	94201	94206	94211	94216	94221	94226	94231	94236	94240	94245	5	2 2 2 3	
876	4250	4255	4260	4265	4270	4275	4280	4285	4290	4295	6	2	
877	4300	4305	4310	4315	4320	4325		4335	4340	4345		3	
879	4349 4399	4354	4359 4409	4364 4414	4369 4419	4374 4424		4384 4433	4389 4438	4394 4443		4	
No.		1	2	3		5	6	7	_		-	-	
110	0	1 1	2	1 3	4	1 9	. 0	1 7	8	9			

1	No. 8800 to 9400. Logarithms. Log. 94448 to 97313.												
No.	0	1	2	3	1 4	5	6	7	18	1 9	1		
880	94448	94453	94458	94463	94468	94473	94478	94483	94488	94493	1	5	
881	4498	4503	4507	4512	4517	4522	4527	4532	4537	4542		1	
882	4517	4552	4557	4562	4567	4571	4576	4581	4586	4591	$\begin{bmatrix} \hat{2} \\ 3 \end{bmatrix}$	2	
883	4596	4601	4606	4611	4616	4621	4626	4630	4635	4640	4	2 2 3	
881 885	4645 94694	4650	4655	4660	4665	4670	4675	4680	4685	4689	5	3	
886	4743	94699 4748	94704 4753	94709 4758	94714 4763	94719 4768	94724 4773	94729 4778	9 4 734 4783	94738	6	3	
887	4792	4797	4802	4807	4812	4817	4822	4827	4832	4787 4836	7	4	
888	4841	4846	4851	4856	4861	4866	4871	4876	4880	4885	8 9	4 5	
889	4890	4895	4900	4905	4910	4915	4919	4924	4929	4934	9 1	9	
890	94939	94944	94949	94954	94959	94963	94968	94973	94978	94983			
891	4988	4993	4998	5002	5007	5012	5017	5022	5027	5032			
892 893	5036	5041	5046	5051	5056	5061	5066	5071	5075	5080			
894	5085 5134	5090 5139	5095 5143	5100 5148	5105 5153	5109 5158	5114 5163	5119 5168	5124 5173	5129 5177			
895	95182	95187	95192	95197	95202	95207	95211	95216	95221	95226			
896	5231	5236	5240	5245	5250	5255	5260	5265	5270	5274			
897	5279	5284	5289	5294	5299	5303	5308	5313	5318	5323			
898	5328	5332	5337	5342	5347	5352	5357	5361	5366	5371			
899	5376	5381	5386	5390	5395	5400	5405	5410	5415	5419			
900	95424	95429	95434	95439	95444	95448	95453	95458	95463	95468			
901 902	5472 5521	5477	5482	5487	5492	5497	5501	5506	5511	5516			
903	5569	5525 5574	5530 5578	5535 5583	5540 5588	5545 5593	5550 5598	5554 5602	5559 5507	5564 5612			
904	5617	5622	5626	5631	5636	5641	5646	5650	5655	5660			
905	95665	95670	95674	95679	95684	95689	95694	95698	95703	95708			
906	5713	5718	5722	5727	5732	5737	5742	5746	5751	5756			
907	5761	5766	5770	5775	5780	5785	5789	5794	5799	5804			
908	5809	5813	5818	5823	5828	5832	5837	5842	5847	5852			
909 910	5856 95904	5861 95909	5866 95914	5871 95918	5875 95923	5880 95928	5885 95933	5890 95938	5895 95942	5899 95947			
911	5952	5957	5961	5966	5971	5976	5980	5985	5990	5995			
912	5999	6004	6009	6014	6019	6023	6028	6033	6038	6042			
913	6047	6052	6057	6061	6066	6071	6076	6080	6085	6090			
914	6095	6099	6104	6109	6114	6118	6123	6128	6133	6137			
915	96142	96147	96152	96156	96161	96166	96171	96175	96180	96185			
916 917	6190	6194	6199	6204	6209	6213	6218	6223	6227	6232			
918	6237 6284	6242 6289	$6246 \\ 6294$	6251 6298	6256 6303	6261 6308	6265 6313	6270 6317	6275 6322	$6280 \\ 6327$			
919	6332	6336	6341	6346	6350	6355	6360	6365	6369	6374			
920	96379	96384	96388	96393	96398	96402	96407	96412	96417	96421			
921	6426	6431	6435	6440	6445	6450	6454	6459	6464	6468		i	
922	6473	6478	6483	6487	6492	6497	6501	6506	6511	6515			
923 924	6520	6525	6530	6534	6539	6544	6548	6553	6558	6562			
925	6567 96614	96619	$6577 \\ 96624$	6581 96628	6586 96633	6591 96638	6595 96642	$6600 \\ 96647$	6605 96652	6609 96656		4	
926	6661	6666	6670	6675	6680	6685	6689	6694	6699	6703	1	0	
927	6708	6713	6717	6722	6727	6731	6736	6741	6745	6750	2	1	
928	6755	6759	6764	6769	6774	6778	6783	6788	6792	6797	3	1	
929	6802	6806	6811	6816	6820	6825	6830	6834	6839	6844	4	2	
930	96848	96853	96858	96862	96867	96872	96876	96881	96886	96890	5	2	
931	6895	6900	6904	6909	6914	6918	6923 6970	6928	6932	6937 6984	$\begin{vmatrix} 6 \\ 7 \end{vmatrix}$	2 3	
933	69 42 6988	6946 6993	6951 6997	6956 700 2	6960 7007	6965 7011	7016	6974 7021	6979 7025	7030	8	3	
934	7035	7039	7044	7049	7053	7058	7063	7067	7072	7077	9	4	
935	97081	97086	97090	97095	97100	97104	97109	97114	97118	97123		-	
936	7128	7132	7137	7142	7146	7151	7155	7160	7165	7169			
937	7174	7179	7183	7188	7192	7197	7202	7206	7211	7216			
938	7220	7225	7230	7234	7239	7243	7248	7253	7257	7262			
939	7267	7271	7276	7280	7285	7290	7294	7299	7304	7308			
No.	0	1	2	3	4	5	6	7	8	9			

N	To. 940	00 to 1	10000.		Loga	rithm	ıs.	Log. 9	7313	to 999	96.	
No.	0	1	2	3	4	5	6	7	8	9		=
940	97313	97317	97322	97327	97331	97336	97340	97345	97350	97354	1	5
941	7359	7364	7368	7373	7377	7382	7387	7391	7396	7400	2	ī
942	7405	7410	7414	7419	7424	7428	7433	7437	7442	7447	3	1 2
943 944	7451 7497	7456 7502	7460 7506	7465 7511	7470 7516	7474 7520	7479 7525	7483 7529	7488 7534	749 3 7539	4	2 3
945	97543	97548	97552	97557	97562	97566	97571	97575	97580	97585	5 6	3
946	7589	7594	7598	7603	7607	7612	7617	7621	7626	7630	7	4
947	7635	7640	7644	7649	7653	7658	7663	7667	7672	7676	8	4
948	7681	7685	7690	7695	7699	770 1 7749	7708	7713 7759	7717 7763	7722 7768	9	5
949 9 5 0	7727 9 7772	7731 97777	7736 97782	7740 97786	7745 97791	97795	7754 97800	97804	97809	97813	-	-
951	7818	7823	7827	7832	7836	7841	7845	7850	7855	7859		
952	7864	7868	7873	7877	7882	7886	7891	7896	7900	7905		
953	7909	7914	7918	7923	7928	7932	7937	7941	7946	7950		
954	7 955 9 8000	7 959 9 8005	7964 98009	7968 9 80 1 4	7973 98019	7978 98023	7982 98028	7987 98032	7991 98037	7996 98041		
956	8046	8050	8055	8059	8064	8068	8073	8078	8082	8087		
957	8091	8096	8100	8105	8109	8114	8118	8123	8127	8132		
958	8137	8141	8146	8150	8155	8159	8164	8168	8173	8177		
959	8182	8186	8191	8195	8200	8204	8209	8214	8218 98263	8223 98268		
960	982 27 82 7 2	98232 8277	98236 8281	98241 8286	98245 8290	98250 8295	98254 8299	98259 8304	8308	8313		
962	8318	8322	8327	8331	8336	8340	8345	8349	8354	8358		
963	8363	8367	8372	8376	8381	8385	8390	8394	8399	8403		
964	8408	8412	8417	8421	8426	8430	8435	8439	8444	8448		
965	98453 8498	98457 8502	98462 8507	98466 8511	98471 8516	9 8475 8520	98480 8525	98484 8529	98489 853 4	98493 8538		
967	8543	8547	8552	8556	8561	8565	8570	8574	8579	8583		
968	8588	8592	8597	8601	8605	8610	8614	8619	8623	8628		
969	8632	8637	8641	8646	8650	8655	8659	8664	8668	8673		
970	98677	98682	98686	98691	98695	98700	98704	98709	98713	98717		
971 972	8722 8767	8726 8771	8731 8776	8735 8780	8740 8784	8744 8789	8749 8793	8753 8798	8758 8802	87 6 2 8807		
973	8811	8816	8820	8825	8829	8834	8838	8843	8847	8851		
974	8856	8860	8865	8869	8874	8878	8883	8887	8892	8896		
975	98900	98905	98909	98914	98918	98923	98927	98932	98936	98941		
976	8945 8989	8949 8994	8954 8998	8 958 9003	8963 9007	8967 9012	8972 9016	8976 9021	8981 9025	\$98 5 9029		
978	9034	9038	9043	9047	9052	9056	9061	9065	9069	9074		
979	9078	9083	9087	9092	9096	9100	9105	9109	9114	9118		
980	99123				99140		99149		99158			
981 982	$9167 \\ 9211$	9171 9216	9176 9220	9180 9224	9185 92 2 9	9189 9233	9193 9238	9198 9242	9202 9247	9207 9251		
983	9255	9260	9264	9269		9277	9282	9286	9291	9295		
984	9300	9304	9308	9313	9317	9322	9326	9330	9335	9339		
985	99344	99348	99352	99357	99361	99366		99374		99383		4
986 987	9388 9432	9392 9436	9396 9441	9401 9445	9405 9449	9410 9454	9414 9458	9419 9463	9 4 23 9 4 67	$9427 \\ 9471$	1 2	0
988	9476	9480	9484	9489	9493	9498	9502	9506	9511	9515	3	1
989	9520	9524	9528	9533	9537	9542	9546	9550	9555	9559	4	2
990	99564	99568	99572	99577	99581	99585	99590	99594	99599	99603		2 2 2
991 992	9607 965 1	9612	9616	9621	9625	9629	9634	9638	9642	9647	$\begin{vmatrix} 6 \\ 7 \end{vmatrix}$	3
993	9695	9656	9660 9704	9664	9669 9712	9673	9677 9721	9682 9726	9686 9730	$9691 \\ 9734$	8	3
994	9739	9743		9752	9756	9760	9765	9769	9774	9778	9	4
995	99782	99787	99791	99795	99800	99804	99808	99813	99817	99822		
996	9826	9830	9835	9839	9843	9848	9852	9856	9861	9865		
997	9870 9913	9874	9878 9922	9883	9887 9930	9891 9935	9896 9939	9900	9904	9909 9952		
999	9957	9961	9965	9970	9974	9978	9983	9987	9991	9996		
No.	_	1	2	3	4	5	6	7		9		
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0ъ	0°			Loga	rithms.			179°	111h
M.S.	M	Sine.	Cosecant.	Tangent.	Cotangent.] Secant.	Cosine.	[M	M.S.
00	0	Inf.Neg.	Infinite.	Inf. Neg.		10.00000	10.00000	60	60
4	ĭ	6.46373	13.53627	6.46373	13.53627	00000	00000	59	56
8	2	76476	23524	76476	23524	00000	00000	58	52
12	3	94085	05915	94085	05915	00000	00000	57	48
16	4	7.06579	12.93421	7.06579	12.93421	00000	00000	56	44
20	5	7.16270	12.83730	7.16270	12.83730	10.00000	10.00000	55	40
24	6	24188	75812	24188	75812	00000	00000	54	36
28	7	30882	69118	30882	69118	00000	00000	53	32
32 36	8 9	$36682 \\ 41797$	63318	36682	63318	00000	00000	52	28
40	10	7.46373	58203 12. 53627	41797 7.46373	58203 12.53627	00000 10.00000	00000 1 0.00000	51 50	24 20
44	11	50512	49488	50512	49488	00000	00000	49	16
48	12	54291	45709	54291	45709	00000	00000	48	12
52	13	57767	42233	57767	42233	00000	00000	47	8
56	14	60985	39015	60986	39014	00000	00000	46	4
1	15	7.63982	12.36018	7.63982	12.36018	10.00000	10.00000	45	59
4	16	66784	33216	66785	33215	00000	00000	44	56
8	17	69417	30583	69418.	30582	00001	9,99999	43	52
12 16	18	71900	28100	71900	28100	00001	99999	42	48
20	19 20	74248 7.76475	25752 12.23525	74248 7.76476	25752 12.23524	00001 10.00001	99999 9. 99999	41 40	44 40
24	21	78594	21406	78595	21405	00001	99999	39	36
28	22	80615	19385	80615	19385	00001	99999	38	32
32	23	82545	17455	82546	17454	00001	99999	37	28
36	24	84393	15607	84394	15606	00001	99999	36	24
40	25	7.86166	12.13834	7.86167	12.13833	10.00001	9.99999	35	20
44	26	87870	12130	87871	12129	00001	99999	34	16
48	27	89509	10491	89510	10490	00001	99999	33	12
52	28	91088	08912	91089	08911	00001	99999	32	8
56	29 30	92612	07388	92613	07387 12.05914	00002	99998 9.99998	31 30	4 58
4	31	7.94084 95508	$\begin{array}{c} 12.05916 \\ 04492 \end{array}$	7.94086 95510	04490	10.00002 00002	9,99998	29	56
8	32	96887	03113	96889	03111	00002	99998	28	52
12	33	98223	01777	98225	01775	00002	99998	27	48
16	34	99520	00480	99522	00478	00002	99998	26	44
20	35	8.00779	1 1.99221	8.00781	11.99219	10.00002	9.99998	25	40
24	36	02002	97998	02004	97996	00002	99998	24	36
28	37	03192	96808	03194	96806	00003	99997	23	32
32	38	04350	95650	04353	95647	00003	99997	22	28
36 40	39 40	$05478 \\ 8.06578$	94522 11.93422	05481 8.06581	94519 11.93419	00003 10.00003	99997 9,99997	21 20	24 20
44	41	07650	92350	07653	92347	00003	9,99997	19	16
48	42	08696	91304	08700	91300	00003	99997	18	12
52	43	09718	90282	09722	90278	00003	99997	17	8
56	44	10717	89283	10720	89280	00004	99996	16	4
3	45	8.11693	11.88307	8.11696	11.88304	10.00004	9,99996	15	57
4	46	12647	87353	12651	87349	00004	99996	14	56
8	47	13581	86419	13585	86415	00004	99996	13	52
12	48	14495	85505 84600	14500 15395	85500 84605	00004 00004	99996 99996	12 11	48
16 20	49 50	15391 8.16268	84609 11.83732	8.16273	11.83727	10.00005	9,99995	10	44 40
24	51	17128	82872	17133	82867	00005	99995	9	36
28	52	17971	82029	17976	82024	00005	99995	8	32
32	53	18798	81202	18804	81196	00005	99995	7	28
36	54	19610	80390	19616	80384	00005	99995	6	24
40	55	8.20407	11.79593	8.20413	11.79587	10.00006	9,99994	5	20
44	56	21189	78811	21195	78805	00006	99994	4	16
48	57	21958	78042	21964	78036	00006	99994	3	12
52 50	58	22713	77287	22720	77280	00006	99994	2	8
56	59 60	23456 24186	76544 75814	$ \begin{array}{c c} 23462 \\ 24192 \end{array} $	76538 75808	00006 00007	99994 99993	1	56 56
M.S.		24186 Cosine.		Cotangent		Cosecant.	Sine.		M. S.
	90°	· Cosme.	Becaut.	-Ootangent	Tangent.	Observation 1		890	
	UU							00 1	0

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0h	1°			Loga	rithms.			178	° ₁₁₁
M.S.	M	Sine.	Cosecant.	Tangent.	Cotangent.		Cosine.	M	M.S
4	0	8.24186	11.75814	8.24192	11.75808	10.00007	9.99993	60	
4	1	24903	75097	24910	75090	00007	99993	59	56
8	2	25609	74391	25616	74384	00007	99993	58	52 48
12 16	3 4	26304 26988	73696 73012	26312 26996	73688 73004	00007	99993	57 56	44
20	5	8.27661	11.72339	8.27669	11.72331	10.00008	9.99992	55	40
24	6	28324	71676	28332	71668	00008	99992	54	36
28	7	28977	71023	28986	71014	00008	99992	53	32
32	8	29621	70379	29629	70371	00008	99992	52	28
36	9	30255	69745	30263	69737	00009	99991	51	24
40	10	8.30879	11.69121	8.30888	11.69112	10.00009	9.99991	50	20
44 48	11 12	$31495 \\ 32103$	68505 67897	31505 32112	68495 67888	$00009 \\ 00010$	99991 99990	49 48	16 12
52	13	32702	67298	32711	67289	00010	99990	47	8
56	14	33292	66708	33302	66698	00010	99990	46	4
5	15	8.33875	11.66125	8.33886	11.66114	10.00010	9. 99990	45	55
4	16	34450	65550	34461	65539	00011	99989	44	56
8	17	35018	64982	35029	64971	00011	99989	43	52
12	18	35578	64422	35590	64410	00011	99989	42	48
16	19	36131	63869	36143	63857	00011	99989	41	44
$\frac{20}{24}$:	20 21	8.36678 37217	11.63322 62783	8.36689 37229	11.63311 62771	10.00012 00012	9. 99988 99988	40 39	40 36
28	22	37750	62250	37762	62238	00012	99988	38	32
32	23	38276	61724	38289	61711	00012	99987	37	28
36	24	38796	61204	38809	61191	00013	99987	36	24
40	25	8.39310	11.60690	8.39323	11.60677	10.00013	9.99987	35	20
44	26	39818	60182	39832	60168	00014	99986	34	16
48	27	40320	59680	40334	59666	00014	99986	33	12
52	28	40816	59184	40830	59170	00014	99986	32	8
56 6	29 30	41307 8.41792	58693 11.58208	41321 8.41807	58679 11.58193	00015 10.00015	99985 9.99985	31 30	4 54
4	31	42272	57728	42287	57713	00015	99985	29	56
8	32	42746	57254	42762	57238	00016	99984	28	52
12	33	43216	56784	43232	56768	00016	99984	27	48
16	34	43680	56320	43696	56304	00016	99984	26	44
20	35	8.44139	11.55861	8.44156	11.55844	10.00017	9.99983	25	40
24	36	44594	55406	44611	55389	00017	99983	24	36
$\begin{array}{c} 28 \\ 32 \end{array}$	37 38	45044 45489	54956	45061	54939 54402	00017	99983	23	32 28
36	39	45930	54511 54070	45507 45948	$54493 \\ 54052$	00018 00018	99982 99982	$\frac{22}{21}$	24
40	40	8.46366	11.53634	8.46385	11.53615	10.00018	9.99982	20	20
44	41	46799	53201	46817	53183	00019	99981	19	16
48	42	47226	52774	47245	52755	00019	99981	18	12
52	43	47650	52350	47669	52331	00019	99981	17	8
56	44	48069	51931	48089	51911	00020	99980	16	4
7	45 46	8.48485 48896	11.51515 51104	8.48505 48917	11.51495 51083	10.00020 00021	9.99980	15 14	53 56
8	47	49304	50696	49325	50675	00021	$ \begin{array}{c} 99979 \\ 99979 \end{array} $	13	52
12	48	49708	50292	49729	50271	00021	99979	$\frac{13}{12}$	48
16	49	50108	49892	50130	49870	00022	99978	11	44
20	50	8.50504	11.49496	8.50527	11.49473	10.00022	9,99978	10	40
24	51	50897	49103	50920	49080	00023	99977	9	36
28	52	51287	48713	51310	48690	00023	99977	8	32
32 36	53 54	51673	48327	51696	48304	00023	99977	7	28 24
40	55	52055 8.52434	$\frac{47945}{11.47566}$	52079 8.52459	47921 11.47541	$00024 \ 10.00024$	99976 9. 99976	6 5	20
44	56	52810	47190	52835	47165	00025	99975	4	16
48	57	53183	46817	53208	46792	00025	99975	3	12
52	58	53552	46448	53578	46422	00026	99974	2	8
56	59	53919	46081	53945	46055	00026	99974	1	4
8	60	54282	45718	54308	45692	00026	99974	0	52
M.S.	M O I O	Cosine.	Secant.	Cotangent	Tangent.	Cosecant.	Sine.		M.S.
0" [91°							88°	5 ^b
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N.S. M. Sine. Coseant. Tangent. Cotangent. Secant. Cosine. M. N.S.	Cib	-)0			W				1770	111
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4	I .	E .			2					M.S.
8	1	1 "								52
12										
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24 6 56400 43600 56429 43571 00029 99970 53 32 32 8 57084 42916 57114 42886 00030 99970 53 32 36 9 57421 42579 57452 42548 00031 99999 51 24 40 10 8.57778 11.42213 00032 99968 49 16 44 11 58089 41911 58121 41879 00032 99968 49 16 48 12 58419 41581 58451 41549 90032 99968 48 12 56 14 59072 40228 59105 40895 00033 99967 46 4 4 16 59715 40285 59749 40251 00034 99966 43 52 12 18 60349 39651 60384 39616 00035 99961										40
32							00029	99971	54	36
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44 11 58089 41911 58121 41549 00032 99968 48 12 52 13 58747 41233 58779 41221 00033 99967 47 88 12 56 14 59072 40928 59105 40895 00033 99967 46 4 9 15 8.59395 11.40605 8.59428 11,40572 10,00033 99967 45 51 4 16 59715 40285 59749 40251 00034 99966 44 56 8 17 60033 39967 60682 39382 00034 99966 44 56 12 18 60662 39338 60698 39302 00036 99964 40 44 26 61282 38718 61319 3881 100037 99963 39 36 28 22 61589 38411 61626 38374 00037 9		a -								
48 12 58419 41881 58451 41549 00032 99968 48 12 56 14 59072 40928 59105 40895 00033 99967 47 8 9 15 8.59395 11.40605 8.59428 11.40572 10.00033 99967 45 51 4 16 59715 40285 59749 40251 00034 99966 44 56 8 17 60033 39967 6068 39932 00034 99966 44 56 16 19 60662 39338 60698 39302 00036 99964 44 56 20 20 8.60973 11.39027 8.61009 11.3891 10.00036 9.9964 40 40 22 21 61589 38411 61626 38374 00037 99963 33 36 24 22 61589 38411 61626 <										
56 14 59072 40928 59105 40895 00033 99967 47 8 9 15 8.59395 11.40605 8.59428 11.4072 10.00033 9.9967 45 51 4 16 59715 40285 59749 40251 00034 99966 45 56 8 17 60033 39967 60068 39332 00034 99966 43 52 12 18 60349 39651 60384 39616 00035 99965 42 48 16 19 60662 39338 60938 39302 00036 99964 40 40 24 21 61282 38718 61319 38681 00037 39963 38 32 32 23 61894 38106 61931 38069 90038 99962 37 28 36 24 62196 37205 62834 37166 <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> <td>12</td>										12
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48 57 71151 28849 71208 28792 00058 99942 3 12			71151							
52 58 71395 28605 71453 28547 00058 99942 2 8		_								
$egin{bmatrix} 56 & 59 & 71638 & 28362 & 71697 & 28303 & 00059 & 99941 & 1 & 4 \\ 12 & 60 & 71880 & 28120 & 71940 & 28060 & 00060 & 99940 & 0 & 48 \end{bmatrix}$									_	48
12 60 71880 28120 71940 28060 00060 99940 0 48										
6h 92°			Cosine. 1	Scoult.	Johansenti	Tungono.	Concounte.	DIEG. I	870	5h
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100			JAUGA	RITHMS	I RIGONOM	EIRIC.			
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0 ^h	30			Loga	rithms.		1	76°	11h
M.S.	М	Sine.	Cosecant.	Tangent.	Cotangent.	Secant.	Cosine.	М	M.S.
12	0	8.71880.	11.28120	8.71940	11.28060	10.00060	9.99940	60	4.8
4	1	72120	27880	72181	27819	00060	99940	59	56
8 12	$\frac{2}{3}$	72359 72597	$27641 \\ 27403$	72420 72659	$27580 \\ 27341$	$00061 \\ 00062$	99939 99938	58 57	52 48
16	4	72834	27166	72896	27104	00062	99938	56	41
20	5	8.73069	11.26931	8.73132	11.26868	10.00063	9.99937	55	40
24	6	73303	26697	73366	26634	00064	99936	54	36
28 32	7	73535	26465	73600 73832	26400	00064 00065	99936 99935	53 52	32 28
36	8	73767 73997	$26233 \\ 26003$	74063	$26168 \\ 25937$	00066	99934	51	24
40	10	8.74226	11.25774	8.74292	11.25708	10.00066	9.99934	50	20
44	11	74454	25546	74521	25479	00067	99933	49	16
48	12	74680 ·	25320	74748	25252	00068	99932	48	12
52 56	13 14	74906 75130	25094	74974 75199	$25026 \\ 24801$	00068 00069	99932 9993 1	47	8 4
13	15	8.75353	24870 11.24647	8.75423	11.24577	10.00070	9.99930	45	47
4	16	75575	24425	75645	24355	00071	99929	44	56
8	17	75795	24205	75867	24133	00071	99929	43	52
12	18	76015	23985	76087	23913	00072	99928	42	48
16 20	19 20	$76234 \\ 8.76451$	23766 11. 23549	76306 8.76525	23694 11.23475	00073 10.00074	99927 9.9 9 926	41	44 40
24	21	76667	23333	76742	23258	00074	99926	39	36
28	22	76883	23117	76958	23042	00075	99925	38	32
32	23	77097	22903	77173	22827	00076	99924	37	28
36	24	77310	22690	77387	22613	00077	99923	36	24
40 44	25 26	8.77522 77733	11.22478 22267	8.77600 77811	11.22400 22189	10.00077 00078	9.99923 99922	35 34	$\begin{vmatrix} 20 \\ 16 \end{vmatrix}$
48	27	77943	22057	78022	21978	00079	99921	33	12
52	28	78152	21848	78232	21768	00080	99920	32	8
56	29	78360	21640	78441	21559	00080	99920	31	4
14	30 31	8.78568 78774	11.21432 21226	8.78649 78855	11.21351 21145	10.00081 00082	9.99919 99918	30 29	46 56
8	32	78979	21021	79061	20939	00083	99917	28	52
12	33	79183	20817	79266	20734	00083	99917	27	48
16	34	79386	20614	79470	20530	00084	99916	26	44
20 24	35 36	8.79588 79789	11.20412 20211	8.79673 79875	11.20327 20125	10.00085 00086	9.99915 99914	25	40
28	37	79990	20010	80076	19924	00087	99913	24 23	$\begin{vmatrix} 36 \\ 32 \end{vmatrix}$
32	38	80189	19811	80277	19723	00057	99913	22	28
36	39	80388	19612	80476	19524	00088	99912	21	24
40	40	8.80585	11.19415	8.80674	11.19326	10.00089	9.99911	20	20
44 48	41 42	80782 80978	19218 19022	80872 81068	$\begin{array}{c} 19128 \\ 18932 \end{array}$	00090 00091	999 1 0 99909	19 18	$\begin{vmatrix} 16 \\ 12 \end{vmatrix}$
52	43	81173	18827	81264	18736	00091	99909	17	8
56	44	81367	18633	81459	18541	00092	99908	16	4
15	45	8.81560	11.18440	8.81653	11.18347	10.00093	9.99907	15	45
8	46 47	81752 81944	18248 18056	81846 82038	$18154 \\ 17962$	$00094 \\ 00095$	99906 99905	14 13	56 52
12	48	82134	17866	82230	17770	00096	99904	12	48
16	49	82324	17676	82420	17580	00096	99904	11	44
20	50	8.82513	11.17487	8.82610	11.17 390	10.00097	9,99903	10	40
24 28	51 52	82701 82888	17299	82799	17201	00098	99902 99901	9	36
32	53	83075	17112 16925	82987 83175	$\begin{array}{c c} & 17013 \\ & 16825 \end{array}$	00099 00 1 00	99901	8 7	32 28
36	54	83261	16739	83361	16639	00101	99899	6	24
40	55	8.83446	11.16554	8.83547	11.16453	10.00102	9,99898	5	20
44	56	83630	16370	83732	16268	00102	99898	4	16
48 52	57 58	83813 83996	16187 1 6 004	83916 84100	16084 15900	00103 00104	99897 99896	3 2	12
56	59	84177	15823	84282	15718	00105	99895	1	8 4
16	60	84358	15642	84464	15536	00106	99894	0	44
M.S.		Cosine.	Secant.	Cotangent	Tangent.	Cosecant.	Sine.	M	M.S.
Qu	930							86°	On

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0p	40						1	750	17h
	4° Logarithms. 175°								11,
M.S.	М	Sine.	Cosecant.	Tangent.	Cotangent.	Secant.	Cosine.	M	M. S
16	0	8.84358	11.15642	8.84464	11.15536	10.00106	9.99894	60	44
8	1	84539 84718	15461	84646 84826	15354 15174	00107	99893	59	56
12	$\frac{2}{3}$	84897	15282 15103	85006	14994	00108 00109	99892 99891	58 57	52 48
16	4	85075	14925	85185	14815	00109	99891	56	44
20	5	8.85252	11.14748	8.85363	11.14637	10.00110	9.99890	55	40
24	6	85429	14571	85540	14460	00111	99889	54	36
28	7	85605	14395	85717	14283	00112	99888	53	32
32	8	85780	14220	85893	14107	00113	99887	52	28
36	9	85955 8.86128	$14045 \\ 11.13872$	86069	13931	00114	99886	51	24
40	10 11	86301	13699	8.86243 86417	11.13757 13583	10.00115 00116	9.99885 99884	50 49	20 16
48	12	86474	13526	86591	13409	00117	99883	48	12
52	13	86645	13355	86763	13237	00118	99882	47	8
56	14	86816	13184	86935	13065	00119	99881	46	4
17	15	8.86987	11.13013	8.87106	11.12894	10 .00120	9.99880	45	43
4	16	87156	12844	87277	12723	00121	99879	44	56
8 12	17	87325 87494	$12675 \\ 12506$	874 1 7 87616	12553 12384	00121	99879	43	52
16	18 19	87661	12339	87785	12384 12215	$00122 \\ 00123$	99878 99877	42 41	48 44
20	20	8.87829	11.12171	8.87953	11.12047	10.00124	9.99876	40	40
24	21	87995	12005	88120	11880	00125	99875	39	36
28	22	88161	1 1839	88287	1 1713	00126	99874	38	32
32	23	88326	11674	88453	11547	00127	99573	37	28
36	24	88490	11510	88618	11382	00128	99872	36	24
40	25	8.88654 88817	11.11346 11183	8.88783 88948	11.11217 11052	10.00129 00130	9.99871	35 34	20 16
44 48	26 27	88980	11020	89111	10889	00130	99870 99869	33	12
52	28	89142	10858	89274	10726	00132	99868	32	8
56	29	89304	10696	89437	10563	00133	99867	31	4
18	30	8.89464	11.10536	8.89598	11.10402	10.00134	9.99866	30	42
4	31	89625	10375	89760	10240	00135	99865	29	56
8	32	89784	10216	89920	10080	00136	99864	28	52 48
12 16	33 34	89943 90102	10057 09898	90080 90240	09920 09760	00137 00138	99863 99862	27 26	48
20	35	8.90260	11.09740	8.90399	11.09601	10.00139	9.99861	$\begin{vmatrix} 25 \\ 25 \end{vmatrix}$	40
24	36	90417	09583	90557	09443	00140	99860	24	36
28	37	90574	09426	90715	09285	00141	99859	23	32
32	38	90730	09270	90872	09128	00142	99858	22	28
36	39	90885	09115	91029	08971	00143	99857	21	24
40	40	8.91040 91195	11.08960 08805	8.91185	11.08815 08660	10.00144	9.99856 99855	20 19	20 16
44 48	41 42	91349	08651	91340 91495	08505	00145	99854	18	12
52	43	91502	08498	91650	08350	00147	99853	17	8
56	44	91655	08345	91803	08197	00148	99852	16	4
19	45	8.91807	11.08193	8.91957	11.08043	10.00149	9.99851	15	41
4	46	91959	08041	92110	07890	00150	99850	14	56
8	47	92110	07890	92262 9241 4	07738 07586	$00152 \\ 00153$	99848 99847	13 12	52 48
12 16	48 49	92261 92411	07739 07589	92414	07435	$00153 \\ 00154$	99846	12 11	44
20	50	8.92561	11.07439	8.92716	11.07284	10.00155	9.99845	10	40
24	51	92710	07290	92866	07134	00156	99844	9	36
28	52	92859	07141	93016	06984	00157	99843	8	32
32	53	93007	06993	93165	06835	00158	99842	7	28
36	54	93154	06846	93313	06687	00159	99841	6	24
40	55 56	8.93301 93448	11.06699 06552	8.93462 93609	11.06538 06391	$\begin{array}{c} 10.00160 \\ 00161 \end{array}$	9.99840 99839	5 4	20 16
44 48	57	93448	06406	93756	$06391 \\ 06244$	00161	99838	3	10 12
52	58	93740	06260	93903	06097	00163	99837	2	8.
56	59	93885	06115	94049	05951	00164	99836	1	4
20	60	94030	05970	94195	05805	00166	99834	0	40
M.S		Cosine.	Secant.	Cotangent	Tangent.	Cosecant.	Sine.	M	M.S.
6h	94°							85°	5ª

N.S. M. Sine. Cosecant. Tangent. Cotangent. Secant. Cosine. M. M.S. M. Sine. Cosecant. Tangent. LoSs05 10.00166 9.99834 60 40 4 1 94174 05826 94340 05660 00167 99833 59 56 56 56 56 56 56 56	100			13002	111111111111111111111111111111111111111	INICONOM	ETICIO.			-
20	0h	5°			Loga	rithms.		· · · · · · · · · · · · · · · · · · ·	174	115
4 1 94174 05826 94345 056515 00168 99332 58 52 12 3 94461 05839 94630 05370 00169 99831 57 48 10 4 94636 05397 9473 06227 00170 99830 56 44 20 5 8,94746 11.05254 8,94917 11.05083 10.00171 9,99820 55 40 23 7 95022 04978 00173 99827 53 32 36 9 93310 04690 9486 04514 00175 99824 51 24 40 10 8,95450 04421 95767 0433 00178 99822 49 16 41 11 95580 04421 95767 0433 00178 99822 49 16 28 13 9461 96896 04320 00179 99821 48 12		M							_	M.S.
S										
12 5										
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24 6 94587 65113 95000 04970 04778 00173 99827 53 36 36 9 93310 04690 95344 04656 00176 99824 51 24 40 10 8,99450 11,04550 8,35627 11,04373 10,00177 99824 51 24 44 11 95589 04411 95767 04233 00173 99822 49 16 48 12 95728 04272 95008 04092 00173 99821 41 16 99820 47 8 12 13 95867 04133 96047 03533 00180 99820 47 8 21 15 8,96133 10,3618 99810 44 7 96220 03383 96018 03813 96916 44 7 96417 96333 00186 99816 44 39 36 224 19 96629 03311 <td< td=""><td>20</td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td></td<>	20									
28										
196 9 95310 04990 95486 04514 00176 99824 50 20 24 11 95589 04411 95767 04233 00178 99822 49 16 28 28 28 28 28 28 28 2	28		95029		95202		00173			32
44	32						00175			
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As 12 95728 04272 95908 04492 00179 99821 48 12 52 13 95867 04133 96047 03953 00180 99820 47 8 86043 11.03857 8.96325 11.03675 10.00183 9.99817 45 34 46 96280 03720 96464 03536 00184 99816 44 56 8 17 96417 03583 96602 03398 00185 99815 43 52 12 18 96553 03347 96739 03261 00186 99814 42 48 48 48 48 49 48 48 48										
52 13 95807 04133 96047 03935 00180 99820 47 8 56 14 96005 03935 96187 03813 00181 99817 46 4 21 15 8.96143 11.08857 8.96325 11.03675 10.00183 9.99817 45 39 4 16 96280 03720 96464 03536 00186 99814 42 43 52 12 18 96553 03447 96739 03261 00186 99814 42 48 20 20 8.96825 11.03175 8.97013 11.02987 10.00188 9.99812 40 40 28 22 97029 02711 97421 02570 00192 99808 37 28 36 24 97363 02637 97426 02444 00193 99806 35 20 48 27 977629 02371					95707					
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4 16 66280 63720 96464 63536 60184 99816 44 56 8 17 96417 03583 96602 03398 00185 99815 43 52 12 18 96553 03447 96733 03261 00186 99814 42 42 20 20 8,06825 11,03175 8,97013 11,02987 10,00188 9,99812 40 40 24 21 96960 03040 97150 02850 00190 99810 39 36 28 22 97095 02905 97285 02715 00191 99800 38 32 32 23 97229 02771 97421 02579 00192 99808 37 28 36 24 97363 02637 97556 02444 00193 99806 35 20 44 26 97629 02371 97825 02175 00194 9,99806 35 20 44 26 97629 02371 97825 02175 00194 9,99806 35 20 48 27 97762 02238 97959 02041 00197 99803 33 12 52 28 97894 02106 98092 01908 00198 99802 32 8 56 29 98026 01974 98225 01775 00198 99802 32 8 4 31 98288 01712 98490 01510 00202 99708 29 56 8 32 98419 01581 98622 01378 00204 99796 27 48 12 33 98549 01451 98753 01247 00204 99796 27 48 16 34 98679 01321 98884 01116 00202 99798 29 56 24 36 98937 01063 99145 00855 00208 99792 24 36 24 36 98937 01063 99145 00855 00209 99791 23 32 25 37 99066 00934 99275 00725 00209 99791 23 32 36 39 99322 00678 99534 00466 00212 99788 19 14 40 40 8.99450 11.00550 8.99662 11.00338 10.00213 9.99787 12 24 40 40 8.99450 11.00550 8.99662 11.00338 10.00213 9.9978 16 4 20 50 9.00704 10.99266 00444 00714 99826 00218 99775 10 40 44 6 00207 99793 00427 99573 00224 99776 11 44 20 50 9.00704 10.98682 400669 90697 00224 99777 12 48 50 9.00704 10.98682 400679 99321 00223 99777 12 48 50 9.00704 10.98682 400679 99321 00224 99777 10 40 44 6 001923 99860			8.96143	11.03857	8.96325					
12						03536				
Tell						03398				
Dec 20										
24 21 96960 03040 97150 02350 00190 99810 39 36 28 22 97095 02905 97285 02715 00191 99808 37 28 36 24 97363 02637 97556 02444 00193 99807 36 24 40 25 8.97496 11.02504 8.97691 11.02309 10.00194 9.99806 35 20 48 27 97762 02238 97959 02041 00197 99803 31 12 52 28 97894 02106 98092 01908 00198 99802 32 8 56 29 98026 01974 98225 01775 00199 99801 31 4 22 30 8.98157 11.01843 8.9838 11.01642 10.00200 9.9980 30 38 4 31 98288 01712 98849										
28 22 97095 02905 97285 02715 00191 99809 38 32 32 23 97229 02771 97421 02579 00192 99808 37 28 28 97363 02637 97556 02444 00193 99807 36 24 24 26 97629 02371 97825 02175 00194 9.99806 35 20 24 26 97629 02371 97825 02175 00196 99804 34 16 25 28 97894 02106 98092 01908 00198 99802 32 8 25 28 97894 02106 98092 01908 00198 99802 32 8 25 28 97894 02106 98092 01908 00198 99802 32 8 22 30 8.98157 11.01843 8.88358 11.01642 10.00200 9.99800 30 38 32 24 31 98288 01712 98490 01510 00202 99708 29 56 32 98419 01581 98622 01378 00203 99797 28 52 23 398419 01451 98753 01247 00204 99796 27 48 48 48 48 98937 01063 99145 00855 00208 99792 24 36 36 98937 01063 99145 00855 00208 99792 24 36 38 99194 00806 99406 00955 00210 99790 22 28 36 39 99322 00678 99534 00466 00212 99788 21 24 40 40 8.99460 11.00508 8.99602 11.00388 10.00213 9.99787 20 20 44 41 99577 00423 99791 00209 00214 99786 19 16 42 46 00207 99793 99791 22 28 40 46 00207 99993 00170 90004 10.09954 00215 99785 18 12 24 46 00207 99793 900068 00553 99447 00222 99788 21 24 24 24 24 24 24 24										
32	24			02040						
36	32		97229	02771	97421	02579		99808		
44	36									
44 26 97629 02371 97825 02175 00196 99804 34 16 52 28 97894 02106 98092 01908 00198 99802 32 8 56 29 98026 01974 98225 01775 00199 99801 31 4 22 30 8.98157 11.01843 8.9838 11.01642 10.00200 9.99800 30 38 4 31 98288 01712 98490 01510 00202 99708 29 56 8 32 98419 01511 98852 01378 00203 99797 28 52 12 33 98549 01451 98753 01247 00204 99706 27 48 16 34 98679 01321 9884 01116 00207 9.9973 26 44 20 35 89837 01663 99145 00855 <td></td> <td></td> <td>8.97496</td> <td></td> <td>8.97691</td> <td></td> <td></td> <td></td> <td></td> <td></td>			8.97496		8.97691					
56 28 97894 02106 98022 01908 00198 99802 32 8 56 29 98026 01974 98225 01775 00199 99801 31 4 22 30 8.98157 11.01843 8.98358 11.01642 10.00200 9.9800 30 38 4 31 98288 01712 98490 01510 00202 99708 29 56 8 32 98419 01581 98622 01378 00203 99797 28 52 16 34 98679 01321 98884 01116 00205 99795 26 44 20 35 8.98808 11.01192 8.99015 11.00207 9.99793 25 40 24 36 98937 01063 99145 00855 00208 99791 23 32 28 37 99066 00934 99274 00655	44	26					00196			
56				02238						
22 30 8,98157 11.01843 8,98358 11.01642 10.00200 9,99800 30 38 8 31 98288 01712 98490 01510 000202 99708 29 56 50 50 50 50 50 50 50				02106			00198			
4 31 98288 01712 98490 01510 00202 99798 29 56 8 32 98419 01581 98622 01378 00203 99797 28 52 16 34 98679 01321 98884 01116 00205 99795 26 44 20 35 8,98808 11.01192 8,99015 11.00985 10.00207 9,9793 25 40 24 36 98937 01063 99145 00855 00208 99791 23 32 38 99194 00806 99405 00595 00210 99790 22 28 36 39 99322 00678 99534 00466 00212 99788 21 24 40 40 8,99450 11.00338 10.00213 9,99787 20 20 44 41 99577 00423 99791 00200 00214 99786	56			01974						4
8 32 98419 01581 98622 01378 00203 99797 28 52 12 33 98549 01451 98753 01247 00204 99796 27 48 16 34 98679 01321 98884 01116 00205 99795 26 44 20 35 8,98808 11.01192 8,9915 11.0085 10,00207 9,99793 25 40 24 36 98937 01063 99145 00855 00209 99791 23 32 28 37 99066 00934 99275 00725 00209 99791 23 32 36 39 99322 00678 99634 00466 00212 99788 21 24 40 40 8,99450 11.00550 8,99662 11.00338 10.00213 9,99787 20 20 44 41 19577 00423 99791										
12										
16 34 98679 01321 98884 01116 00205 99795 26 44 20 35 8.98808 11.01192 8.99015 11.00985 10.00207 9.99793 25 40 24 36 98937 01063 99145 00855 00208 99792 24 36 28 37 99066 0034 99275 00725 00209 99791 23 32 36 39 99322 00678 99534 00466 00212 99788 21 24 40 40 8.99450 11.00550 8.99662 11.00338 10.00213 9.99787 20 20 44 41 99577 00423 99791 00209 00214 99786 19 16 48 42 99704 00296 99919 00081 00215 99785 18 12 52 43 99830 00170 9.0044										
24 36 98937 01063 99145 00855 00208 99792 24 36 28 37 99066 00934 99275 00725 00209 99791 23 32 38 99194 00806 99405 00595 00210 99790 22 28 36 39 99322 00678 99534 00460 00212 99788 21 24 40 40 8.99450 11.00550 8.99662 11.00338 10.00213 9.99787 20 20 44 41 99577 00423 99791 00209 00214 99786 19 16 48 42 99704 00296 99919 00081 00215 99785 18 12 56 44 99956 00044 00174 99826 00217 99783 17 8 23 45 9.0082 10.99918 9.00301 10.99699	16	34	98679	01321	98884	01116		99795		44
28 37 99066 00934 99275 00725 00209 99791 23 32 36 39 99322 00678 99534 00466 00212 99788 21 24 40 40 8.99450 11.00550 8.99662 11.00338 10.00213 9.99787 20 20 44 41 99577 00423 99791 00209 00214 99786 19 16 48 42 99704 00296 99919 00081 00215 99785 18 12 52 43 99830 00170 9.00046 10.99954 00217 99783 17 8 56 44 99956 00044 00174 99826 00218 99782 16 4 23 45 9.0082 10.99918 9.0301 10.9969 10.00219 9.99781 15 37 4 46 002207 99793 00427										
32 38 99194 00806 99405 00595 00210 99790 22 28 36 39 99322 00678 99534 00466 00212 99788 21 24 40 40 8.99450 11.00550 8.99662 11.00338 10.00213 9.99787 20 20 44 41 99577 00423 99791 00209 00214 99786 19 16 48 42 99704 00296 99919 00081 00215 99785 18 12 56 44 9956 00044 00174 99826 00218 99782 16 4 23 45 9.0082 10.9918 9.00301 10.99699 10.00219 9.99781 15 37 4 46 00207 99793 00427 99573 00220 99780 14 56 8 47 00332 99688 00553										
36	28									
40 40 8.99450 11.00550 8.99662 11.00338 10.00213 9.99787 20 20 44 41 99577 00423 99791 00209 00214 99786 19 16 48 42 99704 00296 99919 00081 00215 99785 18 12 56 44 99956 00044 00174 99826 00218 99782 16 4 23 45 9.0082 10.99918 9.00301 10.99699 10.00219 9.99781 15 37 4 46 00207 99793 00427 99573 00220 99780 14 56 8 47 00332 99668 00553 99447 00222 99778 13 52 12 48 00456 99544 00679 99321 00223 99776 11 44 20 50 9.00704 10.99296 9.00930 <td>36</td> <td></td> <td></td> <td></td> <td></td> <td></td> <td>00210</td> <td></td> <td></td> <td></td>	36						00210			
44 41 99577 00423 99791 00209 00214 99786 19 16 48 42 99704 00296 99919 00081 00215 99785 18 12 52 43 99830 00170 9.00046 10.99954 00217 99783 17 8 56 44 99956 00044 00174 99826 00218 99782 16 4 23 45 9.0082 10.99918 9.00301 10.99699 10.00219 9.99781 15 37 4 46 00207 99793 00427 99573 00220 99780 14 56 8 47 00332 99668 00553 99447 00222 99778 13 52 12 48 00456 99544 00679 99321 00223 99776 11 44 20 50 9.00704 10.99296 9.00930										
48 42 99704 00296 99919 00081 00215 99785 18 12 52 43 99830 00170 9.00046 10.99954 00217 99783 17 8 56 44 99956 00044 00174 99826 00218 99782 16 4 23 45 9.00082 10.99918 9.00301 10.99699 10.00219 9.99781 15 37 4 46 00207 99793 00427 99573 00220 99780 14 56 8 47 00332 99668 00553 99447 00222 99778 13 52 12 48 00456 99544 00679 99321 00223 99776 11 44 20 50 9.00704 10.99296 9.00930 10.99070 10.00225 9.99775 10 40 24 51 00828 99172 01055						00209	00214	99786		
56 44 99956 00044 00174 99826 00218 99782 16 4 23 45 9.00082 10.99918 9.00301 10.99699 10.00219 9.99781 15 37 4 46 00207 99793 00427 99573 00220 99780 14 56 8 47 00332 99668 00553 99447 00222 99778 13 52 12 48 00456 99544 00679 99321 00223 99776 11 44 20 50 9.00704 10.99296 9.00930 10.99070 10.00225 9.99775 10 40 24 51 00828 99172 01055 98945 00227 99773 9 36 28 52 00951 99049 01179 98821 00228 99772 8 32 32 53 01074 98926 01303									18	
23 45 9.00082 10.99918 9.00301 10.99699 10.00219 9.99781 15 37 8 47 00332 99668 00553 99447 00222 99778 13 52 12 48 00456 99544 00679 99321 00223 99777 12 48 16 49 00581 99419 00805 99195 00224 99776 11 44 20 50 9.00704 10.99296 9.00930 10.99070 10.00225 9.99775 10 40 24 51 00828 99172 01055 98945 00227 99773 9 36 28 52 00951 99049 01179 98821 00228 99772 8 32 32 53 01074 98926 01303 98697 00228 99771 7 28 36 54 01196 98804 01427										8
4 46 00207 99793 00427 99573 00220 99780 14 56 8 47 00332 99668 00553 99447 00222 99778 13 52 12 48 00456 99544 00679 99321 00223 99777 12 48 16 49 00581 99419 00805 99195 00224 99776 11 44 20 50 9.00704 10.99296 9.00930 10.99070 10.00225 9.99775 10 40 24 51 00828 99172 01055 98945 00227 99773 9 36 28 52 00951 99049 01179 98821 00228 99772 8 32 32 53 01074 98926 01303 98697 00228 99771 7 28 36 54 01196 98804 01427 98573 <td></td>										
8 47 00332 99668 00553 99447 00222 99778 13 52 12 48 00456 99544 00679 99321 00223 99777 12 48 16 49 00581 99419 00805 99195 00224 99776 11 44 20 50 9.00704 10.99296 9.00930 10.99070 10.00225 9.99775 10 40 24 51 00828 99172 01055 98945 00227 99773 9 36 28 52 00951 99049 01179 98821 00228 99772 8 32 32 53 01074 98926 01303 98697 00229 99771 7 28 36 54 01196 98804 01427 98573 00231 99769 6 24 40 55 9.01318 10.98682 9.01550 10.98450 10.00232 9.99768 5 20 44 56 01										
12 48 00456 99544 00679 99321 00223 99777 12 48 16 49 00581 99419 00805 99195 00224 99776 11 44 20 50 9.00704 10.99296 9.00930 10.99070 10.00225 9.99775 10 40 24 51 00828 99172 01055 98945 00227 99773 9 36 28 52 00951 99049 01179 98821 00228 99772 8 32 32 53 01074 98926 01303 98697 00229 99771 7 28 36 54 01196 98804 01427 98573 00231 99769 6 24 40 55 9.01318 10.98682 9.01550 10.98450 10.00232 9.99768 5 20 44 56 01440 98560 01673									_	
16 49 00581 99419 00805 99195 00224 99776 11 44 20 50 9.00704 10.99296 9.00930 10.99070 10.00225 9.99775 10 40 24 51 00828 99172 01055 98945 00227 99773 9 36 28 52 00951 99049 01179 98821 00228 99772 8 32 32 53 01074 98926 01303 98697 00229 99771 7 28 36 54 01196 98804 01427 98573 00231 99769 6 24 40 55 9.01318 10.98682 9.01550 10.98450 10.00232 9.99768 5 20 44 56 01440 98560 01673 98327 00233 99767 4 16 48 57 01561 98439 01796										
20 50 9.00704 10.99296 9.00930 10.99070 10.00225 9.99775 10 40 24 51 00828 99172 01055 98945 00227 99773 9 36 28 52 00951 99049 01179 98821 00228 99772 8 32 32 53 01074 98926 01303 98697 00229 99771 7 28 36 54 01196 98804 01427 98573 00231 99769 6 24 40 55 9.01318 10.98682 9.01550 10.98450 10.00232 9.99768 5 20 44 56 01440 98560 01673 98327 00233 99767 4 16 48 57 01561 98439 01796 98204 00235 99765 3 12 52 58 01682 98318 01918										
28 52 00951 99049 01179 98821 00228 99772 8 32 32 53 01074 98926 01303 98697 00229 99771 7 28 36 54 01196 98804 01427 98573 00231 99769 6 24 40 55 9.01318 10.98682 9.01550 10.98450 10.00232 9.99768 5 20 44 56 01440 98560 01673 98327 00233 99767 4 16 48 57 01561 98439 01796 98204 00235 99765 3 12 52 58 01682 98318 01918 98082 00236 99764 2 8 56 59 01803 98197 02040 97960 00237 99763 1 4 24 60 01923 98077 02162 97838										
32 53 01074 98926 01303 98697 00229 99771 7 28 36 54 01196 98804 01427 98573 00231 99769 6 24 40 55 9.01318 10.98682 9.01550 10.98450 10.00232 9.99768 5 20 44 56 01440 98560 01673 98327 00233 99767 4 16 48 57 01561 98439 01796 98204 00235 99765 3 12 52 58 01682 98318 01918 98082 00236 99764 2 8 56 59 01803 98197 02040 97960 00237 99763 1 4 24 60 01923 98077 02162 97838 00239 99761 0 36 M. S. M Cosine. Secant. Cotangent Tan										
36 54 01196 98804 01427 98573 00231 99769 6 24 40 55 9.01318 10.98682 9.01550 10.98450 10.00232 9.99768 5 20 44 56 01440 98560 01673 98327 00233 99767 4 16 48 57 01561 98439 01796 98204 00235 99765 3 12 52 58 01682 98318 01918 98082 00236 99764 2 8 56 59 01803 98197 02040 97960 00237 99763 1 4 24 60 01923 98077 02162 97838 00239 99761 0 36 M. S. M Cosine. Secant. Cotangent Tangent. Cosecant. Sine. M M. S.										
40 55 9.01318 10.98682 9.01550 10.98450 10.00232 9.99768 5 20 44 56 01440 98560 01673 98327 00233 99767 4 16 48 57 01561 98439 01796 98204 00235 99765 3 12 52 58 01682 98318 01918 98082 00236 99764 2 8 56 59 01803 98197 02040 97960 00237 99763 1 4 24 60 01923 98077 02162 97838 00239 99761 0 36 M. S. M Cosine. Secant. Cotangent Tangent. Cosecant. Sine. M M S.										
44 56 01440 98560 01673 98327 00233 99767 4 16 48 57 01561 98439 01796 98204 00235 99765 3 12 52 58 01682 98318 01918 98082 00236 99764 2 8 56 59 01803 98197 02040 97960 00237 99763 1 4 24 60 01923 98077 02162 97838 00239 99761 0 36 M. S. M Cosine. Secant. Cotangent Tangent. Cosecant. Sine. M M. S.										
48 57 01561 98439 01796 98204 00235 99765 3 12 52 58 01682 98318 01918 98082 00236 99764 2 8 56 59 01803 98197 02040 97960 00237 99763 1 4 24 60 01923 98077 02162 97838 00239 99761 0 36 M.S. M.S. Cosine. Secant. Cotangent Tangent. Cosecant. Sine. M M.S.										
52 58 01682 98318 01918 98082 00236 99764 2 8 56 59 01803 98197 02040 97960 00237 99763 1 4 24 60 01923 98077 02162 97838 00239 99761 0 36 M.S. M Cosine. Secant. Cotangent Tangent. Cosecant. Sine. M M M S.										
56 59 01803 98197 02040 97960 00237 99763 1 4 4 60 01923 98077 02162 97838 00239 99761 0 36 M.S. M Cosine. Secant. Cotangent Tangent. Cosecant. Sine. M M.S.	52	58	01682	98318	01918	98082	00236	99764	2	8
M.S. M Cosine. Secunt. Cotangent Tangent. Cosecant. Sine. M M.S.		_								
			,					_		
0-130			Cosine.	Secunt.	Cotangent	Tangent.	Cosecant.			M.S.
	0"	190							047	9,

0h	6° Logarithms. 173°									
]		Logarithms, 110								
M.S.	M	Sine.	Cosecant.	Tangent.	Cotangent.	Secant.	Cosine.	M	M.S.	
24	$\begin{array}{c} 0 \\ 1 \end{array}$	9.01923 02043	10,98077 97957	9.02162	10.97838	10.00239	9.99761	60	36	
8	$\frac{1}{2}$	$02043 \\ 02163$	97837	$02283 \\ 02404$	97717 9 7 596	$00240 \\ 00241$	99760	59 58	56 52	
12	3	02283	97717	02525	97475	00241	99757	57	48	
16	4	02402	97598	02645	97355	00244	99756	56	44	
20	5	9.02520	10.97480	9.02766	10.97234	10.00245	9.99755	55	40	
24	6	02639	97361	02885	97115	00247	99753	54	36	
28	7	02757	97243	03005	96995	00248	99752	53	32	
32 36	8 9	02874 02992	97126	03124	96876	$00249 \\ 00251$	99751	52	28 24	
40	10	9.03109	97008 10.96891	03242 9.03361	96758 1 0.96639	10.00252	99749 9.99748	51 50	24 20	
44	11	03226	96774	03479	96521	00253	99747	49	16	
48	12	03342	96658	03597	96403	00255	99745	48	12	
52	13	03458	96542	03714	96286	00256	99744	47	8	
56	14	03574	96426	03832	96168	00258	99742	46	4	
25	15	9.03690	10.96310	9.03948	10.96052	10.00259	9.99741	45	35	
8	16 17	$03805 \\ 03920$	96195 96080	$04065 \\ 04181$	95935 9 5819	00260 00262	99740 99738	44 43	56 52	
12	18	04034	95966	04297	95703	00263	99737	42	48	
16	19	04149	95851	04413	95587	00264	99736	41	44	
20	20	9.04262	10.95738	9.04528	10.95472	10.00266	9.99734	40	40	
24	21	04376	95624	04643	95357	00267	99733	39	36	
28	22	04490	95510	04758	95242	00269	99731	38	32	
32	23	04603	95397	04873	95127	00270	99730	37	28	
36	24 25	04715 9.04828	95285 10.95172	04987 9.05101	95013 10.94899	00272 10.00273	99728 9.99727	36 35	24 20	
44	26	04940	95060	05214	94786	00274	99726	34	16	
48	27	05052	94948	05328	94672	00276	99724	33	12	
52	28	05164	94836	05441	94559	00277	99723	32	8	
56	29	05275	94725	05553	94447	00279	99721	31	÷	
26	30	9.05386	10.94614	9.05666	10.94334	10.00280	9.99720	30	34	
4 8	31 32	$05497 \\ 05607$	94503 94393	05778 05890	94222 94110	00282 00283	99718 99717	29 28	56 52	
12	33	05717	94283	06002	93998	00284	99716	27	48	
16	34	05827	94173	06113	93887	00286	99714	26	44	
20	35	9.05937	10.94063	9.06224	10.93776	10.00287	9.99713	25	40	
24	36	06046	93954	06335	93665	00289	99711	24	36	
28	37	06155	93845	06445	93555	00290	99710	23	32	
32	38 39	06264 06372	93736	06556	93444	00292 00293	99708 997 07	22 21	28 24	
36 40	40	9.06481	93628	06666 9.06775	93334 10.93225	10.00295	9.99705	20	20	
44	41	06589	93411	06885	93115	00296	99704	19	16	
48	42	06696	93304	06994	93006	00298	99702	18	12	
52	43	06804	93196	07103	92897	00299	99701	17	8	
56	44	06911	93089	07211	92789	00301	97699	16	4	
27	45	9.07018	10.92982	$9.07320 \\ 07428$	10.92680 92572	10.00302 00304	9.99698 99696	15 14	33	
8	46 47	$07124 \\ 07231$	92876 92769	07536	92372	00304	99695	13	56 52	
12	48	07337	92663	07643	92357	00307	99693	12	48	
16	49	07442	92558	07751	92249	00308	99692	11	44	
20	50	9.07548	10.92452	9.07858	10.92142	10.00310	3. 99690	10	40	
24	51	07653	92347	07964	92036	00311	99689	9	36	
28	52	07758	92242	08071	91929	00313	99687 99686	8.	32	
32 36	53 54	$07863 \\ 07968$	92137 92032	$08177 \\ 08283$	91823 91717	00314 00316	99686	7 6	28 24	
40	55	9.08072	10.91928	9.08389	10.91611	10.00317	9.99683	5	20	
44	56	08176	91824	08495	91505	00319	99681	4	16	
48	57	08280	91720	08600	91400	00320	99680	3	12	
52	58	08383	91617	08705	91295	00322	99678	2	8	
56	59	08486	91514	08810	91190	00323	99677	1	4	
28	60	08589 .		08914	91086	00325	99675 Sine.	0 M	32 M.S.	
M.S. 6h	м 96°	Cosine.	Secant.	Cotangent	Tangent.	Cosecant.	Sine.	83°		
0-	190							00		

1.0			13002	aniiins	THIOONOM	1711110.				
0h	7°	Logarithms. 172°								
M.S.	M	Sine.	Cosecant.	Tangent.	Cotangent.	Secant.	Cosine.	M	M.S.	
28	0	9.08589	10.91411	9.08914	10.91086	10.00325	9.93675	60	32	
, 4	1	08692	91308	09019	90981	00326	99674	59	56	
8 12	2	08795	91205	09123	90877	00328	99672	58	52 48	
3	3 4	08897	91103	09227 09330	90773	00330	99670 99669	57 56	44	
16 20	5	08999 9.09101	91001 10.90899	9.09434	90670 10. 90566	00331 10.00333	9.99667	55	40	
24	6	09202	90798	09537	90463	00334	99666	54	36	
28	7	09304	90696	09640	90360	00336	99664	53	32	
32	8	09405	90595	09742	90258	00337	99663	52	28	
36	9	09506	90494	09845	90155	00339	99661	51	24	
40	10	9.09606	10.90394	9.09947	1 0.90053	10.00341	9,99659	50	20	
44	11	09707	90293	10049	89951	00342	99658	49	16	
48	12	09807	90193	10150	89850	00344	99656	48 47	12 8	
52 56	13 14	$09907 \\ 10006$	90093 8999 4	10252 10353	89748 89647	$00345 \\ 00347$	99655 99653	46	4	
29	15	9.10106	10.89894	9.10454	10.89546	10.00349	9.99651	45	31	
4	16	10205	89795	10555	89445	00350	99650	44	56	
8	17	10304	89696	10656	89344	00352	99648	43	52	
12	18	10402	89598	10756	89244	00353	99647	42	48	
16	19	10501	89499	10856	89144	00355	99645	41	44	
20	20	9.10599	10.89401	9.10956	10.89044	10.00357	9.99643	40	40	
24	21	10697	89303	11056	88944	00358	99642	39	36	
28 32	22	10795 10893	89205 89107	11155 11254	88845 88746	00360	99640	38 37	32 28	
36	23 24	10893	89010	11353	88647	00362 00363	99638 99637	36	$\frac{26}{24}$	
10	25	9.11087	10.88913	9.11452	10.88548	10.00365	9.99635	35	20	
44	$\frac{26}{26}$	11184	88816	11551	88449	00367	99633	34	16	
48	27	11281	88719	11649	88351	00368	99632	33	12	
52	28	11377	88623	11747	88253	00370	99630	32	8	
56	29	11474	88526	11845	88155	00371	99629	31	4	
30	30	9.11570	10.88430	9.11943	10.88057	10.00373	9.99627	30	30	
4 8	31 32	11666 11761	88334 88239	12040 12138	87960	00375	99625	29 28	56 52	
12	$\begin{vmatrix} 32 \\ 33 \end{vmatrix}$	11857	88143	12135 12235	87862 87765	00376 00378	$99624 \\ 99622$	$\frac{20}{27}$	48 48	
16	34	11952	88048	12332	87668	00380	99620	26	44	
20	35	9.12047	10.87953	9.12428	10.87572	10.00382	9.99618	25	40	
24	36	12142	87858	12525	87475	00383	99617	24	36	
28	37	12236	87764	12621	87379	00385	99615	23	32	
32	38	12331	87669	12717	87283	00387	99613	22	28	
36	39	12425	87575	12813	87187	00388	99612	21	24	
40 44	40 41	$egin{array}{c} 9.12519 \ 12612 \ \end{array}$	10.87481 87388	9.1 2969 1 3004	10.87091 86996	10.00390 00392	- 9.99610 99608	20 1 9	20 1 6	
48	42	12706	87294	13099	86901	00393	99607	18	12	
52	43	12799	87201	13194	86806	00395	99605	17	8	
56	44	12892	87108	13289	86711	00397	99603	16	4	
31	45	9.12985	10.87015	9.13384	10.86616	10.00399	9.99601	15	29	
4	46	13078	86922	13478	86522	00400	99600	14	56	
8	47	13171	86829	13573	86427	00402	99598	13	52	
12 16	48 49	13263 13355	86737 86645	13667 13761	86333 86239	$00404 \ 00405$	99596	12 11	48	
20	50	9.13447	10.86553	9.13854	10.86146	10.00407	99 5 95 9.99593	10	44 40	
24	51	13539	86461	13948	86052	00409	99591	9	36	
28	52	13630	86370	14041	85959	00411	99589	8	32	
32	53	13722	86278	14134	85866	00412	99588	7	28	
36	5±	13813	86187	14227	85773	00414	99586	6	24	
40	55	9.13904	10.86096	9.14320	10.85680	10.00416	9.99584	5	20	
44 48	56	13994	86006	14412	85588	00418	99582	4	16	
52	57 58	14085 14175	85915 85825	$14504 \\ 14597$	85496 85403	00419 00421	99581 99579	3 2	12	
56	59	14266	85734	14688	85312	00421	99577	1	8 4	
32	60	14356	85644	14780	85220	00425	99575	0	28	
M. S.	M	Cosine.		Cotangent		Cosecant.	Sine.	_	M.S.	
6h	97°							820		

Ор	8°	Constitution Logarithms. 171°								
M.S.	M	Sine.	Cosecant.	Tangent.	Cotangent.	Secant.	Cosine.	M	M. S.	
32	0	9.14356	10.85644	9.14780	10.85220	10.00425	9.99575	60	28	
4	1	14445	85555	14872	85128	00426	99574	59	56	
8	2	14535	85465	14963	85037	00428	99572	58	52	
12 16	3	14624 14714	85376	15054	84946	00430	99570	57	48	
20	4 5	9.14803	85286 10.85197	15145 9.15236	$84855 \\ 10.84764$	$\begin{bmatrix} 00432 \\ 10.00434 \end{bmatrix}$	99568 9.99566	56 55	44 40	
24	6	14891	85109	15327	84673	00435	99565	54	36	
28	7	14980	85020.	15417	84583	00437	99563	53	32	
32	8	15069	84931	15508	84492	00439	99561	52	28	
36	9	15157	84843	15598	84402	00441	99559	51	24	
40	10 11	9.15245 15333	10.84755 84667	9.15688 15777	10.84312 84223	10.00443 00444	9.99557	50 49	20 16	
48	12	15355 15421	84579	15867	84133	00446	99556 99554	48	12	
52	13	15508	84492	15956	84044	00448	99552	47	8	
56	14	15596	84404	16046	83954	00450	99550	46	4	
33	15	9.15683	10.84317	9.16135	10.83865	10.00452	9.99548	45	27	
1 4	16	15770	84230	16224	83776	00454	99546	44	56	
8 12	17	15857 15944	84143 84056	16312 16401	83688 83599	00455	99545	43	52 48	
16	18 19	16030	83970	16489	83511	$00457 \\ 00459$	99543 99541	42	44	
20	20	9.16116	10.83884	9.16577	10.83423	10.00461	9.99539	40	40	
24	21	16203	83797	16665	83335	00463	99537	39	36	
28	22	16289	83711	16753	83247	00465	99535	38	32	
32	23	16374	83626	16841	83159	.00467	99533	37	28	
36 40	24	16460 9.16545	83540 10.83455	16928 9.17016	83072 10.82984	$00468 \\ 10.00470$	99532 9. 99530	36 35	24 20	
44	25 26	16631	83369	17103	82897	00472	99528	34	16	
48	27	16716	83284	17190	82810	00474	99526	33	12	
52	28	16801	83199	17277	82723	00476	99524	32	8	
56	29	16886	83114	17363	82637	00478	99522	31	4	
34	30	9.16970	10.83030	9.17450	10.82550	10.00480	9.99520	30	26	
8	31 32	17055 17139	82945 82861	17536 17622	82464 82378	$00482 \\ 00483$	99518 99517	29 28	56 52	
12	33	17223	82777	17708	8229 2	00485	99515	27	48	
16	34	17307	82693	17794	82206	00487	99513	26	44	
20	35	9.17391	10.82609	9.17880	10.82120	10.00489	9.99511	25	40	
24	36	17474	82526	17965	82035	00491	99509	24	36	
28	37	17558	82442	18051 18136	81949	00493	99507	23 22	32 28	
32 36	38	17641 17724	82359 82276	18221	81864 81779	$00495 \\ 00497$	99505 99503	21	24	
40	40	9.17807	10.82193	9.18306	10.81694	10.00499	9.99501	20	20	
44	41	17890	82110	18391	81609	00501	99499	1 9	16	
48	42	17973	82027	18475	81525	00503	99497	18	12	
52	43	18055	81945	18560	81440	00505	99495	17	8 4	
56 35	44 45	18137 9.18220	81863 10.81780	18644 9.18728	81356 10.81272	00506 10.00508	99494 9.99492	16 15	25	
4	46	18302	81698	18812	81188	00510	99490	14	56	
8	47	18383	81617	18896	81104	00512	99488	13	52	
12	48	18465	81535	18979	81021	00514	99486	12	48	
16	49	18547	81453	19063	80937	00516	99484	11	44	
20	50	9.18628	10.81372	9.19146	10.80854	10.00518	9.99482	10	40 36	
24 28	51 52	18709 18790	81291 81210	19229 19312	80771 80688	$00520 \\ 00522$	$99480 \\ 99478$	8	32	
32	53	18871	81129	19395	80605	00524	99476	7	28	
36	54	18952	81048	19478	80522	00526	99474	6	24	
40	55	9.19033	10.80967	9.19561	10.80439	10.00528	9.99472	5	20	
44	56	19113	80887	19643	80357	00530	99470	4	16	
48	57	19193	80807	19725	80275	$00532 \\ 00534$	99468 99466	3 2	12 8	
52 56	58 59	19273 19353	80727 80647	19807 19889	80193 80111	00536	99464	1	$\begin{vmatrix} \circ \\ 4 \end{vmatrix}$	
36	60	19433	80567	19971	80029	00538	99462	0	24	
M.S.		Cosine.		Cotangent		Cosecant.	Sine.	M	M.S.	
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32 53 23462 76538 24112 75888 00649 99351 7 28 36 54 23535 76465 24186 75814 00652 99348 6 24 40 55 9.23607 10.76393 9.24261 10.75739 10.00654 9.99346 5 20 44 56 23679 76321 24335 75665 00656 99344 4 16 48 57 23752 76248 24410 75590 00658 99342 3 12 52 58 23823 76177 24484 75516 00660 99340 2 8 56 59 23895 76105 24558 75442 00663 99337 1 4 40 60 23967 76033 24632 75368 00665 99335 0 20 M. S. M Cosine. Secant. Cotaugent Tau										
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40 55 9.23607 10.76393 9.24261 10.75739 10.00654 9.99346 5 20 44 56 23679 76321 24335 75665 00656 99344 4 16 48 57 23752 76248 24410 75590 00658 99342 3 12 52 58 23823 76177 24484 75516 00660 99340 2 8 56 59 23895 76105 24558 75442 00663 99337 1 4 40 60 23967 76033 24632 75368 00665 99335 0 20 M. S. M Cosine. Secant. Cotangent Tangent. Cosecant. Sine. M M. S.		_								
44 56 23679 76321 24335 75665 00656 99344 4 16 48 57 23752 76248 24410 75590 00658 99342 3 12 52 58 23823 76177 24484 75516 00660 99340 2 8 56 59 23895 76105 24558 75442 00663 99337 1 4 40 60 23967 76033 24632 75368 00665 99335 0 20 M. S. M Cosine. Secant. Cotangent Tangent. Cosecant. Sine. M M. S.		,								
48 57 23752 76248 24410 75590 00658 99342 3 12 52 58 23823 76177 24484 75516 00660 99340 2 8 56 59 23895 76105 24558 75442 00663 99337 1 4 40 60 23967 76033 24632 75368 00665 99335 0 20 M. S. M Cosine. Secant. Cotaugent Tangent. Cosecant. Sine. M M. S.			1						_	
52 58 23823 76177 24484 75516 00660 99340 2 8 56 59 23895 76105 24558 75442 00663 99337 1 4 40 60 23967 76033 24632 75368 00665 99335 0 20 M. S. M Cosine. Secant. Cotangent Tangent. Cosecant. Sine. M M. S.										
56 59 23895 76105 24558 75442 00663 99337 1 4 4 4 4 4 4 4 4 4	4					75516				
M. S. M Cosine. Secant. Cotangent Tangent. Cosecant. Sine. M. M. S.	56	59	23895	76105	24558	75442	00663	99337	1	4
	1				_					
0, 188.			Cosine.	Secant.	Cotangent	Tangent.	Cosecant.			
	O_{Π}	199							200	On

LOGARITIMS TRIGONOMETRIC.										
0h	10°			Loga	rithms.		1	.69°	11 ^h	
M.S.	M	Sine.	Cosecant.	Tangent.	Cotangent.	Secant.	Cosine.	M	M.S.	
40	0	9.23967	10.76033	9.24632	10.75368	10.00665	9.99335	60	20	
8	$\frac{1}{2}$	$24039 \\ 24110$	75961 75890	$24706 \\ 24779$	75294 75221	00667	99333	59	56	
12	3	24110 24181	75819	24853	75147	$00669 \\ 00672$	99331 99328	58 57	52 48	
16	4	24253	75747	24926	75074	00674	99326	56	44	
20	5	9.24324	10.75676	9.25000	10.75000	10.00676	9.99324	55	40	
24	6	24395	75605	25073	74927	00678	99322	54	36	
28	7	24466	75534	25146	74854	00681	99319	53	32	
32 36	8 9	$24536 \\ 24607$	75464 75393	25219 25292	74781	00683	99317	52	28	
40	10	9.24677	10.75323	9.25365	74708 10.74635	00685 10.00687	99315 9.99 31 3	51 50	24 20	
44	111	24748	75252	25437	74563	00690	99310	49	16	
48	12	24818	75182	25510	74490	00692	99308	48	12	
52	13	24888	75112	25582	74418	00694	99306	47	8	
56	14	24958	75042	25655	74345	00696	99304	46	4	
41	15 16	9.25028	10.74972	9.25727	10.74273	10.00699	9.99301	45	19	
4 8	17	$25098 \\ 25168$	74902 74832	25799 25871	$74201 \\ 74129$	00 7 01 00703	99299 99297	44 43	56 52	
12	18	25237	74763	25943	74057	00706	99294	42	48	
16	19	25307	74693	26015	73985	00708	99292	41	44	
20	20	9.25376	10.74624	9.26086	10.73914	10.00710	9.99290	40	40	
24	21	25445	74555	26158	73842	00712	99288	39	36	
28	22	25514	74486	26229	73771	00715	99285	38	32	
32	23 24	$25583 \\ 25652$	74417 74348	$26301 \\ 26372$	73699 73628	00 717 00 71 9	99283 99281	37 36	28 24	
40	25	9.25721	10.74279	9.26443	10.73557	10.00722	9.99278	35	20	
44	26	25790	74210	26514	73486	00724	99276	34	16	
48	27	25858	74142	26585	73415	00726	99274	33	12	
52	28	25927	74073	26655	73345	00729	99271	32	8	
56	29	25995	74005	26726	73274	00731	99269	31	4	
42	30	9.26063 26131	10.73937 73869	9.2679 7 2686 7	10.73203 73133	10.00733 00736	9.99267 99264	30 29	18 56	
8	32	26199	73801	26937	73063	00738	99262	28	52	
12	33	26267	73733	27008	72992	00740	99260	27	48	
16	34	26335	73665	27078	72922	00743	99257	26	44	
20	35	9.26403	10.73597	9.27148	10.72852	10.00745	9.99255	25	40	
24	36	26470	73530	27218	72782	00748	99252	24	36	
28 32	37	$26538 \\ 26605$	73462 73395	27288 27357	$72712 \\ 72643$	00750 0 0752	99250 99248	23 22	32 28	
36	39	26672	73328	27427	72573	00755	99245	21	$\frac{26}{24}$	
40	40	9.26739	10.73261	9.27496	10.72504	10.00757	9.99243	20	20	
44	41	26806	73194	27566	72434	00759	99241	19	16	
48	42	26873	73127	27635	72365	00762	99238	18	12	
52	43	26940 27007	73060	27704	72296 72227	00764 00 7 67	99236 99233	17 16	8	
56 43	44 45	9.27073	72993 10.72927	27773 9.27842	10.72158	10.00769	9.99233	15	4 17	
4	46	27140	72860	27911	72089	00771	99229	14	56	
8	47	27206	72794	27980	72020	00774	99226	13	52	
12	48	27273	72727	28049	71951	00776	99224	12	48	
16	49	27339	72661	28117	71883	00779	99221	11	44	
20	50	9.27405	10.72595 72529	$9.28186 \\ 28254$	$\frac{10.71814}{71746}$	10.00781 00783	9. 99 219 99217	10	40 26	
24 28	51 52	27471 27537	72529 72463	28323 28323	71677	00786	99214	9 8	36 3 2	
32	53	27602	72398	28391	71609	00788	99212	7	28	
36	54	27663	72332	28459	71541	00791	99209	6	24	
40	55	9.27734	10.72266	9.28527	• 10.71473	10.00793	9.99207	5	20	
44	56	27799	72201	28595	71405	00796	99204	4	16	
48	57	27861	72136	28662	71338 71270	00798 00800	99202	3	1 2	
52 56	58 59	$27930 \\ 27995$	$72070 \\ 72005$	$28730 \\ 28798$	71202	00803	99200 99197	$\frac{2}{1}$	8 4	
44	60	28060	71940	28865	71135	00805	99195	0	16	
M.S.	M	Cosine.		Cotangent		Cosecant.	Sine.	M	M.S.	
6h	1009)						79°		

The state of the s										
	$0^{\rm h}$	11°			Loga	rithms.		1	.68°	11 ^h
,	M.S.	M	Sine.	Cosecant.	Tangent.	Cotangent.	Secant.	Cosine.	M	M.S.
	44	0	9.28060	10.71940	9.28865	10.71135	10.00805	9.99195	60	16
	4	1	28125	71875	28933	71067	00808	99192	59	56
ł	8	2	28190	71810	29000	71000	00810	99190	58 57	52 48
П	12 16	3 4	$28254 \\ 28319$	71746 71681	29067 29134	70933 70866	$00813 \\ 00815$	99187 99185	56	44
Ш	20	5	9.28384	10.71616	9.29201	10.70799	10.00818	9.99182	55	40
Į.	24	6	28448	71552	29268	70732	00820	99180	54	36
1	28	7	28512	71488	29335	70665	00823	99177	53	32
Н	32	8	28577	71423	29402	70598	00825	99175	52	28
н	36	9	28641	71359	29468	70532	00828	99172	51	24
Ш	40	10	9.28705	10.71295	9.29535	10.70465	10.00830	9.99170	50	20
	44	11	28769	71231	29601	70399	00833	99167	49	16
H	48	12	28833	71167	29668	70332	00835	99165	48 47	12 8
P	52 56	13 14	28596 28960	71104 71040	29734 29800	70266 70200	00838 00840	99162 99160	46	4
	45	15	9.29024	10.70976	9.29866	10.70134	10.00843	9.99157	45	15
10	4	16	29087	70913	29932	70068	00845	99155	44	56
J.	8	17	29150	70850	29998	70002	81800	99152	43	52
	12	18	29214	70786	30064	69936	00850	99150	42	48
N	16	19	29277	70723	30130	69876	00853	99147	41	44
T	20	20	9.29340	10.70660	9.30195	10.69805	10.00855	9.99145	40	40
1	·24 28	21	29403	70597	30261 30326	69739	00858	991 4 2 99140	39 38	$\begin{array}{c} 36 \\ 32 \end{array}$
П	32	22 23	29466 29529	70534 70471	30326	6967 4 69609	00860 00 8 63	99140	37	28
1	36	24	29591	70409	30457	69543	00865	99135	36	24
1	40	25	9.29654	10.70346	9.30522	10.69478	10.00868	9,99132	35	20
1	44	26	29716	70284	30587	69413	00870	99130	34	16
1	48	27	29779	70221	30652	69348	00873	99127	33	12
	52	28	29841	70159	30717	69283	00876	99124	32	8
1	56	29	29303	70097	30782	69218	00878	99122	31	4
1	46	$\begin{vmatrix} 30 \\ 31 \end{vmatrix}$	9.29966 30028	10.70034 69972	$9.30846 \\ 30911$	10.69154 69089	10.00881 00883	9.991 1 9 99117	30 29	14 56
	8	32	30020	69910	30975	69025	00886	99114	28	52
1	12	33	30151	69849	31040	68960	00888	99112	27	48
	16	34	30213	69787	31104	68896	00891	99109	26	44
	20	35	9.30275	10.69725	9.31168	10.68832	10.00894	9.99106	25	40
	24	36	30336	69664	31233	68767	00896	99104	24	36
1	28	37	30398	69602	31297	68703	00899	99101	23	32
1	32 36	38 39	$30459 \\ 30521$	69541 69479	$31361 \\ 31425$	68639	$00901 \\ 00904$	99099 99096	22 21	28 24
1	40	40	9.30582	10.69418	9.31489	68575 10.68511	10.00904	9,99093	20	20
1	44	41	30643	69357	31552	68448	00909	99091	19	16
	48	42	30704	69296	31616	68384	00912	99088	18	12
	52	43	30765	69235	31679	68321	00914	99086	17	8
1	56	44	30826	69174	31743	68257	00917	99083	16	4
	47	45	9.30887	10.69113	9.31806	10.68194	10.00920	9.99080	15	13
	8	$\begin{array}{c c} 46 \\ 47 \end{array}$	30947 31008	69053	31870	68130 68067	00922	99078	14	56
	12	48	31008	68992 - 68932	31933 31996	68067 68004	00925 009 2 8	99075 99072	13 12	52 48
	16	49	31129	68871	$\frac{31990}{32059}$	67941	00930	99070	11	44
	20	50	9.31189	10.68811	9.32122	10.67878	10.00933	9.99067	10	40
	24	51	31250	68750	32185	67815	0 0936	99064	9	36
	28	52	31310	68690	32248	67752	00938	99062	8	32
	32	53	31370	68630	32311	67689	00941	99059	7	28
	36	54	31430	68570	32373	67627	00944	99056	6	24
	40 44	55 56	9.31490 31549	$\begin{array}{c} 10.68510 \\ 68451 \end{array}$	9.32436 32498	$\begin{array}{c} 10.67564 \\ 67502 \end{array}$	10.00946 00949	9,99054	5	20
	48	57	31609	68391	32498 32561	67439	00949	99051 99048	4 3	16 12
	52	58	31669	68331	32623	67377	00954	99046	2	8
	56	59	31728	68272	32685	67315	00957	99043	ĩ	4
	48	60	31788	68212	32747	67253	00960	99040	Ū	12
1	M.S.	M	Cosine.	Secant.	Cotangent	Tangent.	Cosecant.	Sine.		м. S.
	6 ^h	1019							78°	5h
do.										

M.S. M Sine. Cosccant. Tangent. Cotangent. Secant. Cosine. M.S. 48 0 9.31788 10.68212 9.32747 10.67253 10.00960 9.99040 6 4 1 31847 68153 32810 67190 00962 99038 5 8 2 31907 68093 32872 67128 00965 99035 5 12 3 31966 68034 32933 67067 00968 99032 5 16 4 32025 67975 32995 67005 00970 99030 5 20 5 9.32084 10.67916 9.33057 10.66943 10.00973 9.99027 5 24 6 32143 67857 33119 66881 00976 99024 5 28 7 32202 67798 33180 66892 00978 99022 5 36 9	11h
48 0 9.31788 10.68212 9.32747 10.67253 10.00960 9.99040 6 4 1 31847 68153 32810 67190 00962 99038 5 8 2 31907 68093 32872 67128 00965 99035 5 12 3 31966 68034 32933 67067 00968 99032 5 16 4 32025 67975 32995 67005 00970 99030 5 20 5 9.32084 10.67916 9.33057 10.66943 10.00973 9.99027 5 24 6 32143 67857 33119 66820 00976 99024 5 32 7 32202 67798 33180 66820 00978 99022 5 32 8 32261 67739 33242 66758 00981 99019 5 36 9 32319 <t< td=""><td>M.S.</td></t<>	M.S.
8 2 31907 68093 32872 67128 00965 99035 5 16 4 32025 67975 32995 67005 00970 99030 5 20 5 9.32084 10.67916 9.33057 10.66943 10.00973 9.99027 5 24 6 32143 67857 33119 66881 00976 99024 5 28 7 32202 67798 33180 66820 00978 99022 5 36 9 32319 67681 33303 66697 00984 99016 5 40 10 9.32378 10.67622 9.33365 10.66635 10.00987 9.99013 5 44 11 32437 67563 33487 66513 00992 99008 4 48 12 32495 67505 33487 66513 00992 99005 4 56 14 32612	12
12 3 31966 68034 32933 67067 00968 99032 5 16 4 32025 67975 32995 67005 00970 99030 5 20 5 9.32084 10.67916 9.33057 10.66943 10.00973 9.99027 5 24 6 32143 67857 33119 66881 00976 99024 5 28 7 32202 67798 33180 66820 00978 99022 5 32 8 32261 67739 33242 66758 00981 99019 5 36 9 32319 67681 33303 66697 00984 99016 5 40 10 9.32378 10.67622 9.33365 10.66635 10.00987 9.99013 5 44 11 32437 67563 33487 66513 00992 99008 4 52 13 32553	56
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	52
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	48
24 6 32143 67857 33119 66881 00976 99024 5 28 7 32202 67798 33180 66820 00978 99022 5 32 8 32261 67739 33242 66758 00981 99019 5 36 9 32319 67681 33303 66697 00984 99016 5 40 10 9.32378 10.67622 9.33365 10.66635 10.00987 9.99013 5 44 11 32437 67563 33426 66574 00989 99011 4 48 12 32495 67505 33487 66513 00992 99008 4 52 13 32553 67447 33548 66452 00995 99005 4 49 15 9.32670 10.67330 9.33670 10.66330 10.01000 9.99000 4 4 16 32728	40
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	36
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	32
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	28
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	24
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	20 16
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	12
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	8
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	4
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	11
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	56 52
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	48
20 20 9.32960 10.67040 9.33974 10.66026 10.01014 9.98986 4 24 21 33018 66982 34034 65966 01017 98983 3 28 22 33075 66925 34095 65905 01020 98980 3 32 23 33133 66867 34155 65845 01022 98978 3	44
24 21 33018 66982 34034 65966 01017 98983 3 28 22 33075 66925 34095 65905 01020 98980 3 32 23 33133 66867 34155 65845 01022 98978 3	40
32 23 33133 66867 34155 65845 01022 98978 3	36
	32
36 24 33190 66810 34215 65785 01025 98975 3	28 24
36 24 33190 66810 34215 65785 01025 98975 3 40 25 9.33248 10.66752 9.34276 10.65724 10.01028 9.98972 3	20
44 26 33305 66695 34336 65664 01031 98969 3	16
48 27 33362 66638 34396 65604 01033 98967 3	12
52 28 33420 66580 34456 65544 01036 98964 3	8
56 29 33477 66523 34516 65484 01039 98961 3	10
50 30 9.33534 10.66466 9.34576 10.65424 10.01042 9.98958 3 4 31 33591 66409 34635 65365 01045 98955 2	56
4 31 33591 66409 34635 65365 01045 98955 2 8 32 33647 66353 34695 65305 01047 98953 2	52
12 33 33704 66296 34755 65245 01050 98950 2	48
16 34 33761 66239 34814 65186 01053 98947 2	44
20 35 9.33818 10.66182 9.34874 10.65126 10.01056 9.98944 2	40
24 36 33874 66126 34933 65067 01059 98941 2 28 37 33931 66069 34992 65008 01062 98938 2	36 32
28 37 33931 66069 34992 65008 01062 98938 2 32 38 33987 66013 35051 64949 01064 98936 2	28
36 39 34043 65957 35111 64889 01067 98933 2	24
40 40 9.34100 10.65900 9.35170 10.64830 10.01070 9.98930 2	20
44 41 34156 65844 35229 64771 01073 98927 1	16
48 42 34212 65788 35288 64712 01076 98924 1 52 43 34268 65732 35347 64653 01079 98921 1	12 8
52 43 34268 65732 35347 64653 01079 98921 1 56 44 34324 65676 35405 64595 01081 98919 1	4
51 45 9.34380 10.65620 9.35464 10.64536 10.01084 9.98916 1	9
4 46 34436 65564 35523 64477 01087 98913 1	56
8 47 34491 65509 35581 64419 01090 98910 1	52
12 48 34547 65453 35640 64360 01093 98907 1	48
16 49 34602 65398 35698 64302 01096 ,98904 1 20 50 9.34658 10.65342 9.35757 10.64243 10.01099 9.98901 1	44 40
$ egin{array}{ c c c c c c c c c c c c c c c c c c c$	36
28 52 34769 65231 35873 64127 01104 98896	32
32 53 34824 65176 35931 64069 01107 98893	28
36 54 34879 65121 35989 64011 01110 98890	24
40 55 9.34934 10.65066 9.36047 10.63953 10.01113 9.98887 44 56 34989 65011 36105 63895 01116 98884	20 16
44 56 34989 65011 36105 63895 01116 98884 48 57 35044 64956 36163 63837 01119 98881	12
48 57 35044 64936 36163 63679 61113 6661 52 58 35099 64901 36221 63779 01122 98878	8
56 59 35154 64846 36279 63721 01125 98875	4
52 60 35209 64791 36336 63664 01128 98872	8
M.S. M Cosine. Secant. Cotangent Tangent. Cosecant. Sine.	M. S. 5a
6h 102° 77	6 300

Ţ				.,		INIGUNOS				1
	0h	13°)		Loga	rithms.			166°	111
-	M.S.	M	Sine.	Cosecant.	Tangent.	Cotangent.	Secant.	Cosine.	M	M.S.
	52	0	9.35209	10.64791	9.36336	10.63604	10.01128	9.98872	60	8
1	4	1	35263	64737	36394	63606	01131	98869	59	56
	8	2	35318	64682	36452	63548	01133	98867	58	52 48
	12 16	3 4	35373 35427	64627 64573	36509 36566	63491 63434	01136 01 1 39	98864 9 8 861	57 56	44
	20	5	9.35481	10.64519	9.36624	10.63376	10.01142	9.98858	55	40
1	24	6	35536	64464	36681	63319	01145	98855	54	36
	28	7	35590	64410	36738	63262	01148	98852	53	32
	32	8	35644	64356	36795	63205	01151	98849	52	28
4	36	9	35698	64302	36852	63148	01154	98846	51	24
1	40 44	10	9.35752 35806	10.64248 64194	9.36909 36966	10.63091 63034	10.01157 01160	9.988 4 3 988 4 0	50 49	20 16
J	48	11 12	35860	64140	37023	62977	01163	98837	48	12
1	52	13	35914	64086	37080	62920	01166	98834	47	8
-	56	14	35968	64032	37137	62863	01169	98831	46	4
- }	53	15	9.36022	10.63978	9.37193	10.62807	10.01172	9.98828	45	7
Ì	4	16	36075	63925	37250	62750	01175	98825	44	56
	8	17	36129	63871	37306	62694	01178	98822	43	52
1	12	18	36182	63818	37363	62637	01181	98819	42	48
	16 20	19	36236 9.36289	63764 10.63711	37419 9.37476	$\begin{array}{c} 62581 \\ 10.62524 \end{array}$	01184 10.01187	98816 9.98813	41 40	44 40
	24	20 21	36342	63658	37532	62468	01190	98810	39	36
ł	28	22	36395	63605	37588	62412	01193	98807	38	32
	32	23	36449	63551	37644	62356	01196	98804	37	28
	36	24	36502	63498	37700	62300	01199	98801	36	24
-	4()	25	9.36555	10.63445	9.37756	10.62244	10.01202	9.98798	35	20
	44	26	36608	63392	37812	62188	01205	.98795	34	16
1	48	27	36669	63340	37868	62132	01208	98792	33	12
-	52 56	28 29	36713 36766	63287 63234	3 7924 3 7 980	$\begin{array}{c} 62076 \\ 62020 \end{array}$	012 11 01214	98789	32	8 4
	54	30	9.36819	10.63181	9.38035	10.61965	10.01217	98 7 86 9.98783	31 30	6
1	4	31	36871	63129	38091	61909	01220	98780	29	56
1	8	32	36924	63076	38147	61853	01223	98777	28	52
1	12	33	36976	63024	38202	61798	01226	98774	27	48
	16	34	37028	62972	38257	61743	01229	98771	26	44
-	20	35	9.37081	10.62919	9.38313	10.61687	10.01232	9.98768	25	40
- [24 28	36 37	37133 37185	$\begin{bmatrix} & 62867 \\ & 62815 \end{bmatrix}$	38368 38423	$61632 \\ 61577$	$01235 \\ 01238$	$98765 \\ 98762$	24 23	36 32
1	32	38	37237	62763	38479	61521	01230	98759	22	28
1	36	39	37289	62711	38534	61466	01244	98756	21	24
- }	40	40	9.37341	10.62659	9.38589	10.61411	10.01247	9.98753	20	20
-1	44	41	37393	62607	38644	61356	01250	98750	19	16
	48	42	37445	62555	38699	61301	01254	98746	18	12
1	52	43	37497	62503	38754	61246	01257	98743	17	8
	56 55	44 45	375 4 9 9.37600	62451 10.62400	38808 9.38863	61192 10.61137	$\begin{array}{c c} 01260 \\ 10.01263 \end{array}$	98740 9.98737	16 15	4 5
-{	4	46	37652	62348	38918	61082	01266	98734	14	56
	8	47	37703	62297	38972	61028	01269	98731	13	52
1	12	48	37755	62245	39027	60973	01272	98728	12	48
П	16	49	37806	62194	39082	60918	01275	98725	11	44
	20	50	9.37858	10.62142	9.39136	10.60864	10.01278	9.98722	10	40
	24	51	37909	62091	39190	60810	01281	98719	9	36
	28 32	52 53	37960 38011	62040 61989	39245 39299	60755 60701	01285 01288	$98715 \\ 98712$	8 7	32 28
	36	54	38062	61938	39353	60647	01291	98709	6	28
-	40	55	9.38113	10 61887	9.39407	10.60593	10.01294	9.98706	5	20
	44	56	38164	61836	39461	60539	01297	98703	4	16
	48	57	38215	61785	39515	60485	01300	98700	3	12
1	52	58	38266	61734	39569	60431	01303	98697	2	8
	56 56	59	38317	61683	39623	60377	01306	98694	1	4
1	ЭО М. S.	60 M	38368 Cosine.	61632 Secant.	39677 Cotangent	60323 (01310 Cosecant.	98690	0	4
	м. S. (jh	103		Secant.	Commission	rangent.	Cosecant.	Sine.	76°	M. S. 5h
L	0	100							101	0

1			220112		Z I I I O I O I I	1371610.			17		
Oh	Logarienms. 100 II										
M.S.	M	Sine.	Cosecant.	Tangent.	Cotangent.	Secant.	Cosine.	1 M	M.S.		
56	0	9.38368	10.61632	9.39677	10.60323	10.01310	9,98690	60	4		
4	1	38418	61582	39731	60269	01313	98687	59	56		
8	2	38469	61531	39785	60215	01316	98684	58	52		
12	3	38519	61481	39838	60162	01319	98681	57	48		
16	4	38570	61430	39892	69108	01322	98678	56	44		
20	5	9.38620	10.61380	9.39945	10.60055	10.01325	9.98675	55	40		
24 28	7	$38670 \\ 38721$	61330	39999	60001	01329	98671	54	36		
32	8	38771	61279 61229	40052 40106	59948	01332	98668	53	32		
36	9	38821	61179	40106	59894. 59841	01335 01338	98665	52	28 24		
40	10	9.38871	10.61129	9.40212	10.59788	10.01341	98662 9.98659	51 50	20		
44	11	38921	61079	40266	59734	01344	98656	49	16		
48	12	38971	61029	40319	59681	01348	98652	48	12		
52	13	39021	60979	40372	59628	01351	98649	47	8		
56	14	39071	60929	40425	59575	01354	98646	46	4		
5.7	15	9.39121	10.60879	9.40478	10.59522	10.01357	9.98643	45	3		
4	16	39170	60830	40531	59469	01360	98640	44	56		
8	17	39220	60780	40584	59416	01364	98636	43	52		
12	18	39270	60730	40636	59364	01367	98633	42	48		
16	19	39319	60681	40689	59311	01370	98630	41	44		
20 24	20 21	9.39369 39418	10.60631	9.40742	10.59258	10.01373	9.98627	40	40		
28	22	39467	60582	40795 40847	59205 59153	$01377 \\ 01380$	98623 98620	39	36 32		
32	23	39517	60483	40900	59100	01383	98620	37	28		
36	24	39566	60434	40952	59048	01386	98614	36	24		
40	25	9.39615	10.60385	9.41005	10.58995	10.01390	9.98610	35	20		
44	26	39664	60336	41057	58943	01393	98607	34	16		
48	27	39713	60287	41109	58891	01396	98604	33	12		
52	28	39762	60238	41161	58839	01399	98601	32	8		
56	29	39811	60189	41214	58786	01403	98597	31	4		
58	30	9.39860	10.60140	9.41266	10.58734	10.01406	9.98594	30	2		
4	31	39909	60091	41318	58682	01409	.98591	29	56		
8	32	39958	60042	41370	58630	01412	98588	28	52		
12 16	33 34	40006	5999 4 599 4 5	41422	58578	01416	98584	27 26	48		
20	35	40055 9.40103	10.59897	41474 9.41526	58526 10.58474	01419 10.01422	98581 9.98578	25	4± 40		
24	36	40152	59848	41578	58422	01426	98574	24	36		
28	37	40200	59800	41629	58371	01429	98571	$\frac{23}{23}$	32		
32	38	40249	59751	41681	58319	01432	98568	22	28		
36	39	40297	59703	41733	58267	01435	98565	21	24		
40	40	9,40346	10.59654	9.41784	10.58216	10.01439	9.98561	20	20		
44	41	40394	59606	41836	58164	01442	98558	19	16		
48	42	40442	59558	41887	58113	01445	98555	18	12		
52	43	40490	59510	41939	58061	01449	98551	17	8		
56 59	44	40538	59462 10.59414	41990 9.42041	58010 10.57959	01452 10,01455	98548	16 15	4		
4	$\begin{array}{ c c }\hline 45\\ 46 \end{array}$	9.40586 40634	59366	42093	57907	01459	9.98545 98541	14	56		
8	47	40682	59318	42144	57856	01455	98538	13	52		
12	48	40730	59270	42195	57805	01465	98535	12	48		
16	49	40778	59222	42246	57754	01469	98531	11	£4 ±±		
20	50	9.40825	10.59175	9.42297	10.57703	10.01472	9.98528	10	10		
24	51	40873	59127	42348	57652	01475	98525	9	36		
28	52	40921 .	59079	42399	57601	01479	98521	8	32		
32	53	40968	59032	42450	57550	01482	98518	7	28		
36	54	41016	58984	42501	57499	01485	98515	6	24		
40	55	9.41063	10.58937	9.42552	10.57448	10.01489	9,98511	5	20		
44	56	41111	58889	42603	57397	01492	98508	4	16		
48	57	41158	58842	42653	57347	01495	98505	$\frac{3}{2}$	12		
52 56	58 59	$41205 \\ 41252$	58795 58748	$42704 \\ 42755$	57296 57245	01499 01502	98501 98498	$\frac{2}{1}$	8 4		
60	60	41300	58700	42105	57195	01502	98494	0	0		
M.S.	M	Casine		Cotangent		Cosecant.	Sine.		M. S.		
6p	104) Cosine.	Decare.	оошивени	zuagene.	Concount of		750			
	IUI							101	0		

1 ^h	15°		•	Loga	rithms.		1	.64°	10 ^h
M.S.	М	Sine.	Cosecant.	Tangent.	Cotangent.	Secant.	Cosine.	M	M.S.
0	0	9,41300	10.58700	9.42805	10.57195	10.01506	9.98494	60	60
4	1	41347	58653	42856	57144	01509	98491	59	56
8	2	41394	58606	42906	57094	01512	98488	58	52
12	3	41441	58559	42957	57043	01516	98484	57	48
16	4	41488	58512	43007	56993	01519	98481	56	44
20	5 6	9.41535 41582	10.58465 58418	9.43057 43108	10.56943 56892	10.01523 01526	9.98477 98474	55 54	40 36
24 28	7	41628	58372	43158	56842	01520	98471	53	32
32	8	41675	58325	43208	56792	01533	98467	52	28
36	9	41722	58278	43258	56742	01536	98464	51	24
40	10	9.41768	10.58232	9.43308	10.56692	10.01540	9.98460	50	20
44	11	41815	58185	43358	56642	01543	98457	49	16
48	12	41861	58139	43408	56592	01547	98453	48	12
52	13	41908	58092	43458	56542	01550	98450	47	8 4
56	14	41954	58046	43508	56492	01553 10.01557	98447	46 45	59
1 4	15 16	9.42001 42047	10.57999 57953	9.43558 43607	10.56442 56393	01560	9.98443 98440	44	56
8	17	42093	57907	43657	56343	01564	98436	43	52
12	18	42140	57860	43707	56293	01567	98433	42	48
16	19	42186	57814	43756	56244	01571	98429	41	44
20	20	9.42232	10.57768	9.43806	10.56194	10.01574	9.98426	40	40
24	21	42278	57722	43855	56145	01578	98422	39	36
28	22	42324	57676	43905	56095	01581	98419	38	32
32	23	42370	57630	43954	56046	01585	98415	37	28
36 40	24	42416 9.42461	57584 10.57539	44004 9.44053	5599 6 10.55947	01588 10.01591	98 41 2 9.98 4 09	36 35	24 20
44	25 26	42507	57493	44102	55898	01595	98405	34	16
48	27	42553	57447	44151	55849	01598	98402	33	12
52	28	42599	57401	44201	55799	01602	98398	32	8
56	29	42644	57356	44250	55750	01605	98395	31	4
2	30	9.42690	10.57310	9.44299	10.55701	10.01609	9.98391	30	58
4	31	42735	57265	44348	55652	01612	98388	29	56
8	32	42781	57219	44397	55603.	01616	98384	28	52
16	33 34	$42826 \\ 42872$	57174 57128	44446 44495	5555 4 55505	$01619 \\ 01623$	98381 98377	27 26	48
20	35	9.42917	10.57083	9.44544	10.55456	10.01627	9.98373	25	40
24	36	42962	57038	44592	55408	01630	98370	24	36
28	37	43008	56992	44641	55359	01634	98366	23	32
32	38	43053	56947	44690	55310	01637	98363	22	28
36	39	43098	56902	44738	55262	01641	98359	21	24
40	40	9.43143	10.56857	9.44787	10.55213	10.01644	9.98356	20	20
44 48	41 42	43188 43233	56812 56767	44836 44884	5516 4 55116	01648 01651	98352	19 18	16 12
52	43	43278	56722	44933	55067	01655	98349 98345	17	8
56	44	43323	56677	44981	55019	01658	98342	16	4
3	45	9.43367	10.56633	9.45029	10.54971	10.01662	9.98338	15	57
4	46	43412	56588	45078	54922	01666	98334	14	56
8	47	43457	56543	45126	54874	01669	98331	13	52
12	48	43502	56498	45174	54826	01673	98327	12	48
16 20	49 50	43546 9.43591	56454 10.56409	45222 9.45271	54778 10.54729	01676 10.01680	98324	11 10	44 40
24	51	43635	56365	45319	54681	01683	9.98320 98317	9	36
28	52	43680	56320	45367	54633	01687	. 98313	8	32
32	53	43724	56276	45415	54585	01691	98309	7	28
36	54	43769	56231	45463	54537	01694	98306	6	24
40	55	9.43813	10.56187	9.45511	10.54489	10.01698	9.98302	5	20
44 48	56 57	43857	56143	45559	54441	01701	98299	4	16
52	58	43901 43946	56099 5605 4	45606 45654	54394 54346	01705 01709	$98295 \\ 98291$	$\frac{3}{2}$	12 8
56	59	43990	56010	45702	54298	01709	98288	1	4
4	60	44034	55966	45750	54250	01716	98284	0	56
M.S.	M	Cosine.		Cotangent		Cosecant.	Sine.	M	M.S.
7 ^h	105							74°	4h

			2001	RITHE	IRIGONOMI	211010.			11
1 ^b	16°			Loga	rithms.			163°	10 ^h
M.S.	M	Sine.	Cosecant.	Tangent.	Cotangent.	Secant.	Cosine.	[M	M.S.
4	0	9.44034	10.55966	9.45750	10.54250	10.01716	9.98284	60	56
4	1	44078	55922	45797	5 42 03	01719	98281	59	56
8	2	44122	55878	45845	54155	01723	98277	58	52
12	3	44166	55834	45892	54108	01727	98273	57	48
16	4	44210	55790	45940	54060	01730	98270	56	44
20	5	9.44253	10.55747	9.45987	10.54013	10.01734	9.98266	55	40
24	6	44297	55703	46035	53965	01738	98262	54	36
28	7	44341	55659	46082	53918	01741	98259	53	32
32	8	44385	55615	46130	53870	01745	98255	52	28 24
36	9	44428 9.44472	55572 10.55528	$46177 \\ 9.46224$	53823 10.53776	01749 10.01752	98251	51	20
40	10 11	44516	55484	46271	53729	01756	9.98248 98244	50 49	16
48	12	44559	55441	46319	53681	01760	98240	48	12
52	13	44602	55398	46366	53634	01763	98237	47	8
56	14	44646	55354	46413	53587	01767	98233	46	4
5	15	9.44689	10.55311	9.46460	10.53540	10.01771	9.98229	45	55
4	16	44733	55267	46507	53493	01774	98226	44	56
8	17	44776	55224	46554	53446	01778	98222	43	52
12	18	44819	55181	46601	53399	01782	98218	42	48
16	19	44862	55138	46648	53352	01785	98215	41	44
20	20	9.44905	10.55095	9.46694	10.53306	10.01789	9.98211	40	40
24	21	44948	55052	46741	53259	01793	98207	39	36 32
28	22	44992	55008	46788 46835	53212	01796 01800	98204 98200	38	28
32 36	23	45035 45077	54965 54923	46881	53165 53119	01804	98196	36	24
40	24 25	9.45120	10.54880	9.46928	10.53072	10.01808	9.98192	35	20
44	26	45163	54837	46975	53025	01811	98189	34	16
48	27	45206	54794	47021	52979	01815	98185	33	12
52	28	45249	54751	47068	52931	01819	98181	32	8
56	29	45292	54708	47114	52886	01823	98177	31	4
6	30	9.45334	10.54666	9.47160	10.52840	10.01826	9.98174	30	54
4	31	45377	54623	47207	52793	01830	98170	29	56
8	32	45419	54581	47253	52747	01834	98166	28	52
12	33	45462	54538	47299	52701	01838	98162	27	48 44
16	34	45504	54496 10.54453	47346 9.47392	52654 10.52608	01841 10.01845	98159 9.98155	26 25	40
20 24	35 36	9.45547 45589	54411	47438	52562	01849	9.55155	24	36
28	37	45632	54368	47484	52516	01853	98147	23	32
32	38	45674	54526	47530	52470	01856	98144	22	28
36	39	45716	54284	47576	52424	01860	98140	21	24
40	40	9.45758	10.54242	9.47622	10.52378	10.01864	9.98136	20	20
44	41	45801	54199	47668	52332	01868	98132	19	16
48	42	45843	54157	47714	52286	01871	98129	18	12
52	43	45885	54115	47760	52240	01875	98125	17	8 4
56	44	45927	54073 10.54031	47806 9.47852	52194 10.52148	01879 10.01883	98121 9.98117	16 15	53
7	45	9.45969 46011	53989	47897	52103	01887	9.98117	14	56
8	46 47	46053	53947	47943	52057	01890	98110	13.	52
12	48	46095	53905	47989	52011	01894	98106	12	48
16	49	46136	53864	48035	51965	01898	98102	11	44
20	50	9.46178	10.53822	9.48080	10.51920	10.01902	9,98098	10	40
24	51	46220	53780	48126	51874	01906	98094	9	36
28	52	46262	53738	48171	51829	01910	98090	8	32
32	53	46303	53697	48217	51783	01913	98087	7	28
36	54	46345	53655	48262	51738	01917	98083	6 5	24 20
40	55	9.46386	10 53614	9.48307 48353	10.51693 51647	$\begin{array}{c} 10.01921 \\ 01925 \end{array}$	9.98079 98075	4	16
44	56	46428	53572 53531	48398	51602	01929	98071	3	12
48 52	57 58	46469 46511	53489	48443	51557	01983	98067	$\frac{3}{2}$	8
56	59	46552	53448	48489	51511	01937	98063	ī	4
8	60	46594	53406	48534	51466	01940	98060	0	52
M.S.		Cosine.		Cotangent		Cosecant.	Sinc.	M	M.S.
	106							73°	4h
	1200								

1 ^b	17°			Loga	rithms.			162°	10h		
	7.6	Cina	1 Cassant			Connt		(M	M.S.		
M.S. 8	M	Sine. 9.46594	Cosecant. 10.53406	Tangent. 9.48534	Cotangent. 10.51466	Secant. 10.01940	Cosine. 9.98060	60	52		
4	$egin{bmatrix} 0 \ 1 \end{bmatrix}$	46635	53365	48579	51421	01944	98056	59	56		
8	2	46676	53324	48624	51376	01948	98052	58	52		
12	3	46717	53283	48669	51331	01952	98048	57	48		
16	4	46758	53242	48714	51286	01956	98044	56	44		
20	5	9.46800	10.53200	9.48759	10.51241	10.01960	9.98040	55	40		
24	6	46841	53159	48804	51196	01964	98036	54	36		
28	7	46882	53118	48849	51151	01968	98032	53	32		
32	8	46923	53077	48894	51106	01971	98029	52	28		
36	9	46964	53036	48939	51061	01975	98025	51	24 20		
40	10	9.47005 47045	10.52995 52955	9.48984 49029	10.51016 50971	10.01979 01983	9.98021 98017	50 49	16		
44 48	11 12	47086	52914	49073	50927	01987	98013	48	12		
52	13	47127	52873	49118	50882	01991	98009	47	8		
56	14	47168	52832	49163	50837	01995	98005	46	4		
9	15	9.47209	10.52791	9.49207	10.50793	10.01999	9.98001	45	51		
4	16	47249	52751	49252	50748	02003	97997	44	56		
8	17	47290	52710	49296	50704	02007	97993	43	52		
12	18	47330	52670	49341	50659	02011	97989	42	48		
16	19	47371	52629	49385	50615	02014	97986	41	44		
20	20	9.47411	10.52589	9.49430	10.50570	10.02018	9.97982	40 39	40 36		
24 28	21	47452 47492	52548 52508	49474 49519	50526 50481	$02022 \\ 02026$	97978 97974	38	$\frac{30}{32}$		
32	22 23	47533	52467	49563	50437	02030	97970	37	28		
36	24	47573	52427	49607	50393	02034	97966	36	24		
40	25	9.47613	10.52387	9.49652	10.50348	10,02038	9.97962	35	20		
44	26	47654	52346	49696	50304	02042	97958	34	16		
48	27	47694	52306	49740	50260	02046	97954	33	12		
52	28	47731	52266	49784	50216	02050	97950	32	8		
56	29	47774	52226	49828	50172	02054	97946	31	4		
10	30	9.47814 47854	10.52186 52146	9.49872 49916	10.50128 50084	10.02058 02062	9.97942	30 29	50 56		
4 8	31 32	47894	52106	49960	50040	02066	979 3 8 979 3 4	28	52		
12	33	47934	52066	50004	49996	02070	97930	27	48		
16	34	47974	52026	50048	49952	02074	97926	26	44		
20	35	9.48014	10.51986	9.50092	10.49908	10.02078	9.97922	25	40		
24	36	48054	51946	50136	49864	02082	97918	24	36		
28	37	48094	51906	50180	49820	02086	97914	23	32		
32	38	48133	51867	50223	49777	02090	97910	22	28		
36	39	48173	51827 10.51787	50267	$\begin{array}{c c} 49733 \\ 10.49689 \end{array}$	02094	97906	21	24 20		
40	40	9.48213 48252	51748	9.50311 50355	49645	02102	9.97902 97898	20 19	16		
48	42	48292	51708	50398	49602	02102	97894	18	12		
52	43	48332	51668	50442	49558	02110	97890	17	8		
56	44	48371	51629	50485	49515	02114	97886	16	4		
11	45	9.48411	10.51589	9,50529	10.49471	10.02118	9.97882	15	49		
4	46	48450	51550	50572	49428	02122	97878	14	56		
8	47	48490	51510	50616	49384	02126	97874	13	52		
12	48	48529	51471	50659 50703	$\begin{array}{c} 49341 \\ 49297 \end{array}$	02130	97870	12	48		
16 20	49 50	48568 9.48607	51432 1 0.51393	9.50746	10.49254	02134 10.02139	97866 9.97861	$\begin{bmatrix} 11 \\ 10 \end{bmatrix}$	44 40		
24	51	48647	51353	50789	49211	02143	9.97857	9	36		
28	52	48686	51314	50833	49167	02147	97853	8	32		
32	53	48725	51275	50876	49124	02151	97849	7	28		
36	54	48764	51236	50919	49081	02155	97845	6	24		
40	55	9.48803	10.51197	9.50962	10.49038	10.02159	9.97841	5	20		
44	56	48842	51158	51005	48995	02163	97837	4	16		
48	57	48881	51119	51048	48952	02167	97833	3	12		
52 56	58 59	$48920 \\ 48959$	51080 51041	51092 51135	48908 488 6 5	02171	97829	2	8		
12	60	48998	51041	51178	48822	$02175 \\ 02179$	$97825 \\ 97821$	$\frac{1}{0}$	4 48		
M. S.	M	Cosine.		Cotangent		Cosecant.	Sine.		M. S.		
7h	107	0		2000			Dide.	720	4h		
]	4		

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1	h	18°			Logar	rithms.		1	61°	10 th
M.	8.	M	Sine.	Cosedant.	Tongent.	Cotangent.	Secant.	Cosine,	l M	M.S.
1	2	0	9.48998	10.51002	9,51178	10.48822	10,02179	9,97821	60	48
	4	1	49037	50963	51221	48779	02183	97817	59	56
	8	2	49076	50024	51264	48736	02188	97812	58	52
	2	3	49115	50885	51306	48694	02192	97808	57	48
	18	4	49153	50847	51349	48651	02196	97804	56	144
	20	5	0.49192	10.50808	9.51392	10.48608	10.02200	9,97800	55	40
	3-1	6	49231	50769	51435	48565	02204	97796	54	36
	38	7	49269	50731	51478	48523	02208	97792	53	32
	32	8 9	49308 49347	50692	51520	48480	$02212 \\ 02216$	97788	52	28
	10	10	9,49385	50653 10.50615	51568 9.51606	48437 10.48394	10.02221	97784 9.97779	51 50	24 20
	1.1		49424	50576	51648	48352	02225	97775	49	16
	18	12	49462	50533	51691	48309	02229	97771	48	12
	12	18	49500	50500	51734	48266	02233	97767	47	8
	565	1.1	49539	50461	51776	48224	02237	97763	46	4
	13	15	9.49577	10.50423	9.51819	10.48181	10.02241	9.97759	45	47
	.1	16	49615	50385	51861	48139	02246	97754	44	56
	8	17	49654	50346	51903	48097	02250	97750	43	52
	12	18	49692	50308	51946	48054	02254	97746	42	48
	16	19	49730	50270	51988	48012	02258	97742	41	44
	20	20	9.49768	10.50232	9,52031	10.47969	10.02262	9.97738	40	40
	28	21	49806 49844	50194 50156	52073 52115	47927 47885	02266 02271	$97734 \\ 97729$	39 38	36 32
	30	23	49882	50118	52157	47843	02275	97725	37	28
	36	21	49920	50080	52200	47800	02279	97721	36	24
	10	25	9,49958	10.50042	9.52242	10.17758	10.02283	9.97717	35	20
	1.1	26	49996	50004	52284	47716	02287	97713	34	16
	18	27	50034	49966	52326	47674	02292	97708	33	12
	52	28	50072	49928	52368	47632	02296	97704	32	8
	16	29	50110	49890	52410	47590	02300	97700	31	4
	4	30	9.50148	10.49852	9.52452	10.47548	10.02304	9.97696	30	46
400	4	31	50185	49815	52494	47506	02309	97691	29	56
1	8	32	50223	49777	52536	47464	02313	97687	28	52
	12 16	33	50261 50298	49739 49702	52578 52630	47422 47380	0 2 317 02321	97683 97679	27 26	48 44
	20	35	9.50336	10.49664	9.52661	10,47339	10.02326	9.97674	25	40
	3.1	36	50374	49626	52703	47297	02330	97670	24	36
	28	37	50111	49589	52745	47255	02334	97666	$\frac{23}{23}$	32
	32	38	50449	49551	52787	47213	02338	97662	22	28
	36	39	50486	49514	52829	47171	02343	97657	21	24
	10	40	9,50523	10.49477	9.52870	10,47130	110.02347	9.97653	20	20
	1-1	41	50561	49139	52912	47088	02351	97649	19	16
	18	-12	50598	49402	52953	47047	02355	97645	18	12
	52	43	50635	49365	52995	47005	02360	97640	17 16	8
	56 .5	44 45	50673 9.50710	49327 10,49290	53037 9,53078	$\frac{46963}{10.46922}$	02364 10. 02368	$\begin{array}{c} 97636 \\ 9.97632 \end{array}$	15	4 45
1	4	46	50747	49253	53120	46880	02372	97628	14	56
	8	47	50784	49216	53161	. 46839	02377	97623	13	52
1	12	48	50821	49179	53202	46798	02381	97619	12	48
	6	49	50858	49142	53244	46756	02385	97615	11	44
1	2()	50	9:50896	10.49104	9.53285	10.46715	10.02390	9.97610	10	40
	34	51	50933	49067	53327	46673	02394	97606	9	36
	28	52	50970	49030	53368	46632	02398	97602	8	32
	32	53	51007	48993	53409	46591	02403	97597	7	28
	36	54	51043	48957	53450	46550	02407	97593	6	24
	10	55	9.51080	10.48920	9.53492	10.46508	$\begin{array}{c} 10.02411 \\ 02416 \end{array}$	$9.97589 \\ 97584$	5	$\frac{20}{16}$
	14 18	56 57	51117	48883 4884ช	53533 53574	$rac{46167}{46126}$	02410	97580	3	12
	10	58 58	51191	48809	53615	46385	02420	97576	2	8
) (i	59	51227	48773	53656	46344	02429	97571	$\frac{1}{1}$	4
	6	60	51264	48736	53697	46303	02433	97567	0	44
_	. S.	M	Cosine.		Cotangent		Cosecant.	Sine.	M	M. S
	h	108)						710	4h
L	-									

104	100ARITIMS IRIGONOMETRIC.											
1 ^h	19°			Loga	rithms.		1	60°	10h			
M.S.	M	Sine.	Cosecant.	Tangent.	Cotangent.	Secant.	Cosine.	M	M.S.			
16	0	9.51264	10.48736	9.53697	10.46303	10.02433	9.97567	60	44			
4	1	51301	48699	53738	46262	02437	97563	59	56			
8	2	51338	48662	53779	46221	02442	97558	58	52			
12	3	51374	48626	53820	46180	02446	97554	57	48			
16	4	51411	48589	53861	46139	02450	97550	56	44			
20	5	9.51447	10.48553	9.53902	10.46098	10.02455	9.97545	55	40			
24	6	51484	48516	53943	46057	02459	97541	54	36			
28	7	51520	48480	53984	46016	02464	97536	53	32			
32	8 9	51557	48443	54025	45975	$02468 \\ 02472$	97532	52 51	28 24			
36 40		51593 9.51629	48407 10.48371	54065 9.54106	45935 10.45894	10.02477	97528 9.97523	50	20			
44	10 11	51666	48334	54147	45853	02481	9.97519	49	16			
48	12	51702	48298	54187	45813	02485	97515	48	12			
52	13	51738	48262	54228	45772	02490	97510	47	8			
56	14	51774	48226	54269	45731	02494	97506	46	4			
17	15	9.51811	10.48189	9.54309	10.45691	10.02499	9.97501	45	43			
4	16	51847	48153	54350	45650	02503	97497	44	56			
8	17	51883	48117	54390	45610	. 02508	97492	43	52			
12	18	51919	48081	54431	45569	02512	97488	42	48			
16	19	51955	48045	54471	45529	02516	97484	41	44			
20	20	9.51991	10.48009	9.54512	10.45488	10.02521	9.97479	40	40			
24	21	52027	47973	54552	45448	02525	97475	39	36			
28	22	52063	47937	54593	45407	02530	97470	38	32			
32 36	23	52099	47901	54633	$egin{array}{cccc} 45367 & \ 45327 & \ \end{array}$	02534	97466	37 36	28 24			
40	24 25	52135 9.52171	47865 10.4 7829	54673 9.54714	10.45286	$\begin{array}{c c} 02539 \\ 10.02543 \end{array}$	97461 9.97457	35	20			
44	26	52207	47793	54754	45246	02547	97453	34	16			
48	27	52242	47758	54794	45206	02552	97448	33	12			
52	28	52278	47722	54835	45165	02556	97444	32	8			
56	29	52314	47686	54875	45125	02561	97439	31	4			
18	30	9.52350	10.47650	9.54915	10.45085	10.02565	9.97435	30	42			
4	31	52385	47615	54955	45045	02570	97430	29	56			
8	32	52421	47579	54995	45005	02574	97426	28	52			
12	33	52456	47544	55035	44965	02579	97421	27	48			
16	34	52492	47508	55075	44925	02583	97417	26	44			
20	35	9.52527	10.47473	9.55115	10.44885	10.02588	9.97412	25	40			
24 28	36	52563	47437	55155 55195	44845	02592	97408	24 23	36			
32	37 38	52598 52634	47402 47366	55235	$44\$05 \\ 44765$	$02597 \\ 02601$	97403	22	32 28			
36	39	52669	47331	55275	44725	02606	$97399 \\ 97394$	21	24			
40	40	9.52705	10.47295	9.55315	10.44685	10.02610	9.97390	20	20			
44	41	52740	47260	55355	44645	02615	97385	19	16			
48	42	52775	47225	55395	44605	02619	97381	18	12			
52	43	52811	47189	55434	44566	02624	97376	17	8			
56	44	52846	47154	55474	44526	02628	97372	16	4			
19	45	9.52881	10.47119	9.55514	10.44486	10.02633	9.97367	15	41			
4	46	52916	47084	55554	44446	02637	97363	14	56			
8	47	52951	47049	55593	44407	02642	97358	13	52			
12	48	52986	47014	55633	44367	02647	97353	12	48			
16 20	49	53021	46979	55673	44327	02651	97349	11	44			
24	50 51	9.53056 53092	10.46944 46908	9.55712 55752	10.44288 44248	$\begin{array}{c c} 10.02656 & \\ 02660 & \end{array}$	9.97344 97340	$\begin{vmatrix} 10 \\ 9 \end{vmatrix}$	40 36			
28	52	53126	46874	55791	44209	02665	97335	8	32			
32	53	53161	46839	55831	44169	02669	97331	7	28			
36	54	53196	46804	55870	44130	02674	97326	6	24			
40	55	9,53231	10.46769	9.55910	10.44090	10.02678	9.97322	5	20			
44	56	53266	46734	55949	44051	02683	97317	4	16			
48	57	5330 1	46699	55989	44011	02688	97312	3	12			
52	58	53 336	46664	56028	43972	02692	97308	2	8			
06	59	53370	46630	56067	43933	02697	97303	1.	4			
20	60	53405	46595	56107	43893	02701	97299	0	40			
M.S.	M	Cosine.	Secant.	Cotangent	Tangent.	Cosecant.	Sine.	M	M.S.			
7 ^h	109							70°	4 ^h			

No.	_				20011		THOONORE	TATO.			100
20	_	1 ^b	20°)		Loga	rithms.]	159°	10h
4 1 53440 44560 56185 43815 02711 97280 58 52 12 3 53509 446191 66224 43776 02715 97280 58 52 12 3 53509 44616 66224 43776 02716 97280 56 48 24 6 53613 46387 56342 43688 02729 97271 54 36 32 8 53682 46318 56420 43580 02738 97262 52 28 32 8 53682 46318 56420 43580 02738 97262 52 22 40 10 9,55751 10.46234 56459 43541 02743 97245 50 20 44 11 55755 40215 56657 43463 02757 97245 48 12 58819 46181 56676 43324 02757 97245 48 12 58819 </td <td>-1</td> <td>_</td> <td>M</td> <td></td> <td></td> <td>Tangent.</td> <td></td> <td>Secant.</td> <td>Cosine.</td> <td>(M</td> <td>M.S.</td>	-1	_	M			Tangent.		Secant.	Cosine.	(M	M.S.
S	1 5	_								60	
12										1	
16	1										
24											
28 7 53647 46357 56381 43619 02734 97266 53 32 8 53682 46318 66420 43580 02734 97266 53 40 10 9.53751 10.40249 9.56498 10.3502 10.02743 97257 51 24 41 11 55755 40215 56337 *43463 02752 97243 49 16 56 14 53819 46181 56676 43124 02757 97243 49 16 56 14 53884 46146 566654 43346 02766 97234 47 8 21 15 9,53992 10.46078 9.56693 10.43907 10.02771 9,97224 45 8 41 16 59,53991 46009 56771 43229 02776 97224 45 36 41 15 9,54933 10.45907 9,56893 10.43907 <											
28 7 53647 46353 56381 43619 02734 97266 53 32 32 8 53682 46318 56420 43580 02738 97262 52 28 36 9 53716 46249 9.56428 10.43560 02738 97262 52 28 36 9 53716 46249 9.56498 10.43560 210.02748 9.57257 51 24 40 10 9.53751 10.46249 9.56498 10.43560 210.02748 9.57252 50 20 41 11 53785 46215 56537 * 43463 02752 97243 48 12 53819 46181 56676 43424 02757 97243 48 12 53819 46181 56676 43424 02757 97243 48 12 54 15 9.59322 10.46078 9.56693 10.43307 10.02771 9.57229 45 36 14 53888 46112 56654 43346 02766 97234 46 4 16 53957 46043 56732 43268 02776 97224 44 56 8 17 53991 46090 56771 43229 02750 97220 43 52 2 18 54 025 4 54 54 5 5 6 5 6 10 4 5 8 8 17 5 6 9 5 6 8 10 4 5 8 1 1 5 6 6 6 1 5 6 8 1 4 5 6 6 1 5 6 8 1 4 5 6 6 1 5 6 8 1 4 5 6 6 1 5 6 8 1 4 5 6 6 1 5 6 8 1 4 5 6 6 1 5 6											
36 9 53716 46284 56459 43541 02743 97257 51 24 40 10 9.53751 10.46249 9.56488 10.43562 10.02743 9.7257 51 24 40 11 55785 46215 56537 4.4363 02752 97243 49 10 2581 46181 56676 43424 02757 97243 48 12 52 13 53854 46146 56615 43385 02762 97238 47 8 21 15 9.53922 10.46078 9.56684 43346 02766 97234 46 4 21 15 59.5392 10.46078 9.56684 43346 02766 97234 46 4 21 15 9.53922 10.46078 9.56693 10.43307 10.02771 9.97229 45 39 4 16 53957 46043 56732 43268 02776 97224 44 56 19 54059 45941 56849 43511 02769 97216 42 48 12 18 54025 45975 56810 43190 02785 97215 42 48 12 12 18 54025 45975 56810 43190 02785 97215 42 48 12 12 18 54025 45975 56810 43190 02785 97216 42 48 12 12 12 12 12 12 12 12 12 12 12 12 12											
36											
44						56459					
48 12 53819 46181 56676 43424 02757 97243 48 12 50 14 53888 46112 56654 43346 02765 97234 46 4 21 15 9,33922 10,46078 9,56693 10,43307 10,02771 9,97229 45 34 8 17 53991 46009 56771 43229 02780 97212 43 56 16 19 54059 45975 56810 43190 02785 97215 42 48 16 19 54053 10,4597 56887 10,4311 10,0279 97201 41 44 42 22 54161 48839 56966 43035 02804 97196 38 22 54161 48839 56966 43035 02804 97196 38 22 542616 48839 56966 43035 02808 97192 37 28 36 22 <td>ш</td> <td>40</td> <td>10</td> <td></td> <td></td> <td>9.56498</td> <td></td> <td></td> <td></td> <td></td> <td></td>	ш	40	10			9.56498					
52 13 53854 46146 56615 43356 02762 97238 47 4 21 15 9.53922 10.46078 9.56693 10,43307 10,02771 9.7229 45 39 4 16 53957 46043 56732 43268 02776 97224 44 56 8 17 53991 46009 56771 43229 02780 97220 43 52 12 18 54025 45975 56810 43190 02786 97215 42 43 20 20 9.54093 10.45907 9.56887 10.43113 10.02794 9.97206 40 40 28 22 54161 45839 56966 43035 02804 97196 38 32 32 23 54195 45805 57004 42966 02808 97182 35 20 44 26 54227 45703 57120											
56 14 53888 46112 56664 43346 02766 97234 46 4 21 15 9.53922 10.46078 9.56693 10.43307 10.02771 9.97229 45 39 8 17 53991 46009 56771 43229 02780 97210 43 66 4 66 19 46059 45975 56810 43190 02785 97210 41 44 44 20 20 9.54083 10.45907 9.56887 10.4313 10.02794 9.7206 40 44 44 44 44 44 44 44 44 44 44 44 44 44 44 44 44 46 45 45 40 25 9.54263 10.45737 5.5081 10.42919 10.02818 9.97182 35 22 36 24 54229 45771 57042 42958 02813 9.7183 36 24					46181						
1											
4 16 53957 46043 56732 43268 02776 97224 44 66 12 18 54025 45975 56810 43190 02785 97215 42 48 16 19 54059 10.45907 5.68810 43151 02790 97210 41 44 20 20 9.54093 10.45907 9.56887 10.43113 10.02794 9.7206 40 40 24 21 54161 46839 56965 43074 02799 97201 39 36 32 23 54195 45805 57004 42996 02808 97192 37 28 36 24 54229 45711 57042 42988 02831 97182 36 24 40 25 9.54933 10.45673 57120 42880 02822 97178 34 16 42 25 9.54296 145035 57137											
S	Ш						10.45507				
12 18 54025 45975 56810 43190 02785 97215 42 48 48 48 48 48 48 48	ш										
16	Ш										
24											
28 21 54161 45839 56966 43035 02804 97196 38 32 32 23 54195 45805 57004 42996 02808 97192 37 28 36 24 54229 45771 57081 10.42919 10.02838 9.97182 35 20 44 26 54297 45703 57120 42880 02822 97178 34 16 48 27 54331 45669 57158 42842 02827 97173 33 12 52 28 54865 45635 57197 42803 02832 97163 32 8 56 29 54399 45601 57235 42765 02837 97163 31 4 222 30 9.54433 10.45567 9.57274 10.42726 10.02841 9.97159 30 8 8 32 54500 45534 57312 <t< td=""><td>10</td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td></t<>	10										
32	п	24				56926	43074				
36	ш										
40	ш							02808	97192		
44 26 54297 45703 57120 42880 02822 97178 34 16 52 28 54365 45635 57197 42803 02832 97168 32 8 56 29 54399 45601 57235 42765 02837 97163 31 4 222 30 9.54433 10.45567 9.57274 10.42726 10.02841 9.97159 30 38 4 31 54466 45534 57312 42688 02846 97154 29 56 8 32 54500 45500 57351 42649 02851 97149 28 52 12 33 54567 45433 57428 42572 02860 971445 27 48 16 34 54567 45433 57428 42572 02860 97135 25 40 24 36 54635 45365 57504 42496											
48 27 54331 45669 57158 42842 02827 97173 33 12 52 28 54365 45635 57197 42803 02832 97168 32 8 56 29 54399 45601 57235 42765 02837 97163 31 4 22 30 9.54433 10.45567 9.57274 10.42726 10.02841 9.97159 30 38 4 31 54666 45534 57312 42688 02846 97149 29 56 8 32 54500 45500 57351 42649 02851 97149 28 52 144 26 97140 26 44 16 34 54567 45433 57428 42672 02860 97140 26 44 20 35 9.54601 10.45399 9.57466 10.42534 10.02865 9.97135 25 40 24496 02870 97135 <td>16</td> <td></td>	16										
52 28 54365 45635 57197 42803 02832 97168 32 8 56 29 54399 45601 57255 42765 02837 97163 31 4 31 54466 45534 57312 42688 02846 97154 29 56 8 32 54500 45500 57351 42649 02851 97145 27 48 16 34 54567 45433 57428 42572 02860 97140 26 44 20 35 9.54601 10.45399 9.57466 10.42534 10.02865 9.97135 25 40 28 37 54668 45332 57543 42419 02879 97121 22 28 36 39 54735 45265 57619 42381 02884 97111 20 2 36 39 54769 10.45231 9.57658 10.4219 <	ш										
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			_		44567	58418					
$ 7^{h} 110^{\circ}$					Secant.	Cotangent	Tangent.	Cosecant.			
		7h	110	0						69°	4 ⁿ

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	1 ^h	21°			Loga	rithms.			158°	10h
	M.S.	М	Sine.	Cosecant.	Tangent.	Cotangent.	Secant.	Cosine.	, M	M.S.
	24	0	9.55433	10.44567	9.58418	10.41582	10.02985	9.97015	60	36
	4	1	55466	44534	58455	41545	02990	97010	59	56
-	8	2	55499	44501	58493	41507	02995	97005	58	52
1	12	3	55532	44468	58531	41469	02999	97001	57	48
П	16	4	55564	44436	58569	41431	03004	96996	56	44
1	20	5	9.55597	10.41403	9.58606	10.41394	10.03009	9.96991	55	40
ı	24	6	55630	44370 44337	58644	41356	03014 03019	96986	54	36 32
Ш	28 32	.7	55663 55695	44305	58681 58719	41319 41281	03019	96981 96976	53 52	28
ı	36	8	55728	44272	58757	41243	03024	96971	51	24
П	40	10	9.55761	10.44239	9.58794	10.41206	10.03034	9.96966	50	20
П	44	11	55793	44207	58832	41168	03038	96962	49	16
П	48	12	55826	44174	58869	41131	03043	96957	48	12
ı	52	13	55858	44142	58907	41093	03048	96952	47	8
	56	14	55891	44109	58944	41056	03053	96947	46	4
ı	25	15	9.55923	10.44077	9.58981	10.41019	10.03058	9.96942	45	35
	4	16	55956	44044	59019	40981	03063	96937	44	56
	8	17	55988	44012	59056	40944	03068	96932	43	52
1	12	18	56021	43979	59094	40906	03073	96927	42	48
ı	16	19	56053	43947	59131	40869	03078	96922	41	44
П	20	20	9.56085 56118	$\begin{array}{r} 10.43915 \\ 43882 \end{array}$	9.59168 59205	10.40832 40795	10.03083	9.96917	40	40 36
1	24 28	21 22	56150	43850	59243	40757	03088 03093	$96912 \\ 96907$	39 38	32
1	32	23	56182	43818	59280	40720	03097	96903	37	28
1	36	24	56215	43785	59317	40683	03102	96898	36	24
1	40	25	9.56247	10.43753	9.59354	10.40646	10.03107	9.96893	35	20
П	44	26	56279	43721	59391	40609	03112	96888	34	16
ı	48	27	56311	43689	59429	40571	03117	96883	33	12
	52	28	56343	43657	59466	40534	03122	96878	32	8
ı	56	29	. 56375	43625	59503	40497	03127	96873	31	4
	26	30	9.56408	10.43592	9.59540	10.40460	10.03132	9.96868	30	34
ı	4	31	56440	43560	59577	40423	03137	96863	29	56
П	8 12	32 33	56472 56504	43528 43496	59 614 59651	40386 40349	$03142 \\ 03147$	96858	28	52 48
ı	16	34	56536	43464	59688	40312	03152	$96853 \\ 96848$	27 26	44
ı	20	35	9.56568	10,43432	9.59725	10.40275	10.03157	9.96843	25	40
1	24	36	56599	43401	59762	40238	03162	98838	$\frac{20}{24}$	36
П	28	37	56631	43369	59799	40201	03167	96833	23	32
ı	32	38	56663	43337	59835	40165	03172	96828	22	28
	36	39	56695	43305	59872	40128	03177	96823	21	24
ı	4()	40	9.56727	20.20-10	9,59909	10.40091	10.03182	9.96818	20	20
	44	41	56759	43241	59946	40054	03187	96813	19	16
	48	42	56790	43210	59983	40017	03192	96808	18	12
1	52	43	56822	43178	60019	39981	03197	• 96803	17	8
1	56 27	44	56854 9.56886	43146 10.43114	60056 9.60093	39944 10.39907	03202	96798	16	$\begin{vmatrix} 4 \\ 33 \end{vmatrix}$
1	4	45 46	56917	43083	60130	39870	$\begin{array}{c c} 10.03207 \\ 03212 \end{array}$	9.96793 96788	15 14	56
1	8	47	56949	45051	60166	39834	03217	96783	13	52
	12	48	56980	43020	60203	39797	03222	96778	12	48
1	16	$\overline{49}$	57012	42988	60240	39760	03228	96772	11	44
ı	20	50	9.57044	10.42956	9.60276	10.39724	10.03233	9.96767	10	40
ı	24	51	57075	42925	60313	39687	03238	96762	9	36
	28	52	57107	42893	60349	39651	03243	96757	8	32
	32	:53	57138	42862	60386	39614	03248	96752	7	28
1	36	54	57169	42831	60422	39578	03253	96747	6	24
	40	.55	9.57201	10.42799	9.60459	10.39541	10.03258	9.96742	5	20
	44 48	56	57232	42768 42736	60495	39505 39468	03263	96737	4	16
1	52	57 58	57264 57295	42705	60532 60568	39408	03268 03273	96732	$\frac{3}{2}$	12 8
	56	59	57326	42674	60605	39395	03278	$96727 \\ 96722$	$\frac{2}{1}$	4
	28	60	57358	42642	60641	39359	03283	96717	0	32
	M.S.		Cosine.		Cotangent		Cosecant.	Sine.	_	M. S.
1	7h	111				J ,	1		68°	4h
1									1	

τ				22001	TRITHMS	IRIGONOM	ETHIC.			180
	1.6	200								1
	1 ^h	22°			Logar	cithms.		1	57°	10h
į	M.S.	M	Sine.	Cosecant.	Tangent.	Cotangent.	Secant.	Cosine.	1 M	M.S.
	28	0	9.57358	10.42642	9.60641	10.39359	10.03283	9.96717	60	32
	4	1	57389	42611	60677	39323	03289	96711	59	56
	8	2	57420	42580	60714	39286	03294	96706	58	52
ı	12	3	57451	42549	60750	39250	03299	96701	57	48
	16 20	4 5	57482 9.57514	42518	60786	39214	03304	96696	56	44
ı	24	6	57545	10.42486 42455	9.60823 60859	10.39177 39141	10.03309 03314	9.96691	55	40
Ŋ	28	7	57576	42424	60895	39105	03319	96686 96681	54 53	36 32
Ц	32	8	57607	42393	60931	39069	03324	96676	52	28
	36	9	57638	42362	60967	39033	03330	96670	51	24
	40	10	9.57669	10.42331	9.61004	10.38996	10.03335	9.96665	50	20
	44	11	57700	42300	61040	38960	03340	96660	49	16
	48 52	12	57731 57762	42269 42238	61076	38924	03345	96655	48	12
	56	13 14	57793	42238	61112 61148	38888 38852	03350 03355	96650	47	8 4
	29	15	9.57824	10.42176	9.61184	10.38816	10.03360	96645 9.96640	46 45	31
	4	16	57855	42145	61220	38780	03366	96634	44	56
	8	17	57885	42115	61256	38744	03371	96629	43	52
	12	18	57916	42084	61292	38708	03376	96624	42	48
	16	19	57947	42053	61328	38672	08381	96619	41	44
	20	20	9.57978	10.42022	9.61364	10.38636	10.03386	9.96614	40	40
	24 28	21 22	58008 58039	41992 41961	61400 61436	38600 38 5 64	03392 03397	96608	39 38	36 32
	32	23	58070	41930	61472	38528	03402	96603 96598	37	28
	36	24	58101	41899	61508	38492	09407	96593	36	24
	40	25	9.58131	10.41869	9.61544	10.38456	10.03412	9.96588	35	20
	44	26	58162	41838	61579	38421	03418	96582	34	16
	48	27	58192	41808	61615	38385	03423	96577	33	12
	52 56	28 29	58223 58253	41777 41747	61651 61687	38349 383 1 3	$03428 \\ 03433$	96572 96567	32 31	8 4
	30	30	9.58284	10.41716	9.61722	10.38278	10.03438	9.96562	30	30
	4	31	58314	41686	61758	38242	03444	96556	29	56
	8	32	58345	41655	61794	38206	03449	96551	28	52
	12	33	58375	41625	61830	38170	03454	96546	27	48
	16	34	58406	41594	61865	38135	03459	96541	26	44
	$\frac{20}{24}$	35 36	9.58436 58467	10.41564 41533	9.6190 1 61936	10.38099 38064	10.03465 03470	9.96535 96530	25 24	40 36
	28	37	58497	41503	61972	38028	03475	96525	23	32
	32	38	58527	41473	62008	37992	03480	96520	22	28
	36	39	58557	41443	62043	37957	03486	96514	21	24
	40	40	9.58588	10.41412	9.62079	10.37921	10.03491	9,96509	20	20
	44 48	· 41 42	58618 58648	41382 41352	62114 62150	37886 37850	$03496 \\ 03502$	96504	19 18	16 12
	52	43	58678	41322	62185	37815	03507	96498 96493	17	8
	56	44	58709	41291	62221	37779	03512	96488	16	4
	31	45	9.58739	10.41261	9.62256	10.37744	10.03517	9.96483	15	29
	4	46	58769	41231	62292	37708	03523	96477	14	56
	8	47	58799	41201	62327	37673	03528	96472	13	52
ı	12 16	48	58829 58859	41171 41141	$\begin{array}{c} 62362 \\ 62398 \end{array}$	37638 37602	03533 03539	$96467 \\ 96461$	12 11	48 44
ı	20	50	9.58889	10.41111	9.62433	10.37567	10.03544	9.96456	10	40
	24	51	58919	41081	62468	37532	03549	96451	9	36
	28	52	58949	41051	62504	37496	03555	96445	8	32
	32	53	58979	41021	62539	37461	03560	96440	7	28
	36	54	59009	40991	62574	37426	03565	96435	6	24
	40 44	55 56	9,59039 59069	10.40961 40931	$9.62609 \\ 62645$	10.37391 37355	10.03571 03576	9.96429 96424	5 4	20 16
	48	57	59098	40902	62680	37320	03581	96419	3	12
1	52	58	59128	40872	62715	37285	03587	96413	2	8
	56	59	59158	40842	62750	37250	03592	96408	1	4
	32	60	59188	40812	62785	37215	03597	96403	0	28
	M.S. 7 ^L	м 112	Cosine.	Secant.	Cotangent	Tangent.	Cosecant.	Sine.		M.S.
	1-1	112							67°	4h
							,			-

100	DOUALITIMS INCONOMERICS.										
1h	23°			Loga	rithms.		1	.56°	10h		
M.S.	M	Sine.	Cosecant.	Tangent.	Cotangent.	Secant.	Cosine.	M	M.S.		
32	0	9.59188	10.40812	9.62785	10.37215	10.03597	9.96403	60	28		
4	1	59218	40782	62820	37180	03603	96397	59	56		
. 8	2	59247	40753	62855	37145	03608	96392	58	52		
12	3	59277	40723	62890	37110	03613	96387	57	48		
16	4	59307	40693	62926	37074	03619	96381	56	44		
20 24	5 6	9.59336 59366	10.40664	9.62961 62996	10.37039 37004	10.03624	9.96376	55 54	40 36		
28	7	59396	40634 40604	63031	36969	03630 03635	96370 96365	53	32		
32	8	59425	40575	63066	36934	03640	96360	52	28		
36	9	59455	40545	63101	36899	03646	96354	51	24		
40	10	9.59484	10.40516	9.63135	10.36865	10.03651	9.96349	50	20		
44	11	59514	40486	63170	36830	03657	96343	49	16		
48	12	59543	40457	63205	36795	03662	96338	48	12		
52	13	59573	40427	63240	36760	03667	96333	47	8		
56	14	59602	40398	63275	36725	03673	96327	46	4		
33	15	9.59632	10.40368	9.63310	10.36690	10.03678	9.96322	45	27		
4	16	59661	40339	63345	36655	03684	96316	44	55		
8 12	17	59690 59720	40310	63379 63414	36621	03689 03695	96311 96305	43 42	52 48		
16	18 19	59749	40280 40251	63449	36586 36551	03700	96300	41	44		
20	20	9.59778	10.40222	9.63484	10.36516	10.03706	9.96294	40	40		
24	21	59808	40192	63519	36481	03711	96289	39	36		
28	22	59837	40163	63553	36447	03716	96284	38	32		
32	23	59866	40134	63588	36412	03722	96278	37	28		
36	24	59895	40105	63623	36377	09727	96273	36	24		
40	25	9.59924	10.40076	9.63657	1 0.36343	10.03733	9.96267	35	20		
44	26	59954	40046	63692	36308	03738	96262	34	16		
48	27	59983	40017	63726	36274	03744	96256	33	12		
52	28	60012	39988	63761	36239	03749	96251	32	8		
56 34	29 30	60041	39959 1 0.39930	63796	36204	03755 1 0.03760	96245	31 30	26		
4	31	9.60070 60099	39901	9.63830 63865	. 10. 36170 36135	03766	9.96240 96234	29	56		
8	32	60128	39872	63899	36101	03771	96229	28	52		
12	33	60157	39843	63934	36066	03777	96223	27	48		
16	34	60186	39814	63968	36032	03782	96218	26	44		
20	35	9.60215	10.39785	9.64003	10.35997	10.03788	9.96212	25	40		
24	36	60244	39756	64037	35963	03793	96207	24	36		
28	37	60273	39727	64072	35928	03799	96201	23	32		
32	38	60302	39698	64100	35894	03804	96196	22	28		
36	39	60331	39669	64140	35860	03810	96190	21	24		
40	40	9.60359 60388	10.39641 39612	9.64175	10.35825	10.03815	9,96185	20	20		
48	41 42	60417	39583	64209 64243	35791 35757	$03821 \\ 03826$	96179 96174	19 18	16 12		
52	43	60446	39554	$64245 \\ 64278$	$\begin{array}{c} 35757 \\ 35722 \end{array}$	03832	96168	17	8		
56	44	60474	39526	64312	35688	03838	96162	16	4		
35	45	9.60503	10.39497	9.64346	10.35654	10.03843	9.96157	15	25		
4	46	60532	39468	64381	35619	03849	96151	14	56		
3	47	60561	39439	64415	35585	03854	96146	13	52		
12	48	60589	39411	64449	35551	03860	96140	12	48		
16	49	60618	39382	64483	35517	03865	96135	11	44		
20	50	9.60646	10.39354	9.64517	10.35483	10.03871	9.96129	10	40		
24 28	51 52	60675 60704	39325 39296	64 5 52 64586	$35448 \\ 35414$	03877	96123	9	36		
32	53	60732	39268	64620	35380	03888	96118 96112	8 7	32 28		
36	54	60761	39239	64654	35346	03893	96107	6	24		
40	55	9.60789	10.39211	9.64688	10.85312	10.03899	9.96101	5	20		
44	56	60818	39182	64722	35278	03905	96095	4	16		
48	57	60846	39154	64756	35244	03910	96090	3	12		
52	58	60875	39125	64790	35210	03916	96084	2	8		
56	59	60903	39097	64824	35176	03921	96079	1	4		
36	60	60931	39069	64858	35142	03927	96073	0	24		
M.S. 7h	M 1199	Cosine.	Secant.	Cotangent	Tangent.	Cosecant.	Sine.	M	M.S.		
[/"]	113							66° $ $	4h		
								-			

			13COA1	WILLIAM J	RIGONOME	TRIC.			101
1 ^b	24°)		Loga	rithms.			155°	10 ^h
M.S.	M	Sine.	Cosecant.	Tangent.	Cotangent.	Secant.	Cosine.	[M	M.S.
36	0	9.60931	10.39069	9.64858	10.35142	10.03927	9.96073	60	24
4	1	60960	39040	64892	35108	03933	96067	59	56
8	2	60988	39012	64926	35074	03938	96062	58	52
12	3	61016	38984	64960	35040	03944	96056	57	48
16	4	61045	38955	64994	35006	03950	96050	56	44
20	5	9.61073 61101	10.38927 38899	9.65028 65062	10.34972 34938	10.03955	9.96045	55	40 36
24 28	6 7	61129	38871	65096	34904	03961 03966	96039 96034	54 53	32
32	8	61158	38842	65130	34870	03972	96028	52	28
36	9	61186	38814	65164	34836	03978	96022	51	24
40	10	9.61214	10.38786	9.65197	10.34803	10.03983	9.96017	50	20
44	11	61242	38758	65231	34769	03989	96011	49	16
48	12	61270	38730	65265	34735	03995	96005	48	12
52	13	61298	38702	65299	34701	04000	96000	47	8
56	14	61326	38674	65333	34667	04006	95994	46	4
37	15	9.61354	10.38646	9.65366	10.34634	10.04012	9.95988	45	23
4	16	61382	38618	65400 65434	34600	04018	95982	44	56
8	17	61411 61438	38589 38562	65467	34566 34533	$04023 \\ 04029$	95977 95 971	43	52 48
12 16	18 19	61466	38534	65501	34499	04035	95965	42 41	44
20	20	9.61494	10.38506	9.65535	10.34465	10.04040	9.95960	40	40
24	21	61522	38478	65568	34432	04046	95954	39	36
28	22	61550	38450	65602	34398	04052	95948	38	32
32	23	61578	38422	65636	34364	04058	95942	37	28
36	24	61606	38394	65669	34331	04063	95937	36	24
40	25	9.61634	10.38366	9.65703	10.34297	10.04069	9.95931	35	20
44	26	61662	38338	65736	34264	04075	95925	34	16
48	27	61689	38311	65770	34230	04080	95920	33	12
52	28	61717	38283	65803	34197	04086	95914	32	8
56	29	61745	38255 10.38227	65837 9.65870	34163 10.34130	04092 10.04098	95908	31	4 23
38	30	9.61773 61800	38200	65904	34096	04103	9.95902 95897	30 29	56
4 8	31 32	61828	38172	65937	34063	04109	95891	28	52
12	33	61856	38144	65971	34029	04115	95885	27	48
16	34	61883	38117	66004	33996	04121	95879	26	44
20	35	9.61911	10.38089	9.66038	10.33962	10.04127	9.95873	25	40
24	36	61939	38061	66071	33929	04132	95868	24	36
28	37	61966	38034	66104	33896	04138	95862	23	32
32	38	61994	38006	66138	33862	04144	95856	22	28
36	39	62021	37979	66171	33829	04150	95850	21	24 20
40	40	9.62049	10.37951 37924	$9.66204 \\ 66238$	10.33796 33762	10.04156 04161	9.95844	20 19	16
44	41	$62076 \\ 62104$	37896	66271	33729	04167	95839 95833	18	12
48 52	42 43	62131	37869	66304	33696	04173	95827	17	8
56	44	62159	37841	66337	33663	04179	95821	16	4
39	45	9.62186	10.37814	9.66371	10.33629	10.04185	9.95815	15	21
4	46	62214	37786	66404	33596	04190	95810	14	56
8	47	62241	37759	66437	33563	04196	95804	13	52
12	48	62268	37732	66470	33530	04202	95798	12	48
16	49	62296	37704	66503	33497	04208	95792	11	44
20	50	9.62323	10.37677	9.66537	10.33463	10.04214	9.95786	10	40 36
24	51	62350	37650	66570 66603	33430 33397	$04220 \ 04225$	9 57 80 9 577 5	9	32
28	52	62377	37623 37595	66636	33364	04223	95769	7	28
32 36	53 54	62405 62432	37568	66669	33331	04237	95763	6	24
40	55	9.62459	10.37541	9.66702	10.33298	10.04243	9.95757	5	20
44	56	624 86	37514	66735	33265	04249	95751	4	16
48	57	62513	37487	66768	33232	04255	95745	3	12
52	58	62541	37459	66801	33199	04261	95739	2	8
56	59	62568	37432	66834	33166	04267	95733	1	4
40	60	62595	37405	66867	33133	04272	95728	0	20
M.S.	M	Cosine.	Secant.	Cotangent	Tangent.	Cosecant.	Sine.		M.S.
7 ^b	114	0						65°	4 ^h
L									

1 ^h	25°) 		Loga	rithms.			1549	10h
M.S.	М	Sine.	Cosecant.	Tangent.	Cotangent.		Cosine.	1 M	M.S.
40	0	9.62595	10.37405	9.66867	10.33133	10.04272	9.95728	60	20
4	1	62622	37378	66900	33100	04278	95722	59	56
8	2	62649	37351	66933	33067	04284	95716	58	52 48
12 16	3 4	62676 62703	37324 37297	66966 66999	33034 33001	$04290 \\ 04296$	95710 95704	57 56	44
20	5	9.62730	10.37270	9.67032	10.32968	10.04302	9.95698	55	40
24	6	62757	37243	67065	33935	04308	95692	54	36
28	7	62784	37216	67098	32902	04314	95686	53	32
32	8	62811	37189	67131	32869	04320	95680	52	28
36	9	62838	37162	67163	32837	04326	95674	51	24
40	10	9.62865	10.37135 37108	9.67196 67229	10.32804 32771	10.04332	9.95668	50 49	20 16
44 48	11 12	62892 62918	37082	67262	32771	$04337 \\ 04343$	95663 95657	48	12
52	13	62945	37055	67295	32705	04349	95651	47	8
56	14	62972	37028	67327	32673	04355	95645	46	4
41	15	9.62999	10.37001	9.67360	10.32640	10.04361	9.95639	45	19
4	16	63026	36974	67393	32607	04367	95633	44	56
8	17	63052	36948	67426	32574	04373	95627	43	52
12	18	63079	36921	67458	32542	04379	95621	42	48
16 20	19	63106 9.63133	36894 10.36867	67491 9.67524	32509 10.32476	04385 10.04391	95615 9,95609	41 40	44 40
24	$\begin{vmatrix} 20 \\ 21 \end{vmatrix}$	63159	36841	67556	32444	04397	95603	39	36
28	22	63186	36814	67589	32411	04403	95597	38	32
32	23	63213	36787	67622	32378	04409	95591	37	28
36	24	63239	36761	67654	32346	04415	95585	36	24
40	25	9.63266	10.36734	9.67687	10.32313	10.04421	9.95579	35	20
44	26	63292	36708	67719 67752	32281 32248	04427	95573	34 33	16 12
48 52	27 28	63319 63345	36681 36655	67785	32215	04433 04439	95567 95561	32	8
56	29	63372	56628	67817	32183	04445	95555	31	4
42	30	9.63398	10.36602	9.67850	10.32150	10.04451	9.95549	30	18
4	31	63425	36575	67882	32118	04457	95543	29	56
8	32	63451	36549	67915	32085	04463	95537	28	52
12	33	63478	36522	67947	32053	04469	95531	27	48
16 20	34 35	63504 9.63531	36496 10.36469	67980 9.68012	32020 10.31988	04475 10.04481	$955\overline{25} = 9.95519$	$\begin{array}{c} 26 \\ 25 \end{array}$	44 40
24	36	63557	36443	68044	31956	04487	95513	24	36
28	37	63583	36417	68077	31923	04493	95507	23	32
32	38	63610	36390	68109	31891	04500	95500	22	28
36	39	63636	36364	68142	31858	04506	95494	21	24
40	40	9.63662	10.36338	9.68174	10.31826	10.04512	9,95488	20	20
44	41	63689 63715	36311 36285	68206 68239	$31794 \\ 31761$	$04518 \\ 04524$	$95482 \\ 95476$	19 18	16 12
48 52	42 43	63741	36259	68271	31729	04530	95470	17	8
56	44.	63767	36233	68303	31697	04536	95464	16	4
43	45	9.63794	10.36206	9.68336	10.31664	10.04542	9.95458	15	17
4	46	63820	36180	68368	31632	04548	95452	14	56
8	47	63846	36154	68400	31600	04554	95446	13	52
12	48	63872	36128	68432	31568	04560	95440	12	48
16 20	49	63898 9.63924	36102 10,36076	68 46 5 9.68 4 97	31535 10.31503	$04566 \\ 10.04573$	95434	11 10	44 40
24	50 51	63950	36050	68529	31471	04579	$\begin{array}{c} 9.95427 \\ 95421 \end{array}$	9	36
28	52	63976	36024	68561	31439	04585	95415	8	32
32	53	64002	35998	68593	31407	04591	95409	7	28
36	54	64028	35972	68626	31374	04597	95403	6	24
40	55	9.64054	10.35946	9.68658	10.31342	10.04603	9.95397	5	20
44	56	64080	35920	68690	31310	04609	95391	4	16
48 52	57 58	64106	35894 35868	68722 - 68754	$31278 \ 31246$	$04616 \\ 04622$	95384	3 2	12 8
56	59	$64132 \\ 64158$	35842	68786	31214	04628	$95378 \\ 95372$	1	4
44	60	64184	35816	68818	31182	04634	95366	0	16
M. S.	M	Cosine.	_	Cotangent		Cosecant.	Sine.	_	M.S.
	115							64°	4h
	1							0 x	0

				2002		TRIGONOM.	131 1/10.			13
	h	000						_	× 0.0	1
-	1 "	26°			Loga	rithms.		1	.53°	10 ^h
M	.s	M	Sine.	Cosecant.	Tangent.	Cotangent.	Secant.	Cosine.	M	M.S.
4	4	0	9.64184	10.35816	9.68818	10.31182	10.04634	9.95366	60	16
	4	1	64210	35790	68850	31150	04640	95360	59	56
	8	2	64236	35764	68882	31118	04646	95354	58	52
	12	3	64262	35738	68914	31086	04652	95348	57	48
	16	4	64288	35712	68946	31054	04659	95341	56	44
	20	5	9.64313	10.35687	9.68978	10.31022	10.04665	9.95335	55	40
	24 28	6 7	64339 64365	35661	69010	30990	04671	95329	54	36
	32	8	64391	35635 35609	69042 69074	30958 30926	$04677 \\ 04683$	95323 95317	53 52	32 28
	36	9	64417	35583	69106	30894	04690	95310	51	24
	40	10	9.64442	10.35558	9.69138	10.30862	10.04696	9.95304	50	20
	44	11	64468	35532	69170	30830	04702	95298	49	16
-	48	12	64494	35506	69202	30798	04708	95292	48	12
	52	13	64519	35481	69234	30766	04714	95286	47	8
	56	14	64545	35455	69266	30734	04721	95279	46	4
4	15	15	9.64571	10.35429	9.69298	10.30702	10.04727	9.95273	45	15
	4	16	64596	35404	69329	30671	04733	95267	44	56
	$\frac{8}{12}$	17 18	$64622 \\ 64647$	35378 35353	69361 69393	30639 30607	$04739 \\ 04746$	95261	43	52
1	16	19	64673	35327	69425	30575	04740	95254 95248	42	48 44
	20	20	9.64698	10.35302	9.69457	10.30543	10.04758	9.95242	40	40
	24	21	64724	35276	69488	30512	04764	95236	39	36
	28	22	64749	35251	69520	30480	04771	95229	38	32
	32	23	64775	35225	69552	30448	04777	95223	37	28
	36	24	64800	- 35200	69584	30416	04783	95217	36	24
1	40	25	9.64826	10.35174	9.69615	10.30385	10.04789	9.95211	35	20
	44	26	64851	35149	69647	30353	04796	95204	34	16
	48 52	27	64877	35123	69679	30321	04802	95198	33 32	12 8
	56	28 29	64902 64927	35098 35073	69710 69742	30290 30258	04808 04815	95192 95185	31	4
	16	30	9.64953	10.35047	9.69774	10.30226	10.04821	9.95179	30	14
	4	31	64978	35022	69805	30195	04827	95173	29	56
	8	32	65003	34997	69837	30163	04833	95167	28	52
	12	33	65029	34971	69868	30132	04840	95160	27	48
	16	34	65054	34946	69900	30100	04846	95154	26	44
	20	35	9.65079	10.34921	9.69932	10.30068	10.04852	9.95148	25	40
	24	36	65104	34896	69963	30037	04859	95141 95135	24 23	$\begin{array}{c} 36 \\ 32 \end{array}$
	$\frac{28}{32}$	37 38	65130 65155	34870 34845	69995 70026	30005 29974	$04865 \\ 04871$	95129	22	28
	36	39	65180	34820	70058	29942	04878	95122	21	24
	40	40	9.65205	10.34795	9.70089	10.29911	10.04884	9.95116	20	20
	44	41	65230	34770	70121	29879	04890	95110	19	16
	48	42	65255	34745	70152	29848	04897	95103	18	12
	52	43	65281	34719	70184	29816	04903	95097	17	8
	56	44	65306	34694	70215	29785	04910	95090	16	4
1 4	17	45	9.65331 65356	10.34669 34644	9.70247 - 70278	$\begin{array}{c c} 10.29753 \\ \hline 29722 \end{array}$	$\begin{array}{c} 10.04916 \\ 04922 \end{array}$	9. 95084 95078	15 14	13 56
	8	46 47	65381	34619	70309	29691	04929	95078	13	52
-	12	48	65406	34594	703 \ 1	29659	04935	95065	12	48
	16	49	65431	34569	70372	29628	04941	95059	11	44
	20	50	9.65456	10.34544	9.70404	10.29596	10.04948	9.95052	10	40
1 5	24	51	65481	34519	70435	29565	04954	95046	9	36
	28	52	65506	34494	70466	29534	04961	95039	8	32
	32	53	65531	34469	70498	29502	04967	95033	7	28
	36	54	65556	34444	70529	$\begin{array}{c} 29471 \\ 10.29440 \end{array}$	04973 10.04980	95027 9.95020	6 5	24 20
	10 14	55 56	9.65580 65605	10.34420 34395	$9.70560 \\ 70592$	29408	04986	9.95020	4	16
	18	57	65630	34370	70623	29377	04993	95007	3	12
	52	58	65655	34345	70654	29346	04999	95001	2	8
	56	59	65680	34320	70685	29315	05005	. 94995	1	4
	18	60	65705	34295	70717	29283	05012	94988	θ	12
	.S.	M	Cosine.	Secant.	Cotangent	Tangent.	Cosecant.	Sine.	M	M.S.
17	h	116	,						63°	4h
\$									-	

190			100	AKIIIMS	INIGONOM	ETRIC.			
1 ^h	270			Loga	rithms.		-	152°	10 ^t
M.S.	M	Sine.	Cosecant.	Tangent.	Cotangent.	Secant.	Cosine.	M	
48	0	9.65705	10.34295	9.70717	10.29283	10.05012	9.94988	60	
4	1	65729	34271	70748	29252 29221	05018	94982	59	
8 12	$\begin{vmatrix} 2 \\ 3 \end{vmatrix}$	65754 65779	34246 34221	70779	29190	05025 05031	94975 94969	58	
16	4	65804	34196	70841	29159	05038	94962	56	
20	5	9.65828	10.34172	9.70873	10.29127	10.05044	9.94956	55	
24	6	65853	34147	70904	29096	05051	94949	54	36
28	7	65878	34122	70935	29065	- 05057	94943	53	
32	8	65902	34098	70966	29034	05064	94936	52	
36	9	65927	34073	70997 9.71028	29003	05070 10.05077	94930	51	24
40	10	9.65952 65976	10.34048 34024	71028	10.28972 28941	05083	9.94923 94917	50 49	20
48	12	66001	33999	71090	28910	05089	94911	48	12
52	13	66025	33975	71121	28879	05096	94904	47	8
56	14	66050	33950	71153	28847	05102	94898	46	1
49	15	9.66075	10.33925	9.71184	10.28816	10.05109	9.94891	45	111
4	16	66099	33901	71215	28785	05115	94885	44	56
8	17	66124	33876	71246	28751	05122	94878	43	52
12	18	66148 66173	33852 33827	71277	28723 28692	$05129 \\ 05135$	94871	42	48
16 20	19 20	9.66197	10.33803	71308 9.71339	10.28661	10.05142	94865 9.94858	41 40	44 40
24	21	66221	33779	71370	28630	05148	94852	39	36
28	22	66246	33754	71401	28599	05155	94845	38	32
32	23	66270	33730	71431	28559	05161	94839	37	28
36	24	66295	33705	71462	28538	05168	94832	36	24
40	25	9.66319	10.33681	9.71493	10.28507	10.05174	9.94826	35	20
44	26	66343	33657	71524	28476	05181	94819	34	16
48 52	27 28	66368 66392	33632 33608	71555 71586	$28445 \\ 28414$	$05187 \\ 05194$	94813 94806	33 32	12 8
56	29	66416	33584	71617	28383	05201	94799	31	4
50	30	9.66441	10.33559	9.71648	10.28352	10.05207	9.94793	30	10
4	31	66465	33535	71679	28321	05214	94786	29	56
8	32	66489	33511	71709	28291	05220	94780	28	52
12	33	66513	33487	71740	28260	05227	94773	27	48
16	34	66537	33463	71771	28229	05233	94767	26	41
$\frac{20}{24}$	35 36	9.66562 66586	10.33438 33414	9.71802 71833	10.28198 28167	10.05240 05247	9.94760	25 24	40
28	37	66610	33390	71863	28137	05253	94753 94747	23	$\begin{array}{c} 36 \\ 32 \end{array}$
32	38	66634	33366	71894	28106	05260	94740	22	28
36	39	66658	33342	71925	28075	05266	94734	21	24
40	40	9.66682	10.33318	9.71955	10.28045	10.05273	9.94727	20	20
44	41	66706	33294	71986	28014	05280	94720	19	16
48	42	66731 66755	33269	72017	27983	05286	94714	18	12
52 56	43 44	66779	$33245 \\ 33221$	72048 72078	$\begin{array}{c} 27952 \\ 27922 \end{array}$	05293 05300	94707 94700	17 16	8 4
51	45	9.66803	10.33197	9.72109	10.27891	10.05306	9.94694	15	9
4	46	66827	33173	72140	27860	05313	94637	14	56
8	47	66851	33149	72170	27830	05320	94680	13	52
12	48	66875	33125	72201	27799	05326	94674	12	48
16	49	66899	33101	72231	27769	05333	94667	11	44
$\frac{20}{24}$	50 51	9.66922	10.33078 33054	$9.72262 \\ 72293$	10.27738	10.05346	9.94660	10	40
28	52	66970	33030	72323	27707 27677	05353	94654 = 94647	9 8	36 32
32	53	66994	33006	72354	27646	05360	94640	7	28
36	5±	67018	32982	72384	27616	05366	94634	6	24
40	55	9.67042	10.32958	9.72415	10.27585	10.05373	9.94627	5	20
44	56	67066	32934	72445	27555	05380	94620	4	16
48	57 58	67090	32910	72476	27524	05386	94614	3	12
52 56	58 59	67113 67137	32887 32863	$72506 \\ 72537$	$27494 \\ 27463$	05393	94607	2	8
52	60	67161	32839	72567	27433	$05400 \\ 05407$	$94600 \\ 94593$	1	8
M.S.	M	Cosine.		Cotangent		Cosecant.	Sine.	_	M.S.
7h	1179				J			62°	4h
,								7 200	

	LOUARITHMS TRIGONOMETRIC.										
1h	28°			Loga	rithms.		-	151°	10 ^h		
M.S.	M	Sine.	Cosecant.	Tangent.			Cosine.	M	M.S.		
52	0	9.67161	10.32839	9.72567	10.27433	10.05407	9.94593	60	8		
8	$\frac{1}{2}$	67185 67208	$\frac{32815}{32792}$	72598 72628	27402 27372	05413	94587	59	56		
12	3	67232	32768	72659	27341	$05420 \\ 05427$	94580 94573	58 57	52 48		
16	4	67256	32744	72689	27311	05433	94567	56	44		
20	5	9.67280	10.32720	9.72720	10.27280	10.05440	9.94560	55	40		
24	6	67303	32697	72750	27250	05447	94553	54	36		
28	7	67327	32673	72780	27220	05454	94546	53	32		
32 36	8	67350 67374	32650 32626	72811 72841	27189	05460	94540	52	28		
40	9 10	9.67398	10.32602	9.72872	27159 10.27128	05467 10.05474	94533 9,94526	51 50	24 20		
44	111	67421	32579	72902	27098	05481	94519	49	16		
48	12	67445	32555	72932	27068	05487	94513	48	12		
52	13	67468	32532	72963	27037	05494	94506	47	8		
56	14	67492	32508	72993	27007	05501	94499	46	4		
53	15	9.67515 67539	10.32485 32461	9.73023	10.26977	10.05508	9.94492	45	7 56		
4 8	16 17	67562	32438	73054 73084	$26946 \\ 26916$	05515 05521	94 4 85 9 44 79	44 43	52		
12	18	67586	32414	73114	26886	05528	94472	42	48		
16	19	67609	32391	73144	26856	05535	94465	41	44		
20	20	9.67633	10.32367	9.73175	10.26825	10.05542	9.94458	40	40		
24	21	67656	32344	73205	26795	05549	94451	39	36		
28	22	67680	32320 32297	73235 73265	26765	05555	94445	38	32 28		
32 36	23 24	67703 67726	32274	73295	26735 26705	05562 05569	94438 94431	37 36	28		
40	25	9.67750	10.32250	9.73326	10.26674	10.05576	9.94424	35	20		
44	26	67773	32227	73356	26644	05583	94417	34	16		
48	27	67796	32204	73386	26614	05590	94410	33	12		
52	28	67820	32180	73416	26584	05596	94404	32	8		
56	29	67843	32157	73446 9.73476	26554	05603	94397	31	6		
54	30 31	9.67866 67890	10.32134 32110	73507	10.26524 26493	10.05610 05617	9.94390 94383	30 29	56		
8	32	67913	32087	73537	26463	05624	94376	28	52		
12	33	66936	32064	73567	26433	05631	94369	27	48		
16	34	67959	32041	73597	26403	05638	94362	26	44		
20	35	9.67982	10.32018	9.73627	10.26373	10.05645	9.94355	25	40		
24	36	68006	31994	73657	26343	05651	94349	24 23	$\begin{array}{c} 36 \\ 32 \end{array}$		
28 32	37 38	68029 68052	31971 31948	73687 73717	$\begin{array}{c} 26313 \\ 26283 \end{array}$	05658 05665	$94342 \\ 94335$	22 22	28		
36	39	68075	31925	73747	26253	05672	94328	21	24		
40	40	9.68098	10.31902	9.73777	10.26223	10.05679	9.94321	20	20		
44	41	68121	31879	73807	26193	05686	94314	19	16		
48	42	68144	31856	73837	26163	05693	94307	18	12		
52	43	68167 68190	31833 31810	73867 73897	$26133 \\ 26103$	05700 05707	94300 94293	17 16	. 8		
56	44 45	9.68213	10.31787	9.73927	.10.26073	10.05714	9,94286	15	5		
4	46	68237	31763	73957	26043	05721	94279	14	56		
8	47	68260	31740	73987	26013	05727	94273	1 3	52		
12	48	68283	31717	74017	25983	05734	94266	12	48		
16	49	68305	31695	74047	25953	05741 10.05748	94259	11	44 40		
20	50	9.68328	10.31672 31649	9.74077 74107	10.25923 25893	05755	$\begin{array}{c} 9.94252 \\ 94245 \end{array}$	10 9	36		
24 28	51 52	68351 68374	31626	74137	25863	05762	94243	8	$\frac{30}{32}$		
32	53	68397	31603	74166	25834	05769	94231	7	28		
36	54	68420	31580	74196	25804	05776	94224	6	24		
40	55	9.68443	10.31557	9.74226	10.25774	10.05783	9.94217	5	20		
44	56	68466	31534	74256	25744	05790	94210	4	16		
48	57	68489	31511	74286	$25714 \\ 25684$	05797	94203 9 41 96	3 2	12 8		
52 56	58 59	68512 68534	31488 31466	74316 74345	25655	05804 05811	94190	1	4		
56	60	68557	31443	74375	25625	05818	94182	0	4		
M.S.	M	Cosine.		Cotangent		Cosecant.	Sine.		M. S.		
	118							61°	4h		
			MARKETTA P. MARKET								

192	LOGARITHMS TRIGONOMETRIC.									
1 ^b	29°			Loga	rithms.		-	150°	10 ^h	
M.S.	M	Sine.	Cosccant.	Tangent.	Cotangent.	Sceant.	Cosine.	M	M.S.	
56	0	9.68557	10.31443	9.74375	10.25625	10.05818	9.94182	60	4	
4	ĭ	68580	31420	74405	25595	05825	94175	59	56	
8	2	68603	31397	74435	25565	05832	94168	58	52	
12	3	68625	31375	74465	25535	05839	94161	57	48	
16	4	68648	31352	74494	25506	05846	94154	56	44	
20	5	9.68671	10.31329	9.74524	10.25476	10.05853	9.94147	55	40	
24	6	68694	31306	74554	25446	05860	94140	54	36	
28	7	68716	31284	74583	25417	05867	94133	53	32	
32	8	68739	31261	74613	25387	05874	94126	52	28	
36	9	68762	31238	74643	25357	05881	94119	51	24	
40	10	9.68784	10.31216	9.74673	10.25327	10.05888	9.94112	50	20 · 16	
44	11	68807	31193	74702	25298	05895	94105	49	12	
48	12	68829	31171	74732	25268	05902	94098 94090	48 47	8	
52	13	68852 68875	31148	74762 74791	25238 25209	05910 05917	94083	46	4	
56 57	14	9.68897	31125 10.31103	9.74821	10.25179	10.05924	9.94076	45	3	
4	15 16	68920	31080	74851	25149	05931	94069	44	56	
8	17	68942	31058	74880	25120	05938	94062	43	52	
12	18	68965	31035	74910	25090	05945	94055	42	48	
16	19	68987	31013	74939	$25 \cup 61$	05952	94048	41	44	
20	20	9.69010	10.30990	9.74969	10.25031	10.05959	9.94041	40	40	
24	21	69032	30968	74998	25002	05966	94034	39	36	
28	22	69055	30945	75028	24972	05973	94027	38	32	
32	23	69077	30923	75058	24942	05980	94020	37	28	
36	24	69100	30900	75087	24913	05988	94012	36	24	
40	25	9.69122	10.30878	9.75117	10.24883	10.05995	9.94005	35	20	
44	26	69144	3 08 5 6	75146	24854	06002	93998	34	16	
48	27	69167	30833	75176	24824	06009	93991	33	12	
52	28	69189	30811	75205	24795	06016	93984	32	8	
56	29	69212	30788	75235	24765	06023	93977	31	4	
58	30	9.69234	10.30766	9.75264	10.24736	10.06030	9.93970	30	2	
4	31	69256	30744	75294	24706	06037	93963	29	56 52	
8	32	69279 69301	3 0721 3 0699	75323 75353	24677 24647	06045	$93955 \\ 93948$	28 27	48	
12 16	33 34	69323	30677	75382	24618	06052 06059	93940	26	44	
20	35	9.69345	10.30655	9.75411	10.24589	10.06066	9.93934	25	40	
24	36	69368	30632	75441	24559	06073	93927	24	36	
28	37	69390	30610	75470	24530	06080	93920	23	32	
32	38	69412	30588	75500	24500	06088	93912	22	28	
36	39	69434	30566	75529	24471	06095	93905	21	24	
40	40	9.69456	10.30544		10.24442	10.06102	9,93898	20	20	
44	41	69479	30521	75588	24412	06109	93891	19	16	
48	42	69501	30499	75617	24383	06116	93884	18	12	
52.	43	69523	30177	75647	24353	06124	93876	17	8	
56	44	69545	30455	75676	24324	06131	93869	16	4	
59	45	9.69567	10.30433	9.75705	10.24295	10.06138	9.93862	15	1	
4	46	69589	30411	75735	24265	06145	93855	14	56	
8	47	69611	30389	75764	24236	06153	93847	13	52	
12 16	48 49	69633 69655	30367 30345	75793 75822	$24207 \\ 24178$	-06160 -06167	93840	12 11	48 44	
20	5()	9.69677	10.30323	9.75852	10.24148		9.93826		40	
24	51	69699	30301	75881	24119	10.06174 06181	93819	10 9	36	
28	52	69721	30279	75910	24090	06189	93811	8	32	
32	53	69743	30257	75939	24061	06196	93804	7	28	
36	54	69765	30235	75969	24031	06203	93797	6	24	
40	55	9.69787	10.30213	9.75998	10.24002	10.06211	9.93789	5	20	
44	56	69809	30191	76027	23973	06218	93782	4	16	
48	57	69831	30169	76056	23944	06225	93775	3	12	
52	58	69853	30147	76086	23914	06232	93768	2	8	
56	59	69875	30125	76115	23885	06240	93760	1	4	
60	60	69897	30103	76144	23856	06247	93753	0	0	
M. S.		Cosine.	Secant.	Cotangent	Tangent.	Cosecant.	Sine.	M	M.S.	
7h	119							60°	4 ^h	
An orman	-			-						

			23001	***************************************	IMIGONOM	ETRIC.			130
Oh	000						_		
2"	30°			Loga	rithms.		1	49°	9h
M.S.	M	Sine.	Cosecant.	Tangent.	·Cotangent.	Secant.	Cosine.	M	M.S.
0	0	9.69897	10.30103	9.76144	10.23856	10.06247	9.93753	60	60
+	1.	69919	30081	76173	23827	06254	93746	59	56
8	2	69941	30059	76202	23798	06262	93738	58	52
12	3	69933	30037	76231	23769	06269	93731	57	48
16	4	69984	30016	76261	23739	06276	93724	56	44
20	5 6	9.70006 70028	10.29994 29972	$9.76290 \\ 76319$	10.23710 23681	· 10.06283 06291	9.93717 93709	55 54	40 36
28	7	70050	29950	76348	23652	06298	93709	53	32
32	8	70072	29928	76377	23623	06305	93695	52	28
36	9	70093	29907	76406	23594	06313	93687	51	24
40	10	9.70115	10.29885	9.76435	10.23565	10.06320	9.93680	50	20
44	11	70137	29863	76464	23536	06327	93673	49	16
48	12	70159 70180	29841	76493	23507	06335	93665	48	12
52 56	13 14	70202	29820 29798	76522 76551	23478 23449	$06342 \\ 06350$	93658 93650	47	8 4
1	15	9.70224	10.29776	9.76580	10.23420	10.06357	9.93643	45	59
4	16	70245	29755	76609	23391	06364	93636	44	56
8	17	70267	29733	76639	23361	06372	93628	43	52
12	18	70288	29712	76668	23332	06379	93621	42	48
16	19	70310	29690	76697	23303	06386	93614	41	44
20	20	9.70332	10.29668	9.76725	10.23275	10.06394	9.93606	40	40
24 28	$\begin{vmatrix} 21 \\ 22 \end{vmatrix}$	70353 70375	29647 29625	76754 76783	$23246 \\ 23217$	$06401 \\ 06409$	93599 93591	39 38	.36 32
32	23	70396	29604	76812	23188	06416	93584	37	28
36	24	70418	29582	76841	23159	06423	93577	36	24
40	25	9.70439	10.29561	9.76870	10.23130	10.06431	9.93569	35	20
44	26	70461	29539	76899	23101	06438	93562	34	16
48	27	70482	29518	76928	23072	06446	93554	33	12
52	28	70504 70525	29496	76957	23043	06453	93547	32 31	8
56	29 30	9.70547	29475 10.29453	76986 9.77015	23014 10.22985	06461 10.06468	93539 9. 93532	30	58
4	31	70568	29432	77044	22956	06475	93525	29	56
8	32	70590	29410	77073	22927	06483	93517	28	52
12	33	70611	29389	77101	22899	06490	93510	27	48
16	34	70633	29367	77130	22870	06498	93502	26	44
20	35	9.70654	10.29346	9.77159	10.22841	10.06505	9.93495	25 24	40
24 28	36 37	70675 70697	29325 29303	77188 77217	$22812 \\ 22783$	$06513 \\ 06520$	93487 93480	23	$\begin{array}{c} 36 \\ 32 \end{array}$
32	38	70718	29282	77246	22754	06528	93472	22	28
36	39	70739	29261	77274	22726	06535	93465	21	24
40	40	9.70761	10.29239	9.77303	10.22697	10.06543	9.93457	20	20
44	41	70782	29218	77332	22668	06550	93450	19	16
48	42	70803	29197	77361	22639	06558	93442	18	12
52	43	70824 70846	29176 29154	77390 77418	$\begin{array}{c} 22610 \\ 22582 \end{array}$	$06565 \\ 06573$	$\begin{array}{r} 93435 \\ 93427 \end{array}$	$\begin{array}{ c c }\hline 17\\16\\ \end{array}$	8 4
56 3	44 45	9.70867	10.29133	9.77447	10.22553	10.06580	9.93420	15	57
4	46	70888	29112	77476	22524	06588	93412	14	56
8	47	70909	29091	77505	22495	06595	93405	13	52
12	48	70931	29069	77533	22467	06603	93397	12	48
16	49	70952	29048	77562	22438	06610	93390	11	44
20	50	9.70973	10.29027	9.77591	10.22409	10.06618.	9.93382	10	40
24	51	71015	29006 28985	77619 77648	$22381 \ 22352$	$06625 \\ 06633$	93375	8	36 3 2
28 32	52 53	71015 71036	28964	77677	22323	06640	93367 93360	7	28
36	51	71058	28942	77706	22294	06648	93352	6	24
40	55	9.71079	10.28921	9.77734	10.22266	10.06656	9.93344	5	20
44	56	71100	28900	77763	22237	06663	93337	4	16
48	57	71121	28879	77791	22209	06671	93329	3	12
52	58	71142	28858	77820	22180	06678	93322	2	8
56	59 60	71163 71184	28837 28816	77849 77877	$22151 \\ 22123$	$06686 \\ 06693$	93314 93307	$\begin{bmatrix} 1 \\ 0 \end{bmatrix}$	4 56
M.S.	M	Cosine.		Cotangent		Coseeant.	Sine.		M. S.
	120		, , , , , , , , , , , , , , , , , , , ,	Comagon.	20.20.	500000000		59°	
	120								

T2:3			LOGA	ARITHMS	TRIGONOM	ETRIC.			
2h	31°			Loga	rithms.	,	1	.48°	9h
M.S.	M	Sine.	Cosecant.	Tangent.		Secant.	Cosine.	M	M.S
4	0	9.71184	10.28816	9.77877	10.22123	10.06693	9.93307	60	56
4	1	71205	28795	77906	22094	06701	93299	59	56 52
8 12	$\frac{2}{3}$	$71226 \\ 71247$	28774	77935 77963	22065 22037	06709 06716	93291 93284	58 57	48
16	4	71268	28753 28732	77992	22008	06724	93276	56	44
20	5	9.71289	10.28711	9.78020	10.21980	10.06731	9.93269	55	40
24	6	71310	28690	78049	21951	06739	93261	54	36
28	7	71331	28669	78077	21923	06747	93253	53	32
32	8	71352	28648	78106	21894	06754	93246	52	28
36	9	71373	28627	78135	21865	06762	93238	51 50	24 20
40	10 11	9.71393 71414	10.28607 28586	9.78163 78192	10.21837 21808	10.06770 06777	9.93230 93223	49	16
48	12	71435	28565	78220	21780	06785	93215	48	12
52	13	71456	28544	78249	21751	06793	93207	47	8.
56	14	71477	28523	78277	21723	06800	93200	46	4
5	15	9.71498	10.28502	9.78306	10.21694	10.06808	9.93192	45	55
4	16	71519	28481	78334	21666	06816	93184	44	56
8	17	71539	28461	78363	21637	06823	93177	43	52
12 16	18	71560 71581	28440 28419	78391 78419	21609 21581	06831 06839	93169 93161	42 41	48
20	19 20	9.71602	10.28398	9.78448	10.21552	10.06846	9.93154	40	40
24	21	71622	23378	78476	21524	06854	93146	39	36
28	22	71643	28357	78505	21495	06862	93138	38	32
32	23	71664	28336	78533	21467	06869	93131	37	28
36	24	71685	28315	78562	21438	06877	93123	36	24
40	25	9.71705	10.28295	9.78590	10.21410	10.06885	9.93115	35	20
44	26	71726 71747	28274 28253	78618	21382	06892 06900	93108	34 33	16 12
48 52	27 28	71767	28233	78647 78675	$21353 \\ 21325$	06900	$93100 \\ 93092$	32	8
56	29	71788	28212	78704	21296	06916	93084	31	4
6	30	9.71809	10.28191	9.78732	10.21268	10.06923	9.93077	30	54
4	31	71829	28171	78760	21240	06931	93069	29	56
8	32	71850	28150	78789	21211	06939	93061	28	52
12	33	71870	28130	78817	21183	06947	93053	27	48
16 20	34 35	71891 9.71911	28169 10.28089	78845 9.78874	21155 10.21126	$06954 \\ 10.06962$	93046 9,93038	26 ·25	44 40
24	36	71932	28068	78902	21098	06970	93030	24	36
28	37	71952	28048	78930	21070	06978	93022	$\frac{1}{23}$	32
32	38	71973	28027	78959	21041	06986	93014	22	28
36	39	71994	28006	78987	21013	06993	93007	21	24
40	40	9.72014	10.27986	9.79015	10.20985	10.07001	.9.92999	20	20
44	41	72034	27966 27945	79043	20957	07009	92991	19	16
48 52	42 43	72055 72075	27925	79072 79100	20928 20900	$07017 \\ 07024$	92983 92976	18 17	12 8
56	44	72096	27904	79128	20872	07032	92968	16	4
7	45	9.72116	10.27884	9.79156	10.20844	10.07040	9.92960	15	53
4	46	72137	27863	79185	20815	07048	92952	14	56
8	47	72157	27843	79213	20787	07056	93944	13	52
12	48	72177	27823	79241	20759	07064	93936	12	48
16 20	49 50	72198 9.72218	27802 10.27782	79269 9.79297	$\begin{array}{c c} 20731 \\ 10.20703 \end{array}$	07071	$\begin{array}{c} 92929 \\ 9.92921 \end{array}$	11 10	44
24	51	72238	27762	79326	20674	10.07079 07087	9.92921	9	40 36
28	52	72259	27741	79354	20646	07095	92905	8	32
32	53	72279	27721	79382	20618	07103	92847	7	28
36	54	72299	27701	79410	20590	07111	92889	6	24
40	55	9.72320	10.27680	9.79438	10.20562	10.07119	9.92881	5	20
44 48	56 57	72340	27660	79466	20534	07126	92874	4	16
52 52	58	$72360 \\ 72381$	$27640 \\ 27619$	79495 79523	20505 2047 7	$07134 \\ 07142$	92866 - 92858	$\frac{3}{2}$	12 8
56	59	72401	27599	79551	20449	07142	$92858 \\ 92850$	1	4
8	60	72421	27579	79579	20421	07158	92842	0	52
M.S.		Cosine.		Cotangent		Cosceant.	Sine.	M	M.S.
8h	121							5S°	
								-	

LOGARITHMS TRIGONOMETRIC. 19										
2h	329	>		Loos	rithms.			147°	94	
		9	1 0							
M.S. 8	M 0	Sine. 9.72421	Cosecant. 10.27579	Tangent. 9.79579	Cotangent. 10.20421	I	Cosine.	M	M.S.	
4	li	72441	27559	79607	20393	$\begin{array}{c} 10.07158 \\ 07166 \end{array}$	9.92842 92834	60 59	58	
8	2	72461	27539	79635	20365	07174	92826	58	52	
12	3	72482	27518	79663	20337	07182	92818	57	48	
16	4	72502	27498	79691	20309	07190	92810	56	44	
20	5	9.72522 72542	10.27478	9.79719	10.20281	10.07197	9.92803	55	40	
24 28	$\frac{6}{7}$	72562	27458 27438	79747 79776	20253 20224	07205 07213	92795 92787	54 53	36 32	
32	8	72582	27418	79804	20196	07221	92779	52	28	
36	9	72602	27398	79832	20168	07229	92771	51	24	
40	10	9.72622	10.27378	9.79860	10.20140	10.07237	9.92763	50	20	
44	11	72643	27357	79888	20112	07245	92755	49	16	
48 52	12 13	72663 72683	27337 27317	79916 79944	20084 20056	$07253 \\ 07261$	92747 92739	48 47	12 8	
56	14	72703	27297	79972	20028	07269	92731	46	4	
. 9	15	9.72723	10.27277	9.80000	10.20000	10.07277	9.92723	:45	51	
4	16	72743	27257	80028	19972	07285	92715	44	56	
8	17	72763	27237	80056	19944	07293	92707	43	52	
12 16	18	72783 72803	27217 27197	80084 80112	19916	07301	92699	42	48 44	
20	19 20	9.72823	10.27177	9.80140	19888 10.19860	07309 10.07317	92691 9.92683	41 40	40	
24	21	72843	27157	80168	19832	07325	92675	39	36	
28	22	72863	27137	80195	19805	07333	92667	38	32	
32	23	72883	27117	80223	19777	07341	92659	37	28	
36	24	72902	27098	80251	19749	07349	92651	36	24	
40	25 26	9.72922 72942	10.27078 27058	9.80279	10.19721 19693	10.07357 07365	9.92643 92635	35 34	20 16	
48	27	72962	27038	80335	19665	07373	92627	33	12	
52	28	72982	27018	80363	19637	07381	92619	32	8	
56	29	73002	26998	80391	19609	07389	92611	31	4	
10	30	9.73022	10.26978	9.80419	10.19581	10.07397	9.92603	30	50	
8	31	73041 73061	26959 26939	80447 80474	19553 19526	$07405 \\ 07413$	92595 92587	29 28	56 52	
12	32 33	73081	26919	80502	19320	07413	92579	27	48	
16	34	73101	26899	80530	19470	07429	92571	26	44	
20	35	9.73121	10.26879	9.80558	10.19442	10.07437	9.92563	25	40	
24	36	73140	26860	80586	19414	07445	92555	24	36	
28	37	73160	26840	80614 80642	19386	07454	92546	23 22	32 28	
32 36	38 39	73180 73200	26820 26800	80669	$\begin{array}{c} 19358 \\ 19331 \end{array}$	07462 07470	92538 92530	21	24	
40	40	9.73219	10.26781	9.80697	10.19303	10.07478	9.92522	20	20	
44	41	73239	26761	80725	19275	07486	92514	19	16	
48	42	73259	26741	80753	19247	07494	92506	18	12	
52 50	43	73278	26722	80781 80808	19219	07502	92498	17 16	8 4	
56	44 45	73298 9.73318	26702 10.26682	9.80836	19192 10.19164	07510 10.07518	92490 9.92482	15	49	
4	46	73337	26663	80864	19136	07527	92473	14	56	
8	47	73357	26643	80892	19108	07535	92465	13	52	
12	48	73377	26623	80919	19081	07543	92457	12	48	
16	49	73396	26601	80947	19053	07551	92449	11	44	
20 24	50 51	9.73416 73435	$\begin{array}{r} 10.26584 \\ 26565 \end{array}$	9.80975 81003	10.19025 18997	10.07559 07567	9.92441 92433	10	40 36	
28	52	73455	26545	81030	18970	07575	92425	8	32	
32	53	73474	26526	81058	18942	07584	92416	7	28	
36	54	73494	26506	81086	18914	07592	92408	6	24	
40	55	9.73513	10.26487	9.81113	10.18887	10.07600	9.92400	5	20	
44	56	73533	26467	81141 81169	18859 18831	07608 07616	92392 92384	4 3	$\begin{array}{c} 16 \\ 12 \end{array}$	
48 52	57 58	$73552 \\ 73572$	$26448 \\ 26428$	81196	18804	07616	92376	2	8	
56	59	73591	26409	81224	18776	07633	92367	ī	4	
12	60	73611	26389	81252	18748	07641	92359	0	48	
M.S.	M	Cosine.	Secant.	Cotangent	Tangent.	Cosecant.	Sine.		M.S.	
8h	1229							57°	3h	

LOGARITHMS TRIGONOMETRIC.										
26	330							146°	gh	
Z	33			Logar	ithms.			140	9	
M.S.	M	Sinc.	Cosecant.	Tangent.	Cotangent.	Secant.	Cosine.	M	M.S.	
12	0	9.73611	10.26389	9.81252	10.18748	10.07641	9.92359	60	48	
4	1	73630	26370	81279	18721	07649	92351	59	56	
8	2	73650	26350	81307	18693	07657	92343 92335	58 57	52 48	
12 16	3 4	73669 73689	$ \begin{array}{r} 26331 \\ 26311 \end{array} $	81335 81362	18665 18638	$07665 \\ 07674$	92326	56	44	
20	5	9.73708	10.26292	9.81390	10.18610	10.07682	9.92318	55	40	
24	6	73727	26273	81418	18582	07690	92310	54	36	
28	7	73747	26253	81445	18555	07698	92302	53	32	
32	8	73766	26234	81473	18527	07707	92293	52	28	
36	9	73785	26215	81500	18500	07715	92285	51	24	
40	10	9.73805	10.26195 26176	9.81528 · 81556	10.18472	10.07723	9.92277 92269	50 49	20 16	
44 48	11 12	73824 73843	26157	81583	18444 18417	07740	92260	48	12	
52	13	73863	26137	81611	18389	07748	92252	47	8	
56	14	73882	26118	81638	18362	07756	92244	46	4	
13	15	9.73901	10.26099	9.81666	10.18334	10.07765	9.92235	45	47	
4	16	73921	26079	81693	18307	07773	92227	44	56	
8	17	73940	26060	81721	18279	07781	92219	43	52	
12	18	73959 73978	26041 26022	81748 81776	18252 18224	07789 07798	92211 92202	42 41	48 44	
16 20	19 20	9.73997	10.26003	9.81803	10.18197	10.07806	9.92194	40	40	
24	21	74017	25983	81831	18169	07814	92186	39	36	
28	22	74036	25964	81858	18142	07823	92177	38	32	
32	23	74055	25945	81886	18114	07831	92169	37	28	
36	24	74074	25926	81913	18087	07839	92161	36	24	
40	25	9.74093	10.25907	9.81941	10.18059	10.07848	9.92152	35	20 16	
44 48	26 27	74113 74132	25887 25868	81968 81996	$18032 \\ 18004$	$07856 \\ 07864$	921 44 92136	34	12	
52	28	74151	25849	82023	17977	07873	92127	$\frac{33}{32}$	8	
56	29	74170	25830	82051	17949	07881	92119	31	4	
14	30	9.74189	10.25811	9.82078	10.17922	10.07889	9.92111	30	46	
4	31	74208	25792	82106	17894	07898	92102	29	56	
8	32	74227	25773	82133	17867	07906	92094	28	52	
12 16	33 34	74246 74265	25754 25735	82161 82188	$\frac{17839}{17812}$	$07914 \\ 07923$	92086 92077	$\begin{array}{c c} 27 \\ 26 \end{array}$	48 44	
20	35	9.74284	10.25716	9.82215	10.17785	10.07931	9.92069	$\frac{20}{25}$	40	
24	36	74303	25697	82243	17757	07940	92060	24	36	
28	37	74322	25678	82270	17730	07948	92052	23	32	
32	38	74341	25659	82298	17702	07956	92044	22	28	
36	39	74360	25640	82325	17675	07965	92035	21	24	
40	40	9.74379 74398	10.25621	9.82352 82380	10.17648	10 07973	9.92027	20	$\begin{array}{c} 20 \\ 16 \end{array}$	
44 48	41 42	74417	$25602 \\ 25583$	82407	17620 17593	$07982 \\ 07990$	$92018 \\ 92010$	19 18	12	
52	43	74436	25564	82435	17565	07998	92002	17	8	
56	44	74455	25545	82462	17538	08007	91993	16	4	
15	45	9.74474	10.25526	9.82489	10.17511	10.08015	9 91985	15	45	
4	46	74493	25507	82517	17483	08024	91976	14	56	
8	47	74512	25488	82544	17456	08032	91968	13	52	
12 16	48 49	74531 74549	25469 25451	82571 8259 9	$17429 \\ 17401$	08041 08049	91959 91951 *	12 11	48 44	
20	50	9.74568	10.25432	9.82626	10.17374	10.08058	9.91942	10	40	
24	51	74587	25413	82653	17347	08066	91934	9	36	
28	52	74606	25394	82681	17319	08075	91925	8	32	
32	53	74625	25375	82708	17292	08083	91917	7	28	
36	54	74644	25356	82735	17265	08092	91908	6	24	
40 44	55 56	$9.74662 \\ 74681$	10.25338 25319	9.82762 82790	10.17238	10.08100	9.91900	5	$\begin{vmatrix} 20 \\ 16 \end{vmatrix}$	
44 48	57	74681	25300	82817	$17210 \\ 17183$	08109 08117	91891 91883	4 3	12	
52	58	74719	$\frac{25300}{25281}$	82844	17156	08126	91874	2	8	
56	59	74737	2 5263	82571	17129	08134	91866	1	4	
16	60	74756	25244	82899	17101	08143	91857	0	44	
M.S.	M	Cosine.	Secant.	Cotangent	Tangent.	Cosecant.	Sine.		M. S.	
Sn	123							56°	3h	
-					-	-				

	DOGARITAMS TRIGONOMETRIC.									
Oh	0.40						-	450	O'o	
2 ^h	34°			Logar	cithms.		1	45°	9'n	
M.S.	M)	Sine.	Cosecant.	Tangent.	Cotangent.	Secant.	Cosine.	M	M.S.	
16	0	9.74756	10.25244	9.82899	10.17101	10.08143	9.91857	60	44	
4	1	74775	25225	82926	17074	08151	91849	59	56	
8	2	74794	25206	82953	17047	08160	91840	58	52	
12	3	74812	25188	82980	17020	08168	91832	57	48	
16	4	74831	25169	83008	16992	08177	91823	56	44	
20	5 6	9.74850	10.25150	9.83035 83062	10.16965	10.08185	9.91815	55	40 36	
24 28	7	74868 74887	25132 25113	83089	16938 16911	$08194 \\ 08202$	91806 91798	54 53	32	
32	8	74906	25094	83117	16883	08211	91789	52	28	
36	9	74924	25076	83144	16856	08219	91781	51	24	
40	10	9.74943	10.25057	9.83171	10.16829	10.08228	9.91772	50	20	
44	11	74961	25039	83198	16802	08237	91763	49	16	
48	12	74980	25020	83225	16775	08245	91755	48	12	
52	13	74999	25001	83252	16748	08254	91746	47	8 4	
56 17	14 15	75017 9.75030	24983 10.24964	83280 9.83307	16720 10.16693	08262 10. 08271	91738 9.91729	46 45	43	
4	16	75054	24946	83334	16666	08280	91720	44	56	
8	17	75073	24927	83361	16639	08288	91712	43	52	
12	18	75091	24909	83388	16612	08297	91703	42	48	
16	19	. 75110	24896	83415	16585	08305	91695	41	44	
20	20	9.75128	10.24872	9.83442	10.16558	10.08314	9.91686	40	40	
24	21	75147	24853	83470	16530	08323	91677	39	36	
28	22	75165	24835	83497	16503	08331	91669	38	32	
32 36	23 24	75184	24816	835 24 83551	$16476 \\ 16449$	083 4 0 083 4 9	91660 91651	37 36	28 24	
40	25	75202 9.75221	24798 10.24779	9.83578	10.16422	10.08357	9.91643	35	20	
44	26	75239	24761	83605	16395	08366	91634	34	16	
48	27	75258	24742	83632	16368	08375	91625	33	12	
52	28	75276	24724	83659	16341	08383	91617	32	8	
56	29	75291	24706	83686	16314	08392	91608	31	4	
18	30	9.75313	10.24687	9.83713	10.16287	10.08401	9.91599	30	42 56	
4	$\begin{array}{ c c }\hline 31\\ 32\\ \end{array}$	75331	24669 24650	83740 83768	$16260 \\ 16232$	08409 08418	91591 91582	29 28	52	
8 12	33	75350 75368	24632	83795	16205	08427	91573	27	48	
16	34	75386	24614	83822	16178	08435	91565	26	44	
20	35	9.75405	10.24595	9.83849	10.16151	10.08444	9.91556	25	40	
24	36	75423	24577	83876	16124	08453	91547	24	36	
28	37	75441	24559	83903	16097	08462	91538	23	32 28	
32	38	75459	24541	83930 83957	16070	$08470 \\ 08479$	91530 91521	22 21	24	
36 40	39 40	75478 9.75496	24522 10.24504	9.83984	16043 10.16016	10.08488	9.91512	20	20	
44	41	75514	24486	84011	15989	08496	91504	19	16	
48	42	75533	24467	84038	15962	08505	91495	18	12	
52	43	75551	24449	84065	15935	08514	91486	17	8	
56	44	75569	24431	84092	15908	08523	91477	16	4	
19		9.75587	10.24413	9.84119	10.15881	10.08531	9.91469	15 14	41 56	
4 8	46	75605	24395	84146 84173	15854 15827	$08540 \\ 08549$	91460 91451	13	52	
12	47 48	75624 75642	24376 24358	84200	15800	08558	91442	12	48	
16	49	75660	24340	84227	15773	08567	91433	11	44	
20	50	9.75678	10.24322	9.84254	10.15746	10.08575	9.91425	10	40	
24	51	75696	24304	84280	15720	08584	91416	9	36	
28	52	75714	24286	84307	15693	08593	91407	8	32 28	
32	53	75733	24267	84334	15666	08602	91398 91389	$\begin{bmatrix} 7 \\ 6 \end{bmatrix}$	28 24	
36	54 55	75751	24249 10.24231	84361 9.84388	15639 10.15612	08611 10.08619	9,91381	5	20	
44	56	9.75769 75787	24213	84415	15585	08628	91372	4	16	
48	57	75805	24195	84442	15558	08637	91363	3	12	
52	58	75823	24177	84469	15531	08646	91354	2	8	
56	59	75841	24159	84496	15504	08655	91345	1	4	
20	60	75859	24141	84523	15477	08664	91336	0	40	
M.S.	M 104	Cosine.	Secant.	Cotangent	Tangent.	Cosecant.	Sine.	м 55°	м.s. 3h	
8h	124						•	00	U	

198	LOGARITHMS TRIGONOMETRIC.										
2 ^h	35°			Loga	rithms.]	144°	9h		
M.S.	M	Sine.	Cosecant.	Tangent.	Cotangent.	Secant.	Cosine.	1 M	M.S.		
20	0	9.75859	10.24141	9.84523	10.15477	10.08664	9.91336	60	40		
4	1	75877	24123	84550	15450	08672	91328	59	56		
8	2	75895	24105	84576	15424	08681	91319	58	52		
12	3	75913	24087	84603	15397	08690	91310	57	48		
16	4	75931	24069	84630	15370	08699	91301	56	44		
20	5	9.75949	10.24051	9.84657	10.15343	10.08708	9.91292	55	40		
24	6	75967	24033	84684	15316	08717	91283	54	36		
28	7	75985	24015	84711	15289	08726	91274	53	32		
32	8 9	76003 76021	23997 23979	84738 84764	15262 15236	$08734 \\ 08743$	91266 91257	52 51	28 24		
36	10	9.76039	10.23961	9.84791	10.15209	10.08752	9.91248	50	20		
44	11	76057	23943	84818	15182	08761	91239	49	16		
48	12	76075	23925	84845	15155	08770	91230	48	12		
52	13	76093	23907	84872	15128	08779	91221	47	8		
56	14	76111	23889	84899	15101	08788	91212	46	4		
21	15	9.76129	10.23871	9.84925	10.15075	10.08797	9.91203	45	39		
4	16	76146	23854	84952	15048	08806 •	91194	44	56		
8	17	76164	23836	84979	15021	08815	91185	43	52		
12	18	76182	23818	85006	14994	08824	91176	42	48		
16	19	76200	23800	85033	14967	08833	91167.	41	44		
20	20	9.76218	10.23782	9.85059	10.14941	10.08842	9.91158	40	40		
24	21	$76236 \\ 76253$	23764	85086 85113	14914	$08851 \\ 08859$	91149 91141	39	$\begin{array}{ c c }\hline 36\\ 32\\ \end{array}$		
28 32	22 23	76271	$23747 \\ 23729$	85140	14887 14860	08868	91141	37	28		
36	24	76289	23711	85166	14834	08877	91123	36	24		
40	25	9.76307	10.23693	9.85193	10.14807	10.08886	9.91114	35	20		
44	26	76324	23676	85220	14780	08895	91105	34	16		
48	27	76342	23658	85247	14753	08904	91096	33	12		
52	28	76360	23640	85273	14727	08913	91087	32	8		
56	29	76378	23622	85300	14700	08922	91078	31	4		
22	30	9.76395	10.23605	9.85327	10.14673	10.08931	9.91069	30	38		
4	31	76413	23587	85354	14646	08940	91060	29	56		
8	32	76431	23569	85380	14620	08949	91051	28	52		
12 16	33 34	76448 76466	23552 23534	85407 85434	14593	08958 08967	91042	27 26	48 44		
20	35	9.76484	10.23516	9.85460	14566 10.14540	10.08977	91033 9.91023	25	40		
24	36	76501	23499	85487	14513	08986	91014	24	36		
28	37	76519	23481	85514	14486	08995	91005	23	32		
32	38	76537	23463	85540	14460	09004	90996	22	28		
36	39	76554	23446	85567	14433	09013	90987	21	24		
40	40	9.76572	10.23428	9.85594	10.14406	10.09022	9.90978	20	20		
44	41	76590	23410	85620	14380	09031	90969	19	16		
48	42	76607	23393	85647	14353	09040	90960	18	12		
52	43	76625	23375	85674	14326	09049	90951	17	8		
56	44	76642	23358	85700	14300	09058	90942	16	4		
23	45	9.76660	10.23340 23323	9.85727	10.14273	10.09067	9,90933	15	37		
8	46 47	76677 76695	23305	85754 85780	$14246 \\ 14220$	$09076 \\ 09085$	90924 90915	14 13	$\begin{bmatrix} 56 \\ 52 \end{bmatrix}$		
12	48	76712	23288	85807	14193	09094	90906	12	48		
16	49	76730	23270	85834	14166	09104	90896	11	44		
20	50	9.76747	10.23253	9.85860	10.14140	10.09113	9.90887	10	40		
24	51	76765	23235	85887	14113	09122	90878	9	36		
28	52	76782	23218	85913	14087	09131	90869	8	32		
32	53	76800	23200	85940	14060	09140	90860	7	28		
36	54	76817	23183	85967	14033	09149	90851	6	24		
40	55	9.76835	10.23165	9.85993	10.14007	10.09158	9.90842	5	20		
44	56	76852	23148	86020	13980	09168	90832	4	16		
48	57	76870	23130	86046	13954	09177	90823	3	12		
52 56	58 59	76887 76904	23113	86073	13927	09186	90814	2	8		
24	60	76922	23096 23078	86100 86126	13900 13874	09195 09204	90805 90796	1 0	4 36		
M.S.		Cosine.		Cotangent		Cosecant,	Sine.	M	M.S.		
8h	125) .	Docart.	оомивени	Tangent.	Coscoant. 1		54°	3h		
	120							OI	U		

									1
	36°			Logar	ithms.		1	.43°	9ь
M.S.	M	Sine.	Cosecant.	Tangent.	Cotangent.	Secant.	Cosine.	M	M.S.
24	0	9.76922	10.23078	9.86126	10.13874	10.09204	9.90796	60	36
8	1 2	76939	23061	86153	13847	09213	90787	59	56
12	3	76957 76974	23043	86179	13821	09223	90777	58	52
16	4	76991	23026 23009	86206 86232	13794 13768	$09232 \\ 09241$	90768	57	48
20	5	9.77009	10.22991	9.86259	10.13741	10.09250	90759	56 55	40
24	6	77026	22974	86285	13715	09259	90741	54	36
28	7	77043	22957	86312	13688	09269	90731	53	32
32	8	77061	22939	86338	13662	09278	90722	52	28
36	9	77078	22922	86365	13635	09287	90713	51	24
40	10	9.77095	10.22905	9.86392	10.13608	10.09296	9.90704	50	20
44	11	77112	22888	86418	13582	09306	90694	49	16
48 52	12 13	77130 77147	22870 22853	86445	13555	09315	90685	48	12
56	14	77164	22836	86471 86498	13529 13502	09324 09333	90676 90667	47 46	8 4
25	15	9.77181	10.22819	9.86524	10.13476	10.09343	9.90657	45	35
4	16	77199	22801	86551	13449	09352	90648	44	56
.8	17	77216	22784	86577	13423	09361	90639	43	52
12	18	77233	22767	86603	13397	09370	90630	42	48
16	19	77250	22750	86630	13370	09380	90620	41	44
20	20	9.77268	10.22732	9.86656	10.13344	10.09389	9.90611	40	40
24	21	77285 77302	22715	86683	13317	09398	90602	39	36
28 32	22 23	77319	22698 22681	86709 86736	13291 13264	09408 09417	90592 90583	38	32 28
36	24	77336	22664	86762	13238	09426	90574	36	24
40	25	9.77353	10.22647	9.86789	10.13211	10.09435	9.90565	35	20
44	26	77370	22630	86815	13185	09445	90555	34	16
48	27	77387	22613	86842	13158	09454	90546	33	12
52	28	77405	22595	86868	13132	09463	90537	32	8
56	29	77422	22578	86894	13106	09473	90527	31	4
26	30	9.77439	10.22561	9.86921	10.13079	10.09482	9.90518	30	34
4 8	31 32	77456 77473	$22544 \\ 22527$	869 4 7 869 7 4	13053 -13026	$09491 \\ 09501$	90509 90499	29 28	56 52
12	33	77490	22510	87000	13000	09510	90490	27	48
16	34	77507	22493	87027	12973	09520	90480	26	44
20	35	9.77524	10.22476	9.87053	10.12947	10.09529	9.90471	25	40
24	36	77541	22459	87079	12921	09538	90462	24	36
28	37	77558	22442	87106	12894	09548	90452	23	32
32	38	77575	22425	87132	12868	09557	90443	22	28
36	39 40	77592	22408	87158	12842	09566	90434	21 20	24 20
40 44	41	9.77609 77626	$\begin{array}{c} 10.22391 \\ 22374 \end{array}$	9.87185 87211	$10.12815 \\ 12789$	09576 09585	9.90424 90415	19	16
48	42	77643	22357	87238	12762	09595	90405	18	12
52	43	77660	22340	87264	12736	09604	90396	17	8
56	44	77677	22323	87290	12710	09614	90386	16	4
27	45	9.77694	10.22306	9.87317	10.12683	10.09623	9.90377	15	33
4	46	77711	22289	87343	12657	09632	90368	14	56
8	47	77728	$22272 \\ 22256$	87369 \$7306	12631	09642	90358 90349	13 12	52
12 16	48	77744 77761	$\begin{array}{c} 22230 \\ 22239 \end{array}$	87396 87422	$12604 \\ 12578$	09651 09661	90349	11	48 44
20	50	9.77778	10.22222	9.87448	10.12552	10.09670	9,90330	10	40
24	51	77795	22205	87475	12525	09680	90320	9	36
28	52	77812	22188	87501	12499	09689	90311	8	32
32	53	77829	22171	87527	12473	09699	90301	7	28
36	54	77846	22154	87554	12446	09708	90292	6	24
40	55	9.77862	10.22138	9.87580	10.12420	10.09718	9.90282	5	20
44 48	56 57	77879	22121 22104	87606 87633	$12394 \\ 12367$	$09727 \\ 09737$	90273 90263	3	16 12
52	58	77896 77913	2210+	87659	12367	09746	90254	$\begin{bmatrix} 3 \\ 2 \end{bmatrix}$	8
56	59	77930	22070	87685	12315	09756	90244	1	4
28	60	77946	22054	87711	12289	09765	90235	0	32
M.S.	M	Cosine.	Secant.	Cotangent	Tangent.	Cosecant.	Sine.	M	M.S.
8h	126°)						53°	3h

2h													
M.S.	M	Sine.	Cosecant.	Tangent.	Cotangent.	Secant.	Cosine.	M	M.S.				
28	0	9.77946	10.22054	9.87711	10.12289	10.09765	9.90235	60	3:2				
4	1	77963	22037	87738	12262	09775	90225	59	56				
8	2	77980	22020	87764	12236	09784	90216	58	52				
12	3	77997	22003	87790	12210	09794	90206	57	48				
16	4	78013	21987	87817	12183	09803	90197	56	44				
20	5 6	9.78030 78047	10.21970 21953	9.878 43 87869	10.12157 12131	10.09813 09822	9.90187 90178	55 54	36				
24 28	7	78063	21937	87895	12105	09832	90168	53	32				
32	8	78080	21920	87922	12078	09841	90159	52	28				
36	9	78097	21903	87948	12052	09851	90149	51	24				
40	10	9.78113	10.21887	9.87974	10.12026	10.09861	9.90139	50	20				
44	11	78130	21870	88000	12000	09870	90130	49	16				
48	12	78147	21853	88027	11973	09880	90120	48	12				
52	13	78163	21837	88053	11947	09889	90111	47	8				
56	14	78180	21820	88079	11921	09899	90101	46	4				
29	15	9.78197	10.21803 21787	9.88105	10.11895	10.09909 09918	9.90091 90082	45 44	31 56				
4 8	16 17	78213 78230	21770	88131 88158	11869 11842	09918	90032	43	52				
12	18	78246	21754	88184	11816	09937	90063	42	48				
16	19	78263	21737	88210	11790	09947	90053	41	44				
20	20	9.78280	10.21720	9.88236	10.11764	10.09957	9.90043	40	40				
24	21	78296	21704	88262	11738	09966	90034	39	36				
28	22	78313	21687	88289	11711	09976	90024	38	32				
32	23	78329	21671	88315	11685	09986	90014	37	28				
36	24	78346	21654	88341	11659	09995	90005	36	24				
40 44	$\begin{vmatrix} 25 \\ 26 \end{vmatrix}$	9.78362 78379	10.21638 21621	9.88367 88393	10.11633	10.10005	9.89995 89985	35 34	20				
48	20 27	78395	21621	88420	11607 11580	$10015 \\ 10024$	89976	33	12				
52	28	78412	21588	88446	11554	10024	89966	32	8				
56	29	78428	21572	88472	11528	10044	89956	31	1				
30	30	9.78445	10.21555	9.88498	10.11502	10.10053	9.89947	30	30				
4	31	78461	21539	88524	11476	10063	89937	29	56				
8	32	78478	21522	88550	11450	10073	89927	28	52				
12	33	78494	21506	88577	11423	10082	89918	27	48				
$\begin{array}{c c} 16 \\ 20 \end{array}$	34 35	78510 9.78527	21490 10.21473	88603 9.88629	11397 10.11371	$\begin{array}{c} 10092 \\ 10.10102 \end{array}$	89908 9. 89898	26 25	44				
$\frac{20}{24}$	36	78543	21457	88655	11345	10.10102	89888	24	40 36				
28	37	78560	21440	88681	11319	10121	89879	23	32				
32	38	78576	21424	88707	11293	10131	89869	22	28				
36	39	78592	21408	88733	11267	10141	89859	21	24				
40	40	9.78609	10.21391	9.88759	10.11241	10.10151	9.89849	20	20				
44	41	78625	21375	88780	11214	10160	89810	19	16				
48	42	78642	21358	88812	11188	10170	89830	18	12				
52 56	43 44	$78658 \\ 78674$	$ \begin{array}{c c} 21342 \\ 21326 \end{array} $	88838 88864	11162 11136	10180 10090	89820 89810	17 16	8 4				
31	45	9.78691	10.21309	9.88890	10.11110	10.10199	9.89801	15	29				
4	46	78707	21293	88916	11084	10209	89791	14	56				
8	47	78723	21277	88942	11058	10219	89781	13	52				
12	48	78739	21261	88968	11032	10229	89771	12	48				
16	49	78756	21244	88994	11006	10239	89761	11	44				
20	50	9.78772	10.21228	9.89020	10.10980	10.10248	9.89752	10	40				
24 28	51 52	78788 - 78805	$21212 \\ 21195$	89046	10954	10258 10 2 68	89742	9	36				
$\frac{20}{32}$	53	78821	21195	89073 89099	10927 10901	10208	89732 89722	8 7	$\begin{vmatrix} 32 \\ 28 \end{vmatrix}$				
36	54	78837	21163	89125	10875	10288	89712	6	24				
40	55	9.78853	10.21147	9.89151	10.10849	10.10298	9.89702	5	20				
44	56	78869	21131	89177	10823	10307	89693	4	16				
48	57	78886	21114	89203	10797	10317	89683	3	12				
52	58	78902	21098	89229	10771	10327	89673	2	8				
56	59	78918	21082	89255	10745	10337	89663	1	4				
32 M. S.	60 M	78934 Cosino	21066	89281	10719	10347	89653	0	28				
M. S.1	127°	Cosine.	Secant.	Cotangent	Tangent.	Cosecant.	Sine.	52°	M.S.				
0	121							02	0				

<u> </u>	LOCARTIUMS TAIGONOMETRIC, 201										
2h	170 garrennes.										
M.S.	M	Sine.	Cosecant.	Tangent.	Cotangent.	Secant.	Cosine.	M	M.S.		
32	0	9.78934	10.21066	9.89281	10.10719	10.10347	9.89653	60	28		
4	1	78950	21050	89307	• 10693	10357	89643	59	56		
8	2	78967	21033	89333	10667	10367	89633	58	52		
12	3	78983	21017	89359	10641	10376	89624	57	48		
16 20	4	78999 9.79015	21001 10.20985	89385	10615	10386	89614	56	44		
24	5 6	79031	20969	9.89411 89437	10.10589 10563	10.10396 10406	9.89604	55	40 36		
28	7	79047	20953	89463	10503	10406	89594 89584	54 53	32		
32	8	79063	20937	89489	10511	10416	89574	52	28		
36	9	79079	20921	89515	10485	10436	89564	51	24		
40	10	9.79095	10.20905	9.89541	10.10459	10.10446	9.89554	50	20		
44	11	79111	20889	89567	10433	10456	89544	49	16		
48	12	79128	20872	89593	10407	10466	89534	48	12		
52	13	79144	20856	89619	10381	10476	89524	47	8		
56	14	79160	20840	89645	10355	10486	89514	46	4		
33	15	9.79176	10.20824	9.89671	10.10329	10.10496	9.89504	45	27		
4	16	79192	26808	89697	10303	10505	89495	44	56		
.8	17	79208	20792 20776	89723	10277	10515	89485	43	52		
16	18 19	79224 79240	20760	89749 89775	$10251 \\ 10225$	$10525 \\ 10535$	89 47 5 89 4 65	42 41	48 44		
20	20	9.79256	10.29744	9.89801	10.10199	10.10545	9.89455	40	40		
24	$\frac{20}{21}$	79272	20728	89827	10.10199	10.10545	89445	39	36		
28	22	79288	20712	89853	10147	10565	89435	38	32		
32	23	79304	20696	89879	10121	10575	89425	37	28		
36	24	79319	20681	89905	10095	10585	89415	36	24		
40	25	9.79335	10.20665	9.89931	10.10069	10.10595	9.89405	35	20		
44	26	79351	20649	89957	10043	10605	89395	34	16		
48	27	79367	20633	89983	10017	10615	89385	33	12		
52	28	79383	20617	90009	09991	10625	89375	32	8		
56	29	79399	20601	90035	09965	10636	89364	31.	4		
34	30	9.79415	10.20585	9.90061	10.09939	10.10646	9.89354	30	26		
4 8	31 32	79431 79447	20569 20553	90086 90112	09914	10656	89344 893 34	29 28	56 52		
12	33	79463	20537	90138	09888 09862	10666 10676	89324	27	48		
16	34	79478	20522	90164	09836	10686	89314	26	44		
20	35	9.79494	10.20506	9.90190	10.09810	10.10696	9.89304	25	40		
24	36	79510	20490	90216	09784	10706	89294	24	36		
28	37	79526	20474	90242	09758	10716	89284	23	32		
32	38	79542	20458	90268	09732	10726	89274	22	28		
36	39	79558	20442	90294	09706	10736	89264	21	24		
4()	40	9.79573	10.20427	9.90320	10.09680	10.10746	9.89254	20	20		
44	41	79589	20411	90346	09654	10756	89244	19	16		
48	42	79605	20395	90371	09629	10767	89233	18	12		
52 56	43 44	79621 79636	20379 20364	90397 90423	09603 09577	10777 10787	89223 89213	17 16	8 4		
35	45	9.79652	10.20348	9.90449	10.09551	10.10797	9 89203	15	25		
4	46	79668	20332	90475	09525	10.10197	89193	14	56		
8	47	79684	20316	90501	09499	10817	89183	13	52		
12	48	79699	20301	90527	09473	10827	89173	12	48		
16	49	79715	20285	90553	09447	10838	89162	11	44		
20	50	9.79731	10.20269	9.90578	10.09422	10.10848	9.89152	10	40		
24	51	79746	20254	90604	09396	10858	89142	9	36		
28	52	79762	20238	90630	09370	10868	89132	8	32		
32	53	79778	20222	90656	09344	10878	89122	7	28		
36	54	79793	20207	90682	09318	10888	89112	6	24		
40	55	9.79809	10.20191 20175	9.90708 90734	10.09292 09266	10.10899 10909	9.89101 89091	5 4	$\begin{vmatrix} 20 \\ 16 \end{vmatrix}$		
44	56 57	79825 79840	20175	90759	09241	10909	89091	3	12		
52	58	79856	20100	90785	09215	10919	89071	2	8		
56	59	79872	20144	90811	09189	10940	89060	ī	4		
36	60	79857	20113	90837	09163	10950	89050	0	24		
M.S.	M	Cosine.	Secant.	Cotangent	Tangent.	Cosecant.	Sine.		M. S.		
	128							51°	3h		
-											

202	LOGARITHMS TRIGONOMETRIC.									
Oh	000							7 400	9h	
2 ^b	39°			Logar	rithms.			140°	19"	
M.S.	M	Sine.	Cosecant.	Tangent.	Cotangent.	Secant.	Cosine.	M	M.S.	
36	0	9.79887	10.20113	9.90837	10.09163	10.10950	9.89050	60	24	
4	1	79903	20097	90863	09137	10960	89040	59	56 52	
8 12	2	79918 79934	20082 20066	90889 90914	09111 09086	10970 10980	89030 89020	58 57	48	
16	3 4	79950	20050	90940	09060	10991	89009	56	44	
20	5	9.79965	10,20035	9.90966	10.09034	10.11001	9.88999	55	40	
24	6	79981	20019	90992	09008	11011	88989	54	36	
28	7	79996	20004	91018	08982	11022	88978	53	32	
32	8	80012	19988	91043	08957	11032	88968	52	28	
36	9	80027	19973 10,19957	91069 9.91095	08931	11042 10.11052	88958 9.88948	51 50	24 20	
40	10 11	9.80043 80058	19942	91121	10.08905	11063	88937	49	16	
48	12	80074	19926	91147	08853	11073	88927	48	12	
52	13	80089	19911	91172	08828	11083	88917	47	8	
56	14	80105	19895	91198	08802	11094	88906	46	4	
37	15	9.80120	10.19880	9.91224	10.08776	10.11104	9.88896	45	23	
4	16	80136	19864	91250	08750	11114	88886	44	56	
8 12	17	80151 80166	19849 19834	91276 91301	08724 08699	11125 11135	88875 88865	43 42	52 48	
16	18 19	80182	19818	91327	08673	11145	88855	41	44	
20	20	9.80197	10.19803	9.91353	10.08647	10.11156	9.88844	40	40	
24	21	80213	19787	91379	08621	11166	88834	39	36	
28	22	80228	19772	91404	08596	11176	88824	38	32	
32	23	80244	19756	91430	08570	11187	88813	37	28	
36	24	80259	19741	91456	08544	11197 10.11207	88803	36	24 20	
40 44	25 26	9.80274 80290	10.19726 19710	9.91482 91507	10.08518 08493	10.11207	9.88793 88782	35 34	16	
48	27	80305	19695	91533	08467	11228	88772	33	12	
52	28	80320	19680	91559	08441	11239	88761	32	8	
56	29	80336	19664	91585	08415	11249	88751	31	4	
38	30	9.80351	10.19649	9.91610	10.08390	10.11259	9.88741	30	23	
4	31	80366	19634	91636	08364	11270	88730	29	56	
8 12	32 33	80382 80397	19618 19603	91662 91688	$08338 \\ 08312$	11280 11291	88720 88709	28 27	52 48	
16	34	8041 2	19588	91713	08287	11301	88699	$\frac{26}{26}$	44	
20	35	9.80428	10.19572	9.91739	10.08261	10.11312	9.88688	25	40	
24	36	80443	19557	91765	08235	11322	88678	24	36	
28	37	80458	19542	91791	08209	11332	88668	23	32	
32	38	80473	19527	91816	08184	11343	88657	22	28	
36	39	80489	19511 10.19496	91842	08158	11353	88647	21	24 20	
40 44	40	9.80504 80519	10.19496 19481	9.91868 91893	10.08132 08107	10 1136 1 11374	9.88636 88626	20 19	16	
48	42	80534	19466	91919	08081	11374	88615	18	12	
52	43	80550	19450	91945	08055	11395	88605	17	8	
56	44	80565	19435	91971	08029	11406	88594	16	4	
39	45	9.80580	10.19420	9.91996	10.08004	10.11416	9 88584	15	21	
4	46	80595	19405	92022	07978	11427	88573	14	56	
8 12	47 48	80610 80625	$\begin{array}{c} 19390 \\ 19375 \end{array}$	92048 92073	$07952 \\ 07927$	11437 11448	88563 88552	13 12	52 48	
16	49	80641	19359	92099	07901	11458	88542	11	44	
20	50	9.80656	10.19344	9.92125	10.07875	10.11469	9.88531	10	40	
24	51	80671	19329	92150	07850	11479	88521	9	36	
28	52	80686	19314	92176	07824	11490	88510	.8	32	
32	53	80701	19299	92202	07798	11501	88499	7	28	
36 40	54 55	80716	19284	92227 9.92253	07773	$\begin{array}{c c} 11511 \\ 10.11522 \end{array}$	88489	6	24 20	
44	56	9.80731 80746	$10.19269 \mid 19254$	9.92253	$\begin{array}{c} 10.07747 \\ 07721 \end{array}$	10.11522	9.88478 88468	5 4	16 l	
48	57	80762	19238	92304	07696	11543	88457	3	12	
52	58	80777	19223	92330	07670	11553	88447	2	8	
56	59	80792	19208	92356	07644	11564	88436	1	4	
40	60	80807	19193	92381	07619	11575	88425	0	20	
M.S.	100	Cosine.	Secant.	Cotangent	Tangent.	Cosecant.	Sine.		M.S.	
0"	129							50°	3h	

	LOGARITHMS TRIGONOMETRIC. 203									
2h	40°			Taman	i 4 la mari		1	.39°	9h	
	10				ithms.					
M.S.	M	Sine.	Cosecant.	Tangent.	Cotangent.	Secant.	Cosine.	M	M.S.	
40	0	9.80807	10.19193	9.92381	10.07619	10.11575	9.88425	60	20	
4	1	80822	19178	92407	07593	11585	88415	59	56	
8 12	$\begin{vmatrix} 2 \\ 3 \end{vmatrix}$	80837	19163	92433	07567	11596	88404	58	52	
16	4	80852 50867	19148 19133	92458 92484	07542 07516	11606 11617	88394	57 56	48	
20	5	9.80882	10.19118	9.92510	10.07490	10.11628	88383 9.88372	55	40	
24	6	80897	19103	92535	07465	11638	88362	54	36	
28	7	80912	19088	92561	07439	11649	88351	53	32	
32	8	80927	19073	92587	07413	11660	88340	52	28	
36	9	80942	19058	92612	07388	11670	88330	51	24	
40	10	9.80957	10.19043	9.92638	10.07362	10.11681	9.88319	50	20	
44	11	80972	19028	92663	07337	11692	88308	49	16	
48	12	80987	19013	92689	07311	11702	88298	48	12	
52	13	81002	18998	92715	07285	11713	88287	47	8	
56	14	81017 9.81032	18983 10.18968	92740 9.92766	07260 10.07234	11724	88276	46	14 19	
4	15 16	9.81052 810 4 7	18953	92792	07208	10.11734 11745	9.88266 88255	45 44	56	
8	17	81061	18939	92817	07183	11756	88244	43	52	
12	18	81076	18924	92843	07157	11766	88234	42	48	
16	19	81091	18909	92868	07132	11777	88223	41	44	
20	20	9.81106	10.18894	9.92894	10.07106	10.11788	9.88212	40	40	
24	21	81121	18879	92920	07080	11799	88201	39	36	
28	22	81136	18864	92945	07055	11809	88191	38	32	
32	23	81151	18849	92971	07029	11820	881.80	37	28	
36	24	81166	18834	92996	. 07004	11831	88169	36	24	
40	25	9.81180	10.18820	9.93022	10.06978	10.11842	9.88158	35	20	
44	26	81195	18805	93048	06952	11852	88148	34	16	
48 52	27	81210	18790	93073	06927	11863	88137	33 32	12 8	
56	28 29	81225 81240	18775 18760	93099 93124	$06901 \\ 06876$	11874 11885	88126 88115	31	. 8	
42	30	9.81254	10.18746	9.93150	10.06850	10.11895	9.88105	30	18	
4	31	81269	18731	93175	06825	11906	88094	29	56	
8	32	81284	18716	93201	06799	11917	88083	28	52	
12	33	81299	18701	93227	06773	11928	88072	27	48	
16	34	81314	18686	93252	06748	11939	88061	26	44	
20	35	9.81328	10.18672	9.93278	10.06722	10.11949	9.88051	25	40	
24	36	81343	18657	93303	06697	11960	88040	24	36	
28	37	81358	18642	93329	06671	11971	88029	23	32	
32	38	81372	18628	93354	06646	11982	88018	22 21	28 24	
36 40	39 40	\$1387 9.81402	18613 10.18598	93380 9.93406	$06620 \\ 10.06594$	11993 10.12004	88007 9.87996	20	20	
44	41	81417	18583	93431	06569	10.12004 12015	87985	19	16	
48	42	81431	18569	93457	06543	$\frac{12015}{12025}$	87975	18	12	
52	43	81446	18554	93482	06518	12036	87964	17	8	
56	44	81461	18539	93508	06492	12047	87953	16	4	
43	45	9.81475	10.18525	9.93533	10.06467	10.12058	9.87942	15	17	
4	46	81490	18510	93559	06441	12069	87931	14	56	
8	47	81505	18495	93584	06416	12080	87920	13	52	
12	48	81519	18481	93610	06390	12091	87909	12	48	
16	49	81534	18466	93636	06364	12102 10.12113	87898 9.87887	11 10	44 40	
20 24	50 51	9.81549 81563	10.18451 18437	9.93661 93687	10.06339 06313	10.12113	9.87887	9	36	
28	52	81578	$\frac{18437}{18422}$	93712	06288	12123	87866	8	32	
32	53	81592	18408	93738	06262	12145	87855	7	28	
36	54	81607	18393	93763	06237	12156	87844	6	24	
40	55	9.81622	10.18378	9.93789	10.06211	10.12167	9.87833	5	20	
44	56	81636	18364	93814	06186	12178	87822	4	16	
48	57	81651	18349	93840	06160	12189	87811	3	12	
52	58	81665	18335	93865	06135	12200	87800	2	8	
56	59	81680	18320	93891	06109	12211	87789	1	4	
44	60	81694	18306	93916	06084	12222	87778	0	16	
M.S.	M 1	Cosine.	Secant.	Cotangent	Tangent.	Cosecant.	Sine.	49°	M.S. 3h	
8h	1309							19	9,,	

204	LOGARITHMS TRIGONOMETRIC.										
2h	41°			Logar	ithms.		1	38°	9h		
M.S.	M	Sine.	Cosccant.	Tangent.	Cotangent.	Secant.	Cosine.	M	M.S.		
44	0	9.81694	10.18306	9.93916	10.06084	10.12222	9.87778	60	16		
+	ĭ	81709	18291	93942	06058	12233	87767	59	56		
8	2	81723	18277	93967	06033	12244	87756	58	52		
12	3	81738	18262	93993	06007	12255	87745	57	48		
16	4	81752	18248	94018	05982	12266	87734	56	44		
20	5	9.81767	10.18233	9.94044	10.05956	10.12277	9.87723	55	40		
24	6	81781	18219	94069	05931	12288	87712	54	36		
28	7	81796	18204	94095	05905	12299	87701	53	32		
32	8	81810	18190	94120	05880	12310	87690	52	28		
36	9	81825	18175	94146	05854	12321	87679	51	24		
40	10	9.81839	10.18161	9.94171	10.05829	10.12332	9.87668	50	20		
44	11	81854	18146	94197	. 05803	12343	87657	49	16		
48	12	81868	18132	94222	05778	12354	87646	48	12		
52	13	81882	18118	94248	05572	12365	87635	47	8		
56	14	°81897	18103	94273	05727	12376	87624	46	4		
45	15	9.81911	10.18089	9.94299	10.05701	10.12387	9.87613	45	15		
4	16	81926	18074	94324	05676	12399	87601	44	56		
8	17	81940	18060	94350	05650	12410	87590	43	52		
12	18	81955	18045	94375	05625	12421	87579	42	48		
16	19	81969	18031	94401	05599	12432	87568	41	44		
20	20	9.81983	10.18017	9.94426	10.05574	10.12443	9.87557	40	40		
24	21	81998	18002	94452	05548	12454	87546	39	36		
28	22	82012	17988	94477	05523	12465	87535	38	32		
32	23	82026	17974	94503	05497	12476	87524	37	28		
36	24	82041	17959	94528	05472	12487	87513	36	24		
40	25	9.82055	10.17945	9.94554	10.05446	10.12499	9.87501	35	20		
44	26	82069	17931	94579	05421	12510	87490	34. 33	16 12		
48	27	82084	17916	94604	05396	12521	87479	32			
52.	28	82098	17902	94630	05370	$\begin{array}{c} 12532 \\ 12543 \end{array}$	87468 87457	31	8		
56	29	82112	17888	94655	05345 10,05319	10.12554	9.87446	30	14		
46	30	9.82126	10.17874	9.94681	05294	10.12554 12566	87434	29	56		
4	31	82141	17859	$94706 \\ 94732$	05268	$\frac{12500}{12577}$	87423	28	52		
8	32	82155	17845	94757	05243	12588	87412	27	48		
12	33	$82169 \\ 82184$	17831 17816.	94783	05217	12599	87401	26	44		
16	34	9.82198	10.17802	9.94808	10.05192	10.12610	9.87390	25	40		
20	35	82212	17788	94834	05166	12622	87378	24	36		
24 28	36 37	82226	17774	94859	05141	12633	87367	23	32		
	38	82240	17760	94884	05116	12644	87356	22	28		
32 36	39	82255	17745	94910	05090	12655	87345	21	24		
40	40	9.82269	10.17731	9.94935	10.05065	10.12666	9.87334	20	20		
44	41	82283	17717	94961	05039	12678	87322	19	16		
48	42	82297	17703	94986	05014	12689	87311	18	12		
52	43	82311	17689	95012	04988	12700	87300	17	8		
56	44	82326	17674	95037	04963	12712	87288	16	4		
47	45	9.82340	10.17660	9.95062	10.04938	10.12723	9.87277	15	13		
4	46	8235 ±	17646	95088	04912	12734	87266	14	56		
8	47	82368	17632	95113	04887	12745	87255	13	52		
12	48	82382	17618	95139	04861	12757	87243	12	48		
16	49	82396	17604	95164	04836	12768	87232	11	44		
20	50	9.82410	10.17590	9.95190	10.04810	10.12779	9.87221	10	40		
24	51	82424	17576	95215	04785	12791	87209	9	36		
28	52	82439	17561	95240	04760	12802	87198	8	32		
32	53	82453	17547	95266	04734	12813	87187	7	28		
36	54	82467	17533	95291	04709	12825	87175	6	24		
40	55	9.82481	10.17519	9.95317	10.04683	10.12836	9.87164	5	20		
44	56	82495	17505	95342	04658	12847	87153	4	16		
48	57	82509	17491	95368	04632	12859	87141	3	12		
52	58	`82523	17477	95393	04607	12870	87130	2	8		
56	59	82537	17463	95418	04582	12881	87119	1	4		
48	60	82551	17449	95444	04556	12893	87107	0	12		
M.S.	M	Cosine.	Secant.	Cotangent	Tangent.	Cosecant.	Sine.	M	M.S.		
8h	131							48°	3h		

			240 011						
2 ^h	42°			Logari	ithms.		1	37°	9h
M.S.	M	Sine.	Cosecant.	Tangent.	Cotangent.	Secant.	Cosine.	M	M.S.
48	0	9.82551	10.17449	9.95444	10.04556	10.12893	9.87107	60	12
4	1	82565	17435	95469	04531	$12904 \\ 12915$	87096	59	56 52
8 12	$\begin{bmatrix} 2 \\ 3 \end{bmatrix}$	82579 82593	$17421 \\ 17407$	95495 95520	04505 04480	$\frac{12915}{12927}$	87085 87073	58 57	48
16	4	82607	17393	95545	04455	12938	87062	56	44
20	5	9.82621	10.17379	9.95571	10.04429	10.12950	9.87050	55	40
24	6	82635	17365	95596	04404	12961	87039	54	36
28	7	82649	17351	95622	04378	12972	87028	53	32
32	8	82663	17337	95647	04353	12984	87016	52	28
36	9	82677	17323	95672	$\begin{array}{c c} 04328 \\ 10.04302 \end{array}$	12995 10.13007	87005 9,86393	51 50	24 20
40	10 11	9.82691 82705	$\begin{array}{c} 10.17309 \\ 17295 \end{array}$	9,95698 95723	04277	13018	86982	49	16
48	12	82719	17281	95748	04252	13030	86970	48	12
52	13	82733	17267	95774	04226	13041	86959	47	8
56	14	82747	17253	95799	04201	13053	86947	46	4
49	15	9.82761	10.17239	9.95825	10.04175	10.13064	9,86936	45	11
4	16	82775	17225	95850	04150	13076	86924	44	56 52
8 12	17	82788 82802	17212 17198	95875 95901	$04125 \\ 04099$	13087 13098	86913 86902	43 42	48
16	18 19	82816	17184	95926	04074	13110	86890	41	44
20	20	9.82830	10.17170	9.95952	10.04048	10.13121	9.86879	40	40
24	21	82844	17156	95977	04023	13133	86867	39	36
28	22	82858	17142	96002	03998	13145	86855	38	32
32	23	82872	17128	96028	03972	13156	86844	37	28
36	24	82885	17115	96053	03947 10.03922	13168 10.13179	86832 9.86821	36 35	24 20
40	25 26	9,82899 82913	10.17101 17087	9.96078 96104	03896	13191	86809	34	16
44 48	27	82927	17073	96129	03871	13202	86798	33	12
52	28	82941	17059	96155	03845	13214	86786	32	8
56	29	82955	17045	96180	03820	13225	86775	31	4
50	30	9.82968	10.17032	9.96205	10.03795	10.13237	9.86763	30	10
4	31	82982	17018	96231	03769	13248	86752	29 28	56 52
8	32	82996	17004	$96256 \\ 96281$	03744 03719	$13260 \\ 13272$	86740 86728	27	48
12 16	33 34	\$3010 83023	16990 16977	96307	03693	13283	86717	26	44
20	35	9.83037	10.16963	9,96332	10.03668	10.13295	9.86705	25	40
24	36	83051	16949	96357	03643	13306	86694	24	36
28	37	83065	16935	96383	03617	13318	86682	23	32
32	38	83078	16922	96408	03592	13330	86670	22	28
36	39	83092	16908	96433	03567	13341 10.13353	86659	21	24 20
40	40	9.83106 83120	10.16894 16880	9.96459 96484	10.03541 03516	13365	9.86647	20 19	16
44 48	41 42	83133	16867	96510	03490	13376	86624	18	12
52	43	83147	16853	96535	03465	13388	86612	17	8
56	44	83161	16839	96560	03440	13400	86600	16	4
51	45	9.83174	10.16826	9.96586	10.03414	10.13411	9.86589	15	9
4	46	83188	16812	96611	03389 03364	13423· 13435	86577 86565	14	56 52
8	47	83202 83215	16798 16785	96636 96662	03338	13446	86554	12	48
12 16	48 49	83219	16771	96687	03313	13458	86542	11	44
20	50	9.83242	10.16758	9.96712	10,03288	10.13470	9.86530	10	40
24	51	83256	16744	96738	03262	13482	86518	9	36
28	52	83270	16730	96763	03237	13493	86507	8	32
32	53	83283	16717	96788	03212	13505	86495	7	28
36	54	83297	16703	96814 9.96839	03186	13517 10.13528	86483 9.86472	6 5	24 20
44	55 56	9.83310 83324	10.16690 16676	9.96559	()3136	13540	86460	4	16
48	57	83338	16662	96890	03110	13552	86448	3	12
52	58	83351	16649	96915	03085	13564	86436	2	8
56	59	83365	16635	96940	03060	13575	86425	1	4
52	60	83378	16622	96966	03034	13587	86413	0	8
M.S.	M	Cosine.	Secant.	Cotangent	Tangent.	Cosecant.	Sine.	M 470	M.S.
8h	132							47°	3h
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1	Oh	400			_			1	36°	9ь	
	2h	43°			Logar	ithms.		1	.00		
	M.S.	M	Sine.	Cosecant.	Taugent.	Cotangent.	Secant.	Cosine.	M	M.S	
	52	0	9.83378	10.16622	9.96966	10.03034	10.13587	9.86413	60	8	
-	+	1,	83392	10608	96991	03009	13599	86401	59	56	
1	8	2	83405	16595	97016	02984	13611	86389	58	52	
	12	3	83419	16581	97042	02958	13623	86377	57 56	48	
1	16	4	83432	16568	97067	02933	13634	86366 9.86354	55	40	
	20	5	9.83446	10.16554	9.97092 97118	10.02908 02882	10.13646 13658	86342	54	36	
	24	6	83 4 59 83 4 73	$16541 \\ 16527$	97143	02852 02857	13670	86330	53	32	
	$\begin{array}{c} 28 \\ 32 \end{array}$	7 8	83486	$\begin{array}{c} 16521 \\ 16514 \end{array}$	97168	02832	13682	86318	52	28	
	36	9	83500	16500	97193	02807	13694	86306	51	24	
	40	10	9.83513	10.16487	9.97219	10.02781	10.13705	9.86295	50	20	
	44	11	83527	16473	97244	02756.	13717	86283	49	16	
-	48	12	83540	16460	97269	02731	13729	86271	48	12	
	52	13	83554	16446	97295	02705	13741	86259	47	8	
	56	14	83567	16433	97320	02680	13753	86247	46	4	
	53	15	9.83581	10.16419	9.97345	10.02655	10.13765	9.86235	45 44	56	
1	4	16	83594	16406	97371	02629	$13777 \\ 13789$	$86223 \\ 86211$	43	52	
	8	17	83608	$16392 \\ 16379$	97396 97421	$02604 \\ 02579$	13800	86200	42	48	
j	12 16	18 19	$83621 \\ 83634$	16366	97447	02553	13812	86188	41	44	
1	20	20	9.83648	10.16352	9.97472	10.02528	10.13824	9.86176	40	40	
	24	21	83661	16339	97497	02503	13836	86164	39	36	
	28	22	83674	16326	97523	02477	13848	86152	38	32	
	$\overline{32}$	23	83688	16312	97548	02452	13860	86140	37	28	
	36	24	83701	16299	97573	02427	13872	86128	36	24	
	40	25	9.83715	10.16285	9.97598	10.02402	10.13884	9.86116	35	20	
-	44	26	83728	16272	97624	02376	13896	86104	34 33	16 12	
	48	27	83741	16259	97649	02351	13908 13920	86092 86080	32	8	
	52	28	83755 83768	$16245 \\ 16232$	97674 97700	$02326 \ 02300$	13932	86068	31	4	
	56 54	29 30	9.83781	10.16219	9.97725	10.02275	10.13944	9.86056	30	6	
	4	31	83795	16205	97750	02250	13956	86044	29	56	
	8	32	83808	16192	97776	02224	13968	86032	28	52	
	12	33	83821	16179	97801	02199	13980	86020	27	48	
	16	34	83834	16166	97826	02174	13992	86008	26	44	
	20	35	9.83848	10.16152	9.97851	10.02149	10.14004	9.85996	25	40	
	24	36	83861	16139	97877	02123	14016	85984	24	$\begin{bmatrix} 36 \\ 32 \end{bmatrix}$	
ł	28	37	83874	16126	$97902 \\ 97927$	$02098 \\ 02073$	14028	85972 85960	$\begin{array}{c c} 23 \\ 22 \end{array}$	28	
	32	38	83887 83901	16113 16099	97953	$02075 \\ 02047$	$14040 \\ 14052$	85948	21	24	
ı	36 40	39 40	9.83914	10.16086	9.97978	10.02022	10.14064	9.85936	20	20	
	44	41	83927	16073	98003	01997	14076	85924	19	16	
	48	42	83940	16060	98029	01971	14088	85912	18	12	
	52	43	83954	16046	98054	01946	14100	85900	17	8	
	56	44	83967	16033	98079	01921	14112	85888	16	4	
	55	45	9.83980	10.16020	9.98104	10.01896	10.14124	9.85876	15	5	
	4	46	83993	16007	98130	01870	14136	85864	14 13	56 52	
	8	47	84006	15994	98155	$01845 \\ 01820$	$14149 \\ 14161$	85851 85839	12	48	
1	12 16	48 49	84020 84033	15980 15967	$98180 \\ 98206$	01794	14173	85827	11	44	
	20	50	9.84046	10.15954	9.98231	10.01769	10.14185	9.85815	10	40	
	24	51	84059	15941	98256	01744	14197	85803	9	36	
	28	52	84072	15928	98281	01719	14209	85791	8	32	
	32	53	84085	15915	98307	01693	14221	85779	7	28	
	36	54	84098	15902	98332	01668	14234	85766	6	24	
	40	55	9.84112	10.15888	9.98357	10.01643	10.14246	9.85754	5	20	
	44	56	84125	15875	98383	01617	14258	85742	4	16	
	48	57	84138	15862	98408	$01592 \\ 01567$	$14270 \\ 14282$	85 73 0 85 7 18	$\frac{3}{2}$	12 8	
	52 56	58 59	84151 84164	15849 15836	98433 98458	01507	14204	85706	ī	4	
	56	60	84177	15823	98484	01516	14307	85693	ō	4	
	M.S.	M	Cosine.	Secant.	Cotangent		Cosecant.	Sine.	M	M.S.	
	8h	133				3			46°	3h	
		,200									

M.S. M	LOGARITHMS IRIGONOMETRIC.										201
N.S. M Sine. Cosecant. Tangent. Cotangent. Secant. Cosine. M M.S. Secant. Secant. Secant. Cosine. M M.S. Secant. Secant. Secant. Secant. M M.S. Secant. Secant. M M.S. Secant. Secant. M M.S. Secant. Secant. M M.S. Secant. Secant. Secant. M M.S. Secant. M M Secant. M Secant. M M Secant. M Secant. M Secant. M M Secant.		01	110							10~0	105
56 0 0 9.81477 10.15820 9.98484 10.01516 10.14307 9.85030 0 4 8 2 84203 15797 98509 01461 14310 85663 56 55 12 3 84216 15784 98500 01440 14343 85663 58 52 20 5 9.81242 10.16758 9.9850 10.01330 10.14308 985625 56 44 24 6 84255 15713 98661 10.339 14392 85605 53 32 28 8 4282 15718 98666 01331 1494 85906 52 28 36 9 84295 15705 98711 01299 14417 85581 124 40 10 984308 10.15692 998737 10.1023 104429 985671 50 22 8 48 12 48334 156692 98787 0123 14453 85547 48 12 44444 144538 85547 48	1	2	44			Logar	ithms.		-	130	9"
4 1 8 4190 1 58109 1 58109 1 58109 1 58109 1 58109 58009 -1491 1 4319 85668 59 56 8 52 84266 1 5797 98304 0 1466 1 4331 85669 68 52 1 5717 98509 0 1440 1 4331 85669 68 52 1 5717 98509 0 1440 1 4331 85667 67 48 1 5717 98509 0 1440 1 4333 85667 67 48 1 20 5 9 84242 1 0 115735 9.8810 1 0 10390 1 14353 85625 56 44 2 5 84269 1 5713 98660 0 1339 1 4392 83608 3 32 2 8 84282 1 5718 98660 0 1314 1 444 85596 62 28 3 32 3 84261 1 5070 98737 1 0 10290 1 4417 85583 1 24 4 0 10 9.84295 1 5705 98737 1 0 10230 1 4417 85583 1 24 4 10 1 4417 85582 4 4 11 8 4341 1 5663 98812 0 1188 1 4466 85674	į	M.S.	M		Cosecant.	Tangent.	Cotangeut.	Secant.	Cosine.	M	M.S.
S	1	56	0	9.84177	10.15823	9.98484			9.85693	60	4
12	-										
16	ı										
24	ı				15784						
28 7 84265 16746 98635 01363 11398 85608 53 32 32 8 81282 16718 9866 01343 11392 85608 53 32 40 10 9.84308 10.15692 9.98737 10.1023 114447 85583 51 24 41 11 84321 15679 9.98737 10.1023 11444 85550 49 16 56 14 84334 15653 98812 01188 14466 85534 47 8 56 14 81360 15640 98838 01162 14478 85522 40 4 56 9.84373 10.15627 9.9883 10.01137 10.1499 9.85510 45 3 4 16 9.84437 10.5563 9.9898 01061 14527 86473 42 48 12 18 84411 15579 9.9904 01061 14527 <td></td>											
28 7 84209 15731 98661 01339 14392 83608 53 32 23 36 9 84295 15718 98661 01314 14404 85506 52 28 36 9 84295 15718 98656 01314 14404 85506 52 28 340 10 10 9.84308 10.15692 9.98737 10.01263 10.14429 9.85571 50 20 44 11 84321 15679 98762 01238 14441 85559 49 16 84334 15666 98787 01213 14453 85547 48 12 84334 15666 98787 01213 14453 85547 48 12 84334 15666 98787 01213 14453 85547 48 12 84334 15666 98787 01213 14453 85547 48 12 84349 10.15627 9.98863 10.1162 14478 85522 46 4 16 84385 15615 98888 01112 14503 85497 44 56 8517 84398 15602 98913 01087 14515 85494 44 15576 98946 01036 14567 85473 42 48 16 19 84424 15576 98946 01036 14564 85400 41 44 20 20 9.84487 10.15623 9.98989 01061 14527 85473 42 48 16 19 84424 15576 99015 0.0985 14564 85400 15560 99015 0.0985 14564 85400 15560 99015 0.0985 14564 85400 15560 99015 0.0985 14564 85430 39 36 24 84489 15511 99090 0.0910 14601 85390 36 24 84489 15511 99090 0.0910 14601 85390 36 24 84489 15511 99090 0.0910 14601 85390 36 24 84489 15511 99090 0.0910 14601 85390 36 24 84489 15511 99090 0.0910 14601 85390 36 24 84489 15511 99090 0.0910 14601 85390 36 24 84489 15511 99090 0.0910 14601 85390 36 24 84489 15511 99090 0.0910 14601 85390 36 24 8489 15511 990	I		_								
36 9 84295 15706 98711 01289 14417 85583 51 24 40 10 9.84508 10.15692 9.98737 10.01263 10.14429 9.85571 50 20 44 11 84321 15670 98762 01238 14411 85559 49 16 48 12 84334 15666 98787 01213 14453 85547 48 12 52 13 84347 15663 98812 01188 14466 85634 47 8 556 14 84330 15640 98838 01162 14478 85522 46 4 57 15 9.84373 10.15627 9.98863 10.01137 10.14490 9.85510 45 3 4 16 84385 15615 98888 01112 14503 85407 44 56 8 17 84398 15602 98913 01087 14515 85425 44 56 19 84424 15576 98964 01036 14570 85473 42 48 10 19 84424 15576 98964 01036 14500 85400 41 44 20 20 9.84437 10.15663 99015 0.0985 14569 8640 41 44 22 21 84450 15550 99016 0.0985 14569 8641 30 30 22 23 84476 15554 99005 00935 14589 85411 37 28 36 24 84489 15511 99090 00910 14601 85399 36 24 44 26 84515 15485 99141 00859 14626 85374 34 16 48 27 84528 15472 99166 00834 14639 85361 31 2 28 8450 10400 9910 00809 14661 85399 36 24 48 27 84528 15472 99166 00834 14639 85361 32 2 8 8450 10400 9910 00809 14661 85399 36 24 48 27 84528 15472 99166 00834 14639 85361 32 2 8 8450 15630 15449 99217 00783 14663 8537 31 4 8 32 8 8450 15630 9914 00809 14661 85399 36 24 4 26 84515 15485 99141 00859 14626 85377 34 16 8 32 8 8450 15630 9914 00806 14577 85423 38 32 23 8 8466 15586 99141 00859 14626 85377 34 16 8 32 8 8450 15630 15434 99207 00783 14683 85312 29 56 24 8 8458 15511 99207 00783 14683 85312 29 56 25 8 8450 15600 9918 00808 14713 85257 27 48 26 8451 15488 99293 00707 14701 85299 28 52 27 84630 10.15370 999368 10.0063 14768 85250 22 28 40 40 9.8499 15531 99444 00656 14775 8525 22 28 40 40 40 9.8494 10.15366 99938 00631 14768 85257 27 48 40 40 9.8499 1510 9972 00278 14918 85250 22 2 8 40 40 40 9.8499 1510 9972 00278 14918 85087 11 48 20 50 9.84880 15131 9949 00606 14750 8825 20 2 2 2 44 44 84 84720 15280 99645 00456 14855 8515 14 56 44 84745 15256 99596 00404 14856 8527 27 48 47 84784 1526 99664 00354 14888 85112 13 522 25 84898 1510 99090 00910 16001 16001 84999 41 66 49 84809 15101 99722 00278 14918 85087 11 44 56 84898 15102 99899 00001 15001 15001 84999 41 66 60 60 84949 15	ı										
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44 11 84921 15679 98762 01238 14441 885557 50 20 164 17 84921 15679 98762 01238 14441 885559 48 12 84334 15663 98812 01188 14466 85634 47 8 12 84347 15653 98812 01188 14466 85634 47 8 12 8 12 8 12 8 12 8 12 8 12 8 12 8 1			_		15705	98711					
48 12 84334 15666 98787 01213 14463 85547 48 18 56 14 84360 15640 98838 01162 14478 85524 46 4 57 15 9.84373 10.15627 9.88863 110.1137 10.14490 9.85510 45 4 4 16 84398 15602 98913 01087 14515 85485 43 56 12 18 84411 15556 98989 9990 01061 14527 85473 42 48 10 19 84424 15576 98964 01036 14549 95460 41 44 24 21 84450 15550 99040 00960 14561 85486 39 36 28 22 84463 15537 99040 00960 14651 85399 36 44 26 8531 36 29 85452 14549 </td <td>1</td> <td></td> <td></td> <td></td> <td>10.15692</td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td>	1				10.15692						
56 14 843437 15663 98812 01188 14466 85344 74 8 4 4 84385 15615 98883 01102 14478 85522 46 4 4 16 84385 15615 98883 01112 14503 85497 44 56 8 17 84398 15602 98913 01087 14515 85497 44 56 2 12 18 84411 15589 99939 01061 14527 85473 42 42 20 9.84437 10.15563 9.98989 10.01011 10.14552 9.85483 40 40 28 22 84463 15557 99040 0.0960 14577 85423 38 32 32 23 84476 15524 99065 0.0935 14589 85411 37 28 36 24 84456 15651 9916 0.00834 14639 85361 32 4			11					14441		49	
56 14 84360 15640 98838 01102 14478 85522 46 4 3 4 16 84383 15615 98883 10.01137 10.14490 9.85610 4 56 8 17 84398 15602 98939 01061 14515 55485 43 52 16 19 84424 15576 98964 01036 14549 85460 41 44 20 20 9.84437 10.1563 9.8989 10.01011 10.14552 85443 40 24 21 84450 15550 99016 00955 14564 85436 39 36 28 22 84463 15511 99060 00955 14564 85436 39 36 24 24 84489 15511 99090 00910 14601 85386 35 28 36 24 84502 10.1491 99086 00											
57 15 9.84373 10.15627 9.98863 10.01137 10.14400 9.85510 45 3 4 16 84385 1.5615 98888 0.0112 1.4503 85497 44 56 8 17 84398 1.5602 98913 0.0087 14515 85483 42 42 16 19 84442 1.5576 98964 0.036 14540 85473 42 42 20 20 9.84437 10.15563 9.99898 10.0101 10.14552 9.85448 40 40 28 22 84463 1.5550 99015 0.0985 14564 85436 39 36 32 23 84476 1.5524 99065 0.0935 14589 85411 37 844 40 25 9.84502 10.15498 9.9911 0.00884 10.1461 9.85386 35 20 44 26 84515 1.5485 99141 0.0689										_	
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44 26 84515 15485 99141 00859 14626 85374 34 16 52 28 84540 16460 99191 00809 14661 85349 32 8 56 29 84553 15447 99217 00783 14663 85337 31 4 58 30 9.84566 10.15434 9.99242 10.00758 10.14676 9.85324 30 2 4 31 84579 15421 99267 00733 14688 85312 29 56 8 32 84592 15408 99293 00707 14701 85299 28 52 12 33 84605 15395 99318 00682 14713 85287 27 48 20 35 9.84630 10.15370 9.99368 10.00632 10.14738 9.85260 24 36 39 84623 15318 99419 00581 14763 <td></td>											
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56 29 84553 15447 99217 00783 14663 8537 31 4 58 30 9.84566 10.15434 9.9242 10.00758 10.14676 9.85324 30 2 4 31 84579 15408 99293 00707 14701 85299 28 52 12 33 84605 15395 99318 00682 14713 85287 27 48 16 34 84618 15382 99343 00657 14726 85274 26 44 20 35 9.84630 10.15370 9.99348 10.0632 10.14738 9.85262 25 40 24 36 84643 15357 99394 00606 14750 85250 24 36 28 37 84656 15344 99419 00581 14763 85237 23 32 36 39 84682 15318 99469					15460						
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4 31 84579 15421 99267 00733 14688 85312 29 56 8 32 84502 15408 99293 00707 14701 85299 28 52 10 34 84605 15395 99318 00657 14726 85274 26 44 20 35 9.84630 10.15370 9.99368 10.00632 10.14738 9.85262 25 40 24 36 84643 15357 99394 00606 14750 85250 24 36 28 37 84666 15344 99419 00581 14763 85257 23 32 38 84669 15331 99449 00531 14788 85212 21 24 40 40 9.84094 10.15306 9.99495 10.0605 10.1800 9.85200 20 44 41 84707 15293 99520 00480 14813 <td></td>											
12 33		Ł.			15421	99267		14688	85312		
16 34 84618 15382 99343 00657 14726 85274 26 44 20 35 9.84630 10.15370 9.99368 10.00632 10.14738 9.85262 25 40 28 37 84656 15344 99419 00581 14763 85250 24 36 38 84669 15331 99444 00556 14775 85225 22 28 36 39 84682 15318 99469 00531 14788 85212 21 24 40 40 9.84694 10.15306 9.99495 10.00505 10.14800 9.85200 20 20 44 41 84707 15293 99520 00480 14813 85187 19 16 48 42 84720 15280 99545 00455 14825 85175 18 12 52 43 84733 15267 99570 00430 <td></td>											
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56 59 84936 15064 99975 00025 15039 84961 1 4 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0		52			15077	99949		15026	84974		
M.S. M. Cosine Secant, Cotangent, Tangent, Coscoant, Sine, M.M.S.		56									
M. S. M. Cosine. Secant. Cotangent. Tangent. Cosccant. Sine. M. S. 45° 3h		_									
8" 134"					Secant.	Cotangent.	Tangent.	Cosccant.	Sine.	120	31. S.
		8"	134							401	0_

EXPLANATION OF THE TABLES.

The outer columns in the trigonometrical tables contain the angle in time of hours, minutes and seconds, corresponding to the same angle in degrees and minutes in the next columns. The hour is noted at the top and bottom, the minutes in black, and the seconds in ordinary figures.

To find the Logarithm and Natural Line for Seconds exceeding Minutes of a Degree.

Example 1. Find the logarithm for sin. 38° 47′ 55″.

From table, $\begin{cases} \log \sin .38^{\circ} 48' = 9.79699 \\ " " 38^{\circ} 47' = 9.79684 \end{cases}$ diff. 15. Correction, $15 \times 55 : 60 = \frac{+14}{2}$ nearly. The required log. $\sin .38^{\circ} 47' 55'' = 9.79698$

In practice, the difference is subtracted direct from the tables. Example 2. Find the natural cos. 43° 29′ 19″.

From table, cos. $43^{\circ} 29' = 0.72557$ Correction, $20 \times 19: 60 = 6$ nearly. The required cos. $43^{\circ} 29' 19'' = 0.72551$

The correction is added when the function is increasing, and subtracted when decreasing.

To find the Angle corresponding to a given Logarithm or Natural Line.

Example 3. Log. $\sin = 9.56429$. Required the angle. From table, $\left\{ \begin{array}{ll} \log \sin & 21^{\circ} \ 31' & = 9.56440 \\ \text{``` ' ' 21^{\circ} 30'} & = 9.56408 \\ \end{array} \right\}$ diff. 32. The angle required, '' 21° 30′ 29″ = 9.56429 $\left\{ \begin{array}{ll} \text{`` ' 21.} \\ \text{`` ' 21.} \\ \text{`` Correction, 21} \times 60: 32 = 29 \text{ seconds nearly.} \\ \end{array} \right.$

Example 4. Cosine = 0.35254. Required the angle.

Conversion of Minutes and Seconds into Decimals of a Degree or of an Hour.

1	or of an Hour.												
M.	Decimal.	M.	Decimal	M.	Decimal.	s.	Decimal.	s.	Decimal.	s.	Decimal.		
1	.016666	21	.350000	41	.683333	1	.000277	21	.005833	41	.011388		
2	.033333	22	.366666	42	.700000	2	.000555	22	.006111	42	.011666		
3	.050000	23	.383333	43	.716666	3	.000833	23	.006388	43	.011944		
4	.066666	24	.400000	44	.733333	4	.001111	24	.006666	44	.012222		
5	.083333	25	.416666	45	.750000	5	.001388	25	.006944	45	.012500		
6	.100000	26	.433333	46	.766666	6	.001666	26	.007222	46	.012777		
7	.116666	27	.450000	47	.783333	7	.001944	27	.007500	47	.013055		
8	.133333	28	.466666	48	.800000	8	.002222	28	.007777	48	.013333		
9	.150000	29	.483333	49	.816666	9	.002500	29	.008055	49	.013611		
10	.166666	30	.500000	50	.833333	10	.002777	30	.008333	50	.013888		
11	.183333	31	.516000	51	.850000	11	.003055	31	.00°611	51	.014166		
12	.200000	32	.5333333	52	.866666	12	.003333	32	.008888	52	.014444		
13	.216666	33	.550000	53	.883333	13	.003611	33	.009166	53	.014722		
14	.233333	34	.566666	54	.900000	14	.003888	34	.009 144	54	.015000		
15	.250000	35	,583333	55	.916666	15	.004166	35	.009722	55	.015277		
16	266666	36	.600000	56	.9333333	16	.001411	36	.010000	56	.015555		
17	.283333	37	.616665	57	.950900	17	.001722	37	.010277	57	.015833		
18	.300000	38	.633333	58	.966666	18	.005000	38	.010555	58	.016111		
19	.316666	39	.650000	59	.983333	19	.005277	39	.010833	59	.016338		
20	.333333	40	.666666	60	1.00000	20	.005555	40	.011111	60	.016666		

Oh	0°	7	Vatura	d Trig	onom	etrical	Func	tions.	л	79°	1111
M.S.	M.			Cosec'nte		Cotang.	Secante.			M.	M.S.
0	0	.00000	1.0000	Infinite	_	Infinite	1.0000	.00000	1.0000	60	60
8	1 2	. 0029	.99971	3437.7	. 0029	3437.7	.0000	. 0000	.0000	59	56
12	3	. 0058 . 0087	. 9942	1718.9 1!45.9	. 0058	1718.9 1145.9	.0000	. 0000	.0000	58 57	52 48
16	4	. 0116	. 9884	859.44	. 0116	859.44	.0000	. 0000	.0000	56	44
20 24	5 6	.00145 $.0174$.99854	687.55	.00145	687.55	1.0000	.00000	1.0000	55	40
23	7	. 0201	. 9825	572.96 491.11	. 0174	572.96 491.11	.0000	. 0000	.0000	54 53	$\frac{36}{32}$
32	8	. 0233	. 9767	429,72	. 0233	429.72	.0000	. 0000	.0000	52	28
36	9 10	.0262	. 9738	3 ·1.97 343.77	. 0262	381.97	.0000	0000	.0000	51	24
44	11	. 0320	. 9680	312.52	.00291	343.77	1.0000 .0000	.00000	.99999	50 49	$\begin{vmatrix} 20 \\ 16 \end{vmatrix}$
48	12	. 0349	. 9651	286.48	. 0349	286 48	.0000	. 0001	. 9999	48	12
52 56	13 14	. 0378	. 9622	64.44 45.55	. 0378	64.44 45 55	.0000	. 0001	. 9999	47 46	8
1	15	.00436	.99564	229.18	.00436	229.18	.0000 1.0000	.0001	.99939	45	59
4	16	. 0465	. 9534	14.86	. 0465	14.86	.0000	. 0001	. 9999	44	56
8 12	17 18	. 0494	9505	02.22 190.99	. 0494	02.22 190.98	.0000	. 0001	. 9999	43 42	52 48
16	19	. 0553	9417	180.93	. 0553	180.93	.0000.	. 0001	. 9998	41	44
20	20	.00582	.99418	171.89	.00582	171.88	1.0000	.00002	.99998	40	40
24 28	21 22	. 0611	. 9389	63.70 56.26	. 0611	63.70 56.26	.0000	. 0002	. 9998	39 38	36 · 32
32	23	. 0669	9331	49.47	. 0669	49.46	.0000	. 0002	. 9998	37	28
36 40	24	. 0698	. 9302	43.24	. 0698	43.24	.0000	. 0002	. 9997	36	24
44	25 26	.00727	.99273	137.51 32.22	.00727	137.51 32.22	1.0000	.00003	.99997	35 34	20 16
48	27	. 0785	9215	27.32	. 0785	27.32	.0000	. 0003	. 9997	33	12
52 56	28	. 0814	. 9185	22.78	. 0814	22.77	0000.	. 0003	. 9997	32	8
2	29 30	.0843	. 9156	18.54 114.59	.0844	18 54 114.59	.0000 1.0000	.0003	.9996	31 30	58
4	31	. 0902	. 9098	10.90	. 0962	10.89	.0000	. 0004	. 9996	29	56
8 12	32 33	. 0931	9069	07.43	. 0931	07.43	.0000	. 0004	. 9996	28 27	52 48
16	31	. 0960	9040	$04.17 \\ 01.11$. 0960	04.17 01.11	.0000	. 0005	. 9995	26	44
20	35	.01018	.98982	98.223	.01018	98,218	1.0000	.00005	.99995	25	40
24 28	36 37	1047	8953	5.495	. 1047	5.489 2.908	.0000	. 0005	. 9994	2± 23	$\begin{vmatrix} 36 \\ 32 \end{vmatrix}$
32	38	. 1105	8895	2.914 0.469	. 1076 . 1105	0.463	.0000	. 0006	9994	22	28
36	39	. 1134	. 8865	88.149	. 1134	88.143	.0001	. 0006	. 9993	21	24
40	40 41	.01163	.98836	85.946 3.849	.01164	85.940 3.843	1.0001	.00007	.79993	20 19	20 16
48	42	1222	8778	1.853	. 1222	1.847	.0001	. 0007	9992	18	12
52	43	. 1251	. 8749	79.950	. 1251	79.913	.0001	. 0008	. 9992	17	8
56 3	44 45	. 1280	. 8720	78.133 76.396	. 1280	78.126 76.390	.0001	. 0008	. 9992	16 15	57
4	46	. 1338	. 8662	4.736	. 1338	4.729	.0001	. 0009	. 9991	14	56
8	47	. 1367	. 8653	3.146	. 1367	3.13.)	.0001	. 0009	. 9991	13	52
12 16	48	. 1396	8604	1.622 0.160	. 1396	0.153	.0001	. 0010	. 9990	12 11	48 44
20	50	.01454	.98546	68.757	.01454	68.750	1.0001	.00010	.99989	10	40
24 28	51 52	. 1483	. 8516	7.409	. 1484	7.402	.0001	. 0011	. 9989	9	36
32	53	. 1512	. 8487	6.113 4.866	. 1513	6.105 4.858	.0001	. 0011	. 9988	8 7	32 28
36	54	. 1571	. 8429	3.664	. 1571	3.657	.0001	. 0012	. 9988	6	24
40 44	55 56	.01600	.98400	62.507 1.391	.01600	62.499 1.383	1.0001	.00013	.99987	5 4	20 16
48	57	. 1658	8342	0.314	. 1629 . 1658	0.306	.0001	. 0013	. 9987 . 9987	3	12
12	58	. 1657	. 8313	59.274	. 1687	59.286	.0001	. 0014	. 9986	2	8
56	59	. 1716	8284	8.270 7.299	. 1716	8 261 7.290	.0001	. 0015	. 9985	1 0	4 56
M.S.	M.	Cosine.		Secante.	Cotang.	Tangent.	Cosec'nt	Vrs.Cos.	Sine.	M.	M.S.
6h	90°				Nati	ural.				89°	5h
_											

1	NATURAL DINES.												
3												1	
ı	()h	10		Natura	1 Trig	onom	etrical	Func	tions.	1	78°	11h	
ļ				1 1	100		l a .		True Olive	Cogina	M	M.S.	
	M.S	M			Cosec'nte		Cotang.				60	56	
	生	0	.01745	.98255	57.299	.01745	57.290	1.0001	.00015	.99985	59	56	
1	4	$\begin{bmatrix} 1 \\ 2 \end{bmatrix}$. 1774	. 8226	56.359	. 1775	56.350	.0001	. 0016	. 9984	58	52	
	8	3	. 1803	. 8196	55.450	. 1804	55.441	.0002	. 0016	. 9984	57	48	
	12	4	. 1832	. 8167	54.570	. 1833	54.561	.0002	. 0017	. 9983	56	44	
ļ	16 20	5	. 1861	. 8139	53.718	. 1862	53 708	.0002	. 0017	.99382	55	40	
1	24	6	.01891	.98109	52.891	.01891	52.882	1.0002 .0002	.00018	. 9981	54	36	
]	28	7	. 1920	. 8080	2.090 1.313	. 1920 . 1949	2.081 1.303	.0002	. 0019	. 9981	53	32	
	32	8	. 1949	. 8051	0,558	. 1948	0.548	.0002	. 0019	. 9980	52	28	
	36	9	. 1978	. 8022 . 7993	49.826	2007	49.816	.0002	. 0020	. 9980	51	24	
	40	10	.02036	.97964	49.114	.02036	49.104	1.0002	.00021	.99979	50	20	
	41	11	. 2065	. 7935	8.422	2066	8.412	.0002	. 0021	. 9979	49	16	
	48	12	2094	7906	7.750	2095	7.739	.0002	. 0022	. 9978	48	12	
	52	13	. 2123	7877	7.096	. 2124	7.085	.0002	. 0022	. 9977	47	8	
	56	14	. 2152	7847	6.460	2153	6.449	.0002	. 0023	. 9977	46	4	
	5	15	.02181	.97818	45.840	.02182	45.829	1.0002	.00024	.99976	4.5	55	
	4	16	. 2210	. 7789	5.237	. 2211	5.226	.0002	. 0024	. 9975	44	56	
	- 8	17	. 2240	. 7760	4.650	. 2240	4.638	.0002	. 0025	. 9975	43	52	
	12	18	. 2269	7731	4.077	. 2269	4.066	.0002	. 0026	. 9974	42	48	
	16	19	. 2298	7702	3.520	. 2298	3.508	.0003	. 0026	. 9974	41	44	
	20	20	.02327	.97673	42.976	.02327	42.964	1.0003	.00027	.99973	40	40	
	24	21	. 2356	. 7644	2.445	. 2357	2.433	.0003	. 0028	. 9972	39	36	
	28	22	. 2385	. 7615	1.928	. 2386	1.916	.0003	. 0028	. 9971	38	32	
	32	23	. 2414	. 7586	1.423	. 2415	1.410	.0003	. 0029	. 9971	37	28	
	36	24	. 2443	 7557	0.930	. 2444	0.917	.0003	. 0030	. 9970	36	24	
	40	25	.02472	.97528	40.448	.02473	40.436	1.0003	.00030	.99969	35	20	
	44	26	. 2501	. 7499	39.978	. 2502	39.965	.0003	. 0031	. 9969	34	16	
	48	27	. 2530	. 7469	9.518	. 2531	9.506	.0003	. 0032	. 9968	33 32	12 8	
	52	28 29	. 2559	. 7440	9.069	. 2560	9.057	.0003	. 0033	. 9967	31	4	
	56 6	30	. 2589	. 7411	8.631	. 2589	8.618 38.188	.0003 1.0003	.00034	.99966	30	54	
	4	31	.02618	.97382	38.201 7.782	.02618	7.769	.0003	. 0035	. 9965	29	56	
	8	32	. 2676	7353	7.371	. 2677	7.358	.0003	. 0036	9964	28	52	
	12	33	2705	7295	6.969	2706	6.956	.0004	. 0036	. 9963	27	48	
	18	34	2734	7266	6.576	2735	6.563	.0004	. 0037	. 9963	26	44	
	20	35	.02763	.97237	36.191	.02764	36.177	1.0004	.00038	.99962	25	40	
	24	36	2792	7208	5.814	2793	5.800	.0004	. 0039	. 9961	24	36	
	28	37	. 2821	7179	5.445	. 2822	5.431	.0004	. 0040	. 9960	23	32	
	32	38	. 2850	. 7150	5.084	. 2851	5.069	.0004	. 0041	. 9959	22	28	
	36	39	. 2879	. 7121	4.729	. 2880	4.715	.0004	. 0041	. 9958	21	24	
	40	40	.02908	.97091	34.382	.02910		1.0004	.00042	.99958	20	20	
	44	41	. 2937	. 7062	-4.042	. 2939	4.027	.0004	. 0043	. 9957	19	16	
	48	42	. 2967	7033	3.708	. 2968	3.693	.0004	. 0041	. 9956	18	12	
	52	43	. 2996	. 7004	3.381	. 2997	3.366	.0004	. 0045	. 9955	17	8	
	56	44	. 3025	. 6975	3.060	. 3026	3.045	.0004	. 0046	. 9954	16	4	
	7	45	.03054	.96946	32.745	.03055	32.730	1.0005	.00046	.99953	15	53	
	4	46	. 3083	. 9692	2.437	. 3084	2.421	.0005	. 0047	. 9952 . 9951	14 13	56 52	
	8	47 48	. 3112	. 6888	2.134	3113	2.118	.0005	0048	. 9951	12	48	
	12 16	49	. 3141	6859	1.836 1.544	. 3143	$1.820 \\ 1.528$.0005	. 0049	. 9950	11	44	
	20	50	.03199		31.257	.03201	31.241	1.0005	.00051	.99949	10	40	
	24	51	. 3228	.96801	0.976	. 3230	0.960	.0005	. 0052	. 9948	9	36	
	28	52	. 3257	6743	0.699	3259	0.683	.0005	. 0053	. 9917	8	32	
	32	53	. 3286	6713	0.033	3288	0.411	.0005	. 0054	. 9946	7	28	
	36	54	. 3315	6684	0.161	3317	0.145	.0005	. 0055	. 9945	6	24	
	40	55	.03344	.96655	29.899	.03346	29.882	1.0005	.00056	.99944	5	20	
	41	56	. 3374	. 6626	9.641	. 3375	9.624	.0006	. 0057	. 9943	4	16	
	48	57	. 3403	. 6597	9.388	. 3405	9.371	.0006	. 0058	. 9942	3	12	
	52	58	. 3432	. 6568	9.139	. 3434	9.122	.0006	. 0059	. 9941	2	8	
	56	59	. 3461	. 6539	8.894	. 3463	8.877	.0006	. 0060	. 9940	1	4	
	8	60	3490	. 6510	8.654	3492	8.636	.0006	. 0061	9939	0	52	
	M.S.	M	Cosine.	Vrs.Sin-	Secante.			Cosec'nt	vrs. Cos	Sine.	M	M.S. 5h	
	6h	91°				Na	tural.				88°	0.	

Í	$0^{\rm h}$	20		NT - 4	J 7851		4 3	-	4.	1	770	11h
	M. S.	M	Sine.		Cosec nte		Cotang.			Cosine.		M.S.
1	8	0	.03490	.96510	28 654	.03492	28 636	1.0006	Vrs.Sin .00061	.99939	M 60	52
١	4	1	. 3519	. 6481	8.417	. 3521	8.399	.0006	. 0062	. 9938	59	56
	8 12	$\begin{vmatrix} 2 \\ 3 \end{vmatrix}$. 3548	. 6452	8.184	. 3550	8.166	.0006	. 0063	. 9937	58	52
	16	4	. 3606	. 6423	7.955 7.730	3579	7.937 7.712	.0006	. 0064	9936	57 56	48
1	20	5	.03635	.96365	27.508	.03638	27.490	1.0007	.00066	.99934	55	40
ł	24 28	6 7	. 3661	. 6336	7.290	. 3667	7.271	.0007	. 0067	. 9933	54	36
ł	32	8	. 3693	6306	7.075	. 3696	7.056	.0007	. 0068	. 9932	53	32
	36	9	. 3751	6277	6.864 6 655	. 3725	6.845	.0007	. 0069	9931	52 51	2S 24
1	40	10	.03781	.96219	26.450	.03783	26.432	1.0007	.00071	.99928	50	20
1	41 48	$\begin{array}{ c c }\hline 11\\12\\ \end{array}$. 3810	. 6190	6 249	. 3812	6.230	.0007	. 0073	. 9927	49	16
1	52	13	. 3839	6161 6132	6.050 5.854	. 3842	6.031	.0007	. 0074	. 9926	48	12
i	55	14	. 3897	6103	5.661	. 3871	5.835 5.642	.0007	. 0075	. 9925	47 46	8 4
	9	15	.03926	.96074	25.471	.03929	25.452	1.0008	.00077	.99923	45	51
Ì	4.	16	. 3955	. 6045	5.284	. 3958	5.264	.0008	. 0078	. 9922	44	56
-	8 12	17 18	. 3984	6016	5.100	. 3987	5.080	.0008	. 0079	. 9921	43	52
	16	19	4042	5987 . 5958	4.918 4.739	. 4016	4.898 4.718	.0008	0.0080	. 9919	42 41	48
	20	20	.04071	.95929	24.562	.04075	24.542	1.0008	.00083	.99917	40	40
	24	21	. 4100	. 5900	4.388	. 4104	4.367	.0008	. 0084	. 9916	39	36
	28 32	22 23	. 4129	5870	4.216	. 4133	4.196	.0008	. 0085	. 9915	38	$\begin{bmatrix} 32 \\ 28 \end{bmatrix}$
ı	36	24	4187	. 5812	4.047 3.880	. 4102	4.026 3.859	.0009	. 0086	. 9913	37 36	24
ı	40	25	.04217	.95783	23.716	.04220	23.694	1.0009	.00089	.99911	35	20
ł	44	26	. 4246	. 5754	353	. 4249	3.532	.0009	. 0090	. 9910	34	16
	48 52	27 28	4275	. 5725	3.393	. 4279	3.372	.0009	. 0091	. 9908	33	12
	56	29	4333	.5696	3.235 3.079	. 4308 . 4337	3.214 3.058	.0009	. 0093	. 9907	32 31	8 4
	10	30	.04362	.95638	22.925	.04366	22.904	1.0009	.00095	.99905	30	50
	4	31	. 4391	. 5609	2.774	. 4395	2.752	.0010	. 0096	. 9903	29	56
1	8 12	32 33	. 4420	. 5580	2.624	. 4424	2.602	.0010	. 0098	. 9902	28	52
	16	34	. 4449	5551 5522	2.476 2.330	. 4453 . 4483	2.454 2.308	.0010	. 0099	. 9901	27 26	48 44
	20	35	.04507	.95493	22.186	.04512	22.164	1.0010	.00102	.99898	25	40
	24	36	. 4536	. 5464	2.044	. 4541	2.022	.0010	. 0103	. 9897	24	36
1	28 32	37 38	. 4565	. 5435	1.904	4570	1.881	.0010	0104	. 9896	23 22	32 28
	36	39	. 4623	5405	$1.765 \\ 1.629$. 4599 . 4628	1.742 1.606	.0010	. 0106 . 0107	. 9894	21	24
	40	40	.04652	.95347	21.494	.04657	21.470		.00108	.99892	20	20
1	44	41	. 4681	. 5318	1.360	. 4687	1.337	.0011	. 0110	. 9890	19	16
1	48 52	42 43	4711 . 4740	5289	1.228 1.098	. 4716	1.205 1.075	.0011	. 0111 . 0112	. 9889	18	12 8
	56	44	4769	5231	0.970	. 4774	0.946	.0011	. 0114	. 9886	16	4
	11	45	.04798	.95202	20.843	.04803	20.819	1.0011	.00115	.99885	15	49
	4	46	4827	. 5173	0.717	4832	0.693	.0012	. 0116	. 9883	14	56
	8 12	47 48	. 4856 . 4885	5144	$0.593 \\ 0.471$. 4862 . 4891	$0.569 \\ 0.446$	0.0012	. 0118	. 9882	13 12	52 48
	16	49	. 4914	5086	0.350	. 4920	0.325	.0012	. 0113	. 9879	11	44
	20	50	.04943	.95057	20.230	.04949	20.205	1.0012	.00122	.99878	10	40
	24	51	. 4972	. 5028	0.112	. 4978	0.087	.0012	. 0124	. 9876	9	36
	28 32	52 53	. 5001	$\begin{array}{ c c c c c c c c c c c c c c c c c c c$	19.995 9.880	. 5007 . 5037	$ \begin{array}{c c} 19.970 \\ 9.854 \end{array} $.0012	$\begin{bmatrix} . & 0125 \\ . & 0127 \end{bmatrix}$. 9875 . 9873	8 7	32 28
	36	54	. 5059	. 4941	9.766	. 5066	9.710	.0013	. 0128	. 9872	6	24
	4()	55	.05088	.94912	19.653	.05095	19.627	1.0013	.00129	.99870	5	20
1	44 48	56	. 5117	. 4883	9.541	. 5124	9.515	.0013	. 0131	9869	4 3	16
1	52 52	58	. 5146	. 4853 . 4824	$9.431 \\ 9.322$. 5153	$ \begin{array}{c c} 9.405 \\ 9.296 \end{array} $.0013	. 0132	. 9867 . 9866	$\frac{3}{2}$	12 8
1	56	59	5204	. 4795	9.214	5212	9.188	.0013	. 0135	. 9864	ī	4
-	12	60	. 5234	. 4766	9.107	. 5241	9.081	.0014	. 0137	. 9863	0	48
	M.S. 6h	м 92°	Cosine.	vrs.Sin.	Secante.			Cosec'nt	Vrs. Cos	Sine.	87°	M.S. 5h
-	0-	04				Na	tural.				01	0-

ı,						MICHA	THE TAIL OF					
	Θ^{h}	, 3 °		Natur	al Trig	gonom	etrical	l Func	ctions		176°	111h
-	M. S.	M	Sine.	Vrs.Cos.	Cosec'nte	Tang.	Cotang	Secante	Vrs. Sin	Cosine	. M	M.S.
	1.3	0	.05234	.94766	19.107	.05241		1.0014	.00137	.99863		48
	4	1	. 5263	4737	9.002	. 5270		.0014	0138	9861	59	56
	8	2	. 5292	. 4708	8.897	. 5299	8.871	.0014	. 0140	9860		52
	12	3	. 5321	. 4679	8.794	. 5328	8.768	.0014		. 9858		48
	16	4	. 5350	. 4650	8.692	. 5357	8.665	.0014	. 0143	. 9857		44
	20	5	.05379	.94621	18.591	.05387	18.564	1.0014	.00145	.99855		40
1	24 28	6 7	. 5408	. 4592	8.491	. 5416	8.464	.0015	. 0146	. 9854		36
	32	8	5437	4563	8.393	. 5445	8.365	.0015	. 0148	. 9852	53 52	32 28
	36	9	. 5466	4534	8.295 8.198	5502	8.268 8.171	.0015	0149	9850		24
1	40	10	.05524	. 4505	18.103	.05532	18.075	1.0015	.00153	.99847	50	20
i	41	11	. 5553	. 4447	8.008	. 5562	7.980	.0015	. 0154	. 9846	49	16
	48	12	5582	. 4418	7.914	5591	7.886	.0016	. 0156	. 9844	48	12
1	52	13	. 5611	. 4389	7.821	. 5620	7.793	.0016	. 0157	. 9842	47	8
	56	14	. 5640	. 4360	7.730	. 5649	7.701	.0016	. 0159	. 9841	46	4
	13	15	.05669	.94331	17.639	.05678	17.610	1.0016	.00161	.99839	45	47
1	4	16	. £698	. 4302	7.549	. 5707	7.520	.0016	. 0162	. 9837	44	56
1	8	17 18	. 5727	. 4273	7.460	. 5737	7.431	.0016	. 0164	. 9836	43	52
	12 16	19	5756	. 4244	7.372	. 5766	7.343	.0017	. 0166	. 9834	42	48
	20	20	. 5785	. 4214	7.285 17.198	. 5795	7.256 17.169	.0017 1.0017	.0167	. 9832	41 40	44 40
	24	21	. 5843	.94185	7.113	. 5853	7.084	.0017	. 0171	. 9829	39	36
1	28	22	. 5872	. 4127	7.028	. 5883	6.999	.0017	. 0172	. 9827	38	32
	32	23	5902	4098	6.944	. 5912	6.915	.0017	. 0174	. 9826	37	28
	36	24	. 5931	4069	6.861	. 5941	6.832	.0018	. 0176	. 9824	36	24
	40	25	.05960	.94040	16.779	.05970	16.750	1.0018	.00178	.99822	35	20
1	44	26	. 5989	. 4011	6.698	. 5999	6.668	.0018	. 0179	. 9820	34	16
	48	27	. 6018	. 3982	6.617	. 6029	6.587	.0018	. 0181	. 9819	33	12
H	52	28	. 6047	. 3953	6.538	. 6058	6.507	.0018	. 0183	. 9817	32	8
	56 14	29 30	. 6076	3924	6.459	. 6087	6.428	.0018	. 0185	. \$315	31	4
1	4	31	.06105	.93895	16.380 6.303	.06116	$16.350 \\ 6.272$	1.0019 .0019	.00186	.99813	30 29	46 56
	8	32	6163	3837	6.226	6175	6.195	.0019	. 0190	. 9810	28	52
	12	33	6192	. 3808	6.150	6204	6.119	.0019	. 0192	. 9808	27	48
	16	34	. 6221	. 3777	6.075	. 6233	6.043	.0019	. 0194	. 9806	26	44
	20	35	.06250	.93750	16.000	.06262	15.969	1.0019	.00195	.99804	25	40
	24	36	. 6279	. 3721	5.926	. 6291	5.894	.0020	. 0197	. 9803	24	36
	28	37	. 6308	. 3692	5.853	. 6321	5.821	.0020	. 0199	. 9801	23	32
	32	38	. 6337	. 3663	5.780	. 6350	5.748	.0020	. 0201	. 9799	22	28
	36 40	39 40	. 6366	. 3634 .93605	5.708	. 6379	5.676	.0020	$0203 \ 00205$. 9797	21 20	24 20
	44	41	. 6424	. 3576	15.637 5.566	. 6437	15.605 5.534	1.0020 .0021	. 0206	. 9793	19	16
	48	42	6453	. 3547	5.496	6467	5.464	.0021	. 0208	9791	18	12
	52	43	. 6482	. 3518	5.427	6496	5.394	.0021	. 0210	. 9790	17	8
	56	44	. 6511	. 3489	5.358	. 6525	5.325	.0021	. 0212	. 9788	16	4
1	15	45	.06540	.93460	15.290	.06554	15.257	1.0021	.00214	.99786	15	45
	4	46	. 6569	. 3431	4.222	. 6583	5.189	.0022	. 0216	. 9784	14	5.6
	8	47	. 6598	. 3402	5.155	. 6613	5.122	.0022	. 0218	. 9782	13	52
1	12	48	. 6627	3373	5.089	. 6642	5.056	.0022	. 0220	. 9780	12	48
	16 20	49 50	. 6656 .06685	. 3343 .93314	5.023	. 6671	4.930	.0022	00224	9778	11	44
	24	51	. 6714	. 3285	14.958 4.893	.06700	14.924 4.860	1.0022 .0023	.00224	.99776	10 9	40 36
	28	52	6743	3256	4.829	6759	4.795	.0023	. 0228	9772	8	32
	32	53	6772	3227	4.765	6788	4.732	.0023	. 0230	. 9770	7	28
	36	54	. 6801	. 3198	4.702	. 6817	4.668	.0023	. 0231	. 9768	6	24
	40	55	.06830	.93169	14.640	.06846	14.606	1.0023	.00233	.99766	5	20
	44	56	. 6859	. 3140	4.578	. 6876	4.544	.0024	. 0235	. 9764	4	16
	48	57	. 6888	. 3111	4.517	. 6905	4.482	.0024	. 0237	9762	3	12
1	52	58	. 6918	. 3082	4.456	. 6934	4.421	.0024	. 0239	9760	2	8
	56 16	59 60	. 6947	3053	4.395	6963	4.361	.0024	. 0241	9758	1	4
	I.S.!	M		. 3024 Vrs. Sin.	4.335 Secante.	. 6993 Cotang.	4.301 Tangent.	.0024	. 0243 Vrs. Cos	. 9756 Sine.		44 M.S.
	$6^{\widetilde{\rm h}}$	93°			.,	Natu		30000 1101		D.110.	860	
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1												
	0h	40		Natura	d Trig	onom	etrical	Func	tions.	1	.75°	11h
1	M.S	M	Sine.	Vrs.Cos.	Cosce'nte	Tang.	Cotang.	Secante.	Vrs. Sin	Cosine.	M	M.S.
	16	0	.06976	.93024	1 4.335	.06993	14.301	1.0024	.00243	.99756	60	44
1	4	1	. 7005	. 2995	4.276	. 7022	4.241	.0025	. 0246	. 9754	59	56
	8	2 3	. 7034	. 2966	4.217	. 7051	4.182	.0025	. 0248	. 9752	58	52
	12 16	4	. 7063	. 2937	4.159	. 7080	4.123	.0025	. 0250	. 9750	57	48
1	20	5	. 7092	. 2908	4.101 14.043	. 7110	4.065	.0025	. 0252	. 9748	56	144
	24	6	. 7150	.92879	3.986	.07139	14.008 3.951	1.0025 .0026	.00254	.99746	55 54	40 36
ı	28	7	7179	2821	3.930	7197	3.894	.0026	. 0258	9742	53	32
1	32	8	7208	2792	3.874	7226	3.838	.0026	. 0260	9740	52	28
	36	9	. 7237	2763	3.818	. 7256	3.782	.0026	. 0262	. 9738	51	24
	40	10	.07-66	.92734	13.763	.07285	13.727	1.0026	.00264	.99736	50	20
	41	11	. 7295	. 2705	3.708	. 7314	3.672	.0027	. 0266	. 9733	49	16
	48	12	. 7324	. 2676	3.654	. 7343	3.617	.0027	. 0268	. 9731	48	12
Į	52	13	. 7353	. 2647	3.600	. 7373	3.563	.0027	. 0271	. 9729	47	8
	56 17	14 15	. 7382	. 2618	3.547	. 7402	3.510	.0027	. 0273	. 9727	46	4
ı	4	16	.07411	.92589	13.494 3.441	.07431	13.457 3.404	1.0027 $.0028$.00275	.99725	45 44	43 56
ı	8	17	7469	2531	3.389	7490	3.351	.0028	. 0279	. 9721	43	52
ı	12	18	7498	2502	3.337	7519	3.299	.0028	. 0281	. 9718	42	48
ı	16	19	. 7527	. 2473	3.286	. 7548	3.248	.0028	. 0284	. 9716	41	44
	20	20	.07556	.92444	13.235	.07577	13.197	1.0029	.00286	.99714	40	40
	24	21	. 7585	. 2415	3.184	. 7607	3.146	.0029	. 0288	. 9712	39	36
	28	22	. 7614	. 2386	3.134	. 7636	3.096	.0029	. 0290	. 9710	38	32
	32	23	. 7643	. 2357	3.084	. 7665	3.046	.0029	. 0292	. 9707	37	28
	36	24 25	. 7672	. 2328	3.034 12.985	. 7694	2.996 12.947	.0029	. 0295	. 9705	36	24
	40 44	26	. 7730	.92293	$\frac{12.985}{2.937}$. 7753	$\frac{12.9 \pm 1}{2.898}$	1,0030 .0030	.00297	.99703	35 34	20 16
	48	27	7759	2241	2.888	7782	2.849	.0030	. 0301	. 9698	33	12
ı	52	28	. 7788	2212	2.840	. 7812	2.801	.0030	. 0304	. 9696	32	8
ı	56	29	. 7817	. 2183	2.793	. 7841	2.754	.0031	. 0306	. 9694	31	4
ı	18	30	.07846	.92154	12.745	.07870	12.706	1.0031	.00308	.99692	30	42
ı	4	31	. 7875	. 2125	2.698	. 7899	2.659	.0031	. 0310	. 9689	29	56
	8	32	. 7904	. 2096	2.652	. 7929	2.612	.0031	. 0313	. 9687	28	52
ı	12	33	. 7933	. 2067	2.606	. 7958	2.566	.0032	. 0315	. 9685	27	48
	16 20	31	. 7962	. 2038	$2.560 \\ 12.514$. 7987 .08016	2.520 12.474	.0032 1.0032	.0317	. 9682	25 25	44 40
	24	36	. 8020	. 1980	2.469	. 8046	2.429	.0032	. 0322	. 9678	24	36
	28	37	. 8049	. 1951	2.424	. 8.175	2.384	.0032	. 0324	. 9675	23	32
	32	38	. 8078	. 1922	2.379	. 8104	2.339	.0033	. 0327	. 9673	22	28
	26	39	. 8107	. 1893	2.335	. 8134	2.295	.0033	. 0329	. 9671	21	21
	40	4()	.08136	.91864	12.291	.08163	12.250	1.0033	.00031	.99668	20	20
	44	41	. 8165	. 1835	2.248	8192	2.207	.0033	. 0334	. 9666	19	16
	48	42	. 8194	. 1806	2.204	. 8221	2.163	.0034	0336	. 9664	18 17	12 8
	52	43	. 8223 . 8252	. 1777	2.161 2.118	. 8251 . 8280	$2.120 \\ 2.077$.0034	. 0339	. 9661	16	4
ı	56 19	44 45	.08281	.91719	12.076	.08309	12.035	1.0034	.00343	.99656	15	41
1	4	46	. 8310	. 1690	2.034	. 8339	1.992	.0035	. 0346	. 9654	14	56
ı	8	47	. 8339	. 1661	1.992	. 8368	1.950	.0035	. ()348	. 9652	13	52
1	12	48	. 8368	. 1632	1.950	. 8397	1.909	.0035	. 0351	. 9649	12	48
Ì	16	49	. 8397	. 1603	1.909	. 8426	1.867	.0035	. 0353	. 9647	11	44
	20	50	.08426	.91574	11 868	.08456	11.826	1.0036	.00356	.99644	10	40
	24	51	. 8455	. 1545	1.828	. 8485	$egin{array}{c c} 1.785 & \ 1.745 & \ \end{array}$.0036	. 0358	. 9642	9 8	$\begin{array}{c} 36 \\ 32 \end{array}$
	28	52	8484	. 1516 . 1487	1.787 1.747	. 8514 . 8544	1.704	.0036	. 0360	. 9637	7	28
	32 36	53 54	. 8513 . 8542	. 1458	1.707	. 8573	1.664	.0037	. 0365	. 9634	6	21
	4')	55	.08571	.91429	11.668	.08602	11.625	1.0037	.00368	.99632	5	20
-	41	56	. 8600	. 1400	1.628	. 8632	1.585	.0037	. 0370	. 9629	4	16
	48	57	. 8629	. 1371	1.589	. 8661	1.546	.0037	0373	. 9627	3	12
	52	58	. 8658	. 1342	1.550	. 8690	1.507	.0038	. 0375	. 9624	2	8
	56	59	. 8687	. 1313	1.512	. 8719	1.468	.0038	. 0378	9622	1	4
1	20	(61)	. 8715	. 1284	1.474 Secante.	. 0149	1.430	.0038	. 0380 Vrs. Cos	. 9619 Sine.	O M	40 M.S.
	M.S. 6h		Cosine.	VIS. 51H.	Decaute.	Natu		30,500 110	, : ~	DILLO.	850	
L	0 ;	01				TASCEC	LA CAL.					

214				Ţ.	VATURA	L LINES	3.				
Oh	50		Natur	al Trig	onom	etrical	Func	tions.]	74°	_{11h}
				Cosec'nte		Cotang.		Vrs. Sin		M	M.S.
M.S. 20	M	Sine08715	.91284	11.474	Tang08749	11,430	1.0038	.00380	.99619	60	40
4	1	. 8744	. 1255	1.436	. 8778	1.392	.0038	. 0383	. 9617	59	56
8	2	. 8773	. 1226	1.398	. 8807	1.354	.0039	. 0386	. 9614	58	52
12	3	. 8802	. 1197	1.360	. 8837	1.316	.0039	. 0388	. 9612	57	48
16	4	. 8831	. 1168	1.323	. 8866		.0039	. 0391	. 9609	56	44
20	5	.08860	.91139	11.286	.08895		1.0033	.00393	.99607	55	40
24 28	6 7	. 8889	. 1110	1.249	8925	1.205 1.168	.0040	. 0396	9604	54 53	36 32
32	8	. 8918	. 1082	1.213 1.176	. 8954	1.132	.0040	. 0401	. 9599	52	23
36	9	. 8976	. 1024	1.140	9013	1.095	.0040	. 0404	. 9596	51	24
40	10	.09005	.90995	11.104	.09042	11.059	1.0041	.00406	.99594	50	20
44	11	. 9034	. 0966	1.069	. 9071	1.024	.0041	. 0409	. 9591	49	16
48	12	. 9063	. 0937	1.033	. 9101	0.988	.0041	. 0411	. 9588	48	12
52	13	. 9092	. 0908	0.998	. 9130	0.953	.0041	. 0414	. 9586	47	8
56 21	14 15	. 9121	. 0879	0.963	. 9159	0.918	.0042 1.0042	.0417	. 9583	46 45	39
4	16	. 9179	.90850	10.929 0.894	.09189	10.883	.0042	. 0422	. 9578	44	56
8	17	9208	0321	0.860	9247	0.814	.0043	. 0425	. 9575	43	52
12	18	9237	. 0763	0.826	9277	0.780	.0043	. 0427	. 9572	42	48
16	19	. 9266	. 0734	0.792	. 9306	0.746	.0043	. 0430	. 9570	41	44
20	20	.09295	.90705	10.758	.09335	10.712	1.0043	.00433	.99567	40	40
24	21	. 9324	. 0676	0.725	. 9365	0.678	.0044	. 0436	. 9564	39	36
28	22	9353	. 0647	0.692	. 9394	0.645	.0044	. 0438	. 9562	38	32
32 36	23 24	. 9382	. 0618	0.659	. 9423	0.612	.0044	. 0441	. 9559	37	28
40	25	. 9411	. 0589	10.593	.69482	0.579 10.546	.0044	.00446	. 9556 .99553	36 35	24 20
44	26	. 9469	. 0531	0.561	. 9511	0.514	.0045	. 0449	. 9551	34	16
48	27	. 9498	. 0502	0 529	. 9541	0.481	.0045	. 0452	. 9548	33	12
52	28	. 9527	. 0473	0.497	. 9570	0.449	.0046	. 0455	. 9545	32	8
56	29	. 9556	. 0444	0.465	. 9599	0.417	.0046	. 0458	. 9542	31	4
22	30	.09584	.90415	10.433	.09629	10.385	1.0046	.00460	.99540	30	38
4	31	. 9613	. 0386	0.402	. 9658	0.354	.0046	. 0463	. 9537	29	56
8 12	32 33	. 9642	. 0357	0.371 0.340	. 9688 . 9717	$0.322 \\ 0.291$.0047	. 0466	. 9534	28 27	52 48
16	34	. 9700	. 0300	0.309	9746	0.260	.0047	. 0472	. 9528	26	44
20	35	.09729	.90271	10.278	.09776	10.229	1.0048	.00474	.99525	25	40
24	36	. 9758	. 0242	0.248	. 9805	0.199	.0048	. 0477	. 9323	24	36
28	37	. 9787	. 0213	0.217	. 9834	0.168	.0048	. 0480	. 9520	23	32
32	38	. 9816	. 0184	0.187	. 9864	0.138	.0048	. 0483	. 9517	22	28
36	39	. 9845	. 0155	0.157	. 9893 .09922	0.108 10.078	.0049	. 0486	. 9514	21	24
40 44	40 41	.09874	.90126	10.127 0.698	. 9952	0.048	.0049	.00489	.99511 . 9508	20 19	20 16
48	42	. 9932	0068	0.068	. 9981	0.019	.0050	. 0494	. 9505	18	$\begin{vmatrix} 10 \\ 12 \end{vmatrix}$
52	43	. 9961	0039	0.039	.10011	9.9893	.0050	. 0497	. 9503	17	8
56	44	. 9990	. 0010	0.010	.10040	.9601	.0050	. 0500	. 9500	16	4
23	45	.10019	.89981	9.9812	.10069	.9310	1.0050	.00503	.99497	15	37
4	46	. 3048	. 9952	.9525	. 0099	.9021	.0051	. 0506	. 9494	14	56
8	47	. 0077	. 9923	.9239	. 0128	.8734	.0051	. 0509	. 9491	13	52
12	48	. 0106	. 9894	.8955 .8672	. 0158	.8448	.0051	. 0512	9488	12	48
16 20	49 50	. 0134	. 9865 .89836	9.8591	.10216	$\begin{array}{c c} .8164 \\ 9.7882 \end{array}$.0052 1.0052	.0515	. 9485	11 10	44 40
24	51	. 0192	. 9807	.8112	. 0246	.7601	.0052	. 0521	. 9479	9	36
28	52	. 0221	. 9779	.7834	. 0275	.7322	.0053	. 0524	. 9476	8	32
32	53	. 0250	. 9750	.7558	. 0305	.7044	.0053	. 0527	. 9473	7	28
36	54	. 0279	. 9721	.7283	. 0334	.6768	.0053	. 0530	. 9470	6	24
40	55	.10308	.89692	9.7010	.10363	9.6493	1.0053	.00533	.99467	5	20
41	56 57	. 0337	9663	.6739 .6469	. 0393	.6220	.0054	0536	9464	4	16
48 52	57 58	. 0366	. 9634 . 9605	.6200	. 0452	.5949 .5679	.0054	. 0539	. 9461. 9458	$\begin{bmatrix} 3 \\ 2 \end{bmatrix}$	12 8
56	59	. 0424	9576	.5933	. 0481	.5411	.0055	. 0545	9455	1	4
24	60	. 0453	9547	.5668	. 0510		.0055	. 0548	9452	Ü	36
M.S.	М	Cosine.		Secante.	Cotang.	Tangent.			Sine.	М	M.S.
6h	95°				Natu	ral.				84°	5h

T	NATURAL LINES.												
	$0^{\rm h}$	60		Notres	1 Music		otutoal	There e	44	1	73°	11h	
					d Trig								
	M.S. 24	M ()	Sine.	1	Cosec'nte	Tang.	Cotang.			Cosine.	1	M.S.	
1	4	1	.10453	.89547	9.5668	.10510	9.5144	1.0055	.00548	.99452	60	36	
1	8	2	. 0482	. 9518 . 9489	.5404 .5141	. 0549	.4878 .4614	.0055 .0056	. 0551	. 9449	59 58	56 52	
	12	3	. 0540	. 9460	.4880	. 0509	.4351	.0056	0557	. 9443	57	48	
1	16	4	. 0568	. 9431	.4620	. 0628	.4090	.0056	. 0560	. 9440	56	44	
1	20	5	.10597	.89402	9.4362	.10657	9.3831	1.0057	.00563	.99437	55	40	
	24	6	. 0626	. 9373	.4105	. 0687	.3572	.0057	. 0566	. 9434	54	36	
	28 32	7 8	. 0655	. 9345	.3850	. 0716	.3315	.0057	. 0569	. 9431	53	32	
	36	9	. 0684	9316	.3596	. 0746	.3060	.0057	. 0572	. 9428	52	28	
	40	10	.10742	. 9287	.3343 9.3092	.10805	.2806 9.2553	.0058 1.0058	.0575	. 9424	51 50	24 20	
1	41	11	. 0771	. 9229	.2842	. 0834	.2302	.0058	. 0582	. 9418	49	16	
	48	12	. 0800	. 9200	.2593	. 0863	.2051	.0059	. 0585	. 9415	48	12	
ł	52	13	. 0829	. 9171	.2346	. 0893	.1803	.0059	. 0588	. 9412	47	8	
	56	14	. 0858	. 9142	.2100	. 0922	.1555	.0059	. 0591	. 9409	46	4	
	25 4	15 16	.10887	.89113	9.1855	.10952	9.1309	1.0060	.00594	.99406	45	35	
ı	8	17	. 0916	. 9084	.1612	. 0981	.1064	.0060	0597	. 9402	44	56 52	
	12	18	. 0944	. 9055	.1370 .1129	. 1011	.0821	.0060	. 0601	. 9399	43 42	48	
	16	19	. 1002	. 8998	.0890	. 1069	.0338	.0061	. 0607	. 9393	41	44	
	20	20	.11031	.88969	9.0651	.11099	9.0098	1.0061	.00110	.99390	40	40	
	24	21	. 1060	. 8940	.0414	. 1128	8.9860	.0062	. 0613	. 9386	39	36	
ı	28	22	. 1089	. 8911	.0179	. 1158	.9623	.0062	. 0617	. 9383	38	32	
ı	32 36	23 24	. 1118	. 8882	.9944	. 1187	.9387	.0062	. 0620	. 9380	37	28	
	40	25	. 1147	. 8853	8.9711 8.9479	. 1217	.9152 8.8918	.0063 1.0063	.0623	. 9377	36 35	24 20	
	44	26	. 1205	. 8795	.9248	. 1276	.8686	.0063	. 0630	. 9370	34	16	
	48	27	. 1234	8766	.9018	. 1305	.8455	.0064	. 0633	. 9367	33	12	
	52	28	. 1262	. 8737	.8790	. 1335	.8225	.0064	. 0636	. 9364	32	8 -	
	56	29	. 1291	. 8708	.8563	. 1364	.7996	.0064	. 0639	. 9360	31	4	
	26	30	.11320	.88680	8.8337	.11393	8.7769	1.0065	.00643	.99357	30	34	
	8	31 32	. 1349	. 8651	.8112	. 1423	.7542	.0065	0646	. 9354	29	56 52	
	12	33	. 1378	8622	.7888 .7665	. 1452	.7317 .7093	.0065	. 0649	. 9350	28 27	48	
	16	34	1436	8564	.7444	. 1511	.6870	.0066	. 0656	. 9344	26	44	
	20	35	.11465	.88535	8.7223	.11541	8.6648	1.0066	.00659	.99341	25	40	
	24	36	. 1494	. 8506	.7004	. 1570	.6427	.0067	. 0663	. 9337	24	36	
	28	37	. 1523	. 8477	.6786	. 1600	.6208	.0067	. 0666	. 9334	23	32	
	32	38	. 1551	. 8448	.6569	. 1629	.5989	.0067	. 0669	. 9330	22	28 24	
	36 40	39 40	. 1580 .11609	. 8420	.6353 8.6138	. 1659		.0068	.0673	. 9327 .99324	21 20	20	
	44	41	. 1638	.88391	.5924	. 1718	8.5555 .5340	.0068	. 0679	. 9320	19	16	
	48	42	1667	8333	.5711	. 1747	.5126	.0069	. 0683	. 9317	18	12	
	52	43	. 1696	. 8304	.5499	. 1777	.4 913	.006.	. 0686	. 9314	17	8	
	56	44	. 1725	. 8272	.5289	. 1806	.4701	.0069	. 0690	. 9310	16	4	
	27	45	.11754	.88246	8.5079	.11836	8.4489	1.0070	.00693	99307	15	33	
	8	46 47	. 1783	8217	.4871 .4663	. 1865	.4279 .4070	.0070	. 0696	. 9303	14	£6 52	
	12	48	. 1840	8188	.4457	. 1895	.3862	.0070	. 0703	. 9300	12	48	
	16	49	. 1869	8131	.4251	. 1954	.3655	.0071	. 0707	. 9293	11	44	
	20	50	.11898	.88102	8.4046	.11983	8.3449	1.0071	.00710	.99290	10	40	
	24	51	. 1927	. 8073	.3843	. 2013	.3244	.0072	. 0714	. 9286	9	36	
	28	52	. 1956	. 8044	.3640	. 2042	.3040	.0072	. 0717	9283	8	32	
	32	53	. 1985	. 8015	.3439	. 2072	.2837	.0073	. 0721	. 9279	7	28	
	36 40	54 55	. 2014	. 7986 .87957	.3238 8.3039	. 2101 .12131	.2635 8.2434	0.073 1.0073	.0724	. 9276	6 5	$\begin{vmatrix} 24 \\ 20 \end{vmatrix}$	
	44	56	. 2071	. 7928	.2840	. 2160	.2234	.0074	. 0731	. 9269	4	16	
	48	57	2100	7900	.2642	2190	.2035	.0074	. 0735	9265	3	12	
	52	58	. 2129	. 7871	.2446	. 2219	.1837	.0074	. 0738	. 9262	2	8	
	56	59	. 2158.	. 7842	.2250	. 2249	.1640	.0075	. 0742	. 9258	1.	4	
	28	60	. 2187	. 7813	.2055	2278	.1443	.0075	. 0745	, 9255	0	32	
-	M.S. 6h	96°	Cosme.	vrs.Sm.	Secante.			Cosec nt	VIS. COS	Sine.	м 83°	M.S. 5h	
	0	100				Natu	rat.				00	0	

0 ^h	7°													
M.S.	М	Sine.	Vrs. Cos.	Cosec'nte	Tang.	Cotang.	Secante.	Vrs. Sin	Cosine.	M	M.S.			
128	0	.12187	.87813	8.2055	.12278	8.1443	1.0075	.00745	.99255	60	32			
4	1	. 2216	. 7787	.1861	. 2308	.1248	.0075	. 0743	. 9251	59	56			
8	2	. 2245	. 7755	.1668	. 2337	.1053	.0076	. 0752	. 9247	58	52			
12	3	. 2273	. 7726	.1476	. 2367	.0860	.0076	. 0756	. 9244	57	48			
16	4	. 2302	. 7697	.1285 8.1094	. 2396 .12426	.0667 8.0476	.0076	.0760	. 9240	56 55	40			
$\begin{bmatrix} 20 \\ 24 \end{bmatrix}$	5 6	.12331	.87669 . 7640	.0905	.12426	8.0476 0285	1.0077	.00763	.9233	54	36			
28	7	. 2389	. 7611	.0717	2485	.0095	.0078	0770	9229	53	32			
32	8	. 2418	7582	.0529	2515	7.9906	.0078	. 0774	9226	52	28			
36	9	. 2447	7553	.0342	. 2544	7.9717	.0078	. 0778	9222	51	24			
40	10	.12476	.87524	8.0156	.12574	7.9530	1.0079	.00781	.99219	50	20			
44	11	. 2504	. 7495	7.9971	. 2603	.9344	.0079	. 0785	. 9215	49	16			
48	12	2533	. 7467	.9787	. 2633	.9158	.0079	. 0788	. 9211	48	12			
52	13	. 2562	. 7438	.9604.	. 2662	.8473	.0080	. 0792	. 9208	47	8			
56	14	2591	. 7409	.9421	. 2692	.8789	.0080	. 0796	9204	46	4 31			
29	15	.12620	.87380	7.9240 .9059	. 12722	7.8606	1.0080	.00799	.99200	45 44	56			
8	16 17	. 2649 . 2678	. 7351 . 7322	.8879	2781	.8424 .8243	.0081	. 0803	9193	43	52			
12	18	2706	7293	.8700	2810	.8062	.0082	. 0810	. 9189	42	48			
16	19	2735	7265	.8522	2840	.7882	:0082	. 0814	. 9186	41	44			
20 20 .12764 .87236 7.8344 .12869 7.7703 1.0082 .00818 .99182 40 4) 24 21 .2793 .7207 .8168 .2899 .7525 .0083 .0822 .9178 39 36														
24 21 . 2793 . 7207 .8168 . 28997525 .0083 . 0822 . 9178 39 36														
28 22 . 2822 . 71787992292873480083 0825 9174 38 32														
32	23	. 2851	. 7149	.7817	. 2958	.7171	.0084	. 0829	. 9171	37				
36	24	2879	. 7120	.7642	. 2988	.6996	.0084	. 0833	. 9167	36	24			
40	25	.12908	.87091 . 7063.	7.7469 .7296	.13017	7.6821	1.0084	.00837	.99163	35 34	20 16			
44 48	26 27	· 2937 · 2966	7034	.7124	. 3076	.6646 .6473	.0085	. 0844	. 9156	33	12			
52	28	2995	7005	.6953	3106	.6300	.0085	. 0848	9152	32	8			
56	29	. 3024	6976	.6783	. 3136	.6129	.0086	. 0852	. 9148	31	+			
30	30	.13053	.86947	7.6613	.13165	7.5957	1.0086	.00855	.99144	30	30			
4	31	. 3081	. 6918	.6444	. 3195	.5787	.0087	. 0859	. 9141	29	56			
8	32	. 3110	. 6890	.6276	. 3224	.5617	.0087	. 0863	. 9137	28	52			
12	33	. 3139	. 6861	.6108	. 3254	.5449	.0087	. 0867	. 9133	27	48			
16 20	34 35	3168 .13197	. 6832 .86803	.5942 7.5 1 76	. 3284	.5280 7.5113	.0088 1.0088	. 0871	. 9129 .99125	26 25	44 40			
24	$\begin{vmatrix} 36 \end{vmatrix}$. 3226	6774	.5611	. 3343	.4946	.0089	. 00875	. 9121	$\frac{23}{24}$	36			
28	37	. 3254	6745	.5446	3372	.4780	.0089	. 0882	. 9118	23	32			
32	38	. 3283	. 6717	.5282	. 3402	.4615	.0089	. 0886	. 9114	22	28			
36	39	. 3312	. 6688	.5119	. 3432	.4451	.0090	. 0890	. 9110	21	24			
40	40	.13341	.86659	7.4957	.13461		1.0090	.00894	.99106		20			
44	41	. 3370	. 6630	.4795	. 3491	.4124	.0090	. 0898	. 9102	19	16			
48	42	. 3399	. 6601	.4634	3520	.3961	.0091	. 0902	. 9098	18	12			
52 56	43 44	· 3427 · 3456	. 6572 . 6544	.4474 .4315	. 3550 . 3580	.3800 .3639	.0091	. 0305	9094	17 16	8 4			
31	45	.13485	.86515	7.4156	.13609	7.3479	0.0092 1.0092	.00913	. 9090	15	29			
4	46	. 3514	. 6486	.3998	. 3639	.3319	.0092	. 0917	. 9083	14	56			
8	47	. 3543	6457	.3840	3669	.3160	.0093	. 0921	9079	13	52			
12	48	. 3571	. 6428	.3683	. 3698	.3002	.0093	. 0925	. 9075	12	48			
16	49	. 3600	. 6400	.3527	. 3728	.2844	.0094	. 0929	. 9070	11	44			
20	50	.13629	.86371	7.3372	.13757	7.2687	1.0094	.00933	.99067	10	40			
24	51	. 3658	. 6342	.3217	. 3787	.2531	.0094	. 0937	. 9063	9	36			
28 32	52 53	3687	6313	.3063 .2909	3817	.2375	.0095	. 0941	9059	8	32 28			
36	54	. 3716	. 6284 . 6255	.2909	. 3846	.2220 .2066	.0095 :0096	. 0945	. 9055 . 9051	7 6	28 24			
40	55	.13773	.86227	7.2604	.13906	7.1912	1.0096	.00953	.99047	5	20			
44	56	. 38′.2	. 6198	.2453	3935	.1759	.0097	. 0957	. 9043	4	16			
48	57	. 3831	. 6169	.2302	. 3965	.1607	.0097	. 0961	9039	$\hat{3}$	12			
52	58	. 3860	. 6140	.2152	. 3995	.1455	.0097	. 0965	. 9035	2	8			
56	59	. 3888	. 6111	.2002	. 4024	.1394	.0098	. 0969	. 9931	1	+			
33	60)	. 3917	. 6083	.1853	4054	.1154	.0098	. 0973	. 9027	0	28			
M. S. 6h	м 97°	Cosine.	vrs. Sm.	Secante.		Tangent.	Cosec nt	vrCos	Sine. I	82°	M.S. 5h			
	01				Nati	trati.				02	0			

0 _p	8°		Natur	al Trig	onom	etrical	Func	tions.]	71°	11h
M.S.	М	Sine.	Vrs.Cos.	Cosec'nte	Tang.	Cotang.	Secante.	Vrs. Sin	Cosine.	M	M.S.
32	0	.13917	.86083	7.1853	.14054	7.1154	1.0098	.00973	.99027	60	28
8	$\begin{vmatrix} 1\\2 \end{vmatrix}$. 3946	. 6054	.1704	. 4084	.1001	.0099	. 0977	. 9023	59	56
12	3	. 3975	. 6025	.1557 .1409	. 4113	.0854	.0099	. 0981	. 9019	58 57	52 48
16	4	4032	5967	.1263	. 4173	.0558	.0100	. 0989	. 9010	56	44
20	5	.14061	.85939	7.1117	.14202	7.0410	1.0100	.00993	.99006	55	40
24	6	. 4090	. 5910	.0972	. 4232	.0264	.0101	. 0998	. 9002	54	36
28 32	7 8	. 4119	. 5881	.0827	. 4262	.0117	.0101	. 1002	. 8998	53	32
36	9	. 4148	. 5852	.0683	. 4291	6.9972	.0102	. 1006	. 8994 . 8930	52 51	28 24
40	10	.14205	.85795	7.0396	.14351	6.9682	1.0102	.01014	.98986	50	20
44	11	. 4234	. 5766	.0254	. 4380	.9538	.0103	. 1018	. 8982	49	16
48	12	. 4263	. 5737	.0112	. 4410	.9395	.0103	. 1022	. 8978	48	12
52 56	13 14	. 4292	. 5708	6.9971	. 4440	.9252	.0104	. 1026	. 8973	47	8
33	15	.14349	. 5679	6.9830 6.9690 ·	. 4470	.9110 6.8969	1.0104	. 1031	. 8963	46 45	27
4	16	. 4378	. 5622	.9550	. 4529	.8828	.0105	. 1039	. 8961	44	56
8	17	. 4407	. 5593	.9411	. 4559	.8687	.0105	. 1043	. 8957	43	52
12	18	. 4436	. 5564	.9273	. 4588	.8547	.0106	. 1047	. 8952	42	48
16 20	$\begin{array}{ c c }\hline 19 \\ 20 \\ \end{array}$	14464	. 5536	.9135	. 4618	.8408	.0106	. 1052	. 8948	41	44
24	21	.14493	.85507	6.8998 .8861	.14648	6.8269	1.0107	.01056	.98944	40 39	36
28	22	4551	5449	.8725	4707	.7993	.0107	. 1064	. 8936	38	32
32	23	. 4579	. 5420	.8589	. 4737	.7856	.0108	. 1068	. 8931	37	28
36	24	. 4608	. 5392	.8454	. 4767	.7720	.0108	. 1073	. 8927	36	24
40	$\begin{array}{ c c }\hline 25 \\ 26 \\ \hline \end{array}$.14637	.85363	6.8320	.14796	6.7584	1.0109	.01077	.98923	35	20
48	27	. 4666	5334	.8185 .8052	. 4826	.7448 .7313	.0109	. 1085	. 8919	34 33	16 12
52	28	4723	5277	.7919	. 4886	.7179	.0110	. 1090	. 8910	32	8
56	29	. 4752	. 5248	.7787	. 4915	.7045	.0111	. 1094	. 8906	31	4
34	30	.14781	.85219	6.7655	.14945	6.6911	1.0111	.01098	.98901	30	26
8	31 32	. 4810	5190	.7523 .7392	. 4975	.6779 .6646	.0111	. 1103	8897	29 28	56 52
12	33	. 4867	5133	.7262	. 5034	.6514	.0112	. 1111	. 8889	27	48
16	34	. 4896	5104	.7132	. 5064	.6383	.0113	. 1116	. 8884	26	44
20	35	.14925	.85075	6.7003	.15094	6.6252	1.0113	.01120	.98880	25	40
24	36	. 4953	. 5046	.6874	. 5123	.6122	.0114	. 1124	. 8876	24	36
28 32	37 38	. 4982	. 5018	.6745	. 5153 . 5183	.5992 .5863	.0114	. 1129 . 1133	. 8871	23 22	32 28
36	39	. 5040	4960	.6490	. 5213	.5734	.0115	1137	. 8862	21	24
40	40	.15068		6.6363	.15243	6.5605	1.0115	.01142	.98858	$\frac{1}{20}$	20
44	41	. 5097	. 4903	.6237	. 5272	.5478	.0116	. 1146	. 8854	19	16
48	42 43	. 5126	4874	.6111	5302	.5350	.0116	. 1151	. 8849	18	12
52 56	44	. 5155 . 5183	. 4845	.5985 .5860	. 5332	.5223 .5097	.0117	. 1159	. 8845	17 16	8
35	45	.15212	.84788	6.5736	.15391	6.4971	1.0118	.01164	.98836	15	25
4	46	. 5241	. 4759	.5612	. 5421	.4845	.0118	. 1168	. 8832	14	56
8	47	. 5270	4730	.5488	. 5451	.4720	.0119	. 1173	. 8827	13	52
12 16	48 49	. 5298	4701 . 4672	.5365 .5243	. 5481	.4596 .4472	.0119	. 1177	. 8823 . 8818	12 11	48 44
20	50	.15356	.84614	6.5121	.15540	6.4348	1.0120	.01186	.98814	10	4()
24	51	. 5385	. 4615	.4999	. 5570	.4225	.0120	. 1190	. 8809	9	36
28	52	. 5413	. 4586	.4878	. 5600	.4103	.0121	. 1195	. 8805	8	32
32	53	. 5442	4558	.4757	5630	.3980	.0121	. 1199	. 8800	7	28
36 40	54 55	. 5471	. 4529	$\begin{array}{c} .4637 \\ 6.4517 \end{array}$. 5659 .15689	.3859 6.3737	.0122 1.0122	.1204	. 8796 .98791	6 5	24 20
44	56	. 5528	. 4471	.4398	5719	.3616	.0123	. 1213	. 8787	4	16
48	57	. 5557	. 4443	.4279	. 5749	.3496	.0123	. 1217	. 8782	3	12
52	58	. 5586	. 4414	.4160	. 5779	.3376	.0124	. 1222	. 8778	2	8
56	59	. 5615	. 4385	.4042	. 5809	.3257	.0124	. 1227	8773	1	4
36 M.S.	60 M	. 5643 Cosine.	. 4356 Vrs.Sin.	.3924 Secante.	. 5838 Cotang.		.0125 Cosec'nt	. 1231 Sine.	. 8769 Vrs. Cos	O M	24
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N.S. Sine. Vrs.Cos. Coscelute Tang., Cotang. Scanate Vrs.Sin. Cosine. M. M. S. M. Sine. Vrs.Cos. Coscelute Tang., Cotang. Scanate Vrs.Sin. Cosine. M. M. S. M. Sine. Vrs.Cos. Coscelute Tang., Cotang. Scanate Vrs.Sin. Cosine. M. M. S. M	NATURAL IMPES.														
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4 1 5672 4328 3807 5868 3010 0125 1240 8760 58 201 0125 1249 8760 58 201 123 35730 4270 3674 5928 22783 0126 1245 8755 57 48 16 4 6758 4242 3468 5988 2665 0123 1249 8750 56 44 20 5 15816 4184 3228 6017 2432 0127 1259 8744 54 36 32 8 5873 4127 2999 6077 2200 0128 1268 8773 52 28 36 9 5902 4098 2885 6167 1856 0130 1277 ,9872 51 20 40 10 16938 8404 2524 6167 1856 0130 1286 8714 48 12 52 13		2						1			_				
88 2 5 701 4290 5690 5898 2901 10125 1244 8750 58 52 16 4 5758 4242 3458 5058 2666 6129 1249 8750 56 44 20 5 15787 34213 63343 15987 62548 10127 -0124 98740 56 40 28 7 5844 4135 3113 6017 2342 0127 1259 8741 54 54 64 28 7 5844 4155 3113 6017 2322 0122 1268 87373 53 33 36 9 5902 4098 8285 6107 2020 0122 1272 87273 50 204 44 11 5908 4012 2569 6167 1186 6130 1227 87723 50 22 56 14 6045 3934 <td>1 .</td> <td></td>	1 .														
12	1						.3019								
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24			. 5758	. 4242	.3458	. 5958	.2665	.0126	. 1249	. 8750	56				
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32 8 8 5873 4127 2999 6077 200 0128 1208 8732 52 25 36 9 5 502 4498 2885 6107 2085 0129 1272 8727 51 24 40 10 15931 84069 62772 16137 61970 10129 01277 98723 50 20 44 11 5595 4041 2595 6167 1856 0130 1282 8718 49 16 64 11 5595 4041 2659 6167 1856 0130 1282 8718 49 16 6617 3983 2434 6226 1628 0131 1291 8709 47 8 8 6614 6045 394 2222 6255 1615 0131 1296 8704 46 14 37 15 16074 88926 62211 16286 61403 10132 01300 98700 45 23 4 16 6163 3887 2100 6316 1178 0133 1310 8890 43 52 12 18 6160 3810 1880 6376 1096 0133 1314 8885 42 8 12 18 6160 3810 1880 6376 1066 0133 1314 8885 42 8 12 16 19 6189 8811 1770 6405 0955 0134 1310 8890 43 52 2 6256 0734 0135 1898 8971 33 62 2 6256 0134 10132 0133 8681 44 20 20 16218 83782 61661 1645 6054 0134 1313 8861 49 42 42 1 6246 3753 1552 6465 0734 0135 1333 8867 33 36 24 6333 3667 1227 6555 0105 0136 1333 8862 37 28 22 6275 3725 1443 6495 0624 0135 1333 8867 38 32 23 6304 3696 1335 6255 0145 0136 1335 8862 37 28 42 6467 3533 1652 6465 0105 0136 1343 8857 36 24 42 6 6390 3610 1013 6615 0188 0137 1843 8857 62 4 647 3553 000 6674 5098 0137 1357 8643 31 4 27 6416 333 3667 1227 6555 0105 0136 1343 8857 36 24 42 6 6390 3610 1013 6615 0188 0137 1363 8682 37 28 8 6447 3553 0800 6674 59972 0138 1362 8648 31 6 48 27 6419 3551 0906 6644 0080 0137 1357 8643 33 12 2 13 6563 3438 0370 6674 59972 0138 1367 8633 31 4 4 31 6619 3380 0170 6834 9935 10141 1391 8609 25 40 40 40 669 338 6677 1227 6555 0105 0136 1343 8557 8643 33 12 2 2 6562 3648 80379 6704 59865 0138 1367 8633 31 4 2 6 6 6 6 6 7 3243 8 8 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6															
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56 1 4									1280						
37 15 16074 83926 6.2211 16286 6.1402 1.0132 .01300 .98700 45 5 8 17 .6132 .3868 1.190 .6346 1.178 .0133 .1310 .8690 43 52 12 18 .6160 .3840 .1880 .6376 .1066 .0133 .1310 .8690 43 52 16 .19 .6189 .8811 .1770 .6405 .0955 .0133 .1314 .8685 42 42 21 .6246 .3753 .1552 .6465 .0734 .0135 .1313 .8681 41 44 24 21 .6246 .3753 .1552 .6465 .0624 .0135 .1333 .8667 .186 .383 32 223 .6304 .3667 .1227 .6555 .0164 .0136 .1333 .8667 .366 .38 .32 .44 26 .6390 .3610 <t></t>				. 3954											
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24 21 .6246 .3753 .1552 .6465 .0734 .0135 .1328 .8671 39 36 28 22 .6275 .3725 .1443 .6495 .0624 .0135 .1333 .8667 38 32 36 24 .6333 .3667 .1227 .6555 .0405 .0136 .1343 .8657 36 24 40 25 .16361 .83639 .61120 .16585 .60296 .10137 .1352 .8648 34 16 48 27 .6419 .3581 .0906 .6644 .0980 .0137 .1357 .8643 33 12 52 28 .6447 .3553 .0800 .6674 .59972 .0138 .1362 .8648 32 56 29 .6476 .3523 .0694 .6704 .59985 .0138 .1362 .8638 32 48 31 .6533 .3466	20 20 .16218 .83782 6.1661 .16435 6.0844 1.0134 .01324 .98676 40 40 24 21 .6246 .3753 .1552 .6465 .0734 .0135 .1328 .8671 39 36														
32 23	1		. 6246	. 3753	.1552	. 6465	.0734	.0135	. 1328	. 8671	_				
36															
40 25 1,6361 8,3639 6,1120 1,6585 6,0296 1,0136 ,0137 ,98652 35 20 44 26 6390 ,3610 1,013 ,6615 ,0188 ,0137 ,1352 ,8648 34 16 48 27 ,6419 ,3581 ,0906 ,6644 ,0980 ,1377 ,1357 ,8643 31 12 56 29 ,6476 ,3524 ,0694 ,6704 5,9865 ,0138 ,1367 ,8633 31 4 31 ,6533 ,3466 ,0483 ,6764 ,9651 ,0139 ,1376 ,8624 29 56 8 32 ,6562 ,3438 ,0379 ,6794 ,9545 ,0140 ,1381 ,8619 28 26 86824 29 56 8 32 ,6662 ,3438 ,0379 ,6794 ,9543 ,0140 ,1388 8619 28 4 16									1338						
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56 28 6447 .3553 .0800 .6674 5.9972 .0138 .1362 .8638 32 8 56 29 .6476 .3524 .0694 .6704 5.9865 .0138 .1367 .8633 31 4 38 30 .16653 .3466 .0483 .6764 .9651 .0139 .1376 .8624 29 56 8 32 .6562 .3438 .0379 .6794 .9545 .0140 .1381 .8619 28 52 16 34 .6619 .3380 .0170 .6884 .9333 .0140 .1386 .8614 27 48 24 36 .6677 .3323 5.9963 .6914 .9123 .0142 .1400 .8600 24 36 28 37 .6705 .3294 .9860 .6944 .9019 .0142 .1405 .8502 23 22 28 66 .3		26													
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24 36 . 6677 . 3323 5.9963 . 6914 . 9123 . 0142 . 1400 . 8600 24 36 28 37 . 6705 . 3294 . 9860 . 6944 . 9019 . 0142 . 1405 . 8505 23 32 32 38 . 6734 . 3266 . 9758 . 6973 . 8915 . 0143 . 1411 . 8590 22 28 66 39 . 6763 . 3237 . 9655 . 7003 . 8811 . 0143 . 1411 . 8580 22 28 40 40 . 16791 . 83208 5.9554 . 17033 5.8708 . 1.0144 . 01420 . 98580 20 20 44 41 . 6820 . 3180 . 9452 . 7063 . 8605 . 0144 . 1425 . 8575 19 16 48 42 . 6849 . 3151 . 9351 . 7093 . 8502 . 0145 . 1434 . 8565 17 8				23350											
28															
32 38 . 6734 . 3266 . 9758 . 6973 . 8915 . 0143 . 1410 . 8590 22 28 36 39 . 6763 . 3237 . 9655 . 7003 . 8811 . 0143 . 1411 . 8585 21 24 40 40 . 16791 . 83208 5.9554 . 17033 5.8708 1.0144 . 01420 . 98580 20 20 44 41 . 6820 . 3180 . 9452 . 7063 . 8605 . 0144 . 1425 . 8575 19 16 48 42 . 6849 . 3151 . 9351 . 7093 . 8502 . 0145 . 1430 . 8570 18 12 56 44 . 6906 . 3094 . 9150 . 7153 . 8298 . 0146 . 1439 . 8560 17 8 4 46 . 6964 . 3036 . 8950 . 7213 . 8695 . 0147 . 1449 . 8551 14 £6		37	. 6705						. 1405						
40 40 .16791 .83208 5.9554 .17033 5.8708 1.0144 .01420 .98580 20 20 44 41 .6820 .3180 .9452 .7063 .8605 .0144 .1425 .8575 19 16 48 42 .6849 .3151 .9351 .7093 .8502 .0145 .1430 .8570 18 12 52 43 .6878 .3122 .9250 .7123 .8400 .0145 .1434 .8565 17 8 56 44 .6906 .3094 .9150 .7153 .8298 .0146 .1439 .8560 16 4 39 45 .16935 .83065 .59049 .17183 5.8196 1.0146 .01444 .98556 15 21 4 46 .6964 .3036 .8950 .7213 .8695 .0147 .1449 .8551 14 52 12 48 .7021 .2979 .8751 .7273 .7894 .0148 .1459 .8541<							.8915		. 1410	. 8590					
44 41 .6820 .3180 .9452 .7063 .8605 .0144 .1425 .8575 19 16 48 42 .6849 .3151 .9351 .7093 .8502 .0145 .1430 .8570 18 12 52 43 .6878 .3122 .9250 .7123 .8400 .0145 .1434 .8565 17 8 56 44 .6906 .3094 .9150 .7153 .8298 .0146 .1439 .8560 16 4 39 45 .16935 .83065 5.9049 .17183 5,8196 1.0146 .01444 .98556 15 21 4 46 .6964 .3036 .8950 .7213 .8095 .0147 .1449 .8551 14 £6 8 47 .6992 .3008 .8850 .7243 .7994 .0148 .1459 .8541 12 48 16 49 .7050 .2950 .8652 .7303 .7793 .0148 .1459 .8541			6763	. 3237		. 7003	.8811	.0143	. 1411	. 8585	21				
48 42 . 6849 . 3151 .9351 . 7093 .8502 .0145 . 1430 . 8570 18 12 52 43 . 6878 . 3122 .9250 . 7123 .8400 .0145 . 1434 . 8565 17 8 56 44 . 6906 . 3094 .9150 . 7153 . 8298 .0146 . 1439 . 8560 16 4 39 45 . 16935 . 83065 5.9049 . 17183 5.8196 1.0146 .01444 . 98556 15 21 4 46 . 6964 . 3036 . 8950 . 7213 . 8095 . 0147 . 1449 . 8551 14 46 8 47 . 6992 . 3008 . 8850 . 7243 . 7994 . 0147 . 1449 . 8541 12 48 16 49 . 7050 . 2950 . 8652 . 7303 . 7793 . 0148 . 1464 . 8536 11 44															
52 43 . 6878 . 3122 . 9250 . 7123 . 8400 . 0145 . 1434 . 8565 17 8 56 44 . 6906 . 3094 . 9150 . 7153 . 8298 . 0146 . 1439 . 8560 16 4 39 45 . 16935 . 83065 5.9049 . 17183 5.8196 1.0146 . 01444 . 98556 15 21 4 46 . 6964 . 3036 . 8950 . 7213 . 8695 . 0147 . 1449 . 8551 14 £6 8 47 . 6992 . 3008 . 8850 . 7243 . 7994 . 0147 . 1449 . 8541 12 48 12 48 . 7021 . 2979 . 8751 . 7273 . 7894 . 0148 . 1464 . 8536 11 44 20 50 . 17078 . 82922 5.8554 . 17333 5.7694 1.0149 . 01469 . 98531 10 40	1														
39 45 .16935 .83065 5.9049 .17183 5.8196 1.0146 .01444 .98556 15 21 4 46 .6964 .3036 .8950 .7213 .8095 .0147 .1449 .8551 14 .66 8 47 .6992 .3008 .8850 .7243 .7994 .0147 .1454 .8546 13 52 12 48 .7021 .2979 .8751 .7273 .7894 .0148 .1459 .8541 12 48 16 49 .7050 .2950 .8652 .7303 .7793 .0148 .1464 .8536 11 44 20 50 .17078 .82922 5.8554 .17333 5.7694 1.0149 .01469 .98581 10 40 24 51 .7107 .2893 .8456 .7363 .7594 .0150 .1474 .8526 9 36 28 52	52	43	. 6878	. 3122	.9250	. 7123	.8400	.0145	. 1434	. 8565	17				
4 46 .6964 .3036 .8950 .7213 .8695 .0147 .1449 .8551 14 £6 8 47 .6992 .3008 .8850 .7243 .7994 .0147 .1454 .8546 13 52 12 48 .7021 .2979 .8751 .7273 .7894 .0148 .1459 .8541 12 48 16 49 .7050 .2950 .8652 .7303 .7793 .0148 .1464 .8536 11 44 20 50 .17078 .82922 5.8554 .17333 5.7694 1.0149 .01469 .98531 10 40 24 51 .7107 .2893 .8456 .7363 .7594 .0150 .1474 .8526 9 36 28 52 .7136 .2864 .8358 .7393 .7495 .0150 .1479 .8521 8 32 32 53 .7164 .2836 .8261 .7423 .7396 .0151 .1484 .8516										. 8560					
8 47 .6992 .3008 .8850 .7243 .7994 .0147 .1454 .8546 13 52 12 48 .7021 .2979 .8751 .7273 .7894 .0148 .1459 .8541 12 48 16 49 .7050 .2950 .8652 .7303 .7793 .0148 .1464 .8536 11 44 20 50 .17078 .82922 5.8554 .17333 5.7694 1.0149 .01469 .98531 10 40 24 51 .7107 .2893 .8456 .7363 .7594 .0150 .1474 .8526 9 36 28 52 .7136 .2864 .8358 .7393 .7495 .0150 .1479 .8521 8 32 32 53 .7164 .2836 .8261 .7423 .7396 .0150 .1479 .8521 8 32 36 54 .7193 .2807 .8163 .7453 .7297 .0151 .1484 .8516												_			
12 48 .7021 .2979 .8751 .7273 .7894 .0148 .1459 .8541 12 48 16 49 .7050 .2950 .8652 .7303 .7793 .0148 .1464 .8536 11 44 20 50 .17078 .82922 5.8554 .17333 5.7694 1.0149 .01469 .98531 10 40 24 51 .7107 .2893 .8456 .7363 .7594 .0150 .1474 .8526 9 36 28 52 .7136 .2864 .8358 .7393 .7495 .0150 .1479 .8521 8 32 32 53 .7164 .2836 .8261 .7423 .7396 .0151 .1484 .8516 7 28 36 54 .7193 .2807 .8163 .7453 .7297 .0151 .1489 .8511 6 24 40 55 .17221 .82778 5.8067 .17483 5.7199 1.0152 .01494 .98506 </td <td></td> <td>_</td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> <td>_</td>		_										_			
16 49 . 7050 . 2950 . 8652 . 7303 . 7793 . 0148 . 1464 . 8536 11 44 20 50 .17078 .82922 5.8554 . 17333 5.7694 1.0149 . 01469 . 98531 10 40 24 51 . 7107 . 2893 . 8456 . 7363 . 7594 . 0150 . 1474 . 8526 9 36 28 52 . 7136 . 2864 . 8358 . 7393 . 7495 . 0150 . 1479 . 8521 8 32 32 53 . 7164 . 2836 . 8261 . 7423 . 7396 . 0151 . 1484 . 8516 7 28 36 54 . 7193 . 2807 . 8163 . 7453 . 7297 . 0151 . 1489 . 8511 6 24 40 55 . 17221 . 82778 5.8067 . 17483 5.7199 1.0152 . 01494 . 98506 5 20 44 56 . 7250 . 2750 . 7970 . 7513 . 7101 <	12		. 7021								8				
24 51 . 7107 . 2893 . 8456 . 7363 . 7594 . 0150 . 1474 . 8526 9 36 28 52 . 7136 . 2864 . 8358 . 7393 . 7495 . 0150 . 1479 . 8521 8 32 32 53 . 7164 . 2836 . 8261 . 7423 . 7396 . 0151 . 1484 . 8516 7 28 36 54 . 7193 . 2807 . 8163 . 7453 . 7297 . 0151 . 1489 . 8511 6 24 40 55 . 17221 . 82778 5.8067 . 17483 5.7199 1.0152 . 01494 . 98506 5 20 44 56 . 7250 . 2750 . 7970 . 7513 . 7101 . 0152 . 1499 . 8501 4 16 48 57 . 7279 . 2721 . 7874 . 7543 . 7004 . 0153 . 1504 . 8496 3 12	16	49	. 7050	. 2950	.8652	. 7303	.7793	.0148	. 1464	. 8536	11	44			
28 52 . 7136 . 2864 .8358 . 7393 .7495 .0150 . 1479 . 8521 8 32 32 53 . 7164 . 2836 .8261 . 7423 .7396 .0151 . 1484 . 8516 7 28 36 54 . 7193 . 2807 .8163 . 7453 . 7297 .0151 . 1489 . 8511 6 24 40 55 .17221 .82778 5.8067 .17483 5.7199 1.0152 .01494 .98506 5 20 44 56 . 7250 .2750 . 7970 . 7513 .7101 .0152 . 1499 . 8501 4 16 48 57 . 7279 . 2721 . 7874 . 7543 . 7004 .0153 . 1504 . 8496 3 12 . 52 58 . 7307 . 2692 . 7778 . 7573 . 6906 .0153 . 1509 . 8491 2 8 . 66 . 7365 . 2635 . 7588 . 7603 . 6809 .0154 . 1514 . 8486 1 4 40 60 . 7365 . 2635 . 7588 . 7633 . 6713 . 6154 . 1519 . 8481 0 20 . 8491 . 1514 . 8486 . 14 . 1519 . 8481 0 . 152 . 15															
32 53 . 7164 . 2836 . 8261 . 7423 . 7396 . 0151 . 1484 . 8516 7 28 36 54 . 7193 . 2807 . 8163 . 7453 . 7297 . 0151 . 1489 . 8511 6 24 40 55 . 17221 . 82778 5.8067 . 17483 5.7199 1.0152 . 01494 . 98506 5 20 44 56 . 7250 . 2750 . 7970 . 7513 . 7101 . 0152 . 1499 . 8501 4 16 48 57 . 7279 . 2721 . 7874 . 7543 . 7004 . 0153 . 1504 . 8496 3 12 52 58 . 7307 . 2692 . 7778 . 7573 . 6906 . 0153 . 1509 . 8491 2 8 56 59 . 7336 . 2664 . 7683 . 7603 . 6809 . 0154 . 1514 . 8486 1 4 40 60 . 7365 . 2635 . 7588 . 7653 . 6713 . 6154 . 1519 . 8481 0 20 M. S. M Cosine. Vrs. Sin. Secante. Cotang. Tangent.															
36 54 . 7193 . 2807 . 8163 . 7453 . 7297 . 0151 . 1489 . 8511 6 24 40 55 .17221 . 82778 5.8067 . 17483 5.7199 1.0152 . 01494 . 98506 5 20 44 56 . 7250 . 2750 . 7970 . 7513 . 7101 . 0152 . 1499 . 8501 4 16 48 57 . 7279 . 2721 . 7874 . 7543 . 7004 . 0153 . 1504 . 8496 3 12 52 58 . 7307 . 2692 . 7778 . 7573 . 6906 . 0153 . 1509 . 8491 2 8 56 59 . 7336 . 2664 . 7683 . 7603 . 6809 . 0154 . 1514 . 8486 1 4 40 60 . 7365 . 2635 . 7588 . 7653 . 6713 . 6154 . 1519 . 8481 0 20															
40 55 .17221 .82778 5.8067 .17483 5.7199 1.0152 .01494 .98506 5 20 44 56 .7250 .2750 .7970 .7513 .7101 .0152 .1499 .8501 4 16 48 57 .7279 .2721 .7874 .7543 .7004 .0153 .1504 .8496 3 12 52 58 .7307 .2692 .7778 .7573 .6906 .0153 .1509 .8491 2 8 56 59 .7336 .2664 .7683 .7603 .6809 .0154 .1514 .8486 1 4 40 60 .7365 .2635 .7588 .7633 .6713 .6154 .1519 .8481 0 20 M. S. M Cosine. Vrs. Sin. Secante. Cotang. Tangent. Cosce nt Vrs. Cos Sine. M 1.8	36	54	. 7193	. 2807	.8163	. 7453	.7297	.0151	. 1489	. 8511	6				
48 57 . 7279 . 2721 . 7874 . 7543 . 7004 . 0153 . 1504 . 8496 3 12 52 58 . 7307 . 2692 . 7778 . 7573 . 6906 . 0153 . 1509 . 8491 2 8 56 59 . 7336 . 2664 . 7683 . 7603 . 6809 . 0154 . 1514 . 8486 1 4 40 60 . 7365 . 2635 . 7588 . 7653 . 6713 . 6154 . 1519 . 8481 0 20 M. S. M Cosine. Vrs. Sin. Secante. Cotang. Tangent. Cosec nt Vrs. Cos Sine. M 1. S.			.17221	.82778		.17483			.01494	.98506	_	1			
52 58 . 7307 . 2692 . 7778 . 7573 . 6906 . 0153 . 1509 . 8491 2 8 56 59 . 7336 . 2664 . 7683 . 7603 . 6809 . 0154 . 1514 . 8486 1 4 40 60 . 7365 . 2635 . 7588 . 7653 . 6713 . 6154 . 1519 . 8481 0 20 M. S. M Cosine. Vrs. Sin. Secante. Cotang. Tangent. Cosce nt Vrs. Cos Sine. M 1. S.											_				
56 59 . 7336 . 2664768376036809015415148486						7573									
40 60 . 7365 . 2635 7588 7653		_	. 7336	. 2661		. 7603									
M. S. M Cosine. Vrs. Sin. Secante. Cotang. Tangent. Cosee nt Vrs. Cos Sine. M 1.S. 6h 99° Natural. 80° 5h	40	_	. 7365	. 2635	.7588	. 7653	.6713	.0154	. 1519	. 3481	0	20			
0 30 Natural. 80° 3"			Cosine.	Vrs.Sin.	Secante.			Cosee nt l	Vrs. Cos						
	0-	33				TEST	ral.				001	0"			

				-		L DINES	J •				21:
0h	·10°		Natura	al Trig	onom	etrica	l Fun	ctions	. 1	.69°	11h
M.S.	M	Sine.	Vrs. Cos.	Cosec'nte	Tang.	Cotang.	Secante.	Vrs. Sin	Cosine.	M	M.S.
40	0	.17365	.82635	5.7588	.17633	5.6713	1.0154	.01519	.98481	60	20
4	1	. 7393	. 2606	.7493	. 7663	.6616	.0155	. 1524	. 8476	59	56
8	2	. 7422	. 2578	.7398	. 7693	.6520	.0155	. 1529	. 8471	58	52
12	3	. 7451	. 2549	.7304	. 7723	.6425	.0156	. 1534	. 8465	57	48
16	4	. 7479	. 2521	.7210	. 7753	.6329	.0156	. 1539	. 8460	56	44
20	5	17508	.82492	5.7117	.17783	5.6234	1.0157	.01544	.98455	55	40
24	6 7	. 7537 . 7565	. 2463 . 2435	.7023 .6930	. 7813	.6140	.0157	1550	. 8450	54	36
28 32	8	. 7594	2406	.6838	. 7843 . 7873	.6045	.0158	. 1555	8445	53	32 28
36	9	. 7622	2377	.6745	7903	.5857	.0159	. 1565	8435	52 51	24
40	10	.17651	.82349	5.6653	.17933	5.5764	1.0159	.01570	.98430	50	20
44	11	. 7680	. 2320	.6561	. 7963	.5670	.0160	. 1575	8425	49	16
48	12	. 7708	. 2291	.6470	. 7993	.5578	.0160	. 1580	8419	48	12
52	13	. 7737	. 2263	.6379	. 8023	.5485	.0161	. 1585	. 8414	47	8
56	14	. 7766	. 2234	.6288	. 8053	.5393	.0162	. 1591	. 8409	46	4
41	15	.17794	.82206	5.6197	.18083	5.5301	1.0162	.01596	.98404	45	19
4	16	. 7823	. 2177	.6107	. 8113	.5209	.0163	. 1601	. 8399	44	56
8	17	. 7852	. 2148	.6017	. 8143	.5117	.0163	1606	. 8394	43	52
12 16	18 19	. 7880	. 2120	.5928 .5838	. 8173 . 8203	.5026 .4936	.0164	. 1611	. 8388	42 41	48 44
20	20	.17937	.82062	5.5749	.18233	5.4845	1.0165	.01622	.98378	40	40
24	21	. 7966	. 2034	.5660	. 8263	.4755	.0165	. 1627	8373	39	36
28	22	. 7995	. 2005	.5572	. 8293	.4665	.0166	1632	8368	38	32
32	23	. 8023	. 1977	.5484	. 8323	.4575	.0166	. 1638	8362	37	28
36	24	. 8052	. 1948	.5396	. 8353	.4486	.0167	. 1643	. 8357	36	24
40	25	.18080	.81919	5.5308	.18383	5.4396	1.0167	.01648	.98352	35	20
44	26	. 8109	. 1891	.5221	. 8413	.4308	.0168	. 1653	. 8347	34	16
48	27	. 8138	. 1862	.5134	. 8444	.4219	.0169	. 1659	. 8341	33	12
52	28	. 8166	. 1834	.5047 .4960	8474	.4131	.0169	. 1664	. 8336	32 31	8 4
56 42	29 30.	. 8195 .18223	. 1805	5.4874	. 8504 .18534	.4043 5.3955	.0170 1.0170	. 1669	. 8331	30	18
4	31	. 8252	. 1748	.4788	. 8564	.3868	.0171	1680	. 8320	29	56
8	32	. 8281	: 1719	.4702	. 8594	.3780	.0171	. 1685	. 8315	28	52
12	33	. 8309	. 1691	.4617	. 8624	.3694	.0172	. 1690	. 8309	27	48
16	34	. 8338	. 1662	.4532	. 8654	.3607	.0172	. 1696	. 8304	26	44
20	35	.18366	.81633	5.4447	.18684	5,3521	1.0173	.01701	,98299	25	40
24	36	. 8395	. 1605	.4362	. 8714	.3434	.0174	. 1706	. 8293	24	36
28	37	. 8424	. 1576	.4278	. 8745	.3349	.0174	. 1712	. 8288	23 22	32 28
32	38	. 8452 . 8481	. 1548	.4194 .4110	. 8775	.3263 .3178	.0175	. 1717	. 8283 . 8277	21	24
36 40	39 40	. 8481	.81490	5.4026	.18835	5.3093	1.0176	.01728	.98272	20	20
44	41	. 8538	. 1462	.3943	. 8865	.3008	.0176	. 1733	8267	19	16
48	42	. 8567	1433	.3860	. 8895	.2923	.0177	1739	8261	18	12
52	43	. 8595	. 1405	.3777	. 8925	.2839	.0177	. 1744	. 8256	17	8
56	44	. 8624	. 1376	.3695	. 8955	.2755	.0178	. 1749	. 8250	16	4
43	45	.18652	.81348	5.3612	18985	5.2671	1.0179	.01755	.98245	15	17
4	46	. 8681	. 1319	.3530	9016	.2588	.0179	. 1760	8240	14	56
8	47	8709	. 1290 . 1262	.3449 .3367	. 9046	.2505	.0180	. 1766 . 1771	. 8234 . 8229	13 12	52 48
12 16	48 49	. 8738 . 8767	. 1233	.3286	. 9106	.2339	.0180	1777	. 8223	11	44
20	50	.18795	.81205	5.3205	.19136	5.2257	1.0181	.01782	.98218	10	40
24	51	. 8824	. 1176	.3124	. 9166	.2174	.0182	. 1788	. 8212	9	36
28	52	. 8852	. 1147	.3044	. 9197	.2092	.0182	. 1793	. 8207	8	32
32	53	. 8881	. 1119	.2963	. 9227	.2011	.0183	. 1799	. 8201	7	28
36	54	. 8909	. 1090	.2883	. 9257	.1929	.0184	. 1804	. 8196	6	24
40	55	.18938	.81062	5.2803	.19287	5.1848	1.0184	.01810	.98190	5	20
44	56	. 8967	. 1033	.2724	. 9317	.1767	.0185	. 1815	. 8185	4	16
48	57	8995	. 1005	.2645	. 9347 . 9378	.1686	.0185 .0186	. 1821 . 1826	. 8179 . 8174	$\begin{bmatrix} 3 \\ 2 \end{bmatrix}$	$\frac{12}{8}$
52 56	58 59	9024	. 0976	.2566 .2487	. 9408	.1606 .1525	.0186	. 1832	. 8168	1	4
44	60	9081	. 0919	.2405	. 9438	.1445	.0187	. 1837	. 8163	0	16
M.S.	M	Cosine.	Vrs. Sin.				Cosec'nt		Sine.	M	M.S.
	100°)			Nati	ıral.				79°	$5^{\rm h}$
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	1									-	1
C _p	11°	· · · · · · · · · · · · · · · · · · ·	Natur	al Trig	onom	etrical	Fun	ctions		168°	11h
M.S.	M	Sine.	1	Cosec'nte		Cotang.		Vrs. Sin		_	M.S.
44	0	.19081	.80919	5.2408 .2330	.19438 . 9468	5.1445	1.0187	.01837	.98163	60 59	16 56
8	2	9138	. 0890	.2252	. 9498	.1286	.0188	1848	8152	58	52
12	3	. 9166	. 0833	.2174	. 9529	.1207	.0189	. 1854	. 8146	57	48
16 20	4 5	. 9195	. 0805	.2097	. 9559	.1128	.0189	1. 1859	8140	56	44
24	6	.19224	.80776	5.2019	. 19589	5.1 049 .0970	1.0190	.01865	.98135	55 54	40 36
28	7	. 9281	0719	.1865	9649	.0892	.0191	1876	8124	53	32
32	8	. 9309	. 0691	1788	. 9680	.0814	.0192	. 1882	. 8118	52	28
36	9	. 9338	. 0662	.1712 5.1636	. 9710 .19740	.0736 5.0658	.0192 1.0193	. 1887	. 8112	51 50	24 20
41	11	. 9395	. 80634	.1560	. 9770	.0581	.0193	1899	. 8101	49	16
48	12	. 9423	. 0576	.1484	. 9800	.0504	.0194	. 1904	. 8095	48	12
52 56	13 14	. 9452	. 0548	.1409	. 9831	.0427	.0195	. 1910	. 8090	47	8
45	15	. 9480	. 0519	.1333 5.1258	. 9861	.0350 5.0273	0.0195 1.0196	. 1916	. 8084	46	4 15
4	16	. 9537	. 0462	.1183	. 9921	.0197	.0196	. 1927	. 8073	44	56
8	17	. 9566	. 0434	.1109	. 9952	.0121	.0197	. 1933	. 8067	43	52
12 16	18 19	. 9595	. 0405	.1034	9982	.0045	.0198	. 1938	. 8061	42	48
20	20	. 9623 .19652	.80348	.0960 5.0886	.20012	4.9969 4.9894	.0198	. 1944 .01950	. 8056	41 40	44 40
24	21	. 9680	. 0320	.0812	. 0073	.9819	.0199	. 1956	. 8044	39	36
28	22	. 9709	. 0291	.0739	. 0103	.9744	.0200	. 1961	. 8039	38	32
32 36	$\begin{vmatrix} 23 \\ 24 \end{vmatrix}$	9737	. 0263	.0666 .0593	. 0133	.9669 .9594	.0201	. 1967 . 1973	. 8033 . 8027	37 36	28 24
40	25	.19794	.80206	5.0520	.20194	4.9520	1.0202	.01979	.98021	35	20
44	26	. 9823	. 0177	.0447	. 0224	.9446	.0202	. 1984	. 8016	34	16
48 52	$\begin{vmatrix} 27 \\ 28 \end{vmatrix}$. 9851	. 0149	.0375	. 0254	.9372 .9298	.0203	. 1990	. 8010	33	12
56	29	. 9880	. 0120	.0302	. 0285	.9225	.0204	. 1996	. 8004	32 31	8 4
46	30	.19937	.80063	5.0158	.20345	4.9151	1.0205	.02007	.97992	30	14
4	31	. 9965	. 0035	.0087	. 0375	.9078	.0205	. 2013	. 7987	29	56
8 12	32 33	. 9994	. 0006 .79978	.0015 4.9944	. 0406	.9006 .8933	.0206	. 2019	. 7981 . 7975	28 27	52 48
16	34	.20051	.79949	4.9873	. 0466	.8860	.0207	2031	7969	26	44
20	35	.20079	.79921	4.9802	.20497	4.8788	1.0208	.02037	.97963	25	40
24 28	36 37	. 0108	. 9892	.9732 .9661	. 0527	.8716 .8644	.0208	. 2042	. 7957 . 7952	$\begin{array}{c} 24 \\ 23 \end{array}$	36 32
32	38	. 0165	. 9863 . 9835	.9591	. 0588	.8573	.0209	. 2054	7946	22	28
36	39	. 0193	. 9807	.9521	. 0618	.8501	.0210	. 2060	7940	21	24
40	40	.20222	.79778	4.9452	.20648		1.0211	.02066	.97934	20	20
44 48	$\begin{array}{ c c }\hline 41\\ 42\\ \end{array}$	0250 0279	. 9750 . 9721	.9382 .9313	. 0679	.8359 .8288	.0211	. 2072	. 7928 . 7922	19 18	16 12
52	43	. 0307	9693	.9243	. 0739	.8217	.0212	2084	7916	17	8
56	44	. 0336	. 9664	.9175	. 0770	.8147	.0213	. 2089	. 7910	16	4
47	45	.20: 64	.79636	4.9106	.20800	4.8077	1.0214	.02095	.97904	15	13
8	46 47	. 0393	. 9607 . 9579	.9037 .8969	. 0830	.8007 .7937	.0215 .0215	. 2101 . 2107	. 7899 . 7893	14 13	56 52
12	48	. 0450	. 9550	.8901	. 0891	.7867	.0216	. 2113	. 7887	12	48
16	49	. 0478	. 9522	.8833	. 0921	.7798	.0216	. 2119	. 7881	11	44
20 24	50 51	.20506 . 0535	.79 49 3 . 9 4 65	4.8765 .8697	.20952	4.7728 .7659	1.0217 .0218	.02125	.97875 . 7869	10 9	40 36
28	52	. 0563	. 9436	.8630	. 1012	.7591	.0218	. 2137	7863	8	32
32	53	. 0592	. 9408	.8563	. 1043	.7522	.0219	. 2143	. 7857	7	28
36	54	. 0620	. 9379	.8496	. 1073	.7453	.0220	. 2149	. 7851	6	24
40	55 56	.20649	.79351 . 9323	4.8429 .8362	. 21104	4.7385 .7317	1.0220	02155 2161	.97845	5 4	20
48	57	. 0706	. 9294	.8296	. 1164	.7249	.0221	. 2167	. 7833	3	12
52	58	. 0734	. 9266	.8229	. 1195	.7181	.0222	. 2173	. 7827	2	8
56 4 -8	59 60	. 0763	. 9237 . 9209	.8163 .8097	. 1225	.7114 .7046	.0223	. 2179	. 78 21 . 7815	$\begin{bmatrix} 1 \\ 0 \end{bmatrix}$	12
M. S.	M	Cosine.	Vrs.Sin.			Tangent.		Vrs. Cos	Sine.	M	M.S.
6h	101)			Natu	ral.				78°	5 ^h
-											

	NATURAL LINES. 2										
0h.	12°		Natura	al Trig	gonom	etrical	Func	ctions.]	67°	11h
M.S.	M			Cosec'nte	_	Cotang.	Secante.	Vrs.Sin	Cosine.	M	M.S.
4月	1	.20791	.79209	4.8097	.21256	4.7046	1.0223	.02185	.97815	60	12
8	$\frac{1}{2}$. 0820	. 9180	.8032	. 1286	.6979	.0224	. 2191	. 7809	59	56
12	3	. 0848	. 9152	.7966 .7901	. 1316	.6912	.0225	. 2197	÷ 7803	58	52
16	4	. 0905	. 9125	.7835	. 1347	.6845	.0225	. 2203	. 7866	57 56	48 44
20	5	.20933	.79066	4.7770	.21408	4.6712	1.0226	.02215	.97784	55	40
24	6	. 0962	. 9038	.7706	. 1438	.6646	.0227	. 2222	. 7778	54	36
28	7	. 0990	. 9010	.7641	. 1468	.6580	.0228	. 2228	. 7772	53	32
32 36	8 9	. 1019	. 8981		. 1499	.6514	.0228	. 2234	. 7766	52	28
40	10	. 1047	8953	.7512	. 1529	.6448	.0229	. 2240	. 7760	51	24
44	111	. 1104	. 78924	4.7448	.21560	4.6382	1.0230 .0230	.02246	. 97754	50 49	20 16
48	12	. 1132	. 8867	.7320	. 1621	.6252	.0231	2258	. 7741	48	12
52	13	. 1161	. 8839	.7257	. 1651	.6187	.0232	. 2264	7735	47	8
56	14	. 1189	. 8811	.7193	. 1682	.6122	.0232	. 2271	. 7729	46	4
49	15	.21218	.78782	4.7130	.21712	4.6057	1.0233	.02277	.97723	45	11
4 8	16 17	. 1246	. 8754	.7067	. 1742	.5993	.0234	. 2283	. 7717	44	56
12	18	. 1275	8725	.7004 .6942	. 1773	.5928	.0234	. 2289	. 7711	43	52
16	19	. 1331	8668	.6879	. 1834	.5864	.0235	. 2295 . 2302	. 7704 . 7698	42 41	48 44
20	20	.21360	.78640	4.6817	.21864	4.5736	1.0236	.02308	.97692	40	40
24	21	. 1388	. 8612	.6754	. 1895	.5673	.0237	. 2314	. 7686	39	36
28	22	. 1417	. 8583	.6692	. 1925	.5609	.0237	. 2320	. 7680	38	32 .
32	23	. 1445	. 8555	.6631	. 1956	.5546	.0238	. 2326	. 7673	37	28
36 40	24	. 1473	. 8526	.65(9	. 1986	.5483	.0239	2333	7667	36	24
44	25 26	.21502 . 1530	.78508	4. 6507 . 6446	.22017	4.5420	1.0239 .0240	.02339	. 7655	35 34	20 16
48	27	. 1559	8441	.6385	2078	.5294	.0240	2351	. 7648	33	12
52	28	. 1587	8413	.63:24	2108	.5232	.0241	2358	. 7642	32	8
56	29	. 1615	. 8384	.6263	. 2139	.5169	.0242	. 2364	. 7636	31	4
50	30	.21644	.78356	4.6202	.22169	4.5107	1.0243	.02370	.97630	30	10
4	31	. 1672	. 8328	.6142	. 2200	.5045	.0243	. 2377	. 7623	29	56
8 12	32 33	. 1701 . 1729	. 8299 . 8271	.6081 .6021	. 2230 . 2261	.4983 .4921	.0244	. 2383 . 2389	. 7617 . 7611	28 27	52 48
16	34	. 1757	8242	.5961	. 2291	.4860	.0245	2396	7604	26	44
20	35	.21786	78214	4.5901	.22322	4.4799	1.0246	.02402	.97598	$\frac{1}{25}$	40
24	36	. 1814	. 8186	.5841	. 2353	.4737	.0247	. 2408	. 7592	24	36
28	37	. 1843	. 8154	.5782	. 2383	.4676	.0247	. 2415	. 7585	23	32
32	38	. 1871	. 8129	.5722	. 2414	.4615	.0248	. 2421	. 7579	22	28
36	39 40	. 1899 .21928	. 8100 .78072	.5663 4.5604	. 2444	.4555 4.4494	.0249 1.0249	. 2427	. 7573	21 20	24 20
44	41	. 1956	. 8043	.5545	. 2505	.4434	.0249	. 2440	. 7560	19	16
48	42	. 1985	8015	.5486	2536	.4373	.0251	. 2446	. 7553	18	12
52	43	. 2013	. 7987	.5428	. 2566	.4313	.0251	. 2453	. 7547	17	8
56	44	. 2041	. 7959	.5369	. 2597	.4253	.0252	: 2459	. 7541	16	4
51	45	.22070	.77930	4.5311	.22628	4.4194	1.0253	.02466	.97534	15	9
8	46	. 2098	. 7902 . 7873	.5253 .5195	2658. 2689	.4134 .4074	.0253 .0254	. 2472 . 2479	. 7528 . 7521	14 13	56 52
12	47 48	. 2126	7845	.5137	. 2089	.4014	.0255	. 2485	. 7515	12	48
16	49	. 2183	7817	.5079	2750	.3956	.0255	2491	7508	11	44
20	50	.22211	.77788	4.5021	.22781	4.3897	1.0256	.02498	.97502	10	40
24	51	. 2240	. 7760	.4964	. 2811	.3838	.0257	. 2504	. 7495	9	36
28	52	. 2268	. 7732	.4907	. 2842	.3779	.0257	. 2511	. 7489	8	32
32 36	53 54	. 2297 . 2325	. 7703 . 7675	.4850 .4793	. 2872	.3721 .3662	.0258 .0259	. 2517	. 7483 . 7476	7 6	28 2±
40	55	.22353	.77647	4.4736	.22934	4,3604	1.0260	.02530	.97470	5	20
41	56	. 2382	. 7618	.4679	. 2964	.3546	.0260	2537	. 7463	4	16
48	57	. 2410	. 7590	.4623	. 2995	.3488	.0261	. 2543	. 7457	3	12
52	58	. 2438	. 7561	.4566	. 3025	.3430	.0262	. 2550	. 7450	2	8
56	59	. 2467	. 7533	.4510	3056	.3372	.0262	. 2556	7443	1	4
52 M. S.	60 M	. 2495 Cosine.	. 7505 Vrs. Sin.	.4454 Secante.	. 3087	.3315 Tangent.	.0263 Cosecint	. 2563 Vrs. Cos	. 7437 Sine.	0 I	M.S
	102)	113.0111.0	Schauto.	Natu		J., J.C. H. I	. 20.008	D.HC.	770	
	204				Trattl	rat.				-	

NATURAL LINES.														
0^{h}	139)	Natur	al Trig	gonom	etrica	l Fun	ctions	.]	166°	11h			
W.S.	M	Sine.	Vrs. Cos.	Cosec'nte	Tang.	Cotang.	Secante.	Vrs. Sin	Cosine.	1 M	M.S.			
53	0	.22495	.77505	4.4454	.23087	4.3315	1.0263	.02563	.97437	60	8			
+	1	. 2523	. 7476	.4398	. 3117	.3257	.0264	2569	. 7430	59	56			
8	2	. 2552	. 7448	.4342	. 3148	.3200	.0264	. 2576	. 7424	58	52			
12	3	. 2580	. 7420	.4287	. 3179	.3143	.0265	2583	. 7417	57	48			
16	4	. 2608	. 7391	.4231	. 3209	.3086	.0266	. 2589	. 7411	56	44			
20	5	.22637	.77363	4.4176	.23240	4.3029	1.0266	.02596	.97404	55	-40			
24	6	. 2665	. 7335	.4121	. 3270	.2972	.0267	. 2602	. 7393	54	36			
28	7	. 2693	. 7306	.4065	. 3301	.2916	.0268	. 2609	. 7391	53	32			
32	8	. 2722	. 7278	.4011	. 3332	.2859	.0268	. 2616	. 7384	52	28			
36	9	. 2750	. 7250	.3956	. 3363	.2803	.0269	. 2622	. 7378	51	24			
40	10	.22778	.77221	4.3901	.23393	4.2747	1.0270	.02629	.97371	50	20			
44	11	. 2807	. 7193	.3847	. 3124	.2691	.0271	. 2635	. 7364	49	16			
48	12	. 2835	. 7165	,3792	. 3455	.2635	.0271	. 2642	. 7358	48	12			
52	13	. 2863	. 7136	.3738	. 3485	.2579	.0272	. 2649	. 7351	47	8			
56	14	. 2892	. 7108	.3684 4.3630	. 3516	.2524	.0273	.2555 $.02662$. 7344	46 45	4			
53	15	.22920	.77080	.3576	.23547	4.2468	1.0273	2669	.97338	44	50			
8	16 17	. 2948	7023	.3522	3608	.2358	.0274	2675	7324	43	52			
12	18	3005	6995	.3469	3639	.2303	.0276	2682	7318	42	48			
16	19	. 3033	. 6967	.3415	3670	.2248	.0276	2689	7311	41	44			
20	20	.23061	.76938	$\cdot 4.3362$.23700	4.2193	1.0277	.02695	.97304	40	4.)			
24	21	. 3090	. 6910	.3309	. 3731	.2139	.0278	2702	7298	39	36			
- 28	22	. 3118	. 6882	.3256	. 3762	2084	.0278	2709	7291	38	32			
	32 23 . 3146 . 6853 . 3203 . 3793 .2030 .0279 . 2716 . 7284 37 28													
36	24	. 3175	. 6825	.3150	. 3823	.1976	.0280	2722	. 7277	36	24			
40	25	.23203	.76797	4.3098	.23854	4.1921	1.0280	02729	.97271	35	20			
44	26	. 3231	. 6769	.3045	. 3885	.1867	.0281	2736	. 7264	34	16			
48	27	. 3260	. 6740	.2993	. 3916	.1814	.0282	. 2743	. 7257	33	12			
52	28	. 3288	. 6712	.2941	. 3946	.1760	.0283	. 2749	. 7250	32	8			
56	29	. 3316	. 6684	.2888	. 3977	.1706	.0283	. 2756	. 7244	31	Ŧ			
54	30	.23344	.76655	4.2836	.24008	4.1653	1.0284	.02763	.97237	. 30	6			
4	31	. 3373	. 6627	.2785	. 4039	.1600	.0285	. 2770	7230	29	56			
8	32	. 3401	. 6599	.2733	. 4069	.1546	.0285	2777	. 7223	28	52			
12	33	. 3429 . 3458	. 6571 . 6542	.2681 .2630	. 4100	.1493	.0286	2783 2790	. 7216 . 7210	27 26	48 44			
16 20	34 35	.23486	.76514	4.2579	.24162	.1440 4.1388	0.0287 1.0288	02797	.97203	25	40			
24	36	. 3514	. 6486	.2527	. 4192	.1335	.0288	2804	. 7196	24	36			
28	37	. 3542	6457	.2476	. 4223	.1282	.0289	2811	. 7189	23	32			
32	38	3571	6429	.2425	. 4254	.1230	.0290	2818	7182	22	28			
36	39	. 3599	. 6401	.2375	. 4285	.1178	.0291	2824	7175	21	24			
40	40	.23627	.76373	4.2324	.24316	4.1126	1.0291	.02831	.97169	20	20			
44	41	. 3655	. 6344	.2273	. 4346	.1073	.0292	. 2838	. 7162	19	16			
48	42	. 3684	. 6316	.2223	. 4377	.1022	.0293	. 2845	. 7155	18	12			
52	43	. 3712	. 6288	.2173	. 4408	.0970	.0293	. 2852	. 7148	17	8			
56	44	. 3740	. 6260	.2122	. 4439	.0918	.0294	2859	. 7141	16	4			
55	45	.23768	.76231	4.2072	.24470	4.0867	1.0295	.02866	.97134	15	5			
4	46	. 3797	. 6203	.2022	. 4501	.0815	.0296	. 2873	. 7127	14	56			
8	47	. 3825	. 6175	.1972	4531	.0764	.0296	. 2880	. 7120	13	52			
12	48	. 3853	6147	.1923 .1873	4562	.0713	.0297	. 2886	. 7113	12	48			
16 20	49 50	. 3881	. 6118 .76090	$\frac{.1873}{4.1824}$. 4593	.0662 4.0611	0.0298 1.0299	. 2893	. 7106 .97099	11	44			
$\begin{vmatrix} 20 \\ 24 \end{vmatrix}$	51	. 3938	. 6062	.1774	. 4655	.0560	.0299	.02900	. 7092	$\begin{vmatrix} 10 \\ 9 \end{vmatrix}$	40 36			
28	52	3966	6034	.1725	4686	.0509	.0300	2914	7086	8	32			
32	53	3994	6005	.1676	4717	.0458	.0301	2921	7079	7	28			
36	54	. 4023	5977	.1627	4747	.0408	.0302	2928	7072	6	24			
40	55	.24051	.75949	4.1578	.24778	4.0358	1.0302	.02935	.97065	5	$\begin{vmatrix} 24 \\ 20 \end{vmatrix}$			
44	56	. 4079	. 5921	.1529	4809	.0307	.0303	2942	7058	4	16			
48	57	. 4107	. 5892	.1481	. 4840	.0257	.0304	. 2949	. 7051	3	12			
52	58	. 4136	. 5864	.1432	. 4571	.0207	.0305	. 2956	. 7044	2	8			
56	59	. 4164	. 5836	.1384	. 4902	.0157	.0305	. 2963	. 7037	1	4			
56	60	. 4192	. 5808	.1336	4933	.0108	.0306	. 2970	. 7029	0	4			
M.S.	M 109	Cosme.	vrs. Sin.	Secante.		Tangent.	Cosec'nt l	Vrs.Cos	Sine.	M	M.S.			
6h	103				Nati	ıral.				76°	5 ^h			

6							THE THE	~·····································				24
1	$0^{\rm h}$	140		TRT 4	3 00 1					**	1000	1176
		1.2			al Trig			LEune	ctions.	-	100	11h
Ì	M.S. 56	M	Sine.		Cosec'nte)	Vrs. Sin	Cosine.	M	M.S.
ı	4	0	.24192	.75808	4.1336	.24933	4.0108	1.0306	.02970	.97029		4
	8	2	. 4220	5779	.1287	. 4964	.0058	.0307	. 2977	. 7022	59	56
	12	3	. 4243	. 5723	.1191	. 4995	.0009	.0308	. 2984	7015	58	52
	16	4	4305	. 5695	.1144	. 5056	3.9910	.0309	2999	7008	57 56	48
1	20	5	.24333	.75667	4.1096	.25087	3.9861	1.0310	.03006	.96994	£5	40
	24	6	. 4361	. 5638	.1048	. 5118	.9812	.0311	. 3013	. 6987	54	36
	28 32	8	. 4390	. 5610	.1001	. 5149	.9763	.0311	. 3020	. 6980	53	32
	36	9	. 4418	. 5582	.0953	. 5180	.9714	.0312	. 3027	. 6973	52	28
1	40	10	. 4446	. 5554	.0906 4.0859	. 5211	.9665 3.9616	.0313	. 3034	. 6966	51	24
	41	11	. 4502	5497	.0812	. 5273	.9568	1.0314	.03041	.96959	50 49	20 16
1	48	12	4531	5469	.0765	. 5304	.9520	.0315	3055	6941	48	12
1	52	13	. 4559	. 5441	.0718	. 5335	.9471	.0316	. 3063	6937	47	8
	ōΰ	14	. 4587	. 5413	.0672	. 5366	.9423	.0317	. 3070	. 6930	46	4
	57	15 16	.24615	.75385	4.0625	.25397	3.9375	1.0317	.03077	.96923	45	3
1	4 8	17	. 4643	. 5356	.0579	. 5428	.9327	.0318	. 3084	. 6916	44	56
1	12	18	. 4672	5328	.0532	. 5459	.9279	.0319	. 3091	6909	43	52
	16	19	4728	5272	.0440	. 5521	.9231 .9184	.0320	. 3106	6901	42 41	48 44
	20	20	.24756	.75244	4.0394	.25552	3.9136	1.0321	.03113	.96887	40	40
	24	21	. 4784	. 5215	.0348	. 5583	.9089	.0322	. 3120	. 6880	39	36
1	28	22	. 4813	. 5187	.0302	. 5614	.9042	.0323	. 3127	. 6873	38	32
	32	23	. 4841	. 5159	.0256	. 5645	.8994	.0323	. 3134	. 6865	37	28
	36 40	24 25	. 4869	. 5131	.0211	. 5676	.8947	.0324	. 3142	. 6858	36	24
1	44	26	.24897	.75103	4.0165	.25707	3.8900 .8853	1.0325 .0326	.03149	.96851	35 34	20 16
1	48	27	4953	. 5046	.0074	5769	.8807	.0327	. 3163	. 6836	33	12
1	52	28	4982	. 5018	.0029	. 5800	.8760	.0327	. 3171	6829	32	8
k	56	29	. 5010	. 4990	3.9984	. 5831	.8713	.0328	. 3178	. 6822	31	4
ı	58	30	.25038	.74962	3.9939	.25862	3.8667	1.0329	.03185	.96815	30	2
1	4	31	. 5066	. 4934	.9894	. 5893	.8621	.0330	. 3192	. 6807	29	56
ı	8 12	32	. 5094	4906	.9850	. 5924	.8574	.0330	. 3200	. 6800	28	52
1	16	33 34	. 5122	. 4877	.9805 .9760	59555986	.8528 .8482	.0331	. 3207	. 6793 . 6785	27 26	48 44
	20	35	.25179	.74821	3.9716	.26017	3.8436	1.0333	.03222	.96778	25	40
	24	36	. 5207	4793	.9672	. 6048	.8390	.0334	. 3229	. 6771	24	36
1	28	37	. 5235	. 4765	.9627	. 6079	.8345	.0334	. 3236	. 6763	23	32
	32	38	. 5263	. 4737	.9583	. 6110	.8299	.0335	. 3244	. 6756	22	28
1	36	39	. 5291	4709	.9539	. 6141	.8254	.0336	. 3251	6749	21	24
	40	40	.25319	. 4652	3.9495 .9451	.26172 . 6203	3.8208 .8163	1.0337 .0338	.03258 . 3 2 66	. 96741	20	$\begin{array}{c c} 20 \\ 16 \end{array}$
	48	42	5376	. 4624	.9408	6234	.8118	.0338	. 3273	6727	18	12
1	52	43	. 5404	4596	.9364	6266	.8073	.0339	. 3281	6719	17	8
	56	44	. 5432	. 4568	.9320	. 6297	.8027	.0340	. 3288	. 6712	16	4
	59	45	.25460	.74540	3.9277	.26328	3.7983	1.0341	.03295	.96704	15	L
1	4	46	. 5488	. 4512	.9234	. 6359	.7938	.0341	. 3303	. 6697	14	56
1	8	47	. 5516	. 4483	.9190	. 6390	.7893 .7848	.0342	. 3310	. 6690	13 12	52
	12 16	48 49	. 5544 . 5573	. 4455 . 4427	.9147 .9104	6452	.7804	.0343	. 3325	. 6675	11	48 44
	20	50	25601	.74399	3.9061	.26483	3.7759	1.0345	.03332	.96667	10	40
	24	51	. 5629	. 4371	.9018	. 6514	.7715	.0345	. 3340	. 6660	9	36
	28	52	. 5657	. 4344	.8976	. 6546	.7671	.0346	. 3347	. 6652	8	32
1	32	53	. 5685	. 4315	.8933	. 6577	.7627	.0347	. 3355	. 6645	7	28
	36	54	. 5713	. 4287	.8890	. 6608	.7583	.0348	. 3362	. 6638	6	24
	40 44	55 56	.25741	.74259	3.8848	. 6670	3.7539	1.0349	.03370	.96630	5 4	20 16
1	48	56 57	. 5769 . 5798	$\begin{array}{c} \cdot 4230 \\ \cdot 4202 \end{array}$.8805 .8763	6701	.7451	.0350	. 3385	. 6623 . 6615	3	12
	52	58	. 5826	. 4174	.8721	6732	.7407	.0351	3392	. 6018	2	8
	56	59	5854	4146	.8679	. 6764	.7304	.0352	. 3400	. 6600	ī	4
	60	60	. 5882	. 4118	.8637	. 6795	.7320	.0353	. 3407	. 6592	0	0
	M.S.	M (Cosine.	Vrs.Sin.	Secante.			Cosec'nt	Vrs. Cos	Sine.		M.S.
	6h	104°				Natu	ral.				75°	5 ^h
-												

-											
1	h 15	0	Natur	al Triç	conon	etrica	l Fun	ctions		164°	101
75				Cosec'nte							-
M.	ď			3.8637	Tang26795	Cotang. 3.7320	1.0353	Vrs. Sin	.96592	60	M.S 60
0	$\begin{bmatrix} 0 \\ 1 \end{bmatrix}$.25882	.74118 .4090	.8595	. 6826	.7277	.0353	. 3415	. 6585	59	56
	$\frac{1}{3}$ $\frac{1}{2}$	5938	4062	.8553	6857	7234	.0354	3422	6577	58	52
1		5966	. 4034	.8512	6888	.7191	.0355	3430	6570	57	48
1		5994	4006	.8470	6920	.7147	.0356	3438	6562	56	44
20	_	.26022	.73978	3.8428	.26951	3.7104	1.0357	.03445	.96555	55	40
2		. 6050	. 3949	.8387	. 6982	.7062	.0358	. 3453	. 6547	54	36
2		. 6078	. 3921	.8346	. 7013	.7019	.0358	. 3460	. 6540	53	32
39	2 8	. 6107	. 3893	.8304	. 7044	.6976	.0359	. 3468	6532	52	28
30		. 6135	. 3865	.8263	. 7076	.6333	.0360	. 3475	. 6524	51	24
40		.26163	.73837	3.8222	.27107	3.6891	1.0361	.03483	.96517	50	20
44		6191	. 3809	.8181	. 7138	.6848	.0362	. 3491	6509	49	16
43		. 6219	. 3781	.8140	. 7169	.6806	.0362	. 3498	. 6502	48	12
55		. 6247	. 3753	.8100	7201	.6764	.0363	3506	. 6494	47	8 4
50		. 6275	. 3725	.8059 3.8018	. 7232	.6722 3.6679	.0364 1.0365	. 3514	. 6486	46 45	59
1		. 6331	. 3669	.7978	. 7294	.6637	.0366	. 3529	. 6471	44	56
1 8		6359	. 3641	.7937	7326	.6596	.0367	3536	6463	43	52
13		6387	. 3613	.7897	7357	.6554	.0367	3544	6456	42	48
16		6415	. 3585	.7857	. 7388	.6512	.0368	3552	6448	41	44
20		.26443	.73556	3.7816	.27419	3.6470	1.0369	.02560	.96440	40	40
24		. 6471	. 3528	.7776	. 7451	.6429	.0370	. 3567	. 6433	39	36
28		. 6499	. 3500	.7736	. 7482	.6387	.0371	. 3575	. 6425	38	32
32		. 6527	. 3472	.7697	. 7513	.6346	.0371	. 3583	. 6417	37	28
36		6556	. 3444	.7657	. 7544	.6305	.0372	. 3590	. 6409	36	24
4(.26584	.73416	3.7617	.27576	3.6263	1.0373	.03598	.96402	35	20
44		. 6612	. 3388	.7577	7607	.6222	.0374	. 3606	. 6394	34	16
48		. 6640	. 3360	.7538	7638	.6181	.0375	. 3614	. 6386	33	12
52		. 6668	. 3332	.7498 .7459	. 7670	.6140	.0376	. 3621 . 3629	. 6378	32 31	8
50		.26724	.73276	3.7420	.27732	3.6059	1.0377	.03637	.96363	30	58
1 4		. 6752	. 3248	.7380	. 7764	.6018	.0378	3645	. 6355	29	56
1 3		6780	. 3220	.7341	7795	.5977	.0379	. 3652	6347	28	52
12		. 6803	. 3192	.7302	. 7826	.5937	.0380	. 3660	. 6340	27	48
10		. 6836	. 3164	.7263	. 7858	.5896	.0381	. 3668	. 6332	26	44
20	35	.26864	.73136	3.7224	.27889	3.5856	1.0382	.03676	.96324	25	40
24		. 6892	. 3108	.7186	. 7920	.5816	.0382	. 3684	. 6316	24	36
28		. 6920	. 3080	.7147	. 7952	.5776	.0383	. 3691	. 6308	23	32
32		. 6948	. 3052	.7108	. 7983	.5736	.0384	. 3699	. 6301	22	28
36		6976	3024	.7070	. 8014	.5696	.0385	. 3707	. 6293	21	24
40		.27004	.72996	3.7031 .6993	. 8077	3.5656	1.0386	.03715	.96285	20	20
44		. 7032	2940	.6955	. 8109	.5576	.0387	. 3723 . 3731	. 6277	19 18	16 12
52		7088	. 2912	.6917	. 8140	.5536	.0388	. 3739	. 6261	17	8
50		7116	2884	.6878	. 8171	.5497	.0389	3746	6253	16	4
3		.27144	.72856	3.6840	.28203	3.5457	1.0390	.03754	.96245	15	57
4		. 7172	. 2828	.6802	. 8234	.5418	.0391	. 3762	. 6238	14	56
8	47	. 7200	. 2800	.6765	. 8266	.5378	.0392	. 3770	. 6230	13	52
12		. 7228	. 2772	.6727	. 8297	.5339	.0393	. 3778	. 6222	12	48
10		. 7256	. 2744	.6689	. 8328	.5300	.0393	. 3786	. 6214	11	44
20		.27284	.72716	3,6651	.28360	3.5261	1.0394	.03794	.96206	10	40
24		7312	2688	.6614	. 8391	.5222	.0395	. 3802	. 6198	9	36
28		7340	2660	.6576	. 8423	.5183	.0396	. 3810	6190	8	32
32 36		. 7368	. 2632 . 2604	.6539 .6502	. 8454 . 8486	.5144 .5105	.0397 .0398	. 3818 . 3826	6182	7	28 24
40		.27424	.72576	3.6464	.28517	3.5066	1.0399	.03824	. 6174	6 5	20
44		7452	. 2548	.6427	. 8549	.5028	.0399	. 3842	. 6158	4	16
48		. 7480	. 2520	.6390	. 8580	.4989	.0400	3850	. 6150	3	12
52		7508	2492	.6353	. 8611	.4951	.0401	3858	6142	2	8
56	59	. 7536	. 2464	.6316	. 8643	.4912	.0402	. 3866	. 6134	1	4
4	60	. 7564	. 2436	.6279	. 8674	.4874	.0403	. 3874	. 6126	0	56
M.S	3. M	Cosine.	Vrs. Sin.	Secante.		Tangent.	Cosec'nt	Vrs.Cos	Sine.	M	M.S.
7h	1105				Natr	ıral.				74°	4h
-	-										

-											
1 h	16°	,	Madana	d Trig	AT	otutool	III.	+ 1.0	1	.63°	10h
M.S.	M ()	Sine27564	Vrs.Cos. .72436	Cosec'nte 3.6279	Tang28674	Cotang.		ă .	Cosine.	8	M.S.
4	1	. 7592	. 2408	.6243	. 8706	3.4874	1.0403 .0404	.03874	.96126	60 59	56 56
8	2	7620	. 2380	.6206	. 8737	.4798	.0405	. 3890	6110	58	52
12	3	. 7648	. 2352	.6169	. 8769	.4760	.0406	. 3898	. 6102	57	48
16	4	. 7675	. 2324	.6133	. 8800	.4722	.0406	. 3906	. 6094	56	44
20 24	5 6	.27703	.72296	3.6096	.28832	3.4684	1.0407	.03914	.96086	55	40
28	7	. 7731	. 2268 . 2240	.6060 .6024	. 8863 . 8895	.4646	.0408 .0409	. 3922 . 3930	. 6078	54 53	$\begin{array}{c c} 36 \\ 32 \end{array}$
32	8	. 7787	. 2213	.5987	8926	.4570	.0410	. 3938	. 6062	52	28
36	9	. 7815	. 2185	.5951	. 8958	.4533	.0411	. 3946	. 6054	51	24
40	10	.27843	.72157	3.5915	.28990	3.4495	1.0412	.03954	.96045	50	20
44 48	11 12	. 7871	. 2129	.5879	. 9021	.4458	.0413	. 3962	6037	49	16
52	13	. 7927	2101 . 2073	.5843 .5807	. 9053 . 9084	.4420 .4383	.0413	. 3971 . 3979	6029	48 47	12 8
56	14	7955	. 2045	.5772	9116	.4346	.0415	. 3987	. 6013	46	4
5	15	.27983	.72017	3.5736	.29147	3.4308	1.0416	.03995	.96005	45	55
4	16	. 8011	. 1989	.5700	. 9179	.4271	.0417	. 4003	. 5997	44	56
8 12	17 18	. 8039	. 1961	.5665	. 9210	.4234	.0418	. 4011	. 5989	43	52
16	19	. 8067 . 8094	. 1933	.5629 .5594	. 9242	.4197 .4160	.0419	. 4019	. 5980	42 41	48 44
20	20	.28122	.71877	3.5559	.29305	3.4124	1.0420	.04036	.95964	40	40
24	21	. 8150	1849	.5523	. 9337	.4087	.0421	. 4044	. 5956	39	36
28	22	. 8178	. 1822	.5488	. 9368	.4050	.0422	. 4052	. 5948	38	32
32	23 24	. 8206 . 8234	. 1794	.5453	. 9400	.4014	.0423	4060	. 5940	37	28
36 40	25	.825±	. 1765	.5418 3.5383	. 9432	.3977 3.3941	.0424 1.0425	. 4069	. 5931 .95923	36 35	24 20
44	26	. 8290	1710	.5348	. 9495	.3904	.0426	. 4085	. 5915	34	16
48	27	. 8318	. 1682	.5313	. 9526	.3868	.0427	. 4093	. 5907	33	12
52	28	. 8346	. 1654	.5279	. 9558	.3832	.0428	. 4101	. 5898	32	8
56	29	. 8374	. 1626	.5244	. 9590	.3795	.0428	. 4110	. 5890	31	4 54
6 4	30 31	.28401	.71608	3.5209 .5175	.29621 . 9653	3.3759 .3723	1.0429 .0430	.04118	.95882	30 29	56
8	32	. 8457	. 1543	.5140	. 9685	.3687	.0431	. 4134	. 5865	28	52
12	33	. 8485	. 1515	.5106	. 9716	.3651	.0432	. 4143	. 5857	27	48
16	34	. 8513	. 1487	.5072	. 9748	.3616	.0433	. 4151	. 5849	26	44
20	35	.28541	.71459	3.5037	.29780	3.3580	1.0434	.04159	.95840	$\begin{array}{c c} 25 \\ 24 \end{array}$	40 36
24 28	36 37	. 8569 . 8597	. 1431 . 1403	.5003 .4969	. 9811	.354 £ .3509	.0435 $.0436$. 4168 . 4176	. 5824	23	$\frac{30}{32}$
32	38	8624	1375	.4935	. 9875	.3473	.0437	. 4184	. 5816	22	28
36	39	. 8652	. 1347	.4901	. 9906	.3438	.0438	. 4193	. 5807	21	24
4()	40	.28680	.71320	3.4867	.29938	3.3402	1.0438	.04201	.95799	20	20
44 48	41 42	. 8708	. 1292	.4833 .4799	. 9970 .30001	.3367 .3332	.0439	. 4209 . 4218	. 5791 . 5782	19 18	16 12
52	43	. 8736 . 8761	. 1236	.4766	. 0033	.3296	.0441	. 4226	. 5774	17	8
56	44	8792	1208	4732	. 0065	.3261	.0442	. 4234	. 5765	16	4
7	45	.28820	.71180	3.4698	.30096	3.3226	1.0443	04243	.95757	15	53
4	46	. 8847	. 1152	.4665	. 0128	.3191	.0444	4251	5749	14	56
8 12	47	. 8875 . 8903	. 1125	.4632 .4598	. 0160	.3156 .3121	.0445	. 4260 . 4268	. 5740 . 5732	13 12	52 48
16	48 49	. 8931	. 1069	.4565	. 0132	.3087	.0447	. 4276	. 5723	11	14
20	50	.28959	.71041	3.4532	.30255	3.3052	1.0448	.04285	.95715	10	40
24	51	. 8987	. 1013	.4498	. 0287	.3017	.0448	. 4293	. 5707	9	36
28	52	. 9014	. 0985	.4465	. 0319	.2983	0449	. 4302	. 5698	8 7	32 28
32 36	53 54	. 9042	. 0958	.4432 .4399	. 0350	.2948	.0450	. 4310	. 5690	6	$\frac{28}{24}$
40	55	.29098	.70902	3.4366	.30414	3.2879	1.0452	.04327	.95673	5	20
44	56	. 9126	. 0874	.4334	. 0446	.2845	.0453	. 4335	. 5664	4	16
48	57	. 9154	. 0846	.4301	. 0478	.2811	.0454	. 4344	. 5656	3	12
52	58	. 9181	. 0818	.4268	. 0509	.2777	.0455	4352	5647	$\frac{2}{1}$	8
56	59 60	. 9209 . 9237	. 0791	.4236 .4203	. 0541	.2742	.0456 .0 4 57	. 4361 . 4369	. 5639 . 5630	0	52
M.S.	M	Cosine.		Secante.	Cotang.	Tangent.	Cosec'nt	Vrs. Cos	Sine.	M	M.S.
7 ^h 106° Natural. 73° 4 ^h											
-	15								~		
	10										

1h	179		Natur	al Trig	onom	etrica	l Fun	ctions	. 1	16 2 °	10h
	1			Cosec'nte				Vrs. Sin		1 M	M.S.
M.S.	M 0	Sine29237	.70763	3.4203	.30573	Cotang. 3.2708	1.0457	.04369	.95630	60	52
8		. 9265	. 0735	.4170	. 0605	.2674	.0458	. 4378	. 5622	59	56
8	2	9293	0707	.4138	. 0637	.2640	.0459	4386	5613	58	52
12	3	9321	. 0679	.4106	. 0668	.2607	.0460	4395	. 5605	57	48
16	4	. 9348	. 0651	.4073	. 0700	.2573	.0461	4404	5596	56	44
20	5	.29376	.70624	3.4041	.30732	3.2539	1.0461	.04412	.95588	55	40
24	6	. 9404	. 0596	.4009	. 0764	.2505	.0462	. 4421	. 5579	54	36
28	7	. 9432	. 0568	.3977	. 0796	.2472	.0463	4426	5571	53	32
32	8	. 9460	. 0540	.3945	. 0828	.2438	.0464	. 4438	5562	52	28
36	9	. 9487	. 0512	.3913	. 0859	.2405	.0465	4446	5554	51	24
40	10	.29515	.70485	3.3881	.30891	3.2371	1.0466	.04455	.95545	50	20
44	11	. 9543	. 0457	.3849	. 0923	.2338	.0467	. 4463	. 5536	49	16
48	12	. 9571	. 0429	.3817	. 0955	.2305	.0468	. 4472	. 5528	48	12
52	13	. 9598	. 0401	.3785	. 0987	.2271	.0469	. 4481	. 5519	47	8
56	14	. 9626	. 0374	.3754	. 1019	.2238	.0470	. 4489	. 5511	46	4
9	15	.29654	70346	3.3722	.31051	3.2205	1.0471	.04498	.95502	45	51
4	16	. 9682	. 6318	.3690	. 1083	.2172	.0472	. 4507	. 5493	44	56
8	17	. 9710	. 0290	.3659	. 1115	.2139	.0473	. 4515	5485	43	52
12	18	. 9737	. 0262	.3627	. 1146	.2106	.0474	. 4524	. 5476	42	48
16	19	. 9765	. 0235	.3596	. 1178	.2073	.0475	. 4532	5467	41	44
20	20	.29793	.70207	3.3565	.31210	3.2041	1.0476	.04541	.95459	40	40
24	21	. 9821	. 0179	.3534	. 1242	.2008	.0477	. 4550	. 5450	39	36
28	22	. 9848	. 0151	.3502	. 1274	.1975	.0478	. 4558	. 5441	38	32
32	23	. 9876	. 0124	.3471	. 1306	.1942	.0478	. 4567	. 5433	37	28
36	24	. 9904	. 0096	.3440	. 1338	.1910	.0479	. 4576	. 5424	36	24
40	25	.29932	.70068	3.3409	.31370	3.1877	1.0480	.04585	.95415	35	20
44	26	. 9959	. 0040	.3378	. 1402	.1845	.0481	. 4593	. 5407	34	16
48	27	. 9987	. 0013	.3347	. 1434	.1813	.0482	. 4602	. 5398	33	12
52	28	.30015	.69982	.3316	. 1466	.1780	.0483	. 4611	. 5389	32	8
56	29	.30043	. 9957	.3286	. 1498	.1748	.0484	. 4619	. 5380	31	4
10	30	.30070	.69929	3.3255	.31530	3.1716	1.0485	.04628	.95372	30	50
4	31	. 0098	. 9902	.3224	. 1562	.1684	.0486	. 4637	. 5363	29	56
8	32	. 0126	. 9874	.3194	. 1594	.1652	.0487	. 4646	. 5354	28	52
12	33	. 0154	. 9846	.3163	. 1626	.1620	.0488	. 4654	. 5345	27	48
16	34	. 0181	. 9818	.3133	. 1658	.1588	.0489	. 4663	. 5337	-6	44
20	35	.30209	.69791	3.3102	.31690	3.1556	1.0490	.04672	.95328	25	40
24	36	. 0237	. 9763	.3072	. 1722	.1524	.0491	. 4681	. 5319	24	36
28	37	. 0265	. 9735	.3042	. 1754	.1492	.0492	. 4690	. 5310	23	32
32	38	. 0292	. 9707	.3011	. 1786	.1460	.0493	. 4698	. 5301	22	28
36	39	. 0320	. 9680	.2981	. 1818	.1429	.0494	. 4707	. 5293	21	24
40	40	.30348	.69652	3.2951	.31850		1.0495	.04716	.95284	20	20
44	41	. 0375	. 9624	.2921	. 1882	.1366	.0496	. 4725	. 5275	19	16
48	42	. 0403	9597	.2891	. 1914	.1334	.0497	4731	5266	18	12
52	43	. 0431	. 9569	.2861	. 1946	.1303	.0498	4743	5257	17	8
56	44 45	30486	. 9541	.2831 3.2801	. 1978	.1271 3.1240	.0499	. 4751	. 5248	16 15	4
4	46	.30486	. 9486	.2772	. 2042	.1209	1.0500	.04760	.95239 . 5231	14	49 56
8	47	. 0542	. 9458	.2742	. 2042	.1209	.0501 .0502	$\begin{bmatrix} .4769 \\ .4778 \end{bmatrix}$. 5222	13	52
12	48	. 0569	9430	.2712	. 2106	.1146	.0502	. 4787	. 5213	12	48
16	49	. 0597	. 9403	.2683	2138	.1115	.0503	4796	. 5204	11	44
20	50	.30625	.69375	3.2653	.32171	3.1084	1.0505	.04805	.95195	10	40
24	51	. 0653	9347	.2624	. 2203	.1053	.0506	. 4814	. 5186	9	36
28	52	. 0680	9320	.2594	. 2235	.1022	.0507	. 4823	. 5177	8	$\frac{30}{32}$
32	53	. 0708	9292	.2565	. 2267	.0991	.0508	4832	. 5168	7	28
36	54	. 0736	9264	.2535	. 2299	.0960	.0509	. 4840	. 5159	6	24
40	55	.30763	.69237	3.2506	.32331	3.0930	1.0510	.04849	.95150	5	20
44	56	. 0791	. 9209	.2477	2363	.0899	.0511	. 4858	. 5141	4	16
48	57	. 0819	. 9181	.2448	2395	.0868	.0512	4867	. 5132	3	12
52	58	. 0846	. 9154	.2419	2428	.0838	.0513	4876	. 5124	2	8
56	59	. 0874	. 9126	.2390	. 2460	.0807	.0514	. 4885	. 5115	î	4
12	60	. 0902	. 9098	.2361	. 2492	.6777	.0515	. 4894	. 5106	0	48
M.S.	M	Cosine.	Vrs. Sin.				Cosec'nt		Sine.	M	M.S.
7h	107	3			Nati	ıral.				720	4h
1											

						L LINES					
1h	18°		NT - 4	in mm					1	61°	$10^{\rm h}$
T_	10			d Trig		etrical	l Func	tions.	т Т	01	10"
M.S.	_ M]			Cosec'nte		Cotang.		Vrs. Sin		М	M.S.
12	0	.30902	.69093	3.2361	.32492	3.0777	1.0515	.04894	.95106	60	48
4	1	. 0929	. 9071	.2332	. 2524	.0746	.0516	. 4903	. 5097	59	56
8 12	$\frac{2}{3}$. 0957	. 9043 . 9015	.2303 .2274	. 2556	.0716	.0517	. 4912	. 5088	58	52
16	4	. 1012	. 8988	.2245	. 2621	.0686	.0518	. 4921	. 5079	57 56	48 44
20	5	.31040	.68960	3.2216	.32653	3.0625	1.0520	.04939	.95061	55	40
24	6	. 1068	. 8932	.2188	. 2685	.0595	.0521	. 4948	. 5051	54	36
28	7	. 1095	. 8905	.2159	. 2717	.0565	.0522	. 4957	. 5042	53	32
32	8	. 1123	. 8877	.2131	. 2749	.0535	.0523	. 4966	. 5033	52	28
36	9	. 1150	. 8849	.2102	. 2782	.0505	.0524	. 4975	. 5024	51	24
40	10	.31178	.68822	3.2074 .2045	.32814	3.0475	1,0525 .0526	.04985	.95015	50 49	20 16
44 48	11 12	. 1233	8766	.2017	. 2878	.0415	.0527	. 5003	. 4997	48	12
52	13	. 1261	. 8739	.1989	2910	.0385	.0528	5012	4988	47	8
56	14	. 1289	. 8711	.1960	. 2943	.0356	.0529	. 5021	. 4979	46	4
13	15	.31316	.68684	3.1932	.32975	3.0326	1.0530	.05030	.94970	45	47
4	16	. 1344	. 8656	.1904	. 3007	.0296	.0531	. 5039	. 4961	44	56
8	17	. 1372	. 8628	.1876	3039	.0267	.0532	. 5048	. 4952	43	52
12 16	18 19	. 1399	. 8601 . 8573	.1848	. 3072	.0237	.0533	. 5057	4942	42 41	48
20	20	.31454	.68545	3.1792	.33136	3.0178	1.0535	.05076	.94924	40	40
24	21	. 1482	. 8518	.1764	. 3169	.0149	.0536	. 5085	. 4915	39	36
28	22	. 1510	. 8490	.1736	. 3201	.0120	.0537	. 5094	. 4906	38	32
32	23	. 1537	. 8463	.1708	. 3233	.0090	.0538	. 5103	. 4597	37	28
36	24	. 1565	. 8435	.1681	. 3265	.0061	.0539	. 5112	. 4888	36	24
40	25	.31592	.68407	3.1653	.33298	3.0032	1.0540	.05121	.94878	35	20
44	26	. 1620 . 1648	. 8380 . 8352	.1625 .1598	. 3330	3.0003	.0541	. 5131	. 4869	34 33	16 12
48 52	27 28	1675	8325	.1570	. 3395	.9945	.0543	. 5149	. 4851	32	8
56	29	1703	8297	.1543	. 3427	.9916	.0544	. 5158	. 4841	31	4
14	30	.31730	.68269	3.1515	.33459	2.9887	1.0545	.05168	.94832	30	46
4	31	1758	. 8242	.1488	. 3492	.9358	.0546	. 5177	. 4823	29	56
8	32	. 1786	. 8214	.1461	. 3524	.9829	.0547	. 5186	. 4814	28	52
12	33	. 1813	. 8187	.1433	. 3557	.9800	.0548	. 5195 . 5205	. 4805	27 26	48 44
16 20	34 35	. 1841 .31868	. 8159	3.1379	.33621	.9772 2.9743	.0549 1.0550	.05214	.94786	25	40
24	36	. 1896	. 8104	.1352	. 3654	.9714	.0551	. 5223	4777	24	36
28	37	1923	. 8076	.1325	. 3686	.9686	.0552	. 5232	. 4767	23	32
32	38	. 1951	. 8049	.1298	. 3718	.9657	.0553	. 5242	. 4758	22	28
36	39	. 1978	. 8021	.1271	. 3751	.9629	.0554	. 5251	. 4749	21	24
40	40	.32006	1.01994	0.1411	.33783			.05260	.94740	20	20
44	41	2034	. 7966	.1217	3816	.9572 .9 5 44	.0556	. 5270 . 5279	. 4730	19 18	$\begin{array}{ c c }\hline 16\\12\\ \end{array}$
48 52	42 43	2061	7911	.1163	. 3880	.9515	.0558	. 5288	4712	17	8
56	44	2116	7884	.1137	3913	.9487	.0559	. 5297	4702	16	4
15	45	.32144	.67856	3.1110	.33945	2.9459	1.0560	.05307		15	45
4	46	. 2171	. 7828	.1083	. 3978	.9431	.0561	. 5316	. 4684	14	56
8	47	. 2199	. 7801	.1057	4010	.9403	.0562	. 5326	. 4674	13	52
12	48	. 2226	7773	.1030 .1004	4043	9375	.0563	. 5335	. 4665	12 11	48 44
16 20	149 50	. 2254 .32282	.67718	3.0977	.34108	.9347 2.9319	1.0566	.0535 ±	.94646	10	40
24	51	. 2309	7691	.0951	. 4140	.9291	.0567	. 5363	. 4637	9	36
28	52	2337	. 7663	.0925	. 4173	.9263	.0568	. 5373	. 4627	8	32
32	53	. 2364	. 7636	.0898	. 4205	.9235	.0569	. 5382	. 4618	7	28
36	54	. 2392	. 7608	.0872	. 4238	.9208	.0570	. 5391	. 4608	6	24
40	55	.32419	.67581	3.0846	.34270	2.9180	1.0571	.05401	.94599	5	20
44	56	. 2447	. 7553 . 7526	.0820	4303	.9152	.0572	. 5410 . 5420	. 4590 . 4580	4	16 12
48 52	57 58	2474	. 7498	.0767	. 4368	.9097	.0574	5429	. 4571	2	8
56	59	2529	7471	.0741	4400	.9069	.0575	5439	. 4561	$\tilde{1}$	4
16	60	2557	7443	.0715	. 4433		.0576	. 5448	. 4552	0	44
M.S.		Cosine.		Secante.		Tangent.	Cosec'nt	Vrs.Cos	Sine.	M	M.S.
7h	108	0			Nati	ural.				71°	4h
1					-			-			

2	NATURAL LINES.											
	1h	19°]	Natura	d Trig	onom	etrical	Func	tions.	1	60°	10 ^h
	M.S.	М	Sine.	Vrs.Cos.	Cosec'nte	Tang.	Cotang.	Secante.	Vrs. Sin		M	M.S.
	16	()	.32557	.67443	3.0715	.34433	2.9042	1.0576	.05448	.94552	60	44
	4	1	. 2584	. 7416	.0690	. 4465	.9015	.0577	5458	. 4542	59	56 52
Į	8	2 3	. 2612	. 7388	.0664	. 4498	.8987	.0578	. 5467	. 4533	58 57	48
1	12 16	4	. 2639	. 7361	.0638	. 4530	.8960 .8933	.0579	. 5486	. 4514	56	44
١	20	5	.32694	. 7333 .67306	3.0586	.34595	2.8905	1.0581	.05495	.94504	55	40
ı	24	6	. 2722	. 7278	.0561	. 4628	.8878	.0582	. 5505	. 4495	54	36
ı	28	7	. 2749	. 7251	.0535	. 4661	.8851	.0584	. 5515	. 4485	53	32
1	32	8	. 2777	. 7223	.0509	. 4693	.8824	.0585	. 5524	. 4476	52	23
ļ	36	9	. 2804	. 7196	.0484	. 4726	.8797	.0586	. 5534	. 4466	51	24
1	40	10	.32832	67168	3.0458	.34758	2.8770	1.0587	.05543	.94457	50	20 16
	44 48	11 12	. 2859	. 7141	.0433	. 4791	.8743 .8716	.0589	. 5562	. 4438	48	12
	52	13	. 2887	. 7113 . 7086	0.0407 0.0382	. 4856	.8689	.0590	5572	. 4428	47	8
	56	14	2942	7058	.0357	. 4889	.8662	.0591	. 5581	. 4418	46	4
	17	15	.32969	.67031	3.0331	.34921	2.8636	1.0592	.05591	.94409	45	43
	4	16	. 2996	. 7003	.0306	. 4954	.8609	.0593	. 5601	. 4399	44	56
	8	17	. 3024	. 6976	.0281	. 4987	.8582	.0594	. 5610	. 4390	43	52
	12	18	. 3051	. 6948	.0256	. 5019	.8555	.0595	. 5620	4380	42 41	48
	16	19	3079	. 6921	.0231	. 5052	.8529	.0596 1.0598	. 5629 .05639	. 4370 .94361	40	40
	$\begin{array}{c} 20 \\ 24 \end{array}$	$\begin{vmatrix} 20 \\ 21 \end{vmatrix}$.33106	.66894	3.0206 .0181	. 5117	2.8502 .8476	.0599	. 5649	. 4351	39	36
	28	22	. 3161	. 6866	.0156	. 5150	.8449	.0600	. 5658	. 4341	38	32
	32	23	. 3189	6811	.0131	. 5183	.8423	.0601	. 5668	. 4332	37	28
۱	36	24	. 3216	6784	.0106 .	. 5215	.8396	.0602	. 5678	. 4322	36	24
ı	40	25	.33243	.66756	3.0081	.35248	2.8370	1.0603	.05687	.94313	35	20
ı	44	26	. 3271	. 6729	.0056	. 5281	.8344	.0604	5697	4303	34	16
ı	48	27	. 3298	. 6701	.0031	. 5314	.8318	.0605	5707	4293 4283	33 32	12 8
ı	52	28	. 3326	. 6674	$0007 \\ 2.9982$. 5346	.8291 .8265	.0606 .0607	. 5716 . 5726	. 4274	31	4
ı	56 18	29 30	. 3353	. 6647	2.9957	.35412	2.8239	1.0608	.05736	.94264	30	42
	4	31	. 3408	6592	.9933	. 5445	.8213	.0609	. 5745	. 4254	29	56
ı	8	32	. 3435	. 6564	.9908	. 5477	.8187	.0611	. 5755	. 4245	28	52
ı	12	33	. 3463	. 6537	.9884	. 5510	.8161	.0612	. 5765	. 4235	27	48
ı	16	34	. 3490	. 6510	.9859	. 5543	.8135	.0613 1.0614	. 5775 .05784	.4225 $.94215$	$\begin{array}{c c} 26 \\ 25 \end{array}$	44 40
ı	20	35 36	.33518	.66482	2.9835 .9810	.35576	2.8109 .8083	.0615	. 5794	. 4206	24	36
	$\begin{bmatrix} 24 \\ 28 \end{bmatrix}$	37	3572	6427	.9786	. 5641	.8057	.0616	. 5804	. 4196	23	32
ı	32	38	. 3600	6400	.9762	. 5674	.8032	.0617	. 5814	. 4186	22	28
	36	39	. 3627	. 6373	.9738	. 5707	.8006	.0618	. 5823	. 4176	21	24
ı	40	40	.33655	.66345	2.07 1 10	.35739			.05833	.94167	20	20
	44	41	. 3682	. 6318	.9689	. 5772	.7954	.0620	. 5843	. 4157	19	16
	48	42	. 3709	. 6290	.9665	. 5805 . 5838	.7929 .7903	.0622	. 5853 . 5863	. 4147 . 4137	18 17	12 8
	52 56	43 44	3737	. 6263 . 6236	.9641 .9617	. 5871	.7878	.0624	5872	4127	16	4
	19	45	.33792	.66208	2.9593	.35904	2.7852	1.0625	.05882	.94118	15	41
	4	46	. 3819	. 6181	.9569	. 5936	.7827	.0626	. 5892	. 4108	14	56
	8	47	. 3846	. 6153	.9545	. 5969	.7801	.0627	5902	. 4098	13	52
	12	48	. 3874	. 6126	.9521	. 6002	.7776	.0628	5912	. 4088	12	48
	16	49	3901	6099	.9497	. 6035	.7751 2.7725	.0629 1.0630	. 5922 .05932	.4078 $.94068$	11 10	44 40
	20	50	.33928	.66071	2.9474 $.9450$.36068	.7700	.0632	. 5941	. 4058	9	36
	24 28	51 52	. 3956	$\begin{array}{ c c c c c c c c c c c c c c c c c c c$.9426	6134	.7675	.0633	5951	4049	8	32
	32	53	4011	5989	.9402	. 6167	.7650	.0634	. 5961	. 4039	7	28
	36	54	. 4038	. 5962	.9379	. 6199	.7625	.0635	. 5971	. 4029	6	24
	40	55	.34065	.65935	2.9355	.36232	2.7600	1.0636	.05981	.94019	5	20
	44	56	. 4093	. 5907	.9332	6265	.7574	.0637	. 5991	4009	4	16
	48	57	. 4120	. 5880	.9308	6298	.7549 .7524	.0638 .0639	6001 6011	. 3999 . 3989	3 2	$\begin{vmatrix} 12 \\ 8 \end{vmatrix}$
1	52 56	58 59	. 4147	. 5853 . 5825	.9285 .9261	6364	.7500	.0641	. 6021	3979	$\tilde{1}$	4
	20	60	. 4202	5798	.9238	6397	.7475	.0642	. 6031	. 3969	0	40
	M.S.	M	Cosine.		Secante,	Cotang.	Tangent.	Cosec'nt		Sine.	M	M.S.
	7h	109	0			Nati	ural.				70°	4h
		1										

1	4										
1h	20°	,	Mataria	- 7 7973 -		4 .			7	59°	10 ^h
				al Trig		etrica.	I M'ELIDO	ctions	<u> </u>	.09	104
M.S	M	Sine.	1	Cosec'nte		Cotang.		Vrs. Sin	Cosine.		M.S.
20	$\begin{bmatrix} 0 \\ 1 \end{bmatrix}$.34202	.65798	2.9238	.36397	2.7475	1.0642	.06031	.93969	60	40
8	$\frac{1}{2}$. 4229	. 5771	.9215 .9191	. 6430 . 6463	.7450 .7425	.0643	6041	. 3959	59 58	56 52
12	3	. 4284	. 5716	.9168	. 6496	.7400	.0645	6061	. 3939	57	48
16	4	. 4311	. 5689	.9145	6529	.7376	.0646	6071	3929	56	44
20	5	.34339	.65661	2.9122	.36562	2.7351	1.0647	.06080	.93919	55	40
24	6	. 4366	. 5634	.9098	. 6595	.7326	.0648	. 6090	. 3909	54	36
28	7	. 4393	. 5607	.9075	. 6628	.7302	.0650	. 6100	. 3899	53	32
32	8 9	. 4421	5579	.9052 .9029	6661	.7277	.0651	6110	. 3889	52	28
36 40	10	.34475	.65525	2.9006	. 6694	.7252 2.7228	.0652 1.0653	. 6121	. 3879	51 50	24 20
44	11	4502	. 5497	.8983	. 6760	.7204	.0654	. 6141	. 3859	49	16
48	12	. 4530	. 5470	.8960	. 6793	.7179	.0655	. 6151	. 3849	48	12
52	13	. 4557	. 5443	.8937	. 6826	.7155	.0656	. 6161	. 3839	17	8
56	14	. 4584	. 5415	.8915	. 6859	.7130	.0658	. 6171	. 3829	46	4
21	15	.34612	.65388	2.8892	.36892	2.7106	1.0659	.06181	.93819	45	39
4 8	16 17	. 4639	• 5361 • 5334	.8869 .8846	. 6925	.7082 .7058	.0660	. 6191 . 6201	. 3809	44 43	56 52
12	18	. 4693	. 5306	.8824	6991	.7033	.0662	6211	. 3789	42	48
16	19	. 4721	. 5279	.8801	. 7024	.7009	.0663	6221	. 3779	41	44
20	20	.34748	.65252	2.8778	.37057	2.6985	1.0664	.06231	.93769	40	40
24	21	. 4775	. 5225	.8756	. 7090	.6961	.0666	. 6241	. 3758	39	36
28	22	. 4803	. 5197	.8733	. 7123	.6937	.0667	. 6251	. 3748	38	32
32	23	. 4830 . 4857	• 5170 • 5143	.8711 .8688	. 7156	.6913	.0668	6262	. 3738	37	28
36	24 25	.34884	.65115	2.8666	.37223	.6889 2.6865	.0669 1.0670	. 6272	. 3728	36 35	24 20
44	26	. 4912	. 5088	.8644	. 7256	.6841	.0671	. 6292	. 3708	34	16
48	27	. 4939	. 5961	.8621	. 7289	.6817	.0673	. 6302	. 3698	33	12
52	28	. 4966	. 5034	.8599	. 7322	.6794	.0674	. 6312	. 3687	32	8
56	29	. 4993	. 5006	.8577	. 7355	.6770	.0675	. 6323	. 3677	31	4
23	30	.35021	.64979	2.8554	.37388	2.6746	1.0676	.06333	.93667	30	38
8	31 32	. 5048	. 4952 . 4925	.8532 .8510	. 7422 . 7455	.6722 .6639	.0677	. 63 4 3 . 6353	. 3657	29 28	56 52
12	33	. 5102	. 4897	.8488	. 7488	.6675	.0679	. 6363	3637	27	48
16	34	. 5130	4870	.8466	. 7521	.6652	.0681	. 6373	. 3626	26	44
20	35	.35157	.64843	2.8444	.37554	2.6628	1.0682	.06384	.93616	25	40
24	36	. 5184	. 4816	.8422	. 7587	.6604	.0683	. 6394	. 3606	24	36
28	37	. 5211	4789	.8400	7621	.6581	.0684	6404	. 3596	23	32
32	38	5239 5266	. 4761 . 4734	.8378 .8356	. 7654 . 7687	.6558 .6534	.0685	. 6414	. 3585	22 21	28 24
36 40	40	.35293	.64707	2.8334	.37720	2.6511	1.0688	.06435	.93565	20	20
44	41	. 5320	. 4680	.8312	. 7754	.6487	.0689	. 6445	. 3555	19	16
48	42	. 5347	. 4652	.8290	. 7787	.6464	.0690	. 6456	. 3544	18	12
52	43	. 5375	. 4625	.8269	. 7820	.6441	.0691	. 6466	. 3534	17	8
56	44	. 5402	4598	.8247	. 7853	.6418	1.0692 1.0694	. 6476	. 3524	16	217
23	45	.35429	.64571 . 4544	2.8225 .8204	.37887 . 7920	2.6394	0695	. 6497	.93513	15 14	37 56
8	46 47	. 5456 . 5483	. 4516	.8182	. 7953	.6348	.0696	, 6507	. 3493	13	$\frac{50}{52}$
12	48	. 5511	. 4489	.8160	7986	.6325	.0697	6517	. 3482	12	48
16	49	. 5538	. 4462	.8139	8020	.6302	.0698	. 6528	. 3472	11	44
20	50	.35565	.64435	2.8117	.38053	2.6279	1.0699	.06538	.93462	10	40
24	51	. 5592	. 4408	.8096	. 8086	.6256	.0701	. 6548	. 3451	9	36
28	52	. 5619	. 4380	.8074	. 8120	.6233	.0702	. 6559 . 6569	3441	8 7	32 28
32 36	53 54	. 5647	. 4353	.8053 .8032	. 8153 . 8186	.6210 .6187	.0703	6569 6579	. 3431 . 3420	6	28
40	55	.35701	.64299	2.8010	.38220	2.6164	1.0705	.06590	.93410	5	$\frac{24}{20}$
44	56	. 5728	. 4272	.7989	. 8253	.6142	.0707	. 6600	. 3400	4	16
48	57	. 5755	. 4245	.7968	. 8286	.6119	.0708	. 6611	. 3389	3	12
52	58	. 5782	. 4217	.7947	. 8320	.6096	.0709	. 6621	. 3379	2	8
56	59	. 5810	. 4190	.7925	, \$353	.6073	.0710	6631	3368	1	26
24 M.S.	60 M	. 5837 Cosine.	. 4163 Vrs. Sin.	.7904 Secante.	. 8386	.6051 Tangent.	.0711 Cosec'nt	Vrs. Cos	. 3358 Sine.	() M	36 M.S.
	110		, , , , , , , , , , , , , , , , , , , ,	Doggardor 1	Nati			, 10,0001		69°	
	TIO				Matri	erecr.					

200	NATURAL LINES.											
	1										1	
1h	210)	Natur	al Trig	gonom	etrical	Fun	ctions.	-	158°	10h	
M.S.	M	Sine.	Vrs. Cos.	Cosec'nte	Tang.	/ Cotang.	Secante	Vrs. Sin	Cosine.	1 M	M.S.	
24	0	.35837	.64163	2.7904	.38386		1.0711	.06642	.93358	60	36	
4	1	. 5864	. 4136	.7883	. 8420		.0713	. 6652	. 3348	59	56	
8	2	. 5891	. 4109	.7862	. 8453	.6006	.0714	. 6663	. 3337	58	52	
12	3	. 5918	. 4082	.7841	. 8486	.5983	.0715	. 6673	. 3327	57	48	
16	4	. 5945	. 4055	.7820	. 8520	.5960	.0716	. 6684	. 3316	56	44	
20 24	5 6	.35972	.64027	2.7799	.38553	2.5938	1.0717		.93306	55	40	
28	7	. 6000	. 4000	.7778	. 8587	.5916	.0719	6705	. 3295	54	36	
32	8	6027	3973	.775 7 .7736	8620	.5893	.0720	6715	. 3285	53 52	32 28	
36	9	. 6081	. 3919	.7715	8687	.5848	.0722	6736	. 3264	51	24	
40	10	.36108	.63892	2.7694	.38720	2.5826	1.0723	.06747	.93253	50	20	
44	11	. 6135	. 3865	.7674	. 8754	.5804	.0725	. 6757	. 3243	49	16	
48	12	. 6162	. 3837	.7653	. 8787	.5781	.0726	. 6768	. 3232	48	12	
52	13	. 6189	. 3810	.7632	. 8821	.5759	.0727	. 6778	. 3222	47	8	
56	14	. 6217	. 3783	.7611	. 8854	.5737	.0728	. 6789	. 3211	46	4	
25	15	.36244	.63756	2.7591	.38888	2.5715	1.0729	.06799	.93201	45	35	
8	16 17	. 6271	. 3729	.7570	. 8921	.5693	.0731	. 6810	. 3190	44	56	
12	18	. 6298	. 3702	.7550	. 8955	.5671	.0732	6820	. 3180	43 42	52	
16	19	. 6325 . 6352	. 3675	.7529 .7509	. 8988	.5627	.0733	. 6831 . 6841	. 3169	41	48	
20	20	.36379	.63621	2.7488	.39055	2.5605	1.0736	.06852	.93148	40	40	
24	21	. 6406	. 3593	.7468	. 9089	.5583	.0737	. 6863	. 3137	39	36	
28	22	. 6433	. 3566	.7447	. 9122	.5561	.0738	. 6873	. 3127	38	32	
32	23	. 6460	. 3539	.7427	. 9156	.5539	.0739	. 6884	. 3116	37	28	
36	24	. 6488	. 3512	.7406	. 9189	.5517	.0740	. 6894	. 3105	36	24	
40	25	.36515	.63485	2.7386	.39223	2.5495	1.0742	.06905	.93095	35	20	
44	26	. 6542	. 3458	.7366	. 9257	.5473	.0743	. 6916	. 3084	34	16	
48 52	27 28	. 6569	. 3431	.7346	. 9290	.5451	.0744	6926	. 3074	33	12	
56	29	. 6596	. 3404	.7325 .7305	. 9324	.5430 .5408	.0745 .0747	. 6937 . 6947	. 3063 . 3052	32 31	8 4	
26	30	.36650	.63350	2.7285	.39391	2.5386	1.0748	.06958	.93042	30	34	
4	31	. 6677	. 3323	.7265	. 9425	.5365	.0749	. 6969	. 3031	29	56	
8	32	6704	. 3296	.7245	. 9458	.5343	.0750	. 6979	. 3020	28	52	
12	33	. 6731	. 3269	.7225	. 9492	.5322	.0751	. 6990	. 3010	27	48	
16	34	. 6758	. 3242	.7205	. 9525	.5300	.0753	. 7001	. 2999	26	44	
20 24	35	.36785	.63214	2.7185	.39559	2.5278	1.0754	.07012	.92988	25	40	
28	36 37	. 6812	. 3187	.7165	. 9593 . 9626	.5257	.0755	. 7022 . 7033	. 2978	24	36	
32	38	. 6839	. 3160 . 3133	.7145 .7125	. 9660	.5236 .5214	.0756 .0758	7044	. 2967 . 2956	23 22	32 28	
36	39	. 6893	. 3106	.7105	. 9694	.5193	.0759	7054	. 2945	21	24	
40	40	.36921	.63079	2.7085	.39727		1.0760	.07065	.92935	20	20	
44	41	. 6948	. 3052	.7065	. 9761	.5150	.0761	. 7076	. 2924	19	16	
48	42	. 6975	. 3025	.7045	. 9795	.5129	.0763	. 7087	. 2913	18	12	
52	43	. 7002	. 2998	.7026	. 9828	.5108	.0764	. 7097	. 2902	17	8	
56	44	. 7029	. 2971	.7006	. 9862	.5086	.0765	. 7108	. 2892	16	4	
27	45 46	.37056	.62944	2.6986	.39896	2.5065	1.0766	.07119	.92881	15	33	
8	40	. 7083 . 7110	2917	.6967	. 9930	.5044	.0768 .07 6 9	. 7130 . 7141	2870	14 13	£6	
12	48	. 7137	. 2890 . 2863	.6947 .6927	. 9997	.5023 .5002	.0709	. 7151	. 2859	12	52 48	
16	49	. 7164	. 2836	.6908	.40031	.4981	.0771	. 7162	. 2838	11	44	
20	50	.37191	.62809	2.6888	.40065	2.4960	1.0773	.07173	.92827	10	40	
24	51	. 7218	. 2782	.6869	. 0098	.4939	.0774	. 7184	. 2816	9	36	
28	52	. 7245	. 2755	.6849	. 0132	.4918	.0775	. 7195	. 2805	8	32	
32	53	. 7272	. 2728	.6830	. 0166	.4897	.0776	. 7205	. 2794	7	28	
36 40	54 55	. 7299	. 2701	.6810	40000	.4876	.0778	. 7216	. 2784	6	24	
41	56	.37326 . 7353	.62674	2.6791	40233	2.4855	1.0779 .0780	.07227	.92773	5 4	20	
48	57	. 7350	. 2647	.6772 .6752	. 0267	.4834 .4813	.0780	. 7238 . 7249	. 2762 . 2751	3	$\begin{vmatrix} 16 \\ 12 \end{vmatrix}$	
52	58	7407	. 2593	.6733	. 0335	.4792	.0783	7260	2740	2	8	
56	59	. 7434	2566	.6714	. 0369	.4772	.0784	7271	2729	ī	4	
28	60	. 7461	. 2539	.6695	. 0403	.4751	.0785	. 7282	. 2718	Ü	32	
M.S.		Cosine.	Vrs.Sin.	Secaute.	Cotang.	Tangent.			Sine.		M.S.	
7 ^h	111				Natu	ral.				68°	4h	
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1					Δ.	ATUKA	LLINES	•				23
	1h	229	·	Natura	al Trig	onem	etrica	Fun	ctions	. 1	57°	10 ^h
	M.S.	M	Sine.	Vrs. Cos.	Cosec'nte	Tang.	Cotang.	Secante.	Vrs. Sin	Cosine.	M	M.S.
	28	0	.37461	.62539	2.6695	.40403	2.4751	1.0785	.07282	,92718	60	32
	4	1	. 7488	. 2512	.6675	. 0436	4730	.0787	. 7292	. 2707	59	56
	8	2	. 7514	. 2485	.6656	. 0470	.4709	.0788	. 7303	. 2696	58	52
1	12	3	. 7541	. 2458	.6637	. 0504	.4689	.0789	. 7314	. 2686	57	4.8
	16	4	. 7558	. 2431	.6618	. 0538	.4668	.0790	. 7325	. 2675	56	44
i	20	5	.37595	.62404	2.6599	.40572	2.4647	1.0792	.07336	.92664	55	40
-	24	6	. 7622	. 2377	.6580	. 0606	.4627	.0793	. 7347	. 2653	54	36
	28	7	. 7649	. 2351	.6561	. 0640	.4606	.0794	. 7358	. 2642	53	32
	32	8	. 7676	. 2324	.6542	. 0673	.4586	.0795	. 7369	. 2631	52	28
	36	9	. 7703	. 2297	.6523	. 0707	.4565	.0797	. 7380	. 2620	51	24
	40	10	.37730	.62270	2.6504	.40741	2.4545	1.0798	.07391	.92609	50	20
	44	11	. 7757	. 2243	.6485	. 0775	.4525	.0799	. 7402	. 2598	49	16
	48	12	. 7784	. 2216	.6466	. 0809	.4504	.0801	. 7413	. 2587	48	12
	- 52	13	. 7811	. 2189	.6447	. 0843	.4484	.0802	. 7424	. 2576	47	8
	56	14	. 7838	. 2162	.6428	. 0877	.4463	.0803	. 7435	. 2565	46	4
	29	15	.37865	.62135	2.6410	.40911	2.4443	1.0804	.07446	.92554	45	31
	4	16	. 7892	. 2108	.6391	. 0945	.4423	.0806	. 7457	. 2543	44	56
	8	17	. 7919	. 2081	.6372	. 0979	.4403	.0807	. 7468	. 2532	43	52
	12	18	7946	. 2054	.6353	. 1013	.4382	.0808	. 7479	. 2521	42	48
	16	19	. 7972	. 2027	.6335	. 1047	.4362	.0810	. 7490	. 2510	41	44
	20	20	.37999	.62000	2.6316	.41081	2.4342	1.0811	.07501	.92499	40	40
	24	21	. 8026	. 1974	.6297	. 1115	.4322	.0812	. 7512	. 2488	39	36
	28	22	. 8053		.6279	. 1149	.4302	.0813	. 7523	2477	38	32
	32	23	. 8080	. 1920	.6260	. 1183	.4282	.0815	. 7534	, 2466	37	28
	36	24	. 8107	. 1893	.6242 2.6223	. 1217 .41251	.4262	.0816	. 7545	. 2455	36	24
	40	25	.38134			. 1285	2.4242	1.0817	.07556	192443	35	20
	44	26	. 8161	. 1839	6205	. 1319	4222	.0819	. 7579	. 2432	34	16
	48	27	. 8188	. 1812	.6186 .6168	. 1353	.4202	.0820	. 7590	2421 2410	33	12
	52	28	. 8241	. 1758	.6150	. 1387	.4162	.0823	7601	2399	32	8
	56	29	.38268	.61732	2.6131	.41421	2.4142	1.0824	.07612	.92388	30	30
	30	30	. 8295	. 1705	.6113	. 1455	.4122	.0825	7623	. 2377	29	56
	4 8	31 32	. 8322	. 1678	.6095	. 1489	.4102	.0826	7634	2366	28	52
	12	33	. 8349	. 1651	.6076	. 1524	.4083	.0828	7645	2354	27	48
	16	34	8376	. 1624	.6058	. 1558	.4063	.0829	7657	2343	26	44
	20	35	.38403	.61597	2.6040	.41592	2,4043	1.0830	.07668	.92332	25	40
	24	36	. 8429	. 1570	.6022	. 1626	.4023	.0832	7679	. 2321	24	36
	28	37	. 8456	. 1544	.6003	. 1660	4004	.0833	7690	2310	23	32
	32	38	. 8483	. 1517	.5985	. 1694	.3984	.0834	. 7701	2299	22	28
	36	39	. 8510	. 1490	.5967	. 1728	.3964	.0836	7712	2287	21	24
	40	40	.38537	.61463	2.5949	.41762	2.3945	1.0837	.07724	.92276	20	20
	44	41	. 8564	. 1436	.5931	. 1797	.3925	.0838	. 7735	. 2265	19	16
	48	42	. 8591	. 1409	.5913	. 1831	.3906	.0840	. 7746	. 2254	18	12
	52	43	. 8617	. 1382	.5895	. 1865	.3886	.0841	. 7757	. 2242	17	8
	56	41	. 8644	. 1356	.5877	. 1899	.3867	.0842	. 7769	. 2231	16	4
	31	45	.38671	.61329	2.5859	.41933	2.3847	1.0844	.07780	.92220	15	29
	4	46	. 8698	. 1302	.5841	. 1968	.3828	.0845	. 7791	. 2209	14	56
	8	47	. 8725	. 1275	.5823	. 2002	.3808	.0846	. 7802	. 2197	13	52
-	12	48	. 8751	. 1248	.5805	. 2036	.3789	.0847	. 7814	. 2186	12	48
	16	49	. 8778	. 1222	.5787	2070	.3770	.0849	. 7825	. 2175	11	44
	20	50	.38805	.61195	2.5770	.42105	2.3750	1.0850	.07836	.92164	10	40
}	24	51	. 8832	. 1168	.5752	. 2139	.3731	.0851	. 7847	. 2152	9	36
	28	52	. 8859	. 1141	.5734	. 2173	.3712	.0853	. 7859	. 2141	8	32
	32	53	. 8886	. 1114	.5716	. 2207	.3692	.0854	. 7870	. 2130	7	28
	36	54	. 8912	. 1088	.5699	. 2242	.3673	.0855	. 7881	. 2118	6	24
	40	55	.38939	.61061	2.5681	.42276	2.3654	1.0857	.07893	.92107	5	20
	44	56	. 8966	. 1034	.5663	. 2310	.3635	.0858	7904	. 2096	4	16
	48	57	, 8993	. 1007	.5646	2344	.3616	.0859	7915	. 2084	3	12
	52	58	. 9019	. 0980	.5628	2379	.3597	.0861	. 7927	2073	2	8
	56	59	. 9046	. 0954	.5610	2413	.3577	.0862	. 7938	. 2062	1	28
	32 M. S.	60 M	. 9073	. 0927 Vrs. Sin.	.5593	. 2447	.3558 Tangent.	.0864	. 7949 Vrs Cos	Sine.	M	M.S.
-	7h	$1\overset{\mathtt{M}}{1}\overset{\mathtt{C}}{2}$	Cosine.	VIS. SILL	Scoante.			O O O O II I	110,000	Pitto.	67°	4h
1		114				Natu	tritt.					

1h	990								7	 l56°	10h
1"	23°			al Trig		4					
M.S. 32	M 0	Sine.)	Cosec'nte		Cotang.	1	Vrs. Sin	Cosine.		M.S. 28
4	i	.39073	.60927	2.5593 .5575	. 42447	2.3558	1.0864	.07949	.92050	59	56
8	2	. 9126	. 0873	.5558	. 2516	.3520	.0866	7972	. 2028	58	52
12	3	. 9153	. 0846	.5540	. 2550	.3501	.0868	. 7984	. 2016	57	48
16	4	. 9180	. 0820	.5523	. 2585	.3482	.0869	. 7995	. 2005	56	44
20 24	5 6	.39207 . 9234	.60793	2,5506 .5488	.42619	2.3463	1.0870 .0872	.08006	.91993 . 1982	55 54	36
28	7	9254	. 0766	.5471	. 2688	.3426	.0873	. 8029	. 1971	53	32
32	8	9287	. 0713	.5453	2722	.3407	.0874	8041	. 1959	52	23
36	9	. 9314	. 0686	.5436	. 5757	.3388	.0876	. 8052	. 1948	51	24
40	10	.39341	.60659	2.5419	.42791	2.3369	1.0877	.08063	.91936	50	20
41 48	11 12	9367	. 0632	.5402 .5384	. 2826	.3350 .3332	.0878	. 8075	. 1925 . 1913	49 48	16 12
52	13	9421	: 0579	.5367	2894	.3313	.0881	8098	. 1902	47	8
56	14	. 9448	. 0552	.5350	. 2929	.3294	.0882	. 8109	. 1891	46	4
33	15	.39474	.60526	2.5333	.42963	2.3276	1.0884	.08121	.91879	45	27
8	16 17	. 9501 . 9528	. 0499	.5316	. 2998	.3257	.0885	. 8132 . 8144	. 1868	44 43	56 52
12	18	. 9554	. 0452	.5299 .5281	. 3052	.3238	.0886	. 8155	. 1845.	42	48
16	19	. 9581	. 0419	.5264	. 3101	.3201	.0889	. 8167	. 1833	41	44
20	20	.39608	.60392	2.5247	.43136	2.3183	1.0891	.08178	.91822	40	40
24 28	21 22	. 9635	. 0365	.5230	. 3170	.3164	.0892	. 8190 . 8201	. 1810 . 1798	39	36 32
32	23	. 9661	. 0339	.5213 .5196	. 3239	.3145 .3127	.0893	. 8213	. 1787	38 37	28
36	24	. 9715	. 0285	.5179	. 3274	.3109	.0896	. 8224	1775	36	24
40	25	.39741	.60258	2.5163	.43308	2.3090	1.0897	.08236	.91764	35	20
44	26	. 9768	. 0232	.5146	. 3343	.3072	.0899	8248	. 1752	34	16
48 52	27 28	. 9795	$\begin{bmatrix} . & 0205 \\ . & 0178 \end{bmatrix}$.5129 .5112	. 3377	.3053 .3035	.0900	. 8259 . 8271	. 1741 . 1729	33 32	12 8
56	29	. 9848	: 0152	.5095	. 3447	.3017	.0903	. 8282	. 1718	31	4
34	30	.39875	.60125	2.5078	.43481	2.2998	1.0904	.08294	.91706	30	26
4	31	. 9901	. 0098	.5062	. 3516	.2980	.0906	. 8306	. 1694	29	56
8 12	32	. 9928	. 0072	.5045 .5028	. 3550 . 3585	.2962 .2944	.0907	. 8317 . 8329	. 1683 . 1671	28 27	52
16	34	. 9981	. 0018	.5028	. 3620	.2925	.0908	. 8340	. 1659	26	48 44
20	35	.40008	.59992	2.4995	.43654	2.2907	1.0911	.08352	.91648	25	40
24	36	. 0035	. 9965	.4978	. 3689	.2889	.0913	. 8364	. 1636	24	36
28 32	37 38	. 0061	. 9938 . 9912	.4961 .4945	. 3723 . 3758	.2871 .2853	.0914	. 8375 . 8387	. 1625 . 1613	23 22	32 28
36	39	. 0115	9885	.4945	. 3793	.2835	.0915	. 8399	. 1601	$\frac{22}{21}$	28 24
40	40	.40141	.59858	2.4912	.43827	2.2817	1.0918	.08410	.91590	20	20
44	41	. 0168	. 9832	.4895	. 3862	.2799	.0920	. 8422	. 1578	19	16
48	42	. 0195	. 9805.	.4879	3897	.2781	.0921	. 8434	. 1566	18	12
52 56	43 44	. 0221	. 9778 . 9752	.4862 .4846	. 3932 . 3966	.2763 .2745	.0922	. 8445 . 8457	. 1554	17 16	8 4
35	45	.40275	.59725	2.4829	.44001	2.2727	1.0925	.08469	.91531	15	25
4	46	. 0301	. 9699	.4813	. 4036	.2709	.0927	. 8480	. 1519	14	56
8	47	. 3328	. 9672	.4797	. 4070	.2691	.0928	. 8492	. 1508	13	52
12 16	48 49	. 0354	. 9645 . 9619	.4780 .4764	. 4105 . 4140	.2673 .2655	.0929	. 8504 . 8516	. 1496 . 1484	$\begin{vmatrix} 12 \\ 11 \end{vmatrix}$	48
20	50	.40408	.59592	2.4748	.44175	2.2637	1.0932	.08527	.91472	10	40
24	51	. 0434	. 9566	.4731	. 4209	.2619	.0934	. 8539	. 1461	9	36
28	52	. 0461	. 9539	.4715	. 4244	.2602	.0935	. 8551	. 1449	8	32
32 36	53 54	. 0487	. 9512	4699	4279	.2584	.0936	. 8563	. 1437	7	28
40	55	. 0514	. 9486 .59469	.4683 2.4666	. 4314	.2566 2.2548	.0938 1.0939	. 8575	. 1425	6 5	$\frac{24}{20}$
44	56	. 0567	. 9433	.4650	. 4383	.2531	.0941	. 8598	. 1402	4	16
48	57	. 0594	. 9406	.4634	. 4418	.2513	.0942	. 8610	. 1390	3	12
52	58	. 0620	. 9379	.4618	. 4453	.2495	.0943	. 8622	. 1378	2	8
56 36	59 60	. 0647	. 9353 . 9326	.4602 .4586	. 4488	.2478 .2460	.0945	. 8634 . 8645	. 1366	$\frac{1}{0}$	24
M.S.	M	Cosine.		Secante.		Tangent.			Sine.	M	M.S.
7 ^h	113°				Natu			•		66°	4h

						TI LINE	· · · · · · · · · · · · · · · · · · ·	-			20
1 ^h	240		Natur	al Trig	conom	etrical	l Fund	ctions.	, -	155°	10h
M.S.	M	Sine.	Vrs.Cos.	Cosec'nte	Tang.	Cotang.	Secante.	Vrs. Sin	Cosine.	M	M.S
36	0	.40674	.59326	2.4586	.44523	2.2460	1.0946	.08645	.91354	60	24
4	1	. 0700	. 9300	.4570	. 4558		.0948	. 8657	. 1343		56
8	2	. 0727	. 9273	.4554	. 4593	.2425	.0949	. 8669	. 1331	58	52
12	3 4	. 0753	. 9247	.4538	. 4627	.2408	.0951	8681	. 1319	57	48
16	5	. 0780	. 9220	.4522	. 4662	.2390	.0952	. 8693	. 1307	56	44
20 24	6	.40806	.59193	2.4506	.44697	2.2373	1.0953	.08705	.91295	55	40
28	7	. 0833	. 9167	.4490	4732	.2355	.0955	8716	. 1283	54	36
32	8	. 0886	9140	.4474 .4458	. 4767 . 4802	.2338	.0956	. 8728 . 8740	. 1271	53	32 28
36	9	0913	9087	.4442	. 4837	.2303	.0958	8752	. 1260 . 1248	52 51	24
40	10	.40939	59061	2.4426	.44872	2.2286	1.0961	.08764	.91236	50.	20
44	11	. 0966	. 9034	.4411	4907	.2268	.0962	. 8776	. 1224	49	16
48	12	. 0992	. 9008	.4395	. 4942	.2251	.0963	. 8788	. 1212	48	12
52	13	. 1019	. 8981	.4379	. 4977	.2234	.0965	. 8800	. 1200	47	8
56	14	. 1045	. 8955	.4363	. 5012	.2216	.0966	. 8812	. 1188	46	4
37	15	.41072	.58928	2.4347	.45047	2,2199	1.0968	.08824	.91176	45	23
4	16	. 1098	. 8901	.4352	. 5082	.2182	.0969	. 8836	. 1164	44	56
8	17	. 1125	. 8875	.4316	. 5117	.2165	.0971	. 8848	. 1152	43	52
12	18	. 1151	. 8848	.4300	. 5152	.2147	.0972	. 8860	. 1140	42	48
16 20	19 20	. 1178 .41204	. 8822	.4285 2.4269	. 5187	.2130 2.2113	.0973	. 8872	. 1128	41 40	44 40
24	21	. 1231	. 8769	.4254	. 5257	.2096	1.0975	. 8896	. 1104	39	36
28	22	. 1257	8742	.4238	5292	2079	.0978	. 8908	. 1092	38	32
32	23	. 1284	8716	.4222	5327	2062	.0979	. 8920	. 1080	37	28
36	24	. 1310	8689	.4207	. 5362	2045	.0981	. 8932	. 1068	36	24
40	25	.41337	.58663	2.4191	.45397	2.2028	1.0982	.08944	.91056	35	20
44	26	. 1363	. 8636	.4176	. 5432	.2011	.0984	. 8956	. 1044	34	16
48	27	. 1390	. 8610	.4160	. 5467	1994	.0985	. 8968	. 1032	33	12
52	28	. 1416	. 8584	.4145	. 5502	.1977	.0986	. 8980	. 1020	32	8
56	29	. 1443	. 8557	.4130	. 5537	.1960	.0988	. 8992	. 1908	31	4
38	30	.41469	.58531	2.4114	.45573	2.1943	1.0989	10000	.90996	30	22
4	31	. 1496	. 8501	.4099	. 5608	.1926	.0991	. 9016	. 0984	29 28	56 52
8 12	32 33	. 1522	. 8478 . 8451	.4083 .4068	. 5643	.1892	.0992	9040	. 0960	27	48
16	34	1575	. 8425	.4053	5713	.1875	.0995	. 9052	. 0948	26	44
20	35	.41602	.58398	2.4037	.45748	2.1859	1.0997	.09064	.90936	25	40
24	36	. 1628	8372	.4022	. 5783	.1842	.0998	. 9076	. 0924	24	36
28	37	. 1654	. 8345	.4007	. 5819	.1825	.1000	. 9088	. 0911	23	32
32	38	. 1681	. 8319	.3992	. 5854	.1808	.1001	. 9101	. 0899	22	28
36	39	. 1707	. 8292	.3976	. 5889	.1792	.1003	. 9113	. 0887	21	24
40	40	.41734	.58266	2.3961	.45924	2.1775	1.1004	.09125	.90875	20	20
44	41	. 1760	. 8240	.3946	. 5960	.1758	.1005	9137	. 0863	19	16
48	42	. 1787	. 8213	.3931	. 5995	.1741	.1007	. 9149 . 9161	. 0851	18 17	12 8
52	43 44	. 1813 . 1839	. 8187 . 8160	.3916 .3901	. 6030 . 6065	.1725 .1708	.1008 .1010	. 9173	. 0826	16	4
56 39	44 45	.41866	.58134	2.3886	.46101	2.1692	1.1011	.09186	.90814	15	21
4	$\begin{vmatrix} 45 \\ 46 \end{vmatrix}$. 1892	. 8108	.3871	6136	.1675	.1013	. 9198	. 0802	14	56
8	47	1919	. 8081	.3856	6171	.1658	.1014	. 9210	. 0790	13	52
12	48	. 1945	. 8055	.3841	. 6206	.1642	.1016	. 9222	. 0778	12	48
16	49	. 1972	. 8028	.3826	. 6242	.1625	.1017	. 9234	. 0765	11	44
20	50	.41998	.58002	2.3811	.46277	2.1609	1.1019	.09247	.90753	10	40
24	51	. 2024	. 7975	.3796	. 6312	.1592	.1020	. 9259	. 0741	9	36
28	52	. 2051	7949	.3781	. 6348	.1576	.1022	. 9271	. 0729	8	32
32	53	. 2077	7923	.5766	. 6383	.1559	.1023	$\begin{array}{c c} . & 9283 \\ . & 9296 \end{array}$. 0717	$\frac{7}{6}$	28 2 1
36	54	. 2103	. 7896	.3751	. 6418	$\begin{array}{c c} .1543 \\ 2.1527 \end{array}$.1025 1.1026	.09308	.90692	5	20
40	55	.42130	.57870	2.3736	. 46454	.1510	.1028	. 9320	. 6680	4	16
44	$\begin{vmatrix} 56 \\ 57 \end{vmatrix}$. 2156 . 2183	. 7844 . 7817	.3706	6524	.1494	.1028	. 9332	. 0668	3	12
48 52	58	2209	7817	.3691	6560	.1478	.1031	. 9345	. 0655	$\overset{\circ}{2}$	8
56	59	2235	7764	.3677	6595	.1461	.1032	. 9357	. 0643	1	4
40	60	2262	7738	.1662	. 6631	.1445	.1034	. 9369	. 0631	0	20
M.S.	M	Cosine.	Vrs.Sin.		Cotang.	Tangent.	Cosec nt	Vrs. Cos	Sine.	M	M.S.
7h	114°)			Natu	ral.				65°	411

1					ATURA		•				
1 7 5	aro								1	E 40	10h
1h	25°		Natur	al Trig	conom	etrica	l Fund	ctions	. 1	54°	10
M.S.	M	Sine.	Vrs. Cos.	Cosec'nte	Tang.	Cotang.	Secante.	Vrs. Sin	Cosine.	M	M.S.
40	0	.42262	.57738	2.3662	.46631	2.1445	1.1034	.09369	.90631	60	20
4	1	. 2288	. 7712	.3647	. 6666	.1429	.1035	. 9381	. 0618	59	56
8	2	. 2314	. 7685	.3632	. 6702	.1412	.1037	. 9394	. 0606	58	52
12	3	. 2341	. 7659	.3618	. 6737	.1396	.1038	. 9406	. 0594	57	48
16	4	. 2367	. 7633	.3603	. 6772	.1380	,1040	. 9418	. 0581	56	44 40
20	5 6	. 42394	. 7580	2.3588 .3574	.46808	2.1364	1.1041	.09431	.90569	55 54	36
24 28	7	. 2446	. 7554	.3559	6879	.1331	.1044	9455	. 0544	53	32
32	8	. 2473	. 7527	.3544	. 6914	.1315	.1046	9468	. 0532	52	28
36	9	. 24 99	. 7501	.3530	. 6950	.1299	.1047	. 9480	. 0520	51	24
40	10	.42525	.57475	2.3515	.46985	2.1283	1.1049	.09492	.90507	50	20
44	11	. 2552	. 7448	.3501	. 7021	.1267	.1050	. 9505	. 0495	49	16
48	12	. 2578	. 7422	.3486	. 7056	.1251	.1052	. 9517	. 0483	48	12
52	13	. 2604	. 7396	.3472	. 7092	.1235	.1053	. 9530	. 0470	47	8
56	14	2630	. 7369	.3457	. 7127	.1219	.1055	. 9542	. 0458	46	4
41	15	.42657	.57343	2.3443	.47163	2.1203	1.1056	.09554	.90445	45 44	19 56
8	16 17	. 2683	. 7317 . 7290	.3428 .3414	. 7234	.1187	.1058	. 9567	. 0433	43	52
12	18	2736	. 7264	.3399	7270	.1155	.1055	. 9592	. 0408	42	48
16	19	2762	7238	.3385	. 7305	.1139	.1062	. 9604	. 0396	41	44
20	20	.42788	.57212	2.3371	.47341	2.1123	1.1064	.09617	.90383	40	40
24	21	. 2815	. 7185	.3356	. 7376	.1107	.1065	. 9629	. 0371	39	36
28	22	. 2841	. 7159	.3342	. 7412	.1092	.1067	. 9641	. 0358	38	32
32	23	. 2867	. 7133	.3328	. 7448	.1076	.1068	. 9654	. 0346	37	28
36	24	2893	. 7106	.3313	. 7483	.1060	.1070	. 9666	. 0333	36	24
40	25	.42920	.57080	2.3299	.47519	2.1044	1.1072	.09679	.90321	35 34	20 16
44 48	26 27	. 2946	. 7054	.3285 .3271	. 7555 . 7590	.1028	.1073	. 9691 . 970 1	. 0308	33	12
52	28	. 2998	. 7001	.3256	7626	.0997	.1076	. 9716	. 0283	32	8
56	29	3025	6975	.3242	7662	.0981	.1078	. 9729	. 0271	31	4
42	30	.43051	.56949	2.3228	.47697	2.0965	1.1079	.09741	.90258	30	18
4	31	. 3077	. 6923	.3214	. 7733	.0950	.1081	. 9754	. 0246	29	56
8	32	. 3104	. 6896	.3200	. 7769	.0934	.1082	. 9766	. 0233	28	52
12	33	. 3130	. 6870	.3186	. 7805	.0918	.1084	. 9779	. 0221	27	48
16	34	. 3156 .43182	. 6844	.3172	. 7840	.0903	.1085	. 9792	. 0208	26	44
20 24	35 36	. 3208	.56818	2.3158 .3143	.47876 . 7912	2.0887	1.1087 .1088	.09804	.90196	25 24	40 36
28	37	3235	6765	.3129	7948	.0856	.1090	. 9829	. 0171	23	32
32	38	. 3261	6739	.3115	7983	.0840	.1092	. 9842	. 0158	22	28
36	39	. 3287	. 6713	.3101	. 8019	.0825	.1093	. 9854	. 0145	21	24
40	40	.43313	.56686	2.3087	.48055	2.0809	1.1095	.09867	.90133	20	20
44	41	. 3340	. 6660	.3073	. 8091	.0794	.1096	. 9880	. 0120	19	16
48	42	. 3366	. 6634	.3059	. 8127	.0778	.1098	. 9892	. 0108	18	12
52	43	. 3392	. 6608	.3046	. 8162	.0763	.1099	. 9905	. 0095	17	8
56 4.3	44 45	. 3418 .43444	. 6582	.3032 2.3018	. 8198 .48234	.0747	.1101	. 9917	. 0082	16 15	4
4	46	. 3471	. 6529	.3004	. 8270	2.0732 0717	1.1102 .1104	. 9943	. 0057	14	56
8	47	. 3497	. 6503	.2990	. 8306	.0701	.1104	. 9955	. 0044	13	52
12	48	. 3523	6477	.2976	. 8342	.0686	.1107	. 9968	. 0032	12	48
16	49	. 3549	. 6451	.2962	8378	.0671	.1109	. 9981	. 0019	11	44
20	50	.43575	.56424	2.2949	.48414	2.0655	1.1110	.09993	.90006	10	40
24	51	. 3602	. 6398	.2935	. 8449	.0640	.1112	.10006	.89994	9	36
28	52	. 3628	6372	.2921	. 8485	.0625	.1113	. 0019	. 9981	8	32
32	53 54	. 3654 : 3680	6346	.2907	8521	.0609	.1115	. 0031	. 9968	7	28
36 40	54 55	. 3680	. 6320 .56294	.2894 2.2880	. 8557 .48593	.0594 2.0579	.1116 1.1118	. 0044	. 9956 .89943	6 5	24 20
44	56	. 3732	. 6267	.2866	. 8629	.0564	.1120	. 0070	. 9930	4	16
48	57	3759	. 6241	.2853	. 8665	.0548	.1121	. 0082	. 9918	3	12
52	58	3785	6215	.2839	. 8701	.0533	.1123	. 0095	9905	2	8
56	59	. 3811	. 6189	.2825	. 8737	.0518	.1124	. 0108	. 9892	1	4
44	60	. 3837	. 6163	.2812	. 8773	.0503	.1126	. 0121	. 9879	0	16
M.S.		Cosinc.	Vrs. Sin.	Secante.		Tangent.	Cosec'nt	Vrs.Cos	Sine.	M	M.S.
7 ^h	115°				Natu	ral.				64°	4h

-						TURAL	131111201					2.56
-	3 h	26°		Natur	al Trig	gonom	etrica	l Fun	ctions		153°	10 ^h
	M.S.	M	Sine.		Cosec'nte			Secante.				M.S.
Ì	44	0	.43837	.56163	2.2812	.48773	2.0503	1.1126	.10121	89579	60	16
	4	1	. 3863	. 6137	.2798	. 8809	.0488	.1127	. 0133	. 9867	59	56
1	8	2	. 3889	. 6111	.2784	. 8845	.0473	.1129	. 0146	. 9854	58	52
	12	3	. 3915	. 6084	.2771	. 8881	.0458	.1131	. 0159	. 9841	57	48
	16	4	. 3942	. 6058	.2757	. 8917	.0443	.1132	. 0172	. 9828	56	44
	20	5	.4 3968 . 3994	.56032	2.2744 .2730	.48953	2.0427	1.1134	10184	.89815	55	40
۱	24 28	7	4020	. 5980	.2717	. 8989	.0412	.1135 .1137	. 0197	. 9803	54	36
	32	8	4046	. 5954	.2703	9062	.0382	.1139	. 0210	9790	53 52	32 28
	36	9	4072	5928	.2690	. 9098	.0367	.1140	0223	9764	51	24
1	40	10	.44098	.55902	2.2676	.49134	2.0352	1.1142	10248	.89751	50	20
	44	11	. 4124	. 5875	.2663	. 9170	.0338	.1143	0261	9739	49	16
	48	12	. 4150	. 5849	.2650	. 9206	.0323	.1145	. 0274	. 9726	48	12
	52	13	. 4177	. 5823	.2636	. 9242	.0308	.1147	. 0287	. 9713	47	8
	56	14	. 4203 .44229	. 5797	.2623	. 9278	.0293	.1148	. 0300	. 9700	46	4
	45	15 16	. 4255	.55771	2.2610 .2596	. 49314	2.0278	1.1150	.10313	.89687	45	15
	8	17	4281	5719	.2583	9387	.0203	.1153	0338	9674	44 43	56 52
	12	18	4307	5693	.2570	9423	.0233	.1155	0351	9649	42	48
	16	19	. 4333	. 5667	.2556	. 9459	.0219	.1156	0364	9636	41	44
	20	20	.44359	.55641	2.2543	.49495	2.0204	1.1158	10377	.89623	40	40
1	24	21	. 4385	. 5615	.2530	. 9532	.0189	.1159	. 0390	. 9610	39	36
ł	28	22	. 4411	. 5589	.2517	. 9568	.0174	.1161	. 0403	. 9597	38	32
	32	23	. 4437	5562	.2503	. 9604	.0159	.1163	. 0416	. 9584	37	28
ı	36 40	24 25	.44489	. 5536 .55 51 0	2490 2.2477	. 9640	.0145 2.0130	.1164	. 0429	. 9571	36 35	24 20
	41	26	. 4516	. 5484	.2464	9713	.0115	.1167	0455	. 9545	34	16
	48	27	. 4542	. 5458	.2451	. 9749	.0101	.1169	0468	9532	33	12
	52	28	. 4568	. 5432	.2438	. 9785	.0086	.1171	0481	. 9519	32	8
1	56	29	. 4594	. 5406	.2425	. 9822	.0071	.1172	. 0493	. 9506	31	4
	46	30	.44620	.55380	2.2411	.49858	2.0057	1.1174	.10506	.89493	30	14
ı	4	31	4646	5354	.2398	. 9894	.0042	.1176	. 0519	. 9480	29	56
	8 12	32 33	. 4672	5328	.2385 .2372	. 9931	.0028	.1177	0532	9467	28 27	52 48
ı	16	34	4724	5276	.2359	.50003	1.9998	.1180	0558	9441	26	44
	20	35	.44750	.55250	2.2346	.50040	1.9984	1.1182	.10571	.89428	25	40
1	24	36	. 4776	. 5224	.2333	. 0076	.9969	.1184	. 0584	. 9415	24	36
İ	28	37	. 4802	. 5198	.2320	. 0113	.9955	.1185	. 0598	. 9402	23	32
	32	38	. 4828	. 5172	.2307	. 0149	.9940	.1187	. 0611	. 9389	22	28
1	36	39	. 4854	. 5146 .55120	.2294	. 0185	.9926	.1189	. 0624	\$376	21	24
1	40 44	40	.44880	. 5094	2.2282 .2269	.50222	1.9912	1.1190 .1192	. 10637	.89363	20 19	20 16
1	48	42	4932	5068	.2256	. 0295	.9883	.1193	0663	9337	18	12
1	52	43	. 4 958	. 5042	.2243	. 0331	9868	.1195	. 0676	. 9324	17	8
	56	44	. 4984	. 5016	.2230	. 0368	.9854	.1197	. 0689	. 9311	16	4
	47	45	.45010	54990	2.2217	.50404	1.9840	1.1198	.10702	.89298	15	13
	4	46	5036	4964	.2204	0441	.9825	.1200	0715	9285	14	56
	8 12	47 48	. 5062	. 4938 . 4912	.2192 .2179	. 0477	.9811	.1202	. 0728	. 9272	13 12	52 48
	16	49	. 5114	4886	.2166	. 0550	.9782	.1205	0754	9245	11	44
-	20	50	.45140	.54860	2.2153	.50587	1.9768	1.1207	.10768	.89232	10	40
1	24	51	. 5166	. 4834	.2141	. 0623	.9754	.1208	. 0781	. 9219	9	36
	28	52	. 5191	. 4808	.2128	. 0660	9739	.1210	. 0794	. 9206	8	32
	32	53	. 5217	. 4782	.2115	. 0696	.9725	.1212	0807	. 9193	7	28
	36	54	. 5243	. 4756	.2103	. 0733	.9711	.1213	0820	. 9180	6	24
1	40 44	55 56	.45269 . 5295	.54730 . 4705	2.2090 .2077	.50769	1.9697 .9683	1.1215 .1217	.1 6 833 . 0846	.8 9 166	5 4	20 16
	48	57	. 5321	4679	.2065	0843	.9668	.1218	. 0860	. 9140	3	12
1	52	58	. 5347	4653	.2052	0879	.9654	.1220	. 0873	. 9127	2	8
	56	53	. 5373	4627	.2039	. 0916	.9640	.1222	. 0886	. 9114	1	4
	48	60	. 5399	. 4601	.2027	. 0952	.9626	.1223	. 0899	. 9101	0	12
1	M.S.	M	Cosine.	Vrs. Sin.	Secante.		Tangent.	Cosec'nt	Yrs. Cus	Sine.		M.S.
-	711	116°				Natu	ral.				63°i	4"
-												

1 h	279)	Natur	al Trig	onom	etrica	l Fun	ctions	.]	152°	10h		
M. S	. M	Sine.		Cosec'nte	Tang.	Cotang.		Vrs. Sin			M.S.		
1,8		.45399	.54001	2.2027	.50952	1.9626	1.1223	.10899	.89101	60	12		
4		5425	. 4575	.2014	. 0989	.9612	.1225	. 0912	. 9087	59	56 52		
8 12	2 3	. 5451	. 4549	.2002	. 1026	.9598	.1226	. 0926	. 9074	58 57	48		
16	4	5503	4497	.1977	1002	.9570	.1230	. 0953	9048	56	44		
20	5	.45528	.54471	2.1964	.51136	1.9556	1.1231	.10965	.89034	55	40		
24	6	. 5554	. 4445	.1952	. 1172	.9542	.1233	. 0979	. 9021	54	36		
28	7	. 5580	. 4420	.1939	. 1209	.9528	.1235	. 0992	. 9008	53	32		
32	8	. 5606	. 4394	.1927	. 1246	.9514	.1237	. 1005	. 8995	52	28		
36	9	. 5632 .45658	. 4368	.1914 2.1902	. 1283	.9500 1.9486	1.1238 1.1240	.1018	.8981	51 50	24 20		
40	10 11	. 5684	. 4316	.1889	. 1356	.9472	.1242	.11032	. 8955	49	16		
48	12	. 5710	4290	.1877	. 1393	.9458	.1243	1058	8942	48	12		
52	13	. 5736	. 4264	.1865	. 1430	.9444	.1245	. 1072	. 8928	47	8		
56	14	. 5761	. 4238	.1852	. 1466	.9430	.1247	. 1085	. 8915	46	4		
49		.45787	.54213	2.1840	.51503	1.9416	1.1248	.11098	.88902	45	56		
8	16 17	. 5813	. 4187	.1828	. 1540	.9402	.1250 .1252	. 1112	8888	44 43	52		
12	18	. 5865	. 4135	.1803	. 1614	.9375	.1253	1138	8862	42	48		
16	19	. 5891	4109	.1791	. 1651	.9361	.1255	. 1152	. 8848	41	41		
20	20	.45917	.54083	2.1778	.51687	1.9347	1.1257	.11165	.88835	40	40		
24	21	5942	. 4057	.1766	. 1724	.9333	.1258	. 1178	. 8822	39	36		
28	22	5968	4032	.1754	. 1761	.9319	.1260	. 1192	. 8808 . 8795	38	32 28		
32 36	23 24	• 5994 • 6020	. 4006	.1742 .1730	. 1835	.9292	.1262	. 1205	. 8781	37 36	24		
40	25	.46046	.53954	2.1717	.51872	1.9278	1.1265	.11232	.88768	35	20		
41	26	. 6072	. 3928	.1705	. 1909	.9264	.1267	. 1245	. 8755	34	16		
48	27	. 6097	. 3902	.1693	. 1946	.9251	.1269	. 1259	. 8741	33	12		
52	28	6123	. 3877	.1681	. 1983	.9237	.1270	. 1272	. 8728	32	8		
56	29	• 6149 •46175	.53825	$\begin{array}{c} .1669 \\ 2.1657 \end{array}$. 2020 .52057	.9223 1.9210	.1272	. 1285	.8714	31 30	10		
50	30 31	• 6201	. 3799	.1645	. 2094	.9196	.1275	. 1312	. 8688	29	56		
8	32	6226	. 3773	.1633	. 2131	.9182	.1277	. 1326	. 8674	28	52		
12	33	. 6252	. 3748	.1620	. 2168	.9169	.1279	. 1339	. 8661	27	48		
16	34	. 6278	. 3722	.1608	. 2 205	.9155	.1281	. 1353	. 8647	26	44		
20	35	.46304	.53696	2.1596	.52242	1.9142	1.1282	.11366	.88634	25	40		
24 28	36	• 6330 • 6355	. 3645	.1584	. 2279	.9128 .9115	.1284	. 1380 1393	. 8620	24 23	36 32		
32	38	6381	3619	.1560	2353	.9101	.1287	. 1407	. 8593	22	28		
36	39	6407	3593	.1548	. 2390	.9088	.1289	1420	. 8580	21	24		
40	40	.46433	.53567	2. 15 36	.52427		1.1291	.11434	.88566	20	20		
44	41	• 6458	. 3541	.1525	. 2464	.9061	.1293	. 1447	. 8553	19	16		
48	42	• 6484 • 6510	. 3516 . 3490	.1513	25012538	.9047	.1294 .1296	1461	8539	18	12 8		
52 56	43	6536	3464	.1501 .1489	2575	.9034	.1296	. 1474	. 8526 . 8512	17 16	4		
51	45	46561	.53438	2.1477	.52612	1.9007	1.1299	.11501	.88499	15	9		
4	46	- 6587	. 3413	.1465	. 2650	.8993	.1301	. 1515	. 8485	14	56		
8	47	• 6613	. 3387	.1453	. 2687	.8980	.1303	. 1528	. 8472	13	52		
12	48	6639	. 3361	.1441	2724	.8967	.1305	. 1542	. 8458	12	48		
16 20	49 50	. 6664 .46690	.53310	.1430 2.1418	. 2761	.8953 1. 8940	.1306 1.1308	. 1555	. 8444	11 10	44 40		
24	51	6716	. 3284	.1406	. 2836	.8927	.1310	. 1583	. 8417	9	36		
28	52	. 6741	. 3258	.1394	. 2873	.8913	.1312	1596	. 8404	8	32		
32	53	- 6767	. 3233	.1382	. 2910	.8900	.1313	. 1610	. 8390	7	28		
36	54	6793	. 3207	.1371	. 2947	.8887	.1315	. 1628	. 8376	6	24		
40	55	.46819	.53181	2.1359	.52984	1.8873	1.1317	.11637	.88363	5	20		
48	56 57	• 6844 • 6870	. 3156 . 3130	.1347 .1335	. 3022 . 3059	.8860 .8847	.1319 .1320	. 1651	. 8349	4 3	$\begin{array}{c c} 16 \\ 12 \end{array}$		
52	58	. 6896	3104	.1324	. 3096	.8834	.1322	. 1678	. 8322	2	8		
56	59	. 6921	. 3078	.1312	. 3134	.8820	.1324	. 1691	. 8308	1	4		
52	60	6947	. 3053	.1300	3171	.8807	.1326	. 1705	. 8295	0	8		
M.S. 7h	М 117	Cosine.	vrs. Sin.	Secante.			Cosec'nt	Vrs. Cos	Sinc.	м 62°	M S. 4h		
	1111				Natu	ral.				04-1	4"		

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	1h·	289									1 = 1 0	lanh
	1"	40		Natur	al Triş	gonon	etrica	l Fun	ctions	•	101	10 ^h
	W.S.	M	Sine.	Vrs.Cos.	Coscc'nte	Tang.	Cotang.	Secante.	Vrs. Sin	Cosine.	M	M.S.
	5,2	()	.46947	.53053	2.1300	.53171	1.8807	1.1326	.11705	.88295	60	8
	4	1	. 6373	. 3027	.1289	. 3208	.8794	.1327	. 1719	. 8281	59	56
	8	2	. 6998	. 3001	.1277	. 3245	.8781	.1329	. 1732	. 8267	58	52
	12	3	. 7021	. 2976	.1266	. 3283	.8768	.1331	. 1746	. 8254	57	48
	16	4 5	. 7050 .47075	. 2950 .52924	.1254 2.1242	3320	.8754	.1303	. 1760	. 8240	56	44
	20 24	6	. 7101	. 2899	.1231	.53358	1.8741 .8728	1.1334	.11774	.88226	55	40 36
	28 28	7	7127	2873	.1219	. 3432	.8715	.1338	. 1787	. 8199	54 53	32
	32	8	7152	2847	.1208	3470	.8702	.1340	. 1815	8185	52	28
	36	9	. 7178	. 2822	.1196	. 3507	8689	.1341	1828	8171	51	24
	40	10	.47204	.52796	2.1185	.53545	1.8676	1.1343	.11842	.88158	50	20
	44	11	. 7229	. 2770	.1173	. 3582	.8063	.1345	. 1856	. 8144	49	16
	48	12	. 7255	. 2745	.1162	. 3619	.8650	.1347	. 1870	. 8130	48	12
	52	13	. 7281	. 2719	.1150	. 3657	.8637	.1349	. 1883	. 8117	47	8
	56	14	7306	. 2694	.1139	. 3694	.8624	.1350	. 1897	. 8103	46	4
	53	15	.47332	.52668	2.1127 .1116	.53732	1.8611	1.1352	.11911	.88089	45	7
	4 8	$\begin{array}{c} 16 \\ 17 \end{array}$	7383	2617	.1104	. 3807	.8598 .8585	.1354	. 1925 . 1938	. 8075	44 43	56 52
	12	18	7409	2591	.1093	. 3844	.8572	.1357	1952	. 8048	42	48
	16	19	. 7434	2565	.1082	. 3882	.8559	.1359	1966	. 8034	41	41
	20	$\frac{1}{20}$.47460	.52540	2.1070	.53919	1.8546	1.1361	11980	.88020	40	40
	24	21	. 7486	. 2514	.1059	. 3957	.8533	.1363	. 1994	. 80:6	39	36
	28	22	. 7511	. 2489	.1048	. 3995	.8520	.1365	. 2007	. 7932	38	32
	32	23	. 7537	. 2463	.1036	. 4032	.8507	.1366	. 2021	. 7979	37	28
	36	24	. 7562	. 2437	.1025	. 4070	.84 15	.1368	2035	. 79/5	36	24
ı	40	25	47588	.52412	2.1014	.54107	1.8482	1.1370	.12049	.87951	35	20
	41	26 27	. 7613 . 7639	. 2386	.1002 .0391	. 4145	.8469 .8456	.1372	2063 2077	. 7937 . 7923	34	16 12
	48 52	$\frac{21}{28}$	7665	2335	.0980	. 4220	.8443	.1375	2030	7909	32	8
	56	29	. 7630	2310	.0969	. 4258	.8430	.1377	2104	. 7895	31	4
٠	54	30	.47716	.52284	2.0957	.54295	1.8418	1.1379	.12118	.87882	30	6
	4	31	. 7741	. 2258	.0946	. 4333	.8405	.1381	. 2132	. 7868	29	56
	8	32	. 7767	. 2233	.0935	. 4371	.8392	.1382	. 2146	. 7854	28	52
ı	12	33	. 7792	. 2207	.0924	. 4409	.8379	.1384	. 2160	. 7540	27	48
ı	16	34	. 7818	. 2182	.0912	. 4116	.8367	.1386	. 2174	. 7826	26	44
ı	20	35	.47844	.52156	2.0901 $.0890$.51484	1.8354 .8341	1.1388 .1390	.12188	.87812 . 77.38	25 24	40 36
ı	24 28	$\begin{array}{c} 36 \\ 37 \end{array}$	7895	2105	.0879	. 4559	.83 29	.1391	2216	. 7784	23	32
	32	38	. 7920	2080	.0868	. 4597	.8316	.1393	. 2229	. 7770	22	:8
	36	39	. 7946	. 2054	.0857	. 4635	.8303	.1395	2243	. 7756	21	24
	40	40	.47971	.52029	2.0846	.54673	1.8291	1.1397	.12257	.87742	20	20
	44	41	. 7997	. 2003	.0835	. 4711	.8278	.1399	. 2271	. 7728	19	16
	48	42	. 8022	. 1978	.0824	. 4748	.8265	.1401	. 2285	. 7715	18	12
	52	43	8049	. 1952	.0812	4786	.8253	.1402	. 2299	7701	17	8
	56	44	. 8073 .48099	. 1927 .51901	.0801 2.0790	. 4824	.8240 1.8227	.1404 1.1406	.:313 $.12327$. 76 7 .87673	16 15	5
	55	45 46	. 8124	. 1876	.0779	. 4900	.8215	.1408	2341	. 7659	14	56
	8	47	. 8150	. 1850	.0768	4937	.8202	.1410	. 2355	. 7645	13	52
	12	48	. 8175	. 1825	.0757	. 4975	.8190	.1411	. 2369	. 7631	12	48
Ì	16	40	. 8201	. 1799	.0746	. 5013	.8177	.1413	. 2383	. 7617	11	44
	:'0	59	.48226	.5177-	2.0735	. 55051	1.8165	1.1415	.12397	.87603	10	40
1	24	51	8252	. 1748	.0725	. 5089	.8152	.1417	. 2411	. 7588	9	36
	28	52	8277	1723	.0714	5127	.8140	.1419	2425	7574	8	32
	32	53	. 8303 . 8328	1697 1672	.0703 .0692	. 5165 . 5203	.8127	.1421 .1422	. 2439	. 7560 . 7546	$\begin{bmatrix} 7 \\ 6 \end{bmatrix}$	28 24
	36 40	54 55	.48354	.51646	2.0681	.55241	1.8102	1.1424	.12468	.87532	5	20
	44	56	. 8379	. 1621	.0670	. 5279	.8090	.1426	. 2482	. 7518	4	16
	48	57	. 8405	1595	.0659	5317	.8078	.1428	. 2496	. 7501	3	12
	52	58	. 8430	. 1570	.0648	. 5355	.80/35	.1430	. 2510	. 7490	2	8
	56	59	8455	. 1544	.0637	. 5393	.8053	.1432	. 2524	. 7476	1	4
1	56	60	. 8481	. 1519	.0627	. 5431	.8040	.1433	. 2538	. 7462	0	4
	M.S. 7h	м 118°		vrs. Sin.[Secante.		Tangent.	Cosec'nt	118. 008]	Sine.	61°	M S. 4h
1	-	119				Natu	rai.				01	1

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	J h	299			al Trig			l Fun	ctions	• -	150°	ļ	
	i. S.	M			Cosec'nte	_		Secante.			N .	M.S.	
	56	0	.48481	.51519	2.0627	.55431	1.8040	1.1433	12538	.87462	60	4 56	
	8	$\frac{1}{2}$. 8506 . 8532	. 1493	.0616 .0605	. 5469	.8028	.1435	. 2552	. 7448	59 58	52	
	12	3	. 8557	. 1443	.0594	. 5545	.8003	.1439	2580	7420	57	43	
	16	4	. 8583	. 1417	.0583	. 5583	.7991	.1441	2594	7405	56	44	
	20	5	.48608	.51392	2.0573	.55621	1.7979	1.1443	.12609	.87391	55	40	
	24	6	. 8633	. 1366	.0562	. 5659	.7966	.1445	. 2623	. 7377	54	36	
	28	7	. 8659	. 1341	.0551	. 5697	.7954	.1446	. 2637	. 7363	53	32	
	32	8	. 8684	. 1316	.0540	. 5735	.7942	.1448	. 2651	. 7349	52	28	
	36	£	. 8710	. 1290	.0530	. 5774	.7930	.1450	. 2665	. 7335	51	24	
	40	10	.48735	.51265	2.0519	.55812	1.7917	1.1452	.12679	.873.20	50	20	
	44 48	11	. 8760	. 1239	.0508	. 5850	.7905 .7893	.1454	2694 2708	. 7306 . 7292	49 48	16 12	
	52	12 13	. 8786	. 1189	0.0498 0.0487	. 5926	.7881	.1456	. 2708	7278	47	8	
	56	14	. 8837	. 1163	.0476	. 5964	.7868	.1459	2736	7264	46	4	
	57	15	.48862	.51138	2.0466	.56003	1.7856	1.1461	.12750	.87250	45	3	
	4	16	. 8887	. 1112	.0455	. 6041	.7844	.1463	. 2765	. 7235	44	56	
	8	17	. 8913	. 1087	.0444	. 6079	.7832	.1465	. 2779	. 7221	43	52	
	12	18	. 8938	. 1062	.0434	. 6117	.7820	.1467	. 2793	. 7207	42	48	
	16	19	. 8964	. 1036	.0423	. 6156	.7808	.1469	2807	. 7193	41	41	
	20	20	.48989	.51011	2.0413	.56194	1.7795	1.1471	.12821	.87178	40	40 36	
	24 28	21 22	. 9014	. 0986	.0402	. 6232	.7783 .7771	.1473	. 2836	. 7164	39 38	32	
	$\frac{20}{32}$	23	. 9065	. 0935	.0392	6309	.7759	.1476	. 2864	7136	37	28	
	36	24	. 9030	. 0910	.0370	. 6347	.7747	.1478	. 2879	7121	36	24	
	40	25	.49116	.50884	2.0360	.56385	1.7735	1.1480	.12893	.87107	35	20	
	41	26	. 9141	. 0859	.0349	. 6424	.7723	.1482	. 2907	. 7093	34	16	
	48	27	. 9166	. 0834	.0339	. 6462	.7711	.1484	. 2921	. 7078	33	12	
	52	28	. 9192	. 0808	.0329	. 6500	.7699	.1486	. 2936	. 7064	32	8	
	56	29	. 9217	. 0783	.0318	. 6539	.7687	.1488	. 2950	7050	31	4	
'	$\begin{bmatrix} 58 \\ 4 \end{bmatrix}$	30	.49242	.50758 . 0732	2.0308	.56577	1.7675 .7663	1.1489 .1491	.12964	.87035	30 29	2 56	
	8	$\begin{vmatrix} 31 \\ 32 \end{vmatrix}$. 9268	0707	0.0297 0.0287	. 6654	.7651	.1493	2993	. 7021	28	52	
	12	33	. 9318	0682	0276	. 6692	.7639	.1495	3607	. 6992	27	48	
	$\overline{16}$	34	. 9343	. 0656	.0266	. 6731	.7627	.1497	. 3022	6978	26	44	
	20	35	.49369	.50631	2.0256	.56769	1.7615	1.1499	.13036	.86964	25	40	
	24	36	. 9394	. 0606	-0245	. 6808	.7603	.1501	. 3050	. 6949	24	36	
	28	37	. 9419	. 0580	.0235	. 6846	.7591	.1503	3065	. 6935	23	32	
	32	38	. 9445	. 0555	.0224	. 6885	.7579	.1505	. 3079	. 6921	22	28	
	36	39	. 9470	. 0530	.0214	. 6923	.7567	.1507	.13108	. 6906	21	24 20	
	40 44	40 41	.49495 . 9521	. 0479	2.0204 .0194	. 7000	1.7555 .7544	1.1508 .1510	. 3122	.86892 . 6877	20 19	16	
	48	42	. 9546	. 0454	.0183	7039	.7532	.1512	3137	. 6863	18	12	
	52	43	9571	. 0429	.0173	. 7077	.7520	.1514	3151	. 6849	17	8	
	56	4!	. 9596	. 0404	.0163	. 7116	.7508	.1516	. 3166	. 6834	16	4	
	59	45	.49622	.50378	2.0152	.57155	1.7496	1.1518	.13180	.86820	15	1	
	4	46	. 9647	. 0353	.0142	. 7193	.7484	.1520	3194	. 6805	14	56	
	$\frac{8}{12}$	47	9672	. 0328	.0132	7232	.7473	.1522	. \$209	6791	13	52	
	12 16	48 49	. 9697 . 9723	. 0303	.0122	. 7270 . 7309	.7461 .7449	.1524	. 3223 . 3238	. 6776 . 6762	12 11	48	
	20	50	.49748	.50252	2.0101	.57348	1.7437	1.1528	.13252	.86748	10	40	
	24	51	. 9773	. 0227	.0091	. 7386	.7426	.1530	3267	. 6733	9	36	
	28	52	9798	. 0202	:0081	. 7425	.7414	.153 1	. 3281	. 6719	8	32	
	32	53	. 9823	. 0176	.0071	. 7464	.7402	.1533	. 3296	. 6704	7	28	
	36	54	. 9849	. 0151	.0061	. 7502	.7390	.1535	. 3310	. 6690	6	24	
	4()	55	.49874	.50126	2 0050	.57541	1.7379	1.1537	.13325	.86675	5	20	
	44 48	56	9899	. 0101	.0040	7580	.7367 7255	.1539	3339	. 6661	4	16	
	52	57 58	. 9924	. 0076	.0030	. 7619 . 7657	.7355 .7344	.1541 .1543	. 3354 . 3369	6646	3 2	12 8	
	56	59	. 9975	. 0025	.0010	. 7696	.7332	.1545	. 3383	. 6632	$\tilde{1}$	4	
	60	60	.50000	. 0000	.0000	. 7735	.7320	.1547	. 3397	. 6602	ō	0	
IN	1. S.	M	Cosine.		Secante.						M	M S.	
	7 ⁿ	119	O.			Natu	ral.				60°	4h	
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ļ	2h	300			7 507 4						1.400	lob
Ì		30		Natur	al Trig	conom	etrica!	Func	ctions.	-	149°	9h
	M.S.	M	Sine.		Cosec'nte	-	Cotang	Secante.	Vrs. Sin	Cosine.	M	M.S.
u de la composition della comp	0	$\begin{bmatrix} 0 \\ 1 \end{bmatrix}$.50000	.50000	2.0000	.57735	1.7320	1.1547	.13397	.86602	60	60
Ì	8	$\frac{1}{2}$. 0025	.49975	1.9990	. 7774		.1549	. 3412	. 6588	59	56
	12	3	. 0050	. 9950	.9980	. 7813	.7297	.1551	. 3426	. 6573	58	52
ı	16	4	. 0075	9924	.9970 .9960	. 7851 . 7890	.7286	.1553	. 3441	. 6559	57	48
ı	20	5	.50126	. 49874	1.9950	.57929	.7274 1.7262	1.1555	. 3456	. 6544	56	44
1	24	6	. 0151	. 9849	.9940	. 7968	.7251	.1559	. 3485	. 6515	55 54	40 36
	28	7	. 0176	9824	.9930	8007	.7239	.1561	3499	. 6500	53	32
ļ	32	8	. 0201	9799	.9920	. 8046	.7228	.1562	. 3514	6486	52	28
	36	9	. 0226	. 9773	.9910	. 8085	.7216	.1564	. 3529	. 6471	51	24
	40	10	.50252	.49748	1.9900	.58123	1.7205	1.1566	.13543	.86457	50	20
-	44	11	. 0277	. 9723	.9890	. 8162	.7193	.1568	, 3558	. 6442	49	16
	48	12	. 0302	. 9698	.9880	. 8201	.7182	.1570	. 3572	. 6427	48	12
	52 56	13 14	. 0327	. 9673	.9870	. 8240	.7170	.1572	. 3587	. 6413	47	8
	1	15	. 0352	. 9648	0.9860 0.9850	. 8279	.7159	.1574	3602	. 6398	46	4
	4	16	. 0402	. 9597	.9840	. 8357	1.7147 .7136	1.1576	. 3631	.86383	45 44	59 56
	8	17	. 0428	9572	.9830	. 8396	.7124	.1580	. 3646	. 6354	43	52
	12	18	. 0453	. 9547	.9820	. 8435	.7113	.1582	. 3660	6339	42	48
	16	19	. 0478	. 9522	.9811	. 8474	.7101	.1584	. 3675	. 6325	41	44
	20	20	.50503	.49497	1.9801	.58513	1.7090	1.1586	.13690	86310	40	40
	24	21	. 0528	. 9472	.9791	. 8552	.7079	.1588	. 3704	. 6295	39	36
ı	28	22	. 0553	. 9447	.9781	. 8591	.7067	.1590	. 3719	. 6281	38	32
И	32	23	. 0578	. 9422	.9771	. 8630	.7056	.1592	. 3734	. 6266	37	28
N	36	24	. 0603	. 9397	.9761	. 8670	.7044	.1594	. 3749	. 6251	36	24
I	40	25 26	.50628	.49371	1.9752 $.9742$.58709	1.7033 .7022	1.1596	.13763	.86237	35 34	20 16
1	48	27	. 0679	. 9340	.9732	. 8787	.7010	.1598 .1600	. 3778	6207	33	12
	52	28	0704	. 9296	.9722	. 8826	.6999	.1602	. 3807	6192	32	8
1	56	29	. 0729	. 9271	.9713	. 8865	.6988	.1604	. 3822	. 6178	31	4
1	2	30	.50754	.49246	1.9703	.58904	1.6977	1:1606	.13837	.86163	30	58
	4	31	. 0779	. 9221	.9693	. 8944	.6965	.1608	. 3852	. 6148	29	56
- }	8	32	. 0804	. 9196	.9683	. 8983	.6954	.1610	. 3867	. 6133	28	52
- 1	12	33	. 0829	. 9171	.9674	. 9022	.6943	.1612	. 3881	. 6118	27	48
ł	16	34	. 0854	. 9146	.9664	. 9061	.6931	.1614	. 3896	. 6104	26	44
-	20 24	35 36	.50879	.49121 . 9096	1.9654 .9645	.59100 . 9140	1.6920 6909	1.1616 .1618	.13911	.86089 6074	25 24	40 36
	28	37	. 0929	9071	.9635	. 9179	.6898	.1620	. 3941	6059	23	32
	32	38	. 0954	9046	.9625	. 9218	.6887	.1622	. 3955	. 6044	22	28
1	36	39	. 0979	. 9021	.9616	. 9258	.6875	.1624	. 3970	. 6030	21	24
1	40	40	.51004	.48996	1.9606	.59297	1.6864	1.1626	.13985	.86015	20	20
	44	41	. 1029	. 8971	.9596	. 9336	.6 853	.1628	. 4000	. 6000	19	16
	48	42	. 1054	. 8946	.9587	. 9376	.6842	.1630	. 4015	. 5985	18	12
	52	43	. 1079	8921	.9577	. 9415	.6831	.1632	4030	5970	17	8 4
	56 3	44	. 1104	. 8896 .48871	.9568 1.9558	. 59494	.6820 1.6808	.1634 1.1636	. 4044	. 5955	16 15	57
	4	$\begin{array}{c} 45 \\ 46 \end{array}$. 1154	. 8846	.9549	. 9533	.6797	.1638	. 4074	. 5926	14	56
	8	47	. 1179	. 8821	.9539	9572	.6786	.1640	4089	. 5911	13	52
1	12	48	. 1204	. 8796	.9530	. 9612	.6775	.1642	. 4104	. 5896	12	48
	16	49	. 1229	. 8771	.9520	. 9651	•.6764	.1644	. 4119	. 5881	11	44
1	20	50	.51254	.48746	1.9510	.59691	1.6753	1.1646	.14134	.85866	10	4 0
	24	51	. 1279	. 8721	.9501	. 9730	.6742	.1648	. 4149	. 5851	9	36
1	28	52	. 1304	. 8696	.9491	. 9770	.6731	.1650	. 4164	. 5836	8	32
	32	53	. 1329	8671	.9482	. 9809	.6720	.1652 $.1654$. 4178	. 5821 . 5806	7 6	28 24
1	36 40	54 55	. 1354	. 8646	.9473 1.9463	. 9849	$\begin{bmatrix} .6709 \\ 1.6698 \end{bmatrix}$	1.1656	.14208	.85791	5	$\begin{vmatrix} 24 \\ 20 \end{vmatrix}$
	41	56 56	. 1404	. 8596	.9454	. 9928	.6687	.1658	. 4223	5777	4	16
1	48	57	. 1429	8571	.9444	9967	.6676	.1660	4238	. 5 762	3	12
	52	58	. 1454	. 8546	.9435	.60007	.6665	.1662	. 4253	. 5747	2	8
	56	59	. 1479	. 8521	.9425	. 0046	.6654	.1664	. 4268	. 5732	1	4
1	4	60	. 1504	. 8496	.9416	. 0086	.6643	.1666	. 4283	. 5717	0	56
	M.S.	M		Vrs.Sin.	Secante.		Tangent.	Cosec'nt	vrs. Cos	Sine.	M 500	M.S.
1	8h	120°				Natu	ral.				59°	9.
200	-											-

	2 ^h	319		Natur	al Trig	gonom	etrica	l Fun	ctions		148°	9h
	M.S.	M	Sine.	Vrs. Cos.	Cosec'nte	Tang.	Cotang.	Secante.	Vrs. Sin	Cosine.	M	M.S.
Ì	4	0	.51504	.48496	1.9416	.60086	1.6643	1.1666	.14283	.85717	60	56
	4	1	. 1529	8471	.9407	. 0126	.6632	.1668	. 4298	5702	59	56
	8	2	. 1554	8446	.9397	. 0165	.6621	.1670	4313	. 5687	58 57	52 48
	12 16	3 4	. 1578 . 1603	. 8 4 21 . 8396	.9388 .9378	. 0205	.6610	.1672	. 4328 . 4343	5672	56	44
	20	5	.51628	.48371	1.9369	.60284	1.6588	1.1676	.14358	.85642	55	40
1	24	6	. 1653	. 8347	.9360	. 0324	.6577	.1678	. 4373	. 5627	54	36
1	28	7	. 1678	. 8322	.9350	. 0363	.6566	.1681	. 4388	. 5612	53	32
1	32	8	. 1703	. 8297	.9341	. 0403	.6555	.1683	. 4403	. 5597	52	28
1	36	9	. 1728	. 8272	1.9332 1.9322	. 0443	.6544	.1685	. 4418	. 5582	51	24
1	40 44	10 11	.51753	.48247	.9313	. 60483	1.6534 .6523	1.1687 .1689	.14433	.85566	50 49	20 16
	48	12	1803	. 8197	.9304	. 0562	.6512	.1691	. 4463	5536	48	12
	52	13	. 1827	. 8172	.9295	. 0602	.6501	.1693	. 4479	. 5521	47	8
1	56	14	. 1852	. 8147	.9285	. 0642	.6490	.1695	. 4494	. 5506	46	4
1	5	15	.51877	.48123	1.9276	.60681	1.6479	1.1697	.14503	.85491	45	55
	4	16	1902	. 8098	.9267	. 0721	.6469	.1699	4524	5476	44	56
1	8 12	17 18	. 1927 . 1952	. 8073	.9258	. 0761	.6458 .6447	.1701	. 4539	5461	43 42	52 48
	16	19	1977	8023	.9239	. 0841	.6436	.1705	. 4569	. 5431	41	44
1	20	20	.52002	.47998	1.9230	.60881	1.6425	1.1707	.14584	.85416	40	40
1	24	21	. 2026	. 7973	.9221	. 0920	.6415	.1709	. 4599	. 5400	39	36
1	28	22	. 2051	. 7949	.9212	. 0960	.6404	.1712	. 4615	. 5385	38	32
	32	23	2076	. 7924	.9203 .9193	1000	.6393	.1714	. 4630	. 5370	37	28
1	36 40	$\begin{array}{c c} 24 \\ 25 \end{array}$. 2101	. 7899 .47874	1.9184	. 1040	.6383 1.6372	.1716 1.1718	. 4645 .14660	. 5 355	36 35	24 20
1	44	$\frac{23}{26}$. 2151	. 7849	.9175	. 1120	.6361	.1720	. 4675	. 5325	34	16
1	48	27	. 2175	. 7824	.9166	. 1160	.6350	.1722	. 4690	. 5309	33	12
	52	28	. 2200	. 7800	.9157	. 1200	.6340	.1724	. 4706	. 5294	32	8
	56	29	. 2225	. 7775	.9148	. 1240	.6329	.1726	. 4721	. 5279	31	4
1	6	30	.52250	.47750	1. 9139 .9 130	.61280	1.6318	1.1728	.14736	.85264	30	54
1	4 8	31 32	2275 2299	. 7725 . 7700	.9121	. 1320 . 1360	.6308	.1730 .1732	$\begin{bmatrix} . & 4751 \\ . & 4766 \end{bmatrix}$. 5249 . 523 4	29 28	56 52
1	12	33	. 2324	7676	.9112	. 1400	.6286	.1734	4782	. 5218	27	48
	16	34	. 2349	. 7651	.9102	. 1440	.6276	.1737	. 4797	. 5203	26	44
Τ	20	35	.52374	.47626	1.9093	.61480	1.6265	1.1739	.14812	.85188	25	40
1	24	36	. 2398	7601	.9084	. 1520	.6255	.1741	. 4827	5173	24	36
1	28 32	37 38	. 2423	. 7577 . 7552	.9075 .9066	. 1560 . 1601	.6244 .6233	.1743 .17 45	. 4842 . 4858	. 5157 . 5142	23 22	32 28
	36	39	. 2473	. 7527	.9057	. 1641	.6223	.1747	. 4873	. 5127	21	24
	40	40	.52498	.47502	1.9048	.61681	1.6212	1.1749	.14888	.85112	20	20
	44	41	. 2522	. 7477	.9039	. 1721	.6202	.1751	. 4904	. 5096	19	16
1	48	42	. 2547	. 7453	.9030	. 1761	.6191	.1753	. 4919	. 5081	18	12
	52	43	. 2572	. 7428	.9021	. 1801	.6181	.1756	4934	. 5066	17	8
	56	44 45	. 2597	. 7403 .47379	.9013 1.9004	. 1842 .61882	.6170 1.6160	.1758 1.1760	. 4949 .14965	. 5050 .85035	$\begin{vmatrix} 16 \\ 15 \end{vmatrix}$	4 53
-	4	46	. 2646	. 7354	.8995	. 1922	.6149	.1762	. 4980	. 5020	14	56
	8	47	. 2671	. 7329	.8986	. 1962	.6139	.1764	. 4995	. 5004	13	52
	12	48	. 2695	. 7304	.8977	. 2003	.6128	.1766	. 5011	. 4989	12	48
1	16	49	, 2720	7280	.8968	2043	.6118	.1768	. 5026	. 4974	11	44
1	20	50	.52745 . 2770	.47255	1.8959	.62083	1.6107	1.1770	.15041	.84959	10	40
1	24 28	51 52	. 2794	. 7230 . 7205	.8950 .8941	. 2123	.6097 .6086	.1772 .1775	. 5057 . 5072	. 4943 . 4928	9 8	$\begin{vmatrix} 36 \\ 32 \end{vmatrix}$
1	32	53	. 2819	7181	.8932	. 2204	.6076	.1777	5087	4912	7	28
	36	54	. 2844	. 7156	.8924	. 2244	.6066	.1779	. 5103	. 4897	6	24
1	40	55	.52868	.47131	1.8915	.62285	1.6055	1.1781	.15118	.84882	5	20
	44	56	2893	. 7107	.8906	2325	.6045	.1783	. 5133	. 4866	4	16
	48 52	57 58	. 291 8 . 2 942	. 7082 . 7057	.8897 .8888	. 2366 . 2406	.6034 .6024	.1785 .1787	. 5149 . 5164	. 4851	$\begin{bmatrix} 3 \\ 2 \end{bmatrix}$	12 8
	56	59	2 967	7033	.8879	2446	.6014	.1790	. 5180	. 4820	1	4
	8	60	. 2992	. 7008	.8871	. 2487	.6003	.1792	. 5195	. 4805	Ū.	52
1	M.S.	M	Cosine.	Vrs. Sin.	Secante.			Cosec'ut	Vrs. Cos	Sine.		M.S.
1	8h	1219				Natu	ral.				58°	3h
7-00	-											

-	NATURAL LINES.														
1 02	1000														
2h	329		Natur	al Trig	gonom	etrical	Fun	ctions.		L47°	9h				
M.S.	M	Sine.	[Vrs.Cos.	Cosec'nte	Tang.	Cotang.	Secante	Vrs. Sin	Cosine.	Î M	M.S.				
8	0	.52992	.47008	1.8871	.62487	1.6003	1.1792	.15195	.84805	60	52				
4	1	. 3016	. 6983	.8862	. 2527	.5993	.1794	. 5211	. 4789		56				
8	2	. 3041	6959	.8853	2568	.5983	.1796	5226	. 4774	58	52				
12 16	3 4	3066	. 6934	.8844	. 2608	.5972	.1798	. 5241	4758	57	48				
20	5	. 3090	. 6909	.8836 1.8827	. 2649	.5962	.1800	5257	. 4743	56	44				
24	6	. 3140	. 6860	.8818	.62689	1.5952 .5941	1.1802	.15272	.84728	55 54	40 36				
28	7	3164	6835	.8809	2770	.5931	.1807	. 5303.	4697	53	32				
32	8	. 3189	6811	.8801	. 2811	.5921	.1809	5319	4681	52	28				
36	9	. 3214	. 6786	.8792	. 2851	.5910	.1811	. 5334	. 4666	51	24				
40	10	.53238	.46762	1.8783	.62892	1.5900	1.1813	.15350	.84650	50	20				
44 48	11 12	. 3263	. 6737	.8775	. 2933	.5890	.1815	. 5365	. 4635.		16				
-52	13	3288	6688	.8766 .8757	. 2973	.5880	.1818	. 5381	. 4619		12 8				
56	14	. 3337	6663	.8749	. 3055	.5859	.1822	. 5412	4588	46	4				
. 9	15	.53361	.46638	1.8740	.63095	1.5849	1.1824	.15427	.84573	45	51				
4	16	. 3386	. 6614	.8731	. 3136	.5839	.1826	. 5443	. 4557	44	56				
8	17	. 3411	. 6589	.8723	. 3177	.5829	.1828	. 5458	. 4542	43	52				
12	18	. 3435	. 6565	.8714	. 3217	.5818	.1831	. 5474	. 4526	42	48				
16	19	. 3460	. 6540	.8706	. 3258	.5808	.1833	. 5489	. 4511	41	44				
20 24	20 21	.53484	.46516	1.8697 .8688	.63299	1.5798	1.1835	.15505	. 84495	40 39	40 36				
28	22	3533	6466	.8680	. 3380	.5778	.1839	5536	. 4464	38	32				
	32 23 . 3558 . 6442 .8671 . 3421 .5768 .1841 . 5552 . 4448 37 28 36 24 . 3583 . 6417 .8663 . 3462 .5757 .1844 . 5567 . 4433 36 24														
	36 24 . 3583 . 6417 .8663 . 3462 .5757 .1844 . 5567 . 4433 36 24														
40	40 25 .53607 .46393 1.8654 .63503 1.5747 1.1846 .15583 .84417 35 20														
44	26	. 3632	. 6368	.8646	. 3543	.5737	.1848	. 5598	. 4402	34	16				
48	27	. 3656	6344	.8637	. 3584	.5727	.1850	5614	. 4386	33	12				
52 56	28 29	. 3681 . 3705	6319	.8629 .8620	. 3625	.5717 .5707	.1852	. 5630. . 5645	. 4370 . 4355.	32 31	8 4				
10	30	.53730	.46270	1.8611	.63707	1.5697	1.1857	.15661	.84339	30	50				
4	31	. 375 1	6245	.8603	. 3748	.5687	.1859	. 5676	. 4323	29	56				
8	32	. 3779	. 6221	.8595	. 3789	.5677	.1861	. 5692	. 4308.	28	52				
12	33	. 3803	. 6196	.8586	. 3830	.5667	.1863	. 5708	. 4292	27	48				
16	34	. 3828	. 6172	.8578	. 3871	.5657	.1866	. 5723	. 4276	26	44				
20	35	.53852	.46147	1.8569	.63912	1.5646	1.1868	.15739	.84261	25	40 36				
24 28	36 37	. 3877	. 6123	.8561 .8552	. 3953	.5636 .5626	.1870 .1872	. 5755 . 5770	4243	$\begin{array}{ c c }\hline 24 \\ 23 \\ \end{array}$	32				
32	38	. 3926	6074	.8544	. 4035	.5616	.1874	. 5786	. 4214	22	28				
36	39	. 3950	6049	.8535	. 4076	.5606	.1877	. 5802.	. 4198.		$\frac{1}{24}$				
40	40	.53975	.46025	1.8527	.64117	1.5596	1.1879	.15817	.84182	20	20				
44	41	. 3999	. 6000	.8519	. 4158	.5586	.1881	. 5833.	. 4167	19	16				
48	42	4024	. 5976	.8510	. 4199	.5577	.1883	5849.	. 4151	18	12				
52 56	43	. 4048 . 4073	5951 . 5927	.8502 .8493	. 424 0 . 4281	.5567 .5557	.1886 .1888	. 5865. . 5880	. 4135. . 4120	$\begin{bmatrix} 17 \\ 16 \end{bmatrix}$	8 4				
11	44	.54097	.45902	1.8485	.64322	1.5547	1.1890	.15896	.84104	15	49				
4	46	. 4122	. 5878	.8477	. 4363	.5537	.1892	. 5912	. 4088	14	56				
8	47	. 4146	. 5854	.8468	. 4404	.5527	.1894	. 5927.	. 4072	13	52				
12	48	. 4171	. 5 829	.8460	. 4446	.5517	.1897	. 5943	. 4057	12	48				
16	49	. 4195	. 5805	.8452	. 4487	.5507	.1899	. 5959	. 4041	11	44				
20	50	.54220	.45780	1.8443	.64528	1.5497	1.1901	.15975	.84025	10	40				
24 28	51 52	. 4244	. 5756 . 5731	.8435 .8427	. 4569 . 4610	.5487 .5477	.1903 .1906	. 5991 . 6006	. 4009	9 8	36 32				
32	$\frac{52}{53}$. 4293	. 5707	.8418	. 4652	.5467	.1908	. 6022	3978	7	28				
36	54	. 4317	5682	.8410	. 4693	.5458	.1910	. 6038	3962	6	24				
40	55	.54342	.45658	1.8402	.64734	1.5448	1.1912	.16054	.83946	5	20				
44	56.	. 4366	. 5634	.8394	. 4775	.5438	.1915	6070	. 3930	4	16				
48	57	. 4391	5609	.8385	. 4817	.5 128	.1917	6085	. 3914	3	12				
52	58	. 4415	. 5585	.8377	. 4858	.5418	.1919	6101 6117	. 3899 . 3883	$\begin{bmatrix} 2 \\ 1 \end{bmatrix}$	8				
56 12	5 9 60	. 4439 . 4464	5560 5536	.8369 .8361	. 4899	.5408 .5399	.1921 .1922	6133	3867	0	48				
M.S.	M			Secante.	Cotang.	Tangent.			Sine.	MÍ	M.S.				
	1229				Natu					57°	34				
					20000										

1	NATURAL MINES.												
2h	339		Natur	al Triç	vollon.	otnica	1 Elwan	otions	1	46°	9h		
M.S. 12	M 0	Sine54464	.45536	Cosec'nte 1.8361	Tang64941	Cotang. 1.5399	1.1924	Vrs. Sin .16133	Cosine83867	$\begin{bmatrix} M \\ 60 \end{bmatrix}$	M.S. 48		
4	1	. 4488	. 5512	.8352	. 4982	.5389	.1926	6149	. 3851	59	56		
8	$\frac{1}{2}$. 4513	5487	.8344	5023	.5379	.1928	. 6165	3835	58	52		
12	3	. 4537	. 5463	.8336	. 5065	.5369	.1930	. 6180	. 3819	57	48		
16	4	. 4561	. 5438	.8328	. 5106	.5359	.1933	. 6196	. 3804	56	44		
20	5	.54586	.45414	1.8320	.65148	1.5350	1.1935	.16212	.83788	55	40		
24	6 7	. 4610 . 4634	5390	.8311	5189	.5340	.1937	. 6228 . 6244	3772	54 53	36 32		
28 32	8	. 4659	. 5341	.8295	5272	.5320	.1942	6260	3740	52	28		
36	9	. 4683	. 5317	.8287	. 5314	.5311	.1944	. 6276	. 3724	51	24		
40	10	.54708	.45292	1.8279	.65355	1.5301	1.1946	.16292	.83708	50	20		
44	11	. 4732	. 5268	.8271	. 5397	.5291	.1948	. 6308	. 3692	49	16		
48	12	4756	. 5244	.8263	. 5438	.5282	.1951	. 6323	. 3676	48	12		
52 56	13 14,	. 4781 . 4805	. 5219	.8255 .8246	. 5480 . 5521	.5272	.1953	63396355	. 3660	47 46	8 4		
13	15	.54829	.45171	1.8238	.65563	1.5252	1.1958	.16371	.83629	45	47		
4	16	. 4854	. 5146	.8230	. 5604	.5243	.1960	. 6387	. 3613	44	56		
8	17	. 4878	. 5122	.8222	. 5646	.5233	.1962	. 6403	. 3597	43	52		
12	18	. 4902	. 5098	.8214	. 5688	.5223	.1964	. 6419	. 3581	42	48		
16	19	. 4926	5073 .45049	.8206 1.8198	. 5729	.5214	.1967	6435	. 3565	41	44		
20 24	20 21	.54951	. 5025	.8190	.65771	1.5204	1.1969 .1971	.16451	.83549	40 39	40 36		
28	$\begin{vmatrix} 21 \\ 22 \end{vmatrix}$	4999	5000	.8182	. 5854	.5185	.1974	. 6483	. 3517	38	32		
32	23	. 5024	. 4976	.8174	. 5896	.5175	.1976	. 6499	. 3501	37	28		
36	24	. 5048	. 4952	.8166	. 5938	.5166	.1978	. 6515	. 3485	36	24		
40	25	.55072	.44928	1.8158	.65980	1.5156	1.1980	.16531	.83469	35	20		
44	26	. 5097 . 5121	. 4903 . 4879	.8150 .8142	6021	.5147	.1983	6547	. 3453	34 33	16 12		
48 52	27 28	. 5145	. 4855	.8134	6063	.5137 .5127	.1985 .1987	. 6563 . 6579	. 3437	$\frac{33}{32}$	8		
56	$\frac{20}{29}$. 5169	. 4830	.8126	6147	.5118	.1990	6595	. 3405	31	4		
14	30	.55194	.44806	1.8118	.66188	1.5108	1.1992	.16611	.83388	30	46		
4	31	. 5218	. 4782	.8110	. 6230	.5099	.1994	. 6627	. 3372	29	56		
8	32	. 5242	4758	.8102	. 6272	.5089	.1997	. 6643	. 3356	28	52		
12 16	33 34	. 5266 . 5291	. 4733 . 4709	.8094 .8086	. 6314 . 6356	.5080 .5070	.1999 .2001	. 6660 . 6676	. 3340	27 26	48 44		
20	35	.55315	.44685	1.8078	.66398	1.5061	1.2004	.16692	.83308	25	40		
24	36	. 5339	. 4661	.8070	. 6440	.5051	.2006	. 6708	. 3292	24	36		
28	37	. 5363	. 4637	.8062	. 6482	.5042	.2008	. 6724	. 3276	23	32		
32	38	. 5388	. 4612	.8054	. 6524	.5032	.2010	. 6740	. 3260	22	28		
36	39	. 5412	. 4588 .44564	.8047 1.8039	6566	.5023 1.5013	.2013 1.2015	. 6756 .16772	. 3244	$\frac{21}{20}$	24 20		
40 44	40 41	. 5460	. 4540	.8031	. 66608	.5004	.2017	. 6788	. 3211	19	16		
48	42	. 5484	. 4515	.8023	. 6692	.4994	.2020	. 6804	3195	18	12		
52	43	. 5509	. 4491	.8015	. 6734	.4985	.2022	. 6821	. 3179	17	8		
56	44	. 5533	. 4467	.8007	. 6776	.4975	.2024	. 6837	. 3163	16	4		
15	45	.55557	.4 4443	7099	.66818	1.4966 .4957	1.2027	.16853	.83147	15	45		
8	$\begin{array}{c c} 46 \\ 47 \end{array}$. 5581	. 4419	.7992 .7984	. 68 60 . 6902	.4957	.2029 .2031	. 6869 . 6885	. 3131	14 13	56 52		
12	48	. 5629	. 4370	.7976	6944	.4938	.2034	6901	. 3098	12	48		
16	49	. 5654	. 4346	.7968	6986	.4928	.2036	. 6918	. 3082	11	44		
20	50	.55678	.44322	1.7960	.67028	1.4919	1.2039	.16934	.83066	10	40		
24	51	. 5702	. 4298	.7953	. 7071	.4910	.2041	6950	. 3050	9	36		
28 32	52 53	. 5726 . 5750	. 4274	.7945 .7937	. 7113 . 7155	.4900 .4891	.2043 .2046	• 6966 • 6982	. 3034	8 7	32 28		
36	54 54	5774	. 4225	.7929	. 7197	.4881	.2048	. 6999	. 3001	6	24		
40	55	.55799	.44201	1.7921	.67239	1.4872	1.2050	.17015	.82985	5	20		
44	56	. 5823	. 4177	.7914	. 7282	.4863	.2053	. 7031	. 2969	4	16		
48	57	. 5847	. 4153	.7906	. 7324	.4853	.2055	. 7047	. 2952	3	12		
52 56	58 59	. 5871 . 5895	4129 4105	.7898	7366	.4844 .4835	.2057	7064	2936	$\frac{2}{1}$	8 4		
16	60	. 5919	. 4081	.7891 .7883	. 7408 . 7451	.4826	.2060 $.2062$. 7080 . 7036	. 2920 . 2904	0	44		
M.S.	M	Cosine.		Secante.		Tangent.			Sine.	M	M.S.		
8h	123°	2			Natu	ral.				56°	3h		
٠			<u> </u>										

1	1										
2h	340		Natur	al Trig	onom	etrical	Func	ctions.		145°	9h
M.S.	M	Sine.		Cosec'nte		Cotang.	Secante	Vrs. Sin	Cosine	. M	M.S.
16	0	.55919	.44081	1.7883	.67451		1.2062	.17096	.82904		44
8	1	. 5943	. 4057	.7875	. 7493		.2064	. 7112	. 2887		56
12	$\begin{vmatrix} 2\\3 \end{vmatrix}$. 5967	. 4032	.7867	. 7535		.2067	7129	. 2871	58	52
16	4	. 5992 . 6016	. 4008	.7860 .7852	. 7578	.4798	.2069	7145	. 2855		48
20	5	.56040	. 3984	1.7844	. 7620 . 6 7663	.4788 1.4779	.2072 1.2074	. 7161	. 2839 .82822	56 55	44 40
24	6	. 6064	3936	.7837	. 7705	.4770	.2076	. 7194	. 2806		36
28	7	. 6088	3912	.7829	7747	.4761	.2079	7210	2790	53	32
32	8	. 6112	. 3888	.7821	. 7790	.4751	.2081	7227	. 2773	52	28
36	9	. 6136	. 3864	.7814	. 7832	.4742	.2083	. 7243	. 2757	51	24
40	10	.56160	.43840	1.7806	.67875	1.4733	1.2086	.17259	.82741	50	20
44	11	. 6184	. 3816	.7798	. 7917	.4724	.2088	. 7276	. 2724	49	16
48 52	12 13	6208	. 3792	.7791	. 7960	.4714	.2091	. 7292	. 2708	48	12
56	14	6256	. 3768	.7783 .7776	. 8002 . 8045	.4705	.2093	. 7308 . 7325	. 2692 . 2675	47 46	8 4
17	15	.56280	.43719	1.7768	.68087	1.4687	1.2098	.17341	.82659	45	43
4	16	6304	3695	.7760	. 8130	.4678	.2100	. 7357	. 2643	44	56
8	17	. 6328	. 3671	.7753	. 8173	.4669	.2103	. 7374	. 2626	43	52
12	18	. 6353	. 3647	.7745	. 8215	.4659	.2105	7390	. 2610	42	48
16	19	. 6377	. 3623	.7738	. 8258	.4650	.2107	. 7406	. 2593	41	44
20 24	20	.56401	.43599	1.7730	.68301	1.4641	1.2110	.17423	.82577	40	40
28	21 22	6425 6449	3575	.7723 .7715	. 8343	.4632	.2112	. 7439 . 7456	. 2561	39 38	36 32
32	23	6473	3527	.7708	. 8429	.4614	.2117	7472	. 2544	37	28
36	24	6497	3503	.7700	. 8471	.4605	.2119	. 7489	. 2511	36	24
40	25	.56521	.43479	1.7693	.68514	1.4595	1.2122	.17505	.82495	35	20
44	26	. 6545	. 3455	.7685	. 8557	.4586	.2124	. 7521	. 2478	34	16
48	27	. 6569		.7678	. 8600	.4577	.2127	. 7538	. 2462	33	12
52 56	28	6593	. 3407	.7670	. 8642	.4568	.2129	. 7554	. 2445	32	8
18	29 30	. 6617	. 3383	.7663 1.7655	. 8685	.4559 1.4550	.2132 1.2134	. 7571	. 2429	31 30	4 42
4	31	. 6664	. 3335	.7648	. 8771	.4541	.2136	. 7604	. 2396	29	56
8	32	. 6688	. 3311	.7640	. 8814	.4532	.2139	. 7620	. 2380	28	52
12	33	. 6712	. 3287	.7633	. 8857	.4523	.2141	. 7637	. 2363	27	48
16	34	. 6736	. 3263	.7625	. 8899	.4514	.2144	. 7653	. 2347	26	44
20	35	.56760	.43239	1.7618	.68942	1.4505	1.2146	.17670	.82330	25	40
24 28	36 37	. 6784	. 3216 . 3192	.7610 .7603	. 8985 . 9028	.4496 .4487	.2149	. 7686 . 7703	. 2314	24 23	36 32
32	38	6832	. 3168	.7596	. 9071	.4478	.2153	7719	. 2280	22	28
36	39	. 6856	3144	.7588	. 9114	.4469	.2156	. 7736	. 2264	21	24
40	40	.56880	.43120	1.7581	.69157	1.4460		.17752	.82247	20	20
44	41	. 6904	. 3096	.7573	. 9200	.4451	.2161	. 7769	. 2231	19	16
48	42	. 6928	. 3072	.7566	. 9243	.4442	.2163	7786	. 2214	18	12
52 56	43	. 6952	. 3048	.7559 .7551	. 9286	.4433 .4424	.2166 .2168	. 7802 . 7819	. 2198 . 2181	17 16	8 4
19	44 45	.57000	.43000	1.7544	. 9329 .69372	1.4415	1.2171	.17835	.82165	15	41
4	46	7023	. 2976	.7537	. 9415	.4406	.2173	. 7852	. 2148	14	56
8	47	. 7047	2952	.7529	. 9459	.4397	.2175	. 7868	. 2131	13	52
12	48	. 7071	. 2929	.7522	. 9502	.4388	.2178	. 7885	. 2115	12	48
16	49	. 7095	. 2905	.7514	. 9545	.4379	.2180	. 7902	. 2098	11	44
20	50	.57119	.42881	1.7507	.69588	1.4370	1.2183	.17918	.82082	10	40
24 28	51	. 7143 . 7167	. 2857	.7500 .7493	. 9631 . 9674	.4361 .4352	.2185 .2188	. 7935 . 7951	. 2065	9 8	$\begin{vmatrix} 36 \\ 32 \end{vmatrix}$
32	52 53	. 7191	. 2833 . 2809	.7485	. 9718	.4343	.2190	. 7968	. 2032	7	28
36	54	7214	. 2785	.7478	. 9761	.4335	.2193	7985	. 2015	6	24
40	55	.57238	.42761	1.7471	.69804	1.4326	1.2195	.18001	.81998	5	20
41	56	. 7262	. 2738	7463	. 9847	.4317	.2198	. 8018	. 1982	4	16
48	57	. 7286	. 2714	.7456	. 9891	.4308	.2200	. 8035	. 1965	3	12
52	58	. 7310	2690	.7449	. 9934	.4299	.2203	. 8051	. 1948	2	8
56 20	59 60	. 7334 . 7358	$\begin{array}{c c} . & 2666 \\ . & 2642 \end{array}$.7442	. 9977	.4290 .4281	.2205 .2208	. 8068	. 1932 . 1915	$\begin{bmatrix} 1 \\ 0 \end{bmatrix}$	40
M. S.	М	Cosine.	Vrs. Sin.		Cotang	Tangent.			Sine.	M	M.S.
	124	,			Natu					55°	3h

											1
$2^{\rm h}$	35°	·	Natur	al Trig	gonom	etrica	Fun	ctions	. 1	440	$\delta_{\rm p}$
M.S.	M	Sine.	4	Cosec'nte				Vrs. Sin		1	M.S.
20	0	.57358	.42642	1.7434	.70021	1.4281	1.2208	.18085	.81915	60	40
4	1	. 7381	. 2618	.7427	. 0064	.4273	.2210	. 8101	. 1898	59	56
8 12	2 3	. 7405	. 2595	.7420 .7413	. 0107	.4264 .4255	.2213	. 8118 . 8135	. 1882	58 57	52 48
16	4	. 7453	2547	.7405	. 0194	.4246	.2218	8151	1848	56	44
20	5	.57477	.42523	1.7398	.70238	1.4237	1.2220	.18168	.81832	55	40
24	6	. 7500	. 2499	.7391	. 0281	.4228	.2223	. 8185	. 1815	54	36
28	7	. 7524	. 2476	.7384	. 0325	.4220	.2225	. 8202	. 1798	53	32
32	8	. 7548	. 2452	.7377	. 0368	.4211	.2228	8218	. 1781	52	28
36	9	. 7572	. 2428	.7369	. 0412	.4202	.2230	. 8235	. 1765	51	24
40 44	10 11	.57596	.42404	1.7362 .7355	.70455	1.4193 .4185	1.2233	.18252 . 8269	.81748	50 49	20 16
48	12	. 7643	2357	.7348	. 0542	.4176	.2238	. 8285	. 1714	48	12
52	13	. 7667	. 2333	.7341	. 0586	.4167	.2240	. 8302	1698	47	8
56	14	. 7691	. 2309	.7334	. 0629	.4158	.2243	. 8319	. 1681	46	4
21	15	.57714	.42285	1.7327	.70673	1.4150	1.2245	.18336	.81664	45	39
4	16	. 7738	. 2262	.7319	. 0717	.4141	.2248	. 8353	. 1647	44	56
8	17	7762	. 2238	.7312 .7305	. 0760	.4132	.2250	8369	. 1630	43	52
12 16	18 19	. 7786 . 7809	2214 2190	.7298	. 0804	.4123 .4115	.2253	. 8386	. 1614	42 41	48
20	20	.57833	.42167	1.7291	.70891	1.4106	1.2258	.18420	.81580	40	40
24	21	. 7857	. 2143	.7284	. 0935	.4097	.2260	. 8437	. 1563	39	36
28	22	. 7881	. 2119	.7277	. 0979	.4089	.2263	. 8453	. 1546	38	32
32	23	. 7904	. 2096	.7270	. 1022	.4080	.2265	. 8470	. 1530	37	28
36	24	. 7928	. 2072	.7263	. 1066	.4071	.2268	. 8487	. 1513	36	24
40 44	$\begin{array}{c c} 25 \\ 26 \end{array}$.57952 . 7975	.42048 . 2024	1.7256 .7249	.71110 . 1154	1.4063 .4054	1.2270 .2273	. 18504	.81496 . 1479	35 34	20 16
48	$\frac{20}{27}$	7999	2001	7242	. 1198	.4045	.2276	. 8538	. 1462	33	12
52	28	. 8023	. 1977	.7234	. 1241	.4037	.2278	. 8555	. 1445	32	8
56	29	. 8047	. 1953	.7227	. 1285	.4028	.2281	. 8571	. 1428	. 31	4
22	30	.58070	.41930	1.7220	.71329	1.4019	1.2283	.18588	.81411	30	38
4	31	. 8094	. 1906	.7213	. 1373	.4011	.2286	. 8605	. 1395	29	56
8 12	32 33	. 8118 . 8141	. 1882 . 1859	.7206 .7199	. 1417	.4002 .3994	.2238	. 8622 . 8639	. 1378	28 27	52
16	$\frac{33}{34}$. 8165	. 1835	.7192	. 1505	.3985	.2293	. 8656	. 1361	26	48
20	35	.58189	.41811	1.7185	.71549	1.3976	1.2296	.18673	.81327	25	40
24	36	. 8212	. 1788	.7178	. 1593	.3968	.2298	. 8690	. 1310	24	36
28	37	. 8236	. 1764	.7171	. 1637	.3959	.2301	. 8707	. 1293	23	32
32	38	. 8259	. 1740	.7164	. 1681	.3951	.2304	. 8724	. 1276	22	28
36 40	39 40	. 8283 .58307	. 1717 .41693	.7157 1.7151	. 1725 .71769	.3942	.2306	. 8741	. 1259 .81242	21 20	24
44	41	. 8330	. 1669	.7144	. 1813	1.3933 .3925	1.2309 .2311	. 18758 . 8775	. 1225	19	20 16
48	42	. 8354	. 1646	.7137	. 1857	.3916	.2314	. 8792	. 1208	18	12
52	43	. 8378	. 1622	.7130	. 1901	.3908	.2316	. 8809	. 1191	17	8
56	44	. 8401	. 1599	.7123	. 1945	.3899	.2319	. 8826	. 1174	16	4
23	45	.58425	.41575	1.7116	.71990	1.3891	1.2322	.18843	.81157	15	37
8	46 47	. 8448 . 8472	. 1551 . 1528	.7109 .7102	. 2034	.3882 .3874	.2324 .2327	. 8860 . 8877	. 1140	14 13	56
12	48	. 8496	. 1504	.7095	. 2122	3865	.2329	. 8894	. 1123	$\frac{13}{12}$	52 48
16	49	. 8519	. 1481	.7088	2166	.3857	.2332	. 8911	. 1089	11	44
20	50	.58543	.41457	1.7081	.72211	1.3848	1.2335	.18.428	.81072	10	40
24	51	. 8566	. 1433	.7075	. 2255	.3840	.2337	. 8945	. 1055	9	36
28	52	. 8590	. 1410	.7068	. 2299	.3831	.2340	. 8962	. 1038	8	32
32 36	53 54	. 8614 . 8637	. 1386 . 1363	.7061 .705±	. 2344	.3823	.2342 .2345	. 8979	. 1021	7	28
40	55	.58661	. 1303	1.7047	.72432	.3814 1.3806	1.2348	. 8996 .19013	. 1004	6 5	$\begin{vmatrix} 24 \\ 20 \end{vmatrix}$
44	56	. 8684	. 1316	.7040	2477	.3797	.2350	. 9030	. 0970	4	16
48	57	. 8708	. 1292	.7033	. 2521	.3789	.2353	9047	. 0953	3	12
52	58	. 8731	. 1268	.7027	2565	.3781	.2355	. 9064	. 0936	2	8
56	59	. 8755	. 1245	.7020	. 2610	.3772	.2358	. 9081	. 0919	1	4
24 M.S.	60 M	. 8778 Cosine.	. 1221 Vrs. Sin.	.7013 Secante	. 2654	.3764 Tangent.	.2361 Cosec'nt	. 9093	. 0902	() M	36
	125°		T D. DIII.	Scourio.	Natu		COSCO III	713.008	Sine.	54°	M.S. 3h
	120				TATELLE	Tall.				OT	0

				4.12	TURAL	THES.					240	
2h	369		Natur	al Trig	conom	etrical	Fun	ctions.	. 1	43°	9н	
M.S.	М	Sine.		Cosee'nte	_	Cotang.		Vrs. Sin	Cosine.	M	M.S.	
24	0	.58778	.41221	1.7013	.72654	1.3764	1.2361	.19098	.80902	60	36	
4	1	8802	. 1198	.7006	. 2699	.3755	.2363	. 9115	. 0885	59	56	
8 12	2	8825	. 1174	.6999	2743	.3747	.2366	. 9132	. 0867	58	52	
16	3 4	8849	. 1151	6993	. 2788	.3738	.2368	. 9150	. 0850	57	48	
20	5	• 8873 •58896	. 1127	.6986 1.6979	. 2832	.3730 1.3722	.2371 1.2374	. 9167	. 0833	56 55	44	
24	6	• 8920	. 1080	.6972	. 2921	.3713	.2376	9201	.80816	54	40 36	
28	7	. 8943	. 1057	.6965	2966	.3705	.2379	9218	. 0782	53	32	
32	8	8967	. 1033	.6959	3010	.2697	.2382	9235	. 0705	52	28	
36	9	8990	. 1010	.6952	. 3055	.3688	.2384	. 9252	0747	51	24	
40	10	.59014	.40986	1.6945	.73100	1.3580	1.2387	.19270	.80730	50	20	
44	11	. 9037	. 0963	.6938	. 3144	.3672	.2389	. 9287	. 0713	49	16	
48	12	. 9060	. 0939	.6932	. 3189	.3663	.2392	. 9304	. 0696	48	12	
52	13	. 9084	. 0916	.6925	. 3234	.3655	.2395	. 9321	. 0679	47	8	
56	14	. 9107	. 0892	.6918	. 3278	.3647	.2397	. 9338	. 0662	46	4	
25	15	.59131	.40869	1.6912	73323	1.3638	1.2400	.19355	.80644	45	35	
8	17	9154 9178	. 0845	.6905 .6898	3368 3412	.3630 .3622	.2403	9373	. 0627	44 43	56 52	
12	18	9201	0799	.6891	3457	.3613	.2408	9407	. 0510	42	48	
16	19	9225	0775	.6885	. 5502	.3605	.2411	9424	. 0576	41	44	
20	20	.59248	.40752	1.6878	.73547	1.3597	1.2413	1.19442	.80558	40	40	
24	21	. 9272	. 0728	-6871	. 3592	.3588	.2416	. 9459	. 0541	59	36	
28	22	. 9295	. 0705	.6865	. 3637	.3580	.2419	. 9476	. 0524	38	32	
32	23	. 9318	. 0681	.6858	. 3681	.3572	.2421	. 9493	. 0507	37	28	
36	24	. 9342	. 0658	.6851	. 3726	.3564	.2424	. 9511	. 0489	36	24	
40	25	.59365	.40635	1.6845	.73771	1.3555	1.2427	.19528	.80472	35	20	
44	26	. 9389	. 0611	.6838	. 3816	.3547	.2429	. 9545	. 0455	34	16	
48 52	27	9412	. 0588	.6831	. 3861	.3539	.2432	. 9562	. 0437	33 32	12	
56	28 29	• 9435 • 9459	. 0564	.6825 .6818	· 3906 · 3951	.3531 .3522	.2435 .2437	. 9580 . 9597	. 0420	31	8 4	
26	$\begin{vmatrix} 29\\30 \end{vmatrix}$.59482	.40518	1.6812	.73996	1.3514	1.2440	.19614	.80386	30	34	
4	31	. 9506	. 0494	.6805	. 4041	.3506	.2443	. 9632	. 0368	29	56	
8	32	• 9529	. 0471	6798	. 4086	.3498	.2445	. 9649	. 0351	28	52	
12	33	. 9552	. 0447	6792	. 4131	.3489	.2448	. 9666	. 0334	27	48	
16	34	. 9576	. 0424	.6785	• 4176	.3481	.2451	. 9683	. 0316	26	44	
20	35	.59599	.40491	1.6779	.74221	1.3473	1.2453	.19701	.80299	25	40	
24	36	• 9622	. 0377	6772	. 4266	.3465	.2456	. 9718	. 0282	24	36	
28	37	9646	. 0354	.6766	4312	.3457	.2459	9736	. 0264	23	32	
32 36	38 39	• 9669	. 0331	.6759 $.6752$. 4357 . 4402	.3449 .3440	.2461	9753	. 0247	22 21	28 24	
40	40	• 9692 • 59716	. 0307	1.6746	.74447	1.3432	$\frac{.2464}{1.2467}$. 9770 .19788	. 0230	$\frac{21}{20}$	20 .	
44	41	. 9739	. 0261	.6739	. 4452	.3424	.247()	. 9805	. 0195	19	16	
48	42	9762	0237	.6733	4538	.3416	.2472	. 9822	. 0177	18	12	
52	43	9786	: 0214	.6726	. 4583	.3408	.2475	. 9840	. 0160	17	8	
56	44	. 9809	. 0191	.6720	. 4628	.3400	.2478	. 9857	. 0143	16	4	
27	45	-59832	.40167	1.6713	.74673	1.3392	1.24 0	.19875	.80125	15	33	
4	46	9856	0144	.6707	. 4719	.3383	.2483	9892	. 0108	14	56	
8	47	• 9879	. 0121	.6700	4764	.3575	.24 6	. 9909	. 0090	1 3	52	
12 16	48	9902	. 0098	.6694	. 4809 . 4855	.3367 .3359	2485	9927	. 0073	12 11	48	
20	49 50	. 9926 .59949	.40051	1.6687 1.6681	.74900	1.3351	.2495 1.2494	0.9944 0.19962	. 0056 .80038	$\frac{11}{10}$	44 40	
24	51	. 9972	. 0028	.6674	. 4946	.3343	.2497	. 9979	. 0021	9	36	
28	$\frac{51}{52}$	9995	. 0004	.6668	. 4991	.3335	.2499	9997	. 0003	8	32	
32	53	.60019	.39981	.6661	. 5037	.3327	.2502	.20014	.79986	7	28	
36	54	. 0042	. 9958	.6655	. 5082	.3319	.2505	. 0031	. 9968	6	24	
40	55	.60065	.39935	1.6648	.75128	1.3311	1.2508	.20049	.79951	5	20	
44	56	. 0088	. 9911	.6642	. 5173	.3303	.2510	. 0066	. 9933	4	16	
48	57	. 0112	. 9888	.6636	. 5219	.3294	.2513	. 0084	. 9916	3	12	
52	58	. 0135	9865	.6629	. 5264	.3286	.2516	. 0101	. 9898	2	8	
$\begin{array}{ c c } 56 \\ 28 \end{array}$	59	. 0158	9842	.6623	5310	.3278	.2519	. 0119	. 9881	$\begin{bmatrix} 1 \\ 0 \end{bmatrix}$	32	
IM S	M. S. M. Cosine, Vrs. Sin Secante, Cotang, Tangent, Cosec'nt, Vrs. Cos Sine, M. M. S.											
	126				Natu		2 2000 1101			53°	3h	
9	120				Ta 46 £ (1	A CEAL				3		

2	NATURAL LINES.											
	•>h	37	0								1.400	9h
	2"	31			al Triș		<u> </u>	l Fun	ctions	•	142°	
	M.S.	1	Sine.		Cosec'nte	_	Cotang.		Vrs. Sin			M.S.
	*8	0	.60181	.39818	1.6616	.75355	1 200-0	1.2521	.20136	.79863	60 59	32 56
	8	1 2	. 0205 . 0 228	9795	.6610	5401		.2524	. 0154	9846	58	52
ı	12	3	0251	9749	.6597	5492		.2530	0189	9811	57	48
ı	16	4	. 0274	. 9726	.6591	. 5538	.3238	.2532	. 0206	. 9793	56	44
ı	20	5	.60298	.39702	1.6584	.75584		1.2535	.20224	.79776	55	40
ı	24 28	6 7	0320	. 9679	.6578	. 5629 . 5675	.3222	.2538	. 0242	9758	54 53	36 32
ı	32	8	0344	9633	.6565	5721	.3206	.2543	0233	9723	52	28
ı	36	9	. 0390	. 9610	.6559	5767	.3198	.2546	. 0294	9706	51	24
ı	40	10	.60413	.39586	1.6552	.75812	1.3190	1.2549	.20312	.79688	50	20
ı	44	11	0437	9563	.6546	- 5858	.3182	.2552	. 0329	. 9670	49 48	16 12
ı	48 52	12 13	. 0460	9540	.6540 .6533	5904	.3174	.2554	. 0347	9635	47	8
ı	56	14	. 0506	9494	.6527	. 5996	.3159	2560	. 0382	9618	46	4
ı	29	15	-60529	.39471	1.6521	.76042	1.3151	1.2563	.20400	.79600	45	31
ı	4	16	0552	9447	.6514	6088	.3143	.2565	. 0417	. 9582	44	56
ı	8 12	17 18	• 0576 • 0599	. 9424	.6508 .6502	6134	.3135	.2568	. 0435	. 9565	43 42	52 48
	16	19	0622	9378	.6496	6225	.3119	.2574	. 0470	9530	41	41
	20	20	60645	.39355	1.6489	.76271	1.3111	1.2577	.20488	.79512	40	40
	24	21	. 0668	. 9332	.6483	6317	.3103	.2579	. 0505	. 9494	39	36
1	28	22	• 0691	. 9309	.6477	6364	.3095	.2582	0523	. 9477	38	32 28
1	32 36	23 24	0714	9285	.6470 .6464	6410	.3087	.2585	. 0541	. 9459	36	24
	40	25	60761	.39239	1.6458	.76502	1.3071	1.2591	.20576	.79424	35	20
	44	26	. 0784	. 9216	.6452	. 6548	.3064	.2593	. 0594	. 9406	34	16
Į	48	27	0807	. 9193	.6445	. 6594	.5056	.2596	. 0611	. 9388	33 32	12
-	52 56	28 29	· 0880 · 0853	9170	.6439 .6433	6640	.3048	.2599	. 0629	9371	31	8 4
Ì	30	30	60876	.39124	1.6427	.76733		1.2605	.20665	.79335	30	30
	4	31	. 0899	. 9101	.6420	. 6779	.3024	.2607	. 0682	. 9318	29	56
	. 8	32	• 0922	. 9078	.6414	. 6825	.3016	.2610	. 0700	. 9300	28	52
	12 16	33 34	· 0945 · 0963	. 9055	.6408 .6402	6871 6918	.3009	.2613	0718	. 9282 . 9264	27 26	48
	20	35	60991	.39008	1.6396	.76964	1.2993	1.2619	. 0735 .20753	.79247	25	40
1	24	36	. 1014	. 8985	.6389	. 7010	.2985	.2622	. 0771	9229	24	36
	28	37	• 1037	. 8962	.6383	. 7057	.2977	.2624	0789	. 9211	23	32
	$\frac{32}{36}$	38 39	1061	. 8939	.6377 .6371	. 7103 . 7149	.2970 .2962	.2627 .2630	. 0806	. 9193	$\frac{22}{21}$	28 24
1	40	90 99	· 1084 ·61107	. 8916 .38893	1.6365	.77196	1.2954	1.2633	.20842	.79158	20	20
ı	44	41	• 1130	. 8870	.6359	. 7242	.2946	.2636	. 0860	. 9140	19	16
ı	48	42	• 1153	. 8847	.6352	. 7289	.2938	.2639	. 0878	. 9122	18	12
1	52	43	• 1176	. 8824	.6346	. 7335	.2931	.2641	. 0895	. 9104	17	8
1	56 31	44 45	• 1199 •61222	8801 38778	$\begin{array}{c} .6340 \\ 1.6334 \end{array}$. 7382 .77428	.2923 1.2915	.2644 1.2647	. 0913	. 9087	16 15	4 29
-	4	46	. 1245	. 8755	.6328	. 7475	.2907	.2650	. 0949	. 9051	14	56
ı	8	47	• 1268	. 8732	.6322	. 7521	.2900	.2653	. 0967	. 9033	13	52
ı	12	48	• 1290	. 8709	.6316	. 7568	.2892	.2656	. 0984	. 9015	12	48
ı	16 20	49 50	. 1314	. 8686	.6309	. 7614 .77661	2884	.2659 1.2661	. 1002	. 8998	11 10	44
	24	51	•61337 • 1360	.38663 . 8640	1.6303 .6297	. 7708	1.2876 $.2869$.2664	.21020 . 1038	.78980 . 8962	9	$\begin{vmatrix} 40 \\ 36 \end{vmatrix}$
	28	52	. 1383	8617	.6291	. 7754	.2861	.2667	. 1056	. 8944	8	32
	32	53	• 1405	. 8594	.6285	. 7801	.2853	.2670	. 1074	. 8926	7	28
	36	54	. 1428	. 8571	.6279	7848		.2673	. 1091	. 8908	6 5	24
1	40	55 56	.61451 . 1474	.38548 . 8525	1.6273 .6267	.77895 . 7941	1.2838 .2830	1.2676 .2679	.21109	.78850 . 8873	4	20 16
-	48	57	. 1497	. 8503	.6261	7988	.2822	.2681	. 1145	. 8855	3	12
-	52	58	. 1520	. 8480	.6255	. 8035	.2815	.2684	. 1163	. 8837	2	8
1	56	59	. 1543	. 8457	.6249	. 8082	.2807	.2687	. 1181	. 8819	1	4
1	32 M.S.	60 M	. 1566 Cosine.	. 8434 Vrs. Sin.	.6243 Secante.	. 8128 Cotaug.	.2799 Fangent.	.2690 Cosec'nt.	. 1199 Vrs. Cos	. 8801 Sine.	() M	28 M.S.
		127°)	, and out	200011001	Natu		C0500 H6.	125, 005	Dille.	52°	3h
L	1					2-44	LL COAS				-	

	NATURAL LINES. 24										
2h	389	>	Natur	al Trig	gonon	etrical	Fun	ctions	,	141°	9h
M.S.		Sine.		Cosee nte		Cotang.		Vrs.Sin	Cosine	. M	M.S
32	0	.61566	.38434	1.6243	.78128		1.2690	.21199	.78801	60	28
4	$\begin{vmatrix} 1 \\ 2 \end{vmatrix}$. 1589	. 8411	.6237	. 8175	.2792	.2693	. 1217	8783	59	56
8 12	3	. 1612	. 8388	.6231	8222	.2784	.2696	. 1235	8765	58	52
16	4	. 1635	. 8365	.6224	. 8269	.2776	.2699	. 1253	8747		48
20	5	. 1658	. 8342	.6218 1.6212	. 8316	.2769	.2702	. 1271	. 8729	56	44
24	6	. 1703	. 8296	.6206	. 8410	1.2761 .2753	1.2705	.21288	.78711	55	40
28	7	1726	8273	.6200	8457	.2746	.2710	. 1306 . 1324	8693	54 53	36 32
32	8	1749	8251	.6194	8504	.2738	.2713	1342	8657	52	28
36	9	. 1772	. 8228	.6188	. 8551	.2730	.2716	1360	8640	51	24
40	10	.61795	.38205	1.6182	.78598	1.2723	1.2719	.21378	.78622	50	20
44	11	. 1818	. 8182.	.6176	8645	.2715	.2722	. 1396	. 8604	49	16
48	12	. 1841	. 8159	.6170	. 8692	.2708	.2725	. 1414	8586	48	12
52 56	13	. 1864	. 8136	.6164	. 8739	.2700	.2728	. 1432	. 8568	47	8
33	14 15	. 1886	. 8113	.6159	. 8786	.2692	.2731	. 1450	. 8550	46	4
4	16	.61909	.38091	1.6153 .6147	.78834	1.2685	1.2734	.21468	.78532	45	27
8	17	1955	8045	.6141	8928	.2677	.2737	. 1486	. 8514 . 8496	44 43	56 52
12	18	1978	8022	.6135	8975	.2662	.2742	1522	8478	42	48
16	19	2001	7999	.6129	9022	.2655	.2745	1540	8460	41	44
20	20	.62023	.37976	1.6123	.79070	1.2647	1.2748	.21558	.78441	40	40
24	21	. 2046	. 7954	.6117	9117	.2639	.2751	. 1576	. 8423	39	36
28	22	. 2069	. 7931	.6111	. 9164	.2632	.2754	. 1594	. 8405	38	32
32	23	. 2092	. 7908	.6105	. 9212	.2624	.2757	. 1612	. 8387	37	28
36	24	. 2115	. 7885	.6099	. 9259	.2617	.2760	. 1631	. 8369	36	24
40 44	25	.62137	.37862	1.6093	.79306	1.2609	1.2763	.21649	.78351	35	20
48	26 27	. 2160	7840	.6087 .6081	. 9354	.2602	.2766	. 1667	. 8333	34 33	16
52	28	2206	7794	.6077	9449	.2587	.2772	. 1685	. 8315 . 8297	32	12 8
56	29	2229	7771	.6070	9496	.2579	.2775	1721	8279	31	4
34	30	.62251	.37748	1.6064	.79543	1.2572	1.2778	.21739	.78261	30	26
4	31	. 2274	. 7726	.6058	. 9591	.2564	.2781	. 1757	. 8243	29	56
8	32	. 2297	. 7703	.6052	. 9639	.2557	.2784	. 1775	. 8224	28	52
12	33	. 2320	. 7680	.6046	. 9686	.2549	.2787	. 1793	. 8206	27	48
16	34	. 2342	. 7657	.6040	. 9734	.2542	.2790	. 1812	. 8188	26	44
20	35	.62365	.37635	1.6034	.79781	1.2534	1.2793	.21830	.78170	25	40
24 28	36 37	. 2388	. 7612	.6029 .6023	. 9829	.2527	.2795 .2798	. 1848 . 1866	. 8152 . 8134	24 23	36 32
32	38	. 2411	. 7589 . 7566	.6023	9924	.2519 .2512	.2801	. 1884	. 8116	22	28
36	39	2456	7544	.6011	9972	.2504	.2804	1902	. 8097	21	24
40	40	.62479	.37521	1.6005	.80020	1.2497	1.2807	.21921	.78079	20	20
44	41	. 2501	. 7498	.6000	. 0067	.2489	.2810	. 1939	. 8061	19	16
48	42	. 2524	. 7476	.5994	. 0115	.2482	.2813	. 1957	. 8043	18	12
52	43	. 2547	. 7453	.5988	. 0163	.2475	.2816	. 1975	. 8025	17	8
56	44	. 2570	. 7430	.5982	. 0211	.2467	.2819	. 1993	. 8007	16	4
35	45	.62592	.37408	1.5976	.80258	1.2460	1.2822	.22011	.77988	15	25
4	46	. 2615	7385	.5971 .5965	. 0306	.2452 .2445	.2825	. 2030	. 7970 . 7952	14 13	56 52
8 12	47	. 2638 . 2660	. 7362 . 7340	.5959	. 0402	.2435 $.2437$.2828	. 2048	. 7932	$\frac{13}{12}$	48
16	49	. 2683	. 7317	.5953	. 0450	.2430	.2834	. 2084	7915	11	44
20	50	.62706	.37294	1.5947	.80498	1.2423	1.2837	.22103	.77897	10	40
24	51	. 2728	7272	.5942	. 0546	.2415	.2840	. 2121	. 7879	9	36
28	52	. 2751	. 7249	.5936	. 0594	.2408	.2843	. 2139	. 7861	8	32
32	53	. 2774	7226	.5930	. 0642	.2400	.2846	. 2157	. 7842	7	28
36	54	. 2796	. 7204	.5924	. 0690	.2393	.2849	. 2176	. 7824	6	24
40	55	.62819	.37181	1.5919	.80738	1.2386	1.2852	.22194	.77806	5	20
41	56	. 2841	7158	.5913	. 0786	.2378	.2855	. 2212	. 7788 . 7769	4 3	$\begin{array}{c c} 16 \\ 12 \end{array}$
48 52	57 58	. 2864	7136	.5907	. 0834	.2364	.2861	2249	7751	$\begin{bmatrix} 3 \\ 2 \end{bmatrix}$	8
56	59	. 2887	. 7113 . 7090	.5896	. 0032	.2356	.2864	2267	7733	í	4
36	60	. 2932	7068	.5890	. 0978	.2349		. 2285	7715		24
M.S.	M	Cosine.	Vrs.Sin.			Taugent.			Sine.	M	M.S.
8h	1289				Natu					51°	3h

2h 39° Natural Trigonometrical Functions. 140° 9h												
2h	399									40°		
M.S.	M	Sine.		Cosec'nte				Vrs. Sin	Cosine.	_	M.S.	
36	0	.62932	.37068	1.5890 .5884	.80978	1.2349 .2342	1.2867	.22285	77715	60 59	24 56	
8	2	. 2977	7023	.5879	1075	.2334	.2874	2322	7678	58	52	
12	3	3000	7000	.5873	1123	.2327	.2877	2340	7660	57	48	
16	4	. 3022	. 6977	.5867	. 1171	.2320	.2880	. 2359	7641	56	44	
20	5	.63045	.36955	1.5862	.81219	1.2312	1.2883	.22377	.77623	55	40	
24	6	. 3067	6932	.5856	. 1268	.2305	.2886	. 2395	. 7605	54	36	
28	7	. 3090	. 6910	.5850	. 1316	.2297	.2889	. 2414	. 7586	53	32	
32 36	8 9	. 3113	6887	.5845 .5839	. 1364	.2290	.2892	. 2432	. 7568	52 51	28 24	
40	10	.63158	.36842	1.5833	.81461	1.2276	1.2898	.22469	.77531	50	20	
44	11	. 3180	. 6820	.5828	. 1509	.2268	.2901	. 2487	. 7513	49	16	
48	12	. 3203	6797	.5822	. 1558	.2261	.2904	. 2505	. 7494	48	12	
52	13	. 3225	. 6774	.5816	. 1606	.2254	.2907	. 2524	. 7476	47	8	
56	14	. 3248	. 6752	.5811	. 1655	.2247	.2910	2542	. 7458	46	4	
37	15	.63270 . 3293	.36729	1.5805	.81703	1.2239	1.2913	.22561	.77439	45 44	23 56	
8	16 17	. 3315	6707	.5799 .579 4	. 1752 . 1800	.2232	.2916	. 2579	. 7421	43	52	
12	18	. 3338	6662	.5788	1849	.2218	.2922	2616	7384	42	48	
16	19	. 3360	6639	.5783	. 1898	.2210	.2926	. 2634	. 7365	41	44	
20	20	.63383	.36617	1.5777	.81946	1.2203	1.2929	.22653	.77347	40	40	
24	21	. 3405	. 6594	.5771	. 1995	.2196	.2932	. 2671	. 7329	39	36	
28	22	. 3428	6572	.5766	. 2043	.2189	.2935	. 2690	. 7310	38	32	
32 36	$\begin{array}{c c} 23 \\ 24 \end{array}$. 3450 . 3473	$6549 \\ 6527$	-5760	. 2092	.2181	.2938	. 2708	. 7292 . 7273	37 36	28 24	
40	$\frac{24}{25}$.63495	.36504	.5755 1.5749	. 2141 .82190	1.2167	1.2944	.22745	.77255	35	20	
44	26	. 3518	. 6482	.5743	. 2238	.2160	.2947	. 2763	. 7236	34	16	
48	27	. 3540	. 6459	.5738	. 2287	.2152	.2950	. 2782	. 7218	33	12	
52	28	. 3563	. 6437	.5732	. 2336	.2145	.2953	. 2800	. 7199	32	8	
56	29	. 3585	. 6415	.5727	. 2385	.2138	.2956	. 2819	. 7181	31	4	
38	30	.63608 . 3630	.36392 .6370	1.5721	.82434	1.2131	1.2960	.22837	.77162	30 29	22 56	
8	$\begin{array}{c} 31 \\ 32 \end{array}$. 3653	6347	.5716 .5710	. 2482	.2124	.2963	. 2856	. 7144	28	52	
12	33	. 3675	6325	.5705	2580	.2109	.2969	. 2893	. 7107	27	48	
16	34	. 3697	. 6302	.5699	. 2629	.2102	.2972	. 2912	. 7088	26	44	
20	35	.63720	.36280	1.5694	.82678	1.2095	1.2975	.22930	.77070	25	40	
24	36	. 3742	. 6258	.5688	. 2727	.2088	.2978	. 2949	. 7051	24	36	
28	37	. 3765	6235	.5683	. 2776	.2081	.2981	. 2967	. 7033	23	32	
32 36	38 39	. 3787	. 6213 . 6190	.5677 .5672	. 2825	.2074	.2985 .2988	. 2986 . 3004	. 7014	22 21	$\begin{array}{c} 28 \\ 24 \end{array}$	
40	40	.63832	.36168		.82923		1.2991	.23023	.76977	20	20	
1 44	41	. 3854	. 6146	.5661	2972	.2052	.2994	. 3041	. 6958	19	16	
48	42	. 3877	. 6123	.5655	. 3022	.2045	.2997	. 3060	. 6940	18	12	
52	43	. 3899	. 6101	.5650	. 3071	.2038	.3000	. 3079	. 6921	17	8	
56	44	. 3921	. 6078	.5644	. 3120	.2031	.3003	. 3097	. 6903	16	4	
39	45 46	.63944	.36056 . 6034	1.5639 .5633	.83169 . 3218	1.2024 .2016	1.3006 .3010	.23116 . 3134	.76884	15 14	21 56	
8	47	. 3989	6011	.5628	. 3218	2009	.3013	. 3153	. 6847	13	52	
12	48	. 4011	. 5989	.5622	. 3317	2003	.3016	. 3172	. 6828	12	48	
16	49	. 4033	. 5967	.5617	. 3366	.1995	.3019	. 3190	6810	11	44	
20	50	.64056	.35944	1.5611	.83415	1.1988	1.3022	.23209	.76791	10	40	
24	51	. 4078	. 5922	.5606	. 3465	.1981	.3025	. 3227	. 6772	9	36	
28 32	52	. 4100	5900	.5600	. 3514	.1974	.3029	3246	6754	8	32	
36	53 54	. 4123	. 5877 . 5855	.5595 .5590	. 3563 . 3613	.1967 .1960	.3032 .3035	. 3265 . 3283	. 6735 . 6716	7 6	28 24	
40	55	.64167	.35833	1.5584	.83662	1. 1953	1.3038	.23302	.76698	5	20	
44	56	. 4189	. 5810	.5579	. 3712	.1946	.3041	. 3321	. 6679	4	16	
48	57	. 4212	. 5788	.5573	. 3761	.1939	.3044	. 3339	. 6660	3	12	
52	58	. 4234	: 5766	.5568	. 3811	.1932	.3048	. 3358	. 6642	2	8	
56 40	59 60	. 4256	5743	.5563	3860		.3051	. 3377	6623	1	20	
M.S.	M	. 4279 Cosine.	. 5721 Vrs.Sin.	.5557 Secante.	. 3910 Cotang.	.1917 Tangent.	.3054 Cosec'nt	. 3395 Vrs. Cos	6604 Sine.	0 M	20 M.S.	
	129)			Natu		2000 1101		,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,	50°	3h	

1	-	1										
	2 ^h	400		Natur	al Trig	gonom	etrical	l Fun	ctions.		1399	9h
ı	M.S.	M	Sine.		Cosec'nte		Cotang		. Vrs. Sin		. [M	M.S.
Į	40	0	.64279	.35721	1.5557	.83910	1.1917	1.3054	23395	.76604		
	4	1	. 4301	. 5699	.5552	. 3959	.1910	.3057	3414	. 6586		56
	8	2	. 4323	. 5677	.5546	. 4009	.1903	.3060	. 3433	6567		52
	12 16	3 4	. 4345	. 5654	.5541	. 4059	.1896	.3064	. 3452	6548		48
ı	20	5	.4369	. 5632	.5536	. 4108	.1889	.3067	3470	6530		44
	24	6	. 4412	. 35610	1.5530 .5525	.84158	1.1882	1.3070 .3073	.23489	.76511	55	36
	28	7	4435	. 5565	.5520	4257	.1868	.3076	3527	6473		32
	32	8	. 4457	5543	.5514	4307	.1861	.3080	3545	6455		28
	36	9	. 4479	. 5521	.5509	. 4357	.1854	.3083	. 3564	. 6436		24
	40	10	.64501	.35499	1.5503	.84407	1.1847	1.3086	.23583	.76417		20
:	44 48	11 12	. 4523	. 5476	.5498	. 4457	.1840	.3089	3602	. 6398		16
,	52	13	. 4546	5454	.5493	. 4506	.1833	.3092	3620	6380		132
ı	56	14	. 4590	. 5410	.5482	. 4606	.1826	.3096	. 3639	. 6361 . 6342	47 46	8
I	41	15	.64612	.35388	1.5477	.84656	1.1812	1.3102	.23677	.76323	45	19
ı	4	16	. 4635	. 5365	.5471	. 4766	.1805	.3105	. 3695	6304	44	56
ł	8	17	. 4657	. 5343	.5466	. 4756	.1798	.3109	. 3714	. 6286	43	52
	12	18	. 4679	. 5321	.5461	. 4806	.1791	.3112	. 5733	. 6267	42	48
ı	16 20	19 20	. 4701	. 5299	.5456	. 4856	.1785	.3115	. 3752	. 6248	41	44
ı	24	21	.64723	.35277	1.5450 .5445	.84906	1.1778	1.3118	.23771	.76229	40 39	40 36
	28	22	4768	5232	.5440	5006	.1764	.3125	3790	6191	38	32
I	32	23	4790	5210	.5434	. 5056	.1757	.3128	3827	6173	37	28
ı	36	24	. 4812	. 5188	.5429	. 5107	.1750	.3131	. 3846	. 6154	36	2.1
ı	40	25	.64834	.35166	1.5424	.85157	1.1743	1.3134	.23565	.76135	35	20
	44	26	. 4856	. 5144	.5419	. 5207	.1736	.3138	. 3884	. 6116	34	16
ı	48 52	27	. 4878	. 5121	.5413	5257	.1729	.3141	3903	6097	33	12
ı	56	28 29	. 4900	. 5099	.5408 .5403	. 5307 . 5358	.1722	.3144	. 3922	6078	32 31	8 4
	42	30	.64945	.35055	1.5398	.85408	1.1708	1.3151	.23959	.76041	30	18
	4	31	. 4967	. 5033	.5392	. 5458	.1702	.3154	. 3978	. 6022	29	56
	8	32	. 4989	. 5011	.5387	. 5509	.1695	.3157	. 3997	. 6003	28	52
	12	33	. 5011	. 4989	.5382	. 5559	.1688	.3161	. 4016	. 5984	27	48
	16	34	. 5033	. 4967	.5377	. 5609	.1681	.3164	. 4035	. 5965	26	44
	20 24	35 36	.65()55	.34945	1.5371 .5366	.85660 . 5710	1.1674	.3167	.24054	.75946 . 5927	25 24	40 36
ļ	28	37	. 5099	4900	.5361	5761	.1660	.3174	. 4092	. 5908	23	32
Ì	32	38	. 5121	. 4878	.5356	5811	.1653	.3177	. 4111	. 5859	22	28
1	36	39	. 5144	. 4856	.5351	. 5862	.1647	.3180	. 4130	. 5870	21	24.
	40	40	.65166	.34834	1.5345	.85912	1.1640	1.3184	.24149	.75851	20	20
	44	41	. 5188	. 4812	.5340	. 5963	.1633	.3187	. 4168	. 5832	19	16
-	48 52	42	5210	4790	.5335	6013	.1626	.3190	. 4186	5704	18 17	12 8
1	56	43	. 5232 . 5254	. 4768	.5330 .5325	. 6064 . 6115	.1619 .1612	.3193	. 4205 . 4224	. 5794 . 5775	16	8 4
	43	45	.65276	.34724	1.5319	.86165	1.1605	1.3200	.24243	.75756	15	17
1	4	46	. 5298	. 4702	.5314	. 6216	.1599	3203	. 4262	. 5737	14	56
	8	47	. 5320	. 4680	.5309	. 6267	.1592	.3207	. 4281	. 5718	13	52
1	12	48	. 5342	. 4658	.5304	. 6318	.1585	.3210	. 4300	. 5699	12	48
۱	16	49	. 5364	. 4636	.5299	. 6368	.1578	.3213	. 4319	. 5680	11	44
	20 24	50	.65386	.34614 . 4592	1.5294	.86419	1.1571 .1565	1.3217 $.3220$.24338	.75661 . 5642	$\begin{array}{c c} 10 \\ 9 \end{array}$	40 36
-	28	51 52	. 5430	. 4570	.5283	. 6521	.1558	.3223	4376	5623	8	32
1	32	53	5452	4548	.5278	6572	.1551	.3227	4396	5604	7	28
-	36	54	. 5474	. 4526	.5273	. 6623	.1544	.3230	. 4415	. 5585	6	24
1	40	55	.65496	.34504	1.5268	.86674	1.1537	1.3233	.24434	.75566	5	20
-	44	56	. 5518	. 4482	.5263	. 6725	.1531	.3237	. 4453	. 5547	4	16
1	48	57	. 5540	. 4460	.5258	6775	.1524	.3240	. 4472	5528	3 2	12 8
	52 56	58 59	. 5562	. 4438	.5253	6826	.1517	.3243	. 4491	. 5509 . 5490	1	4
-	44	60	. 5606	. 4394	.5242	6929	.1504	.3250	4529	5471	0	16
1	M.S.	M	Cosine.				Tangent.			Sine.	M	M.S.
1	8h	130°				Natu					49°	3h
L												

1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1												
2h	41°		Natura	ıl Trig	onom	etrical	Func	ctions	. 1	33°	9h	
M.S.	М	Sine.		Cosec'nte		Cotang.	Secante.				M.S.	
44	0	.65606	.34394	1.5242	.86929	1.1504	1.3250	.24529	.75471	60 59	16 56	
8	$\frac{1}{2}$. 5628 . 5650	. 4372 . 4350	.5237 .5232	. 6980 . 7031	.1497 .1490	.3253 .3257	. 4546	5433	58	52	
12	3	. 5672	4328	.5227	7082	.1483	.3260	4586	. 5414	57	48	
16	4	. 5694	4306	.5222	. 7133	.1477	.3263	. 4605	. 5394	56	44	
20	5	.65716	.34284	1.5217	.87184	1.1470	1.3267	.24624	.75375	55	40	
24	6	. 5737	. 4262	.5212	. 7235 . 7287	.1463 .1456	.3270 .3274	. 4644 . 4663	. 5356	54 53	$\begin{array}{c} 36 \\ 32 \end{array}$	
28 32	7 8	. 5759 . 5781	. 4240	.5207 $.5202$. 7338	.1450	.3277	. 4682	5318	52	28	
36	9	. 5803	. 4197	.5197	7389	.1443	.3280	4701	5299	51	24	
40	10	.65825	.34175	1.5192	.87441	1.1436	1.328±	.24720	.75280	50	20	
44	11	. 5847	. 4153	.5187	. 7492	.1430	.3287	. 4739	. 5261	49	16	
48	12	. 5869	. 4131	.5182	7543	.1423	.3290 .3294	. 4758	. 5241	48 47	12 8	
52 56	13 14	. 5891 . 5913	. 4109	.5177	. 7595	.1409	.3297	. 4797	5203	46	4	
45	15	.65934	.34065	1.5166	.87698	1.1403	1.3301	.24816	.75184	45	15	
4	16	. 5956	. 4043	.5161	. 7749	.1396	.3304	. 4835	. 5165	44	56	
8	17	. 5978	. 4022	.5156	. 7801	.1389	.3307	. 4854	. 5146	43	52	
12	18	. 6000	. 4000	.5151	. 7852	.1383	.3311	. 4873	. 5126 . 5107	42 41	48 44	
16	19	. 6022 .66044	. 3978	.5146 1.5141	.87955	.1376 1.1369	.3314 1.3318	. 4893	.75088	40	40	
20 24	$\begin{vmatrix} 20 \\ 21 \end{vmatrix}$. 6066	. 3934	.5136	. 8007	.1363	.3321	. 4931	. 5069	39	36	
28	22	. 6087	:3912	.5131	. 8058	.1356	.3324	. 4950	. 5049	38	32	
32	23	. 6109	. 3891	.5126	. 8110	.1349	.3328	. 4970	. 5030	37	28	
36	24	. 6131	. 3869	.5121	. 8162	.1343	.3331	. 4989	. 5011	36	24	
40	25	.66153	.33847	1.5116 .5111	.88213	1.1336 .1329	1.3335 .3338	. 25008	.74992 . 4973	35 34	20 16	
44 48	$\begin{bmatrix} 26 \\ 27 \end{bmatrix}$	6175	3803	.5106	. 8317	.1323	.3342	5047	4953	33	12	
52	28	6218	3781	.5101	. 8369	.1316	.3345	. 5066	. 49.34	32	8	
56	29	. 6240	. 3760	.5096	. 8421	.1309	.3348	. 5085	. 4915	31	4	
46	30	.66262	.33738	1.5092	.88472	1.1303	1.3352	.25104	.74895	30	14	
4	31	. 6284	3716	.5087	. 8524	.1296	.3355	5124	. 4876 . 4857	29 28	56 52	
8 12	32 33	. 6305	. 3694	.5082 .5077	. 8576 . 8628	.1290 .1283	.3359 .3362	5143	. 4838	$\frac{20}{27}$	48	
16	34	6349	3651	.5072	. 8680	.1276	.3366	5181	. 4818	26	44	
20	35	.66371	.33629	1.5067	.88732	1.1270	1.3369	.25201	.74799	25	40	
24	36	. 6393	. 3607	.5062	. 8784	.1263	.3372	. 5220	4780	24	36	
28	37	. 6414	. 3586	.5057	. 8836	.1257	.3376 .3379	5239 5259	. 4760	23 22	32 28	
32	38	. 6436 . 6458	. 3564	.5052 .5047	. 8888	.1243	.3383	5278	4722	21	24	
36	40	.66479	.33520	1.5042	.88992		1.3386	.25297	.74702	26	20	
44	41	. 6501	. 3499	.5037	. 9044	.1230	.3390	. 5317	. 4683	19	16	
48	42	. 6523	. 3477	.5032	. 9097	.1224	.3393	. 5336	. 4664	18	12	
52	43	. 6545	. 3455	.5027	. 9149	.1217	3397	. 5355	. 4644	17 16	8 4	
56	44 45	. 6566	.3433	.5022 1.5018	. 9201	.1211 1.1204	3400 1.3404	. 5375	.74606	15	13	
4	46	. 6610	. 3390	.5013	. 9306	.1197	.3407	. 5414	4586	14	56	
8	47	. 6631	. 3368	.5008	. 9358	.1191	.3411	. 5433	. 4567	13	52	
12	48	. 6653	. 3347	.5003	. 9410	.1184	.3414	. 5452	. 4548	12	48	
16	49	. 6675	. 3325	.4998	. 9463	.1178	.3418	. 5472	4528	11	44	
20 24	50	.66697	.33303	1.4993 .4988	.89515	1.1171 .1165	1.3421 .3425	.25491	.74509 . 4489	10	40 36	
28	52	6740	3260	.4983	9620	.1158	.3428	. 5530	. 4470	8	32	
32	53	6762	3238	.4979	. 9672	.1152	.3432	. 5549	. 4450	7	28	
36	54	. 6783	. 3217	.4974	. 9725	.1145	.3435	. 5569	. 4431	6	24	
40	55	.66805	.33195	1.4969	.89777	1.1139	1.3439	.25588	.74412	5	20	
44	56	6826	3173	.4964 .4959	9830	.1132 .1126	.3442 .3446	5608	. 4392 . 4373	4 3.	$\frac{16}{12}$	
48 52	57	6848	3152	.4954	. 9935	.1119	.3449	. 5647	4353	2	8	
56.	59	6891	3108	.4949	. 9988	.1113	.3453	. 5666	4334	ī	4	
48	60	. 6913	. 3087	.4945	.90040	.1106	.3456	. 5685	. 4314	0	12	
M.S. M Cosine. Vrs. Sin. Secante. Cotang. Tangent. Cosec'nt Vrs. Cos Sine. M M.S.												
8h	131				Natu	ral.				48°	3h	

TATOMAE DINES.												
2h	420)								0=0	9h	
Transfer and an armonical relations.												
M.S.	M	Sine.	Vrs. Cos.	Cosec'nte	Tang.	Cotang.	Secante.	Vrs.Sin	Cosine.	M	M.S.	
48	0	.66913	.33087	1.4945	.90040	1.1106	1.3456	.25685	.74314	60	12	
4	1	. 6935	. 3065	.494()	. 0093	.1100	.3460	. 5705	. 4295	59	56	
8	2	. 6956	. 3044	.4935	. 0146	.1093	.3463	. 5724	. 4275	58	52	
12	3	. 6978	. 3022	.4930	. 0198	.1086	.3467	. 5744	. 4256	57	48	
16	4	. 6999	. 3000	.4925	. 0251	.1080	.3470	. 5763	. 4236	56	14	
20	5	.67021	.32979	1.4921	.90304	1.1074	1.3474	.25783	.74217	55	40	
24	6	. 7043	2957	.4916 .4911	0357	.1067	.3477	. 5802	. 4197	54	36	
28 32	7 8	. 7064 . 7086	. 2936	.4911	. 0410	.1061	.3481	. 5822	. 4178	53	32	
36	9	7107	. 2893	.4901	. 0463	.1054	.3485	. 5841	. 4158	52 51	28 24	
40	10	.67129	.32871	1.4897	.90568	1.1041	1.3492	.25880	.74119	50	$\frac{24}{20}$	
44	11	. 7150	2849	.4892	. 0621	.1035	.3495	. 5900	. 4100	49	16	
48	12	. 7172	2828	.4887	0674	.1028	.3499	5919	4080	48	12	
52	13	7194	2806	.4882	0727	.1022	.3502	5939	. 4061	47	8	
56	14	. 7215	. 2785	.4877	. 0780	.1015	.3506	. 5959	. 4041	46	4	
49	15	.67237	.32763	1.4873	.90834	1.1009	1.3509	.25978	.74022	45	11	
4	16	. 7258	. 2742	.4868	. 0887	.1003	.3513	. 5998	. 4002	44	56	
8	17	. 7280	. 2720	.4863	• 0940	.0996	.3517	. 6017	. 3983	43	52	
12	18	. 7301	. 2699	.4858	. 0993	.0990	.3520	. 6037	. 3963	42	48	
16	19	. 7323	2677	.4854	. 1046	.0983	.3524	. 6056	. 3943	41	44	
20	20	.67344	.32656	1.4849	.91099	1.0977	1.3527	.26076	.73924	40	40	
24 28	21 22	. 7366 . 7387	. 2634	.4844 .4839	· 1153 · 1206	.0971	.3531	6096	. 3904	39 38	36 32	
32	23	. 7409	2591	.4835	1259	.0958	.3538	6115	. 3865	37	28	
36	24	7430	2570	.4830	1312	.0951	.3542	6154	. 3845	36	24	
40	25	.67452	.32548	1.4825	.91366	1.0945	1.35 15	.26174	.73826	35	20	
44	26	. 7473	. 2527	.4821	• 1419	.0939	.3549	: 6194	. 3806	34	16	
48	27	. 7495	. 2505	.4816	• 1473	.0932	.3552	. 6213	. 3787	33	12	
52	28	. 7516	. 2484	.4811	. 1526	.0926	.3556	. 6233	. 3767	32	8	
56	29	. 7537	. 2462	.4806	• 1580	.0919	.3560	. 6253	. 3747	31	4	
50	30	.67559	.32441	1.4802	•91633	1.0913	1.3563	.26272	.73728	30	10	
4	31	• 7580	. 2419	.4797	• 1687	.0907	.3567	. 6292	. 3708	29	56	
8	32	. 7602	. 2398	.4792	. 1740	.0900	.3571	6311	. 3688	28	52	
12	33	. 7623	. 2377	.4788	1794	.0894	.3574	6331	. 3669	27 26	48 41	
16 20	34 35	• 7645	. 2355	.4783 1.4778	.1847	.0888	1.3581	. 6351 .26371	. 3649	25	40	
24	36	.67666 .7688	.32334	.4774	• 1955	.0875	.3585	. 6390	. 3610	24	36	
28	37	7709	2291	.4769	2008	.0868	.3589	6410	. 3590	23	32	
32	38	7730	2269	.4764	2062	.0862	.3592	. 6430	3570	22	28	
36	39	. 7752	2248	.4760	2116	.0856	.3596	. 6449	. 3551	21	24	
40	40	.67773	.32227	1.4755	.92170	1.0849	1.3600	.26469	.73531	20	20	
44	41	. 7794	. 2205	.4750	• 2223	.0843	.3603	. 6489	. 3511	19	16	
48	42	. 7816	. 2184	.4746	. 2277	.0837	.3607	6508	. 3491	18	12	
52	43	• 7837	. 2163	.4741	. 2331	.0830	.3611	. 6528	. 3472	17	8	
56	44	. 7859	. 2141	.4736	. 2385	.0824	.3614	6548	3452	16	4	
51	45	•67880	.32120	1.4732	.92439	1.0818	1.3618	.26568	.73432	15	9	
4	46	7901	2098	.4727	. 2493 . 2547	.0812	.3622 .3625	. 6587 . 6607	. 3412	14 13	56 52	
8 12	47	· 7923 · 7944	. 2077	.4723 .4718	2601	.0505	.3629	. 6627	. 3373	12	48	
16	48 49	7965	2034	.4713	. 2655	.0793	.3633	. 6647	. 3353	11	44	
20	50	.67987	.32013	1.4709	.92709	1.0786	1.3636	.26666	.73333	10	40	
24	51	. 8008	. 1992	.4704	. 2763	.0780	.3640	. 6686	. 3314	9.	36	
28	52	. 8029	. 1970	.4699	. 2817	.0774	.3644	. 6706	. 3294	8	32	
32	53	. 8051	. 1949	.4695	. 2871	.0767	.3647	. 6726	. ::274	7	28	
36	54	. 8072	. 1923	.4690	. 2926	.0761	.3651	. 6746	. 3254	6	24	
40 55 .68093 .31907 1 4686 .92980 1.0755 1.3655 .26765 .73234 5 20												
44 56 . 8115 . 1885 . 4681 . 3034 . 0749 . 3658 . 6785 . 3215 4 16 48 57 . 8136 . 1864 . 4676 . 3088 . 0742 . 3662 . 6805 . 3195 3 12												
48	57	. 8136	. 1864	.4676	. 3088	.0742	.3662	. 6805	. 3195		12	
52	58	. 8157	. 1843	.4672	. 3143	.0736	.3666	. 6825	. 3175	2	8	
56	59	. 8178	. 1821	.4667	. 3197	.0730 .0724	.3663 .3673	. 6845 . 6865	. 3155 . 3135	$\begin{bmatrix} 1 \\ 0 \end{bmatrix}$	4 8	
52 M.S.	M. S. M. Cosine, Vrs. Sin. Secante, Cotang, Taugent, Cosec'nt, Vrs. Cos. Sine, M. M. S.											
8h	1329)	, 12. DIE.	Double !	Natu		JUDGU HIN			470	31	
0	102				TASTE	1410						

2 ^h	43°		Natur	al Trig	onom	etrical	Func	tions.]	36°	9h
ı.s.	M	Sine.		Cosec'nte		Cotang.		Vrs. Sin	Cosine.		M.S
52	0	.68200	.31800	1.4663	.93251	1.0724	1.3673	.26865	.73135	60	8
4 8	$\frac{1}{2}$. 8221	1779	.4658	. 330 6 . 3360	.0717	.3677	. 6884	. 3115	59 58	56 52
12	3	. 8242 . 8264	. 1758	.4654 .4649	. 3415	.0711	.3084	6921	. 3076	57	48
16	4	. 8285	1715	.4644	. 3469	.0699	.3688	6944	. 3056	56	44
20	5	.68306	.31694	1.4640	.93524	1.0692	1.3492	.26964	.73036	55	40
24	6	. 8327	. 1673	.4635	. 3578	.0686	.3695	. 6984	. 3016	54	36
28	7	. 8349	. 1651	.4631	. 3633	.0680	.3699	. 7004	. 2996	53	32
32	8	. 8370	. 1630	.4626	. 3687	.0674	.3703	. 7023	. 2976	52	28
36 40	9 10	. 8391	. 1609	.4622	. 3742	.0667	.3707 1.3710	. 7043	. 2 9 56 .72937	51 50	24 20
44	11	.68412	.31588	1.4617 .4613	. 3851	1.0661 .0655	.3714	. 7083	. 2917	49	16
48	12	. 8455	. 1545	.4608	3906	.0649	.3718	. 7103	2897	48	12
52	13	. 8476	1524	.4604	. 3961	.0643	.3722	. 7123	. 2877	47	8
56	14	. 8497	. 1503	.4599	. 4016	.0636	.3725	. 7143	. 2857	46	+
53	15	.68518	.31482	1.4595	.94071	1.0630	1.3729	.27163	.72837	45	7
4	16	. 8539	. 1460	.4590	. 4125	.0624	.3733	. 7183	. 2817	44	56
8	17	. 8561	. 1439	.4586	. 4180	.0618	.3737	. 7203	. 2797	43	52
12	18 19	. 8582	. 1418	.4581	1235	.0612	.3740	7223	. 2777	42 41	48
16 20	20	. 8603	. 1397	.4577 1.4572	. 4290	.0605 1.0599	.374 1 1.3748	. 7243 .27263	.72737	40	40
24	21	. 8645	. 1355	.4568	. 4400	.0593	.3752	. 7283	. 2717	39	36
28	22	. 8666	. 1333	.4563	. 4455	.0587	3756	7302	. 2697	38	32
32	23	. 8688	. 1312	.4559	. 4510	.0581	.3759	. 7322	. 2677	37	28
36	24	. 8709	. 1291	.4554	. 4565	.0575	.3763	. 7342	. 2657	36	24
40	25	.68730	.31270	1.4 550	.94620	1.0568	1.3767	.27362	.72637	35	20
44	26	. 8751	. 1249	.4545	. 4675	.0562	.3771	. 7382	. 2617	34	16
48	27	. 8772	. 1228	.4541	. 4731	.0556	.3774	. 7402	. 2597	33	12
52 56	28 29	. 8793 . 8814	. 1207	.4536	. 4786	.0550	.3778	. 7422 . 7442	. 2577 . 2557	$\begin{vmatrix} 32 \\ 31 \end{vmatrix}$	8 4
54	30	.68835	. 1186	$egin{array}{c} .4532 \ 1.4527 \ \end{array}$. 4841	.0544 1.0538	.3782 1.3786	.27462	.72537	30	6
4	31	. 8856	. 1143	.4523	. 4952	.0532	.3790	. 7482	. 2517	29	56
8	32	. 8878	. 1122	.4518	. 5007	.0525	3794	7503	2497	28	52
12	33	. 8899	. 1101	.4514	. 5062	.0519	.3797	. 7523	. 2477	27	48
16	34	. 8920	. 1080	.4510	. 5118	.0513	.3801	7543	. 2457	26	44
20	35	.68941	.31059	1.4505	.95173	1.0507	1.3805	.27563	.72437	25	40
24	36	. 8962	. 1038	.4501	. 5229	.0501	.3809	7583	. 2417	2 4 23	$\begin{array}{c} 36 \\ 32 \end{array}$
28 32	37 38	. 8983	. 1017	.4496 .4492	. 5284	0495 $.0489$.3813 .3816	. 7603 . 7623	. 2397 . 2377	22 22	28
36	39	. 9004	. 0975	.4487	. 5395	.0483	.3820	7643	. 2357	21	24
40	40	.69046	.30954		.95451	1.0476	1.3824	.27663	.72337	20	20
44	41	. 9067	. 0933	.4479	. 5506	.0470	.3\28	. 7683	. 2317	19	16
48	42	. 9088	. 0912	.4474	. 5562	.0464	.3832	. 7703	. 2297	18	12
52	43	. 9109	. 0891	.4470	. 5618	.0458	.3886	. 7723	. 2277	17	8
56	44	. 9130	. 0870	.4465	. 5673	.0452	.3839	. 7743	. 2256	16	4
55	45	.69151	.30849	1.4461	.95729	1.0446	1.3843	.27764	.72236	15	5
4	46	. 9172	. 0828	.4457	. 5785	.0440	.3847	. 7784	. 2216	14 13	56 52
$\begin{bmatrix} 8 \\ 12 \end{bmatrix}$	47 48	. 9193	. 0807	.4452 .4448	. 5841	.0434 .0428	.3851 .3855	. 7824	. 2176	12	48
16	49	. 9235	. 0765	.4443	. 5952	.0422	.3859	. 7844	. 2156	11	44
20	50	.69256	.30744	1.4439	.96008	1.0416	1.3863	.27864	.72136	10	40
24	51	. 9277	. 0723	.4435	. 6064	.0410	.3867	. 7884	. 2115	9	36
28	52	. 9298	. 0702	.4430	. 6120	.0404	.3870	. 7901	. 2095	8	32
32	53	. 9319	. 0681	.4426	. 6176	.0397	.3874	. 7925	. 2075	7	28
36	54	. 9340	. 0660	.4422	. 6232	.0391	.3878	. 7945	. 2055	6	24
40	55	.69361	.30639	1.4417	.96288	1.0385	1.3882	.27965	.72035	5	20
44 48	56 57	. 9382	. 0618	.4413	6344	.0379	.3886 .3890	. 7985 . 8005	. 2015 . 1994	$\begin{bmatrix} 4 \\ 3 \end{bmatrix}$	16 12
52	58	. 9403 . 9424	. 0597	.4404	. 6400 . 6456	.0373	.3894	8026	. 1994	$\frac{3}{2}$	8
74	59	. 9445	. 0555	.4400	. 6513	.0361	.3898	8046	. 1954	1	4
56			. 50.50								
_	60	. 9406	. 0534	.4395	. 6569	.0355	.3902	. 8066	. 1934	0	4
56 56 1. S. Sh		Cosine.	. 0534 Vrs.Sin,		. 6569 Cotang.	.0355 Taugent.	.3902 Cosce'nt	. 8066 Vrs. Cos	Sine.		M.S.

NATURAL LINES. 20												
2h 44° Natural Trigonometrical Functions. 135° 9												
M.S.	М	Sine.		Cosec nte	Tang.	Cotang.	Secante.			M	M.S.	
56	0	.69466	.30534	1.4395	.96563	1.0355	1 3902	.28066	.71934	60	4	
4	1	. 9487	. 0513	.4391	. 6625	.0349	.3905	. 8086	1914	59	56	
8	2 3	9508	. 0492	.4387	. 6681	.0343	.3)(19	. 8106	. 1893	58	52	
12 16	4	• 9528 • 9549	. 0471	.4382 .4378	6738	.0337	.3913	8127	. 1873	57	43	
20	5	.69570	.30430	1.4374	.96850	.0331	3917	. 8147	. 1853	56 55	44 40	
24	6	9591	. 0409	.4370	6307	.0319	.3925	. 8187	. 1813	54	36	
28	7	. 9612	. 0388	.4365	. 6963	.6313	.3929	. 8208	1792	53	32	
32	8	. 9033	. 0367	.4361	. 7020	.0307	.3933	. 8228	1772	52	28	
36	9	. 9651	. 0246	4357	. 7076	.0:01	.3937	. 8248	. 1752	51	24	
40	10	.69675	.30325	1.4352	.97133	1.0.95	1.3941	.28268	.71732	50	20	
44	11	9696	. 03:04	.4348	. 7189	.0289	.3945	. 8289	. 1711	49	16	
48	12	9716	. 0283	.4344	- 7246	.6283	.394.)	. 8309	. 1691	48	12	
52	13	9737	. 0263	.4339	. 7302	.0277	.3953	. 8329	. 1671	47	8	
56	14	9758	. 0242	.4335	73:9	.0271	.3957	. 8349	16.0	46	3	
4	15 16	.69779	. 0200	1.4331 .4327	.97416 $.7472$	1.0265	1.396 ⁻⁾ .3964	.28370	.71630	45 44	56	
8	17	9821	. 0179	.4322	7529	.0253	.3968	. 8; 90 . 8410	1589	43	52	
12	is	. 9841	0158	.4318	7586	.0247	.3974	. 8431	1. 1769	42	48	
16	19	. 9862	0138		. 7643	.0241	.3974	8451	1549	41	44	
20	20	-69583	.30117	1.4310	.97699	1.0235	1.3980	.28471	.71529	40	40	
24	21	. 9904	. 0096	.4305	. 7756	.0229	.39 4	. 8 92	. 1508	39	36	
28	22	• 9925	. 0075	.4301	• 7813	.0223	.8983	. 8512	. 1488	38	32	
32	23	. 9945	. 0054	.4297	- 7870	.0218	.3992	. 8532	. 1468	37	28	
36	24	. 9966	. 0034	.4292	. 7927	.0212	.3996	. 8553	. 1447	36	24	
40	25	69987	.30013	1.4288	.97984	1.0206	1.4000	.28573	.71427	35	20	
141	26	•70008	.29992	.4284	. 8041	.0200	.4004	. 8593	. 1406	34	16 12	
48 52	27 28	• 0029 • 0049	9971	.4280 .4276	• 8098 • 8155	.0194	.4008	. 8614	. 1386	33	8	
56	$\begin{bmatrix} 26 \\ 29 \end{bmatrix}$	0070	9930	.4271	8212	.0168	.4016	8654	. 1345	31	4	
58	$\frac{25}{30}$.70091	.29.09	1.4267	.98270	1.0176	1.4020	.28675	.71325	30	2	
4	31	. 0112	. 9888	.4263	8327	.0170	.4024	. 8695	. 1305	29	56	
8	32	• 0132	. 9867	4259	8384	-0164	.4028	. 8716	. 1284	28	52	
12	33	. 01:3	. 9847	-4254	8441	.0158	.4032	. 8736	. 1:64	27	48	
16	34	• 0174	. 9826	.4250	8499	-0152	.4026	. 8756	. 1243	26	44	
20	35	70194	.29805	1.4246	•98556	1.0146	1.4040	.28777	.71223	25	40	
24	36	• 0215	. 9785	4242	8613	.0141	.4044	. 8797	. 1203	24	36 32	
28 32	37 38	02360257	. 9764	.4238 .4233	• 8671 • 8728	.0135	.4048	8818	. 1182	23 22	28	
36	39	0257	9722	.4229	5786				. 1102	21	24	
40	40	70298	.29702	1.4225	.98843	1.0117	.4060	.28879	71121	20	20	
44	41	. 0319	. 9681	.4221	• 8901	.0111	.4065	. 8899	. 1100	19	16	
48	42	• 0339	. 9660	.4217	8958	.0105	.4069	. 8920	. 1080	18	12	
52	43	. 0360	. 9640	.4212	. 9016	.00 9	.4073	. 8940	. 1059	17	8	
56	41	0381	. 9619	.4208	• 9073	.0093	.4077	. 8961	. 1039	16	4	
59	45	.70401	.29598	1.4204	.99131	1.0088	1.4081	.28981	.71018	15	1	
8	46	0422	9578	.4200	9189	.0052	.4085	9002	. 0998	14 13	56 52	
12	47 48	• 0443 • 0463	. 9557 . 9536	.4156 .4192	• 9246 • 9304	.0076	.4089	. 9022 . 9043	. 0977	12	48	
16	49	. 0484	. 9516	.4188	9362	.0070	.4097	. 9063	. 0938	11	44	
20	50	.70505	.29495	1.4183	.99420	1.0058	1.410	.29084	.70916	10	40	
24	51	. 0525	. 9475	.4179	. 9478	.0052	.4105	. 9104	. 08:5	9	36	
28	52	. 0546	. 9454	.4175	. 95:16	.0047	.4109	. 9125	. 0875	8	32	
32	53	· 05t6	. 9433	.4171	• 9593	.0041	.4113	. 9145	. 0854	7	28	
36	54	. 0587	. 9413	.4167	9651	.0035	.4117	. 9166	. 0804	6	24	
40	55	.70608	.29392	1.4163	.99709	1.0029	1.4122	.29186	.70813	5	20	
41	56	. 0628	. 9372	.4159	9767	.0023	,4126	9207	07:3	4 2	16	
48 52	57 58	. 0649 . 0669	. 9351 . 9330	.4154 .4150	. 9826 . 9884	.0017	.4130 .41:'4	. 9228	0772	$\begin{bmatrix} 3 \\ 2 \end{bmatrix}$	12 8	
56	59	. 0690	. 9310	.4146	. 9942	.0012	.4138	. 9269	. 0752	$\tilde{1}$	4	
60	60	. 0711	9289	.4142	1.0000		.4142	9289	. 0711	0	0	
M. S.	M	Cosine.	Vrs. Sin.			l'angent.			Sine.	M	MS.	
	1349)			Natu					45°	3h	
L												

MECHANICS.

Mechanics is that branch of Natural Philosophy which treats of the action of force, motion, and power. Mechanics is divided into four parts, namely,

Statics the science of forces in equilibrium.

Dynamics, the science of forces in motion, it produces power or effect. Hydrostatics, the science of fluids in equilibrium

Liydrodynamics the science of fluids in motion, its causes, power or effects.

Lever. Momentum. Statics.

Lever is an inflexible bar, supported in one point called the Fulcrum, or, centre of motion. The length of a lever is measured from the fulcrum to where the ferce or resistance acts, (when the force acts at right angles to the lever) or, the length of a lever is measured from the fulcrum at right angles to the direction of the force.

W = Weight, and l = lever for $K \in F$ and L = lever for $K \in F$ See Fig. 139.

Momentum is the product of force or weight, multiplied by the length of

the lever it acts upon.

The products Wl and FL are called *Statics Momentums*; when these momentums are equal there will be no motion, and the weight W will balance the force F. When one momentum is greater than the other, there will be a motion, and the velocity of that motion is measured by the difference of the momentums.

Levers are of three distinct kinds, with reference to the relative positions of the Force F, Weight W, and Fulcrum C.

1st. Fulcrum C, is between the force F, and the weight W.

2d. Weight W, is between the fulcrum C, and the force F.

3d. Force F, is between the fulcrum C, and the weight W.

Example 1. Figure 139. The weight W = 68 pounds, the lever l = 3.86 feet

and L = 10 feet 6 inches.

Required the force F=?

Formula 1.
$$F = \frac{Wl}{L} = \frac{68 \times 3.86}{10.5} = 25$$
 pounds nearly.

a =distance between the force F and the weight W.

The formula 3, 4, 7, 8, 11, 12, are for finding the fulcrum C, when the force F, weight W, and the distance a, are given.

Example 2. Fig. 140. The force F = 360 pounds, W = 1870, and a = 8 feet. 4

Required the position of the fulcrum c?

Formula 7.
$$l = \frac{F \cdot a}{W - F} = \frac{360 \times 8 \cdot 333}{1870 - 360} = \frac{2999 \cdot 988}{1510} = 19.86$$
 feet.
 $L = 8 \cdot 333 + 19.86 = 28 \cdot 193$ feet, the answer.

Example 3. Fig. 144. The weight of the lever is Q=18 pounds. The centre of gravity is x=2.25 feet from the fulcrum. W=299 pounds, l=5.5 feet, and L = 11.95.

Required the force F = ? in pounds.

$$F = \frac{Wl - Qx}{L} = \frac{299 \times 5.5 - 18 \times 2.25}{11.95} = 134.25$$
 pounds.

Inclined Flane.

Example 4. Fig. 163. A load W = 3466 pounds, is to be drawn up an inclined plane, l = 638 feet long, and h = 86 feet high.

What force is required to keep the load on the inclined plane?

$$F = \frac{hW}{l} = \frac{86 \times 3466}{638} = 467.2$$
 pounds.

Example 4. Fig. 167. A Cylinder of east iron, weighing W=5245 pounds, is to be rolled up an inclined plane; the angles $v=18^{\circ}$ 20' and $v'=8^{\circ}$ 10'

What force is required to keep the cylinder on the plane?

$$F = W. \sin(v+v) = 5245 \times \sin(18^{\circ} 20' + 8^{\circ} 10') = 2340$$
 pounds.

Example 5. Fig. 168. An iron ball which weighs 398 pounds, is tied to an inclined plane with a rope; the angle of the rope and the inclined plane is $v' = 16^{\circ} 40'$, and $v = 14^{\circ} 30'$. What force is acting on the rope?

$$F = \frac{W \sin v}{\cos v'} = \frac{398 \times \sin .14^{\circ} 30'}{\cos .16^{\circ} 40'} = 104 \text{ pounds.}$$

Example 6. Fig. 153. What force F is required to raise a weight W = 8469pounds, by a double moveable pulley?

$$F = \frac{1}{4}W = \frac{1}{4} \times 8469 = 2117.25$$
 pounds.

Example 7. Fig. 156. How much weight can a force F = 269 pounds lift by three compound moveable pulleys?

$$W = 2^u F = 2^s \times 269 = 2152$$
 pounds, the answer.

Screw.

Example 8. Fig. 172. What force is required to lift a weight W = 16785 pounds. by a screw, with a pitch P = 0.125 feet, the lever being r = 5 feet. 4 inches?

$$F = \frac{WP}{2\pi r} = \frac{16785 \times 0.125}{2 \times 3.14 \times 5.333} = 62.62$$
 pounds, the answer.

Including friction the force F will be

$$F = \frac{W(P + f d \pi)}{2 \pi r}.$$

Find the friction f on page 267. d diameter of the screw in fect.

Wedge.

Example 9. Fig. 169. The head of the wedge $\alpha=3$ inches, and length $l=16\frac{1}{2}$ inches; the resistance to be separated is R=4846 pounds. Required the force F=? (Friction omitted.)

$$F = \frac{4846 \times 3}{16.5} = 881$$
 pounds.

Including friction the force F will be.

146

$$F = R \left[\frac{a}{l} + f \left(2 + \frac{a^2}{l s} \right) \right]$$

in which the friction f is to be found on page 267.

Catenaria.

Example 10. An iron chain 256 feet long, weighing 1560 pounds, is to be suspended between two points in the same horizontal line, but 196 feet apart.

How deep will the chain hang under the line of suspension, and with what

force will the chain act at the points of suspension?

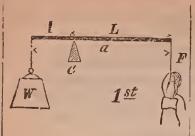
Figure and Formula 161, we have given, $W = \frac{1}{2} \times 1500 = 780$ pounds, $l = \frac{1}{4} \times 256 = 128$ feet, and $a = \frac{1}{2} \times 196 = 98$ feet.

 $h = 0.6525\sqrt{128^2 - 98^2} = 53.73$ feet, the required depth under the horizontal line.

$$\cot v = \frac{2 \times 53.73}{98} = 1.096$$
, or $v = 44^{\circ}$ 44', and $2v = 89^{\circ}$ 28'.

The required force will be,

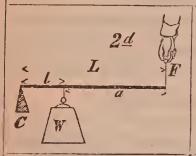
$$F = \frac{780 \times \sin.44^{\circ} 44'}{\sin.89^{\circ} 28'} = 549 \text{ pounds.}$$



139.
$$F: W = l: L, \quad FL = Wl,$$

$$W = rac{W \ l}{L}$$
 , $W = rac{FL}{l}$.

$$l = \frac{F a}{W + F}, \qquad L = \frac{W a}{W + F'} \qquad 3, 4,$$



140.
$$F: W = l: L, FL - Wl,$$

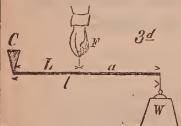
$$F = \frac{W l}{L}, \qquad W = \frac{F L}{l}.$$

$$W = \frac{F'L}{7}$$

1, 2,

$$L = \frac{Wa}{W - F},$$

$$L = \frac{Wa}{W - F}, \qquad l = \frac{Fa}{W - F} \quad 7, 8,$$



141.
$$F: W = l: L, \quad FL = W l,$$

$$F = \frac{W \, l}{L} \,, \qquad W = \frac{F \, L}{I} \,,$$

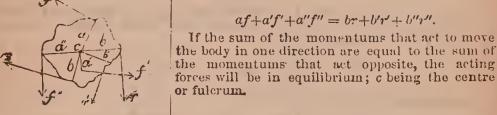
$$W = \frac{FL}{r}$$

$$L = \frac{W a}{F - W},$$

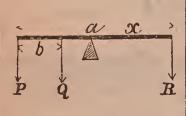
$$L = \frac{Wa}{F - W}, \qquad l = \frac{Fa}{F - W}, \quad 11, 12.$$

142.

$$af + a'f' + a''f'' = br + b'r' + b''r''.$$



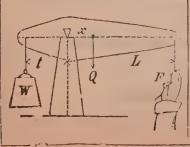
143.



To find the fulcrum c when three forces act on one lever

$$R x = Q(a-b-x)+P(a-x),$$

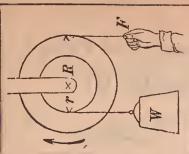
$$x = \frac{Qa+Pa-Qb}{R+Q+P}.$$



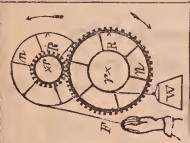
144.

Q = weight of the lever. x = distance from the centre of gravity of the lever to the fulcrum. Balance the lever over a sharp edge, and the centre of gravity is found.

$$F = \frac{Wl - Qx}{L}, \quad W = \frac{FL + Qx}{l}.$$



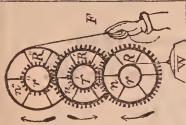
145.
$$F:W=r:R$$
, $FR=Wr$, $F=\frac{Wr}{R}$, $R=\frac{Wr}{F}$, $W=\frac{RF}{r}$, $r=\frac{RF}{W}$.



146

$$F = \frac{W r r'}{R R'}, \quad W = \frac{F R R'}{r r'},$$

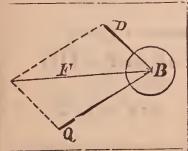
n = number of revolutions of the wheels, $n: n' = r': R, \quad v: v' = rr': RR',$ $v = \text{velocity of } W, \quad v' = \text{velocity of } F.$



147.
$$F = \frac{W r r' r''}{R R' R''}, \quad W = \frac{F R R' R''}{r r' r''},$$

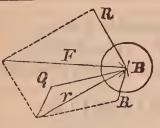
n: n'' = r'r'' : R R', v: v' = rr'r'' : R R'R''

r r'r'' &c. = radii of the pinions. R R'R''&c. = radii of the wheels.



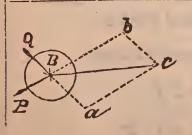
148.

Let P and Q represent the magnitudes and directions of two forces which act to move the body B. By completing the parallelogram, there will be obtained a diagonal force F, whose magnitude and direction is equal to the sum P and Q. F is called the resultant of P and Q.



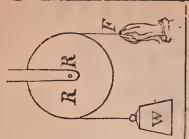
149.

If three or more forces act in different directions to move a body B, find the resultant of any two of them, and consider it as a single force. Between this and the next force find a second resultant, thus: P, Q, and R are magnitudes and directions of the forces. P+Q=r, r+R=F=P+Q+R, or F is the magnitude and direction of the three forces, P, Q, and R.



150.

A force Q acting (alone) on the body B, can move it to a in a unit of time, another force P is able to move it to b in the same time; now if the two forces act at the same time, they will move the body to c. c is the resultant of a and b.

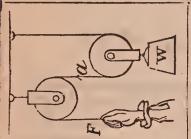


151.

PULLEYS .- A single fixed Pulley.

$$F: W = R: R, \text{ or } F = W,$$

$$v = v'$$
.



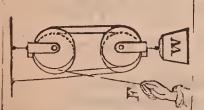
152.

A single moveable Pulley.

$$F: W = R: 2R$$
, or $F = \frac{1}{2}W$,

If the force F being applied at a and act upwards, the result will be the same.

$$v'=2v.$$

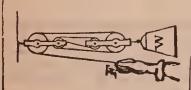


153.

A double moveable Pulley.

$$F: W = R: 4R, \text{ or } F = \frac{1}{4}W,$$

$$v'=4v$$
.



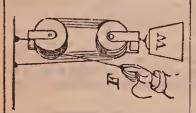
154.

A double moveable Pulley.

$$F: W = R: 4R, \text{ or } F = \frac{1}{4}W,$$

$$F=\frac{W}{2u},$$

$$v:v'=1:2u.$$



155.

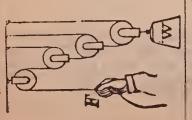
Quadruple moveable Pulley.

$$F = \frac{1}{8}W$$
. $F : W = R : 8R$.

Let u = any number of moveable pulleys, then

$$F=\frac{W}{2u}$$

$$v:v'=1:2u.$$



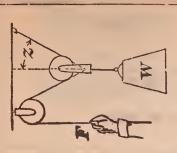
156.

Compound Pulleys.

u = number of moveable Pulleys.

$$F=\frac{w}{2^{u}}, \quad W=2^{u}F,$$

$$v:v'=1:2^{u}.$$

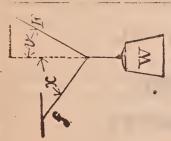


157.

An oblique fixed Pulley.

$$F: W = \text{sec.z}: 2,$$

$$W = \frac{2F}{\sec z'} \qquad F = \frac{W \sec z}{2}$$

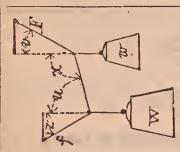


158.

$$W: F = \sin(x+v): \sin x,$$

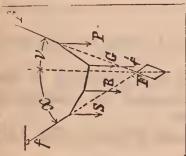
$$F = \frac{W \sin x}{\sin (x+v)}, \quad f = \frac{W \sin x}{\sin (x+v)},$$

$$W: f = \sin(x+v) : \sin v.$$



159. $F = \frac{w \sin x}{\sin (x+v)},$

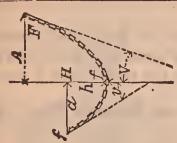
$$f = \frac{W \sin u}{\sin (u+z)}.$$



160.

$$W = P + Q + R + S, F = F', f = f',$$

$$F = \frac{W \sin x}{\sin (x+v)}, \quad f = \frac{W \sin x}{\sin (x+v)}.$$

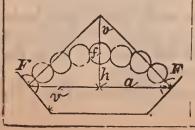


161.

$$l = \frac{1}{3}(2a + \sqrt{a^2 + 9h^2}).$$

l = length, and W = weight of half the chain, ff',

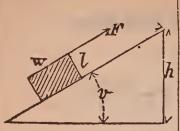
$$\cot v = \frac{2h}{a}, F = \frac{W. \sin V}{\sin 2V}, f = W \tan v.$$



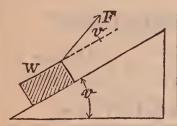
$$F = \frac{W. \sin v}{\sin 2v}, \quad f = W \tan v,$$

$$\cot v = \frac{2h}{a}$$
.

W =weight of half the number of balls.



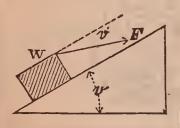
163.	$F = \frac{Wh}{l} = W\sin v,$
	$W = \frac{F l}{h} = \frac{F}{\sin \cdot v},$
	$w = \frac{Wl}{h} = W \cos v$.



164.
$$F = W \sin(v+v'),$$

$$W = \frac{F}{\sin(v+v')},$$

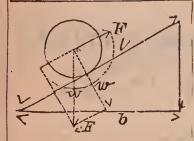
$$W = W \cos(v+v').$$



165.
$$F = \frac{W \sin v}{\cos v},$$

$$W = \frac{F \cos v'}{\sin v},$$

$$w = W (\cos v + \sin v \cdot \tan v').$$

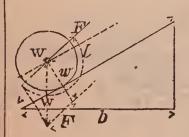


166.

To solve an Inclined Plane by diagrams.

 F^{i} = magnitude and direction of the force, which is obtained by completing the parallelogram.

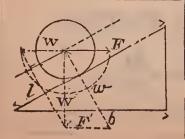
By calculation see Formula, Fig. 163.



167.

W = weight of the body, and direction of the force of gravity; to be drawn at right-angles to the base b, and F parallel to F.

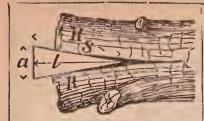
By calculation see Formula, Fig. 164.



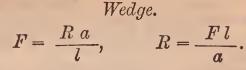
168.

w = the force with which the body presses against the plane, to be drawn at right-angles to the plane l; then the parallelogram is completed.

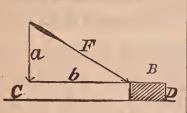
By calculation see Formula, Fig. 165.



169.



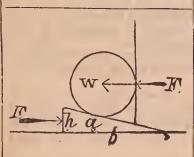
F =force acquired to drive the wedge.



170.

Let the line F represent the magnitude and direction of a force acting to move the body B on the line CD; then the line a represents a part of F which presses the body B against CD, and the line b represents the magnitude of the force which actually moves the body B.

$$b = \sqrt{F^2 - a^2}, \quad b = F \cos v.$$

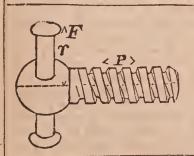


71.

 $F: W = h: b = \sin v: \cos v = \tan v.$

$$F = \frac{Wh}{b} = W \tan v. \quad F' = F.$$

$$W = \frac{Fb}{h} = \frac{F}{\tan v} = F \cot v.$$



172.

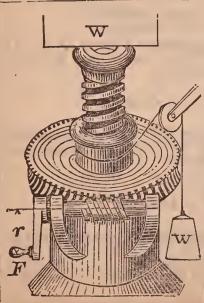
Force by a Screw.

P = Pitch of the screw,

r = radius on which the force Facts.

$$F:W=P:2\pi r.$$

$$F = \frac{WP}{2\pi r}, \qquad W = \frac{F2\pi r}{P}.$$



173. Force by Compound Screws.

P = Pitch of the large screw,

p =Pitch of the endless screw.

R= radius of spur-wheel for the endless crew.

$$W: F = 4\pi^2 R r : P p.$$

$$F = \frac{W P r}{4\pi^2 R r}, \qquad W = \frac{F4^2 \pi R r}{P p}.$$

On the spur-wheel is a cylinder by which the weight W' is wound up, the formula will be, r' = radius of the cylinder, and

$$F: W' = p \ r': 2\pi R r.$$

$$F = \frac{W'}{2\pi} \frac{p}{R} \frac{r'}{r}, \quad W = \frac{F2\pi}{p} \frac{R}{r'}$$

Dynamics.

Quantity is that which can be increased and diminished by homogeneous parts. Quantity is of two kinds,—geometrical and physical.

Element is that which cannot be dissolved into two or more different

Function is the product of two or more different elements.

Force, motion, and time are simple physical elements; and

Power, space, and work are functions or products of those elements.

Force is a mutual tendency of bodies to attract or repel each other. Its physical constitution is not yet known. We only know its action on matter, which is recognized as pressure and measured by weight.

Force is the first element of power and work. It is here denoted by the letter

F in pounds avoirdupois.

Motion is a continuous change of position, recognized as velocity. It is the second element of power and work, and here denoted by V in ft. per second. Time implies a continuous action recognized as duration. It is the third element of work, and here denoted by T in seconds.

Power is a function of the two first elements, force F and velocity V, or the product obtained by multiplying together the force F and velocity V, denoted P = FV. Power P is expressed in footpounds, and called dynamic effect, of which there are 550 in a horse-power; or, if the velocity is measured in feet per minute, there will be 33,000 footpounds in a horse-power.

Space is a function of the second and third elements, velocity V and time T, denoted by S = VT, which means that the space S is the product of the

velocity V and time T, expressed in linear feet.

Work is a function of the three elements force F, velocity V, and time T, denoted by K = F V T, which means that the work K is the product obtained

by multiplying together the three elements F, V, and T. Work may also be denoted by K = FS, where it appears as if the work was independent of time; but the time is included in the space S = VT.

Work is also denoted by K = PT, or the product of the power P and the time T, where it appears as if work was independent of force and velocity, which latter are included in the power P. Either of the three cases expresses the work K in units of one pound lifted one foot called featneyed. the work K in units of one pound lifted one foot, called footpounds. For large quantities of work, this unit is too small. The work done by one man in a day may amount to some two millions of footpounds. It is therefore proposed to adopt an additional unit for work, namely, the work a horse can perform in the time of one hour, which is equivalent to that of eleven men working one hour, or of one man working eleven hours, to be called a Workmanday, and denoted by the letter k. This unit is to express great amounts of work, such as the building of a house, bridge, canal, ship, large fly-wheels, and to express the magnitude of steam-boiler and gunpowder explosions; also the capacity of heavy ordnance, to be noted in workmandays.

One horse-power = 550 effects = 11 men's power. One man's power = 50 effects = 0.0909 horse-power.

Example 1.—What force F = ? is required to generate a power of H = 54 horses, with a velocity V = 15 feet per second? Find the formula for force, which contains the given quantities H and V, which is,

$$F = \frac{550 \ H}{V} = \frac{550 \times 54}{15} = 1980$$
 pounds, the answer.

Example 2.—The pull of a belt over a belt-pulley is F = 350 pounds, the radius of the pulley is r = 1.5 feet, making n = 52 revolutions per minute. Required the horse-power H = ? transmitted by the belt.

See formulas for circular motion.

$$H = \frac{F \ r \ n}{5250} = \frac{350 \times 1.5 \times 52}{5250} = 5.2 \text{ horses.}$$

Example 3.—How many workmandays k=? are required to raise a load of F = 72968000 pounds, a height of S = 25 feet.

$$k = \frac{F~S}{1980000} = \frac{72968000~\times~25}{1980000} = 911.212$$
 workmandays, the answer.

Dynamical Formulas for Uniform Motion.

Space in Feet passed through in the Time T.

$$S = VT$$
. $S = \frac{PT}{F}$. $S = \frac{550 \ TH}{F}$. $S = \frac{K}{F}$.

Force or Pressure in Pounds.

$$F = \frac{P}{V}$$
. $F = \frac{550 \ H}{V}$. $F = \frac{K}{S}$. $F = \frac{1980000k}{S}$

Velocity in Feet per Second.

$$V = \frac{S}{T}$$
. $V = \frac{P}{F}$. $V = \frac{550 \ H}{F}$. $V = \frac{K}{F \ T}$.

Time of Duration in Seconds.

$$T = \frac{S}{V}$$
. $T = \frac{SF}{P}$. $T = \frac{FS}{550 H}$. $T = \frac{K}{FV}$.

Power in Effects.

$$P = F V$$
. $P = \frac{F S}{T}$. $P = 550 H$. $P = \frac{K}{T}$.

Horse-power.

$$H = \frac{P}{550}$$
. $H = \frac{F \ V}{550}$. $H = \frac{F \ S}{550 \ T}$. $H = \frac{K}{550 \ T}$.

Work in Footpounds.

$$K = F \ V \ T$$
. $K = P \ T$. $K = F \ S$. $K = 550 \ H \ T$.

Workmandays.

$$k = \frac{F \ V \ T}{1980000}$$
. $k = \frac{F \ S}{1980000}$. $k = \frac{P \ T}{1980000}$. $k = \frac{H \ T}{3600}$.

Circular Motion.

$$V = \frac{2 \pi r n}{60}$$
. $n = \frac{60 V}{2 \pi r}$. $r = \frac{60 V}{2 \pi n}$. $S = 2 \pi r N$.

$$P = \frac{F2 \pi r n}{60}$$
. $H = \frac{F2 \pi r n}{550 \times 60}$. $H = \frac{Fr n}{5250}$. $K = F2 \pi r N$.

$$F = \frac{5250 \, H}{r \, n}$$
. $T = \frac{60 \, N}{n}$. $n = \frac{5250 \, H}{F \, r}$. $N = \frac{K}{F \, 2 \, \pi \, r}$.

n = revolutions per minute. | r = radius of the circle in feet. N = total no. of revolutions. $| \pi = 3.14159265.$

OBSERVED RESULTS OF POWER.

	Work-				
Description of Works.	hrs. per day.	Force.	Veloc'y	Effects.	Horses.
A man can raise a weight by a single fixed				40	0.070
pulley,	8	50 20	$0.8 \\ 2.5$	40 50	0.072
A man on a tread-wheel (horizontal),	8	144	0.5	72	0.130
A man in a tread-wheel (axis 24° from ver-					0.10
tical),	8	30	2.3	69	0.125
A man draws or pushes in a horizontal direction,	8	30	2	60	0.109
A man pulls up or down,	8	12	3.7	44.4	0.080
A man can bear on his back,	7 8	95 106	$\frac{2.5}{3}$	237.5 318	0.577
A horse in a horse-mill, walking moderately, A horse in a horse-mill, running fast,	5	72	9	648	0.165
An ox in a horse-mill, walking moderately,	8	154	2	308	0.558
A mule	8 8	71 33	3 2.65	213 87.4	0.30S 0.160
An ass " " "	0	99	2,00	01.4	0.100
On bad Foot-roads, like those in					
Peru.			٥.*		
A man can bear,	10 10	50 100	3.5 3.5	175 350	
Donkey can bear,	10	200	3.5	700	
Donkey can bear,	10	400	5	2000	
Flour Mills,					
For every 100 pounds of fine flour ground per	hour, re	quire,		550	1.000
One pair of mill-stones of 4 feet diameter, ma per minute, can grind 5 bushels of wheat to fi				2400	4.36
One pair of mill-stones of 4 feet diameter, ma	aking 12	20 revol	utions	2400	4.50
per minute, can grind 5 bushels of rye to coar				1 600	2.91
Saw Mills, alternati	ve.				
For every 20 square feet sawed per hour,	in dry o	ak, the	re re-		
quires,		•	• •	550	1.000
Dry pine, so square feet per nour,	•	•	•	550	1.000
Circular Saw.				(
A saw 2.5 feet in diameter, and making			s per		
minute, will saw 40 square feet in oak per hou			• •	550	1.000
In dry spruce, 70 square feet per hour, .	•	•	•	550	1.000
Threshing Machine	е.				
Velocity of the feed-rollers at the circums		0.55 fee	et per		
second. Diameter of threshing-cylinder 3.5 fe	eet and	$4\frac{1}{2}$ feet	long,		
making 300 revolutions per minute, can the bushels of oats, and from 25 to 35 bushels of v	resh fi	om 30	to 40	9000	4.000
One man with a flail can thresh half a bush				2200 7 0	4.000 0.127
· ·		7	,,		
Rolling Mills.					
Bar iron-mills. Two pair of rough rollers,					
rollers, six puddle furnaces, two welding furn of bar iron per 24 hours, rollers making 70 rev				1016	100
require,				29000	80
Plate-mill requires about five horses per s	square f	oot of	plates		
rolled. Largest size plate rollers should not tions per minute.	пике о	ver su r	evoru-		1

DREDGING MACHINES.

Letters denote.

T = tons of materials excavated

and raised per hour.

h = hight in feet in which the materials are raised above the bottom of the excavated channel.

k = 0.1 for hard clay with gravel.

k = 0.07 for hard pure clay.

k = 0.05 for common clay or sand. k = 0.04 for soft clay or loose sand.

k = 0.03 for very loose materials. H = horse power required for ex-cavating and raising the ma-

terials. F = force in pounds required to feed the Dredge ahead.

v = velocity of the buckets in feet

per second.

$$H = T \left(\frac{h}{700} + k \right) - \bullet \bullet 1$$

$$T = \frac{700 \ H}{h + 700 \ k} - 2$$

$$F = \frac{550 \ Tk}{v} \qquad - \qquad - \qquad 4$$

$$k = \frac{H}{T} + \frac{h}{700} \quad - \quad - \quad - \quad 5$$

Example 1. What power is required to excavate T=160 tons of hard pure clay per hour, and raise it up h=25 feet above the bottom of the channel? For hard clay k=0.07.

$$H = 160 \left(\frac{25}{700} + 0.07 \right) = 16.9$$
, or 17 horses.

Example 2. What force F=? is required to feed the Dredge ahead for the above example when the buckets move v=1 foot per second.

$$F = \frac{550 \times 16.9}{1} = 9295$$
 pounds.

LEATHER BELTS.

Letters denote.

b = breadth of leather belt in inches, H = horse power transmitted by the belt. v = velocity of the belt in feet per second.

d = diameter in inches n = revolutions per mintute of the smallest belt pulley. F = force in pounds transmitted by the belt. $S = \text{safe working strength in pounds per inch of width of belt, which, for oak-tanned leather <math>\frac{1}{4}$ inch thick, cemented and riveted joint, can be taken at 100 pounds, and less in proportion for weaker belts.

Example. A leather belt is to transmit H=75 horse power over a pulley d=36 inches in diameter, making n=80 revolutions per minute, angle of contact $a=170^{\circ}$, and the safe working strength S=100 pounds per inch of width. Required the width of the belt.

Formula 1. Width
$$b = \frac{30,000,000 \times 75}{36 \times 80 \times 170 \times 100} = 46$$
 inches, nearly.

FRICTION.

THE resistance occasioned by Friction is independent of the velocity of motion; but the re-effect of friction is proportional to the velocity. Friction is independent of the extent of surface in contact when the pressure remains the same, but proportional to the pressure. This law was established from experiments by Arthur Morin in the years 1831-32 and 1833, from which a summary is contained in the accompanying Table.

Letters denote.

a = Fibres of the woods are parallel to themselves, and to the direction of motion.

b = Fibres at right-angles to fibres.

c = Fibres vertical on the fibres which are parallel to the motion.

d = Fibres parallel to themselves, but at right-angles to the motion, length by length.

e = Fibres vertical, end to end.

Example. A vessel of 800 tons is to be hauled up an inclined plane, which inclines 9° 40′ from the horizon; the plane is of oak, and greased with tallow. What power is required to haul her up?

The coefficient for oak on oak with continued motion is f = 0.097, say 0.1,

then,

$$800 \times \sin.9^{\circ} 40' = 800 \times 0.16791 = 124.328 \text{ tons},$$

the force required if there were no friction, and

$$800 \times \cos.9^{\circ} 40' \times 0.1 = 800 \times 0.9858 \times 0.1 = 78.864 \text{ tons}$$

the force required for the friction only, and

134·328 78·864

213.192 tons, the force required to haul her up.

The effect lost by friction in axle and bearings is expressed simply by the formula

$$P = \frac{\pi \, d \, W \, n \, f}{12.60} = \frac{W \, d \, n \, f}{230},$$

in which W= the weight of pressure in the bearing, d= diameter on which the friction acts in inches, n= number of revolutions per minute, and f= coefficient of friction from the Table. In common machinery kept in good order the coefficient of friction can be assumed to f=0.065, then

$$P = \frac{Wdn}{3530}$$
, $H = \frac{Wdn}{1941500}$

Example. The pressure on a steam-piston is 20000 pounds, and makes n = 40 double strokes per minute. Required the friction in the shaft of d = 8 inches?

$$H = \frac{20000 \times 8 \times 40}{1941500} = 3.3$$
 horses, the loss by friction.

Friction in Guides.

W= pressure on the steam piston in pounds.

S = stroke of piston in feet.

l = length of connecting rod in feet.

H= horse power of the friction.

$$H = \frac{W \, S \, n}{350000 \, \sqrt{5 \, l^2 - S^2}}$$

Example. The pressure on a steam piston being W = 30,000 pounds, stroke S = 4 feet, length of connecting rod l = 7 feet, and making 50 revolutions per minute. Required the horse power of the friction H = ?

$$H = \frac{30000 \times 4 \times 50}{350000 \sqrt{5 \times 7^{2} - 4^{2}}} = 1.13$$
 horses.

TABLE OF FRICTION FOR PLANE SURFACES IN CONTACT.

Kind of Materials in contact. Lubricated with. Coefficient in Motion. Starting. 0ak on Oak,			Inbricated	Coeffic	ient in
Oak on Oak, a 0 0.478 0.625 """ """ 1ard 0.097 0.160 """ """ 0 0.324 0.540 """ """ 0 0.324 0.540 """ """ 1allow 0.083 0.254 """ """ 0 0.336 0.254 """ """ 0 0.336 0.254 """ """ 0 0.336 0.251 """ """ 0 0.400 0.570 """ """ 0 0.400 0.570 """ """ 1allow 0.078 0.108 Wroughtiron on Oak, """ """ tallow 0.078 0.108 """" """" """ tallow 0.078 0.108 Wroughtiron, together, """" """" """" """ """ """ """ """ """ """ """ "	Kind of Materials in contact.				
" " tallow 0.097 0.160 " " " 0	Oak on Oak.	10			
" " " " " " " " " " " " " " " " " " "	44 44				
" " " " " " " " " " " " " " " " " " "	" "	"			
" " " " " " " " " " " " " " " " " " "	" "	ő			
## ## ## ## ## ## ## ## ## ## ## ## ##	" "	19			
" " " " " " " " " " " " " " " " " " "		1 1	tallow	0.083	0.254
" " " " " " " " " " " " " " " " " " "			water,	0.25	
Cast-iron on Oak, """""""""""""""""""""""""""""""""""			Ó	0.336	
Cast-iron on Oak, """""""""""""""""""""""""""""""""""		0	0	0.192	0.271
" " " " " " " " " " " " " " " " " " "		(-	0	****	
""" tallow 0.078 0.108 Wrought-iron on Oak, """ tallow 0.078 """ tallow 0.078 Wrought iron, together, a 0 0.138 0.137 """ """ unctuous 0.177 """ """ tallow 0.082 """ """ tallow 0.070 0.115 """ """ 0 01ye oil 0.060 0.104 """ """ unctuous 0.18 0.118 """ """ tallow 0.003 0.10 """ """ tallow 0.066 0.100 """ """ """ tallow 0.0197 """ <t< td=""><td></td><td>a</td><td>0</td><td>0 200</td><td>0.570</td></t<>		a	0	0 200	0.570
Wrought-iron on Oak, """ tallow 0 0.252 """ tallow 0.0138 0.137 """ tallow 0.082 """ tallow 0.096 0.118 <td></td> <td>99</td> <td></td> <td></td> <td></td>		99			
Wrought iron, together. a o 0-138 0-137 """"""""""""""""""""""""""""""""""""		22	tallow		0.108
Wrought iron, together, a o 0-138 0-137 """"""""""""""""""""""""""""""""""""	Wrought-iron on Oak, • •	22			• • • •
"" "" "" "" "" "" "" "" "" "" "" "" ""	***				• • • •
## ## ## ## ## ## ## ## ## ## ## ## ##	Wrought iron, together •		_		0.137
"" "" olive oil 0.070 0.115 Wrought on cast-iron, "" "" unctuous 0.18 0.118 "" "" "" unctuous 0.18 0.118 0.118 "" "" "" tallow 0.103 0.10 0.10 0.10 0.10 0.10 0.314	" "	a			• • • •
Wrought on cast-iron, a o 0·194 0·103 0·100 0·100 0·100 0·100 0·100 0·100 0·100 0·100 0·100 0·100 0·100 0·100 0·100 0·100 0·100 0·100 0·100 0·100 0·100 0·100 0·100 0·100 0·100 0·100 0·100 0·100 0·100 0·100 0·100 0·100 0·100 0·100 0·100 0·100 0·100 0·100 0·100 0·100 0·100 0·100 0·100 0·100 0·100 0·100 0·100 0·100 0·100 0·100 0·100 0·100 0·100 0·100 0·100 0·100 0·100 0·100 0·100 0·100 0·100 0·100 0·100 0·100 0·100				* * * * * * * * * * * * * * * * * * * *	
"" "" "" "" "" "" "" "" "" "" "" "" ""					
""" """ tallow 0·103 0·100 Cast-iron on cast-iron, """ """ """ 0°314 0°316	"		_		
Cast-iron on cast-iron, """""""""""""""""""""""""""""""""""	"	1			
Cast-iron on cast-iron, """" soap "" tallow 0·100 0·1	" "	''			
""" """ soap 0·197 """ """ tallow 0·100 0·100 """ """ """ 0 0ive oil 0·064 """ """ """ unctuous 0·160 """ """ tallow 0·103 """ """ olive oil, 0·075 """ """ unctuous 0·132 """ """ unctuous 0·132 """ """ """ olive oil 0·075 """ """ """ unctuous 0·134 """ """ """ unctuous 0·134 """ """ """ """ Brass on brass, """ """ """ """ """ """ """ """		1 1			
""" """ tallow 0·100 0·100 Wrought-iron on brass, """	"	"			
"Wrought-iron on brass," """ olive oil o'.064 """ """ unctuous o'.160 """ "" tallow o'.075 """ "" olive oil, o'.078 """ olive oil, o'.078 """ olive oil, o'.075 """ olive oil, o'.075 """ olive oil, o'.078 <	"	1 1			
Wrought-iron on brass, a o 0.172 """ """ unctuous 0.160 """ """ tallow 0.103 """ """ olive oil, 0.078 Cast-iron on brass, a o 0.147 """ """ unctuous 0.132 """ """ tallow 0.103 """ """ lard 0.075 """ """ olive oil 0.078 Brass on brass, a o 0.201 """ """ unctuous 0.134 """ """ """ """ Steel on cast-iron, """ """ """ """ """ """ """ """ """ """ """ """ """ """ """ """ """ """ """ """ """ """ """ """ """ """ """ """ """ """ """ """ <td>" "</td> <td>1</td> <td></td> <td></td> <td>0 100</td>	" "	1			0 100
"" "" "" "" "" "" "" "" "" "" "" "" ""	Wrought-iron on brass .				
" " " " " " " " " " " " " " " " " " "	- // //	99	- 1		
" " " lard 0.075 " " " olive oil, 0.078 " " " unctuous 0.132 " " " tallow 0.103 " " " olive oil 0.075 " " " olive oil 0.078 " " " unctuous 0.134 " " unctuous 0.134 " " unctuous 0.135 " " unctuous 0.105 " " " unctuous 0.105 " " unctuous 0.105 " " " " unctuous 0.105 " " " " " " " " " " " " " " " " " " "	"	1 1			
Cast-iron on brass, """ """ """ """ """ """ """ """ """	"				
" " unctuous 0·132	"	1			
" " unctuous 0·132	Cast-iron on brass, • •	a		0.147	
" " Callow O·103 O·075 O·075 Oive oil O·078 O·07	" "	9,	unctuous	0.132	
" " olive oil 0.078		,,,	tallow	0.103	
Brass on brass, """ """ """ """ """ """ """		"	lard	0.075	
" " " " " " " " " " " " " " " " " " "	" "	22	olive oil		
" " " " " " " " " " " " " " " " " " "		a			
Steel on cast-iron,		22			
" " tallow 0.105 lard 0.081		97	olive oil		
" " lard 0.081		22	-		****
, lard 0.081	• • •	22			• • • •
• a olive oil 0.079					
	•	a	01146 011	0.079	

FRICTION OF AXLES IN MOTION.

	1	Oil, Tallow, or	Hog's Lard.
Designation of surface in contact.	Dry or slightly greasy, or wet.	Supplied in the ordinary manner.	The grease continually running.
Brass on Brass,	• • • • •	0.079	
" on cast-iron, •	• • • • •	0.072	0.049
Iron on Brass,	0.251	0.075	0.054
" on cast-iron,		0.075	0.054
Cast-iron on cast-iron, •	0.137	0.075	0.054
" on Brass,	0.194	0.075	0.054
Iron on lignum-vitæ, •	0.188	0.125	
Cast-iron on "	0.185	0.100	0.092
Lignum-vitæ on cast-iron,		0.116	0.170

STRENGTH OF MATERIALS.

Table I., shows the weight a column can bear with safety; when the weight presses through the length of the column. The tabular number is the weight in pounds or tons per square inch on the transverse section of a column a length less than 12 times its smallest thickness.

Table I.
RESISTANCE FOR COMPRESSION.

174.

Kind of Materials.	Pounds.	Tons.	1 2
Oak, of good quality,	432	0.1885	/ 707 \
Oak, common, · · · ·	280	0.125	
Spruce, red (Sapin rouge),	540	0:241	4
" white, (Sapin blanc),	140	0.6256	
Iron, wrought,	14400	6.43	
Iron, cast, • • • • • •	28750	12.85	
Basalt,	2875	1.285	
Granite, hard,	1000	0.446	
" common, • • • •	575	0.256	h
Marble, hard,	1435	0.640	
" common,	431	0.192	
Sandstone, hard, • • • •	1295	0.577	
" loose, - · · ·	5.6	0.0025	
Brick, good quality,	175	0.078	
" common,	58	0.0259	
Lime-stone, of hardest kind,	720	0.321	
common,	432	0.193	
Plaster-Paris,	86	0.0384	
Mortar, good quality, and 18 months old,	58	0.0259	- W
Do. common,	36	0.016	

When the length or height of the column is more than 12 times its smallest thickness, divide the tabular weight by the corresponding number in this Table.

Length×thickness	12	18	24	30	36	42	48	54	60
Divide by	1.2	1.6	2	2.8	4 .	5	6	8	12

Example. A building which is to weigh 2000 tons is to be supported by piles of Sapin rouge Spruce 18 feet in length, and 12 inches diameter. How many piles are required to support the building?

$$\frac{12^2 \times 0.785 \times 0.241}{1.6} = 17 \text{ tons, the weight which each pile can bear,}$$

and

$$\frac{2000}{17}$$
 = 118 piles.

Professor Hodgkinson's Formulæ for Crushing Strength of Cast Iron Pillars.

The ends of the pillars should be perfectly flat and square, and the load to bear even on the whole surface.

T=crushing weight in tons.

D=outside and d inside diameters in inches.

l = length or height of pillar in feet.

$$T=46.65 \left(\frac{D^{3.55}-d^{3.66}}{l^{1.7}}\right)$$

Table showing the Weight in tons which Cast Iron Pillars or Tubes can bear with Safety,

	24	tons, 2 195 195 195 195 195 195 491 491 491 301 263 232 206 184 184 184 196 1138 126	
	07	tons 1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1.	
	138	73 13 13 13 147 677 677 74 240 346 346 328 328 328 3475 497 497	
bore,	17	88 86 87 88 88 17 18 18 18 18 18 18 18 18 18 18 17 17 18 18 17 17 18 17 18 18 19	
the b	16	78.775.23.9.00.08.00.00.00.00.00.00.00.00.00.00.00.	
to	15	tons, 11161 11161 125867 125867 12593 12593 12593 125557 125557 125557 125557 125557 125557 125553 12555	
weight due	14	tons, 296 910 910 1919 1919 1919 1919 1919 1919 1919 1919 1919 1919 1919	
Weig	13	tons, 697 697 2260 2148 1470 1078 8296 6611 6412 5412 2553 22553 22553 1836 1665 1665	
the	12	tons, 169. 523 262 161 110 8082 6219 4956 4057 3391 2487 2487 2171 1914 1702 1526 1339 1139	
subtract	11	tons, 124 38 162 1177 1177 8056 5909 2479 2966 2479 1818 1818 1587 1400 1244 11115 11115 1006 913 832	
gns	10	ons, 85 7714 36 354. 716 192 225 571 104 760 760 760 760 760 760 760 760 760 760	
Labes	6	6 8 85.1 2 932.2 1 2032.2 1 1760.2 3 1760.2 3 1760.2 3 1760.2 3 1760.2 3 1760.2 3 1771.1 1 883.1	
For T	00	tons, 3995 6101 6101 63741 2560 1878 11444 1151 1444 1151 1444 1151 1444 1151 1444 1151 1444 1151 1444 1151 1444 1151 1444 1151 1445 1151 1445 1151 1445 1151 1445 1151 1445 1151 1451 1	
	7	tons, 7500 3744 2313 1583, 1161 1161 1161 894 712 583. 4414 414 357 250 250 218 198 1174 1163	
Inches.	9	tous, 14 4315 2166 1328 908 666 513 408 335 280 280 280 179 179 179 113 1103	
ın	G	tons, 7272 2238 1123 689 471 346 266 212 174 1145 1174 1174 1174 1174 1174 1174	
Diameters	4	tons, 3256 1000 500 500 500 1155 1155 119 78 65 65 65 82 84 22 22 22 22 20 20 33 33 33 33 33 33 33 34 35 36 36 36 36 36 36 36 36 36 36 36 36 36	
Dian	က	tons, 11156 355 178 178 110 75 20 117 115 115 110 90.4 88.5 7.1	
	C)	tons, 218 82.5 411.5 411.5 17.4 112.8 6.4 6.4 6.4 6.3 7.8 8.9 8.3 2.7 2.7 2.7 1.8 1.8	
	T .	22 6.8 6.8 3.5 2.1 1.4 1.0 0.53 0.53 0.32 0.28 0.20 0.20 0.14 0.18	
	H		

These values are about half of that by Prof. Hodgkinson's formula. The points after the numbers mean ciphers.

Table II.

COHESIVE STRENGTH PER SQ. INCH OF CROSS-SECTION.

	Just tear	asunder.	II · With	safety.	1
Kind of Materials.	Pounds.	Tons.	Pounds.		
Cast Steel,	134256	59.93	33600	14.98	175.
Blistered Steel,	133152	59.43	33300	14.86	-
Steel, Shear,	128632	56.97	32160	14.24	
Iron, Swedish bar, • •	65000	29.2	16260.	7.3	
"Russian,	59470	26.7	14900	6.7	
" English, - ·	56000	25.0	14000	6.25	
" common, over 2 in. sq.		16.00	9000	4.0	
" sheet, parallel rolling,		17.85	10000	4.46	
" at right angles to roll,		15.35	8600	3.84	
Cast iron, good quality, -	45000	20.05	11250	5.00	
" inferior,	18000	8.03	4500	2.0	
Copper, cast,	32500	14.37	8130	3.6	
rolled,	61200	27.2	15300	6.8	
Tin, cast,	5000	2.23	12500	0.56	
Lead, cast,	880	0.356	220	0.09	
" rolled,	3320	1.48	830	0.37	
Platinum, wire,	53000	2 3·6	13250	5.9	
Brass, common,	45000	20.05	1 1250	5.0	
Wood.					_
Ash, - • •	16000	7.14	4000	1.87	
Beach, • • •	11500	5.13	2875	1.28	<u>d</u>
Box,	20000	8.93	5000	2.23	
Cedar,	11400	5.09	2850	1.27	
Mahogany,	21000	9.38	5250 3000	2·34 1·34	/W/
ррашын,	12000	5·36 5·13	2875	1.28	
Oak, American white, -	11500	4.46	$\frac{2500}{2500}$	1.11	
" English " • seasoned, • •	13600	6.07	3400	1.52	
Pine, pitch, . • •	12000	5.35	3000	1.34	
"Norway,	13000	5.8	3250	1.45	
Walnut,	7800	3.48	1950	0.87	
Whalebone,	7600	3.40	1900	0.85	
Hemp ropes, good,	6400	2.86	2130	0.95	
Manilla ropes,	3200	I·43	1100	0.49	le le
Wire ropes,	38000	17	12600	5-36	
Iron chain, - •	65000	29	21600	9.38	
" with cross pieces, -	90000	40	30000	13.4	

To Find the Cohesive Strength.

RULE.—Multiply the cross-section of the materials in square inches by the tabular number in Table II., and the product is the cohesive strength.

Example. An iron-bar has a cross-section of 2.27 sq. in. How many tens are required to tear it asunder, and how many pounds can it bear with safety? English iron 2.27×25 = 56.75 tons, which will tear it asunder, and it will hear with safety

 $2.27 \times 14000 = 31780$ pounds.

71	Tuche	a and	1645.0	33°1.+	non fo	thom:	Drice	nom for	Abana	
Safety proof.	Chain.	Hemp.		Chain.		thom.	Chain.			,
Cwt.	Diam.	(Circ'm.	1		Pounds			Wire.	Strain.
)	0·10			0.08		\$ cts.		\$ ets.	Cwt
1.3	$\begin{array}{ c c }\hline 1\\ 2 \end{array}$	1.6	0.4	0.23		0.06	0.15	0.06	0.08	2.6
4.5	3	$\frac{1.0}{2 \cdot 1}$	0.3	0.93	0.47	0.24	0.25	0.12	0.15	9
10	4	2.12	0.12	2.11	1.06	0.54	0.36	0.17	0.22	20
18 28	5	3.7	1.1	3.75	1.89	1.10	0.48	0.25	0.32	35
	1		1.6	5.86		1.83	0.60	0.33	0.43	55
40	6	4.2	1.10	8.45	4.52	2.56	0.96	0.42	0.54	80
55	7	4.15	1.14	11.5	6.09	3-42	1.25	0.48	0.62	109
69	8	5.8	2.2	15.0	7.55	4.39	1.44	0.60	0.78	138
80	9	6.3	2.6	18.8	9.56	5.48	1.60	0.76	0.90	160
94	10	6.14	2.11	23.0	11.8	7.00	1.86	0.95	1.20	218
109	11	7.9	2.15	27.7	14.3	8.38	2.16	1.14	1.50	187
127	12	8.4	3.3	33.0	17.1	9.90	2.43	1.37	1.80	254
147	13	8.15	3.8	38.5	19.9	11.9	2.70	1.60	2.10	293
168	14	9.10	3.12	44.7	23.1	13.6	3.06	1.85	2.28	335
199	15	10.5	4.1	51.1	26.3	16.0	3.70	2.10	2.45	397
220	1 in.	11.	4.6	58.0	30.2	18.6	4.33	2.42	2.73	440
246	1.1	11.11	4.11	65.6	34.1	21.3	4.68	2.73	3.10	492
278	1.2	12.6	5 in.	73.7	38.2	24.2	5.58	3.06	3.50	545
302	1.3	13.1	5.5	82.1	42.6	27.4	5.86	3.40	3.91	604
332	1.4	13.12	5.10	91.0	47.1	30.7	6.42	3.77	4.35	663
365	1.5	14.7	6 in	100	52.0	35.	7.08	4.16	4.89	730
399	1.6	15.2	6.5	110	57.1	38.7	7.75	4.57	5.35	798
435	1.7	15.15	6.10	120	63.4	42.6	8.42	5.07	5.86	869
472	1.8	16.8	6.15	131	67.9	46.7	9.15	5:44	6.35	944
553	1.10	17.14	7.10	154	79.8	56.4	10.07	6.38	7.63	1105
538	1.12	19.4	8.4	178	92.6	66.0	12.38	7.40	8.83	1275
729	1.14	20.10	8.14	205	106	76.5	14.15	8.48	10.00	1457
825	2 in	22.	9.8	232	121	88.0	16.00	9.70	11.50	1650
1072	2.4	24.12	10.12	293	153	112	20.75	10.25	14.60	2141
1288	2.8	27.8	12 in.	363	189	140	25.	15.10	18.00	2575
1559	$\begin{vmatrix} 2 \cdot 12 \end{vmatrix}$	30.4	13.4	438	229	172	30.25	18.30	21.80	3117
1854	3 in.	1		522	272		36.00		1	3708
	11		1							

The prices of the chains are taken from that in England and added 50 per cent. Price of hemp ropes from Weaver, Fitler & Co., Rope manufacturers, Philadelphia. The prices of Wire ropes are deduced from the price list of John A. Roebling, Patent Wire Rope Manufacturer, Trenton, N. J.

The Safety proof is here taken and the first telephone are the first telephone and the first telephone an

The Safety proof is here taken one half of the ultimate strength which may be trusted on for new ropes, but when much in use only one quarter

or less should be trusted upon for safety.

LATERAL STRENGTH OF MATERIALS.

The formulas for lateral strength are here reduced to the simplest possible form, and are in consequence subject to conditions which must be particularly attended to. In calculating the strength of beams of irregular sections as shown by the figures 210 to 217 on page 173, it is necessary to maintain the proportions marked on the figures and the calculation will be correct. For the sections 206 to 209 any proportion will answer in the formulas. The weight of the beam itself has not here been taken into consideration, for which allowance must be made if considerable.

Letters denote.

l = length of beam in feet. See figures.

h = height, b = breadth or thickness in inches of the beam, where the strain is acting.

k = coefficient for the different materials and sections of beams, to be found in the tables.

x =modulus of elasticity of materials. See Table.

f =elastic deflection in inches.

W = weight in pounds which the beam can bear with safety, being about one quarter of the ultimate strain at which the beam would break.

Example 1. Fig. 200. A rectangular beam of oak fastened in a wall projects out l=6 feet 4 inches, h=8 inches, and b=5 inches. Required what weight it can bear on the end W=3

$$W = \frac{30 \times 5 \times 8^2}{6.333} = 1509$$
 pounds, with perfect safety.

Example 2. Fig. 201. A beam of section fig. 211, with thickness b=1.25 inches, height h=22.5 inches, supported at the two ends in a length l=25 feet. Required what weight W=? it can bear in the middle. For cast iron coefficient k=260.

$$W = \frac{4 \times 260 \times 1.25 \times 22.5^3}{25} = 26325$$
 lbs.=11.8 tons nearly.

Example 3. Required the elastic reflection for the same beam and condition as in the foregoing example? See Table, modulus of elasticity x=2285 for cast iron. See page 276.

$$f = \frac{26325 \times 25^3}{16 \times 2285 \times 1 \cdot 25 \times 22 \cdot 5^3} = 0.80$$
 inches, nearly.

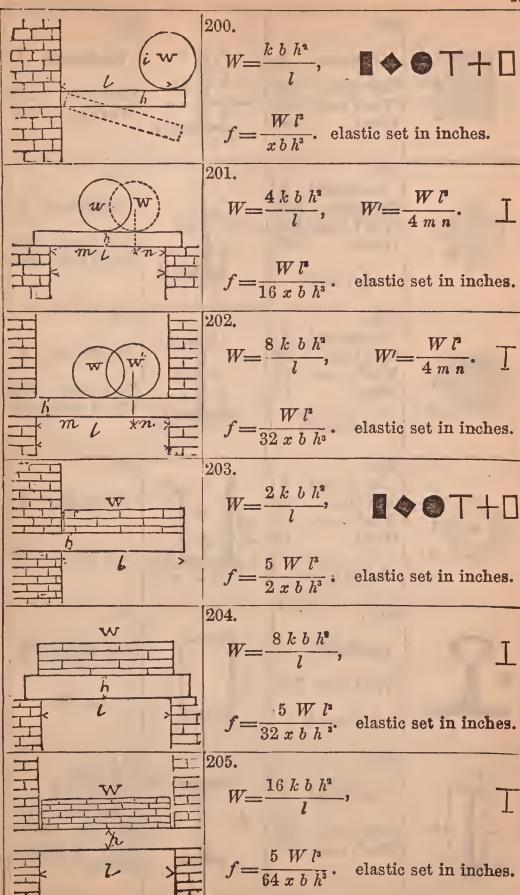
Example 4. Fig. 204. A wrought iron girder of section fig. 217, consisting of four angle irons of $a=3.5\times0.5\times2\times4=14$ square inches, the plate being 0.5:1.35=0.37 inches thick, and h=18 inches deep by l=22 feet. Required how much weight evenly distributed the girder can bear with safety?

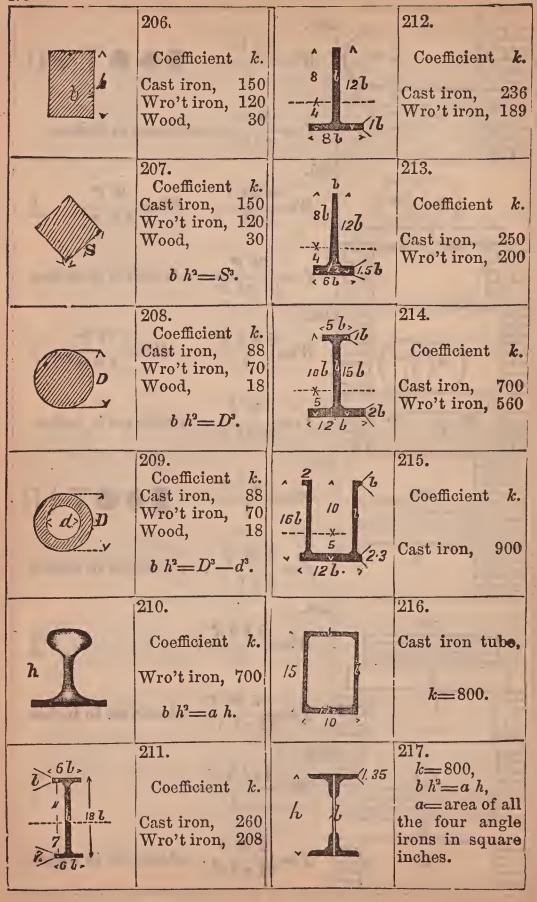
$$W = \frac{8 \times 800 \times 14 \times 18}{22} = 73309 \text{ lbs.} = 32.75 \text{ tons.}$$

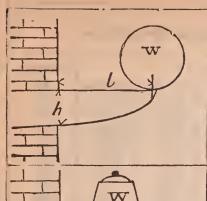
If plates being riveted to the angle iron at top and bottom, add that area to a.

Example 5. Fig. 222. The crank R=3.5 feet, force F=3860 lbs., length of the shaft l=64 feet, diameter D=5.25 inches. Required the twisting in degrees. The shaft being of wrought iron for which x=4110.

Degrees =
$$\frac{425 \times 3860 \times 3.5 \times 64}{4110 \times 5.25^4}$$
 = 11.76°.







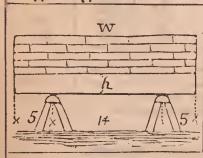
218.

A beam fixed in one end and loaded at the other, should have the form of a Parabola, in which l = abscissa and k = ordinate. y = depth, x = length from W.

$$y = h \sqrt{\frac{x}{l}}$$

219.

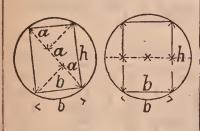
$$W = \frac{k b h^2}{l \cos v} = \frac{k b h^2}{b'}.$$



220.

$$W = \frac{36 \ k \ b \ h^2}{l}.$$

Divide the length into 24 equal parts, place 14 in the middle and 5 at each end.



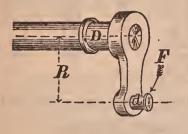
221. To cut out the stoutest rectangular beam from a log.

1st case, divide the diameter in 3 equal parts, and draw lines at right-angles as represented.

2d, divide the diameter in 4 equal parts.

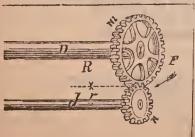
1, b=1.414 b, non-elastic.

 $\frac{2}{222}$, h=1.73 b, elastic beams.



$$D=4\sqrt[3]{\frac{FR}{x}}=80\sqrt[3]{\frac{H}{xn}},$$

Twisting in degrees $=\frac{425 FR l}{x D^i}$.



$$D: d=\sqrt[3]{R}:\sqrt[3]{r},$$

$$D = 80 \sqrt{\frac{3}{x}} \frac{H}{n}$$

Twisting in degrees $=\frac{2233000}{x n} \frac{H l}{D^4}$

Absolute and Ultimate Strength of Materials.

	1				Elasticity.				
Kind of Materials.		Coefficient k.							
	Safety.	Inter.	Pr. cir.	Ultimate.	x				
Wrought iron,	120	162	240	488	4110				
Cast iron,	150	200	300	600	2285				
Cast steel, soft,	385	519	170	1540	4300				
Cast steel, hardened,	1050	1400	2100	4200	6000				
Blistered steel, soft,	175	233	350	700	4200				
Brass,	58	75	113	226	1280				
Copper,	63	71	106	212	2160				
Zinc,	15	20	30	61	2360				
Tin,	17	23	34	69	• . •				
Lead,	4	6	9	18	100				
Ash,	45	56	85	170	221				
Hickory,	67	90	135	270					
Chestnut, sweet,	42	56	85	170					
Oak, white,	5 0	66	100	2 00	300				
Oak, English,	25	33	50	100	248				
Canadian oak,	37	49	73	147	283				
Pine, white,	34	45	67	135					
Yellow pine,	38	50	75	150	268				
Teak,	51	68	102	205	316				

The absolute safety weight is here taken one-quarter of the ultimate breaking weight, but when the weight is acting at short intervals one-third might be relied upon, or in pressing circumstances one-half, when the materials in the beams are known to be of good quality; but the latter never to be exceeded.

Properties of some South American Woods,

Taken from the borders of the rivers Perene and Madre de Dios, and experimented upon by the author of this Pocket-Book.

Peruvian Names of the Woods.	Color.	Specific gravity.	Wt. per cub. foot. lbs.	Hard- ness. H	Ultimate strength.	Elas- ticity.
Chonta (Palm),	Black,	1.564	96.75	28	450	640
Balsamo,	Brown,	1.207	75.25	22	422	492
Shacaranda,		0.991	61.75	18	343	322
Jebe (Indrubber tree)*	Light yellow,	0.797	49.65	15	351	305
Amarillo,	Yellow,	0.734	45.75	13	334	300
	Light brown,	0.613	38.20	11	128	
Huachapeli,	0ak,	0.566	35.25	10	134	180
Nogal,		0.551	34.35	10	131	158
Jebe (best Indrubber)*		0.527	32.85	9	162	262
M. Barigon,	White,	0.282	17.58	6	62	92

^{*} There are different kinds of trees which give India-rubber, but of different quantity and quality.

The woods were perfectly dry. Four experiments on each were made. The hardness, H, is compared with that of substances on page 333. The coefficient, k, is the ultimate lateral strength of the woods. x = modulus of elasticity determined near the ultimate strength.

$$k = \frac{Wl}{4b h^2}$$
 and $x = \frac{Wl^3}{16fb h^3}$. Fig. 201, p. 273.

Meaning of letters is the same as that on page 272.

PILE DRIVING.

Letters denote.

M :=weight of the ram in pounds.

S = fall of the ram in inches.

m =weight of the pile in pounds.

s = space in inches which the pile sinks by the blow.

r = resistance of the ground in pounds.

a = section area in sq. in. of the pile, sharpened to a point not more than 45°.

k =coefficient for the hardness of the ground.

h =depth to which the pile is driven.

W = weight in pounds which a driven pile can bear with safety after the last blow when the pile sunk sinches.

V = velocity in feet per second by which the ram strikes the pile. Ram and pilehead considered non-elastic and perfectly hard.

$$V = 8\sqrt{S} - 1 \qquad v = \frac{8M\sqrt{S}}{M+m} - 4$$

$$S = \frac{M^3S}{r(M+m)^2} - 2$$

$$V = \frac{M^3S}{s(M+m)^2} - 5$$

$$W = \frac{M^3S}{6s(M+m)^2} - 3$$

$$r = ak\sqrt{h} - 6$$

Example 1. A wooden pile 18 feet long by 12 inches square, driven h=12 feet into common natural ground imbedded with tenacious clay for which may be assumed the coefficient k=50. Required how much the pile will set s=? into the ground at a blow with a ram of M=3500 lbs. falling S=42 inches.

The weight of the wooden pile will be about $m=18\times40=720$ lbs.

Area of the pile a=144 square inches.

Resistance $r=144 \times 50 \sqrt{12} = 23840 \text{ lbs.}$

The resistance sought from this formula 6, cannot be depended upon for calculating the weight the pile can bear with safety.

The set
$$s = \frac{3500^3 \times 42}{23840 (3500 + 720)^2} = 4.23$$
 inches.

Suppose the set to be s=4.23 inches at the last blow, required what weight the pile can bear with safety?

$$W = \frac{3500^3 \times 42}{6 \times 4.23 (3500 + 720)^2} = 3984 \text{ lbs.}$$

This can be depended on with safety, if calculated from the actual set of the pile at the last blow.

For ordinary pile driving a heavy ram and short fall is the most effective, but in some cases when the ground itself is elastic, or when driving piles in pure sand it is found more advantageous to use a high fall of the ram.

Approximate Coefficients.							
In coral formations,							. 120
In hard clay with gravel,	•		•			•	100
In hard pure clay,		•		•	•		. 70
In common clay or sand,	•		٠			•	50
In soft clay or loose sand,		•		•	•		. 40
In very loose materials,	٠		٠	•	•	•	30

LATERAL STRENGTH.

For wrought iron beams, letters denote.

W = weight in tons with safety, uniformly distributed on a beam resting on two supports.

S =compressive strain in tons per square inch of top 0.5 $\left(a + \frac{a'}{2}\right)$

a = section area in square inches of top and bottom flanges of the beam. Top and bottom flanges to be alike.

a'= section area in square inches of web or stem.

h =height of beam in inches.

l = length in feet between supports. f = deflection in inches of the beam in the centre, when the weight is uniformly distributed.

P = weight in pound per square foot of flooring to be supported by the beams, which in ordinary cases is estimated to P=140 lbs. B= distance in feet between the beams.

w = weight of the whole beam in pounds.

$$W = \frac{3h}{l} \left(a + \frac{a'}{3} \right) - 1 \qquad f = \frac{W l^3}{46 h^2 (3 a + a')}, \qquad 5$$

$$W = \frac{Sh}{3l} \left(a + \frac{a'}{3} \right) \qquad 2 \qquad f = \frac{l^3}{46h}, \qquad 6$$

$$S = \frac{3W l}{h \left(a + \frac{a'}{3} \right)} \qquad 3 \qquad B = \frac{2240W}{Pl}, \qquad 7$$

$$w = 3.384 l (a + a') \qquad 4 \qquad P = \frac{22wW}{Bl}, \qquad 8$$

Formula 6 gives the safety deflection of a wrought iron beam, which should never be exceeded.

Example. A flooring of l=32 feet by 60 feet long to be constructed to support P=175 pounds per square foot. Required what kind of beams and how many are necessary? and what will be the cost of them? In the table will be found the nearest star to 32 feet span is a 12 inch beam bearing W=8.71 tons, when the distance between the beams in

the flooring will be,

Formula 7.
$$B = \frac{2240 \times 8.71}{175 \times 32} = 3.5$$
 feet.

Number of beams =
$$\frac{60}{3.5}$$
 - 1=16 about.

Add one foot to each beam for the supports at the ends, and the cost will be, $33 \times 16 \times 1.90 = 1003.70$ dollars.

The following Table contains sections of iron rouled by the Phœnix Iron Company. Office 410 Walnut Street, Philadelphia.

Rules.

The price per foot multiplied by 5280 gives the price per mile. The weight in pounds per foot multiplied by 2.36 gives the weight in tons per mile.

The price per foot multiplied by 2240 and divided by the weight in pounds per foot gives the price per ton.

Strength of different Sections of Wrought Iron Beams

Made by the Phænix Iron Company, for Sustaining with Safety a Load Uniformly Distributed.

1	Compo	und Gi	rders.	Solid Rolled Beams.							
Dis.	800	667	553	490	296	308	168	84	48		
bet.	$W=\frac{1}{1}$	$W = \frac{001}{l}$	$W=\frac{553}{l}$	$W=\frac{1}{l}$	$W = \frac{1}{l}$	$w = -\frac{1}{l}$	$W = \frac{1}{l}$	"=-1	$W=\frac{1}{l}$		
$\sup_{=\boldsymbol{l}}$	1		h=12 i.	h = 15 i.	h=12 i.	h=9 i.	h = 9 i.	h = 7 i.	h=6 i.		
feet.	tons.	tons.	tons,	tons.	tons.	tons.	tons,	tons.	tons.		
10	80.00	66.67	55.33	49.00	29.60	30.80	16.80	8.40	4.80		
12	66.66	55.56	44.44	40.83	24.66	25.69	14.00	7.00	4.00		
14	57.14	47.61	38.09	35.00	21.14	22.05	12.00	6.00	3.43*		
16	50.00	41.67	33.33	30.63	18.50	19.25	10.50	5.25	3.00		
18	44.44	37.04	28.52	27.22	16.44	17.11	9.33	4.66	2.66		
20	40.00	33.33	26.66	24.50	14.80	15.40	8.40	4.20	2.40		
22	36.36	30.30	24.24	22.27	13.45	14.00	7.63	3.81*	2.18		
24	33.33	27.77	22.22	20.42	12.33	12.85	7.00	3.50	2.00		
26	30.77	25.64	20.05	18.85	11.38	11.87	6.46	3.23	1.84		
28	28.57	23.80	19.05	17.50	10.57	11.00	6.00*	3.00	1.71		
30	26.66	22.22	17.77	16.33	9.86	10.26	5.60	2.80	1.60		
32	25.00	20.83	16.66	15.31	9.25	9.62	5.25	2.62	1.50		
34	23.53	19.60	15.65	14.41	8.71*			2.47	1.40		
36	22.22	18.52	14.26	13.61	8.22	8.55	4.66	2.33	1.33		
38	21.05	17.37	14.00	12.90*		8.11	4.42	2.21	1.26		
40	20.00	16.66	13.33	12.25	7.40	7.70	4.20	2.10	1.20		
42	19.05	15.87	12.70*	11.67	7.05	7.34	4.00	2.00	1.14		
44	18.18		12.12		6.72	7.00	3.81	1.91	1.09		
46		15.15		11.13	6.43	6.70	3.65	1.83	1.04		
48	17.37	14.48*	11.11	10.00	6.16	6.42	3.50	1.75	1.00		
	16.66	13·88 13·33	10.66	9.80	5.92		3.36	1.68	.96		
50	16.00*			1		6.16					
Per	78 lbs.		59 5 lbs.	47.8 lbs.	40 lbs.	50 lbs.	29 3 lbs.		13 3 lbs.		
Foot'	\$4.68	\$4.26	\$3.57	\$2.40	\$1.90	\$2.40	\$1.50	\$1.00	\$0.66		

The above Table gives the weight in tons, sustained by the several kinds of beams, uniformly distributed over them as in a floor. The weights given are what may be used in practice, being only 9 tons per square inch of that part of the metal subjected to a crushing force.

Under these weights the beams are within the limits of perfect elasticity, and the deflections are therefore in direct proportion to the load.

If it be intended to apply the entire weight at the centre, the figures in the Table must be divided by two; if at any other point, the weight at the centre is to the weight at any other point, as the square of half the beam is to the rectangle of the two parts from where the weight is applied. The prices are subject to changes of the market and agreement.

* When the span of the flooring is given, the star in the Table gives an approximation to what beam ought to be employed; for instance, l=38 feet span should have beams of l=15 inches high, able to bear l=12.9 tons uniformly distributed.

		Iron.		1	Variety of Forms. Price						
	Dimensions.	Per I Weight.			Section.	Area.	Wt.p.ft.	Wt. p. Mile.	Per Ft.		
	Inches.	lbs.	cents.		Figure,	Sq. In.		Tons	\$ cts,		
	$\frac{3}{16}(1\frac{1}{2}+1\frac{1}{2})$	1.77	5.13	1	N	7.4	25	117.86	0.56		
	$\frac{1}{4} \left(1\frac{1}{2} + 1\frac{1}{2}\right)$	2.32	6.74	2 .	n	5.9	20	92.7	0.45		
	$\frac{3}{16}(1\frac{3}{4}+1\frac{3}{4})$	2·09 3·49	6·07 10·1	3	1	7.1	24	113.14	0.54		
	$\frac{5}{16} \binom{1\frac{1}{4} + 1\frac{3}{4}}{2+2}$ $\frac{1}{4} \binom{2+2}{4}$	3.17	8.60	4	2	1.95	6.6	31.45	0.16		
	$\frac{3}{8}(2+2)$	4.59	13.3	5		5.41	18.3	86.43	0.45		
	$\frac{5}{16}(2\frac{1}{2}+2\frac{1}{2})$	4.97	14.4	6		4.44	15	70.71	0.37		
	78 (2½+2½)	6.84	19-9	7		4.22	14.3	67-75	0.35		
	3 (3+3)	7.13	20.7	8		7.00	23.6	111.57	0.58		
	$\frac{1}{2}(3+3)$ $\frac{3}{8}(3\frac{1}{2}+3\frac{1}{2})$	9·32 8·40	27.1	9 -		5.32	18	Chair.	0.72		
-	$\frac{9}{16}(3\frac{1}{2}+3\frac{1}{2})$	12.2	34.9	10		9.65	32.6	Channel.	1.16		
The state of the s	7 (4+4)	11.2	32.5	11		5.41		Channel.	0.65		
	5 (4+4)	15.5	45.0	12	I	2.66	9	Purlin.	0.35		
	ShipFrames.				1	2.66	9	T iron.	0.32		
	$\frac{1}{4} \cdot 1\frac{1}{2} + \frac{3}{16} \cdot 2\frac{1}{4}$	2.5	7.95	13 14		0.65	2.2	Window-	12		
	$\frac{5}{16} \cdot 2 + \frac{1}{4} \cdot 3$ $3 \cdot 21 + 5 \cdot 23$	4.36	13.8	15	1	0.50	1.7	Sashes.	12		
	$\frac{3 \cdot 2\frac{1}{2} + \frac{5}{16} \cdot 3\frac{3}{4}}{16 \cdot 3\frac{1}{2} + \frac{5}{16} \cdot 4\frac{1}{2}}$	6.68 8.85		16	-	0.89	3	Sash bar.	12		
	78.3+3.27	11.0	35.0	17		2.07	7	Shoe.	0.25		
	$\frac{5}{8} \cdot 4 + \frac{7}{16} \cdot 6$	16.4	51.0	18		6.66	22.5	Girder.	0.80		
				20	Th h	This is the beam for which the formulas and table are se up. Top and bottom are alike					
				21	ap h	This compound Gird made to order of any size about 6 cents per pound			ze, for		
					dip.	20 intermediate sizes,					

Spheres, Balls-Surfaces, Capacity and Weight of.

spne	res, Balls-	-Surfaces,	Capacity a	ind Weigh	t of,
Diameter.	Surface.	Capacity.	Cast iron.	Lead.	Water.
Inches.	Sq. inches.	Cub. Inches.	Pounds.	Pounds.	Pounds.
1 in.	3.1416	0.5236	0.1365	0.2147	0.0188
1.125	3.9760	0.7455	0.1943	0.3062	0.0264
1.25	4.9087	1.0226	0.2673	0.4200	0.0368
1.375	5.9395	1.3611	0.3550	0.5579	0.0490
1.5	7.0686	1.7671	0.4607	0.7248	0.0636
1.625	8.2957	2.2467	0.5861	0.9227	0.0809
1.75	9.6211	2.8061	0.7325	1.1528	0.1050
1.875	11.044	3.4514	0.8000	1.4156	0.1242
2 in.	12.566	4.1888	1.0920	1.7180	0.1508
2.125	14.186	5.0243	1.3124	2.0631	0.1809
2.25	15.904	5.9640	1.5592	2.4482	0.2147
2.375	17.720 19.635	7.0143 8.1812	1.8334 2.1328	$2.8811 \\ 3.3554$	$0.2525 \\ 0.2945$
2.5	21.647	9.4708	2.1525 2.4725	$\frac{5.5334}{3.8892}$	0.2945
2.625 2.75	21.047 23.758	10.889	$\frac{2.4725}{2.8400}$	4.4623	0.3410 0.3920
$\frac{2.75}{2.875}$	25.755	12.442	$\frac{2.5400}{3.2512}$	5.1056	0.3920
	28.274	14.137	3.6855	5.7982	0.5089
3 in. 3.125	30.680	15.979	4.1721	6.5568	0.5752
3.25	33.183	15.979 17.974	4.6835	7.3623	0.5752
3.375	35.785	20.129	5.2612	8.2521	0.7246
3.5	38.484	20.129 22.449	5. 8525	9.2073	0.8081
3.625	41.282	24.941	6.5089	10.231	0.8979
3.75	44.179	27.612	7.2135	11.323	0.9941
3.875	47.173	30.466	7.9556	12.500	1.0968
4 in.	50.265	33.510	8.7361	13.744	1.2064
4.25	56.745	40.194	10.510	16.482	1.4470
4.5	63.617	47.713	12.439	19.569	1.7177
4.75	70.882	56.115	14.666	23.035	2.0202
5 in.	78.540	65.450	17.063	26.843	2.3562
5.25	86.590	75.766	19.810	31.089	2.7276
5.5	95.033	87.114	22.720	35.729	3.1361
5.75	103.87	99.541	26.000	40.856	3.5835
6 in.	113.10	113.10	29.484	46.385	4.0716
6.5	132.73	143.79	37.453	58.976	5.1765
7.	153.94	179.59	46.820	73.659	6.4653
7.5	176.71	220.89	57.587	90.598	7.9520
8 in.	201.06	268.08	69.889	109.95	9.6509
8.5	226.98	321.55	83.839	131.38	11.576
9 in.	254.47	381.70	99.510	156.55	13.741
9.5	283.53	448.92	117.03	184.12	16.161
10	314.16	523.60	136.50	214.75	18.850
: 11	380.13	696.91	181.76	285.83	26.289
12	452.39	904.78	235.87	371.09	32.572
13	530.92	1150.3	299.62	471.80	41.411
14	615.72	1436.7	374.56	589.27	51.721
. 15	706.84	1767.1	460.69	724.78	63.616
16	804.24	2144.6	559.11	879.61	77.206
17	853.96	2572.4	670.71	1055.0	92.607
18	1017.8	3053.6	796.08	1252.4	109.93
19	1134.1	3591.3	936.27	1472.9	129.29
20	1256.6	4188.8	1092.0	1718.0	150.80





	Spinish and resident Stations						
Side in inches	Weight in pounds.	Side in inches.	Weight in pounds	Diameter in inches.	Weight in pounds.	Diameter in inches.	Weight in pounds.
16	0.013	35	44.418	16	0.010	35	34.886
18	0.53	33	47.534	निक हिल्ली से से से निक से निक	0.041	33	37.332
3	0.118	37/8	50.756	16	0.119	37	39.864
2. 14 de 12 12 de 124 12 e	0.211	4	54.084	1 1	0.165	4	42.464
38	0.475	41/8	57.517	38	0.373	41/8	45.174
1/2	0.845	41/4	61.055	1 2	0.663	41	47.952
5 8	1.320	43/8	64.700	5 8	1.043	43/8	50.815
34	1.901	$4\frac{1}{2}$	68.448	34	1.493	$4\frac{1}{2}$	53.760
8	2.588	45/8	-72.305	7 8	2.032	$\begin{array}{c c} 4\frac{5}{8} \\ 4\frac{3}{4} \end{array}$	56.788
1	3.380	43	76.264	1.	2.654	$4\frac{3}{4}$	59.900
11/8	4.278	47	80.333	118	3.360	47/8	63.094
11	5.280	5	84.480	11	4.172	5	66.752
18	6.390	5 1	88.784	13/8	5.019	5 1	69.731
11/2	7.604	51	93.168	$1\frac{1}{2}$	5.972	$5\frac{1}{4}$	$73 \cdot 172$
1844 1458 1158 1158 144 158 144 158 144 158 144 158 144 158 144 144 144 144 144 144 144 144 144 14	8.926	5 3	97.657	15	7.010	$5\frac{3}{8}$	76.700
13	10.325	$5\frac{1}{2}$	102.24	$1\frac{3}{4}$	8.128	$5\frac{1}{2}$	80.304
178	11.883	5 §	106.95	17	9.333	5 §	84.001
2	13.520	5 3	111.75	2	10.616	$5\frac{3}{4}$	87.776
21/8	15.263	5 7	116.67	21/8	11.988	5 7	91.634
21	17.112	6	121.66	21/4	13.440	6	95.552
258 212 258 24	19.066	61	132.04	23/8	14.975	61	103.70
$2\frac{1}{2}$	21.120	$6\frac{1}{2}$	142.82	$2\frac{1}{2}$	16.688	$6\frac{1}{2}$	112.16
$2\frac{5}{8}$	23.292	63	154.01	$2\frac{5}{8}$ $2\frac{3}{4}$	18.293	$6\frac{3}{4}$	120.96
23	25.56	7	165.63	$2\frac{3}{4}$	20.076	7	130.05
278	27.939	$7\frac{1}{2}$	190.14	27/8	21.944	71/2	149.33
3	30.416	8	216.34	3	23.888	8	169.85
31/8	33.010	81/2	244.22	318	25.926	81/2	191.81
3 ¹ / ₄ 3 ³ / ₈	35.704	9	273.79	3 1 3 3 38	28.040	9	215.04
338	38.503	10	337.92	3 8	30.240	10	266.29
31/2	41.408	12	486.66	31/2	32.512	12	382.21

Rule for Finding the Weight of Pipes.

The diameter of the pipe in inches, measured from inside to outside, multiplied by the coefficient for the metal, will be the weight in pounds per linear foot.

Coefficients.

Lead,			. 0.1005	Brass, rolled,	•	0.0985
Copper, .			0.0989	Iron, rolled,		0.0876
Brass, cast, .		•	. 0.0882	Cast iron, .		0.0811
Cast steel,			0.0891	Tin, rolled,		0.0821
Clay, burnt,	,		. 0.0214	Zinc, rolled,	•	0.0808

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A solid cast-iron cylinder 42 % in. diameter weighs 4482.6 paunds per foot.		A s	olid cast-	iron cyli	inder 42	5∕8 in. dia	meter we	eighs 448	32.6 pyui	nds per	foot.
A solid cast-iron cylinder 42 % in. diameter weighs 4482 6 pounds per foot. Subtract inside cylinder 40 % in. diameter weighs 3972 5 " Weight of pine 11/2 in thick will be		Sut	tract in	side cyli	nder 40	8 in. dia	meter w	eighs 397	72.5		
Weight of pipe 1 1/4 in. thick will be 510·1 " "		We.	ignt of p	ipe 1 1/4 i	in. thick	will be		5	ro.T		

28 |20.06

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Weight of Flat Rolled Iron per Foot,	
the of Flat Rolled Iron]	Foot,
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Look first for the thickness, and follow that line until the column where the breadth is on the top; is the number of pounds per foot.

11 | 5.808 | 6.337 | 6.864 | 7.393 | 7.921 | 8.448 | 8.977 | 9.505 | 10.03 | 10.56 2.956 3.326 3.696 4.065 4.435 4.805 5.178 5.544 5.914 6.283 6.653 7.022 7.392 16-16 17-05 17-95 2 12.36 15.21 16.05 16.89 13 12.67 13.46 14.26 15.05 15.84 13 11.09 11.83 12.57 13.31 14.04 14.78 18 9.610 10.30 10.98 11.67 12.36 13.04 13.73 13 8.237 8.871 9.505 10.14 10.77 11.40 12.04 12.67 $|6\cdot970|7\cdot551|8\cdot132|8\cdot713|9\cdot294|9\cdot874|10\cdot45|11\cdot03|11\cdot62$ 3.802 4.224 4.646 5.069 5.492 5.914 6.336 6.758 7.181 7.604 8.025 8.448 **2.2**17 2.534 2.850 3.168 3.484 3.802 4.119 4.435 4.752 5.069 5.386 5.703 6.019 6.336 18 |4.752|5.227|5.703|6.178|6.653|7.129|7.604|8.079|8.554|9.028|9.504

4 | 1.056 | 1.265 | 1.477 | 1.690 | 1.901 | 2.112 | 2.325 | 2.535 | 2.746 | 2.957 | 3.168 | 3.379 | 3.591 | 3.802 | 4.013 | 4.224

8 | **0.634** | 0.792 | 0.950 | 1.108 | 1.267 | 1.425 | 1.584 | 1.742 | 1.900 | 2.059 | 2.218 | 2.376 | 2.534 | 2.693 | 2.851 | 3.009 | 3.168

3 0·162 0·237 0·316 0·396 0·474 0·553 0·633 0·712 0·792 0·870 0·949 1·029 1·109 1·188 1·267 1·346 1·425 1·504 1·584 $|0.081|0.108|0.158|0.211|0.264|0.316|0.369|0.422|0.475|0.528|0.580|0.633|0.686|0.739|0.792|0.845|0.950|0.898|1.00 \\ |1.056|0.081|0.108|0.158|0.118|0.211|0.264|0.316|0.369|0.422|0.475|0.528|0.580|0.633|0.686|0.739|0.792|0.845|0.950|0.898|1.00 \\ |1.056|0.081|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108|0.108$

Weight of Flat Rolled Iron per Foot,

The thickness is in the first column, and the breadth in the top line.

WEIGHT OF FLAT ROLLED	IRON PER FOOT.	285
47.76 44.82 42.69 39.55 38.01 36.49 32.86 30.42	25.35 22.81 20.27 17.74 15.20 12.67 10.23 7.594 5.069	2.535
45.95 43.32 41.09 38.86 36.43 34.01 31.53 29.15	23.23 24.29 25.35 20.91 21.86 22.81 18.59 19.43 20.27 16.26 17.00 17.74 13.94 14.57 15.20 11.61 12.14 12.67 9.294 9.716 10.23 6.970 7.287 7.594 4.647 4.858 5.069 3.485 3.643 3.801	2.429
54 44.14 41.82 39.49 37.17 34.85 32.53 30.20 27.88	22.18 23.23 19.96 20.91 17.74 18.59 15.52 16.26 13.31 13.94 11.09 11.61 8.871 9.294 6.653 6.970 4.436 4.647 3.327 3.485	2.323
5 54 54 40·13 42·13 44·14 38·02 39·92 41·82 35·90 37·70 39·49 33·79 35·48 37·17 31·68 33·26 34·85 29·57 31·05 32·53 27·46 28·83 30·20 25·35 26·61 27·88 23·23 24·39 25·55	21.12 22.18 23.23 24.29 19.01 19.96 20.91 21.86 16.90 17.74 18.59 19.43 14.78 15.52 16.26 17.00 12.67 13.31 13.94 14.57 10.56 11.09 11.61 12.14 8.449 8.871 9.294 9.716 6.386 6.653 6.970 7.287 4.224 4.436 4.647 4.858 3.168 3.327 3.485 3.643	2.218
5 40.13 38.02 35.90 33.79 31.68 29.57 29.57 27.46 25.35	20.07 21.12 18.06 19.01 16.05 16.90 14.04 14.78 12.04 12.67 10.03 10.56 8.026 8.449 6.019 6.386 4.013 4.224 3.009 3.168	2.112
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3\frac{3}{8} 3\frac{4}{8} 4\frac{4}{4} 4\frac{4}{4} 4\frac{4}{4} 5\frac{4}{4} 5\frac{4}{4}<	14.25 14.78 15.31 15.84 16.37 16.90 17.95 19.01 20.07 21.12 22.18 23.23 24.29 25.35 12.83 13.31 13.79 14.27 14.74 15.21 16.15 17.11 18.06 19.01 19.96 20.91 21.86 22.81 11.40 11.83 12.52 14.36 15.21 16.05 16.90 17.74 18.59 19.43 20.27 9.980 10.35 10.46 11.83 12.56 13.31 14.04 14.78 15.52 16.26 17.00 17.74 8.554 8.871 9.188 9.505 9.822 10.14 10.77 11.41 12.04 12.67 13.31 14.57 15.20 7.129 7.893 7.657 7.921 8.183 8.445 8.975 9.507 10.03 10.56 11.09 11.61 12.44 15.20 12.44 15.20 12.45 12.45 12.87 12.84 8.871 9.294 9.716 10.23 10.294 9.716 10.23 10.294 </td <td>1.426 1.479 1.531 1.584 1.637 1.690 1.795 1.901 2.006 2.112 2.218 2.323 2.429 1.426 1.426 1.428 1.42</td>	1.426 1.479 1.531 1.584 1.637 1.690 1.795 1.901 2.006 2.112 2.218 2.323 2.429 1.426 1.426 1.428 1.42
44 32.32 30.52 30.52 26.92 25.13 25.13 21.54	14.78 15.31 15.84 16.37 16.90 17.95 11.83 12.20 12.67 13.09 13.52 14.36 11.83 12.20 12.67 13.09 13.52 14.36 10.35 10.72 11.09 11.46 11.83 12.56 8.871 9.188 9.505 9.822 10.14 10.77 7.393 7.657 7.921 8.183 8.445 8.975 5.914 6.125 6.336 6.547 6.759 7.181 4.436 4.594 4.752 4.910 5.069 5.386 2.957 3.062 3.168 3.274 3.380 3.591 2.218 2.297 2.376 2.455 2.535 2.693	262-1,0
3\frac{3}{8} 3\frac{4}{8} 3\frac{4}{8} 3\frac{4}{8} 4 27.18 28.09 28.84 29.59 30.84 32.10 25.66 26.61 27.56 28.51 29.46 30.41 24.23 25.13 25.78 26.43 27.57 28.72 22.81 23.65 24.50 25.35 26.19 27.04 21.38 22.18 22.97 23.76 24.55 25.35 19.96 20.70 21.44 22.18 22.92 23.66 18.53 19.22 19.90 20.59 21.28 21.97 17.10 17.74 18.37 19.01 19.64 20.28 15.68 16.26 16.84 17.42 18.00 18.59	16.90 13.52 11.83 11.83 11.83 11.83 8.445 7 6.75 6.75 6.75 6.75 6.75 7 6.75 7 7 6.75 7 7 6.75 7 7 6.75 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7	11.690
33 38 29.59 30.84 28.51 29.46 26.43 27.57 25.35 26.19 23.76 24.55 22.18 22.92 20.59 21.28 19.01 19.64 7.42 18.00	116.37 714.74 713.06 911.46 9.822 6.54.91 8.183 8.3.274	11.63
38 33 28.84 29.59 27.56 28.51 25.78 26.43 24.50 25.35 22.97 23.76 21.44 22.18 19.90 20.59 18.37 19.01	1 15.8 1 14.2 1 14.2 1 11.0 2 11.0 2 11.0 5 6.33 6 6.33 7 7.92 7 7.92 2 3.16 5 6.33 7 7.2 7 7.3 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7	11.58
38 1 27.56 2 24.50 8 22.97 0 21.44 1 18.37	8 15.3 8 15.3 12.2 1 0.7 1 0.18 1 0.18 1 6.12 6 4.59 7 3.06 8 2.29	9 1.53
3½ \$ 28.09 \$ 26.61 \$ 25.13 \$ 25.13 \$ 22.18 \$ 22.18 \$ 20.70 \$ 19.22 \$ 17.74	14.25 14.78 12.83 13.31 11.40 11.83 9.980 10.35 8.554 8.871 7.129 7.393 5.703 5.914 4.277 4.436 2.851 2.957 2.138 2.218	611-47
34 6 24.7 26.0 6 24.7 2 21.9 2 21.9 8 19.2 8 19.2 8 16.4 16.4	11.62 12.14 12.67 13.20 13.73 10.45 10.93 11.41 11.88 12.36 9.294 9.716 10.14 10.55 10.98 8.132 8.502 8.871 9.740 9.610 6.970 7.287 7.604 7.920 8.237 5.808 6.072 6.337 6.601 6.865 4.647 4.858 5.069 5.280 5.492 3.485 3.644 3.802 3.960 4.119 2.320 2.429 2.535 2.640 2.746 1.741 1.822 1.901 1.980 2.059	0 1-37
3\$ 7 25.0 1 23.7 4 22.4 8 21.1 1 19.8 1 19.8 4 18.4 1 17.1 1 15.8	7 13.2 11.8 11.18 4 10.5 1 9.7 4 7.9 2 1.9 5 2.8 5 2.6 1 1.9 8 1.9	7/1-32
3 6 22-8 6 22-8 5 21-5 3 20-2 2 19-0 0 17-7 7 15-2 7 15-2	4 12.6 11.4 11.4 11.4 10.1 10.1 10.1 10.1 10.1	5 1.26
24 7 23.0 1 21.8 1 21.8 5 20.6 8 19.4 8 19.4 6 17.0 6 17.0 14 14.5 8 13.3	12.12.11.12.12	2 1-21
$ \begin{array}{c c c c c c c c c c c c c c c c c c c $	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	\$\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\
28 30 31 30 31 30 31 31 31 31 31 31 31 31 31 31	56 11.09 04 9.981 48 8.872 92 7.763 36 6.654 80 5.545 24 4.436 68 3.372 12 2.218 84 1.663	56/1-10
23 20.0 24 19.0 24 19.0 28 17.9 28 17.9 28 17.9 28 17.9 14 14.7 14 14.7 18 13.7 18 13.7	14 10.56 14 10.56 1 8.448 1 8.448 1 8.448 2 7.392 2 7.392 2 7.392 3 7.392 3 7.392 4 7.392 5 7.392 6 7.392 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7	11.05
04 04 04 04 04		

54 97.58 102.0 106.4

88-71 92-93 97-16 101-4

54 106.9 111.5

Weight of Flat Rolled Iron per Foot,

RULE.—Look first for the thickness, and follow the line until the column where the breadth is on the top, is the number of pounds per foot

34 37.07 38.44 39.81 41.19 42.51 43.93 46.68 49.25 52.17 54.92 57.66 60.41 63.15 65.89 33 | 49.09 | 50.69 | 53.86 | 57.03 | 60.20 | 63.36 | 66.53 | 69.70 | 72.87 | 76.04 44 | 64.63 | 68.22 | 71.81 | 75.40 | 78.99 | 82.58 | 86.17 57-45 60.83 64.21 67.59 70.97 74.35 77.73 81.11 32 | 52.38 | 55.65 | 58.93 | 62.20 | 65.97 | 68.75 | 72.02 | 75.30 | 78.58 34 | 42.87 | 44.35 | 45.83 | 47.31 | 50.27 | 53.23 | 56.18 | 59.14 | 62.10 | 65.05 | 68.01 | 70.97 39.92 41.34 42.77 44.19 45.62 48.47 51.24 54.17 57.03 59.88 62.73 65.58 68.43 44 | 72.23 | 76.04 | 79.84 | 83.64 | 87.44 | 91.24 45.93 47.46 49.00 52.06 55.13 58.19 61.25 64.31 67.37 70.44 73.51 80.26 84.27 88.29 92.30 96.41

 $|34\cdot33|35\cdot64|36\cdot96|38\cdot28|39\cdot60|40\cdot92|42\cdot24|44\cdot88|47\cdot43|50\cdot16|52\cdot80|55\cdot44|58\cdot08|60\cdot72|63\cdot36|$

|31.94|32.95|34.21|35.48|36.75|38.02|39.28|40.55|43.09|45.62|48.16|50.69|53.23|55.76|58.30|60.84

26.72 27.88 29.04 30.20 31.36 32.53 33.69 34.85 36.01 37.17 39.50 41.82 44.14 46.47 48.79 51.11 53.44 55.77

29.42 30.49 31.57 32.78 34.00 35.21 36.43 37.64 38.86 41.29 43.72 46.15 48.58 51.01 53.43 55.87 58.31

24·39 25·50 26·61 27·72 28·83 29·93 31·04 32·15 33·26 34·37 35·48 37·70 39·92 42·13 44·35 46·57 48·79 51·01 53·23 22.18 23.23 24.29 25.34 26.40 27.46 28.51 29.57 30.62 31.68 32.73 33.79 35.91 38.02 40.13 42.24 44.35 46.47 48.58 50.69

Weight Per Square Foot in Pounds.

(F).		1	1 ì		1
Thickness in inches.	Cast Iron.	Wrought or Sheet Iron.	Sheet Copper.	Sheet Lead.	Sheet Zinc
16	2.346	2.517	2.890	3.694	2.320
1 1	4.693	5.035	5.781	7.382	4.642
16	7.039	7.552	8.672	11.074	6.961
4	9.386	10.070	11.562	14.765	9.275
T ₆	11.733	12.588	14.453	18.456	11.61
16 16	14.079	15.106	17.344	22.148	13.93
76	16.426	17.623	20.234	25.839	16.23
1/2	18.773	20 141	23.125	29.530	18.55
<u> </u>	21.119	22.659	26.016	33.222	20.87
7 7 7 7 8	23.466	25.176	28.906	36.913	23.19
16	25.812	27.694	31.797	40.604	25.53
. 3	28.159	30.211	34.688	44.296	27.85
13 16 15 15	30.505	32.729	37.578	47.987	30.17
78	32.852	35.247	40.469	51.678	32.47
15	35.199	37.764	43.359	55.370	34.81
1	37.545	40.282	46.250	59.061	37.13
11/8	42.238	45.317	52.031	66.444	41.78
14	46.931	50.352	57.813	73.826	46.42
13	• 51 • 625	55.387	63.594	63.594	51.04
$\frac{1\frac{1}{2}}{15}$	56.317	60.422	69.375	88.592	55.48
1 5 1 3	61·011 65·704	65·458 70·493	$\begin{bmatrix} 75.156 \\ 80.938 \end{bmatrix}$	95.975 103.358	60·35 65.00
17/8	70.397	75.528	86.719	110.740	69.61
28	75.090	80.28	92:500	118.128	74.25
	10000	0000	72.000		1120

Weight of Copper Rods or Bolts per Foot,

Diameter. Inches.	Weight. Pounds.	Diameter. Inches	Weight. Pounds.	Diameter. Inches.	Weight. Pounds.	Diameter Inches-	Weight. Pounds.
1 6 3 8 7	0.1892	1	3.0270	17	10.642	338	34.487
5 16	0.2956	1 1 6	3.4170	2	12.108	$3\frac{1}{2}$	37.081
38	0.4256	11	3.8912	$2\frac{1}{8}$	13.668	$3\frac{5}{8}$	39.737
7 6	0.5794	13	4.2688	$2\frac{1}{4}$	15.325	33	42.568
1 6 2 9 16 §	0.7567	11	4.7298	$2\frac{3}{8}$	17.075	378	45.455
16	0.9578	1.3 1.6	5.2140	$2\frac{1}{2}$	18.916	4	48.433
	1.1824	18	5.7228	$2\frac{5}{8}$	20.856	41/4	53.550
11 16 34	1.4307	17 ₇₆	6.2547	$2\frac{3}{4}$	22.891	$4\frac{1}{2}$	61.321
4	1.7027	$1\frac{1}{2}$	6.8109	2 7	25.019	434	68.312
13 16 7	1.9982	$1\frac{9}{16}$	7.3898	3	27.243	5	76.130
8	2.3176	$1\frac{5}{8}$	7.9931	3\frac{1}{8}	29.559	5 1/2	91.550
16	2.6605	12	9.2702	31	31.972	6	109.
						- 1	

	~.	1 ,				11 -)	*****	
Gauge	Size inches.			l Plate				n Wire r 1000 fe	
num.	inches.	We	ight per	square	loot.				
No.	In.	Iron.	Steel.	Copper Lbs.	Brass.	Iron.	Steel.	Copper Lbs.	Brass.
0000	.4600	Lbs. 18.75	18.97	21.36	20.84	566.3	571.7	646.8	634.1
000	.4096	16.70	16.90	19.01	18.56	449.1	453.3	512.9	502.9
00	.3648	14.87	15.05	16.93	16.52	356.1	359.5	406.8	398.8
0	.3249	13.24	13.40	15.08	14.72	282.4	285.1	322.5	316.3
1	.2893	11.79	11.93	13.43	13.11	224.5	226.1	255.8	250.8
2 3	.2576	10.50	10.63	11.96	11.67	177.6	179.3	202.9	198.9
3	.2294	9.354	9.464	10.65	10.39	140.8	142.2 112.7	160.8 127.5	157.8 125.1
4 5	.2043	8.330	8.428 7.505	9.486 8.448	$9.255 \\ 8.242$	111.7 88.59	89.43	101.2	99.2.)
3	.1819	7.418	1.000	0.110	0.242				
6	.1620	6.606	6.683	7.523	7.340	70.26	70.92	80.25	78.67
7	.1443	5.882	5.952	6.699	6.536	55.71 44.18	56.24 44.60	63.64 50.46	62.38 49.48
8 9	.1285 .1144	5.238	$5.300 \\ 4.720$	5.966 5.313	5.821 5.18 4	35.01	35.37	40.02	39.24
10	.1019	4.154	4.203	4.731	4.616	28.26	28.05	31.73	31.11
11	.0907	3.700	3.743	4.213	4.110	22.03	22.24	25.16	24.68
12	.0808	3.294	3,333	3.752	3.661	17.47	17.64	19.95	19.57
13	.0720	2.934	2.968	3.341	3.260	13.85	13.99	15.82	15.52
14	.0641	2.613	2.643	2.978	2.903	10.99	11.09	12.55	12.31
15	.0571	2.327	2.354	2.650	2.585	8.717	8.899	9.953	9.761
16	.0508	2.072	2.096	2,359	2.302	6.913	6.978	7.896	7.741
17	.0452	1.845	1.867	2.101	2.050	5.481	5.532	6.261	6.137
18	.0403	1.643	1.662	1.872	1.826	4.347	4.387	4.965	4.867
19	.0359	1.463	1.480	1.666	1.626	3.447	3.479	$\begin{array}{c c} 3.937 \\ \hline 3.125 \end{array}$	3.861 3.064
20	.0320	1.303	1.318	1.484	1.448	2.735	2.761	5,120	
21	.0285	1.160	1.174	1.321	1.289	2.168	2.188	2.476	2.428
22	.0253	1.033	1.045	1.176	1.148	1.720	1.736	1.964	1.926
23	.0226	.9203	.9310	1.048	1.023	1.363	1.376	1.557	1.527 1.211
24 25	.0201	.8195	.8291 .7383	.9334	.9105 .8109	1.081	1.091 .8656	1.235 .9795	.9603
			.1500						
26	.0159	.6499	.6575	.7401	.7221	.6801	.6864	.7768	.7616
27	.0142	.5787	.5855	.6591	.6430	.5393 .4277	.5444	.6160 .4885	.60 3 9 . 47 89
28 29	.0126	.5154 .4580	.5214 .4643	.5869	.5726 .5099	.3391	.4317 .3422	.3873	.3797
30	.0100	.4087	.4135	.4654	.4541	.3699	.2714	3072	.3012
31	.0089	.3640	.3683	.4145	.4044	.2134	.2153	.2437	.2389
32	.0080	.3241	.3279	.3691	.3601	.1691	.2193	.1932	.1894
33	.0071	.2887	.2920	3287	.3207	.1341	.1354	.1532	.1502
34	.0063	.2570	.2600	.2927	.2856	.1063	.1073	.1216	.1192
35	.0056	.2289	.2316	.2606	.2543	.0845	.0853	.0965	.0947
36	.0050	.2039	.2062	.2322	.2265	.0669	.0675	.0764	.0750
37	.0045	.1816	.1837	.2067	.2017	.0531	.0536	.0606	.0594
38	.0040	.1617	.1636	.1841	.1796	.0118	.0424	.0480	.0471
39 40	.0035	.1440	.1456 .1297	.1640	.1600 .1424	.0334	.0337	.0381	.0374
40	10001								
Spec	. grav.	7.828	7.92	8.917	8.70	7.85	7.93	8.96	8.78
1									

The American Wire Gange is introduced and manufactured by J. R. Brown & Sharpe, of Providence, R. I., and is to be had in the principal hardware stores in the country. It is adopted by most manufacturers of plates and wire, and is now considered the American Standard Gange.

Birmingham Gauge for Wire, Sheet Iron and Steel.

			Weigh	nt per Squar	e Foot in P	ounds.	
Thickne		Thickness in	Sheet and	Sheet Cast	Sheet	Sheet Lead.	Thickness in
the ga		inches.	Boiler fron.	Steel.	Copper.		inches.
No. 00		0.454	18.267	18.259	20.566	26.75	7:16
U	000	0.425	17.053	17.280	19.252	25.06	27:64
-	00	0.380	15.247	15.451	17.214	22.42	3:8
	0	0.340	13.7	14.0	15.6	20.06	11:32
	1	0.300	12.1	12.4	13.8	17.72	5:16
	2	0.284	11.4	11.7	13.0	16.75	9:32
	3	0.259	10.4	10.6	11.9	15.26	1:4
	4	0.238	9.60	9.80	11.0	14.02	7:32
	5	0.220	8.85	9.02	10.1	12.98	7:32
	6	0.203	8.17	8.33	9.32	11.98	7:32
	7	0.180	7.24	7.38	8.25	10.63	3:16
7	8	0.165	6.65	6.78	7.59	9.73	3:16
	9	0.148	5.96	6.08	6.80	8.72	5:32
•	10	0.134	5.40	5.51	6.16	7.90	5:32
	11	0.120	4.83	4.93	5.51	7.08	1:8
	12	0.109	4.40	4.50	5.02	6.42	1:8
	13	0.095	3.83	3.91	4.37	5.60	3:32
	14	0.083	3.34	3.41	3.81	4.90	3:32
	15	0.072	2.90	2.96	3.31	4.25	1:16
	16	0.065	2.62	2.67	3.00	3.83	1:16
	17	0.058	2.34	2.39	2.67	3.42	1:16
	18	0.049	1.97	2.01	2.25	2.90	1:16
- 1	19	0.042	1.69	1.72	1.93	2.48	3:64
10 1	20	0.035	1.41	1.42	1.61	2.04	3:64
	21	0.032	1.29	1.31	1.47	1.89	3:64
1 44	22	0.028	1.13	1.15	1.29	1.65	1:32
•	23	0.025	1.00	1.02	1.14	1.47	1:32
	24	0.022	0.885	0.903	.1.01	1.30	1:32
	25	0.020	0.805	0.820	0.918	1.18	1:32
	26	0.018	0.724	0.738	0.826	1.06	1:64
	27	0.016	0.644	0.657	0.735	0.945	1:64
	28	0.014	0.563	0.574	0.642	0.826	
1	29	0.013	0.523	0.533	0.597	0.767	
	30	0.012	0.483	0.493	0.551	0.708	-
	31	0.010	0.402	0.410	0.480	0.600	
	32	0.009	0.362	0.370	0.420	0.532	
	33	0.008	0.322	0.328	0.370	0.472	
	34	0.007	0.282	0.288	0.323	0.413	
	35	0.005	0.230	0.235	0.262	0.309	
	36	0.004	0.170	0.173	0.194	0.236	

Birmingham Gauge for Silver and Gold.

No.	Thick.	No.	Thick.	No.	Thick.	No.	Thick.	No.	Thick.	No.	Thick.
1	.004	7	.015	13	.036	19	.064	25	.095	31	.133
2	.005	8	.016	14	.041	20	.067	26	.103	32	.143
3	.008	9	.019	15	.047	21	.072	27	.113	33	.145
4	.010	10	.024	16	.051	23	.074	28	.120	34	.148
5	.013	11	.029	17	.057	23	.077	29	.120	35	.158
6	.013	12	.034	18	.061	24	.082	30	.126	36	.167.

Proportion of Bolts and Nuts. Number of Threads per In.

*						Diameter.	Number of per I	Threads,
		A		A			3	墨
						3		
3 inch.	$4\frac{1}{2}$	$5\frac{1}{4}$	5	$7\frac{1}{16}$	$2\frac{1}{2}$	1/4	20	10
2_4^3	41	$4\frac{3}{4}$	$4\frac{1}{2}$	$6\frac{3}{8}$	$egin{array}{c} -2 \ 2rac{1}{4} \end{array}$	5 16	18	9
$2\frac{1}{2}$	33	$4\frac{3}{8}$	41/8	$5\frac{1}{1}\frac{3}{6}$	2	3/8	16	9
$2\frac{1}{4}$	3 ⁸ / ₄ 3 ⁸ / ₈	$4\frac{3}{8}$ $3\frac{7}{8}$ $3\frac{1}{2}$ $3\frac{1}{4}$	$\frac{4\frac{1}{8}}{3\frac{3}{4}}$	$5\frac{5}{16}$	13/4		14	8
2	3	$3\frac{1}{2}$	33	$4\frac{3}{4}$ $4\frac{3}{16}$	$1\frac{5}{8}$,	1/2	12	7
$\begin{array}{ c c }\hline 2\\1\frac{7}{8}\\ \end{array}$	23/4	3_{4}^{1}	3	$4\frac{3}{16}$	$egin{array}{c} 1rac{5}{8} \ , \ 1rac{1}{2} \ . \end{array}$	5/8	11	7
$1\frac{3}{4}$.	$2\frac{5}{8}$	$\frac{3}{2\frac{7}{8}}$	$2\frac{3}{4}$	$3\frac{7}{8}$	$1\frac{3}{8}$.	7 16 12 58 34 78	10:	6
15/8	$2\frac{1}{2}$	$2\frac{7}{8}$	$egin{array}{c} 2rac{3}{4} \ 2rac{5}{8} \ 2rac{1}{2} \ 2rac{1}{4} \ \end{array}$	$3\frac{11}{16}$	11/4	78	9	6
$1\frac{1}{2}$	$2\frac{1}{4}$	$egin{array}{c} 2rac{5}{8} & & & \\ 2rac{3}{8} & & & \\ 2rac{1}{8} & & & \\ 1rac{3}{4} & & & \\ & 1rac{3}{4} & & & \\ & & & & \\ \end{array}$	$2\frac{1}{2}$	$egin{array}{c} 3rac{1}{2} \\ 3rac{3}{16} \\ 2rac{7}{8} \\ 2rac{5}{8} \\ 2rac{1}{16} \\ 2rac{1}{8} \\ 1rac{7}{16} \\ 1rac{1}{16} \end{array}$	11/8	1	8	5
13 13 ···	2	$2\frac{3}{8}$		$3\frac{3}{16}$	116	11/8	7	4
g 1½	$1\frac{7}{8}$	$2\frac{1}{8}$	2.	$2\frac{1}{8}$	1	$1\frac{1}{4}$		31
Diameter of Bolt, $1\frac{1}{3}$	$egin{array}{c} 1rac{7}{8} \\ 1rac{5}{8} \\ 1rac{1}{2} \end{array}$	$1\frac{7}{8}$	$1\frac{7}{8}$ $1\frac{5}{8}$	28	- * 8	$1\frac{1}{2}$	6 5	3
mail 7	1 2	14	18	276	8	$1\frac{3}{4}$		$2\frac{1}{2}$
A 8	$1\frac{5}{16}$	$\begin{array}{c c} 1\frac{1}{2} \\ 1\frac{3}{8} \end{array}$	11/2	17	34	2	$4\frac{1}{2}$ 4	$2\frac{1}{4}$
4	$1\frac{3}{16}$	$\begin{array}{c c} 1\frac{5}{8} \\ 1\frac{1}{8} \end{array}$	$1\frac{5}{1.6}$	131	8	$2\frac{1}{2}$		2
8		1 8	$1\frac{3}{16}$	$\begin{array}{c c} 1_{\overline{16}} \\ 1_{\overline{16}} \end{array}$	শ্তি, শৃত্ত জাধু চ্চাত্ত লাগে লাগে	$\frac{3}{3\frac{1}{2}}$	$3\frac{1}{2}$ $3\frac{1}{4}$	
16	3	7	78	$\begin{array}{c c} 1_{\overline{16}} \\ 1_{\overline{4}} \end{array}$	$\frac{2}{16}$	$\frac{3}{2}$	$\frac{\sigma_4}{3}$	3
78 34 58 9 6 12 7 6 38	3 3 4 3 4	7 7		$1\frac{1}{16}$	3 8	$4\frac{1}{2}$	$2\frac{7}{8}$	1.75 400 7100
30	7 16	5.0	3 3 4	$1\frac{1}{16}$	5 16		$2\frac{7}{8}$	2 2
5 16	9	58	16	11 16	5 16	$\begin{array}{c c} 5 \\ 5\frac{1}{2} \end{array}$	$2\frac{5}{8}$	
1 1 4	9 16 <u>8</u> 8	78 78 58 58 7 6	9 16 9 16	$\begin{array}{c c} 11\\ \hline 11\\ \hline \end{array}$	1 1 1	6	$2\frac{1}{2}$	

The above proportions of bolts and nuts are established by Sir Joseph Whitworth.

Weight in Pounds of Nut and Bolt-Head.

-	Diameter of Bolt in Inches.												
	Head and Nut.												
	Hexagon, Square,	.017 .05	.128 0 .164	.267	.43 .553	.73 .882	1.1	2.14 2.56	3.77 4.42	5.62 7.00	8.75 10.5	17.2 21.	28.8 36.4

Proportion of Screw-Threads, Nuts and Boltheads.

D: c	(D))	D: 1	T171 741 1		77 13		
Diam. of Screw	Threads per inch.	of core.	- Width of flat.	Outside diamet.	Inside diamet.	Diagonal.	height
BCIGW	per men.	or core.	or nat.	damet.	diamet.		of h'd.
		鱼人鱼					
		d		60	2 2	as s	
	" un "	· .					
2 2 2	ARA		AAA	-			
154	20	:185	.0062	.9516	152	11/16	154
.5 16	18	•240	.0070	11516	·19\(\int 32\)	·13 £ 16	19564
358	16	•294	.0078	25,532	11516	31 532	11532
$0.7 \int 16$ $0.1 \int 2$	14 13	·344 ·400	·0089 ·0096	·43 \(\)48	•25 \(\) 32 •7 \(\) 8	1:1516 1:154	·25 \ 64 \ · 7 \ \ 16
9516	12	1 .454	0090	1.7 / 64	31 532	1·5∫16	31 \ 64
•5∫8	11	:507	0113	1.7532	1.15.16	$1.1 \int 2$	17 532
•3∫4	10	.620	.0125	1.7 / 16	1.154	1.3 4	558
.7∫8	9	.731	.0140	1.21 / 32	1.7516	2.1 532	23 / 32
1.	8	·837	.0156	1.758	1.5 \(\) 8	2.5 ∫ 16	13∫16
1.158	7	•940	·0180	2.3 ∫ 32	1.13 ∫ 16	2.152	.29 5 64
1.154	7	1.065	.0180	2.5 16	2.	2.27 \(\) 32	1.
1.358	6	1.160	0210	$2.1 \int 2$	2.3 516	3.1 10	1.3 \(\)32
1.152	$\begin{array}{c} 6 \\ 5 \cdot 1 \int 2 \end{array}$	1·284 1·389	·0210 ·0227	2.354	2.3 58	3·3∫8 3·5∫8	$1.3 \int 16$ $1.9 \int 32$
1.5∫8 1.3∫4	5.	1.490	0227	2·15 ∫ 16 3·3 ∫ 16	2.9 ∫ 16 2.3 ∫ 4	3.29∫32	1:358
1.758	5.	1.615	0250	3.13∫32	$2.15 \int 16$	4.3∫16	1·15 ∫ 32
2.	4.152	1.712	.0280	3.5 \(\)8	3.158	4.7 516	1.9516
2.154	4.152	1.962	.0280	4.1516	3.152	4.31∫32	1.354
2.152	4	2.175	·0310	4.152	3.758	5.152	1.15 16
2.3 \(\) 4	4.	2.425	·0310	4.29 \(\) 32	4.154	6.	2.158
3.	3.152	2.628	.0357	5.3∫8	4.5∫8	6.9516	2.5 16
3.154	3.152	2.878	0357	5.354	5.	7.158	2.1 52
$\frac{3.1 \int 2}{2.2 \text{cs}}$	3.1 ∫ 4	3·100 3·317	·0384 ·0410	6.7 5 64	5.358	7.5 58	2·11 £16 2·7 £8
3·3∫4 4·	3.	3.566	0410	6.5 \in 8 7:3 \in 64	5·3 £ 6·1 £ 8	8·3 <i>5</i> 16 8·11 <i>5</i> 16	3.1 16
4.154	2.758	3.798	.0435	7.152	$6.1 \int 2$	9.154	3.1.54
4.152	$2.3 \int 4$	4.027	•0460	-7.31 532	6.7 58	9.354	3.7 16
4.354	2.5 \(\) 8	4.255	•0480	8.378	7.154	10.9 532	3.5 \(\) 8
5	2.152.	4.480	0500-	8.13 € 16	7.558	10.13 ∫ 16	3.13∫16
5.1 54	2.152	4.730	.0500	9.154	8.	11.358	4.
5.152	2.358	4.953	•0526	9.11 516	8.358	11.29 532	4·3 £16
5.354	2.3 58	5.203	0526	10.158	8.354	12.7 516	4.358
6.	2.154	5.423	•0555	10.9 516	9.158	12.9 \$ 10	4. 9∫16

Mr. Whitworth makes the angle of the threads 55°, with round top and bottom; whilst William Sellers makes the angle of the thread 60°, with flat top and bottom, and of the following proportions, which are recommended by a special committee appointed by the Franklin Institute of Philadelphia. For full information see Journal of the Institute, May, 1864, and Jan., 1865.

Notation of letters. All dimensions in inches.

D =outside diameter of screw. d =diameter of root of thread, or of hole in the nut.

p = pitch of screw.

t =number of threads per inch. f =flat top and bottom.

or bolthead.

$$p = \frac{\sqrt{16\ D + 10} - 2.909}{16.64}.$$

i =inside diameter of hexagon, or side of square nut or bolthead.

s =diagonal of square nut or bolthead. h =height of rough or unfinished bolthead.

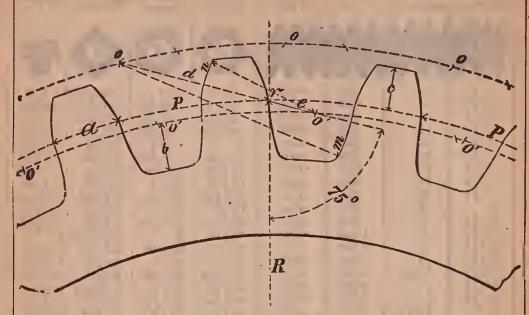
The height of finished nut or bolto = outside diameter of hexagon nut head is made equal to the diameter D of the screw.*

$$t = \frac{1}{p} \cdot \qquad \qquad s = 1.414 \ i.$$

$$d = D - \frac{1 \cdot 299}{t}$$
 $i = \frac{3 D}{2} + \frac{1}{8}$ $o = 1 \cdot 155 i$. $f = \frac{p}{8}$

* Whitworth makes the height of the nut about half the hexagon diameter v.





Letters denote.

P = pitch,—the distances between the centres of two teeth in the pitch circle.

D = diameter

C = circumference

of the wheel. M = number of teeth

N = number of revolutions

d = diameter

c = circumference

m = number of teeth

n = number of revolutions

of the pinion.

Pitch
$$\begin{cases} P = \frac{C}{M} & \cdot & 1 \\ P = \frac{\pi D}{M} & \cdot & 2 \end{cases}$$
 Circum.
$$\begin{cases} C = PM \\ C = \pi D \end{cases}$$
 No. of teeth
$$\begin{cases} M = \frac{C}{P} & \cdot & 3 \\ M = \frac{\pi D}{P} & \cdot & 4 \end{cases}$$
 Diameter
$$\begin{cases} D = \frac{PM}{\pi} \\ D = \frac{C}{\pi} \end{cases}$$

$$D:d=C:c=M:m=n:N$$

Example 1. A wheel of D=40 inches in diameter, is to have M=75 teeth. Required the pitch P=?

Formula 2. Pitch
$$P = \frac{3.14 \times 40}{75} = 1.66$$
 inches nearly.

Example 2. The pitch of teeth in a wheel, is to be P=1.71 inches, and having M=48 teeth. Required the diameter D=? of the wheel.

Formula 7. Diam.
$$D - \frac{1.71 \times 48}{3.14} = 26.14$$
 in. of the pitch circle

Construction of Teeth for Wheels.

Draw the radius R r, and pitch circle P P. Through r draw the line o o at an angle of 75° to the radius R r.

Half the angle between two teeth in the pinion,
$$V = \frac{180}{M}$$
.

 $D: d = sin. \ V: sin. \ v.$

Diameter of the
$$\begin{cases} \text{wheel, } D = \frac{d \ sin. \ V}{sin. \ v}. & \cdot & \cdot & \cdot & 3 \\ \text{pinion, } d = \frac{D \ sin. \ v}{sin. \ V}. & \cdot & \cdot & \cdot & 4 \end{cases}$$

Pitch (chord) of teeth $\{$ wheel, $P = D \sin v$. - 5 in the pitch circle $\{$ pinion, $P = d \sin V$. - 6

Approximate pitch in the wheel P = 0.028 D. • 7

Number of teeth about
$$\begin{cases} \text{wheel, } M = \frac{3\cdot 14D}{P}. \\ \text{pinion, } m = \frac{dM}{D}. \end{cases}$$

Thickness of tooth,
$$a = 0.46 P^*$$
 • • • 10

Bottom clearance, b = 0.4 P. • • • 11

Depth to pitch line,
$$c = 0.3 P.$$
 • • 12

Distance
$$r \ o_r = \frac{P(m+6)}{2(m-11)}$$
. • • • 13

* If a wheel of more than 80 teeth is to gear a pinion of less than 20 teeth, and the wheel and pinion are of the same kind of materials; take the thickness

of the tooth in the
$$\begin{cases} \text{wheel, } a = P\left(0.42 + \frac{m}{700}\right) & . \\ \text{pinion, } a = 0.5 P\left(1 - \frac{m}{350}\right). \end{cases}$$

A rack is to be considered as a wheel of 200 teeth.

Example with Plate I.

Example. A wheel of D=48 inches diameter is to gear a pinion about 8 revolutions to 1. Required a complete construction of the gearing?

Approximate pitch
$$P = 0.028 \times 48 = 1.34$$
 in.

Number of teeth in the
$$\begin{cases} \text{wheel, } M = \frac{3.14 \times 48}{1.34} = 112. \\ \text{pinion. } m = \frac{112}{8} = 14 \end{cases} . \qquad 9$$

Half the angle between two teeth in the pinion
$$V = \frac{180}{112} = 1^{\circ}36'$$
. $sin=0.028$. 1

pinion $V = \frac{180}{14} = 12.51'$. $sin=0.2224$. 2

Diameter of pinion
$$d = \frac{48 \times 0.028}{0.2224} = 6.043 \text{ in.}$$
 4

Draw the pitch circle for the wheel and pinion so that they tangent one an other at r on a straight line between the centres of the circles.

Pitch in the gearing
$$P = 48 \times 0.028 = 1.344$$
 in.

Take this chordial pitch in a pair of compasses, and set it off in the pitch circles.

Thickness of tooth
$$\begin{cases} \text{wheel } a = 1.344 \left(0.42 + \frac{14}{700}\right) = 0.592 \text{in.} & 15 \\ \text{pinion } a = 0.5 \times 1.344 \left(1 - \frac{14}{350}\right) = 0.645 \text{ in.} & 16 \end{cases}$$

Set off the thickness of tooth in the corresponding pitch circles.

Bottom clearance
$$b = 0.4 \times 1.344 = 0.5376$$
 in. - 11

Depth to pitch line
$$c = 0.3 \cdot 1.344 = 0.4032$$
 in. • 12

Distances
$$r$$
 o and c d = $\frac{1.344(112+6)}{2(112-11)} = 0.7851$ in. - 13 c e = $0.11 \times 1.344 \sqrt{112} = 0.7126$ in. 14

Set off these distances on the line o o' from r,-d beyond and c within the pitch circle for the wheel; then o is the centre and o m radius for the flank m. o' the centre and o' n radius for the face n. Draw circles through o and o' concentric with the pitch circle of the wheel.

Proceed with the pinion similar as the wheel

On the plate is a scale of inches and decimals, which will be convenient for the above measurements.

Gearing. Plate 1. J.W.Nystrom



On the Strength of Teeth in Cast-iron Wheels.

P = pitch, a = thickness, and h = face of teeth in inches.

S=strain in pounds, H=horsepower, and V=velocity in feet per second in the pitch circle.

Pitch P.	Thickness a.	Face h.
$P = \frac{S}{1000}$	$a = \frac{S}{1000 h}.$	$h = \frac{S}{1000 \ a}.$
460 h	1000 h	
$P = \frac{1.2 \ H}{h \ V}.$	$a = \frac{0.55 H}{h V}.$	$h = \frac{1.2 H}{P V}$
h V	h V	PV
Strain S.	Horsepower H.	Velocity V.
$S = 1000 \ a \ h.$	$H=\frac{h \ a \ V}{0.55}$.	$V = \frac{0.55 \ H}{h \ a}.$
2000 4 700		
$S = 460 \ P \ h.$	$H=\frac{h\ P\ V}{1.2}.$	$V = \frac{1.2 H}{h P}$
	1.2	h P

The face h is generally made = 2.5 P = 5.435 a. a = 0.46 P, and P = 2.1739 a.

To Find the Diameter of Axles and Shaft.

Letters denote,

d = diameter in inches, in the bearing; and the length of the bearing 1.5d. W = weight in pounds, acting in the bearing.

Water-Wheels.
$$\begin{cases} d = \frac{\sqrt{W}}{18} \text{ of cast iron.} & \text{Common Machinery in good} \\ d = \frac{\sqrt{W}}{21} \text{ of wrought iron.} & \text{order.} \end{cases} \begin{cases} d = \frac{\sqrt{W}}{24} \text{ of cast iron.} \\ d = \frac{\sqrt{W}}{28} \text{ of wrought iron.} \end{cases}$$

Example 1. A water-wheel weighs 58,680 pounds, and is supported in two bearings. Required the diameter of the wheel axles? The weight acting in each bearing will be 58680:2=29340 pounds, and

diameter
$$d = \frac{\sqrt{29340}}{21} = 8.15$$
 inches of wrought iron.

Example 2. Fig. 226, page 307. Required the diameter of the axle in the wheel, when the weights P+Q=4864 pounds? If the wheel is supported in two bearings W=4864:2=2432 pounds.

diameter
$$d = \frac{\sqrt{2432}}{28} = 1.76$$
 inches of wrought iron. (Continued on page 298.)

STANDARD PITCH OF GEAR-WHEELS.

The difficulty in finding cog-wheel patterns made at different establishments to gear correctly into one another is well known, and much time and money is lost for the want of a standard scale of pitch in gearings. The pitch of teeth in a cog-wheel should always be understood to mean the chord-pitch, and not the arc-pitch, because equal arc-pitch in wheels of widely different diameters will not gear well.

The pitch of gear-wheels should be even measures of the inch and binary fractions thereof, and the number of teeth and diameter of pitch-circle should

be regulated accordingly.

The following pitch-table is offered or proposed as standard, in which the first column varies with sixteenths of an inch from 0 to 1 inch, with eighths from 1 to 3 inches, and with quarters from 3 to 7 inches. The pitch of wheels from 1 to 7 inches should not be made of any other measure than of those in the table, and the fractions with the most decimals should be avoided as much as possible:

Standard Pitch for Gear-Wheels.

Pitch from 1 to 1 inch.	Pitch from 1 to 3 inches.	Pitch from 3 to 7 inches.
Binary Decimals.	1 in. Decimals.	3 in. Decimals.
$\frac{1}{16} = 0.0625$	$1\frac{1}{8} = 1.125$	$3\frac{1}{4} == 3.25$
$\frac{1}{8} = 0.125$	$1\frac{1}{4} = 1.25$	$3\frac{1}{2} = 3.5$
$\frac{3}{16} = 0.1875$ $\frac{1}{4} = 0.25$	$1\frac{3}{8} = 1.375$	$3\frac{1}{4} = 3.75$
	$1\frac{1}{2} = 1.5$	4 in.
$\frac{5}{16} = 0.3125$ $\frac{3}{2} = 0.375$	$1\frac{5}{8} = 1.625$ $1\frac{3}{4} = 1.75$	$\begin{array}{c} 4\frac{1}{4} = 4.25 \\ 4\frac{1}{9} = 4.5 \end{array}$
$\frac{8}{76} = 0.4375$	$1\frac{7}{8} = 1.875$	$4\frac{3}{4} = 4.75$
$\frac{1}{1} = 0.5$	2 in.	5 in.
$\frac{9}{16} = 0.5625$	$2\frac{1}{8} = 2.125$	$5\frac{1}{4} = 5.25$
$\frac{5}{16} = 0.625$ $\frac{16}{16} = 0.6875$	$ \begin{array}{c} 2\frac{1}{4} = 2.25 \\ 2\frac{3}{8} = 2.375 \end{array} $	$ 5\frac{3}{4} = 5.5 5\frac{3}{4} = 5.75 $
$\frac{16}{3} = 0.75$	$2\frac{1}{9} = 2.513$ $2\frac{1}{9} = 2.5$	6 in.
$\frac{13}{16} = 0.8125$	$2\frac{5}{8} = 2.625$	$6\frac{1}{4} = 6.25$
$\frac{7}{8} = 0.875$	$2\frac{3}{4} = 2.75$	$6\frac{1}{2} = 6.5$
$\frac{15}{16} = 0.9375$	$2\frac{7}{8} = 2.875$ 3 in.	$6\frac{3}{7} = 6.75$
1 in.	9 In.	7 111.

The width of the face should be two and a half the pitch.

The following table contains the proportions of number of teeth, diameter, and chord-pitch of wheels from 6 to 250 teeth. The first column is the number of teeth, the second is the diameter when the chord-pitch is unit, and the third column is the chord-pitch when the diameter is the unit.

Example 1.—What diameter is required for a wheel of 45 teeth and chord-pitch 13 inches? Opposite 45 teeth we find the diameter.

 $14.3356 \times 1.75 = 25.0874$ inches in pitch-line.

Example 2.—A wheel of 62.35 inches diameter in the pitch-line has 198 teeth. What is the chord-pitch?

Pitch = $62.35 \times 0.015866 = 0.989$ of an inch.

That wheel will not work with the standard gear.

The number of teeth multiplied by the pitch gives the length of the pitch-polygon and *not* the pitch-circle. The difference between the length of the two pitch-lines is greater the less number of teeth in the wheels. For 250 teeth and one-inch pitch the difference is only $\tau \sigma_{000}^{2}$ part of an inch in the whole pitch-line.

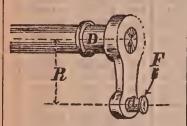
For properly-constructed *cut*-gearing there should be no clearance between the teeth, as shown in Plate I., but the thickness a of the teeth should be half the pitch.

$ \begin{array}{c c c c c c c c c c c c c c c c c c c $												
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$		Diam	Ditab		Diam	7314 - 3		7.				
6 2.0000 50000 66 21.016 0.0478 126 40.111 .02493 186 59.28 10.689 8 2.6131 .38268 68 21.652 .04618 128 40.748 .02454 188 59.845 10.671 19 2 .02928 .31202 69 21.970 .04552 129 41.066 .02454 188 59.845 10.671 19 2 .02928 .3261 .30902 70 22.289 0.4486 130 44.384 .02416 190 60.482 .01653 11 3.5490 .28177 71 22.607 .04423 131 41.702 .02380 192 61.118 .01653 13 44.785 .23932 73 23.243 .04507 133 42.330 .02362 193 61.436 .01628 14 4.4840 .22252 74 28.562 .04618 132 42.021 .02380 192 61.118 .01653 15 6 6 6 51.255 .0150 15 6 51.255 .015	.सं		FILCH	.4		Piten			Pitch	, d		Pitch
6 2.0000 50000 66 21.016 0.0478 126 40.111 .02493 186 59.28 10.689 8 2.6131 .38268 68 21.652 .04618 128 40.748 .02454 188 59.845 10.671 19 2 .02928 .31202 69 21.970 .04552 129 41.066 .02454 188 59.845 10.671 19 2 .02928 .3261 .30902 70 22.289 0.4486 130 44.384 .02416 190 60.482 .01653 11 3.5490 .28177 71 22.607 .04423 131 41.702 .02380 192 61.118 .01653 13 44.785 .23932 73 23.243 .04507 133 42.330 .02362 193 61.436 .01628 14 4.4840 .22252 74 28.562 .04618 132 42.021 .02380 192 61.118 .01653 15 6 6 6 51.255 .0150 15 6 51.255 .015	No Set No	when	when	ee N		when	No		when	No		when
7 2.3068 .43358 67 21.334 .04687 127 40.429 .02454 188 59.845 .01680 9 2.9238 .31202 69 21.970 .04552 129 41.066 .02451 188 60.163 .01662 10 3.2361 .30902 70 22.289 .04486 130 41.384 .02416 190 60.820 .01662 11 3.5490 .28177 71 22.697 .04423 131 41.762 .02380 19 61.118 .01662 12 3.8367 .25882 72 22.925 .04481 133 42.921 .02380 193 61.118 .01666 14 4.4940 .22257 74 22.562 .04242 134 42.657 .02344 194 61.755 .01619 16 6.7568 13830 40 138 42.94 .0211 196 62.391 .0163 18 5.7588<	1	P=1.	D=1.	H	P=1.	D=1.	T	P=1.	D=1.	E	P=1.	D=1.
7 2.3068 .43358 67 21.334 .04687 127 40.429 .02454 188 59.845 .01680 9 2.9238 .31202 69 21.970 .04552 129 41.066 .02451 188 60.163 .01662 10 3.2361 .30902 70 22.289 .04486 130 41.384 .02416 190 60.820 .01662 11 3.5490 .28177 71 22.697 .04423 131 41.762 .02380 19 61.118 .01662 12 3.8367 .25882 72 22.925 .04481 133 42.921 .02380 193 61.118 .01666 14 4.4940 .22257 74 22.562 .04242 134 42.657 .02344 194 61.755 .01619 16 6.7568 13830 40 138 42.94 .0211 196 62.391 .0163 18 5.7588<				-111								
7 2.3068 43358 67 21.334 .04687 127 40.429 .02454 188 59,827 .01680 9 2.9238 .34202 69 21.970 .04552 129 41.066 .02451 188 60.163 .01662 11 3.5490 .28177 71 22.890 .04861 130 41.884 .02416 190 60.896 .01632 11 3.5490 .28177 71 22.890 .04861 132 42.021 .02380 193 61.118 .01632 12 3.837 .25882 72 22.925 .04242 134 42.657 .02341 194 60.755 .01636 61.118 .0166 6.118 .01636 61.118 .0166 61.118 .0166 62.919 .01636 62.978 .01619 6.0756 .0241 .01636 82.94 .02210 196 62.931 .01603 84.94 .02210 196 62.346 .01638	6	2.0000	.50000	66	21.016	.04758	126	40.111	.02493	186	59.208	.01689
8 2.6131 ,38268		2.3068		67								
10						.04618	128					
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$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	55	17.517	.05709	115	36.610	.02731	175	55.707	.01795	235	74.805	.01337
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63 20.062 .04982 123 39.156 .02554 183 58.253 .01717 243 77.351 .01293 64 20.380 .04907 124 39.475 .02533 184 58.572 .01707 244 77.670 .01287												
64 20.380 .04907 124 39.475 .02533 184 58.572 .01707 244 77.670 .01287												
65 20.698 .04831 125 39.793 .02513 185 58.890 .01698 245 77.988 .01282				124	39.475	.02533	184	58.572	.01707	244	77.670	.01287
	65	20.698	.04831	125	39.793	.02513	185	58.890	.01698	245	77.988	.01282
												V

Example 3. The pressure on the steam piston, in a walking boam engine is 25000 pounds. Required the diameter of the beam journals?

diameter
$$d = \frac{\sqrt{25000}}{28} = 5.64$$
 inches the centre one.
$$d = \frac{\sqrt{12500}}{28} = 4$$
 inches at the ends.

In this example it is supposed that the beam is worked by a fork connecting rod.

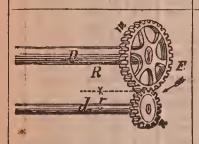


$$D = \frac{\sqrt[3]{FR}}{4} = 5\sqrt[3]{\frac{\overline{H}}{n}}$$

D = inches wrought iron.

R = radius of crank in feet.

F = force from the steam piston, lbs.



$$D: d = \sqrt[3]{R}: \sqrt[3]{r}$$

$$D = 4.35 \sqrt[3]{\frac{\overline{H}}{n}}$$

H =horse-power transmitted.

n = number revolutions per minute.

When an axle or shaft not only serves as a fulcrum, but effect is transmitted by the act of twisting it, the diameter is to be calculated as follow.

Example 4. The pressure on the piston in a steam engine is F=45,600 pounds, applied direct on a crank of R=3 feet radius. Required the diameter of the shaft and crank pin?

Diameter of the shaft $D = \frac{\sqrt[3]{45600 \times 3}}{4} = 12.9$ inches.

Diameter of the crank pin $d = \frac{\sqrt{45600}}{28} = 7.63$ inches.

Example 5. A steam engine of 368 horses is to make 32 revolutions per minute. Required the diameter of the main shaft?

Diameter
$$D = 5 \sqrt[3]{\frac{368}{32}} = 114$$
 inches.

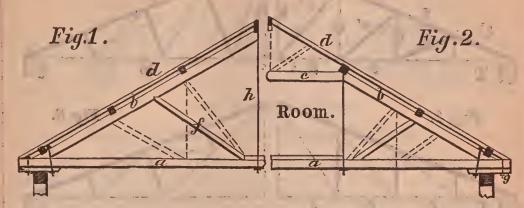
Example 6. A cog wheel of R=6.5 feet radius is to gear with a pinion of r=1.25 feet radius, and to transmit an effect of 231 horses with 42 revolutions per minute. Required the diameter of the wheel and pinion shafts? The force F is aeting uniformly at the periphery.

Diameter of wheel shaft D = 4.35 $\sqrt[3]{\frac{231}{42}} = 7.66$ inches

$$D: d = \sqrt[3]{R}: \sqrt[3]{r}$$

Diameter of pinion shaft $d = 7.66 \sqrt[3]{\frac{1.25}{6.5}} = 4.41$ inches.

ROOFS OF WOOD AND IRON.



The Figs. 1 and 2 illustrate the common form of wooden roofs, as constructed over spans of from 30 to 80 feet. When the span exceeds 60 feet, a proportionate number of struts and tie-rods must be inserted, as shown by the dotted lines, or as illustrated for iron roofs.

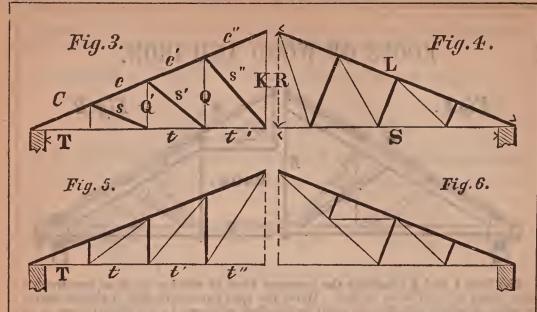
Table of Timber Dimensions, in Inches, for Roofs over Spans from 30 to 80 feet.

					Span in feet.					
Name of timbers.		30	35	40	45	50	55	60	70	80
Tie-beams,	a	5×6	6×7	$\dot{6} \times 8$	7×8	8×9	8×12	9×11	10×11	10×12
									9×10	
Collar-beams	c	5×5	5×6	6×7	7×7	8×8	8× 9	9×9	9×10	10×11
Com. rafter,	d	2×5	2×5	2×6	2×6	2×6	2×7	2×7	$2\frac{1}{2} \times 8$	3×9
Purlins, .								6×9		
Struts,	F	3×4	3×5	3×6	4×7	4×8	5× 8	5× 9	6× 9	6×9
King's rod,	h	1	1	1	118	11	13	11/2	13	2
Bolts,		34	34	34	34	7 8	1	$1\frac{1}{8}$	$1\frac{1}{4}$	13/8

Load on Roofs in Pounds per Square Foot, exclusive of Framing.

Lead covering, 8	Tiles, 9 to 16
Zinc covering, 2 Corrugated Iron, 3.5	Boarding, # thick, . 3 Boarding, 1 thick, . 6
Slates, 10	Pressure of wind, . 40

In high latitudes the roofs may be covered with snow, which makes a pressure of 10 pounds per square foot per foot of depth of the snow.



STRAIN ON ROOFS.

The above figures illustrate four different kinds of pointed iron roofs, of which figure 3 is most in use.

FINE LINES IN TENSION AND THICK LINES IN COMPRESSION. Notation of Letters.

L =length of principal rafter.

R = rise of roof above centre of tierod, which is generally one-fifth of the span.

S = half the span, or one-half the length of tie-rod between support on the walls.

N= number of bays or divisions in the whole span, which is 8 in the diagram.

s, s' and s'' = compression on the corresponding struts.

W= load, uniformly distributed on the rafter, including weight of framing.

C = compression at the end of principal rafter.

T = tension at the end of tie-rod.

c, c' and c" = compressions between the corresponding divisions of the rafter.

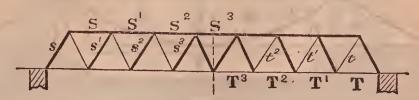
t and t" = tensions between the corresponding divisions of the tierod.

The formulas will answer for any units of weight and measure.

Compression on Principal Rafter. Tension on Tierod. Tension on King and Queen Rods. $C = \frac{L \ W}{2R}$. $T = \frac{WS}{2R}$. $K = \frac{4 \ W}{N}$. $S = \frac{4 \ W}{N}$. $S = \frac{4 \ W}{N}$. $S = \frac{4 \ W}{N}$. $S = \frac{4 \ W}{N}$. $S = \frac{4 \ W}{N}$. $S = \frac{4 \ W}{N}$. $S = \frac{4 \ W}{N}$. $S = \frac{4 \ W}{N}$. $S = \frac{4 \ W}{N}$. $S = \frac{4 \ W}{N}$. $S = \frac{4 \ W}{N}$. $S = \frac{4 \ W}{N}$. $S = \frac{4 \ W}{N}$. $S = \frac{4 \ W}{N}$. $S = \frac{4 \ W}{N}$. $S = \frac{4 \ W}{N}$. $S = \frac{4 \ W}{N}$. $S = \frac{4 \ W}{N}$. $S = \frac{4 \ W}{N}$.

The principals to be placed not more than 7 feet apart.

BRIDGES.



The Warren Girder.

FINE LINES IN TENSION AND THICK LINES IN COMPRESSION.

The Warren girder consists of fifteen equilateral triangles formed by the trusses and ties, which make eight divisions or bays in the span.

The depth of the girder is 0.10825 of the span.

The load uniformly distributed on each girder, multiplied by the tabular number, will be the strain on the corresponding part.

	Parts in C	ompression	n.	Parts in Tension.					
$S \\ 0.5 \\ T$	$\left \begin{array}{c}S^1\\0.875\\T^1\end{array}\right $	$egin{array}{c} S^2 \ 1.125 \ T^2 \ \end{array}$	$egin{array}{c} S^3 \ 1.25 \ T^3 \end{array}$	0.8 8	$\begin{bmatrix} t^1 \\ 0.6 \\ s^1 \end{bmatrix}$	$\begin{array}{ c c } & t^2 \\ 0.4 \\ & s^2 \end{array}$	$\begin{bmatrix} t^3 \\ 0.2 \\ s^3 \end{bmatrix}$		
	Bottom	Tie-rod.		Trusses.					
-	Parts in	Tension.		Parts in Compression.					

Weight of one pair of Warren's Girders in tons,

for a single track of railway on the top or on the bottom (approximate).

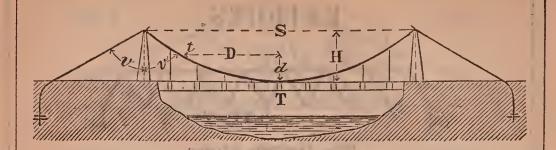
On		Span of the girder in feet.												
the	50	60	70	80	90	100	110	120	130	140	150	160		
Top,	11	15	18	23	27	32	38	44	51 64	58 72	66	75		
Bottom,	15	19	24	29	35	41	48	56	07	12	80	89		

Table of Dimensions in inches of Rolled Iron,

for roofs on spans from 30 to 80 feet (figures 3 to 6, page 300).

Name of			S	pan in feet			
iron.		30	40	50	60	70	80
Rafter T-iron,	L	24×2½×½	$3\frac{1}{8}\times3\times\frac{1}{8}$	$4\times3\frac{1}{2}\times\frac{5}{8}$	5×4½×₹	$5\frac{1}{2}\times5\times\frac{3}{4}$	6×6×3
Struts T-iron,	3	$2\frac{1}{9} \times 2\frac{1}{9} \times \frac{3}{8}$	$3\times2\frac{1}{9}\times\frac{1}{9}$	3×3×5 8	4 ×4× ⁵ / ₈	$4\frac{1}{9}\times4\frac{1}{9}\times\frac{5}{8}$	5×4½×¾
King bolt,	K	1	$1\frac{1}{4}$	18	$1\frac{1}{2}$	15/8	13
Queen bolt, {	Q	2	<u> 7</u> 8	1	11/8	11/4	13
G.110011 2010, {	Q'	<u>5</u>	3	7 B	1	11/8	$1\frac{1}{4}$
Tie-rod, {	T	1 ½	13	$1\frac{1}{2}$	$1\frac{5}{8}$	13	17/8
110-100,	t'	1	11/8	11/4	13	$1\frac{1}{2}$	15/8
Weight, lbs.,		1500	3000	4800	7000	9550	12400

The last line shows the approximate weight in pounds of each principal when the rise of the roof is 0.2 of the span.



SUSPENSION BRIDGES.

Notation of Letters.

W = total load on the bridge.

T =tension on the chain in the centre.

t = tension at any point of distance,

D, from the centre.

t' = tension at abutments.

S = span.

L = length of chain between the

H = versed sine, or height of abutments above centre of chain.

D and d = co-ordinates for any point of the chain.

v = angle of suspension at abutments.
 (The angle of the counter-chain ought to be equal to that of suspension.)

The formulas will answer for any system of weights and measures.

$$d = \frac{HD^2}{(\frac{1}{2}S)^2}.$$

 $T = \frac{1}{2}W \cot v$.

$$t = T\sqrt{\left(\frac{2d}{D}\right)^2 + 1}.$$

$$T = \frac{WS}{8H}$$

$$H = \frac{WS}{8T}$$

$$H = \frac{S}{13}$$
, generally.

$$\cot x = \frac{4H}{S}.$$

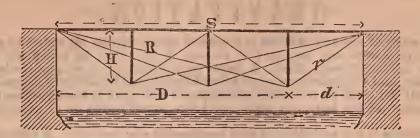
$$-L = \frac{2}{3}(S + \sqrt{0.25S^2 + 9H^2})$$

$$t' = \frac{W}{2} \cot v \sqrt{\left(\frac{4H}{S}\right)^2 + 1}$$

$$W = \frac{2t' \sin x}{\sqrt{\left(\frac{4H}{S}\right)^2 + 1}}$$

$$t' = \frac{WS}{8H} \sqrt{\left(\frac{4H}{S}\right)^2 + 1}.$$

$$W = \frac{8Ht'}{S} \sqrt{\left(\frac{4H}{S}\right)^2 + 1}$$



BOLLMAN'S AMERICAN TRUSS BRIDGES.

Notation of Letters.

 $W = \text{total load uniformly distributed on } \mid R \text{ and } r = \text{lengths of tension and coun-}$ the bridge.

w =load on each point of suspension. S = span.

D and d = distances from abutments Aand B to point of suspension.

A and a = cross areas of the tension and counter-tension rods in square inches.

ter-tension rods.

H = depth of truss, which is usuallyone-seventh of the span.

N = number of points of suspension. T and t = tensions on the rods R and rrespectively.

C =compression on the top at centre.

These formulas will answer for any system of weights and measures.

$$w = \frac{W}{N}$$
 $T = \frac{w D R}{SH}$ $t = \frac{w d r}{SH}$ $C = \frac{S W}{8H}$

When T and t are tons, A and a =square inches, D, d, S, H, R and r =feet,

$$A = \frac{WDR}{5NSH}$$
 $a = \frac{Wdr}{5NSH}$ $W = \frac{5aNSH}{dr}$ $W = \frac{5ANSH}{DR}$

STEAM HAMMER.

A heavy steam hammer with short fall produces a better forging than a light hammer with a high fall, although the dynamical momentum may be the same in

both cases. This is accounted for by the inertia of the ingot forged.

The effect of blows of a heavy hammer and short fall will penetrate through the metal, and nearly with the same effect on the anvil side, while a light hammer and high fall will affect the metal on or near the surface of the blow, because most of the momentum is in the latter case discharged in the inertia of the ingot forged. In forging a large shaft, it is generally piled up with iron bars sometimes rolled into a segment form to suit the pile. When placed under the hammer in a welding heat, very light and gentle blows are first given, then the momentum of a light hammer may be discharged in the bars nearest to the blow, while a heavy hammer will squeeze the whole mass together throughout, and a sound welding will be produced.

The additional expense of a heavy hammer is fully compensated by the waste of labor and materials under a small one. I have often seen, in broken shafts, the bars in the centre as clear and unwelded as when first piled, which is a sure indication that the shaft has been forged by a too light hammer. In crank-shafts for propeller engines, forged under a light hammer, when brought to the machineshop the best part of the metal is worked away by planing and turning, and the poorest left for the engine; but if forged under a leavy hammer, the difference in quality of metal will not be so great.

Cases of this kind are well known in the United States navy.

Weight of Steam Hammers.

The weight of a steam hammer in pounds should be at least eighty times the square of the diameter of the shaft in inches.

GRAVITATION.

Gravity or Gravitation is a mutual faculty which all bodies in nature possess, to attract one another; or Gravity is the force by which all bodies tend to approach each other. A large body attracting a comparatively very small one, and their distance apart being inconsiderable, the force of gravity iu the small body will be very sensible compared with that in the large one; such is the case with the body, our earth, attracting small bodies on or near her surface.

Gravitation is not periodical, it acts continually ever and ever. A body placed unsupported at a distance from the earth, the force of gravity is instantly operating to draw it down, and then we say, "the body fell down" If it were possible to withdraw the attraction between the body and the earth, it would not fall down, but remain unsupported in the space where it was placed; -giving the body a motion upwards it would continue that, and never come back to the

earth again.

Law of Gravity.

The force of Gravity is proportional to the mass of the attracting bodies, and inverse as the square of their distance apart.

This law was discovered by Sir Isaac Newton. It is this law that supports the condition of the whole universe, and enables us to calculate the distances, mo-

tions and masses, &c., of the heavenly bodies.

The unit or measure of force of gravity is assumed to be the velocity a falling body has attained at the end of the first second it falls; this unit is commonly denoted by the letter g; its value at the level of the sea in New York is $g = 32\cdot166$ feet per second, in vacuum. The space fallen through in the first second is $\frac{1}{2}g = 16.083$ feet.

This value augments with the latitude, and abates with the elevation above

the level of the sea.

l = latitude, h = height in feet above the level of the sea, and <math>r = radius of the earth in feet, at the given latitude l.

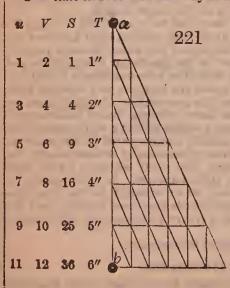
$$r = 20887510(1+0.00164 \cos .2l),$$

$$g = 32.16954(1 - 0.00284 \cos .2l) \left(1 - \frac{2h}{r}\right)$$

Letters denote.

S = the space in feet, which the falling body passes through in the time T. u = the space in feet, which the body falls in the Tth second.

V = velocity in feet per second, of the falling body at the end of the time T. T = time in seconds the body is falling.



The accompanying Diagram is a good illustration of the acceleration of a falling body. The body is supposed to fall from a to b, every small triangle represents the space 16.08 feet which the body falls in the first second; when the body has reached the line 3" seconds, it will be found that it has passed 9 triangles, and $9 \times 16.08 = 144.72$ feet the space which a body will fall in 3" seconds. The number of triangles between each line is the space u which the body has fallen in that second. Between 3" and 4" are 7 triangles and $7 \times 16.08 = 112.56$ feet, the space fallen through in the fourth sec-ond. Under the line 3" will be found 6 triangles, which represents the velocity V the body has obtained at the end of the third second or $6 \times 16.08 = 96.48$ feet per second. For every successive second the body will gain two triangles or $2 \times 16.08 = 32.16$ feet per second.

Formulas for Accelerated Motion.

$$V = g \ T = \frac{2 S}{T} = \sqrt{2g \ S} = 8.02 \sqrt{S}, \qquad 1.$$

$$S = \frac{g \ T^2}{2} = \frac{V \ T}{2} = \frac{V^2}{2g} = \frac{V^2}{64.33}, \qquad 2.$$

$$T = \frac{V}{g} = \frac{2 S}{V} = \sqrt{\frac{2 S}{g}} = \frac{\sqrt{S}}{4.01}, \qquad 3.$$

$$u = g(T - \frac{1}{2}), \qquad T = \frac{u}{g} + \frac{1}{4}, \qquad 4.$$

Example 1. A body is dropped at a height of 98 feet. What velocity will it have when it reaches the ground, and what time will it take to fall down?

Formula 1. $V = 8.02\sqrt{S} = 8.02\sqrt{98} = 79.39$ feet per second.

Formula 3.
$$T = \frac{\sqrt{8}}{4.01} = \frac{\sqrt{98}}{4.01} = 2.46 \text{ seconds.}$$

Example 2. A body was dropped at the opening of a hole in a rock, and reached the bottom after 3.5 seconds. How deep was the hole?

Formula 2.
$$S = \frac{g T^2}{2} = \frac{32.16 \times 3.5^2}{2} = 196.98$$
 feet.

Retarded Motion.

A body thrown up vertically will obtain inversely the same motion as when it falls down, because it is the same force that acts upon it, and causes retarded motion when it ascends, and accelerated motion when it descends.

V = the velocity at which the body starts to ascend.

v = velocity at the end of the time t.

T = time in seconds in which the body will ascend.

t =any time less than T.

S = height in feet to which the body will ascend.

s =the space it ascends in the time t.

Formulas for Retarded Motion.

$$v = V - gt = \frac{s}{t} - \frac{gt}{2}; \qquad . \qquad . \qquad . \qquad . \qquad . \qquad . \qquad .$$

$$s = Vt - \frac{gt^2}{2} = tv + \frac{gt^2}{2}; \qquad . \qquad . \qquad . \qquad . \qquad . \qquad . \qquad .$$

$$V = v + gt = \frac{s}{t} + \frac{gt}{2}; \qquad . \qquad . \qquad . \qquad . \qquad . \qquad .$$

$$t = \frac{V - v}{a} = \frac{V}{a} - \sqrt{\frac{V^2}{a^2} - \frac{2s}{a}}; \qquad . \qquad . \qquad . \qquad . \qquad . \qquad . \qquad . \qquad .$$

Formulas for T and S are the same as for accelerated motion.

Example 3. A ball starts to ascend with a velocity of 135 feet per second. At what velocity will it strike an object 60 feet above? Find the time t by the Formula 8.

$$t = \frac{135}{32.16} - \sqrt{\frac{135^2}{32.16^2} - \frac{2 \times 60}{32.16}} = 0.41 \text{ seconds},$$

until it strikes, and from Formula 5 we have

$$v = 135 - 32.16 \times 0.41 = 121.83$$
 feet per second.

Example 4. A ball thrown up vertically from a cannon, occupied 20 seconds, until it arrived at the same place it started from. How high up was the ball, and at what velocity did it start?

One-half of 20 = 10 seconds. Formula 2.

$$S = \frac{32.16 \times 10^2}{2} = 1608$$
 feet high.

$$V = 32.16 \times 10 = 321.6$$
 feet per second.

If a cannon-ball be shot from A, in the direction AB, at an angle BAC to the horizon, there are two forces acting on the ball at the same time, namely — the force of gunpowder, which would propel the ball uniformly in the direction AB, and the force of gravity, which only acts to draw the ball down at an accelerated motion; these two different (uniform and accelerated) motions will cause the ball to move in a curved line (Parabola) AaC. Fig. 225.

V = velocity of the ball at A. W = weight of the ball in pounds.

S = the greatest height of ball over the horizontal line $A\hat{C}$.

t = time from A to C, vià a. p = pounds of powder in the charge. <math>b = the distance from A to C, called horizontal range.

$$V = 2800 \sqrt{\frac{p}{W}}, \qquad p = \frac{W V^2}{7840000}, \qquad b = 87.06 \sin x \cos x \frac{p}{W}.$$

Example 5. The cannon being loaded sufficiently to give the ball a velocity of 900 feet per second, the angle $x = 45^{\circ}$. Required, the distance b = ? and the time t=?

$$b = \frac{900^2 \times \sin .45^\circ \times \cos .45^\circ}{32.16} = 1259 \text{ feet, the distance from } A \text{ to } C.$$

It will be observed that the distance b will be longest when the angle x is 45° , because the product of sine and cosine is greatest for that angle. $\sin .45^{\circ} \times \cos .$ $45^{\circ} = 0.5$.

Example 6. What time will it take for a ball to roll 38 feet on an inclined plane, angle $x = 12^{\circ} 20'$, and what velocity has it at 38 feet from the starting-

$$T = \sqrt{\frac{2S}{g \sin x}} = \sqrt{\frac{2 \times 38}{32.16 \times \sin .12^{\circ} \ 20'}} = 3.33 \text{ seconds.}$$

 $V = q T \sin x = 32.16 \times 3.33 \times \sin 12^{\circ} 20' = 22.8$ feet per second.

Resistance of Air to the Flight of Projectiles.

A = area of resistance of the projectile in square inches.

 ϕ = angle of resistance of the projectile, which for flat surfaces $\sin^2 \phi = 1$, for sphere $\sin^2 \phi = 0.5$.

For a pointed projectile of parabolic form, and when the ordinate is double the abscissa $\sin^2 \phi = 0.25$.

V = velocity of the projectile in feet per second.

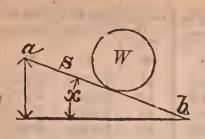
R = resistance to the projectile in pounds.

tile in pounds.
$$R = \frac{A V^2 \sin^2 \phi}{57000}.$$

Let T denote the time of flight in seconds, and W = weight in pounds of the

D = distance in feet which the projectile is retarded by resistance of air in the time T.

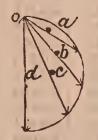
 $D = \frac{32.166RT^2}{2W} = \frac{16RT^2}{W}$.



$$\dot{r} = g \ T \sin x = \sqrt{2g \ S \sin x},$$

$$S = \frac{g \ T^{\bullet}}{2 \sin x} = \frac{\overline{r^2}}{2 \ g \sin x},$$

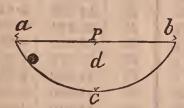
$$T = \frac{V}{g \sin x} = \sqrt{\frac{2S}{g \sin x}}$$



223.

A body will fall from o the distances a, b, c and d, in equal times.

$$T = \sqrt{\frac{2d}{g}}$$
.

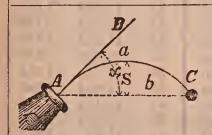


224.

A body will fall from a to b via c in the shortest time, if the curve is a Cycloid.

S=4d, the length of the Cycloid.

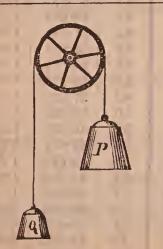
$$T = \pi \sqrt{\frac{d}{2g}} = \pi \sqrt{\frac{p}{2\pi g}}.$$



$$b = \frac{2V^2 \sin x \cos x}{g}$$

$$T = \frac{V \sin x}{\sigma},$$

$$S = \frac{V^2 \sin^{2}x}{2g}$$



$$S=grac{T^{2}}{2M}$$

$$S = g \quad 2M \qquad = 2g F$$

$$V = g T \frac{F}{M} = \sqrt{$$

$$T = \frac{V M}{g F} \qquad = \sqrt{\frac{2S M}{g F}},$$

$$F = \frac{V M}{g T}, \qquad = \frac{2S M}{g T^2},$$

$$M = P + Q$$
, and $F = P - Q$.

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Velo-								
csty	Space fall-	Time in	Velocity at the	Space fall- en through	Time in	Velocity at the	Space fall.	Time in seconds.
at the	en through	seconds.	end.	en urrouga	seconds.	end.	en intough	seconus.
V	S	\mathbf{T}	v	S	T	v	S	T
0.1	.00015	0.0031	5.1	.40388	0.158	11	1.8789	0.342
0.2	.00062	0.0062	5.2	•41987	0.162	12	2.0652	0.373
0.3	.00139	0.0093	5.3	•43618	0.165	13	2.6242	0.405
0.4	.00248	0.0124	5.4	•45279	0.168	14	3.0435	0.436
0.5	.00388	0.0155	5.5	•46972	0.171	15	3.4938	0.467
0.6	.00559	0.0187	5.6	•48695	0.174	16	3.9751	0.498
0.7	.00761	0.0218	5.7	.50450	0.177	17	4.4876	0.530
0.8	.00994	0.0230	5.8	•52236	0.181	18	5.0310	0.560
0.9	.01257	0.0280	5.9	.55057	0.184	19	5.6056	0.591
1.	.01552	0.0311	6.	.55900	0.187	20	6.2112	0.622
1.1	.01879	0.0342	6.1	.57779	0.190	21	6.8478	0.654
1.2	.02065	0.0373	6.2	•59689	0.193	22	7.5155	0.685
1.3	.02624	0.0404	6.3	·61630	0.196	23	8.2143	0.716
1.4	•03043	0.0436	6.4	63602	0.199	24	8.9441	0.747
1.5	.03493	0.0467	6.5	65606	0.202	25	9.7049	0.778
1.6	.03975	0.05	6.6	67639	0.205	26	10.497	0.810
1.7	.04487	0.052	6:7	69705	0.209	27	11.320	0.840
1.8	•05031	0.556	6.8	•71801	0.212	28	12.174	0.872
1.9	.05605	0.0591	6.9	.73928	0.215	29	13.059	0:903
2.	•06211	0.0623	7.	.76087	0.218	30	13.975	0.933
2.1	.06847	0.0654	7.1	.78276	0.221	31	14.922	0.965
2.2	.07515	0.0685	7.2	*80497	0.224	32	15.900	0.996
2.3	.08214	0.0717	7.3	*82748	0.227	33	16.910	1.025
2.4	•08944	0.0747	7.4	.85031	0.231	34	18.789	1.058
2.5	.09705	0.0780	7.5	*87344	0.234	35	19.022	1.091
2.6	•10497	0.0810	7.6	·89689	0.237	36	20.124	1.120
2.7	11320	0.0841	7.7	•92065	0.240	37 38	21.258	1.151
2.9	12174	0.0872	7·8 7·9	.94472 .96910	0.243	39	22.422	1·184 1·213
3.	·13059 ·13975	0·0903 0·0934	8.	•99379	$0.246 \\ 0.250$	40	23·618 24·844	1.243
3.1	13973	0.0966	8.1	1.0187	$0.250 \\ 0.253$	41	26.102	1.276
3.2	14922	0.0997	8.2	1.0441	0.256	42	27.391	1.308
3.3	·16910	0.1025	8.3	1.0697	0.259	43	28.57	1.338
3.4	18788	0.1059	8.4	1.0956	0.262	44	30.062	1.370
3.5	·19022	0.1092	8.5	1.1218	0.265	45	31.444	1.400
3.6	.20124	0.1121	8.6	1.1484	0.268	46	32.857	1.431
3.7	21257	0.1152	8.7	1.1753	0.271	47	34.301	1.463
3.8	•22422	0.1185	8.8	1.2015	0.274	48	35.776	1.495
3.9	•23618	0.1214	8.9	1.2299	0.278	49	37.282	1.525
1.	•24844	0.1246	9.	1.2577	0.281	50	38.820	1.555
4.1	·26102	0.1278	9.1	1.2858	0.283	51	40.388	1.588
4.3	•27391	0.1309	9.2	1.3143	0.287	52	41.987	1.619
4.3	.28571	0.1339	9.3	1.3430	0.290	53	43.618	1.650
4.4	*30062	0.1371	9.4	1.3720	0.293	54	45.279	1.680
4.5	·31444	0.1403	9.5	1.4041	0.296	55	46.972	1.711
4.6	·32857.	0.1433	9.6	1.4310	0.300	56	48.695	1.742
4.7	•34301	0.1465	9.7	1.4610	0.302	57	50.450	1.774
4.8	*35776	0.1496	9.8	1.4913	0.306	58	52.236	1.805
4.9	*37282	0.1526	9.9	1.5219	0.309	59	55.058	1.835
5.	*38820	0.1559	10	1.5528	0.312	60	55.900	1.868
				-				

DYNAMICS OF MASS AND WEIGHT MOVING BODIES.



Let a constant force, F, be applied to a body, W, free to move, then the body will start and continue with an accelerated velocity until the force ceases to act, when it will continue in the same direction with a uniform velocity equal to that of the final action of the force. Any force, however small, is able to set in motion any body free to move, or to bring to rest any moving body, however large.

The direction of the force F must pass through the centre of gravity of W,

otherwise the body will be set in rotation.

A force applied obliquely from space to the surface of the earth would change the axis of rotation, which is actually the case with meteors falling on the earth.

No force is required to maintain a uniform motion of a body free to move; but force is required to bring a body from rest into a uniform motion. If force is applied to maintain a body not free to move in uniform motion, such force is expended in overcoming the friction and resistance of the medium in which the body moves. A steamboat or a railway train in motion is thus suspended between the action of two opposite forces—namely, the driving force on the one side, and the friction and resistance on the other. When the opposite forces are equal, the motion will be uniform; and any change of velocity is due to a disparity between these opposing forces.

Mass means the real quantity of matter in a body. It is proportionate to

weight when compared in one locality.

The mass of a body is a constant quantity, whilst the weight varies with the force of attraction or gravity. A body weighed on a spring balance at the equator will weigh less than if weighed at the poles, because the radius of the earth is greater, and consequently the force of gravity is less at the equator.

A body weighing one hundred pounds at the surface of the earth would weigh

only twenty-five pounds at a height of 3956 miles (radius of the earth) above the

surface, whilst the mass of the body remains constant.

The weight of a body is inverse as the square of its distance from the centre of the earth when weighed above the surface; but if weighed below the surface, the weight will be only

$$w = \frac{Wr}{R}.$$

W = weight at the surface; w = weight below the surface; R = radius of theearth, and r =radius where the body is weighed.

A body weighed at a height h above the surface of the earth would weigh

$$w = \frac{WR^2}{(R+h)^2},$$

and the force of gravity, or acceleratrix g, at the height h, is

$$g = \frac{32.166R^2}{(R+h)^2}.$$

Therefore the mass M of a body is

$$M = \frac{W}{g}$$
, which is a constant quantity.

Below the surface of the earth the acceleratrix g is

$$g = \frac{32.166r}{R}.$$

Attraction of the Sun and Moon on the Earth.

Assuming the mean radius of the earth as a unit for the distances to the sun and to the moon, and the attraction in pounds per 100,000 pounds of material in the earth, then the data will be as follows:

Location of Attraction in the centre or ends of	Attracti	on of the	Distance	s to the
the diameter of the earth pointing to the sun or moon.	Sun.	Moon.	Sun.	Moon.
In the centre of the earth, or where the sun or moon is seen to set or rise,	11.3273	0.0769971	24000	60
On the surface of the earth nearest to the sun or moon,	11.3283	0.0794466	23999	59
On the surface of the earth farthest from the sun or moon.	11.3264	0.0744936	24001	61
	0.00190	0.0049530	2	2

It is these differences of attraction which, in co-operation with similar differences of centrifugal forces, cause the tidal waves of the ocean. Although the sun's attraction on the earth is one hundred and ninety-five times that of the moon, its difference of attraction in the diameter of the earth is only one-half that of the moon, for which reason the moon causes the highest tidal waves.

A weight of 100,000 pounds weighed on a spring balance at sunrise would weight only 100,000 — 11.328 = 99,988.67 pounds where the sun is in the zenith; and if the same weight is weighed at midnight in a latitude opposite the sun, it would weigh 100,011.328 pounds on the same spring balance. But when substances are weighed by weights, there will be no difference where they are weighed.

Dynamic Momentum in a body free to move is of two kinds—namely,

Momentum of time F T = M V momentum of motion.

A force multiplied by its time of action on a body free to move is the momentum of time, which is equal to the mass of the body multiplied by its uniform velocity after the force has ceased to act, the momentum of motion.

Vis-Viva, or *living force*, is a term intended to express the quantum of work concentrated in a moving mass, and is usually denoted by MV^2 , which is twice the true amount of work; but as there is no living force in a dead body, the term is improper and confusing. See Journal of the Franklin Institute for 1864 and 1865.

Moment of Inertia is another confused term not always properly understood. In substance it means work imparted to or given out by a revolving body. It is denoted by MR^2 , in which M = the mass, and R = radius of gyration.

Inertia in a body free to move is equal to the force applied to change its motion.

A force multiplied by the lever it acts upon is called static momentum, which is analogous to the force of inertia multiplied by the radius of gyration in a revolving body, which seems to have a better claim to be called moment of inertia.

A List of Confused Dynamical Terms,

which ought to be abolished in our school-books.

Quantity of motion.
Total quantity of work.
Actual total amount of work.
Virtual velocity.
Heat a mode of motion.

Rate of work (which is power).
Quantity of moving force in a body (inertia or work).
Vis-viva and principle of vis-viva.
Moment of inertia (if you please).

See Nystrom's Elements of Mechanics, which establishes strict precision in the meaning of dynamical terms, and abolishes the ideal vocabulary heretofore used in text-books on Mechanics. The subject of confusion in dynamical terms has been thoroughly discussed, and may now be considered exhausted.

Proper Dynamical Terms.

All the terms necessary in statics and dynamics are as follows:

Elements. Functions. Power, P = FV. Force = F. Velocity = V. Space, S = VT. Time = T. Work, W = F V T. Static momentum = Fl.Dynamic momentum, FT = MV.

These terms include all cases in dynamics, whether by mechanical force, gravity. uniform accelerated, retarded, straight or curved linear motion.

In the static momentum Fl, the lever l may mean radius of gyration in revolv-

ing bodies.

In irregular motion, V means the mean velocity in the line T.

Force is any action which can be expressed simply by weight, such as pressure, attraction, repulsion, gravity, inertia, exertion, cohesion, electricity, magnetism, strain, stress, strength, thrust, burden, load, squeeze, pull, push, resistance, compression, etc.

Power is any action of force and velocity, such as dynamic momentum of inertia, impetus, dynamic effect, traction, propulsion, impulsion, labor, etc.

Work is any action which includes the three simple elements force, velocity and time, such as energy, vis-vivæ, labor, throw, cast, haul, drag, draw, occupation, exercise, toiling, lift, raise, heave, cultivate, to tilt, etc.

The term effect is used in three senses—namely, effect of force, effect of power and

effect of work.

Much inconvenience has been experienced for the want of distinction between elements and functions in dynamics, and sufficient room cannot be allowed for a full explanation of the subject in this Pocket Book. In the Elements of Mechanics before mentioned the subject is fully elucidated.

The Work concentrated in a moving body is equal to the work expended in bestowing its motion, and is equal to the work required in bringing the body to rest, which is derived from the primitive formula FVT; but for accelerated motion V means the mean velocity in the time T, which is just one-half of the final velocity V, when the acceleratrix G or g is constant.

The following table of formulas will show what a variety of problems are con-

nected with a force acting on a body free to move.

When a body is left free to the action of gravity in falling or rising, the acceleratrix G = g, and the force F = W.

Example 1. What force F = ? is required to give a body W = 1689 pounds a

velocity of V = 36 feet per second in a time T = 5.6 seconds? Find in the formulas under constant force the one which contains the given quantities W, V and T, which is the second formula.

$$F = \frac{W\ V}{g\ T} = \frac{1689 \times 36}{32.166 \times 5.6} = 337.55$$
 pounds, the answer.

Example 2. A projectile of W = 150 pounds is fired horizontally from a rifled gun of S=11 feet in length, in which it receives a velocity of V=950 feet per second. Required, the mean force F=? of the powder acting on the projectile, when the friction in the rifle is 230 pounds.

$$F = \frac{W V^2}{2g S} = \frac{150 \times 950^2}{2 \times 32.166 \times 11} = 191302 + 230 = 191532 \text{ pounds,}$$

the force required.

Example 3.—The moving parts in a propeller steam-engine, such as the steam-piston, piston-rods, cross-heads, connecting-rod, &c. &c., weigh W=8456 pounds. Stroke of piston = 4 feet, making n=52 revolutions per minute. What force F is required for each stroke, to set in motion and bring to rest the moving mass?

The velocity of the moving mass at half stroke will be (formula, page 263)

$$V = \frac{2 \pi r n}{60} = \frac{2 \times 3.1416 \times 2 \times 52}{60} = 10.79 \text{ feet per second.}$$

The time for each half stroke will be

$$T = \frac{60}{4 \times 52} = 0.28846$$
 seconds.

Then the required mean force of the momentum will be

$$F = \frac{WV}{gT} = \frac{8456 \times 10.79}{32.166 \times 0.2846} = 9966.8$$
 pounds.

For high grade of expansion of steam, this force acts beneficially to the move-

ment of the engine.

Example 4.—The mean force of gunpowder in a rifled gun is known to be 231400 pounds, on a projectile W=180 lbs. The friction of the projectile through the gun is estimated to 264 pounds, leaving F=231400-264=231136 pounds. The length of the gun is S=12 feet, elevated to an angle $x=6^{\circ}$ 30'. Required the velocity V=? of the projectile when it leaves the gun.

$$V = \sqrt{2 g S \left(\frac{F}{W} - \sin x\right)} = \sqrt{2 \times 32166 \times 12 \left(\frac{231136}{180} - \sin .6^{\circ} 30'\right)}$$

= 995.64 feet per second, the answer.

Example 5.—What velocity V = ? can a steam-engine of H = 56 horses impart to a body W = 9 tons in a time T = 30 seconds?

$$P = 56 \times 550 = 19800$$
 effects, and $W = 9 \times 2240 = 20160$ lbs.

$$V = \sqrt{\frac{2 g P T}{W}} = \sqrt{\frac{2 \times 32 \cdot 166 \times 19800 \times 30}{20160}} = 43.538 \text{ feet per second.}$$

Example 6.—A body W = 3685 lbs. is moving with a velocity V = 56 feet per second. What time T = ? is required to bring that body to rest, with a force F = 128 pounds?

$$T = \frac{WV}{gF} = \frac{3685 \times 56}{32 \cdot 166 \times 128} = 50 \cdot 121$$
 pounds, the answer.

Example 7.—What power P = ? is required to drive a centrifugal gun to throw out balls of W = 50 lbs. every T = 8 seconds, with a velocity V = 785 feet per second (friction omitted)?

$$P = \frac{W V^2}{2 g T} = \frac{50 \times 785^2}{2 \times 32 \cdot 166 \times 8} = 59867$$
 effects,

divided by 550 = 108.85 horses, the power required.

Example 8.—A sledge of W=20 lbs. strikes a spike into a log S=0.08 foot, with a velocity of V=25 fect per second. Required the force F=? with which the spike was driven into the log, omitting the weight of the spike.

$$F = \frac{W V^2}{2 g S} = \frac{20 \times 25^2}{2 \times 32.166 \times 0.08} = 2628.9 \text{ pounds.}$$

Example 9.—A body starts to ascend vertically with a velocity of 860 feet per second. What will be its velocity at the end of T=5 seconds?

$$\textit{V} = \textit{G} \; \textit{T} = 32 \cdot 166 \times 5 = 160 \cdot 830 \; \text{feet per second},$$

and 860 - 160.83 = 699.17 feet per second, the answer.

Dynamical Formulas for Accelerated or Retarded Motion.

Constant Force in Pounds acting on a Body free to move.

$$F = \frac{GW}{g} = \frac{WV}{gT} = \frac{2WS}{gT^2} = \frac{WV^2}{2gS} = \frac{PT}{S} = \sqrt{\frac{2PW}{gT}} = \frac{2K}{GT^2} = \frac{K}{S}$$

Final Velocity in the Time T, or Uniform Velocity of a Moving Body.

$$V = G T = \frac{g F T}{W} = \frac{2 S}{T} = \sqrt{\frac{2 g S F}{W}} = \sqrt{\frac{2 G S}{W}} = \frac{P T}{K} = \sqrt{\frac{2 g P T}{W}} = \sqrt{\frac{2 g K}{W}}$$

Time in Seconds in which the Force acts on the Body free to move.

$$T = \frac{V}{G} = \frac{WV}{gF} = \sqrt{\frac{2WS}{gF}} = \sqrt{\frac{2S}{G}} = \frac{2FS}{VK} = \frac{K}{P} = \frac{2SW}{gTK} = \sqrt{\frac{2WK}{gF^2}}$$

Constant Acceleration of the Force F in Feet per Second.

$$G = \frac{g \ F}{W} = \frac{2 \ S}{T^2} = \frac{V}{T} = \frac{V^2}{2 \ S} = \frac{g \ P \ T}{W \ S} = \frac{F \ V^2}{P \ T} = \frac{g \ K}{W \ S} = \frac{2 \ K}{F \ T^2}.$$

Space in Feet in which the Force acts on the Body free to move.

$$S = \frac{G \ T^2}{2} = \frac{V \ T}{2} = \frac{V^2}{2 \ G} = \frac{g \ F \ T^2}{2 \ W} = \frac{P \ T}{F} = \frac{g \ P \ T^2}{W \ V} = \frac{g \ K}{G \ W} = \frac{K}{F}$$

Weight in Pounds of the Moving Body.

$$W = \frac{g \ F}{G} = \frac{g \ F \ T^2}{2 \ S} = \frac{2g \ FS}{V^2} = \frac{g \ F \ T}{V} = \frac{g \ P \ T^3}{2 \ S} = \frac{g \ F^2 \ T}{2 \ P} = \frac{2 \ g \ K}{V^2} = \frac{g \ T^2 \ K}{2 \ S}$$

Mean Power in Effects during the Time T, or in the Space S.

$$P = \frac{F \ S}{T} = \frac{g \ F^2 \ T}{2 \ W} = \frac{2 \ W S^2}{g \ T^3} = \frac{W \ V^2}{2 \ g \ T} = \frac{2 \ K}{T} = \frac{T \ K}{2 \ S} = \frac{V \ K}{2} = \frac{F \ V^2}{G \ T}$$

Work in Footpounds concentrated in a Moving Body.

$$K = FS = \frac{W V^2}{2 g} = \frac{F V T}{2} = \frac{G W V T}{2 g} = \frac{F G T^2}{2} = \frac{g F^2 T^2}{2 W} = \frac{2 S P}{T} = PT.$$

The Body moving in an Inclined Direction of an Angle x.

Applied Constant Force in Pounds.

$$F = W\left(\frac{V}{gT} \pm \sin x\right) = W\left(\frac{2S}{gT^2} \pm \sin x\right) = W\left(\frac{V^2}{2gS} \pm \sin x\right).$$

Final Velocity in Feet per Seconds when the Force F ceases to act.

$$V = g T \left(\frac{F}{W} \mp \sin x \right) = \frac{2 S \sin x}{T} = \sqrt{2 g S \left(\frac{F}{W} \mp \sin x \right)}.$$

Time of Action in Seconds.

Acceleration.

$$T = \frac{WV}{g(F \mp W \sin x)} = \sqrt{\frac{2WS}{g(F \mp W \sin x)}}$$
 $G = g(\frac{F}{W} \mp \sin x)$.

Space in Feet.

Work done by F.

$$S = \frac{g T^2}{2} \left(\frac{F}{W} \mp \sin x \right). \quad K = W S \left(\frac{V}{g T} \mp \sin x \right) = \frac{Fg T^2}{2} \left(\frac{F}{W} \mp \sin x \right).$$

Use the upper sign when the direction of motion rises above the horizon, and the lower sign when the direction of motion dips under the horizon.

Force and Work in Revolving Bodies. Centre of Gyration. Fly-Wheels.

Centre of gyration is a point in revolving bodies in which, if all the revolving matter were there collected, it would obtain equal angular velocity from, and sustain equal resistance to, the force that gives it the rotary motion.

The centre of gyration in different forms of bodies will be found by the for-

mulas on pages 204 and 205.

F =constant force in pounds, acting to rotate the body as in figs. 249 and 250, or the mean force on a steam-piston.

r = radius in feet upon which the force Facts. For a steam-engine the mean

radius will be $r=0.63661 \times$ the radius of the crank, or 0.3183 S, when S= stroke of the steam-piston in feet.

W = weight in pounds of a fly-wheel, or other rotating body.

x = radius of centre gyration in feet.

T =time in seconds in which the force F is applied from the first start, or the time in which the velocity is accelerated.

N = number of revolutions in the time T. n = number of revolutions per minute.

K = work concentrated in the revolving body. f = irregularity in a fraction of the mean revolutions n.

For a double-acting single-cylinder engine, the fly-wheel in its regular course of running has an irregular velocity through each revolution. Its smallest velocity is when the crank is at an angle of 40° from the beginning of the stroke, and its greatest velocity when at 40° from the end of the stroke. The larger the fly-wheel is for a given velocity, the more regular will the machinery run without limit. But the fly-wheel may be made so small that its accumulated work cannot carry the machinery around, which will be the case when the irregularity f = 1. In ordinary practice make irregularity f = 0.1 to 0.01. Example 1.—What force F = ? is required to give a body W = 3600 pounds

an angular velocity n=76 revolutions per minute in a time T=24 seconds, the radius of gyration being x = 12 feet, and the force Facting on a radius r = 3 feet?

 $F = \frac{W x^2 n}{307 \cdot 1 \ Tr} = \frac{3600 \times 12^2 \times 76}{307 \cdot 1 \times 24 \times 3} = 1779 \cdot 5$ pounds, the answer.

Example 2.—Required the weight W = ? of a fly-wheel for an engine of D=36 inches diameter of cylinder double acting, with steam-pressure p=50lbs. per sq. in. S=6 feet the stroke of piston. Area of steam-piston 1017.8 sq. in., and the force $F = 1017.8 \times 50 = 50890$ pounds. Radius of gyration x = 10 feet, and n = 48 revolutions per minute. Assume f = 0.05.

$$W = \frac{2542 \ FS}{n^2 \ x^2 f} = \frac{2542 \times 50890 \times 6}{48^2 \times 10^2 \times 0.05} = 67376.2$$
 pounds, the weight required.

Should the steam be used expansively, the fly-wheel ought to be so much heavier, as the initial pressure is greater than the mean pressure.

The radius of gyration in a fly-wheel, including the arms, can in practice be

assumed to be the inner radius of the ring.

Example 3.—What time from the start of engine is required to give the flywheel in Ex. 2 a velocity of n=48 turns per minute? r=0.3183 S=1.9098 ft.

$$T = \frac{Wx^2 n}{307 \cdot 17 \ F r} = \frac{67376 \cdot 2 \times 10^2 \times 48}{307 \cdot 17 \times 50890 \times 1 \cdot 9098} = 10.85 \text{ seconds.}$$

Example 4.—Let the steam-engine in the preceding examples be applied to a rolling-mill, geared two to one of the rollers. An iron plate is rolled through with N=8 revolutions of the engines, after which the revolutions were found to be reduced to $n_1=36$ per minute. Required the work done in rolling the plate; and what time is required for the engine to regain the n=48 revolutions? Work done by engine, $K=2FSN=2\times67376\cdot2\times6\times8=6468115\cdot2$ footps.

Work done by fly-wheel,

$$K = \frac{W x^2 (n^2 - n_1^2)}{5866 \cdot 5} = \frac{67376 \cdot 2 \times 10^2 (48^2 - 36^2)}{5866 \cdot 5} = 1157671 \text{ footpounds,}$$

to which add $6468115\cdot 2 = 7625786\cdot 2$ footpounds, work consumed in rolling plate. The time required for the engine to make up the n=48 revolutions will be

$$T = \frac{W \, x^2 \, (n - n_1)}{307 \cdot 17 \, F \, r} = \frac{67376 \cdot 2 \, \times \, 10^2 \, (48 - 36)}{307 \cdot 17 \, \times \, 50890 \, \times \, 1 \cdot 9098} = 2 \cdot 71 \, \text{seconds.}$$

Formulas for Accelerated Circular Motion.

Force F, in pounds, acting on the Lever or Radius r, to rotate the Body.

$$F = \frac{W \ x^2 \ n}{307 \cdot 17 \ T' \ r} = \frac{W \ x^2 \ N}{2 \cdot 56 \ T^2 \ r} = \frac{60 \ K}{\pi \ r \ n \ T} = \frac{K}{2 \ \pi \ r \ N}.$$

Final Revolutions per Minute in the Time T.

$$n = \frac{120 \ N}{T} = \frac{307 \cdot 17 \ F \ T \ r}{W \ x^2} = \frac{60 \ K}{\pi \ r \ T \ F} = \sqrt{\frac{5866 \cdot 5 \ K}{W \ x^2}}.$$

Total Number of Revolutions in the Time T.

$$N = \frac{Tn}{120} = \frac{2.56 \ F \ T^2 \ r}{W \ x^2} = \frac{K}{2 \ \pi \ r \ F} = \frac{T}{1.566 \ x} \sqrt{\frac{K}{W}}.$$

Time of Acceleration, in Seconds, from the Start of Change of Motion.

$$T = \frac{W x^2 n}{307 \cdot 17 \ F \ r} = \sqrt{\frac{W x^2 N}{2 \cdot 56 \ F r}} = \frac{60 \ K}{\pi \ r \ n \ F} = \frac{x \sqrt{W K}}{2 \ F \ r}.$$

Radius of Gyration, in Feet, of the Revolving Body.

$$x = \sqrt{\frac{307 \cdot 17 \ Fr \ T}{W \ n}} = \sqrt{\frac{2 \cdot 56 \ F \ r \ T^2}{W \ N}} = \frac{K \ T}{4 \ N \ \sqrt{W N F r}} = \frac{327 \cdot 78 \ K}{n \ \sqrt{W \ n \ T F \ r}}.$$

Weight, in Pounds, of the Revolving Body.

$$W = \frac{307 \cdot 17 \ T \ F \ r}{x^2 \ n} = \frac{2 \cdot 56 \ T^2 \ F \ r}{x^2 \ N} = \frac{5866 \cdot 5 \ K}{n^2 \ x^2} = \frac{K \ T^2}{2 \cdot 454 \ x^2 \ N^2}.$$

Work in Footpounds, concentrated in a Revolving Body.

$$K = \frac{W \ x^2 \ n^2}{5866 \cdot 5} = \frac{2 \cdot 454 \ W \ x^2 \ N^2}{T^2} = \frac{\pi \ r \ n \ F \ T}{60} = 2 \ \pi \ r \ N \ F$$

Fly-Wheels for Steam-Engines.

Fly-Wheel for a Single Acting Steam-Engine for Uniform Work.

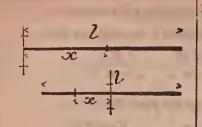
$$W = \frac{5866 \cdot 5 \ F \ S}{n^2 \ x^2 f} \cdot n = \frac{76 \cdot 6}{x} \sqrt{\frac{FS}{Wf}} \cdot x = \frac{76 \cdot 6}{n} \sqrt{\frac{FS}{Wf}} \cdot f = \frac{5866 \cdot 5 \ F \ S}{x^2 \ n^2 \ W}.$$

Fly-Wheel for a Double Acting Steam-Engine for Uniform Work.

$$W = \frac{2542 \ FS}{n^2 \ x^2 f} \cdot n = \frac{50.42}{x} \sqrt{\frac{FS}{Wf}} \cdot x = \frac{50.42}{n} \sqrt{\frac{FS}{Wf}} \cdot f = \frac{2542 \ FS}{x^2 \ n^2 \ W}.$$

Fly-Wheel for a Double Acting Two-Cylinder Engine for Uniform Work.

$$W = \frac{1172 \ FS}{n^2 \ x^2 f} \cdot n = \frac{34 \cdot 23}{x} \sqrt{\frac{FS}{Wf}} \cdot x = \frac{34 \cdot 23}{n} \sqrt{\frac{FS}{Wf}} \cdot f = \frac{1172 \ FS}{x^2 \ n^2 \ W}.$$

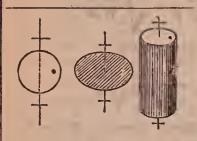


239.

A line or bar.

$$x = 0.5775l$$
,

$$x = 0.2887l.$$



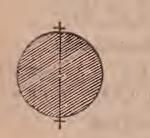
240.

A circumference round its diameter,

A circle-plane round its centre,

A cylinder round its axis.

$$x = 0.7071r$$
.



241.

A circle-plane round its diameter.

$$x = 0.5r.$$

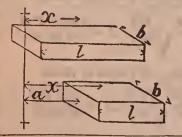


242.

A Sphere round its diameter.

Convex surface, x = 0.8165r,

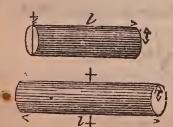
Solid, . .
$$x = 0.6324r$$
.



243. Parallelopiped.

$$x = \sqrt{\frac{4l^2 + b^2}{12}}$$

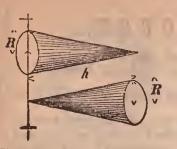
$$x = \sqrt{\frac{4l^2 + b^2}{12} + a^2 + a l}$$

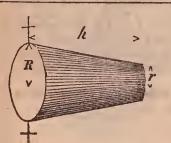


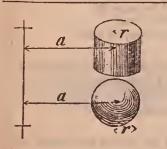
244. Cylinder.

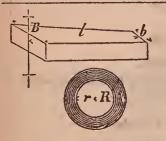
$$x=\sqrt{\frac{4l^2+3r^2}{12}},$$

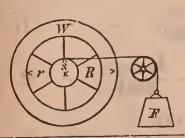
$$x = \sqrt{\frac{l^2 + 3r^2}{12}}.$$

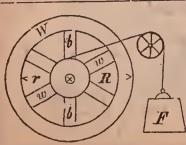












245. Cone.

$$x = \sqrt{\frac{2h^2 + 3R^2}{20}},$$
 $x = \sqrt{\frac{12h^2 + 3R^2}{20}}.$

246. Conic Frustum.

$$x = \sqrt{\frac{\frac{h}{10} \left(\frac{R^2 + 3R \ r + R \ r^2}{R^2 + R \ r + r^2} \right) + \frac{3}{20} \left(\frac{R^5 - r^5}{R^2 - r^3} \right)}$$

247.

Cylinder and Sphere.

$$x = \sqrt{a^2 + \frac{1}{2}r^2},$$

$$x = \sqrt{a^2 + \frac{2}{5}r^2}.$$

248.

Wedge and Ring.

$$x = 0.204 \sqrt{12l^2 + B^2 + b^2},$$
 $x = \sqrt{\frac{R^2 + r^2}{2}}.$

249.

Fly Wheel.
$$x = \sqrt{\frac{R^2 + r^2}{2}},$$

$$FG: Wg = x^2: s^2.$$

250. Fly Wheel with Arms.

$$x^{2}(W+w) = W \frac{R^{2}+r^{2}}{2}+w \frac{4r^{3}+b^{2}}{12},$$

$$x = \sqrt{\frac{6W(R^2+r^2)+w(4r^2+b^2)}{12(W+w)}}.$$

CENTRIFUGAL FORCE.

Central Forces are of two kinds, centrifugal and centripetal.

Centrifugal Force is the tendency which a revolving body has to depart from its centre of motion.

Centripetal Force is that by which a revolving body is attracted or at-

tached to its centre of motion.

The Centrifugal and Centripetal forces are opposites to each other, and when equal the body revolves in a circle; but when they differ the body will revolve in other curved lines, as the Ellipse, the Parabola, &c., according to the nature of the difference in the forces. If the centrifugal force is o while the other is acting, the body will move straight to the centre of motion; and if the centripetal force is o while the other is acting, the body will depart from the circle in a straight line, tangent to the circle in the point where the centripetal force ceased to act. The central forces are distinct from the force that has set the body in motion.

If the centrifugal force be made use of to produce an effect, such effect will be at the expense of the one producing the rotary motion.

Letters denote.

F = Centrifugal force in pounds.

M = the Mass or weight of the revolving body in pounds. v = Velocity of the revolving body, in feet per second.

R = Radii of the circle in which the body revolves, in feet.

n = number of revolutions per minute.

Example 1. Required the centrifugal force of a body weighing 63 pounds, and making 163 revolutions per minute, in a circle of 4 feet, 4 inches radius?

$$F = \frac{MR n^2}{2933} = \frac{63 \times 4.33 \times 163^2}{2933} = 2475$$
 pounds.

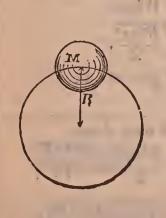
Example 2. A Railroad train runs 43 miles per hour on a curved track of 115 feet radii. What should be the obliquity of the track?

$$\tan x = \frac{\text{Miles}^2}{69R} = \frac{43^2}{69 \times 115} = 0.233,$$

or $x = 13^{\circ} 10'$, the obliquity of the track.

Example 3. A governor having its arms l=1 foot, 6 inches, how many revolutions must it make per minute to form an angle $x=30^{\circ}$?

$$n = \frac{54.16}{\sqrt{1.5 \times \cos .30^{\circ}}} = 47.5$$
 revolutions per minute.



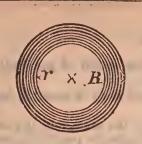
$$F = \frac{M v^{2}}{g R} = \frac{M v^{2}}{32 \cdot 16 R}, \qquad 1,$$

$$F = \frac{4M R \pi^{2} n^{2}}{60^{2} g} = \frac{M R n^{2}}{2933}, \qquad 2,$$

$$M = \frac{F g R}{v^2} = \frac{2933 F}{M n^2}, \quad - \quad 3,$$

$$R = \frac{M v}{F g} = \frac{2933 F}{M n^2},$$
 - 4,

$$n = \sqrt{\frac{2933 F}{M R}}, \quad v = \sqrt{\frac{F R g}{M}}, \quad 5,$$



Centrifugal force of a ring.

$$F = \frac{M \, n_2 \, \sqrt{R^2 + r^2}}{4150}.$$



229.

Centrifugal force of a grinding stone, circle-plane, cylinder, rotating round its centre.

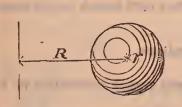
$$F = \frac{M R n^2}{4150}.$$



230.

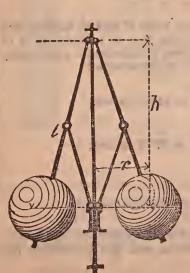
Centrifugal force of a cylinder rotating round the diameter of its base.

$$F = \frac{Mn^2l}{5866}.$$



231.

Centrifugal force of a ball, $F = \frac{M n^2 R}{2933}.$



232.

Governor.

$$n = \frac{60}{2\pi} \sqrt{\frac{g}{h}} = \frac{54 \cdot 16}{\sqrt{h}} = \frac{54 \cdot 16}{\sqrt{l \cos x}},$$

$$h = \frac{2933}{n^2}, \quad l = \frac{2933}{n^2 \cos x} = \frac{h}{\cos x},$$

$$\cos x = \frac{2933}{n^2 l} = \frac{h}{l}, \quad r = \sqrt{l^2 - h^2}.$$

PENDULUM.

Simple Pendufum is a material point under the action of gravitation, and suspended at a fixed point by a line of no weight.

Compound Pendulum is a suspended rod and body of sensible magnitude, fixed as the simple pendulum.

Centre of Oscillation is a point in which if all the matter in the compound pendulum were there collected, it would make a simple pendulum oscillate at the same times.

Angle of Oscillation is the space a pendulum describes when in mo-

The velocity of an oscillating body through the vertical position, is equal to the velocity a body would obtain by falling vertically the distance versed sine of half the angle of oscillation.

Letters denote.

l = *length* of the simple pendulum, or the distance between the centre of suspension, and centre of oscillation in inches.

t = time in seconds for n oscillations.

n = number of single oscillations in the time t.

Example 1. Required the length of a pendulum that will vibrate seconds? here n = 1, and t = 1''.

$$l = 39\cdot109 \frac{t^2}{n^2} = 39\cdot109$$
 inches, the length of a pendulum for seconds.

Example 2. Require the length of a pendulum that will make 180 vibrations per minute? here t = 60'' and n = 180.

$$l = \frac{39 \cdot 109t^2}{n^2} = \frac{39 \cdot 109 \times 60^2}{180^2} = 4.346$$
 inches.

Example 3. How many vibrations will a pendulum of 25 inches length make in 8 seconds?

$$n = \frac{6.254t}{\sqrt{l}} = \frac{6.254 \times 8}{\sqrt{25}} = 10 \text{ vibrations.}$$

Example 4. A pendulum is 137.67 inches long and makes 8 vibrations in 15 seconds. Required the unit or accelleratrix g=?

$$g = \frac{0.8225l \ n^2}{t^2} = \frac{0.8225 \times 137.67 \times 8^2}{15^2} = 32.209.$$

Example 5. A compound pendulum of two iron balls P and Q, having the centre of suspension between themselves: see Fig. 238. P=38 pounds, Q=12 pounds, a=25 inches, and b=18 inches. How long is the simple pendulum, and how many vibrations will the pendulum make in 10 seconds?

$$x = \frac{a P - b Q}{P + Q} = \frac{25 \times 38 - 18 \times 12}{38 + 12} = 14.68 \text{ inches.}$$

$$l = \frac{a^{9} P + b^{2} Q}{x(P+Q)} = \frac{25^{9} \times 38 + 18^{9} \times 12}{14 \cdot 68(38+12)} = 37.68$$
 inches,

the length of the single pendulum.

$$n = \frac{6.254t}{\sqrt{t}} = \frac{6.254 \times 10}{\sqrt{37.68}} = 10.193 \text{ vibrations in 10 seconds.}$$

If a compound pendulum is hung up at its centre of oscillation, the former centre of suspension will be the centre of oscillation, and the pendulum will oscillate the same time.



	endulum.
$l = \frac{12g\ t^2}{\pi^2\ n^2}$	$=\frac{39\cdot1t^2}{n^2},$

$$t = \frac{n\sqrt{l}}{6.25},$$

$$n = \frac{6254t}{\sqrt{l}},$$

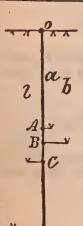
1

$$g = \frac{l \pi^2 n_2}{12t^2}$$

$$g=\frac{0.8225l\,n^2}{t^2},$$

o = centre of suspension.

$$l = a + \frac{2r}{5a}$$



234.

A = centre of gravity.

B =centre of gyration.

C centre of oscillation.

$$a:b=b:l,$$

$$b = \sqrt{al} = 1.1432a,$$

$$l = 1\frac{1}{3}a.$$

6

237.

$$l = \frac{a^2 P + b^2 Q}{a P + b Q}.$$

P and Q expressed in pounds, or cubic contents.



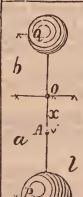
 $2\overline{35}$.

Compound Pendulum.

r = radius of cylinder.

$$l = \frac{16a^2 + 3r^2}{12a},$$

$$l = \frac{4a}{3} + \frac{r^2}{4a}.$$



238.

$$x = \frac{a P - b Q}{P + Q},$$

$$l = \frac{a^2 P + b^2 Q}{x(P + Q)}.$$

Length of a Pendulum vibrating seconds at the level of the sea, in various places.

At the Equator, lat. 0° 0′ 0″
"Washington, lat. 38° 53′ 23″

" New York, lat. 40° 42′ 40″ " London, lat. 51° 31′ -

lat. 45° " Stockholm, lat. 59° 21' 30" 39.0152 inches. 39.0958 66

39.1017 39.139344

39.1270 39.1845

 $l = 39.127 - 0.09982 \cos 2$ lat. for seconds.

COLLISION OF BODIES IN MOTION.

When bodies in motion come in collision with each other, the sum of their concentrated momentum will be the same after the collision as

before, but their velocities and sometimes their directions will differ.

On the accompanying page the bodies are supposed to move in the same straight line, and the formula illustrates the consequences after

collision.

Letters denote.

M and m = weight of the bodies in pounds.

W and w = their respective velocities in feet per second. V' and v = their respective velocities of the bodies after impact. K and k = coefficient of elasticity, which for perfectly hard bodies k = 0 and for perfect elastic bodies k = 1, therefore the elastic coefficient will always be between 0 and 1. When the bodies are perfectly hard their velocities after impact will be common.

For
$$M$$
, $K = \frac{MV}{M(V-V')}$, For m , $k = \frac{mv}{m(v-V')}$.

Example 1. Fig 191. The non-elastic body weighs M=25 pounds, and moves at a velocity V=12 feet per second; m=16 pounds, and v=9. Required the bodies' common velocities, v'=1 after impact.

$$v' = \frac{MV + mv}{M + m} = \frac{25 \times 12 + 16 \times 9}{25 + 16} = 10.83 \text{ feet per second.}$$

Example 2. Fig. 195. The perfect elastic body M=84 pounds, V=18, m=48, and v=27. Required the velocity V'=1 after impact with the body m.

$$V = \frac{18(84 - 48) - 2 \times 48 \times 27}{84 + 48} = -23.64.$$

the negative sign denotes that the body will return after the collision

with a velocity of 23.63 feet per second.

Example 3. Fig. 196. The partly elastic body M=38 pounds and V=79 feet per second, will strike the body in rest m=24 pounds; what will be the velocity v'=1 of the body m, its elasticity being k'=0.6.

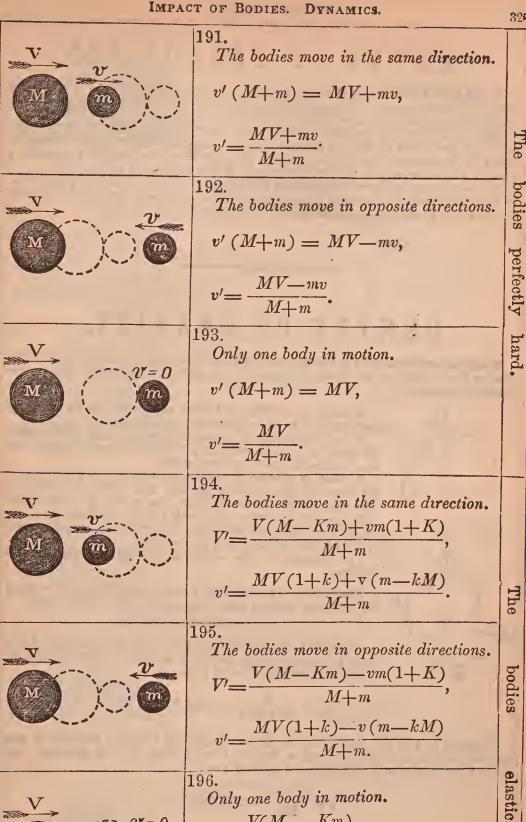
$$v' = \frac{79 \times 38 (1+0.6)}{38+24} = 70.6$$
 feet per second.

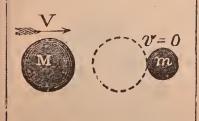
When a moving body strikes a stationary elastic plane, its course of departure from the plane will be equal to its course of incident.



Problem. A body in a is to strike the plane AB so that it will depart to the given point b; required its course of incident from a?

Draw bd, at right angles through AB, make cd=bc join a and d; then ad is the course of incident, and eb, the course of departure, and the body will strike in e.





Only one body in motion. $V' = \frac{V(M - Km)}{M + m},$

$$V' = \frac{1}{M+m},$$

$$v' = \frac{VM(1+k)}{M+m}.$$

CENTRE OF PERCUSSION.

Centre of Percussion is a point in which the momentums of a moving body are concentrated. Centre of Percussion is the same as centre of oscillation, and to be calculated by the same formulas.

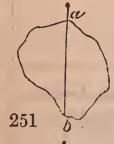
Take an iron bar in one hand, and strike heavily over a sharp edge, if the centre of percussion of the bar strikes over the edge, the whole momentum will there be discharged, but if it strikes at a distance from the centre of percussion a part of the momentum will be discharged in the hand, and a shock felt.

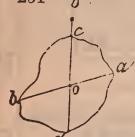
It is sometimes of great importance to properly place the centre of percussion. If it is dislocated, the moving body not only fails to properly transmit its effect,

but the lost momentum acts to wear out the machinery.

CENTRE OF GRAVITY.

Centre of Gravity is a point around which the momentums of all matters (under the action of the force of gravity) in a body, or system of bodies, are equally divided.





A body or system of bodies suspended at its centre of gravity, will be in equilibrium in all positions.

A body or system of bodies, suspended in a point out of its centre of gravity, will hang with its centre of gravity ver-

tical under the point of suspension.

A body or system of bodies suspended in a point out of its centre of gravity, and having two different positions, the two vertical lines through the point of suspension will meet in the centre of gravity; thus if a plane be hung up in two different positions, the vertical lines a, b, and c, d, will meet in the centre of gravity o.

z =distance to the centre of gravity as noted in the

figures.

Example 1. The radius of a circle being 3 feet, how far is its centre of gravity from the centre of the half circle?

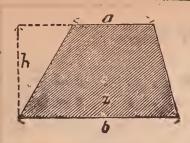
$$z = 0.6367 \times 3 = 1.91$$
 feet.

Example 2. How far from the bottom of a cylindric shell, open at one end, is its centre of gravity? The cylinder is 4 feet long, radius r = 0.8 feet.

$$z = \frac{h}{r+2h} = \frac{4}{0.8+2\times4} = 0.625 \text{ feet.}$$

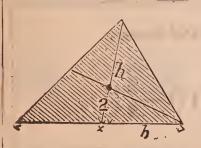
Example 3. Fig. 264. An irregular figure weighing P=138 pounds, is suspended between a fulcrum and a weight, l=5.6 feet, W=57 pounds. Required the distance to the centre of gravity z=?

$$s = \frac{57 \times 5.6}{138} = 2.31$$
 feet.



Quadrangle.—a and b parallel.

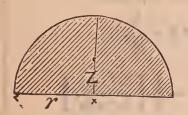
$$z=\frac{h}{2}-\frac{h}{6}\left(\frac{b-a}{b+a}\right).$$



253.

Triangle.

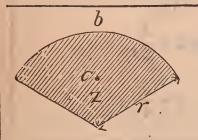
$$z=\frac{h}{3}$$
.



254.

Half a circle plane or Elliptic plane.

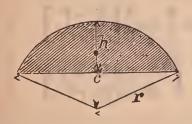
$$z = 0.424r.$$



255.

Circle sector.

$$z=\frac{2c\ r}{3b}.$$

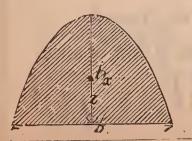


256.

Circle Segment. a = area.

$$z=\frac{c^3}{12\mathbf{a}}.$$

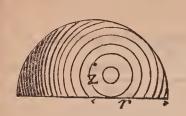
$$x = h + z - r$$



257. Parabola.

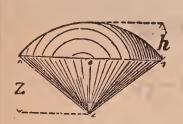
$$z=\frac{2h}{5}.$$

For half a Parabola $x = \frac{3}{8}b$.



Half Sphere.

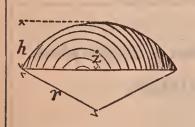
Convex surface $z = \frac{1}{2}r$. Solid $z = \frac{1}{8}r$.



259.

Spherical Sector.

Solid,
$$z = \frac{1}{4} \left(r - \frac{h}{2} \right)$$
.

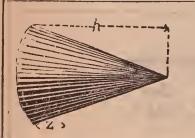


260.

Spherical Segment.

Convex surface $z = \frac{h}{2}$,

Solid
$$z = \frac{h}{2} \cdot \left[\frac{2r^2 + h^2}{3r^2 + h^2} \cdot \right]$$



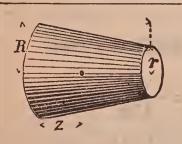
261.

Cone.

Convex surface $z = \frac{h}{3}$,

Solid

 $z=\frac{h}{4}$.

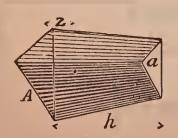


262.

Conic Frustum.

Con. sur.
$$z = \frac{h}{2} - \frac{h}{6} \left[\frac{R-r}{R+r} \right]$$

Solid
$$z = \frac{h}{4} \cdot \left[\frac{R^2 + r(2R+3r)}{R^2 + r(R+r)} \cdot \right]$$

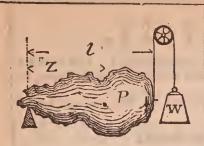


263.

Fyramidic Frustum.

A and a =area of the two bases.

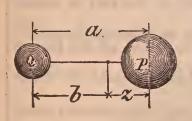
Solid
$$z = \frac{h}{4} \left[\frac{A+3a+2\sqrt{Aa}}{A+a+\sqrt{Aa}} \right]$$



Irregular Figure.

$$P: W=l: z,$$

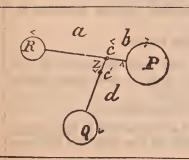
$$z = \frac{Wl}{P}$$



265.

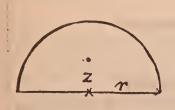
To find the Centre of Gravity of two bodies, P and Q.

$$z = \frac{Q \ a}{P + Q}, \qquad b = \frac{P \ a}{P + Q}.$$



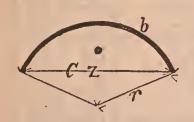
266.
To find the Centre of Gravity of a system of bodies.

$$b = \frac{R a}{P+R}, \qquad z = \frac{Q d}{P+R+Q}.$$



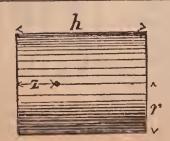
Half a circumference of a Circle or Ellipse.

$$z=0.6367r.$$



Circle arc or Elliptic arc.

$$z = \frac{c r}{b} = \frac{c(c^2 + 4h^2)}{8h b}.$$



269.

268.

267.

Cylindric Surface with a bottom in one

$$z=\frac{h}{r+2h}.$$

SPECIFIC GRAVITY.

Specific Gravity is the comparative density of substances. The unit for measuring the specific gravity is assumed to be the density of rain water, or distilled water.

One cubic foot of distilled water weighs 1000 ounces, or 62.5 pounds avoir-

dupois.

To Find the Weight of a Body.

RULE 1. Multiply the contents of the body in cubic feet by 62.5, and the product by its specific gravity, will be the weight of the body in pounds avoirdupois.

RULE 2. Multiply the contents of the body in cubic inches by 0.03616, and the product by its specific gravity, will be the weight of the body in pounds avoirdupois.

RULE 3. Divide the specific gravity by 0.016 and the quotient is the weight of a cubic foot.

Example 1. A bottle full of mercury is 3 inches, inside diameter, and 6 inches high. How much mercury is there in the bottle in pounds?

One cubic inch of mercury weighs 0.491 pounds, and by the formula for Fig. 119 we have the

weight =
$$0.491 \times 0.785 \times 32 \times 6 = 20.85$$
 pounds.

Example 2. Required the weight of a cone of cast iron, diameter at the base d=1.33 feet, height h=4 feet? One cubic foot of cast iron weighs 450.5 pounds, and by formula for Fig. 117 we have the

weight =
$$450.5 \times 0.2616 \times 1.332 \times 4 = 834$$
 pounds.

Example 3. The section area of the lower hole in a steam boat is 245 square feet; how much space must be taken in the length of the hole for 131 tons of anthracite coal?

Anthracite coal are 42.3 cubic feet per ton.

length =
$$\frac{42.3 \times 131}{245}$$
 = 22.6 feet, the space required.

Weight and Bulk of Substances,

	Cubic	Cubic		Cubic	Cubic
Names of Substances.	foot	feet	Names of Substances.	foot	feet
Tramos of Sacounices.	in	per	Trames of Substantees.	in	per
	pounds.	ton.		pounds.	ton.
Cast iron,	450.5	4.97	Sand,	94.5	23.7
Wrought iron, •	486.6	4.60	Granite,	165	13.5
Steel,	489.8	4.57	Earth, loose,	78.6	28.5
Copper,	555*	4.03	Water, salt, (sea) -	64.3	34.8
Lead,	707.7	3.16	" fresh	62.5	35.9
Brass, · · ·	537.7	4.16	Ice,	58·0 8	38.56
Tin,	456	4.91	Gold,	1013	2.21
Pine, white	29.56	75.6	Silver,	551	4.07
" yellow,	33-81	66.2	Coal, Anthracite -	53	42.3
Mahogany,	66.4	33.8	" Bituminous -	50	44.8
Marble, common, -	165	13.6	" Cumberland -	53	42.3
Mill-stone,	130	17.2	" Charcoal -	18.2	123
Oak, live	70	32.0	Coke, Midlothian -	32.70	68.2
" white,	45.2	49.5	" Cumberland -	31.57	70.9
Clay,	101.3	22.1	" Natural Virginia	46.64	48.3
Cotton Bales,	100	20.4	Conventional rate of		
Brick,	100	22.4	Stone coal, 28 bushels		
Plaster Paris,	1 105	21.3	(5 pecks) = 1 ton, -		43.56

To Find the Specific Gravity.

W = weight of a body in the air.

w = weight of the body (heavier than water) immersed in water. S = specific gravity of the body. Then,

$$W-w: W=1: S. \quad S=\frac{W}{W-w}, \quad \cdot \quad \cdot \quad 1,$$

Example 4. Required the specific gravity of a piece of iron-ore weighing 6.245 pounds in the air, and 4.935 pounds in water, S=?

$$S = \frac{6.345}{6.345 - 4.935} = 4.5$$
 the specific gravity.

When the body is lighter than water, annex to it a heavier body that is able to sink the lighter one.

S = specific gravity of the heavier annexed body.

s = specific gravity of the lighter body.

W = weight of the two bodies in air.

w = weight of the two bodies in water. V = weight of the heavier body in air.

v = weight of the lighter body in air.

$$s = \frac{v}{W - w - \frac{V}{S}}, \qquad 2$$

Example 5. To a piece of wood, which weighs v = 14 pounds in the air, is annexed a piece of cast-iron V = 28 pounds; the two bodies together weigh w = 11.7 pounds in water. Required the specific gravity of the wood?

> W = V + v = 28 + 14 = 42 pounds. S = 7.2 specific gravity of cast-iron.

$$S = \frac{14}{42 - 11.7 - \frac{28}{7.2}} = 0.529$$
, the specific

gravity of the wood, (Poplar White Spanish.)

A simple way to obtain the specific gravity of woods, is to form it to a parallel rod, and place it vertically in water, then when in equilibrium, the immersed end is to the whole rod as the specific gravity is to 1.

Example 6. A cylinder of wood is 6 feet, 3 inches long, when Immersed vertically in water it will sink 3 feet, 9 inches by its own weight. Required its specific gravity.

$$3.75:6.25 = S:1, \qquad S = \frac{3.75}{6.25} = 0.600.$$

To discover the Adulteration in Metals. or to find the proportions of two Ingredients

$$V = \frac{W - s(W - w)}{1 - \frac{s}{S}}, \qquad 3,$$

Example 7. A metal compounded of silver and gold weighs W=6 pounds in the air, and in water w = 5.636 pounds. Require the proportions of silver and gold?

S = 19.36 specific gravity of gold. s = 10.51 specific gravity of silver.

weight
$$V = \frac{6 - 10.51(6 - 5.636)}{1 - \frac{10.51}{19.36}} = 4.755$$
 pounds of gold.

	1	Weight			Weight
	Specific			Specific	per
Names of Substances.	gravity.		Names of Substances.	gravity.	cubic
	gracity.	inch.		3	inch.
Metals.					lbs.
	00.000	lbs.	Alaba dan mbita	0.720	
Platinum, rolled	22.669	•798	Alabaster, white	2.730	•0987
WILE,	21.042	.761	" yellow Coral, red	$2.699 \ 2.700$	·0974 ·0974
	19.50	•736	Granite, Susquehanna	2.704	*0976
" purified, crude, grains		·706 ·565	" Onincy -	2.652	0958
Gold, hammered	19.361	•700	" Quincy " Patapsco " Scotch	2.640	*0954
" pure cast	19.258	-697	" Scotch	2.625	*0948
" 22 carats fine -	17.486	•733	Marble, white Italian	2.708	.0978
" 20 ·· " -	15.702	•568	" common	2.686	.0968
Mercury, solid at - 40°	15.632	•566	Tale, black - · · ·	2.900	.0105
" at+32° Fahr.	13.619	•493	Quartz	2.660	. 0962
	13.580	•491	Slate	2.672	•0965
" " 212° "	13.375	•484	Pearl, oriental	2.650	*0957
Lead, pure	11.330	•410	Shale	2.600	.0940
" hammered	11.388	•412	Flint, white • • •	2.594	.0936
Silver, hammered	10.511	·381	black	2.582	.0933
pure	10.474	•379	Stone, common	2.520	*0910
Bismuth,	9.823	355	1)115001 "	2.510	·0906
Red Lead,	8·940 8·098	•324	" Mill Paving	2·484 2·416	·0897 ·0873
Cinnabar, Manganese,	8.030	•293	Gypsum, opaque • •	2.168	•0783
Copper, wire and rolled	8.878	·290 ·321	Grindstone, - · · ·	2.143	•0775
" pure	8.788	318	Salt, common	2.130	.0770
Bronze, gun metal -	8.700	•315	Saltpetre,	2.090	0755
Brass, common	7.820	•282	Sulphur, native	2.033	.0735
Steel, cast steel	7.919	•286	Common soil,	1.984	.0717
" common soft -	7.833	283	Rotten stone, ·	1.981	0416
" hardened & temp.		.283	Clay.	1-930	.0698
Iron, pure	7.768	•281	Brick,	1.900	•0686
" wrought and rolled		.282	Nitre,	1.900	•0636
" hammered	7.789	•282	Plaster Paris, {	1.872	.0677
" cast-iron	7.207	•261		2.473	•0894
Tin, from Böhmen -	7.312	•265	Ivory,	1.822	*0659
"English Zinc, rolled	7·291 7·191	•264	Sand,	1.800	*0651
cast	6.861	·260 ·248	Phosphorus, Borax,	1.770 1.714	*0640 *0620
Antimony,	6.712	•244	Borax,		•0593
Aluminium	2.2	0.09	Coal, Anthracite - {	1.436	.0592
Arsenic,	5.763	208	" Maryland	1.355	•0490
•		200	" Scotch	1.300	.0470
Stones and Earths.			" New Castle	1.270	.0460
Topaz, oriental	4.011	•145	" Bituminous	1.270	.0460
Emery,	4.000	•144	Charcoal, triturated -	1.380	.0500
Diamond,	3.521	127	Earth, loose	1.500	•05 42
Limestone, green white	3.180	•115	Amber,	1.078	60387
Asbestos, starry	3.156	•114	Pimstone,	1.647	•0596
Glass, flint	3.073	•111	Lime, quick	0.804	.0291
" white	2·933 2·892	·106 ·104	Charcoal,	0.441	•0160
bottle	2.732	0987	Woods (Dry.)		
" green	2.642	0954	Alder,	·800	.0289
Marble, Parian		103	Apple-tree,	•793	.0287
" African		.0978	Ash, the trunk	·845	.0306
" Egyptian		0964	Bay-tree,	•822	•0297
Mica,		1000	Beech,	·852	.0308
Hone, white razor -		104	Box, French	•912	.0330
Chalk,		•100	" Dutch	1.328	.0480
Porphyry,		0999	" Brazilian red	1.031	•0373
Spar, green blue		0976	Cedar, wild	•596	•0219
DIUG	2.693	0971	" Palestine - •	•613	.0222

Names of Substances. Specific part gravity. cubic inch.	1			H7odab t			Milaiaht
Cedar, Indian	1	•	Specific			Specific	Weight
Cedar, Indian	Ł	Names of Substances.			Names of Substances.		
Cedar, Indian	I		gravity.			gracing.	
Girron, - 7561 -0203 "Olive - -915 -0331 Cocoa-wood, - 1-040 -0376 "Unrepetine - -870 -0332 Cherry-tree, - -240 -087 "Orberty-tree, - -240 -083 Cork, - -240 -087 Sea - 1-080 -0390 Cork, - -240 -087 Vinegar, - 1-080 -0390 Cork, - -606 -6252 Water, distilled 1-000 -0361 Elder-tree, - -600 -0252 Elm, trunk of - -671 -0243 Filbertree, - -600 -0217 Fir, male - -550 -0199 "formale - -498 0180 Hazel, - -600 -0217 Jasmine, Spanish - -700 -0279 Juniper-tree, - -556 -0201 Lignum-vitze, - -133 -4482 Lignum-vitze, - -942 -941 Jay -944 -941 Mahogany - -75	1	Orden Tudion	1.015		Oil Timesed	.040	
Citron,					Ull, Linseed • •		
Cocca-wood,							
Cherry-tree,	1	Cocce wood			" Whole		
Cork,		Champy-troo			Proof Spirit		
Cypress		Cork			Vinegar		
Ebony, American		Cynress Spanish .			Water, distilled		
Elder-tree,							
Elder-tree,	-	"Indian •					
Filpert-tree - -600 -0217 Fir, male - -498 -0180 -01							
Filpert-tree - -600 -0217 Fir, male - -498 -0180 -01					" Port		
Fir. male		Filbert-tree •	•600				
Hazel, - - - 600 0217 Jasmine, Spanish - 770 0279 Juniper-tree, - 565 0201 Lemon-tree, - 703 0452 Lignum-vitæ, - 1-333 0452 Linden-tree, - 604 0219 Log-wood, - 913 0331 Mastic-tree - 849 0307 Mahogany, - 1063 0385 Maple, - 0750 0271 Medlar, - 944 0342 Mulberry 0ak, heart of, 60 old 0170 0423 07ange-tree, - 705 0255 Pear-tree, - 705 0255 Pear-tree, - 1-354 0490 1-327 0485 0490 0460 1-327 0485 0490 0490 0450 0		Fir. male - · ·	•550	·0199	Miscellaneous.		
Hazel,		"female • •				-005	• 0207
Juniper-tree		Hazel,			Asphaltum, {		
Juniper-tree,		Jasmine, Spanish .	.770		· · · · · · · · · · · · · · · · · · ·		0340
Lignum-vitæ,					Butter		0341
India rubber - 923 0338 0338 Mastic-tree - 913 0335 Mastic-tree - 849 0307 Mahogany - 1063 0385 Maple - 1063 0385 Matton, - 1222 0334 Mastic - 1063 0365 0385 Maple - 1063 0385 Matton, - 1222 0334 Mastic - 1063 0365 03		Lemon-tree,					
Linden-tree,					India rubber • •		
Mastic-tree 349 0307 Mathogany, 1063 0385 Maple, - 750 0271 Mutton, 1222 0442 Mulberry 397 0324 Mulberry 60 old 1170 0423 60 orange-tree, - 705 0225 Pear-tree, - 705 0225 Pear-tree, - 1354 0409 Poplar, - 383 0138 Mastic, - 1009 0365 1500 0650		Linden-tree, • •			Fat of Beef.		
Mable of Mahogany 1'063' 0385' 750' 0271' 0324' 0342' 0342' 0342' 0342' 0342' 0342' 0342' 0342' 0342' 0342' 0342' 0342' 0342' 0342' 0342' 0344' 0342' 0342' 0344' 0342' 0344' 0342' 0344' 0342' 0344' 0342' 0344' 0342' 0344' 0342' 0344' 0342' 0344' 0342' 0344' 0342' 0344' 0342' 0344' 03	1	Log-wood,					
Maple, - - - - - - - - -	1				" Mutton.		
Medlar, 944 0342 collar, 0324 collar, 0324 collar, 0324 collar, 0324 collar, 0324 collar, 0324 collar, 0325 collar, 0423 collar, 0424 colla	}	Manogany, -			Gamboge,		
Mulberry		Maple, • • •					
Oak, heart of, 60 old Orange-tree, - ' ' ' ' ' ' ' ' ' ' ' ' ' ' ' ' ' '	-	Mulhamur					
Orange-tree, - -661 .0255 Gum Arabic, - 1.452 .0525 Pear-tree, - .0384 .0490 .0365 .0239 .0138 .0138 .0138 .0138 .0138 .0138 .0138 .0234 .0244 .0490 .0255 .0244 .0341 .0341 .0341 .0341 .0341 .0341 .0341 .0341 .0341 .0341 .0341 .0342 .03	1	Oak heart of 60 old			" solid - S		
Pear-tree,	-1	Orange tree					
Pomegranate-tree, 1.354 0.490 0.138 0.138	- [Gum Arabic, -		
Poplar,		Pomegranate-tree.			Indigo, - • •		
Plum-tree,					Lard,		
Quince-tree,		" white Spanish			Mastic,		
Quince-tree,	i				Spermaceti, - •		
Sassafras, '382 '0174 '500 '0181 'a		Quince-tree,			Sugar,		
Pine, yellow 6600 0239 Atmospheric air, Weight Vine, - - - 671 0243 Yew, Dutch - - 671 0243 Yew, Dutch - <	Ì	Sassafras, • •					
Pine, yellow 6600 0239 Atmospheric all, Weight Vine, - - - 671 0243 Yew, Dutch - - 671 0243 -		Spru e, - · ·					
Pine, yellow		" old • •			0239		
Wine, - 1.327 0480 0243 Gases. Vapours. Weight cub. ft. grains. Yew, Dutch - .671 .0285 .807 -0292 Atmospheric air, - 1.000 527.0 Liquids. 1.062 .0384 .0292 Ammoniacal gas, - .500 263.7 Acid, Acetic 1.217 .0440 .0440 .0542 .0542 .0540 .072 .072 .0523 .053 .053 .053 .057 .0524 .0542 .05	2	Pine, yellow			Atmospheric an,	0012	
Walnut,		" white					Weight
Yew, Dutch '788 '0292 Atmospheric air, - Ammoniacal gas, - Carbonic acid, - Stopheric air, - Ammoniacal gas, - Carbonic acid, - Stopheric air, - Ammoniacal gas, - Carbonic acid, - Stopheric air, - Ammoniacal gas, - Carbonic acid, - Stopheric ac		Vine,			Gases. Vapours.		cub. ft.
*** Spanish - *** *** *** *** *** *** *** *** ***							grains.
Liquids. Acid, Acetic					Atmospheric air, •	1.000	
Acid, Acetic 1.062 .0384 Carbonic oxid, .972 512.7 "Nitric 1.217 .0440 Carburetted hydrogen, .972 512.7 "Sulphuric 1.841 .0666 Chlorine, - .2500 1316 "Muriatic 1.500 .0434 Chlorocarbonous acid, 3.472 1828 "Fluoric 1.558 .0563 Fluoboric acid, 2.371 1250 Alcohol, commercial .833 .0301 Hydriodic acid, 2.371 1250 Ammoniac, liquid .897 .0324 Oxygen, .009 36:33 Beer, lager 1.034 .0374 Sulphuretted hydrogen, .972 512.7 Champagne, .997 .0360 Nitrogen, .972 512.0 Vapour of Alcohol, .972 512.0 .972 512.0 Vapour of Alcohol, .603 .503 .503 .503 .503 .503 Ether, sulphuric .739 .0267 .0524 .0524 .0524 .0524 .0524 .0524 .0524 .0524 .0524 .0524		*	001	0202	Ammoniacal gas, -		
"Nitric 1.217 .0440 Carburetted hydrogen, .972 512.7 "Sulphuric 1.841 .0666 Chlorine, - 2.500 1316 "Muriatic 1.200 .0434 Chlorocarbonous acid, 3.472 1828 "Fluoric 1.550 .0542 Chloroprussic acid, 2.152 1134 "Phosphoric 1.558 .0563 Fluoboric acid, 2.371 1250 Alcohol, commercial .833 .0301 Hydriodic acid, 4.346 2290 "pure .792 .0287 Hydrogen, .069 36.33 Ammoniac, liquid .897 .0324 Oxygen, .0xygen, .0yyer .0xygen, .0xygen, .0yyer .0yyer <td< td=""><td></td><td>Liquids.</td><td>1</td><td></td><td>Carbonic acid,</td><td></td><td></td></td<>		Liquids.	1		Carbonic acid,		
"Nitric" 1.217 .0440 Carburetted hydrogen, 0666 .972 512.7 "Sulphuric" 1.841 .0666 .0434 Chlorine,		Acid, Acetic			Carbonic oxid, -		
"Muriatic 1:200 :0434 Chlorocarbonous acid, 3:472 1828 "Fluoric - 1:500 :0542 Chloroprussic acid, 2:152 1134 "Phosphoric - 1:558 :0563 Fluoboric acid, 2:371 1250 Alcohol, commercial ropuro - :833 :0301 Hydriodic acid, 4:346 2290 Ammoniac, liquid - :897 :0324 Oxygen, - :069 36:33 Beer, lager - 1:034 :0374 Sulphuretted hydrogen, 1:777 9370 Champagne, - 9:97 :0360 Nitrogen, - :972 512:0 Vapour of Alcohol, 1:613 851:0 5:013 2642 Egg, - - 1:090 :0394 Smoke of bitumin. coal, :102 53:80 Honey, - 1:054 :0381 "wood, - 90 474:0 Human blood 1:054 :0381 "wood, - 90 474:0							
"Fluoric - 1.500		bulphario					
"Phosphoric - Alcohol, commercial "pure - 792		Diuliano			Chlorocarbonous acid,		
Alcohol, commercial *833 *0301 Hydriodic acid, 4*346 2290 """>Ammoniac, liquid *897 *0324 Oxygen, *069 36*33 Beer, lager *034 *0374 Sulphuretted hydrogen, 1*777 9370 Champagne, *097 *0360 Nitrogen, *972 512*0 Cider, *0381 *0267 "turpen'e spir., 5*013 2642 Egg, *0524 Smoke of bitumin. coal, *102 53*80 Human blood *1*054 *0381 "wood, *90 474*0							
Ammoniac, liquid - - - - - - - - -		I Hophion					
Ammoniac, liquid - Beer, lager - 1.034							
Beer, lager 1.034 0.0374 Sulphuretted hydrogen, 1.777 9370 Champagne, Cider, Ether, sulphuric 1.018 0.0361 Vapour of Alcohol, 1.613 851.0 Ether, sulphuric Egg, Honey, Honey, Human blood 1.450 0.0524 Smoke of bitumin. coal, 1.02 53.80 Human blood 1.054 0.0381 "wood, Wood, Honey, 1.02 90 474.0		paro					
Champagne, - '977 '0360 Nitrogen, - '972 512.0 Vapour of Alcohol, "1.018 '0361 Vapour of Alcohol, "1.018 '0361 Vapour of Alcohol, "1.018 50.013 5.013					Sulphuratted hydrogen		
Cider, - 1.018 .0361 Vapour of Alcohol, 1.613 851.0 .0267 .0267 .090 .0394 .0394 .0457.0 .0524 .0524 .0524 .0881							
Ether, sulphuric - 1090 10394 1090 10534 1090 10534 1090 1054 1054 1054 1054 1054 1054 1054 105					Vanour of Alcohol		
Egg, 1.090 .0394 "water, - 623 328.0 Honey, - 1.450 .0524 Smoke of bitumin. coal, 1.054 .0381 "wood, - 90 474.0 .0553.80		Ether sulphune			" turpen'e spir.		
Honey, - 1.450 .0524 Smoke of bitumin. coal, 102 53.80 Human blood - 1.054 .0381 "wood, - 90 474.0							
Human blood - 1.054 .0381 " wood, - 90 474.0							
10100						•90	474.0
		Milk,	1.032	•0373			257.3

ALLOYS.

A = Antimony, B = Bismuth, C = Copper, G = Gold, I = Iron, L = Lead, N = Nickel, S = Silver, T = Tin, and Z = Zinc.

NAME.		ALLOY.	Туре	Metals.	
Brass, common y					
Brass, to be rolle	d, .	32C, 10Z, 1.5T.	NAME. Smallest type,	27 1 4	
Brass castings, co	m.,	20 <i>C</i> , 1.25 <i>Z</i> , 2.5 <i>T</i> .	Smallest type,	• 5L, 1A.	
" " ha	ard, .	25C, 2Z, 4.5T.	Small type, Medium type,	. 4L, 1A.	
Brass propellers,			Medium type, .	CT 1 A	
Gun-metal,		8C, 1T.	Large type,	. 0 <i>L</i> , 1 <i>A</i> .	
Copper-flanges,	•	9C, 1Z, 0.26T.	Largest type, .	bo 121, 124.	
Muntz's metal, .			Metal which can		
Statuary, .	•		forged at red l		
a au		1.37 <i>L</i> .	and strong as	38.2 <i>Z</i> , 60 <i>C</i> , 1.75	. 7
German Silver, .	•	2C, $7.9N$, $6.3Z$,	11011,	. 35.22, 000, 1.10	1.
TD 14 1 1 1		6.5 <i>I</i> .	Alloys f	or Solders	
Britannia metal,					
Chinese Silver, .	•	65.1 <i>C</i> , 19.3 <i>Z</i> , 13 <i>N</i> ,			TS
Oh: -l.4 Connon		2.58 <i>S</i> , 12 <i>I</i> .	Newton's fusible,	8B, 5L, 3T, 215	20
Cni. wht. Copper	•	20.2 <i>C</i> , 12.7 <i>Z</i> , 1. 3 <i>T</i> , 15.8 <i>N</i> .	Rose's " A more "	2B, 1L, 1T, 20	
Modela		10.01%	A more	5B, 3L, 2T, 199	90
Medals, Pinchbeck, .	•	5017	Still more "	12.7, 25.L, 50.B	
Babbitt's metal,	•	95/7 9 4 0 5 C		13 cadium, 158	50
Bell metal, large	•	201, 2A, 0.0 O.	For tin solder,		
" " small	•	10,17.	coarse,	1T, 3L, 500	00
Chinese gongs,	, •	4050007	For tin solder, or-	•	
Telescope mirror		33.3 <i>C</i> 16.7 <i>T</i>	dinary,	2T, 1L, 360	00
White metal, ord		37C 37Z 142T	For brass, soft spel- ter,		
White metal, ord	•, •	28.4 <i>A</i> .			~
" " har	đ	35 C, 13 Z, 2.2 T.	Hard, for iron, For steel,	2 <i>C</i> , 1 <i>Z</i> , 700	Jo
		56C, 45Z, 12 arse-	For steel,	19S3C;1Z.	
Drooting motal,		nic.	Lot min or ass work,		
Metal, expand in	cool-		Pewterer's soft sol-		
ing.		75L,16.7A, 8.3B.	der,		
3,		, ,	Pewterer's soft sol-		
Imitat	ion (of Gold.	der,	1D, 1D, 2T,	
		$C_{\infty} = 91 C 13 T$	Gold solder,	1910	
Melt separately,		$\begin{cases} x = 21C, 13T. \\ y = 62C, 9Z. \end{cases}$	Silver solder, hard, soft,	28 1 braga wire	
Gold imitation.		y = 020, 92.	For Lead, .	16 T 33 T.	
dola illitation.		119,000	prof Boat,	101,0011.	

Tempering of Steel.

The property of heat to color steel or iron can be applied for ascertaining the temperature in flues and chimneys of steam-boilers, and for other temperatures limited between 430° and 600° Fah.

Yellow, very faint, for lancets,	 4300
" pale straw, for razors, scalpels,	4500
full, for penknives and chisels for cast iron,	4700
Brown, for scissors and chisels for wrought iron,	4900
Red, for carpenters' tools in general,	510°
Purple, for fine watch-springs and table-knives,	530°
Blue, bright, for swords, lock-springs,	 5500
" full, for daggers, fine saws, needles,	5600
" dark for common saws	 6000

Relative Hardness, H, of Substances.

	1 1	1			
MINTRALS.	Н.	METALS.	H.	Woods, Dry.	H.
Diamond, Ormuz,	100	Cast steel, hardened,	65	Chonta, S. Am., .	28
Diamond, Pink,	97	Cast steel, unhard.,	40	Lignum vitæ,	25
Diamond, Yellow,	94	Cast iron,	38	Ebony, .	24
Diamond, Cubic,	92	Iron, hammered, .	37	Pomegranate,	23
Sapphire,	90	Pure iron, .	35	Boxwood,	22
Topaz,	80	Antimony, ham.,	36	Oak, very old,	22
Garnet,	72	Antimony, cast,	32	Oak, ordinary,	21
Agate,	71	Platinum, cast,	40	Mulberry, .	20
Amethyst,	71	Platinum, ham.,	45	Cedar, India,	20
Quartz,	70	Brass, common .	32	Beech,	19
Ruby, pala Brazil,	65	White metal, hard,	38	A rib	18
Ruby,	64	Gold, hammered,	30	Alder,	18
Iron pyrites, .	63	Gold, cast,.	26	Apple tree,	17
Opal, .	62	Copper, ham.,	34	Plum tree,	16
Felspar,	60	Copper, cast,	29	Vew.	15
Fluor spar,	40	Silver, ham.,	32	Yew, Maple,	14
Copper pyrites, .	38	Silver, cast,	27	Pine, yellow,	14
Calcareous spar,	30	Zinc,	26	Hazel,	13
Anthracite coal, .	28	Aluminum, .	24	Cedar, wild,	13
Galena,	27	Tin, ham.,	24	Birch,	12
Amber,	23	Tin, cast, .	20	Thin	12
Granite,	22	Babbitt's metal, .	20	Pine, white,	11
Gypsum,	20	Silenium,	22	Spruce,	10
Bituminous coal,	16	Bismuth,	20	Sassafras,	9
Chalk,	15	Lead, ham.,	18	Hemlock,	8
Talc,	10	Lead, cast,	15	Cork,	5
	1	A	1 -0 (, 00111,	0

Mr. Chapman has arranged a scale for the hardness of minerals, as follows:

- 1 yields easily to the nail.
- 2 yields with difficulty to the nail, or merely receives an impression from it.

 Does not scratch a copper coin.
- 3 scratches a copper coin, but is also scratched by it, being of about the same hardness.
- 4 not scratched by a copper coin. Does not scratch glass.
- 5 scratches glass, though rather with difficulty, leaving its powder on it. Yields easily to the knife.
- 6 scratches glass easily. Yields with difficulty to the knife.
- 7 does not yield to the knife. Yields to the edge of a file, though with difficulty.
- 8, 9 and 10, harder than flint.

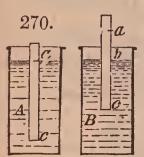
The numbers in Chapman's scale multiplied by 10 will correspond with the hardness in the preceding table.

Charcoal from 1000 Weights of Dry Wood.

Oak,	226 232 254 206	Pine, 200 Birch,	184 174
Elm,	195	Scotch Pine, . 164 Sycamore,	197

HYDROMETER.

A pody wholly immersed in a liquid will lose as much of its weight, as the weight of the liquid it displaces.



A floating body will displace its own weight of the liquid in which it floats.

A cylindrical rod of wood or some light materials, being set down in two liquids, A and B, of different specific gravities, when in equilibrium it will sink to the mark a in the liquid A, and to b in the liquid B; then the specific gravity of A:B=b,c:a,c, or inverse as the immersed part of the rod. This is the principle upon which a hydrometer is constructed.

Table showing the comparative Scales of Gay Lussac and Baumè, with the Specific Gravity and Proof, at the temperature of 60° Fahr.

	-			
A	Gay Lussac's.	Baumè s	Specific Grav.	Proof.
271.			_	
	100	46	•796	100 7
- 90	95	40	*815	
- 80			010	
-70	6 90 €	36	•833	82 6
-60	ਕੁ 85	33	•848	7210
-	alcohol.	31	•863	62 5
-50	ন্তি 75	28	·876	62 52 centage Proof.
-40	g 70	26	•889	42 84
30			1007	
	ng 65	24	•901	
	5 60	23	•912	22 2
	o 55	21	•923	12]
	25 0 45 40 40 40 40 40 40 40 40 40 40 40 40 40	19	. 933	0 Proof.
	t 45	18	•942	8)
三 三	u 40	17	•951	
	υ 1 0			18 29 35 Lood.
	35	16	•958	29 } 0
	Per 30	15	•964	18 Childer Proof.
	25	14	•970	48
[-]				
4				

HYDROSTATICS.

Letters denote.

A and a = areas of the pressed surfaces in square feet.

I and p = hydrostatic pressure in pounds.

 $d = \text{depth of the centre of gravity of } \mathbf{A}$ or a under the surface of the liquids $\ln f \cdot \text{et}$.

S =specific gravity of the liquid.

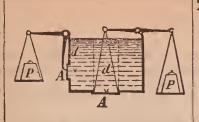
Example 1. Fig. 272. The plane A = 3.3 square feet, at a depth of d = 6 feet under the surface of fresh water. Required the pressure P = ? Specific gravity of fresh water S = 1.

 $P = 62.5 \text{A} d = 62.5 \times 3.3 \times 6 = 1237.5 \text{ pounds.}$

Example 2. Fig. 275. The area of the pistons A = 8.5 square feet, a = 0.02 square feet, l = 4 feet, e = 9 inches, and F = 18 pounds. Required the pressure P = ?

$$P = \frac{Fl \mathbf{A}}{e \mathbf{a}} = \frac{18 \times 4 \times 8.5}{0.75 \times 0.02} = 40800 \text{ pounds.}$$

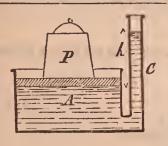
It must be distinguished that the centre of pressure and centre of gravity of the planes, are two different points; the centre of pressure is below the centre of gravity, when the plane is inclined or vertical.



$$P = 62.5 \text{ SAd,}$$

$$A = \frac{P}{62.5 \text{ Sd,}}$$

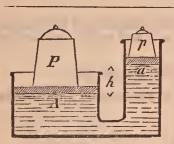
$$d = \frac{P}{62.5 \text{ SA.}}$$



The Hydrostatic paradox.

The pressure P is independent of the width of column C.

P = 62.5 S A h. (same as above.)

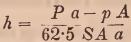


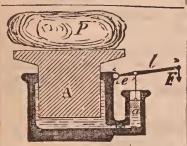
274.

$$P = A\left(62.5Sh + \frac{p}{a}\right)$$

$$p = a\left(\frac{P}{A} - 62.5Sh\right),$$

$$h = \frac{Pa - pA}{A}$$

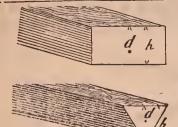




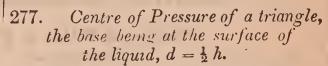
275. Bramali's Hydraulic Press.

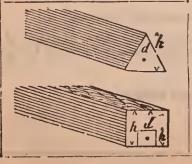
$$P = \frac{F \, l \, A}{e \, a} \, , \qquad A = \frac{P \, e \, a}{F \, l} \, ,$$

$$F = \frac{P e a}{A}$$
, $\alpha = \frac{F A l}{P e}$.

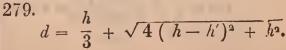


276. Centre of Pressure of a rectangle, the upper edge at the surface of the liquid $d = \frac{2}{3} h$.





Centre of Pressure of a triangle, the vertex being at the surface of the liquid. $d = \frac{3}{4} h$.



HYDRAULICS.

Let the vessel A, Fig. 284, be kept constantly full of water up to the water line w. In two horizontal faces lower than the water line w, are made orifices a and a', through which the water will pass up vertical nearly to the water line w. Omitting the resistance of air, &c., the jet should theoretically reach the water line w; practically it reaches 0.967h.

It is evident that the velocity of the jet through the orifices, must be the velocity due to a body falling the height h, according to the law of force of

gravity.

Letters denote.

Q =actual quantity of water discharged per second or in the time t, in cubic

h = head, or height of water over the orifice.

t =operating time in seconds.

a = area of the orifice in square feet.

m = the coefficient for contraction. (See Fig. 299) G = gallon of 231 cubic inches discharged in the time t. V = velocity through the orifice in feet per second.

Example 1. Fig. 284. How many gallons of water will be discharged in five minutes, through an orifice of 0.025 square feet, applied at 8 feet under the level of the water?

$$G = 37.75 a t /h = 37.75 \times 0.025 \times 5 \times 60 /8 = 800 \text{ gallons.}$$

Fig. 285. The weight P can represent the weight of a column of water whose

height =
$$\frac{P}{62.5A} = \frac{h'}{0.967}$$
, acting on the area A.

Fig. 286. n = number of down, strokes per minute, s = stroke of piston; theair vessel C = 6A s at the pressure of the atmosphere.

Example 2. Fig. 286. How many double strokes must be made per minute by the lever of a hand pump, to throw up 22 cubic feet of water 18 feet high, in the time of 8 minutes and 15 seconds; the levers l = 30 inches, e = 8 inches, s = 0°6 feet, F = 20 pounds? $8 \times 60 + 15 = 495$ seconds.

$$n = \frac{3630 Q h' e}{t s F l} = \frac{3630 \times 22 \times 18 \times 8}{495 \times 0.6 \times 20 \times 30} = 64.5 \text{ strokes per minute.}$$

Example 3. Fig. 294. A vessel of rectangular form is of dimensions A = 6 square feet, the height h = 5 feet. What time will it take the water level to sink 2 feet, when the orifice a = 0.212 square feet.

$$t = \frac{A (h - h')}{2.52a(y'h + y'h)} = \frac{6(5 - 3)}{2.52 \times 0.212(y'5 + y'3)} = 5.66.$$

Motion of Water in Pipes.

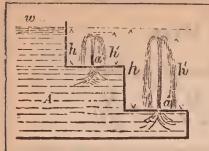
Letters denote.

L = extreme length of the pipe in feet.

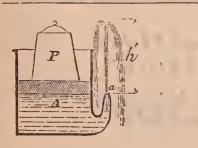
d =inside diameter in feet, and uniform throughout the length L.

Example 4. Fig. 287. What will be the velocity of the water through a pipe of 0 45 feet inside diameter, and L=68 feet long, the head pressure of water being h == 8 feet?

$$V = 48$$
 $\sqrt{\frac{0.45 \times 8}{68 + 50 \times 0.45}} = 9.6$ feet per second.

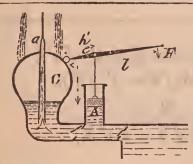


284.	¥ = 8.	$02\sqrt{h}$	
Q = m a	t 8.02 V	$\sqrt{h}=5.08$	$5 a t \sqrt{h}$
G=37	77 $at\sqrt{p}$	\overline{h} , $m =$	0.63, 0.967 h
h	Q^2	jet =	0.967 h,
$h = \overline{25}$	$5 a^2 t^2$		



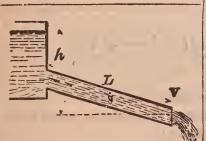
$$V = 1.015 \sqrt{\frac{P}{A}}, \quad Q = at \sqrt{\frac{P}{A}},$$

$$G = 7.5at \sqrt{\frac{P}{A}}, \quad h' = \frac{P}{60.5 A}.$$



286.
$$Q = at \sqrt{\frac{Fl}{Ae}}, \quad n = \frac{3630 \ Qh'e}{ts Fl},$$

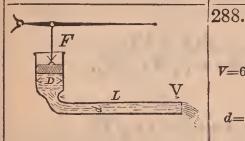
$$G=7.5 \ at \sqrt{\frac{Fl}{Ae}}, \quad h'=\frac{Fl}{60.5 \ Ae}$$



287. Motion of Water in Pipes.

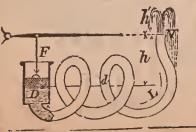
$$V=48\sqrt{\frac{d h}{L+50d}}, \quad Q=37.7d^{2}\sqrt{\frac{d h}{L+50d}},$$

$$d=0.24\sqrt{\frac{L Q^{2}}{h}}, \qquad h=\frac{Q^{2} (L+5 d)}{142 d^{5}}.$$



Motion of Water in Pipes.
$$V=6.86\sqrt{\frac{d F}{D(L+50d)}}, Q=5.38d^2\sqrt{\frac{d F}{D(L+50d)}}$$

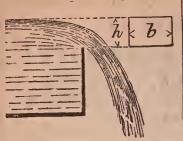
$$d=1.68\sqrt{\frac{L D Q'}{F}}, F=\frac{Q^2D(L+5d)}{2.9d^3}.$$



289.

$$V=6,86 \sqrt{\frac{d(F-49D^2h)}{D(L+50d)}} \qquad Q=5.38Vd^2t$$

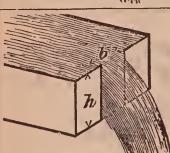
$$h'=\frac{V^2}{66\cdot 5}, \quad h'=\frac{D \sqrt{s} n}{57\cdot 65d.}$$



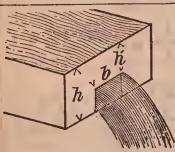
291.

Weirs.

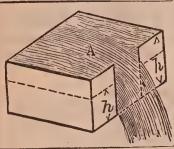
 $Q = k \ b \ t$. See Table for Weirs. $t = \frac{Q}{k \ b}$, $b = \frac{Q}{k \ t}$,



 $Q = 5.35m \ b \ h \ t \sqrt{h},$ $G = 40m \ b \ h \ t \sqrt{h},$ $t = \frac{Q}{5.35m \ b \ h \sqrt{h}},$

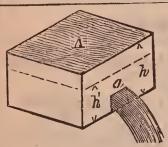


292. $Q = 5.35m \ b \ t(h\sqrt{h} - h' \sqrt{h'}),$ $G = 40m \ b \ t(h\sqrt{h} - h' \sqrt{h'}),$ $t = \frac{Q}{5.35m \ b(h\sqrt{h} - h' \sqrt{h'})},$



293. $t = \frac{0.95m \ A(\sqrt{h} - \sqrt{h'})}{b \ \sqrt{h \ h'}},$

A = area of the vessel in square feet. t = time in seconds, in which the water level will sink the space h - h'.



294. $t = \frac{A(h-h')}{4m \ a \ (\sqrt{h}+\sqrt{h'})},$

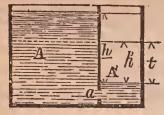
$$Q = 4m \ a \ t(\sqrt{h} + \sqrt{h'}),$$

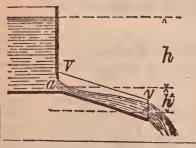


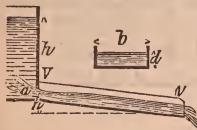
$$t=\frac{A}{3.85a\ m}(\sqrt{h}-\sqrt{h'}),$$

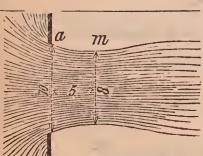
$$a = \frac{A\sqrt{h}}{3.85t'm}, \quad t' = \frac{A\sqrt{h}}{3.85am},$$

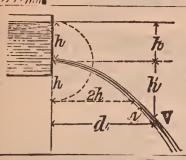


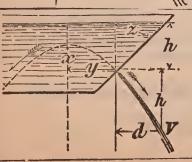












$$t = \frac{A A' \sqrt{h}}{13 \cdot 7 m a \sqrt{A + A'}},$$

$$h = \frac{A h'}{A + A},$$

297. Short Drain.

$$V = \frac{8 \cdot 02 \sqrt{h}}{\sqrt{1 + (\frac{1}{m} - 1)^2}},$$

$$v = \sqrt{V^2 + 32 \cdot 1 h'},$$

 $Q = a \, mVt. \, from \, V \, to \, v \, about \, 6 \, \sqrt{a}$

298. Long Drain.
$$V = \frac{8 \cdot 02 \sqrt{h}}{\sqrt{1 + (\frac{1}{m} - 1)^{2}}},$$

$$v = 3\left(\sqrt{h} + 14.145\sqrt{\frac{h's}{l a}}\right)$$

$$s = b+2d$$
 $l = V to v, feet.$

299. Proportions of the contracted Vein.

 $a: m = 10^{\circ}: 8^{\circ}. \quad m = 0.64 \ a.$

m = 0.64 when contracted on 4 sides.

" 3 sides. m = 0.72

" 2 sides. 66 m = 0.866

m = 0.9" 1 side.

300.

The form of the Vein is a Parabola. $d=2\sqrt{hh'}, \qquad V=8\sqrt{h+h'}$

 $Q = 8 m a t \sqrt{h},$

 $tan \ v = \frac{2 \ h'}{d} \ , \qquad h = \frac{d^{\circ}}{4 \ h'} \ .$

301.

 $x = sin^2 z h$ y = sin. z cos. z h.

 $d = 2 \sqrt{(h'+x)(h-x)} - y$

 $Q = 8 mat \sqrt{h} \qquad V = 8\sqrt{h+h'}.$

Example 5. Fig. 289. Required the velocity and quantity of water discharged in a long pipe or hose of L=135 feet long, and d=0.17 feet, attached to a handpump of D=0.2 feet in diameter P=44 pounds, and the end of the pipe elevated h=200 feet above the piston D?

$$V = 6.86 \sqrt{\frac{0.17(44 - 49 \times 0.2^2 \times 20)}{0.2(135 + 50 \times 0.17)}} = 1.95 \text{ feet per second.}$$

 $Q=1.95\times5.38\times0.2^2=0.042$ per second $\times60=2.52$ cubic feet per minute. s=0.8 feet, the stroke of piston, we shall have

$$n = \frac{2.52}{0.8 \times 0.785 \times 0.22} = 100 \text{ strokes per minute.}$$

Table for Water flowing over Weirs.

This table is set up from careful experiments on a large scale, and is suited for weirs only. See Fig. 290. $Q = 4.327 b \sqrt{h^3}$.

RULE. Multiply the width b, in feet, of the weir by the coefficient k, and the product is the quantity of water discharged per second, in cubic feet. h is the height as represented by Fig. 290. The width b should be b > h.

Example 6. How much water will flow over a weir of b=5 feet, h=0.5 feet, in one minute? Q=k b $t=1.1295 \times 5 \times 60=338.35$ cubic feet.

h. inches.	h. feet.	m.	k.
0.4	0.033	0.424	0.01365
0.8	0.066	0.417	0.05452
1.2	0.100	0.412	0.10592
1.6	0.133	0.407	0.16616
2.4	0.200	0.401	-0.29171
3.2	0.266	0.397	0.44480
4.	0.333	0.395	0.63111
6.	0.500	0.393	1.1295
8	0.666	0.390	1.7464
9.	0.750	0.385	2.0331
12.	1.000	0.376	3.1350

On the Velocity of Water in Rivers.

Notation of Letters.

F = fall of the river in feet per mile.

R = hydraulic radius in feet, or the area of the cross-section of the river in square feet, divided by the wet perimeter in feet.

V = mean velocity of the water in inches per second.

M = mean velocity in miles per hour.

$$V = 10.9 \sqrt{FR},$$
 $F = \frac{V^2}{118.8 R}.$ $M = 0.619 \sqrt{FR},$ $F = \frac{M^2}{3.83 R}.$

The mean velocity of the water throughout the whole section of the river is to the velocity at the surface in the middle of the river as 84:100, or as 100:120.

Example 1. The cross-section of a river is measured to be 560 square feet, and the wet perimeter 196 feet; the fall of the river is 5 feet per mile. Required, the hydraulic radius and the mean velocity of the water in miles per hour?

Hydraulic radius
$$R = \frac{560}{196} = 2.86$$
 feet.

Mean velocity
$$M = 0.619 \sqrt{5 \times 286} = 2.34$$
 miles per hour.

Example 2. The velocity of the surface in the middle of a river is 36 inches per second; hydraulic radius R=2 feet. Required, the mean velocity and the fall of the river per mile?

Mean Velocity $V = 36 \times 0.84 = 30.24$ inches per second.

Fall
$$F = \frac{30.24^2}{118.8 \times 2} = 3.8487$$
 feet per mile.

Obstruction in Rivers.

R =rise of water in feet caused by obstruction.

A = sectional area in square feet of river unobstructed, and a = that when obstructed. V = velocity in feet per second of the water without obstruction.

$$R = \left(\frac{V^2}{5.86} + 0.05\right) \left(\left(\frac{A}{a}\right)^2 - 1 \right).$$

Resistance to a Plane Facing a Current of Water

or Moving in Still Water.

A = area of the plane in square feet.

R = resistance in pounds.

V = velocity in feet per second.

$$R = A V^2$$
, in fresh water.

$$R = 1.032 A V^2$$
, in salt or sea water.

When the plane is set at an angle of less than 90° to the direction of motion, the resistance will be, when $\phi = \text{angle of the plane}$,

$$R = A (V \sin \phi)^2$$
, in fresh water.

$$R = 1.032 A (V \sin \phi)^2$$
, in salt water.

Theoretical Velocity of Water, due to Head of Fall.

See table for falling bodies, page 308, in which the column S represents the head of fall in feet.

To find the Number of Gallons of Water G which can be raised per Hour from a Well of Depth D,

By a Suitable Double-action Force-and-lift-pump.

D may also denote the height to which water may be raised in water-works.

One man working a crank,
$$G = \frac{18000}{D}$$

A donkey working a gin,
$$G=rac{36000}{D}$$
 .

A horse working a gin,
$$G = \frac{126000}{D}$$
.

Per steam horse-power,
$$G = \frac{190000}{D}$$
,

or 0.8 of the natural effect.

Example 1. How many gallons of water can be raised per hour from a well 150 feet deep by a horse working a gin?

$$G = \frac{126000}{150} = 840$$
 gallons, the answer.

Example 2. How many gallons of water can be raised per hour to a height of D = 150 feet by a steam-engine of 120 actual horse-power?

$$G = \frac{190000 \times 120}{150} = 152,000$$
 gallons, the answer.

MOTION OF WATER IN PIPES.

Letters denote-

Q = cubic feet of water passed through the pipe per minute. D = inside diameter of the pipe in feet.

L =length of the pipe in feet, increased by 50 diameters.

H = head of fall in feet.

V = velocity of the water in the pipe in feet per minute.

$$Q = 2356 \sqrt{\frac{H D^5}{L}}, \qquad D = \frac{1}{22.329} \sqrt[5]{\frac{Q^2 L}{H}}, \qquad V = 3000 \sqrt{\frac{H D}{L}}.$$

Example 1. A water-pipe of D = 1.75 feet in diameter, $L = 36,000 + 50 \times 1.75$ = 36087.5 feet long, head pressure H = 390 feet. Required, how much water it can discharge per minute?

$$Q = 2356 \sqrt{\frac{390 \times 1.75^5}{36087.5}} = 992.26.$$

Example 2. At a distance of 27960 feet from a water-work is required Q = 564 cubic feet of water per minute, head pressure being H = 256 feet. Required, the diameter of the pipe? L = 27960 + 50 = 28010 feet.

$$D = \frac{1}{22.329} \sqrt[5]{\frac{564^2 \times 28010}{256}} = 1.4436 \text{ feet.}$$

Example 3. A water-pipe of D=0.75 feet in diameter, L=8650+50=8700 feet, has a head pressure of H=128 feet. Required the velocity v=l of the discharge.

$$V = 3000 \sqrt{\frac{128 \times 0.75}{8700}} = 315.13$$
 feet per minute.

Consumption of Water in Cubic Feet per head of Population,

Including all Uses, as for Manufactories, Fires, etc., in 24 hours.

2.73 | July, 4.58 3.37 | August, 4.75 3.50 | Sept., 4.61 January, 4.46 February, May, November, 4.12 June, December. 3.61 March.

On the Flow of Water in Bends of Pipes.

Notation of Letters.

L = the whole length of pipe in feet, straight and curved or bent, increased with 50 D.

R = radius in feet of the bend of the centre-line of the pipe.

 ϕ = angle of deflection or bend of pipe in degrees. Should the pipe have several bends, add all the angles to ϕ .

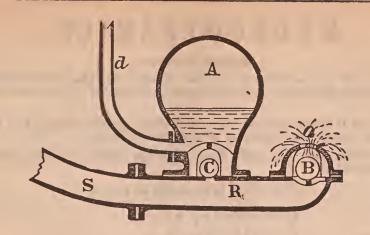
Sin. ϕ to be used only up to 90°, and disappears in the formulæ for greater angles.

D= inside diameter in feet of the pipe; V= velocity of the water in feet per minute; and H= head of fall in feet; Q= cubic feet of water dis-

$$Q = 2356 \sqrt{\frac{HD^5}{L} \left(\frac{90}{\phi + 90}\right) \left(1 + \frac{R \sin \phi}{R + 10}\right)}.$$

$$V = 3000 \sqrt{\frac{HD}{L} \left(\frac{90}{\phi + 90}\right) \left(1 + \frac{R \operatorname{Sin.} \phi}{R + 10}\right)}.$$

The formulæ will answer for a pipe of the form of a screw-spiral.



THE HYDRAULIC RAM.

This hydraulic motor appears to be too little known in many parts of the world. The author of this book has been in the interior of many countries where water is raised in a very rude and laborious way, and where the hydraulic ram would be of great utility. The useful effect of the ram, like that of water-wheels and turbines, depends much upon its construction. In ordinary cases it returns about 50 per cent. of the natural effect. That is, the quantity of water (q) multiplied by the height (h) of the delivery above the ram will be about 50 per cent. of the quantity of water (Q) working the ram, multiplied by the head of fall (F), in the ame unit of time.

$$qh = 0.5QF.$$
 $q = \frac{0.5QF}{h}.$ $Q = \frac{2qh}{F}.$

Q and q can be expressed in any unit of volume or weight.

Fand h can be expressed in any unit of length.

But let us assume Q and q to be cubic feet per minute,

F and h = fall and height in feet,

L = length in feet and D = diameter in inches of the supply-pipe S

l = length and d = diameter of the delivery-pipe d.

Then
$$D = \sqrt[5]{\frac{2Q^2(L+5D)}{F}}$$
, and $d = \sqrt[5]{\frac{4q^2(l+5d)}{h}}$.

Description of the Hydraulic Ram.

Reference to the figure above.

The water working the ram is supplied through the pipe S, and escapes through an opening at o, until it has gained a velocity sufficient to raise the valve or ball B, which suddenly stops the current, and causes an excessive pressure in the ram R, which opens the valve or ball C; the water is forced into the vessel and airchamber A, and finally through the delivery-pipe d to its destination. When equilibrium of pressure is restored between S and R, the ball B falls, and the operation is repeated. The ram can make as much as 200 strokes per minute, depending upon its size.

The length of the supply-pipe S should not be less than five times the height of the fall F, because it is the dynamic momentum (see page 310) in the pipe columns of water which works the ram. But the pipe may be made 10 times, or

more, the height of the fall.

HYDRODYNAMICS.

Water Power.

The natural effect concentrated in a fall of water is equal to the weight of the quantity of water passed through per second, multiplied by the vertical space it falls.

Fig. 297. Let Q be the quantity of water which passes through the orifice a in the time t = 1'' second, in cubic feet of 62.5 pounds each.

h = the vertical space the water falls; then the value or natural effect of the fall is at the orifice a.

$$P = 62.5 Q h$$
, effects of power.

But,

$$Q = 5.06 \ a \ h \sqrt{h}$$
;
 $P = 315.5 \ a \ h \sqrt{h}$.

Then we have

This will be in horse power. $H = 0.573 \, a \, h \sqrt{h}$, $H = 0.1134 \, Q \, h$,

$$h = \frac{1}{1.07} \sqrt[3]{\frac{\overline{H}^2}{a^2}}, \qquad h = \frac{H}{0.1134 \ Q}.$$

Example 1. In a creek passes 18 cubic feet of water per second. How high must that creek be dammed up to produce an effect of ten horses?

$$h = \frac{10}{0.1134 \times 18} = 4.9$$
 feet, the answer.

Comparison of Columns of Water in Feet.

Mercury in inches, and pressure in pounds, per square inch.

Pounds	Water.	Merc'ry.	Water.	Merc'ry.	Pounds.	Merc'ry	Water.	Pounds.
Pr.sq.in.	Feet.	Inches.	Feet.	Inches.	Pr. sq. in.	Inches.	Feet.	Pr. sq. in.
1	2.311	2.046	1	0.8853	0.4327	1	1.1295	0.4887
2	4.622	4.092	2	1.7706	0.8654	2	2.2590	0.9775
3	6.933	6.138	3	2.6560	1.2981	3	3.3885	1.4662
4	9.244	8.184	4	3.5413	1.7308	4	4.5181	1.9550
5	11.555	10.230	5	4.4266	2.1635	5	5.6476	2.4437
6	13.866	12.2276	6	5.3120	2.5962	6	6.7771	2.9325
7	16.177	14.322	7	6.1973	3.0289	7	7.9066	3.4212
8	18.488	16.368	8	7.0826	3.4616	8	9.0361	3.9100
9	20.800	18.414	9	7.9680	3.8942	9	10.165	4 3987
10	23.111	20.462	10	8.8533	4.3273	10	11.295	4.8875
11	25.422	22.508	11	9.7386	4.7600	11	12.424	5.3762
12	27.733	24.554	12	10.624	5.1927	12	13.554	5.8650
13	30.044	26.600	13	11.509	5.6255	13	14.683	6.3537
14	32.355	28.646	14	12.394	6.0582	14	15.813	6.8425
15	34.666	30.692	15	13.280	6.4909	15	16.942	7.3312
16	36.977	32.738	16	14.165	6.9236	16	18.072	7.8200
17	39.288	34.784	17	15.050	7.3563	17	19.201	8.3087
18	41.599	36.830	18	15.936	7.7890	18	20.331	8.7975
19	43.910	38.876	19	16.821	8.2217	19	21.460	9.2862
20	46.221	40.922	20	17.706	8.6544	20	22.590	9.7750
21	48.532	42.968	21	18.591	9.0871	21	23.719	10.264
22	50.843	45.014	22	19.477	9.5198	22	24.849	10.752
23	53.154	47.060	23	20.362	9 9525	23	25.978	11.241
24	55.465	49.106	24	21.247	10.385	24	27.108	11.7300
25	57.776	51.152	25	22.133	10.818	25 .	28.237	12.219
26	60.087	53.198	26	23.018	11.251	26	29.367	12.707
27	62.398	55 244	27	23.903	11.683	27	30.496	13.196
28	64.709	57.290	28	24.789	12.116	28	31.626	13.685
29	67.020	59.336	29	25.674	12.549	29	32.755	14.174
30	69.331	61.386	11 30	26.560	12.981	30	33.885	1 14.662

WATER-WHEELS.

Water-wheels are of two essential kinds, namely, Vertical and Horizontal.

The Vertical are subdivided into

Overshot-wheels, Undershot-wheels, Breast-wheels, and High-breast and Low-breast wheels.

The Horizontal are with Floats, Screw-wheels, Turbine, Reaction-wheels, &c.

Waterwheels do not transmit in full the natural effect concentrated in a fall of water; under most favourable circumstances 80 per cent. has been utilized, but under poor arrangements only 20 per cent. may be expected.

Example 1. Fig. 302. The vertical section of the immersed floats of an undershot-wheel in a mid-stream is a = 27 square feet, velocity of the stream V = 8.6, and v = 4 feet per second. Required the horse-power of the wheel H = 2?

$$H = \frac{\mathbf{a} \ v}{200} (V - v)^2 = \frac{27 \times 4}{200} (8.6 - 4)^2 = 11.4 \text{ horses.}$$

Example 2. Fig. 307. On a breast-wheel is acting Q=88 cubic feet of water per second, the head h=8 feet, velocity of the wheel at the centre of the buckets v=5 feet per second; the water strikes the buckets at an angle $u=8^\circ$ and velocity V=7 feet per second. Required the horse-power of the wheel, H=7

$$H = \frac{88}{11.4} \left(8 + \frac{5}{25} (7 \times \cos.8^{\circ} - 5) \right) = 65 \text{ horses.}$$

Example 3. Required the effect of Poncelet's wheel, the head h=4 feet, and the orifice a=5 square feet, the velocity of the wheel at the centre of pressure of the floats is v=6.78 feet per second?

$$V = 6.91 \overline{\sqrt{4}} = 13.82$$
 feet per second.
 $Q = 6.5 \times 5 \times \sqrt{4} = 65$ cubic feet per second.
 65×6.78

$$H = \frac{65 \times 6.78}{197} (13.82 - 6.78) = 15.8 \text{ horses.}$$

Example 4. Fig. 309. A saw-mill wheel is to be built under a fall of h = 18 feet, and to make n = 110 revolutions per minute. Required the proper diameter of the wheel.

$$D = \frac{100}{110} \sqrt{18} = 3.857$$
 feet,

at the centre of pressure of the buckets.

Velocity $V = 8\sqrt{18} = 33.94$ feet per second.

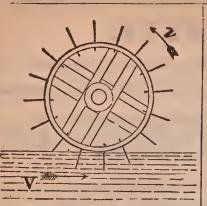
Velocity
$$v = \frac{3.14 \times 3.857 \times 110}{60} = 22.2$$
 feet per second.

The fall discharged 30 cubic feet of water per second. Required the horse power of the wheel. H=?

$$H = \frac{30 \times 22.2}{200}$$
 (33.94 - 22.2) = 39 horses.

How many square feet of dry Pine can it saw per hour? See page 264. 30×39 =1170 square feet.

The saw is meant to be applied direct on the wheel shaft.

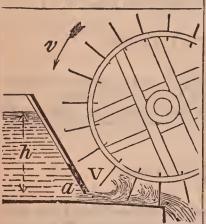


Undershot wheel in a mid-stream.

$$H = \frac{\mathbf{a} \ v}{200} (V - v)^2,$$

When V=2v about, the effect will be,

$$H = \frac{\mathbf{a} V_3}{1600}$$
, $\mathbf{a} = \text{area of float.}$



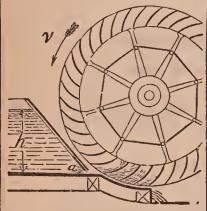
303.

Undershot-Wheel.

$$H = \frac{Q}{454}(V - v),$$

$$H = \frac{m \ a \ v}{86.8} (V - v) \sqrt{h_*}$$

When
$$V=2v$$
, about, $H=\frac{a\ h\sqrt{h}}{0.47}$.



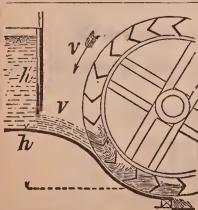
304.

Poncelet's Wheel.

$$H=\frac{Q v}{228}(V-v)$$
, when $h>5$ feet,

$$H = \frac{Q v}{197} (V - v) \text{ when } h < 5 \text{ feet,}$$

$$Q = 8m \, a\sqrt{h}, \qquad V = 6.91\sqrt{h}.$$

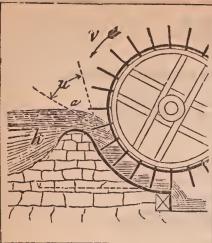


305.

Breast-Wheel with Parabolic drain.

$$H = \frac{Q}{12} \left[h + \frac{v}{28} (V - v) \right],$$

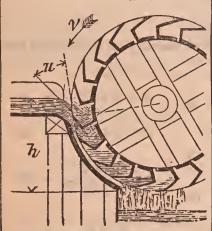
$$Q = 6.5a\sqrt{h'}.$$



306. Low-breast Wheel.

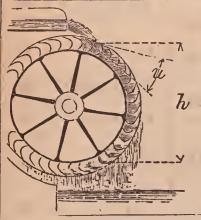
$$H = \frac{Q}{11\cdot 2} \left[h + \frac{v}{32} \cdot \left(V \cos u - v \right) \right]$$

$$Q = kb$$
. $V = \frac{Q}{a}$. See table for weirs.



307. Breast Wheel.

$$H = \frac{Q}{11\cdot4} \left[h + \frac{v}{25} (V \cos u - v) \right]$$

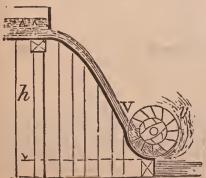


308. Over-shot Wheel.

$$H = \frac{Q}{13.7} \left[h + \frac{v}{21.5} \left(V \cos u - v \right) \right]$$

Proper velocity about $n = \frac{35 D + 100}{D}$.

revolutions per minute.



309. Saw-Mill Wheel.

$$H = \frac{Q \, v}{200} \, (V - v)$$

Proper diameter of the Wheel,

$$D = \frac{100}{n} \sqrt{h}, \text{ in feet,}$$

n = revolutions per min.

TURBINES.

Letters denote.

Q = cubic feet of water passed through the turbine per second.

h = height of fall in feet.

D =diameter in inches of circle of effort in the turbine.

a = area in sq. in. of the conduit passage into the turbine wheel.

b = depth in inches of turbine buckets.
c = depth in inches of leading buckets.
r = breadth of turbine buckets in inches.
m = number of buckets in the turbine wheel.
m' = number of leading buckets.
n = number of revolutions of turbine per minute.
S and s = height of conduit and discharge in inches.
t = thickness of steel plate buckets in 16ths of an inches.

t = thickness of steel plate buckets in 16ths of an inch.

H= actual horse power of the turbine. l= length in feet of conduit pir d = length in feet of conduit pipe.

d' = diameter in inches of the discharge pipe.

W= Hydraulic pressure on the turbine wheel bearing on the end of the shaft.

$$H=0.1134\ Q\ h$$
 natural effect of the fall, - - 25
 $H=\frac{30\ Q^3}{a^2},$ actual horse power, 26
 $H=\frac{a\ h\sqrt{h}}{267.5},$ 26

The coefficient k can vary from 800 to 1200 without seriously affecting the per centage of the ultilized power, but it is best between 900 and 1000. This is a great advantage of the turbine over water wheels, that under the same head of fall it can run at different velocities and still utilizing the maximum effect. Whatever coefficient k adopted it must be kept the same throughout the construction of the turbine.

Jonval's Turbine has so many advantages above other hydraulic motors that it is considered sufficient to describe the construction of that

one only, but the principal formulas will answer for any kind of turbines.
On the accompanying plate is a drawing of a Jonval Turbine such as the Author of this Pocket Book has built in Russia. The buckets are not supported by concentric rings, but are fastened only on one side, which is considered more simple and convenient for replacing new backets. For falls over 30 feet it may be better to make it with concentric rings. When a turblne is to be constructed we have on the one side given the natural effect of the fall, and on the other side the actual work to be done, which latter should not exceed 66 per cent. of the former. Between these two points the turbine is to be so proportioned as to utilize the greatest possible effect with smallest expense of Machinery.

Jonval's turbine in good condition generally utilizes 60 to 80 per cent. Suppose a fall of h=25 feet, discharging Q=12 cubic feet of water per

second, the natural effect will be,

$$H = 0.1134 \times 12 \times 25 = 34$$
 horses,

of which 34×66=22.4 horses to be counted upon as the actual effect of the turbine.

Turbine shaft to make n=200 revolutions per minute with the assumed coefficient k=960. From these dates we will obtain all the principal dimensions of the turbine, namely,

$$D = \frac{960 \sqrt{25}}{200} = 24 \text{ inches.} - 1 \qquad r = \frac{48}{0.436 \times 24} = 4.6 \text{ in.} - - 6$$

$$a = \frac{20 \times 960 \times 12}{24 \times 200} = 48 \text{ sq. in.} \quad 10 \qquad b = \frac{0.625 \times 24}{\sqrt{25}} = 3 \text{ in.} - - - 19$$

$$m = 5\sqrt{24} = 24.5 \text{ say } 25. \quad - 17 \qquad c = \frac{0.78 \times 24}{\sqrt{22}} = 4 \text{ inches.} - - 20$$

$$m' = 4.5\sqrt{24} = 22 \text{ buckets.} - 18 \qquad t = \frac{25}{10} = 2.5, 16 \text{ ths.} - - - 8$$

In calculating the breadth r from formula 5, it must come inside of formula 7, if not the diameter D must be altered.

Now proceed with the construction as shown at the bottom of the plate, which represents a section of the buckets through the circle of effort of the turbine.

The drawing of the turbine is ? of an inch to the foot, and the construc-

tion of the buckets 3 inches to the foot.

Draw the base line AB, set off the angle of the leading buckets-10°. The distance between the leading buckets will in this case be $24 \times 3.14:22 = 3.43$ inches, set off this from S towards A, draw the straight part of the second bucket parallel to the first one, draw from S the line d d at right angle to the buckets, and e will be the centre for the curved part. From the centre of S draw the line o to the end of the second buckets, divide this line into eight equal parts take five of them as radus and draw from the end of the second bucket a circleare of about 50°, which will be the

propelling part of the turbine wheel bucket.

Distance between the wheel buckets will be $24 \times 3.14.25 = 3.02$ inches, set off this from A towards S, draw the second propelling arc. Set off from A the depth of the wheel buckets b=3 inches, set off 2 b to s, which will be the length of the first wheel bucket. Set off from s to u the distance between the buckets 3.02 inches. Make s=0.86 S. Draw from u a curved line in the form of a parabola that will leave the space s and tangent the line in the form of a parabola that will leave the space s and tangent the propelling circlears somewhere about x. Care must be taken that the discharging area a' of all the wheel buckets will be about 2 per cent. less than the conduit area a of all the leading buckets. The surface of the buckets should be made as smooth as possible, or even polished.

For very high falls the Hydraulic pressure W becomes very considerable.

and may recessitate another arrangement, namely, to lay the shaft horizontally and place on it two turbines, so that the leading buckets are either between or outside of the wheels; but then comes another disadvantage, namely, that the number of revolutions will be greatly increased and may be required to gear it down 10 to 20 times to the proper speed of the main shaft.

To avoid this as much as possible, take k = 800, and make $r = \frac{D}{8}$.

One great advantage with Jonval's turbine is that it can be placed almost anywhere between the high and low levels to suit the location, though it should not be more than 20 feet above the lower level; then, in order to utilize the whole fall, care must be taken to make the discharge-pipe perfectly air-tight. It is not necessary to make the discharge straight down from the turbine: it can be carried horizontally or inclined, as may suit the location. The author has built turbines similar to that represented on the accompanying plate, at General Maltzof's establishment, Kaluga, Russia.

Approximate or Proportionate Price of Turbines,

as fitted and delivered at the foundry, without shaftings or gearings, is-

$$\$ = \frac{400\sqrt{H}}{\sqrt[3]{F}},$$

in which H=horse power of the turbine and F the height of fall in feet.

Example. Required the price of a turbine, H = 100 horses, to work under a fall of F = 25 feet.

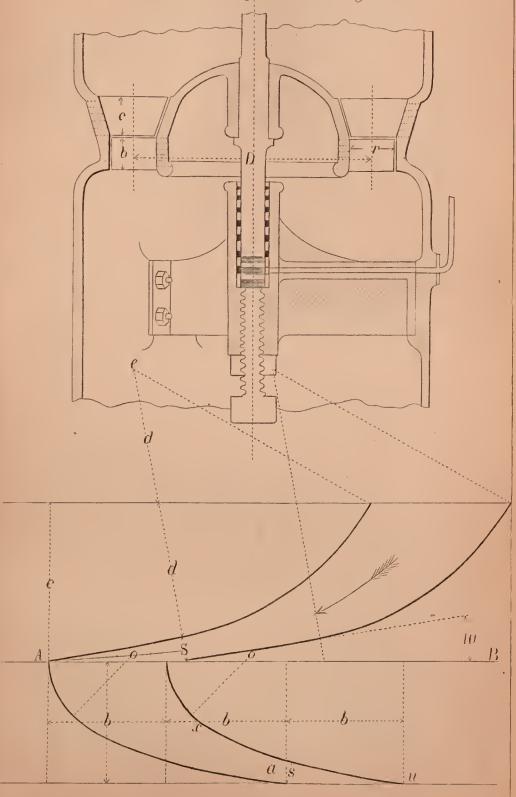
$$\$ = \frac{400\sqrt{100}}{\sqrt[3]{25}} = \frac{400 \times 10}{2.92} = 1375 \text{ dollars.}$$

Price List of Turbines in Dollars.

The same of the sa										
Horse	Head of fall in feet, F.									
power.	5	10	15	20	30	40	· 50	75	100	150
\overline{H}	\$	\$	\$	\$	\$	\$	\$	\$	\$	\$
1	234	186	163	148	130	117	110	95	86	76
2	330	263	231	209	183	167	154	134	122	107
4	467	372	326	295	258	235	218	190	172	151
6	552	455	400	262	316	288	266	232	211	185
8	660	526	462	418	365	332	308	269	244	213
12	808	642	565	510	447	405	377	329	300	261
16	935	742	654	590	516	468	434	380	345	302
20	1045	830	730	660	577	524	485	425	385	338
30	1280	1020	894	810	705	642	595	520	472	414
40	1480	1180	1035	932	815	740	686	600	545	476
50	1650	1320	1155	1045	913	828	768	671	610	532
60	1810	1440	1264	1140	1000	908	840	735	668	584
80	2090	1645	1460	1320	1155	1050	975	848	770	674
100	2340	1860	1630	1480	1295	1175	1090	948	860	753
125	2620	2080	1820	165 0	1440	1310	1220	1000	984	845
150	2860	2280	2000	1810	1580	1440	1330	1170	1060	924
175	3100	2460	2150	1950	1700	1550	1440	1260	1140	1000
200	3310	2630	2300	2090	1825	1655	1540	1350	1220	1066
225	3510	2790	2440	2215	1935	1755	1630	1430	1300	1130
250	3700	2940	2570	2335	2035	1850	1720	1500	1365	1195
275	3890	3090	2700	2450	2135	1945	1800	1580	1430	1255
300	4060	3225	2820	2560	2235	2030	1890	1650	1500 .	1300
350	4380	3480	3035	2760	2410	2190	2035	1780	1610	1410
400	4680	3720	3250	2950	2580	2340	2175	1900	1725	1510
450	5080	3950	3450	3130	2740	2480	2310	2015	1825	1600
500	5240	4160	3610	3300	2890	2620	2535	2125	1925	1685

JONVAL'S TURBINE,

as constructed by John W. Nystrom.





Coefficient for Capacity and Weight,

Names of Substances.	FFF.	Fii.	iii.	FF_2 .	F_{i2} .	ii2.	F^3 .	i ² .
Cubic inches,	1728	12	1	1356	9.42	0.785	903.7	0.523
Cubic feet,	1	694	•58	0.785	549	•41	0.523	3
Gallons,	7.476	0.052	·433	5.868	• .408	*34	3.91	226
Water, fresh,	62.5	0.433	0.036	49	0.34	. 283	32.7	0.019
Water, salt,	64.3	0.445	0.037	50.4	0.35	0.029	33.6	0.02
Oil,	57.5	0.4	0.033	45.1	0.313	0.026	30	0.017
Cast-iron,	450	3.12	0.26	353	2.45	0.204	235	0.136
Wrought-iron,	487	3.37	0.281	382	2.65	0.221	255	0.147
Steel,	490	3.4	0.283	385	2.67	0.222	257	0.149
Brass,	532	3.68	0.307	417	2.9	0.241	278	0.161
Tin, · · · ·	456	3.16	0.263	358	2.48	0.207	239	0.138
Lead, · · · ·	710	4.92	0.41	557	3.87	0.322	371	0.215
Zinc,	440	3.05	0.254	345	2.4	0.2	230	0.133
Copper,	556	3.85	0.321	436	3.03	0.252	291	0.168
Mercury,	850	5.9	0.491	666	4.63	0.385	445	0.257
Stone, common, -	156	1.08	0.09	122	0.85	0.071	82	0.047
Clay, - ·	135	0.936	0.078	106	0.735	0.061	70	0.04
Earth, compact, -	127	0.88	0.0733	99	0.692	0.058	66	0.038
Earth, loose,	95	0.66	0.055	74	0.517	0.043	50	0.029
Oak, dry,	58	0.4	0.033	44	0.316	0.026	30	0.017
Pine,	30	0.208	0.017	24	0.163	0.014	1.6	0.009
Mahogany,	66	0.457	0.038	52	0.36	0.03	34	0.02
Coal, stone,	54	0.375	0.031	42	0.294	0.024	28.2	0.016
Charcoal,	27.5	0.19	0.016	21	0.15	0.012	14.4	0.008

To Find the Weight and Capacity by this Table

RULE. The product of the dimensions in feet or in inches, as noted in the columns, multiplied by the tabular coefficient, is the capacity of the solid, or weight in pounds avoirdupois.

Example 1. A cistern is 6 feet long, 27 inches wide, and 20 inches deep. How many gallons of liquid can be contained in it?

 $6 \times 27 \times 20 \times 0.052 = 16848$ gallons.

Example 2. A cast-iron cylinder is 4.5 feet long, and 7.5 inches diameter Required the weight of it?

 $4.5 \times 7.5^{2} \times 2.45 = 620$ pounds.

SELECTION OF WATER COLOURS.

Blue. Real Ultramarine.

" French Blue. " Indigo.

" Cobalt Blue.

Green. Olive Green.

Yellow. Cadmium.

" Gamboge. " Ochre.

Red. Carmine.

" Crimson Lake.

Red. Rose Madder.

" Light Red.

Brown. Vandyke. Brown Madder.

Black. India Ink.

" Blue Black.

" Ivory Black.
" Lamp Black.

White. Chinese White.

PAPER.

1 ream = 20 quires = 480 sheets. 1 quire = 24 sheets.

Drawing Paper.

Cap, Demy, Medium, Royal, Super Roy	•	$13 \times 16 i$ $20 \text{ " } 15$ $22 \text{ " } 17$ $24 \text{ " } 19$ $27 \text{ " } 19$	nches. " " " " " "	Columbier, Atlas, Theorem, Double Elephant, Antiquarian, Emperor	•	33 " 34 " 40 " 52 "	26 28 26 31	inches.
Imperial, Elephant,		30 " 21 28 " 22	"	Emperor, Uncle Sam, .	•	40 " 48 "		

Continuous Colossal Drawing Paper, No. A and No. B, 56 inches wide, and of any required length. No A of this paper is excellent for mechanical drawings. Price, from 40 to 50 cents per yard.

Tracing Paper.

Double Crown,			30 by 20 inches. Glazed or Crystal.
Double Double Crown,		•	40 " 30 " Yellow or Blue Wove
Double Double Crown,	•	•	60 " 40 ") Tenow of Blue work

Finest French Vegetable Tracing Paper.

Grand Raisin (or Royal), 24 in. by 18. Grand Aigle, 40 in. by 27.

Mounted Tracing Paper.

This paper is mounted on cloth, and is still transparent; it will take ink and water-colors. It is 38 inches wide, and of any required length.

Vellum Writing Cloth.

Adapted for every description of tracing; it is transparent, durable and strong. It is 18 to 38 inches wide, and of any required length.

Weight and Marks of English Tin-plates.

	Plates	Length	Weight		Plates	Length	Weight
Brand.	per	and	per	Brand.	per	and	per
	Box.	Breadth.	Box.		Box.	Breadth.	Box.
	No.	In.	Lbs.		No.	In.	Lbs.
1 C	225	13 ‡×1 0	112	1 XX	225	13 3 ×10	161
2 C	225	13½ " 9¾	105	1 XXX	225	133 "10	182
3 C	225	123 " 91	98	1 XXXXX.	225	133 "10	203
H C	225	133 "10	119	1 XXXXXX.	225	133 "10	224
H X	225	137 "10	157	1 XXXXXXX.	225	133 "10	245
1 X	225	134 "10	140	DC	100	163 "121	98
2 X.	225	131 " 91	133	DX	100	163 " 121	126
3 X	225	123 " 91	126	DXX	100	163 "121	147
Leaded IC.	112	20 "14	112	DXXX	100	163 " 123	168
" IX.	112	20 "14	140	DXXXX.	100	16월 " 12를	189
ICW.	225	133 "10	112	SDC.	200	15 "11"	168
IXW.	225	13# "10	140	SDX	200	15 "11	188
CSDW.	200	15 "11	168	SDXX	200	15 "11	209
CHW.	100	163 " 121	105	SDXXX	200	15 "11	230
XIIW.	100	163 " 121	126	SDXXXX.	200	15 "11	251
TT.	450	133 "10"	112	SDXXXXX.	200	15 "11	272
XTT.	450	134 "10	126	SDXXXXXX.		15 "11	293

When the plates are 14 by 20 inches, there are 112 in a box.

Thickness and Weight of Window Glass.

	1	Number	of the	glass	or weig	ght in c	ounces	per squ	are foo	t.	
.059	13	15 .071	.077	.083	.091	.100	24	$\begin{array}{ c c } 26 \\ .125 \end{array}$	$\frac{32}{.154}$	36 .167	42 .200
						imals o					

THE ATMOSPHERE

The mean height of the atmosphere is about 302 feet greater at the equator than at the poles, which is caused by the difference of the earth's attraction at the two places, and also by centrifugal force.

The mean height of the atmosphere in 45° latitude is 60158.6 feet; at the poles,

 $60 \cup 07.6$ feet, and at the equator, 60309.6 feet.

The temperature of the atmosphere is greatest at the surface of the earth, and decreases with the height above the surface. The compression of the air by the upper layers of the atmosphere generates heat in the lower layers, as explained in the article ou Air and Heat. The rays of light from the sun, passing through a denser air near the surface of the earth, also generate more heat by friction, as it were. The temperature of congelation of water being 32°, which is marked by the perpetual snow-line on high mountains, as shown in the accompanying table.

Heights of Snow-Line in Different Latitudes.

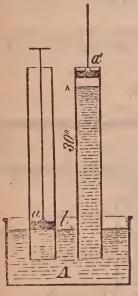
Latitudes of snow-line on high mountains. 250 350 400 450 550 14,760 | 12,560 | 10,290 | 9,000 | 7,670 2,230 5,030 120 Heights of snow-line in feet above the sea.

New-fallen snow occupies eight times its volume in water.

Heat is constantly absorbed from the atmosphere by evaporation of water on the surface of the seas, which heat is carried up and warms the atmosphere above; heat is also absorbed by support of the growth of vegetation on land. It is this operation of consuming and generating heat which causes the winds and difference of weather.

As the atmosphere is a material substance, it is subject to the action of the force of gravity, which causes a pressure of 14.75 pounds to the square inch at the level of the sea; or a column of air one square inch base and of the height of the atmosphere weighs 14.75 pounds, which balances an equal weight of a column of mercury 30 inches high at the temperature of 60° Fahr., or a column of water of 34 feet high.

Columns of Air, Mercury and Water.



A is a vessel full of mercury, in which is placed vertically a glass tube about 3 feet high above the surface l; in the glass tube is fitted an air-tight piston a, just one square inch area, which can be moved by the piston-rod c; now the piston stand is at α on the level l, and in contact with the mercury in the tube; raise the piston by the piston-rod and handle c, the mercury in the tube will follow until the height of 30 inches, the piston still continues to move higher in the tube, but the mercury will maintain its position at 30 inches from l. Now it may be supposed that it is some force of the piston that draws the mercury up in the tube; if so, why did it separate at 30 inches? If the column becomes too heavy, it could separate at l, and the 30 inches of mercury follow the piston; as this is not the case, but the weight of the atmosphere pressing on the surface l and forcing the mercury up in the tube until they (the mercury and the atmosphere) come in equilibrium, which occurs at the 30 inches; and the piston only served to remove the atmospheric pressure in the tube; hence we have the weight of a column of atmospheric air with one square inch base equal to the weight of a column of mercury 30 inches high and one sq. in, base. One cubic inch of mercury at 60° Fahr. weighs 0.941 pounds; this, multi-

plied by the height, 30 inches, gives 14.73 pounds, the weight of the column of mercury or atmosphere; this is generally termed "the atmospheric pressure per square inch."

The specific gravity of mercury at 60° Fahr. is 13.58, and
$$\frac{13.58 \times 30}{12} = 33.95 \text{ feet,}$$

the height of a column of water required to balance the atmosphere.

WIND, AERODYNAMIC.

The motions and effects of gases by the force of gravity are precisely the same

as that of liquids. (See Hydraulics.)

The altitude or head of the atmosphere at uniform density will be the altitude of a column of water 33.95 feet, divided by the specific gravity of the air, 0.0012046, or,

$$\frac{33.95}{0.0012046} = 28133 \text{ feet.}$$

The velocity due at the foot of this head will be -

 $V=8.02\,\sqrt{28183}=1346.4$ feet per second, the velocity at which the air will pass into a vacuum.

Velocity of Wind.

When air passes into an air of less density, the velocity of its passage is measured by the difference of their density.

H and h = density of the air in inches of mercury; t = temperature at the time of passage; and V = velocity of the wind in feet per second.

$$V = 1346.4 \sqrt{\frac{H-h}{h}(1+0.00208t)}, \dots 6.$$

The force of wind increases as the square of its velocity.

 $\mathbf{a} = \text{area exposed at right angles to the wind in square feet; } F = \text{force of the wind in pounds; } H = \text{horse-power, and } v = \text{velocity of the plane } \mathbf{a} \text{ in direction of the wind, } + \text{when it moves opposite, and } - \text{when it moves with the wind.}$

$$F = 0.002288 \mathbf{a} \ V^2$$
, when $v = o$, . . 7.
 $F = 0.002288 \mathbf{a} (V \pm v)^2$, 8. $H = \frac{\mathbf{a} v (V \pm v)^2}{241400}$, 9.

Example. A rail-train running ENE 25 miles per hour exposes a surface of 1000 square feet to a pleasant brisk gale NE by E. Required the resistance to the train in the direction it moves, and the horse-power lost.

ENE-NE by N=3 points = 33° 45′; V=14 feet per second, a brisk gale; $v=25\times 1.467=36.6$ feet per second, and F=0.002288 sin. 233° 46′ \times 1000 (14 + cos. 33° 45′ \times 36.6)² = 305.1 pounds.

$$H = \frac{305.1 \times 36.6}{550} = 20$$
 horses.

Table of Velocity and Force of Wind, in Pounds per Square Inch.

Miles per hour.	Feet per second	Force per sq. ft. pound.	Common Application of the force of Wind.	Miles per hour.	Feet per second	Force per sq. ft. pound.	Common Application of the force of Wind.
1	1.47	0.005		18 20	26.4 29.34	1.55 1.968	Very brisk.
2	2.93	0.020	Just perceptible.	25	36.67	3.075	
3	4.4	0.044	Soust perceptible.	30	44 01	4.429)
4	5.87	0.079		35	51.34	6 027	>High wind.
5	7.33	0.123	Gentle pleasant	40	58.68	7.873	
6	8.8	0.177	• wind.	45	66.01	9.963	
7	10.25	0.241		50	73.35	12.30	> Very high.
8	11.75	0.315		55	80.7	14.9	
9	13.2	0 400		60	88.02	17.71	Storm.
10	14.67	0.492	Pleasant brisk	66	95.4	20.85	
12	17.6	0.708	gale.	70	102.5	24.1	Great storm.
14	20.5	0 964	gare.	75	110	27.7	Hurricane.
15	22.00	1.107		80	117.36		fildricane.
16	23.45	1.25	']	100	140.66	50.	Tornado.

THE BAROMETER.

The barometer measures the pressure of the atmosphere, as described in the former editions of this Pocket Book.

The English have graduated the barometer to indicate weather as follows:

Barometer in inches. Weather. At 28.3 Stormy. At 28.7 Much rain. At 29.1 Rain. At 29.5 Change of weather. = At 29.9 Fair weather. == At 30.3 Set fair. =At 30.7 Very dry.

The following guides in predicting weather-changes are selected from the "Barometer Manual" of the London Board of Trade:

I. If the mercury, standing at thirty inches, rise gradually while the thermometer falls, and dampness becomes less, N.W., N. or N.E. wind; less wind or less snow and rain may be expected.

II. If a fall take place with a rising thermometer and increasing dampness, wind and rain may be expected from S.E., S. or S.W. A fall in winter with a low thermometer foretells snow.

III. An impending north wind, before which the barometer often rises, may be accompanied with rain, hall or snow, and so forms an apparent exception to the above rules, for the barometer always rises with a north wind.

IV. The barometer being at $29\frac{1}{2}$ inches, a rise foretells less wind or a change of it northward, or less wet. But if at 29 inches, a fast first rise precedes strong winds or squalls from N.W., N. or N.E., after which a gradual rise with falling thermometer, a S. or S.W. wind will follow, especially if the rise of the barometer has been sudden.

V. A rapid barometric rise indicates unsettled, and a rapid fall stormy, weather with rain or snow; while a steady barometer, with dryness, indicates continued fine weather.

VI. The greatest barometric depressions indicate gales from S.E., S. or S.W.; the greatest elevations foretell wind from N.W., N. or N.E., or calm weather.

VII. A sudden fall of the barometer, with a westerly wind, is sometimes followed

with a violent storm from the N.W., N. or N.E.

VIII: If the wind veer to the south during a gale from the E. to S E., the barometer will continue to fall until the wind is near a marked change, when a lull may occur. The gale may afterward be renewed, perhaps suddenly and violently; and if the wind then veer to the N.W., N. or N.E., the barometer will rise and the thermometer fall.

1X. The maximum height of the barometer occurs during a north-east wind, and the minimum during one from the south-west; hence these points may be considered the poles of the wind. The range between these two heights depends on the direction of the wind, which causes, on an average, a change of half an inch; on the moisture of the air, which produces, in extreme cases, a change of half an inch; and on the strength of the wind, which may influence the barometer to the extent of two inches. These causes, separately or conjointly with the temperature, produce either steady or rapid barometric variations, according to their force.

HYGROMETRY.

On the Humidity and other Properties of Air, deduced from Glaisher's Tables of the Greenwich Observatory.

Mason's hygrometer, consisting of wet and dry bulb thermometers, is considered

the best for determining humidity in the air and the dew-point.

Example. The temperature of the air being 75°, and the wet-bulb thermometer showing 63°, or 12° cold; barometer 30 inches. Required, the humidity of the air, the dew-point, weight of vapor per cubic foot, and the weight of a cubic foot

of the air in grains troy?
Table I., 75° and 12° cold = 55 per cent. of humidity. Table II., = 57° temperature of dew-point. Table III., weight of dry air = 516.7 grains per cubic foot. " saturated air = 511.4

> $5.3 \times 0.55 = 2.915$ grains. Difference =

Weight of the air 511.4 + 2.9= 514.3 grains per cubic foot.

Table III., 9.31 + 0.55=5.12 grains of vapor per cubic foot.

The weight of air of equal temperature and humidity is inverse as the height of the barometer.

TABLE I.

Humidity of the Air, or Percentage of Full Saturation,

At Different Temperatures, indicated by the Dry and Wet Bulbs of the Hygrometer (Glaisher).

Temp. of the air,	1	Diff	ere	nce	in	Te	mp	era	tur	e, c	or C	Cold	l or	ı th	e V	Vet	-bu	lb '	The	erm	om	ete	r.
Fahr.	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23
	-	-	-			_	-	_	_	-	_		_			_	—	_		_	-	_	
30		73																					
35					64															Ĭ.		İ	
40										46		,		į					l i				
45	93									48								İ					
50										49													
55										53													
60										56													
65																				34			
70																				35			
75																				37			
80																				38			
85																				38			
80	96	91	87	83	79	75	72										44	42	40	38	36	34	32
								P	erc	ent	tag	e of	H	um	idi	ty.							

TABLE II.

Temperature of the Dew-point,

At Different States of the Hugrometer.

Temp. of the air.	1	Diff	ere	nce	in	Te	mp	era	tur	о, с	or C	Cold	lon	th	e V	Vet	-bu	lb !	The	erni	om	ete	r.
Fahr.	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	'?3
30	25		_																		_		
35	32	30	27	25	22	20	17	15	13														
40									20														
45									25														
50									32														
55																		24					
60	58	56	55	53	51	50	48	46	45	43	41	39	38	36	34	33	31	29	28	26			
65	63	62	60	58	57	55	54	52	50	49	47	46	44	43	41	39	38	36	24	33	31	30	28
70	68	67	65	64	62	61	59	58	56	55	53	52	50	49	47	46	44	43	41	40	38	37	35
75	73	72	70	69	67	66	64	63	61	60	.58	57	55	54	52	51	49	48	46	45	43	42	40
80	78	77	75	74	72	71	69	68	66	65	63	62	60	59	57	56	£4	53	51	50	48	47	45
85	84	83	82	81	80	79	78	77	76	75	74	73	72	71	70	69	68	67	66	65	64	63	62
90	89	88	87	86	85	84	83	82	81	80	79	78	77	76	75	74	73	72	71	70	69	68	67
	1		*****									e o											

TABLE III.

Properties of Air, by Glaisher, Greenwich Observatory.

Barometer 30 inches, at 60° Fahrenheit.

Temp.	Force of	Weight of vapor	Wt. pe	er cub. ft.	m	Force of	Weight	Wt. per	cub.ft.
of the	vapor in	more curb		Satu-	Temp. of the	vapor in	of vapor per cub.		1
air.	inchesof	ft. of	Dry	rated	air.	inchesof	foot of	Dry	Sat'd
	mercury	sat. air.	i air.	air.	3321	mercury	sat. air.	air.	air.
Fahr.	Inches.	Grains.	Grains.	Grains.	Fahr.	Inches.	Grains.	Grains.	Grains.
10°	0.089	1.11	590.0	589.4	520	0.400	4.56	540.5	537.9
11	0.093	1.15	588.7	588.1	53	0.414	4.71	539.4	536.7
12	0.096	1.19	587.5	586.8	54	0.428	4:86	538.3	535.5
13	0.100	1.24	586.2	585.5	55	0.442	5.02	537.3	534.4
14	0.104	1.28	584.9	584.2	56	0.458	5.18	536.2	533.2
15	0.103	1.32	583.7	582.9	57	0.473	5.34	535.1	532.1
16	0.112	1.37	582.4	581.6	58	0.489	$0.54 \\ -5.51$	534.1	530.9
17	0.112	1.41	581.1	580.3	59	0.506	5.69	533.0	529.8
18	0.110	1.47	579.9	579.1	60	0.523	5.87	532.0	528.6
19	$0.120 \\ 0.125$	1.52	578.7	577.8	61	0.541	6.06	530.9	527.5
20		1.58	577.4	576.5	$\begin{array}{ c c c c c c c c c c c c c c c c c c c$	0.541 0.559	6.25	529.9	526.3
1	0.129		576.2	575.3	63	0.578	-5.45	528.8	525.2
21	$0.134 \\ 0.139$	1.63			64	0.578	6.65	527.8	524.0
22	i .	1.69	$575.0 \\ 573.7$	574.0 572.7	65	0.537		526.9	522.9
23	0.144	1.75			66		6.87	525.8	
24	0.150	1.81	572.5	571.5	67	0.638	7.08	524.7	521.7
25	0.155	1.87	571.3	570.2		0.659	7.30	523.7	520.6
26	0.161	1.93	570.1	569.0	68	0.681	7.53	523.7	519.4
27	0.167	2.00	568.9	567.7	69	0.704	7.76	521.7	518.3
28	0.173	2.07	567.7	566.5	70	0.727	8.00	521.7 520.7	517.2 516.0
29	0.179	2.14	566.5	565.3	$\begin{array}{ c c }\hline 71\\ 72\\ \end{array}$	0.751	8.25	519.7	514.9
30	0.186	2.21	$\begin{bmatrix} 565.3 \\ 564.2 \end{bmatrix}$	564.1	73	$0.776 \\ 0.801$	$\begin{array}{c} 8.50 \\ 8.76 \end{array}$	518.7	513.7
31	0.192	2.29		562.8		$0.801 \\ 0.827$		517.7	512.6
32	0.199	2.37	$\begin{bmatrix} 563.0 \\ 561.8 \end{bmatrix}$	561.6	74 75	0.854	$\begin{array}{c} 9.04 \\ 9.31 \end{array}$	516.7	511.4
33	0.207	2.45	560.7	566.4	76	0.882	9.60	515.7	510.3
34	0.214	2.53	559.5	559.2	77	0.882	9.89	.514.7	509.2
35	0.222	2.62	558.3	558.0	78	0.910 0.940	$\begin{array}{c} 9.89 \\ 10.19 \end{array}$	513.8	508.0
36	0.230	2.71	557.2	556.8	79	0.940	10.19	512.8	506.9
37	$0.238 \\ 0.246$	$\frac{2.80}{2.89}$	556.0	555.6 554.4	80	1.001	10.30	511.8	505.7
38	1	2.99	554.9	553.2	81	1.034	11.14	511.0	504.6
39	0.255			$553.2 \\ 552.0$	82	1.034 1.067	11.47	509.9	503.4
40	0.264	3.09	553.8 552.6	550.8	83	1.101	11.82	508.9	502.3
41	0.274	3.19	551.5		84	1.101 1.136	12.17	508.0	501.1
42	0.283	3.30	550.4	549.6	85	1.150 1.171	$\begin{array}{c c} 12.17 \\ 12.53 \end{array}$	503.0	500.0
43	0.293	3.41		548.4 547.2	86	1.209	$\begin{array}{c c} 12.55 \\ 12.91 \end{array}$	506.1	498.9
44	0.304	3.52	549.3		87	1.247	12.91 13.29	505.1	497.7
45	0.315	3.64	548.1	546.1	88	1.286		503.1	
46	0.326	3.76	547.0	544.9	89	1.280 1.326	13.68	504.2	496.6 495.4
47	0.337	3.88	546.0	543.7			14.08	1	
48	0.349	4.01	544.8	542.5	90	1.368	14.50	502.3	494.3
49	0.361	4.14	543.7	541.3	91	1.411	14.91	501.3	493.2
50	0.373	4.28	542.6	540.2	92	1.456	15.33	500.4	
51	0.386	4.42	541.5	539.0	93	1.502	15.76	499.4	491.9

MEAN TEMPERATURE AT DIFFERENT SEA-SONS OF THE YEAR.

•								
_		l M	lean Te	mperat	ure, Fal	hr.	Hemis-	Height
LOCATIONS.		Year.	Spring.	Sum.	Autm.	Wint'r.		ab. sea Feet.
Algiers,		63.0	63.0	74.5	70.5	54.0	N.	310
Berlin,	•	47.5	46.4	63.1	47.8	30.6	N.	128
Berne,	•	46.0	45.8	60.4	47.3	30.4	N.	1918
	•	49	48	66	53	28	N.	71
Boston,		62.5	59.4	73.0	64.6	52.5	s.	
Cairo,		72.3	71.6	84.6	74.3	58.5	N.	
Calcutta,		78.4	82.6	83.3	80.0	67.8	N.	
Calcutta,		69.8	69.8	82.0	72.9	54.8	N.	10
Christiania,		41.7	39.2	59.5	42.4	25.2	N.	71
Christiania,	. 1	66.4	63.5	74.1	66.9	58.6	S.	
Constantinople,		56.7	51.8	73.4	60.4	40.6	N.	150
Constantinople, Copenhagen,		46.8	43.7	63.0	48.7	31.3	N.	20
Edinburgh		47.5	45.7	57.9	48.0	38.5	N.	288
Jerusalem,		62.2	60.6	72.6	66.3	49.6	N.	2500
Jerusalem, Jamaica (Kingston), Lima, Peru, Lisbon, London		79.0	78.3	81.3	0.03	76.3	N.	10
Lima, Peru,		66.2	63.0	73.2	69.6	59.0	S.	511
Lisbon,		61.5	59.9	71.1	62.6	52.3	N.	236
London,		50.7	49.1	62.8	51.3	39.6	N.	50
Madeira (Funchal),	. •	65.7	63.5	70.0	67.6	61.3	N.	
Madrid,		57.6	57.6	74.1	56.7	42.1	N.	2175
London, Madeira (Funchal), Madrid, Mexico, City, Montreal, Moscow,	•	60.5	53.6	63.4	65.2	60.1	N.	6990
Montreal,	•	43.7	44.2	69.1	47.1	17.5	N.	
Moscow, Naples, New Orleans, New York, New Zealand,	•	38.5	43.3	62.6	34.9	13.5	N.	480
Naples,	•	61.5	59.4	74.8	62.2	49.6	N.	180
New Orleans,	•	72 53	73	84 72	$\frac{72}{56}$	58 33	N.	20
New York,	•	59.6	50 60.1	66.7	58.0	53.5	N. S.	20
Nice Zealand,	•	60.1	55.9	72.5	63.0	48.7	N.	
Nicolaiof (Russia)	•	48.7	49.3	71.2	50.0	25.9	N.	• • •
Nice, Nicolaief (Russia), Paramatta (Australia),	•	64.6	66.6	73 9	64.8	54.5	S.	
Palermo,	•	63.0	59.0	74.3	66.2	52.5	N.	180
Pokin China	•	52.6	56.6	77.8	54.9	29	N.	97
Paris.		51.4	50.5	64.6	52.2	37.9	N.	210
Philadelphia.	•	55	52	76	57	34	N.	30
Quito, Ecuador.		60.1	60.3	60.1	62.5	59.7	S.	9560
Rio Janeiro.		73.6	72.5	79.0	74.5	68.5	s.	10
Rome,		59.7	57.4	73.2	61.7	46.6	N.	174
Paris, Philadelphia, Quito, Ecuador, Rio Janeiro, Rome, San Francisco, St. Petersburg,		57.5	58	59	60	53	N.	150
St. Petersburg,		38.3	35.1	60.3	40.5	16.7	N.	10
prockholm,		42.1	383	61.0	43.7	25.5	N.	134
Trieste,		55.8	53.8	71.5	56.7	39.4	N.	288
Turin,		53.1	53.1	71.6	53.8	33.4	N.	915
Vienna.	•	50.7	49.1	62.8	51.3	39.6	N.	480
Warsaw, Washington,	•	45.5	44.6	63.5	46.4	27.5	N.	397
washington,		59	60	79	58	38	N.	

Seasons.

	HERN LATI	1	SEASONS.		HERN LATI	
June,	July,	February, May, August, November,	Winter.	June, September, December, March,	January, j	February.

Rain and Melted Snow.

Fall in Inches at Different Places.

1 400 110 1110	reco at Del	7070100 1 00			
Locations.	Year.	Spring.	Summ'r.	Fall.	Winter,
Albany, North America,	40.67	9.79	12.3	10,3	8,30
Algiers,	37.04	8.34	0.60	10.3	17.8
Baltimore, North America,	42.00	11.2	11.1	10.52	9.31
	23.56	5.66	7.21	5.45	5.24
Berlin, Prussia,	87.61	15.7	18.6	29.8	23.5
Bombay, India.	110.	10.1	10.0	20.0	1
Boston, North America,	44.48	10.8	11.8	12.57	9.89
Buffalo "	27.35	5.90	8.45	7.48	5.52
Buffalo, "Canton, China,	69.3	18.8	27.9	19.3	3.3
Charleston, North America,	48.29	8.60	18.7	11.6	9.40
Copenhagen,	18.35	2.84	6.86	5.13	3.52
Dover, England,	38.				0.02
Dublin, Ireland,	25.				
Edinburgh, Scotland,	28.				
England.	33.				
England,	28.9	5.43	7.13	8.95	7.39
Granada (Colombia),	115.			• • •	
Liverpool.	34.1	6.19	9.78	10.8	7.32
Liverpool,	13.5	5.1	0.2	1.2	7.0
London,	20.69	4.09	6.00	6.15	4.45
Madeira Islands.	30.87	5.11	2.30	6.96	16.5
Manchester, England,	36.	7.	9.	11.	9.
Milano, Italy,	38.	9.04	9.18	11.7	8.05
Mississippi Štate,	53.00	10.9	14.2	9.50	18.4
New York,	42.23	11.5	11.3	10.3	9.63
New Orleans,	52.31	13.3	16.1	10.8	12.6
Ohio, State,	39.69	10.4	10.9	9.03	6.91
Pekin, China,	26.9	2.67	20.5	3.22	0.53
Peru (Interior), Carabaya, .	355.	88.	120.	87.	60.
St. Petersburg,	17.65	2.89	6.73	5.11	2.93
Paris,	22.64	5.53	5.92	6.51	4.68
	48.00	13.	12.	11.	12.
Philadelphia, Rio Janeiro, Brazil, Rome, Italy,					10.76
Rome, Italy,	30.87	7.27	3.4	10.9	9.3
1 Stockholm	19.67	2.17	7.81	6.94	2.75
Tiffis, Caucasus,	19.26	6.25	7.62	3.51	1.88
Washington,	41.20	10.4	10.5	10.2	11.1
San Francisco. California,	83.	22.	1.	15.	45.

Volume of Evaporation and Rain-Fall.

Inches \times 2,323.200 = cubic feet per square mile. Inches \times 17,335,019 = gallons per square mile. Inches \times 3630 = cubic feet per acre.

Length in Miles of the Principal Rivers.

0					
EUROPE.		North and South America.		ASIA AND AFRICA.	
Volga, Russia,	2000	Missouri,	2900	Yang-tse-kiang, .	2800
Danube,	1600	Mississippi,	2800	Lena,	2600
Don and Dnieper, .	1000	Mackenzie's,	2500	Obe, Hoangho, .	2500
Rhine,	950	St. Lawrence, .	2200	Yenesei,	2300
Dwina,	700	Rio Grande,	1800	Amor,	2200
Petchora, Elbe, Loire,			1100	Cambodia,	2000
Vistula, Tagus,	550	Alabama,	600	Indus, Irrawaddy,	1700
Dniester, Guadiana,	500	Amazon,	3600	Nile,	3000
Rhone, Po, Seine, .	450	Rio de la Plata, .	2250	Niger or Joliba,	2600
Mezene, Desna, .	400	Orinoco,	1500	Senegal,	1200
Dahl, Bug,	300	Araguay,	1100	Orange,	1000
Thames,	233	Magdalena,	900	Gambia,	700

Evaporation on the Surface of Water in the Open Air.

When the surface of water is freely exposed under the atmosphere, the dry air in contact with it becomes charged with vapor, and consequently becomes lighter (see Table, page 357), rises, and gives place to drier air, to repeat the same operation, by which moisture is constantly carried up into the air from the surface of the water. The rate of this evaporation depends upon the temperature of the water, the dryness, the temperature and the velocity of the air.

Evaporation of Water in Decimals of an Inch, per 24 Hours, on the surface of fresh-water lakes, rivers and canals, at different temperatures of the water and currents of the air.

Water.	1	Velocity	of wind in	miles per	hour on th	ne water.	
Temp.	Calm.	10	20	30	40	50	60
320	0.012	0.014	0:016	0:017	0.019	0.021	0.023
35 -	0.020	0.023	0.026	0:029	0.032	0.035	0.038
40	0.040	0.046	0:052	0.058	0.064	0.070	0.076
45	0.068	0.078	0.088	0.098	0.109	0.119	0.129
50	0.100	0.115	0.130	0.145	0.160	0.175	0.190
55	0.133	0.153	0.173	0.193	0 213	0.233	0.253
60	0.177	0.203	0.230	0.256	0.283	0.310 ⁻	0.336
65	0.225	0.259	0.292	0.326	0.360	0.394	0.427
70	0.278	0.320	0.361	0.404	0.444	0.486	0.527
75	0.335	0.385	0.435	0.485	0.535	0.585	0.635
80	0.400	0.460	0.520	0.580	0.640	0.700	0.760
85	0.468	0 538	0.608	0.679	0.749	0.819	0.889
90	0.540	0.621	0.703	0.784	0.865	0.946	1.025
95	0.620	0.713	0.808	0,900	0.995	1.088	1.180
100	0.700	0.805	0.912	1.015	1.123	1.225	1.332

The evaporation on the surface of salt water on the occan is about 0.8 of that in

The quantity of water evaporated on the surface of all the waters on the earth is equal to the quantity of rain-fall.

Area in Square Miles of the largest Inland Lakes.

LAKES.	Sq. Miles.	LAKES.	Sq. Miles.
Eastern Hemisphere.		Tonting, China,	1200
_		Wenern, Sweden,	2400
Aral Sea, Tartary,	16650	Wettern, Sweden,	1045
Azov Sea, Russia,	8800	Zaizan, Mongolia,	1600
Baikal Sea, Siberia,	13000		
Balkash, Mongolia,	5200	Western Hemisphere.	
Black Sea, Turkey,	113000	Athabasca, N. America, .	3200
Caspian Sea, Russia, .	13 8000	Erie Lake, N. America,	7000
Constance, Switzerland, .	456	Great Bear, N. America, .	4000
Dead Sea, Palestine,	370	Great Slave, N. America,	12000
Dembia, Abyssinia,	13000	Great Salt Lake,	1880
Enare, Lapland,	870	Huron, N. America, .	22 800
Geneva, Switzerland,	400	Maracaibo, S. America, .	6000
Hjelmaren, Sweden,	900	Michigan, N. America,	22600
Tchad, Africa,	11600	Nicaragua, Cent. America,	3905
Ladoga, Russia,	6200	Ontario, N. America, .	4950
Loch Lemond, Scotland, .	27	Otehenantekane, N. Amer.,	2500
Lough leaugh, Ireland,	80	Superior, N. America, .	30000
Onega, Russia,	3300	Titicaca, Peru,	5400
Ouroomia, Persia,	1000	Winnipeg, N. America,	7200

BAROMETRICAL OBSERVATIONS.

For Determining Difference of Levels.

Notation of letters for the complete formulæ of La Place, in French and English measures.

Lower station,
$$\begin{cases} h = \text{height of barometer} = h' \\ T = \text{temp. of barometer} = T' \\ t = \text{temp. of the air} = t' \end{cases}$$
 Upper station.

H= height of barometer at the upper station reduced to the temperature of the barometer at the lower station. When the height is read on a brass scale, the reduction will be in

French measures. English measures.
$$H = h' [1+0.0001614 (T-T')]. H = h' [1+0.00008967 (T-T')].$$

Mean radius of the earth = 6,366,200 metres = 20,886,860 feet.

Mean height of the atmosphere = 18,336 metres = 60,158.6 feet.

L = mean latitude between the two stations.

Z =difference of level between the two stations.

French measures.

$$\underbrace{Z = \log \cdot \frac{h}{H} \times 18336}_{18336} \times \left\{ \frac{\left(1 + \frac{t + t'}{533.2}\right) \times \cdot \cdot \cdot \cdot 2}{\left(1 + 0.00251 \times \cos \cdot 2L\right) \times \cdot \cdot \cdot \cdot 3}_{\left(1 + \frac{Z + 15926}{6366200}\right) \cdot \cdot \cdot \cdot \cdot \cdot \cdot 4} \right\}$$

English measures.

$$\underbrace{Z = \log \cdot \frac{h}{H} \times 60158.6} \begin{pmatrix} \left(1 + \frac{t + t' - 64}{960}\right) \times \cdot \cdot \cdot 2. \\ \left(1 + 0.00251 \times \cos \cdot 2L\right) \times \cdot \cdot 3. \\ \left(1 + \frac{Z + 52252}{20886860}\right) \cdot \cdot \cdot \cdot \cdot 4.$$

The factor (1) gives the difference of level when the observations are made in a temperature of 32° Fahr., or 0° Cent., the freezing-point of water, and in latitude 45°, without the factors of correction (2), (3) and (4).

The factor (2) is the correction for temperature of the air above or below the freezing-point.

The factor (3) is the correction for latitude above or below 45°.

The factor (4) is the correction for the decrease of the earth's attraction. This correction is included in the following Table I., to suit any level of the stations.

There are some other barometrical corrections not included in the above formulæ, such as for humidity of the air, capularity and boiling of the glass tube, for the hour of the day and season of the year, all of which are so insignificant, uncertain and complicated that I have concluded to omit them.

Explanation of the Barometrical Tables.

The tables have been calculated in Peru, under actual practice, by the author.

Table I. is calculated from the factors (1) and (2), which gives the approximate heights above the level of the sea, in English and French measures, for every tenth of an inch from 11 to 31 inches. The mean temperature of the air and of the barometer is assumed to be 60° Fahrenheit = 15.555 Centigrade, and in latitude 45°. The barometer is assumed to be 30 inches = 762 centimetres at the level of the sea, but when it is observed to be higher or lower, make the corresponding addition or subtraction for difference of levels in the table.

Table II. contains the correction for difference of level in feet or metres at different temperatures of the air above or below 60° Fahr.

Table III. contains the correction for heights in different latitudes above or below 45°.

Tables IV. and V. are logarithmic corrections for temperature and latitude.

Table VII, gives the height of a column of air in metres, corresponding to a difference of one milimetre of mercury at different heights of the barometer.

Table VIII. gives the height of a column of air in feet, corresponding to a difference of one-tenth of an inch of mercury at different heights of the barometer.

Tables X. and XI. contain the correction for the mercurial column at different temperatures of the barometer above or below 60° Fahr. = 15.555 Cent. This correction must be made before the barometrical height is applied to Table I.

Table XII. contains the approximate mean temperature of the air at the level of the sea for every month of the year in different latitudes. This table has been deduced from observations of Mr. Dove, Humboldt, Raimondi, and other distinguished authors. The table agrees very well with the mean temperatures on the Atlantic and Pacific coasts, but will not answer for the North Sea and the Baltic where the temperatures are much higher. I have found a great deal of inconvenience in the interior of South America for want of a table of this kind.

When barometrical observations are made far inland, some means must be resorted to for estimating the temperature of the air at the level of the sea in the latitude of observation, in order to make proper corrections for difference of level From all the meteorological observations of different authors it appears that the mean temperature of 24 successive hours is near 9 o'clock in the morning, and that the mean temperature of the day from 9 to 5 p. M. is at noon.

The variation of temperature throughout the day varies with the latitude, that is, the higher the latitude, the greater is the variation.

Example 1. On the 14th of March, 1869, 2h. 15m. P. M., in Oroya, Peru, latitude 11° 30′, the barometer stood 19.46 inches, the temperature of the air 62°, and that of the barometer 60°. Required, the height of Oroya above the level of the sea in feet?

```
Table
             Barometer 19.4 in.,
                                                          = 12099.6 feet.
                             0.6 \times \text{diff.} 142.6 \text{ feet,}
              Correction
                                                                 85.5 feet.
              Approximate height,
                                                          = 12014.1 feet.
                                                      62° Fahr.
              Temperature at Oroya,
Table XII.
              Latitude 11° 30′, 14th of March,
                                                      790
              Mean temp. of the column of air,
                                                      141 = 70.5^{\circ}.
                                              10000 \text{ feet} =
                                                                208.2 feet.
Table II.
              Correct mean temp. 70°
                                                2000 \text{ feet} =
                                                                 41.6 feet.
                of the air,
                                                  10 feet ==
                                                                  0.2 feet.
                                               10000 \text{ feet} =
                                                                 23.6 feet.
Table III. Correct for lat. 11° 30',
                                                                  4.8 feet.
                                                2000 \text{ feet} =
                                                  10 feet =
                                                                  0.0 feet.
Sum of corrections,
                                                                278.4 feet.
Approximate height, .
                                                              12014.1 feet.
Height of Oroya,
                                                              12292.5 feet.
```

Example 2. In the city of Paucartambo, Peru, the barometer was observed to stand 21.272 inches, the temperature of the air 70°, and that of the barometer 69°, in latitude 13° 18′ south. About three miles from the city, on the mountain Huanacaury, the barometer stood 18.224 inches, the temperature of the air 62°, and that of the barometer 64°. Required, the height of the mountain above the city of Paucartambo?

Barometer at the lower station, . 21.272 inches. Correction for 69°, Table XI., subtract . .017 inches. Height of barometer at 60°, . . 21.255 inches. Barometer at the upper station, . 18.224 inches. Correction for 64°, Table XI., subtract .006 inches. Height of barometer at 60°, . 18.218 inches.

Table I. $\begin{cases} 18.218 & 13845.0, \text{ upper station.} \\ 21.255 & 9565.3, \text{ lower station.} \end{cases}$ Logarithms $\begin{array}{l} 3.6314133 = 4279.7 \text{ feet, approximate height.} \\ 0.0053929 = 66^{\circ} \text{ mean temperature.} \\ 0.0009888 = 13^{\circ} 18' \text{ latitude.} \\ \hline 3.6377950 = 4343.1 \text{ feet, the height required.} \\ \end{array}$

Aneroid Barometer.

The aneroids made by Negretti & Zambra, London, are compensated, and show the height of a column of mercury at the temperature of the freezing-point of water, 32° Fahr., or zero Centigrade. The aneroid is not affected by different temperatures. When the aneroid is used with the accompanying Table I., a correction must be made to convert the column of mercury from 32° to 60° Fahr., namely:

Height of a column of mercury as indicated by the aneroid.

16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | .25 | 26 | 27 | 28 | 29 | 30 .046 | .048 | .050 | .053 | .056 | .059 | .061 | .064 | .067 | .070 | .073 | .075 | .078 | .081 | .084 Correction in fraction of an inch, always additive.

Heights of the Principal Mountains and Volcanoes.

North America.	Feet.	EUROPE.	Feet.	Volcanoes, Active.	Feet.
Mount St. Elias,	17,860	Elbruz, Caucasus,	17,776	Aconcagua, Chili,	23,100
Mt. Brown, R. M.,	16,000	Mont Blanc, Alps,	15,668	Gualatieri, Peru,	22,000
Sierra Nevada, Cal.,	15,500	Malhaven, Spain,	11,678	Cotapaxi, Equador,	19,500
Fremont's Peak,	13,470	Mt. Maladetta, Py.,	11,436	Misti, Peru*,	18,136
Long's Peak, R. M.,	12,500	Mt. Caballo, Alps,	10,154	Popocatapeti, .	17,735
Cibao Mt., Hayti,	8,600	Mt. Scardus, Tur.,	[10,000]	Pichincha, Equa.,	16,000
Cierra del Cobre,	7,200	Ural Mts., Russia,	5,397		15,763
Black Mt., S. C.,	6,476	ASIA.			14,000
Mt. Washington.	6,234	Kunchinginga. Hv.	28.176	Mauna Loa, S. Isl.,	
Mansfield Mt., Vt.,	4,280	Dhawalaghiri, Hy.,	. ,	St. Helen's, Oreg'n,	[13,300]
Peak of Otter, Vt.,	4,260	Hindo Koo, Cabul,	20,000	Indrapura, Sum.,	12,300
	1	Mt. Ararat, Tur.,	17,210	Teneriffe, Can. Isl,	12,182
South America.	1	Mt. Lebanon, Syr.,	12,000	Erebus, Vic. Land,	
Illimani, Bolivia,*	24,100	AFRICA.		Cartago, C. Amer.,	11,480
Ausangati, Peru,*	22.150	Abba Yared, Aby.,	15,200	Etna, Sicily,	10,874
Chimborazo, Eq.,	21,960	Piton des Neiges,	12,500	Hecla, Iceland,	5,110
Sorato, Bolivia,	21,500	Talba Waha, Aby.,	12,000	Souffriere, Guad.,	5,108
Tolima, N. Gran.,	18,250		12,000	Jurollo, Mexico,	4.205
Cerro de Potosi,	16,150	OCEANICA.		Vesuvius, Italy,	3,948
Cerro de Pasco,	13,780	Mt. Ophir, Sum.,	13,842	1	
Organ Mt., Brazil,	7,500	Mt. Semero, Java,	13,000		

^{*} Measured by the author of this Pocket-book.

TABLE I.

Barometric and Atmospheric Heights.

	***			Drazza			Unnavaer			Danaga	
	FRENCH.			ENGLISH		Į.	FRENCH.		D	ENGLISH	
Dif.	Altitude.		Bar.	Altitude.	Dif.	Dif.	Aititude.	Bar.	Bar.	Altitude.	Dif.
	metres.	m.m.	in.	feet.			metres.	m.m.	in.	feet.	
	8488.09	279.4	11.	27848.5		1	5318.11	406.4	16.	17448.2	
76.59	8411.48	1 .	.1	27597.2	251.3	52.72	5265.39		1.1	17275.2	173.0
75.87	1	281.9			248.9	52.49	5212.90				171.9
75.19	8335.61	284.5	.2	27348.3	246.7	51.94				17103.3	170.7
74.56	8260.42	287 0	.3	27101.6	244.6	51.78	5160.96			16932.6	169 9
73.88	8185.86	289.5	.4	26857.0	242.4	51.39	5109.18		_	16762.7	168.6
73.24	8111.96	292.2	.5	26614.6	240.3	51.14	5057.79		.5		167.7
72.63	8038.74	294.7	.6	26374.3	238.3	50.82	5006.65			16426.3	166.7
71.98	7966.11	297.3	.7	26136.0	236.2	50.50	4955.83		.7	16259.6	165.7
71.43	7894.13	299.8	.8	25899.8	234.3	50.20	4905.33			16093.9	164.7
70.77	7822.70	302.2	.9	25665.5	232.2	49.90	4855.13			15929.2	163.7
70.23	7751.93	304 8	12.	25433.3	230.4	49.65	4805.23		17.	15765,5	162.8
69 61	7681.70	307.3	.1	25202.9	228.4	49.34	4755.58	434.3		15602.6	161.9
69.07	7612.09	309.8	.2	24974.5	226.6	49.07	4706.24	4368		15440.7	161.0
	7543.02	312.4	.3	24747.9	224.7	48.77	4657.17	439.4		15279.7	
68.48	7474.54	314.9	.4	24523.2	222.9		4608.40	441.9	.4	15119.7	160.0
67.94	7406.60	317.5	.5	243003		48.47	4559.93	444.5	.5	14960.7	159.0
67.42	7339.18	320.0	.6	24079.1	221.2	48.18	4511.75	447.0	.6	14802.6	158.1
66 88	7272.30	322.5	.7	23859.7	219.4	47.91	4463.84	449.5	.7	14645.4	157.2
66.38	7205.92	325.1	.8	23641.9	217.8	47.64	4416.20		.8	14489.1	156.3
65.84	7140.08	327.6	.9	23425.9	216.0	47.40	4368.80			14333.6	155.5
65.32	7074.76	330.2	13.	23211.6	214.3	47.15	4321.65		18.	14178.9	154.7
64.80	7009.96	332.7	.1	22999.0	212.6	46 85	4274.80		.1	14025.2	153.7
64 34	6945.62	335.2	.2	22787.9	211.1	46.60	4228.20		.2	13872.3	152.9
63.88	6881.74	337.8	.3	22578.3	209.6	46.36	4181.84		.3	13720.2	152.1
63.36	6818.38	340.3	.4	22370.4	207.9	46.11	4135.73			13568.9	151.3
62.91	6755.47	342.9	.5	22164.0	206.4	45.88	4089.85		.5	13418.4	150.5
62 46	6693.01	345.4	.6	21959.1	204.9	45.60	4044.25			13268.8	149.6
61.97	6631.04	347.9	.7	21755.8	203.3	45.35	3998.90			13120.0	148.8
61.50	6569.54	350.5		21554.0	201.8	45.10	3953.80		.8	199790	148.0
61.09	6508.45	353.0		21353.6	200.4	44.90	3908.90			12824.7	147.3
60.65	6447.80	355.6		21154.6	199.0	44.69	3864.21		19.	19678 1	146.6
60.23	6387.57	358.1	.1	20957.0	197.6	44.44	3819.77			195323	145.8
59.76	6327.81	360.6		20760.9	196.1	44.19	3775.58			193873	145.0
59.34	6268.47	363.2		20566.2	194.7	43.95	3731.63			199431	144.2
58.92	6209.55	365.7	.4	20372 9	193.8	43.74	3687.89			12099 6	143.5
58.68		368.3		20180.4	192.5	43.47	3644.42			119570	142.6
58.12	6092.75	370.8		19989.7	190.9	43.22	3601.20			11815 2	141.8
57.79	6034 96	373.3	.7	19800.1	189.6	43.00	3558.20		.7	11674 1	141.2
57.40	5977.56	375.9		19611.8	188.3	42.82	3515.38			11533 6	140.5
56.90	5920.66	::78 4		19425.1	187.2	42.62	3472.76			11202 8	139.8
56.57		381.0	15	10939 5	185.6	42.42	3430.34	508 0	20.	11254.6	139.2
56.20	5807.89	383.5		19055.1	184.4	42 24	3388.10	510.5		11116.0	138.6
55.84	5752.05	386.0	.2	18871.9	183.2	42.04	3346.06	513.0		100781	137.9
55.47		388.6		18689.9	182.0	41.82	3304.24	516 G		10978,1	137.2
55.11	5641.47	391.1	.0	18509 1	180.3	41.60	3262.64			10040.9	136.5
54.74		393.6		18329.5	179.6	41.39	3221.25	590.7		10104.4	135.8
54.41		396.2		18151.0	178.5	41.15				1000000	135.0
54.10		398.7		17072 5	177.5	40.94	3180.10			TO 499'0	134.3
53.70		401.3			176.2	40.75	3139.16		.()	10299.3	133.7
53.37				11191.0	175.1	40.54	3098.41			10100.0	133.0
53.04	5371.15	403.8	.9	17622.2	174.0	40.37	3057.87	530.8	.9		132.3
					1				- 1		

The columns Bar. is the height of the Barometer in inches and milimetres.

The columns Altitude is the corresponding height of level above the sea in feet and metres.

The altitude in metres can be read from the barometer in inches; or, the altitude in feet can be read from the barometer in milimetres.

TABLE I.

Barometric and Atmospheric Heights.

FRENCH. ENGLISH. ENGLISH.												
				English		1	FRENCH.	i		ENGLISH		
Dif.	Altitude.	Bar.	Bar.	Altitude.	Dif.	Dif.	Altitude.	Bar.	Bar.	Altitude.		
D11.	metres.	m.m.	in.	feet.	Dii.	DII.	metres.	m.m.	in.	feet.	Dif.	
40.45	3017.50	533.4	21.	9900.1			1210.61	660.4	26.	3971.9	1	
40.17	2977.33	535.9	.1	9768.3	131.7	32.46	1178.15	662.9	.1	3865.4	106.5	
40.09	2)37.34	538.4	.2	9637.1	131.9	32.34	1145.81	665.4	.2	375).3	106.1	
39.81	2897.53	541.0	.3	9506.5	130.6	32.22	1113.59		.3	3653.6	105.7	
30.65	2857.88	543.5	.4	9376.4	130.1	32.09	1081.50	668.0			1053	
39.44	2818.44	£46.1	.5	92 17.0	129.4	31.98		670 5	.4	3548.3	104.9	
39.23	2779.21	548.6			128.7	31.88	1049.52	673.1	.5	3443.4	104 6	
39.11			.6	9118.3	128.3	31.76	1017.64	675 6		3338.8	104.2	
38.99	2740.10	551.1	.7	89.40.0	127.6	31.64	985.888	678.1	.7	3234 6	103.8	
38.74	2701.21	553.7	.8	8862.4	127.1	31.52	954.251	680.7	.8	3130.8	103.4	
38.53	2662.47	556.2	9	8735.3	126.4	31.39	922.734	683 2	99	3027.4	103 0	
38.37	2623.94	558.8	22.	8608.9	125.9	31 27	891.341	685 8	27.	2924.4	102.6	
38.20	2585.57	561.3	.1	8483.0	125.3	31.15	860.070	688.3	.1	2821.8	102.2	
38.00	2547.37	563.8	.2	8357.7	124 7	31.03	828 919	690.8	.2	2719.6	101.8	
37.88	2509.37	566.4	.3	8233.0	124.3	30.94	797.891	693.4	.3	2617.8	101.5	
37.67	2471.49	563.9	.4	8108.7	123.6	30.81	766 953	695.9	.4	25163		
37.52	2433 82	571.5	.5	7985.1	123.1	30.72	736.140	698 5	.5	2415.2	101.1	
37.37	2396.30	574.0	.6	7862.0	122.6	31.60	705.416	701.0	.6	2314.4	100.8	
37.16	2358.93	576.5	.7	7739.4	121.0		674.815	703.5	.7	2214.0	100.4	
37.06	2321.77	579.1	.8	7617.5	121.6	30.48	644 335	706.1	-8	2114.0	100.0	
	2284.71	581.6	.9	7495.9		30.41	6:3.927	708.6	.9	2014.3	\$9.7	
36.82	2247.89	584.2	23.	7375.1	120.8	30.24	583.682	711.2	28.	1915.0	99.3	
36.69	2211.20	556.7	.1	7254.7	120.1	30.18	553.503	713.7	.1	1816.0	99.0	
36.59	2174.61	589.2	.2	7134.7	120.0	30.05	523 454	716.2	.2	1717.4	98.6	
36.39	2138.22	591.8	.3	7015.3	119.4	29.93	493 523	7188	.3	1619.2	98.2	
36,21	2102.01	594.3	.4		118.8	29.84	463.683	721.3	.4	1521.3	97.9	
36.09	2065.92	596.9	.5	6778.1	1184	29.75	433 935	723.9	.5	1423 7	97.6	
35.93	2029.99	599.4	.6		117.9	29 63	404.309	726.4	.6	1326.5	97.2	
35.79	1994.20	601.9	.7	6542.8	117.4	29 52	374.785	728.9	.7	122).6	96.9	
35.60	1958.60	604.6	.8	6426.0	116.8	29 45	345.332	731.5	.8	1133.0	96.6	
35.46	1923.14	607.0	.9	6309.6	1164	29.32	316.010	734.0	.9	1036.8	96.2	
35 30	1887.34	609.6	24.	6193.8	115.8	29.23	286.784	736.6		940.9	95.9	
35.21	1852.63	612.1		6078.3	115.5	29.11	257.672				95.5	
35.02		614.6	.1	5963.4	114.9	29.02		739.1	.1	845.4	95.2	
34.90	1817.61	617.2	.3		114.5	28.92	228.657	741.6	.2	750.2	94.9	
34.75	1782.71				114.0	28.84		744.2	.3	655.3	94.5	
34.59	1747.96	619 7	.4		1135	28.71		746.7	.4		94.2	
34.47	1713.37	622.3	.5		113.1	28.62		749.3		466.5	93.9	
31,32	1678.90	624.5	.6	5508.3	112.6	28.53		751.8		372 6	93.6	
34.17	1644.58	627.3	.7	5395.7	112.1	28 43		754.3	.7	279 0	93.3	
34.05	1610.41	629.9	.8	5283.6	111.7	28 35	30.000	756 9	.8,		93.0	
33 92	1576.36	632.4	9		111.3	28.25	40.404	759.4	.9	927	92.7	
33,78	1542.44	635 0	25.	5060.6	110.8	28.19	0.0000	762.0	30.	0.0000	92.5	
33,61	1508.66	637.5	.1	4949.8	110.3	28.10	20.170	764.5	.1	92.5	92.2	
33.50	1475.05	640.0	.2	4839.5	109.9	28.01	00.290	767.0	.2	184.7	91.0	
33.: 7	1441.55	642.6	.3		109.5	27.92	04.000	769.6		276.6	91.6	
	1409.18	645.1	.4		109.1	27.83	112 220	772.1	.4	368.2	91.3	
33,25	1374.93	617.7	.5		108.7	27.77	147.000	774 7		459.5		
33.13	13 1.80	650.3	.6		108.7	27.67	167.820	777.2	.6	550.6	91.1	
33.01	1308.79	652.8	.7	4294.0	107.7	27.58	195.495	779.7		641.4	90.8	
32.83	1275 96	655.3	.8	4186.3	107.4	$\frac{21.58}{27.52}$		782.3		731.9	90.5	
32.74	1243.22	657.9	.9				250.601	784.8	.9	822.2	90.3	
32.61		1	1	1	107.0	27.43		7874	31.	912.2	90.0	
						-						

The difference in the Bar. m.m. column is 2.5 milimetres; therefore, multiply the difference of altitude in metres by the exceeding milimetres and by 0.4; subtract the product from the tabular altitude, and the remainder will be the altitude of level in metres, corresponding to the reading of the barometer in milimetres.

TABLE II.—Correction for Mean Temperature.

Temp. Height in feet or metres. Temp.														
Ten	ip.				12									
Fahr.	Cent	1000	2000	3000	4000	5000	6000	7000	8000	9000	10000	Cent.	Fah	ır.
61		2.08	4.17	6.25	8.34	10.42	12.50	14.59	16.68	18.76	20.85	15.0	59	
62		4.17			16.61	20.82	24.98		33.32		41.65		58	
63		6.25		18.74		31.23		43.72	49.97	56.21	62.46		57	
65	17.7 18.3	8.33		24.99 31.24		41.65 52.06		58.31 72.89	66.64 83.30	74.97 93.72	83.30 104.1	13.3 12.7	56 55	
66		12.49			49.98	62.47		87.46		112.4	124.9	12.2	51	
67	19.4	14.58			58.31	72.89		102.1			145.8	11.6		
68	20.0		33.32		66.64	83.30		116.6		148.8	166.6	11.1	52	
69	20.5		37.49			93.71	112.4	131.2	149.9	168.7	187.4	10.5		
70	21.1				83.28	104.1			166.5	187.4	208.2		50	
. 71 2 72	21.6	22.91				114.5	137.4		183.2	206.1 224.9	229.1 249.9	9.4	49 48	ıre
# 73	22.2 22.7	24.99 27.07		74.77	108.3	124.9 135.3	149.5 162.4	174.9 189.5	199.9 216.6		270.7	8.3	17	121
E 74	23.3			87.46		145.7	174.9	204.1	233.2	262.4	291.5	7.7	46	eΓ
å 75		31.24			124.9	156.2	187.4	218.6	249 9	281.1	312.4	7.2	45	temperature.
₹ 76					133.3	166.6	199.9	233.2	266.5	299.9	333.2	6.6	11	ter
77	25.0	35.40			141.6	177.0	212.4			318.6	35 ± 0	6.1	43	this
this temperature.	25.5	37.48			149.9	187.4	224.9		299.8		374.8	5.5	12	th
₹ 79 ₹ 80	26.1	39.57	79.13		158.2	197.8	$237.4 \\ 249.9$		316.5	356.1	395.7 41 6. 5	5.0	41 40 c	for.
Add the correction for 188 88 88 88 88 88 88 88 88 88 88 88 88	26.6 27.2	41.65	83.30 87.46		166.6 174.9	208.2 218.6	262.4	306.1	333.2 349.8	393.6	437.3	3.8		
\frac{2}{5} 82	27.7		91.63			229.0	274.8	320.7	366.5		458.1	3.3	38 :	correction
± 83	28.3	47.90	95.79	143.3	191.6	239.5	286.6	335.3	383.2	431.1	478.9	2.7	37	ect
1 84		49.98	99.96	149.9	199.9	249.9		349.8			499.8	2.2	36	11.
5 85	اختشانا		104.1		208.2	260.3		364.4			520.6	1.6	35	<u>ಪ</u>
9 86 2 87	- 000		108.2		216.5	270.7		379.0			541.5	1.1	34	the
88	30.5 31.1	56.23	112.4 116.6		224.9 233.2	281.1 291.5		393.6 408.2			562.2 583.1	0.0	$\frac{33}{32}$	t
₹ 89		59.37	118.7		237.5	296.8		415.5			593.7	0.5	31	ac.
₹ 90		61.77	123.5	185.3	247.1	308.8	370.6	432.4	494.1	555.9	617.7	-1.1	30	Subtract
91	32.7		129.1			322.8		451.9			645.6	-1.6	29	200
92				199.9		333.2		466.5			666.4	-2.2	28	
	33,8				274.9	343.6		471.0			687.2	-2.7	27	
	34.4 35.0		141.6 145.8			354.0 364.4		$\begin{vmatrix} 495.6 \\ 510.2 \end{vmatrix}$			708.0 728.9	-3.3 -3.8	26 25	
	35.5		149.6		299.3	374.1		523.8			748.3	4.4		
. 97		77.05	154.1	231.1	308.2	385.2	462.3	539.3	616.4	693.4	770.5	-5.0	23	
	36.6	79.13	158.2	237.4	316.5	395.6				712.2	791.3	-5.5		
	37.2		162.4			406.1		560.5			812.2	-6.1	21	
1	37.7	1 :			333.2	416.5	499.8		666.4		833.0	-6.6	-	
Fahr.	Cent	□ 1000	2000	3000	4000	5000	: 6000	17000	8000	1 9000	10000	Cent.	Fah	ır.

TABLE III.—Correction for Mean Latitude.

Mean]	Teight	s in fe	et or m	etres.				Mean
latitude.	1000	2000	3000	4000	5000	6000	7000	8000	9000	10000	latitude.
	0.00	0.10			0.45	0.74	0.00	0 = 0			40
44	0.09	0.18	0.27	0.36	0.45	0.54	0.63	0.76	0.81	0.90	46
42	0.27	0.54	0.81	1.08	1.35	1.62	1.89	2.16	2.43	2.7	48 2
, 40	0.44	0.88	1.32	1.76	2.20	2.64	3.08	3.52	3.96	4.4	5') 🕱
# 38 38 38 36 36 36 36 36 36 36 36 36 36 36 36 36	0.62	1.24	1.86	2.48	3.10	3.72	4.34	4.96	5.58	6.2	48 55 52 latitudes
<u>₹</u> 36	0.79	1.58	2.37	3.16	3.95	4.74	5.53	6.32	7.11	7.9	54 🗷
₹ 34	0.96	1.92	2.88	3.84	4.80	5.76	6.72	7.68	8.64	9.6	56 c
= 30	1.28	2.56	3.84	5.12	6.40	7.68	8.96	10.2	11.5	12.8	60 8
© 28	1.43	2.86	4.29	5.72	7.15	8.58	10.0	11.4	12.9	14.3	62 =
65 24 20 18 28 28 28 28 28	1.71	3.42	5.13	6.84	8.55	10.26	12.0	13.7	15.4	17.1	66 5
20	1.95	3.90	5.85	7.80	9.75	11.7	13.6	15.6	17.5	19.5	10
5 18	2.06	4.12	6.18	-8.24	10.3	12.3	14.4	16.5	18.5	29.6	72 5
= 14	2.25	4.50	6.75	9.00	11.2	13.5	15.7	18.0	20.2	22.5	76 😤
PY 10	2.39	4.78	7.17	9.56	11.9	14.3	16.7	19.1	21.5	23.9	72 76 87 87 87 88 84 84 84 84 84 84 84 84 84 84 84 84
₹ 6	2.49	4.98	7.47	9.96	12.4	14,9	17.4	19.8	22.4	24.9	84 5
2	2.54	5.08	7.62	10.2	12.7	15.2	17.8	20.3	22.9	25.4	88

TABLE IV.—Logarithmic Correction for Temperature of the Atmosphere. Always positive.

i ——						,					
Ten	ıp.	Loga-	Ten	ap.	Loga-	Ten	np.	Loga-	Ten	ap.	Loga-
Cent.	Fahr	rithms.	Cent.	Fahr	rithms.	Cent.	Fahr	rithms.	Cent.	Fahr	rithms
-2.2	28	9.97005	8.33	47	9.98808	18.8	66	0.00539	29.4	85	0.02204
-1.6	29	9.97102	8.88	48	9.98901	19.4	67	0.00628	30.0	86	0.02230
-1.1	30	9.97198	9.41	49	9.98993	20.0	68	0.00717	30.5	87	0.02376
-0.5	31	9.97294	10.0	50	9.99086	20.5	69	0.00806	31.1	88	0.02461
0.0	32	9.97391	10.5	51	9.99178	21.1	70	0.00895	31.6	8)	0.02547
+ 55	33	9.97487	11.1	52	9.99270	21.6	71	0.00984	32.2	90	0.02632
1.11	34	9.97682	11.6	53	9.99362	22.2	72	0.01072	32.7	91	0.02717
1.63	35	9.97678	12.2	54	9.99454	22.7	73	0.01160.	33.3	92	0.02802
2 22	36	9.97773	12.7	55	9.99545	23.3	74	0.01248	33 8	93	0.02886
2.77	37	9.97868	13.3	56	9.99637	23.8	75	0.01336	34.4	94	0.02371
3 33	38	9.97963	13.8	57	9.99728	24.4	76	0.01423	35.0	95	0.03055
3.88	39	9.98058	14.4	58	9.99819	25.0	77	0.01511	35.5	96	0.03139
4.44	40	9.98152	15.0	59	9.99909	25.5	78	0.01598	36.1	97	0.03224
5.00	41	9.98247	15.5	60	0.00 000	26.1	79	0.01685	36.6	98	0.03307
5.55	42	9.98341	16.1	61	0.00090	26.6	80	0.01772	37.2	99	0.03391
6.11	43	9.98434	16.6	62	0.00186	27.2	81	0.01859	37.7	100	0.03475
6 66	44	9.98523	17.2	63	0.00270	27.7	82	0.01945	38.3	101	0.03558
7.22	45	9.98622	17.7	64	0.00360	28.3	83	0.02032	38.8	102	0.03641
7.77	46	9.98715	18.3	65	0.00450	28.8	84	0.02118	39.4	103	0.03724

TABLE V.—Logarithmic Correction for Mean Latitude of Observation. Always positive.

Lat.	Log.	Lat.	Log.	Lat.	Log.	Lat.	Log.	Lat.	Log.	Lat.	Log.
0	0.00111	15	0.00096	30	0.00055	45	0.00000	60	9.99944	75	9.99904
1	0.00110	16	0.00094	31	0.00052	46	9.99996	61	9.99941	76	9.99902
2	0.00110	17	0.00092	32	0.00048	47	9.99992	62	9.99938	77	9.99900
3	0.00110	18	0.00089	33	0.00045	48	9.99988	63	9.90935	78	9.998 18
4	0.00109	19	0.00087	34	0.00041	49	9.99984	64	9.99932	79	9.99897
5	0.00109	20	0.00085	35	0.00038	50	9.99981	65	9.99929	80	9.99896
6	0.00108	21	0.00082	36	0.00034	51	9.99977	66	9.99926	81	9 99894
7	0.00107	22	0 00079	37	0.00030	52	9.99973	67	9.99923	82	9.49 93
8	0.00106	23	0.00077	38	0.00027	53	9.99969	68	9,99920	83	9.99892
. 9	0.00105	24	0.00074	39	0 00023	54	9.99966	69	9.99917	84	9.998J1
10	0.00104	25	0.00071	40	0.00019	55	9 99962	70	9.99915	85	9.99891
11	0 00103	26	0.00068	41	0.00015	56	9.99958	71	9.99913	86	9.93890
12	0.00101	27	0.00065	43	0.00011	57	9.99955	72	9.99910	87	9.99889
13	0.00093	23	0.00062	43	0.00008	58	9.99951	73	9.99908	88	9.99889
14	0 00093	29	0.00059	44	0.00004	59	9.99948	74	9.99306	89	9,99889

TABLE VI.—Temperature of Boiling Water, Corresponding to the Height of the Barometer at 60° Fuhrenheit.

	Cor	respond	ling to	the Heig	tht of	the Bai	rometer e	$at 60^{\circ} I$	uhrenh	eit.	
Frei	nch Mea	sures.	Engli	sh Meas	Fren	French Measures. English Meas					
Diff.	Height Barom. M. M.	Temp. Water. Cent.	Temp. Water Fahr.	Height Barom. Inches.	Diff.	Diff.	Height Barom. M. M.	Temp. Water. Cent.	Temp. Water Fahr.	Height Barom. Inches.	Diff.
9,61 9,77 9,96 0,14 10,31 10,47 10,65 11,08 11,24 11,46 11,84 11,85 12,07 12,27	434.07 443.68 453.45 463.41 473.55 483.86 434.33 504.99 515.84 526.92 533.16 543.62 561.26 573.11 585.18	85.00 85.55 86.11 86.66 87.22 87.77 88.33 84.99 89.44 90.00 90.55 91.11 91.66 92.22 92.77	185 186 187 188 189 190 191 192 193 194 195 196 197 198 199	17.090 17.468 17.853 18 245 18.644 19.050 19.462 19.882 20.309 20.745 21.188 21.639 22.097 22.564 23.039	.378 .385 .392 .399 .406 .412 .420 .27 .436 .443 .451 .458 .467 .475 .483	12.49 12.70 12.91 13.18 13.36 13.57 13.83 14.05 14.28 14.53 14.73 15.04 15.26 15.52	597.45 609.94 622.64 635.55 648.73 662.09 675.66 689.47 703.54 717.82 732.35 747.13 762.17 777.43 792.95	93.33 93.88 94.44 95.00 95.55 96.11 96.66 97.22 97.77 98.33 98.88 9).44 100.0 160.5 101.6	200 201 202 203 204 205 206 207 2 8 209 210 211 212 213 214	23.522 24.014 24.514 25.022 25.551 26.067 26.602 27.146 27.639 28.833 29.415 30.007 30.608 31.219	.492 .500 .508 .519 .526 .535 .544 .553 .562 .572 .582 .601 .611

TABLE VII.—Height of a Column of Air in Metres, Corresponding to one milimetre in the barometer, at different temperatures.

Bar.															
M.M.	6	3	0	+3	6	9	12	15	18	21	24	27	50	33	36
	00 5	-			07.7	37.0	07.0	07.4	07.5	01.0	07.5	07.0	27.0		00.7
400	20.7	20.8	20.9	21.0	21.1	21.2	21.3	21.4	21.5	21.6	21.7	21.8	21.9	22.0	22.1
420	19.7	19.8	19.9	20.0	20.1	20.2	20.3	20.4	20.5	20.6	20.7	20.8	20.9	21.0	21.1
440	18.8	18.9	19.0	19.1	19.2	19.3	19.4	19.5	19.6	19.7	19.8	19.9	20.0	20.1	20.2
460	18.0	18.1	18.2	18.3	18.4	18.4	18.5	18.6	18.7	18.8	18:8	18.9	19.0	19.1	19.2
480	17.2	17.3	17.4	17.5	17.6	17.6	17.7	17.8	17.9	18.0	18.1	18.1	18.2	18.3	18.4
500	16.5	16.6	16.7	16.8	16.9	16.9	17.0	17.1	17.2	17.3	17.3	17.4	17.5	117.6	17.7
520	15.8	15.9	16.0	16.1	16.2	16.2	16.3	16.4	16.5	16.6	16.6	16.7	16.8	16.9	17.0
540	15.3	15.3	15.4	15.5	15.6		15.7	15.8	15.9	16.0	16.0	16.1	16.2	16.3	16.3
560	14.8	14.8	14.9	15.0	15.1	15.1	15.2	15.3	15.4		15.5	15.6	15.7	15.8	15.8
	14.3	14.3	14.4	14.5	14.6		14.7	14.8	14.9	15.0	15.0	15.1	15.2	15.3	15.3
580		1		1		14.1		14.3	1	14.5	14.5		14.7		
600	13.8	13.8	13.9	14.0	14.1	_	14.2		14.4			14.6		14.8	14.8
620	13.3	13.3	13.4	13.5	13.6	13.6		13.8	13.9	14.0	14.0	14.1	14.2	14.3	14.3
640	12.9	12.9	13.0	13.1	13.2	13.2		13.4	13.5	13.6	13.6	13.7	13.8	13.9	13.9
660	12.5	12.6	12.6	12.7	12.8	12.8	12.9	13.0	13.1	13.2	13.2	13.3	13.3	13.4	13.4
680	12.2	12.2	12.3	12.3	12.4	12.5	12.5	12.6	12.7	12.7	12.8	12.9	12.9	13.0	13.1
700	11.9	11.9	12.0	12.0	12.1	12.2	12.2	12.3	12.4	12.4	12.5	12.6	12.6	12.7	12.7
720	11.5	11.5	11.6	11.6	11.7	11.8	11.8	11.9	11.9	12.0	12.1	12.1	12.2	12.3	12.3
740	11.2	112	11.3	11.3	11.4	11.5	11.5	11.6	11.7	11.7	11.8	11.9	11.9	12.0	12.0
760	10.9	10.9	11.0		11.1		11.2	11.3	11.4	11.4		11.6	11.6	11.7	11.7
780	10.6	10.6			10.8				11.1	11.1		11.3	11.3		11.4

TABLE VIII.—Height of a Column of Air in Feet, Corresponding to one-tenth of an inch in the barometer at different temperatures.

Bar.			Fah	renhe	eit te	mper	ature	of th	ne air	and	the b	arom	eter.		
In.	300	350	4()0	450	500	550	600	650	700	750	800	850	900	950	1000
16	163	165	167	168	170	172	174	176	178	179	181	183	185	187	188
17	153	155	156	158	159	161	163	165	166	168	170	171	173	175	177
18	145	157	158	160	161	162	154	156	157	159	160	162	163	165	166
19	135	137	138	140	142	144	146	148	149	151	152	153	155	157	158
20	130	132	133	135	136	137	139	140	142	143	145	146	148	149	151
21	124	126	127	128	130	131	132	133	135	136	137	139	140	142	143
22	118	120	121	123	124	125	126	127	129		131	132	134	135	136
23	112	114	115	116	117	118	120	121	122	124	125	126	127	129	130
24	108	110	111	112	113	114	115	116	117	119	120	121	122	123	125
25	104	106	107	108	109	110	111	112	113	115	116	117	118	119	120
25.5	102	104	105	106	107	108	109	110	112	113	114	115	116	117	118
26	100	102	103	104	105	106	107	103	109	111	112	113	114	115	116
26.5	98	100	101	102	103	101	105	106	108	109	110	111	112	113	114
27	96	97	98	100	101	102	103	104	105	107	108	109	110	111	112
27.5	95	96	97	98	99	100	101	102	103	104	105	106	107	108	109
28	93	94	95	96	97	98	99	100	101	102	103	104	105	106	107
28.5	91	92	93	94	95	96	97	98	99	100	101	102	103	104	105
29	90	91	92	93	94	95	96	97	98	99	100	101	102	103	104
29.5	88	83	90	91	92	93	94	95	96	97	98	99	100	101	102
30	87	88	89	90	91	92	93	94	9)	96	97	98	99	100	101

TABLE IX.—Mean Height of the Barometer in different countries, reduced to the level of the sea, and to 60° Fahr. temperature.

TABLE X.—Correction for the Mercurial Column

in Millimetres at Different Temperatures of Barometer.

Tem		Height of barometer in millimetres.											Temp.			
Cen	415	440	465	490	515	540	565	590	615	640	665	690	715	740	765	Cent.
. 16	0.03	0.03	0.04	0.04	0.04	0.04	0.04	0.05	0.05	0.05	0.05	0.05	0.06	0.06	0.06	15
Se 17	0.10	0.11	0.11	0.12	0.12	0.13	0.14	0.14	0.15	0.15	0.16	0.17	0.17	0.18	0.18	14 ,
# 18	0.16	1	i			_									4	13 5
per 13	$0.24 \ 0.35$									$0.36 \\ 0.54$						12 # 11 # 1
S 21										0.66						10 %
98 22	11		1							0.75					0 1	9 5
the 53										0.85 0.96						7 0
2 2										1.06						6 5
E 20	0.75	0.80	0.84	0.89	0.93	0.98	1.02	1.07	1.11	1.16	1.20	1.25	1.30	1.34	1.39	5 2
ect	0.82									1.27						4 00
10 2:	11									1.47						2 2
) be			1.15							1.58						1 5
Set t	112100					3			1	1.68 1.78						0 ==
± 3:										1.89						_2 =
	1 1.29	1.37	1.44	1.52	1.60	1.68	1.76	1.83	1.91	1.99	2.07	2.14	2 22	2.30	2.38	
3	5 1.36	1.44	1.52	1.60	1.69	11.76	1.85	1.93	2.01	[2.10]	2.17	2.25	2.33	2.42	2.50	-4

TABLE XI.—Correction for the Mercurial Column in Thou-

sands of an Inch, at Different Temperatures of the Barometer above or below 60°.

Temp.			Н	leigh	t of	the l	aron	neter	in i	n c he	s.					Temp
Fahr.	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	Fahr.
d 62	003	003	003	003	003	003	004	004	004	004	005	005	005	005	005	58
	006	006	006			007	008	008	008	009	009	009	010	010		56 =
mnloo 66	009	009	009	010		011	012	012	012		014	014	015	015		54 =
	011	012	013		014	015	01.6	016	017	018	018	019	020	020		52 =
Ë 70	014	015	016		018	019	020	020	021	022	023	024	025	026		50 0
70 72 74	017	018	019	020	021	022	023	024	024	027	028	029	030	031	032	48 -
e 74	020	021	622	024	025	026	027	028	029	031	032	034	035	036	038	46 8
0 76	023	021	026	027	028	030	031	032	034	036	037	039	040	041	043	44 10
3 78	026	027	029	030	032	033	035	036	038	040	,042	044	045	046	048	42 =
80	029	(13)	032	034	036	037	039	041	043	045	,046	048	050	052	054	40 g
= 82	031	033	035	037	039	041	043	045	048		051	053	055	057	059	38 5
5 84	034	036	039	041	04 3	045	047	049	052		.056	058	060	062	064	36 g
5 86	037	040	042		046	049	051	053	056		060	063	065	067	070	34 🕏
correction 88 88 90	040	043	045		050	052	055	057	061		065	068	070	072	075	32 2
4	043	(146	()48		054	056	059	061	065	067	070	072	075	077	080	30 5
92	046	049	051		057	060	063	065	069	071	074	077	080	083	086	28 c
	049	052	054		060	064	067	069	074	التكافا	079	082	085	- 088	091	26 €
Subtract 86 100	051	055	058	060		067	071	073	078	_	084	087	090	093	097	24 5
2 98	054	058	061	064		071	075	077	082		088	092	095	098	102	22 4
$\frac{1}{2}$ 100	057	061	064	068	071	075	079	082	086	089	093	,097	100	104	107	20

Heights in Feet of the Principal Waterfalls.

9					
Gavarny, Pyrenees,	1260	Gray Mare's Tail,		Rupin, Himalayas,	120
Lauterbrun, Switz.,	912	Hepste,	300	Kakabika, S. Am.,	115
Staubbach, Switz.,	900	Nakchikin, Kamch.		Lidford, England,	100
Ruican, Norway,	800	Terni, Italy, .	270	Genesec, N. York,	100
Seculego, Pyrenees,	795	Montmorency, Can.,	242	Oyapock, S. Amer.,	80
Luleă, Sweden, .	600	Foyers, Scotland,		Rhine Lauffen, Swl.	65
Tequendama, Colum.	540	Wilberforce, N. A.,	160	Trollhetta, Sweden,	60
Tosa. Piedmont, .		Cetina, Dalmatia,		Parana, Paraguay, .	52
Missouri, N. Amer.,	400	Niagara Falls, .	145	Tivoli, Italy, .	50
Powerscaurt, Irel.,		Tendon, France,		Cataracts of Nile.	40

TABLE XII.—Mean Temperature of the Air

at the Level of the Sea.

Months in the year.	60	No 50	rth L	atitud	le. 20	10	0	Sont	h Lat	itude. 30	40	Ther.
January, February, March, April, May, June, July, August, September, October, November, December,	25 28 32 38 48 58 61 59 52 44 35 28	46 48 50 55 61 67 69 68 64 57 52 48	62 63 64 67 72 75 76 75 72 68 65 63	72 73 74 76 78 80 81 80 78 76 74 73	78 78 79 81 83 84 85 84 83 81 80 79	80 81 82 83 84 85 86 85 84 83 82 81	80 80 81 82 83 84 84 83 82 81 80 80	80 80 79 79 78 78 77 78 78 79 79	77 77 76 75 74 72 73 73 72 71 73 75	75 74 72 70 68 66 64 62 63 66 71	72 71 69 64 61 65 52 51 54 59 66 71	Fahrenheit,
January, February, March, April, May, June, July, August, September, October, November, December,	-3.8 -2.2 0.0 +3.3 8.8 14.4 16.1 15. 11.1 6.6 1.6 -2.2	7.7 8.8 10. 12.7 16.1 19.4 20.5 20. 17.7 13.8 11.1 8.8		22.2 22.7 23.3 24.4 25.5 26.6 27.2 26.6 25.5 24.4 23.3 22.7	25.5 25.8 26.1 27.2 28.3 28.8 29.4 28.8 28.3 27.2 26.6 26.1	27.2 27.7 28.3 28.8 29.4 30.	26.8 27.2 27.7 28.3 28.8 28.8 28.3 27.7 27.2 26.8	26.4 26.6 26.1 26.1 25.5 25.5 25.5 25.5 25.8 26. 26.1	25.3 25. 24.4 23.8 23.3 22.2 22.7 22.7 22.2 21.6 22.7 23.8	23.8 23.3 22.2 21.1 20. 18.8 17.7 16.6 17.2 18.8 21.6	22.2 21.6 20.5 17.7 16.1 18.3 11.1 10.5 12.2 15. 18.8 21.6	Centigrade.

Heights of Natural and Artificial Works.

		,	
HEIGHTS ABOVE LEVEL OF THE SEA.	Feet.	HEIGHTS ABOVE THE GROUND.	Feet.
Green in a balloon, 1837,	27.000	Tower of Babel, said to have been	-680
Gay-Lussac, Paris, 1804,	22,900	Pyramid Cheops, Egypt,	520
Highest flight of condor,	21,000	Tower of Baalbec, Syria, .	500
Humboldt in the Andes, .	19,500	St. Peter's Cathedral, Rome, .	500
Growth of vegetation,	17,000	Spire of Strasbourg,	486
The author in the Andes,*	15.120	Cathedral, Antwerp,	476
Lake Manasarooa, Thibet, .	14.500	St. Stephen's spire, Vienna,	465
Pine and birch grow,	14.000	Highest chimney, Glasgow, .	455
Highest habitation of people,*	14.000	Spire of Salisbury,	450
Potosi silver mine, Bolivia,	13.350	Cathedral, Milan	438
Lake Titicaca, Pern,*	13,000	St. Mary, Liibeck,	404
La Paz, Bolivia,*	12.400	Cathedral, Florence,	384
Poplar grows at	12.000	St. Paul, London,	366
City of Cuzeo, Peru,*	11,500	Hotel des Invalides, Paris, .	344
Oak grows at	11,000	Cathedral, New York,	325
City Riobamba, Andes,	10.800	Dome of Capitol, Washington,	287
Quito, Equador,	9,560	Trinity Church, New York,	286
City St. Bernard, Switzerland,	8,600	Notre Dame, Paris	220
City Santa Fe de Bogota,	8.350	Column City of London, .	202
Wild monkeys found at*	8.000	Porcelain, China,	200
City of Mexico,	6,990	Leaning Tower of Pisa,	188
St. Gothard. Alps,	6.900	Alexander Column, St. Petersb'g,	175
Lake Lucon, France,	6.220	July Column, Paris,	157
Palm and bananas grow at	2.500	Column Napoleon, Paris	138

^{*} Measured by the author of this Pocket-book.

Diam	Pagel	Agate.	Nonn	Min	Rraviar	Roure	L. Prim.	R Pies	Pica.	English	Gr. Prim.
	1	1		1	1	1	1	1	1	Dugneu 7	7
1 2 3 4 5	2 3	2 3	1 2 3	2	2		$\overset{1}{2}$	$\frac{1}{2}$		7	1
5 6	4 5	3 4 5	4	3	3	2 3	3		2	2	9
8	6 7 8	5 6 7	5 6	4 5	4	4	4	3	3	3	2 3
10	9	8	7	6	5 6	4 5 6	5	4	4		3
2 2	10 1	9 10	8	7	7	6	6	5	5	4	
1 2 3 4 5	3	$\begin{bmatrix} 1 \\ 2 \\ 3 \end{bmatrix}$	10 11	8 9	8 _ 9_	7 8	7	6	$\begin{array}{c} 4 \\ 5 \\ -6 \end{array}$	5	4
6	$-rac{4}{5}$	- ³	-12	-10-		- 9 -	- 8-	- 7—		- 6-	
8 9	8	5 6	13 14	11	10	10	9	8	7		- 5
20 1 2 3	8 9	7 8	15 16	12 13	11 12	11	10	9	8	7	6
3 4	20 1	9	17	14	13	12	11	10	9	8	
5 6	1 2 3	20	18 19	15	14	13	12	11			7
8	4 5	1 2 3	20	16 17	15	14	13	$\overline{12}$	10	9	
30	6	4 5	$\begin{array}{c} 21 \\ 22 \end{array}$	18	1·6 17	15 16	14	13	11	10	8
3	-30	6 _ 7	23 _24	19	18	_17	_15	-14	12	77	- 9
5	1	- <u>8</u> 9	.25	-20- 21	19	18 19	$\frac{16}{16}$	$\frac{14-}{15}$	13	10	- 3
6 7 8	3	30	26 27	22	20	19	17		14	12	10
9	5	2	28	23	21	20	18	16		13	
1	6 7	3 4	29 30	24 25	$\begin{array}{c} 22 \\ 23 \end{array}$	21	19	17	15	14	11
2 3 4 5	8 9	5 6	31 32	26	24	22 23	20	18	16		
6	40 1 2	7 8	33	27	25	24	21	19	17	15	12
7 8 9	2 3 4	9 4 0	3 1 35	28 29	26	25	22	20	18	16	13
50	- 5	- 1 2	_36 37	-30 -	$-\frac{27}{2}$	_26	-23-	-21			-10
2 3 4 5	6	3	38	31	28 29	27	$\overline{24}$	22	19	17	14
5 6	8 9	4 5	39 40	32 33	30	28	25	23	20	18	
6 7 8	50 1	67	41 42	34	31	29 30	26	24	21	19	15
9	3	8 9 50	43	35	32	31	27	25			16
60	3 4 5 6	50 1	44	36 37	33 34	32	28		92	20	
4 5	7	$\frac{2}{4}$	44 45 46 47 48	38	35	33	29	27	20	21	17
5 6 7 8	9	4 _ 5		39 -40	36	34	28 29 30_	28	24	22	
9	00		-49 	-40 41	37 38	-35- 26	31	-20 00	25	-22-	-18
70	7 8 9 60	6 7 8 9 60	50 51 52 53 54 55 56 57 58	42	38 39	33 34 -35- 36 37	32	26 27 -28 29 30	$ \begin{array}{r} 22 \\ 23 \\ 24 \\ -25 \\ 26 \\ 27 \\ 28 \end{array} $	21 -22- 23 24	10
3 4 5	5	9 6 0	53	43 44	40	38	33	50	2.7	24	19
5 6	7 8	1 2	54 55	44	41	38 39	34	31	20	25	20
8	9	1 2 3 4 5	56	46	42	40	35	32	20		
6 7 8 9 80 1 2		5	57 58	47 48	43	41 42	36	33	29	26	21
2 8	2 3 4	6 7 8	59 60	49	44 45	42	37 _38	34	30	27	-
4 5 6	5	- ('	-61-	-50-	-46-	$-\frac{43}{44}$		-35-	-31-	-00-	_22
8 9	6 7 8	70	62 63 64	51	47	45	39	36	32	28	23
9 90	8 9 80	70 1 2 3	64	52 53	48	46	40	33 34 35 36 37	04	26 27 28 29	40
	80										

BELTING.

Fig. 1, Plate III., represents a pulley hung from the points a and b by the belt T, t, forming an angle of contact 2z on the pulley. The weight W is hung on the pulley for stretching the belt from a and b, in which case the tensions T and t will be alike. The letters on the illustrations correspond with the letters in the formulas, and the number of each example corresponds with the number of the formula used.

W = weight in pounds hung on the belt.

T and t = respective tensions of the belt in pounds.

Z= half the angle of contact of the belt on the pulley. C = force of contact of the belt on the pulley in pounds.

F= motive force in pounds transmitted by the belt.

f = friction coefficient of the surfaces in contact. F = (T - t). T = (F + t). t = (T - F). T + t = F + 2t = 2T - F.

Fig. 2, Plate III., represents two pulleys of different sizes and connected by a belt T, t, in which case the smallest pulley will be in the same condition as that in Fig. 1, but the weight W is the pressure in the journal boxes, and the system is arranged for transmitting power. The greatest motive force Fthat can be transmitted by the belt cannot exceed the product of the force of contact C and the friction f without slipping of the belt.

When F > fC, the belt will slide.

When F < fC, there is no sliding.

In good practice the motive force F should not exceed 75 per cent. of fC. Example 1. Fig. 1. The weight W=84 pounds, and half the angle of contact $Z=45^{\circ}$. Required the sum of tension.

Tension
$$T + t = \frac{84}{\sin .45^{\circ}} = \frac{84}{0.70711} = 118.7928$$
 pounds.

That is, 118.7928:2 = 59.3964 pounds, the tension at each point of suspension a and b.

Example 2. It is found by experiment that the tension at a is 41.36 pounds, that is $T+t=41.36\times 2=82.72$ pounds, half the angle of contact being $Z=48^{\circ}$ 36'. Required the weight W.

Weight $W=82.72 \times \sin .48^{\circ} 36'=82.72 \times 0.75011=61.05$ pounds. Example 4. The suspended weight W=86 pounds and the angle of contact 120°, making $Z=60^{\circ}$. Required the force of contact of the belt on the pulley.

$$C = \frac{86 \times 3.1416 \times 60}{180 \times \sin .60^{\circ}} = 104 \text{ pounds.}$$

Example 9. Fig. 2. What motive force F can be transmitted by a leather belt of tension T+t=45 pounds when at rest, half the angle of contact Z=78° on a smooth cast-iron pulley of friction f = 0.35?

Motive force
$$F = \frac{0.35 \times 3.1416 \times 78 \times 450}{180} = 214.4$$
 pounds.

This is the maximum motive force that can be applied under the given conditions, but only 75 per cent. of it should be applied in practice, or $214.4 \times$

0.75 = 160.8 pounds.

When at rest, (T+t)=450 pounds, or T=t=225 pounds, but when in motion half the motive force is added to T=250+107.2=357.2 pounds, the pulling tension, and the other half of the motive force is subtracted from t=100225 - 107.2 = 117.8 pounds, the slack tension. This rule is, however, influenced by the grade of elasticity of the belt.

Example 10. How much tension must be given to a belt when at rest, in order to transmit when in motion a motive force F = 500 pounds, when the angle of contact is 165°, or $Z=82^{\circ}$ 30′, and the friction coefficient f=0.4? $T+t=\frac{180\times500}{0.4\times3.1416\times82.5}=868.1 \text{ pounds.}$

$$T+t = \frac{180 \times 500}{0.4 \times 3.1416 \times 82.5} = 868.1$$
 pounds.

The tension of the belt should be 868:2=434 pounds, to which must be added 1d for practical working, making the required tension 579 pounds.

The friction coefficient is found by formulas 13 and 26.

The formulas will answer equally well for any system of weights and measures.

Formulas for Oblique Belting, Figs. 1 and 2.	Formulas for Parallel Belting on Pulleys of Equal Diameters.
$(T+t): W=1: \sin Z.$	
Sum of tensions $(T+t) = \frac{W}{\sin Z} \dots 1$.	Sum of tensions $(T+t)=W$ 14.
Weight $W = (T+t)\sin z$ 2.	Pressure in journals $W = (T + t)$. 15.
Half-angl. cont. sin. $Z = \frac{W}{(T+t)}$ 3.	Half-angl. cont. sin. $Z = \frac{W}{(T+t)} = 1$ 16.
Force of contact $C = \frac{W\pi Z}{180^{\circ} \sin Z} \dots 4$.	Force of contact $C = \frac{iV\pi}{2} \dots 17$.
Force of contact $C = \frac{\pi Z(T+t)}{180}$ 5.	Force of contact $C = \frac{\pi(T+t)}{2} \dots 18$.
Sum of tensions $(T+t) = \frac{180C}{2Z}$ 6.	Sum of tensions $(T+t) = \frac{2C}{\pi}$ 19.
Half-ang. cont. $Z = \frac{180^{\circ}C}{\pi(T+t)}$ 7.	Half-angle cont. $Z=90^{\circ}$ 20.
Weight suspended $W = \frac{180^{\circ} C \sin Z}{\pi Z}$. 8.	Pressure in journals $W = \frac{2C}{\pi}$ 21.
Motive force $F = \frac{f\pi Z(T+t)}{180^{\circ}}$ 9.	Motive force $F = \frac{f\pi(T+t)}{2}$ 22.
Sum of tensions $(T+t) = \frac{180^{\circ} \text{ F}}{f\pi Z}$. 10.	Sum of tensions $(T+t) = \frac{2F}{f\pi} \dots 23$.
Greatest tension $T = t \left(\frac{180^{\circ} + f\pi Z}{180 - f\pi Z} \right).11$.	Greatest tension $T = t \left(\frac{2 + f\pi}{2 - f\pi} \right)$. 24.
Slack tension $t = T\left(\frac{180^{\circ} - f\pi Z}{180^{\circ} + f\pi Z}\right)$. 12.	Slack tension $t = T\left(\frac{2-f\pi}{2+f\pi}\right)$ 25.
Friction coeff. $f = \frac{180 (T-t)}{\pi z (T+t)}$ 13.	Friction coeff. $f = \frac{2(T-t)}{\pi(T+t)}$ 26.

Friction Coefficient for Different Surfaces in Contact.

Surface	Co	ondition of	leather be	elt.	India-		Gutta-	
of pulley.	Hair side on pulley.	Flesh side on pulley.			rubber belt.	Canvas belt.	percha belt.	
•	f	f	f	f	f	f	f	
Rubber	0.50	0.46	0.42		0.43	0.30	0.42	
Leather	0.48	0.45	0.50	0.60	0.42	0.27	0.40	
Wood	$\begin{array}{c} 0.46 \\ 0.40 \end{array}$	$\begin{array}{c} 0.40 \\ 0.35 \end{array}$	$\begin{array}{c c} 0.48 \\ 0.45 \end{array}$	$0.55 \\ 0.50$	$0.41 \\ 0.38$	$0.23 \\ 0.20$	0.38	
11011	0.40	0.00	0.10	0.50	0.00	0.20	0.00	

TABLE I.-Motive Force F, when the Pulling Tension T=1.

Angle of contact. 0	0.20	1 0.25	0.90						
			0.30	0.35	0.40	0.45	0.50	0.55	0.60
	$F \mid F$	F	F'	F	F	F	F	F	F
60° 0.	147 0.189	0.231	0.272	0.310	0.346	0.367	0.415	0.447	0.462
70° 0.	171 0.219	0.269	0.316	0.352	0.393	0.455	0.467	0.481	0.536
800 0.	189 0.245	0.297	0.346	0.393	0.436	0,478	0.514	0.555	0.598
900 0.	$202 \mid 0.274$	0.330	0.388	0.431	0.477	0.522	0.544	0.620	0.648
1000 0.	$231 \mid 0.300$	0.358	0.415	0.468	0.517	0.564	0.608	0.648	0.687
1100 0.	$254 \mid 0.325$	0.392	0.453	0.503	0.542	0.602	0.648	0.688	0.731
120° 0.	$272 \cdot 0.346$	0.416	0.478	0.536	0.590	0.640	0.687	0.731	0.793
130° 0.	$.292 \mid 0.373$	0.445	0.515	0.568	0.624	0.676	0.724	0.768	0.810
1400 , 0.	$310 \mid 0.398$	0.468	0.536	0.594	0.656	0.709	0.758	0.797	0.846
150° 0.	$.330 \mid 0.418$		0.570	0.628	0.687	0.741	0.791	0.837	0.880
160° 0.	$.346 \mid 0.436$	0.517	0.591	0.656	0.717	0.793	0.822	0.869	0.912
170° 0.	$.365 \mid 0.461$	0.545	0.623	0.683	0.745	0.801	0.852	0.898	0.942
180° 0.	$.380 \mid 0.478$	0.564	0.640	0.709	0.772	0.828	0.880	0.927	0.970
1900 0.	$.399 \mid 0.499$	0.592	0.671	0.727	0.797	0.854	0.906	0.953	0.997
2000 0.	$415 \mid 0.517$	0.607	0.687	0.758	0.822	0.880	0.932	0.975	1.000
210° · 0.	$433 \mid 0.539$	0.633	0.717	0.781	0.846	0.904	0.956	1.000	1.000
2200 0.	$.447 \pm 0.555$	0.668	0.731	0.803	0.868	0.926	0.979	1.000	1.000
2300 0.	464 0.571	0.674	0.758	0.825	0.890	0.949	1.000	1.000	1.000
2400 . 0.	478 0.590	0.687	0.772	0.845	0.912	0.970	1.000	1.000	1.000
	492 0.612		0.795	0.866	0.932	0.991	1.000	1.000	1.000

TABLE II .- Pulling Tension T, when the Motive Force F=1.

Angle of		Friction	coefficie	nt f for	the surfa	ces in c	ontact or	the smal	lest pulley	7.
contact.	0.15	0.20	0.25	0.30	0.35	0.40	0.45	0.50	0.55	0.60
2 Z	T	T	T	T	T	T	T	T	T	T
600	6.779	5.291	4.321	-3.680	3.227	2.887	2.724	2.410	2.236	2.163
700	5.855	4.558	3.711	3.165	2.838	2.546	2.198	2.140	2.078	1.863
800	5.274	4.077	3.363	2.887	2.546	2.290	2.092	1.944	1.802	1.671
900	4.703	3.646	3.028	2.580	2.319	2.092	1.915	1.838	1.613	1.543
100°	4.321	3.364	2.792	2.410	2.136	1.933	1.773	1.645	1.542	1.455
110°	3.941	3.079	2.548	2.206	1.988	1.845	1.660	1.542	1.453	1.368
120° ·	3.680	2.887	2.403	2.091	1.864	1.693	1.561	1.455	1.368	1.261
130°	3.421	2.683	2.246	1.942	1.759	1.601	1.479	1.381	1.302	1.234
140°	3.227	2.546	2.136	1.864	1.699	1.523	1.411	1.319	1.254	1.182
1500	3.032	2.390	2.009	1.755	1.591	1.455	1.349	1.264	1.195	1.137
1600	2.887	2.290	1.932	1.690	1.523	1.395	1.261	1.216	1.151	1.097
1700	2.739	2.169	1.835	1.581	1.463	1.342	1.249	1.174	1.113	1.062
1800	2.631	2.091	1.773	1.561	1.410	1.296	1.207	1.136	1.079	1.030
1900	2.506	2.004	1.688	1.490	1.374	1.253	1.170	1.103	1.049	1.003
2000	2.410	1.932	1.646	1.455	1.319	1.216	1.136	1.073	1.026	1.000
2100	2.307	1.853	1.580	1.395	1.280	1.182	1.106	1.046	1.000	1.000
2200	2.236	1.802	1.495	1.368	1.244	1.151	1.080	1.021	1.000	1.000
2300	2.153	1.730	1.489	1.318	1.212	1.123	1.053	1.000	1.000	1.000
2400	2.091	1.693	1.455	1.296	1.196	1.098	1.030	1.000	1.000	1.000
2500	2.023	1.633	1.416	1.257	1.155	1.073	1.009	1.000	1.000	1.000

It is assumed in the above tables that the friction gripe on the smallest pulley just balances the motive force, for which allowance must be made to prevent slipping.

The slack tension t is the difference between the pulling tension T and the motive force F, or t = T - F.

When the friction and angle of contact are great, the pulling tension is equal to the motive force, and no slack tension is then required.

TABLE III.—Pressure P in the Shaft Journals, when the Motive Force F = 1 and the System in Motion.

1										
Angle of	F	riction o	coefficien	t f for t	the surfa	aces in o	contact or	the sma	llest pulle	ey-
contact.	0.15	0.20	0.25	0.30	0.35	0.40	0.45	0.50	0.55	0.60
									·	
2Z	P	P	P	P	P	P	P	P	P	P
600	6.779	5.291	4.325	3.680	3.227	2.887	2.724	2.410	2.236	2.163
700	6.570	5.082	4.110	3.484	3.109	2.774	2,414	2.308	2.135	1.989
800	6.495	4.956	4.038	3.352	2,988	2.658	2.339	2.214	2.030	1.863
900	6.237	4.742	3.868	3.235	2.865	2.544	2.294	2.093	1.867	1.768
100°	6.088	4.624	3.746	3.100	2.740	2.430	2.184	1.988	1.829	1.697
110°	5.818	4.406	3.536	2.976	2.619	2.384	2.081	1.888	1.701	1.602
126°	5.642	4.268	3.430	2.890	2.497	2.200	1.972	1.788	1.637	1.451
1300	5.388	4.051	3.259	2.708	2.376	2.089	1.868	1.691	1.547	1.424
1400	5.185	3.906	3.135	2.624	2.257	1.983	1.772	1.600	1.477	1.342
1500	4.925	3.685	2.949	2.456	2.142	1.879	1.674	1.510	1.377	1.264
1600	4.717	3.541	2.836	2.359	2.030	1.778	1.513	1.431	1.297	1.191
170°	4.465	3.329	2.664	2.157	1.922	1.681	1.496	1.351	1.224	1.122
1800	4.262	3.182	2.546	2.122	1.824	1.592	1.414	1.272	1.158	1.060
1900	4.000	3.000	2.371	1.976	1.745	1.504	1.339	1.169	1.097	1.005
2000	3.777	2.836	2.261	1.896	1.628	1.425	1.268	1.134	1.050	1.000
2100	3.525	2.648	2.120	1.763	1.541	1.352	1.205	1.101	1.000	1.000
2200	3.323	2.507	1.930	1.692	1.458	1.284	1.150	1.020	1.000	1.000
2300	3.090	2.323	1.886	1.576	1.384	1.223	1.066	1.000	1.000	1.000
2400	2.890	2.200	1.788	1.513	1.340	1.170	1.032	1.000	1.000	1.000
2500	2.676	2.037	1.681	1.421	1.254	1,120	1.015	1.000	1.000	1.000

TABLE IV.—Pressure P in the Shaft Journals, when the Motive Force F = 1 and the System at Rest.

-		-								
Angle of	F	riction o	eoefficien	t f for t	he surfa	ces in c	ontact on	the smal	llest pulle	у.
contact.	0.15	0.20	0.25	0.30	0.35	0.40	0.45	0.50	0.55	0.60
	l					•			<u> </u>	
2Z	p	p	p	p	p	p.	p	p	p	p
600	5.779	4.291	3,325	2.680	2.227	1.887	1.724	1.410	1.236	1.163
700	5.570	4.082	3.110	2.484	2.109	1.774	1.414	1.308	1.135	0.989
800	5,495	3.956	3.038	2.352	1.988	1.658	1.339	1.214	1.030	0.862
900	5.237	3.742	2,863	2.235	1.865	1.544	1.294	1.093	0.867	0.768
100°	5.088	3.624	2.746	2.100	1.740	1.430	1.184	0.988	0.829	0.697
110°	4.818	3.406	2.536	1.976	1.619	1.384	1.081	0.888	0.701	$\{0.602$
120°	4.642	3.268	2.430	1.890	1.497	1.200	0.972	0.788	0.637	0.451
130°	4.388	3.051	2.259	1.708	1.376	1.089	0.868	0.691	$\cdot 0.547$	0.424
140°	4.185	2.906	2.135	1.624	1.257	0.983	0.772	0.600	0.477	0.342
150°	3.925	2.685	1.949	1.456	1.142	0.879	0.674	0.510	0.377	0.264
160°	3.717	2.541	1.836	1.359	1.030	0.778	0.513	0.431	0.297	0.191
1700	3.465	2.329	1.664	1.157	0.922	0.681	0.496	0.351	0.224	0.122
180°	3.262	2.182	1.546	1.122	0.824	0.592	0.414	0.272	0.158	0.060
1900	3.000	2.000	1.371	0.976	0.745	0.504	0.339	0.169	0.097	0.005
2000	2.777	1.836	1.261	0.896	0.628	0.425	0.268	0.134	0.050	0.000
2100	2.525	1.648	0.120	0.763	0.541	0.352	0.205	0.101	0.000	0.000
2200	2.323	1.507	0.930	0.692	0.458	0.284	0.150	0.020	0.000	0.000
2300	2.090	1.323	0.886	0.576	0.384	0.223	0.066	0.000	0.000	0.000
2400	1.890	1.200	0.788	0.513	0.340	0.170	0.032	0.000	0.000	0.000
250°	1.676	1.037	0.681	0.421	0.254	0.120	0.015	0.000	0.000	0.000

The belt should be tightened to the pressure p in the journals when the system is at rest, to enable it to transmit the motive force F when the system is in motion. The friction gripe on the smallest pulley will then just balance the motive force, or C = F = P - p. The pressure p should therefore be made $\frac{1}{3}$ greater for safe working.

CONE PULLEYS.

The illustration Fig. 2, Plate III., represents the largest and smallest diameters of a pair of cone pulleys, of which letters denote as follows:

R = radius of the largest step or pulley.

r = radius of the smallest step of pulley. a = distance between the centres of rotation of the pulleys. b = distance or length of the belt between the tangenting points on thetwo pulleys. L = whole length of the belt.

x = distance from the centre of the small pulley to the vertex c'.

Z = half the angle of contact of the belt on the large pulley. Z = half the angle of contact of the belt on the small pulley.

For open belts the sum of the whole angles of contact is always 360°, and $Z' + Z = 180^{\circ}$, omitting the slack of belt.

$$b = \sqrt{a^2 - (R - r)^2} \cdot \cdot \cdot \cdot 1 \cdot \left| x = a \left(\frac{R}{R - r} - 1 \right) \cdot \cdot \cdot 3.$$
Sin. $Z = \frac{b}{a} \cdot \cdot \cdot \cdot \cdot \cdot 2 \cdot \left| L = \frac{\pi}{90} (RZ + rZ) + 2b \cdot \cdot \cdot 4.$

Three-step Pulley, Fig. 3, Plate III.

The object is to make two cone pulleys cast from one pattern, and to have three steps on each pulley. Having given the diameters of the largest and smallest steps, the problem is to find the diameter of the middle step, so proportioned that the belt will have the same tension on all the three steps. D = diameter of the middle step.

Four-step Pulley, Fig. 4, Plate III.

Having given the radii of the largest and smallest pulleys 1 and 4, the problem is to find the diameters of the inner pulleys 2 and 3.

d = diameter of the pulley 3, next to the smallest. d' = diameter of the pulley 2, next to the largest pulley.

Five-step Pulley, Fig. 5, Plate III.

Cone pulleys of five steps are constructed as follows: The largest and smallest pulleys, 1 and 5, are assumed to be given from the first start. The diameter of the middle step 3 is calculated by formula 5, and the problem remains to find the diameters of the steps 2 and 4. R' = radius of the middle step 3; d and d' = diameters of the respective

steps 4 and 2.

$$d = R' + r + \frac{(R' - r)^2}{\pi a}. \dots 8.$$

$$d' = R + R' + \frac{(R - R')^2}{\pi a}. \dots 9.$$

It is supposed in the above that each pair of cone pulleys is cast from one pattern.

To find the Proper Distance between Centres.

Having given two equal cone pulleys, to find at what distance they ought to be placed to make the belt of equal tension on all the steps.

This formula can be used only for pulleys of an odd number of steps, of which D= diameter of the middle step, and R and r are the respective radii of the largest and smallest pulleys.

Cone Pulleys of any Number of Steps and Proportions, Figs. 6 and 7, Plate III.

The conoids a, b, c d B and A d c b a are drawn alike and inverted to one another, as represented by Fig. 6. The centre lines A B can be divided into any number of steps, and the conoids determine the corresponding diameters on each pulley. The pulleys can thus be made of widely different sizes, as required in many cases, particularly in foot-lathes.

The construction of the conoid is represented by Fig. 7. Draw the centreline AB, in the middle of which erect the mean diameter D, which will be alike on each pulley. The largest radius B is determined by the formula

$$R = \sqrt{\frac{\pi^2 a}{4} + \pi a D} - \frac{\pi a}{2}. \qquad . \qquad . \qquad . \qquad . \qquad . \qquad . \qquad 11.$$

Divide the centre line AB into four equal parts and draw the diameters d and d', the lengths of which are determined by the following formulas:

Draw a regular curve through the points a, b, c, d and B which form the sides of the conoid. Draw also the inverted conoid as shown by the dotted lines. Any line drawn through the conoids at right angles to AB determines the diameters of the corresponding steps on each cone pulley. The diameter b o on one pulley corresponds to the diameter m n on the other pulley. It is not intended that the conoid should determine the width of the steps, as may be inferred from Fig. 6, for it only determines the diameters of the steps.

In practice the conoids should be laid out on a full-size scale to make the measurements correct. The length of the centre-line A B should not be less than the diameter D, but better to make it 2D, for the less inclination of the conoid makes sharper measurements for the diameters of the steps.

The whole length of the belt will be,

$$L = \pi D + 2a. \qquad . \qquad . \qquad . \qquad . \qquad 14.$$

For different lengths of the belt and diameter D, with the same distance a between the shafts, the conoid a, b, c, d, B will be of more or less curvature. When $a = \infty$, the conoid becomes a straight line, and when a = D, the radius R = 0.8D, which forms the greatest curvature of the conoid.

For a given length of belt the diameter of the middle step should be

$$D = \frac{L - 2a}{\pi}. \qquad . \qquad . \qquad . \qquad . \qquad . \qquad 15.$$

The diameter of the middle step can also be obtained by assuming a definite value on the greatest radius R—namely:

The length of the belt will then be-

Having given the greatest radius R and middle diameter D, the distance between the shafts should be—

Dimensions, Strength, and Power of Belts.

The strain on a belt is its pulling tension T, and not only the motive force F, as is often considered.

The motive force, under some conditions, is only a small fraction of the pulling tension, as seen in the Tables I. and II., page 374.

The strength of the belt must, therefore, be in proportion to the pulling

tension T.

The following formula 1 is more correct for calculating the breadth of belts than the formulas on page 265. The difference is, however, very small. $S = \max$ maximum strain in pounds per inch of width of belt, which should not

exceed the safety strength given in the accompanying tables, but may be made less.

B =breadth of belt in inches. T =pulling tension in pounds.

India-rubber belts are best in wet or damp places where leather belts cannot be used.

Dimensions and Strength of India-rubber Belts.

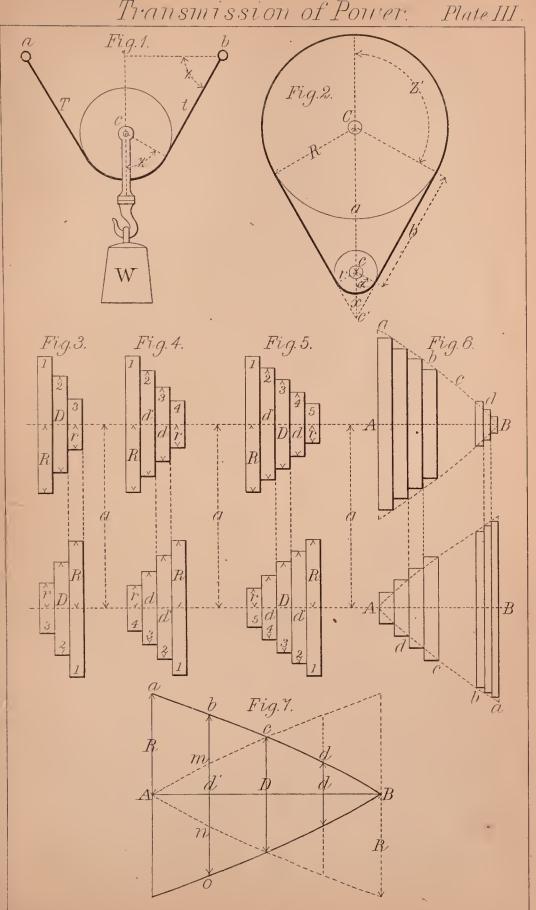
Number of plies.	Wt. per. sq. ft. Pounds.	Thickness. Inches.	Ult. strength. Lbs. per in.	Safety strength.
2 ply.	1.25	$\frac{3}{16} = 0.1875$ $\frac{5}{24} = 0.2083$ $\frac{7}{16} = 0.3125$ $\frac{5}{12} = 0.4166$ $\frac{7}{16} = 0.4375$	625	104
3 ply.	1.66		830	138
4 ply.	2		1000	166
5 ply.	2.4		1200	200
6 ply.	2.8125		1400	233

Thickness in Inches and Strength in Pounds of Belts.

Kind of material in belts.	Thickness.	Stre.	ngth. Safety.
Oak-tanned leather	0.25	1000	166
(6	0.1875	780	130
((0.125	560	95
Ordinary tanned leather	0.25	740	125
(6 66 66 66	0.1875	560	95
(6 (6 (6	0.125	290	50
Raw hide, best quality	•••	1250	225
" " ordinary	•••	1100	185
Horse-skin		800	135
Calf's-skin		360	60
Sheep-skin		322	54
Cowhide	•••	790	130 -
Cotton duck	•••	200	66
Flax, woven belt	•••	1250	200

The above data are for new belts, and cannot be trusted for old and wornout belts.

Carc should be taken to prevent animal oil or fat from coming in contact with the working surfaces of the belt and pullcys, for it reduces the friction. and if once got into the leather it is difficult to get rid of.





HEAT. CALORIC.

The physical constitution of heat is yet under investigation by operative minds: its well-known character and effect upon matter is the base for the investigation.

Heat resembles light, electricity and magnetism. It is convertible into dynamic work, and can consequently be resolved into the three physical elements, force, velocity and time. Temperature is convertible into force, which is only one element of heat, and is no measure of quantity of heat. (See Dynamics and Units of Heat.)

The temperature or intensity of heat is measured in various ways, but most

generally by the expansion of mercury and alcohol, or the thermometer.

Thermometers.

There are three differently graduated thermometers in use—namely, Fahrenheit, Centigrade and Reaumur. The last named is gradually being abolished, and now used only in Peru.

Graduation.

Zero Fahr. = -17.77° Cent.-14.22° Reau.

Freezing-Point of Water.

Zero Cent. = 32 Fahr. = zero Reau.

Boiling-Point of Water.

212° Fahr. = 100° Cent. = 80° Reau.

 9° Fahr. = 5° Cent. = 4° Reau.

Formulas.

Cent. = $\frac{5}{9}$ (Fahr. ∓ 32) = $\frac{5}{4}$ Reau.

Fahr. = $\frac{9}{5}$ Cent. $\pm 32 = \frac{9}{4}$ Reau. ± 32 .

Reau. $=\frac{4}{5}$ Cent. $=\frac{4}{9}$ (Fahr. \mp 32).

The accompanying tables give the equivalents of Centigrade's and Fahrenheit's thermometers. The first numbers in the table of comparison, —276* and 461*, are the absolute zero of temperature.

Example 1. How many degrees on Fahr. scale is 964.5° Cent.?

Table comparison, Cent. $960^{\circ} = 1760^{\circ}$ Fahr. Table Centigrade, Cent. 4.5 = 8.1 "

The required, Cent. 964.5 1768.1 "

Example 2. How many degrees is 2136.7° Fahr. on Centigrade thermometer?

Table comparison, Fahr. 2120° = 1160° Cent.

Table Fahrenheit, " $16^{\circ} = 8.90$ "

" 0.7 = 0.389"

The required degrees, Fahr. $\overline{2136.7} = \overline{1169.289}$ "

Comparison of Fahrenheit and Centigrade Thermometers.

Fahr.	Centig.	Fahr.	Centig.	Fahr.	Centig.	Fahr.	Centig.	Fahr.	Centig.
-5	- 20.55	57	13.88	119	48.33	181	82.77	243	117.22
4	-20.00	58	14.44	120	48.88	182	83.33	214	117.77
-3	— 19.44	59	15.00	121	49.44	183	83.88	245	118.33
-2	- 18.88	60	15.55	122	50.00	184	84 44	246	118.88
ī	- 18.33	61	16.11	123	50.55	185	85.00	247	119.44
Zero.	- 17.77	62	16.66	124	51.11	186	85.55	248	120.00
+1	-17.22	63	17.22	125	51.66	187	86.11	249	120.55
2	-16.66	64	17.77	126 .	52.22	188	86.66	250	121.11
3	- 16.11	65	18.33	127	52.77	189	87.22	251	121.66
3 4	15.55	66	18.88	128	53.33	190	87.77	252	122.22
5	15.00	67	19.44	129	53.88	191	88.33	253	122.77
6	14.44	68	20.00	130	54.44	192	88.88	254	123,33
7	13.88	69	20.55	131	55.00	193	89.44	255	123.88
8	13.33	70	:1.11	132	55.55	194	90.00	256	124.44
9	- 12.77	71	21.66	133	56.11	195	90.55	257	125.00
10	- 12.22	72	22.22	134	56.66	196	91.11	258	125.55
11	11.66	73	22.77	135	57.22	197	91.66	259	126.11
12	- 11.11	74	23.33	136	57.77	198	92.22	260	126.66
13	- 10.55	75	23 88	137	58.33	199	92.77	261	127.22
14	- 10.00	76	24.44	138	58.88	200	93.33	262	127.77
15	- 9.44	77	25.00	139	59.44	201	93.88	263	128.33
16	- 8.88	78	25.55	140	60.00	202	94.44	264	128.88
17	— 8 33	79	26.11	141	60.55	203	95.00	265	129.44
18	— 7.77	80	26.66	142	61.11	204	95.55	266	130.00
. 19	— 7.22	81	27.22	143	61.66	205	96.11	267	130.55
20	- 6.66	82	27.77	144	62.22	206	96.66	268	131.11
21	- 6.11	83	28.33	145	62.77	207	97.22	269	131.46
22	- 5.55	84	28,88	146	63.33	208	97.77	270	132.22
23 24	$\begin{bmatrix} -5.00 \\ -4.44 \end{bmatrix}$	85 86	29.44 30.00	147 148	63.88	209	98.33	271	132.7 7 133.33
25	-3.88	87	30.55	149	64.44 65.00	210 211	98.88 99.41	$\begin{array}{c c} 272 \\ 273 \end{array}$	133.88
26	- 3.33	88	31.11	150	€5.55	212	100.00	274	134,44
27	$\begin{bmatrix} -3.33 \\ -2.77 \end{bmatrix}$	89	31.66	151	(6.11	213	100.55	275	135.00
28	2.22	90	32.22	152	66.66	214	101.11	276	135.55
29	- 1.66	91	32.77	153	67.22	215	101.66	277	136.11
30	- 1.11	92	33,33	154	67.77	216	102.22	278	136.66
31	55	93	33.88	155	68.33	217	102.77	279	137.22
32	Zero.	94	34.44	156	68.88	218	103.33	280	137.77
33	+ 0.55	95	35.00	157	69.44	219	103.88	281	138.33
34	1.11	96	35.55	158	70.00	220	104.44	282	138.88
35	1.66	97	36.11	159	70.55	221	105.00	283	139.44
36	2.22	98	36.66	160	71.11	222	105.55	284	140.00
37	2.77	99	37 22	161	71.66	223	106.11	285	140.55
38	3.33	100	37.77	162	72.22	224	106.66	286	141.11
39	3.88	101	38,33	163	72.77 -	225	107.22	287	141.66
40	4.44	102	38.88	164	73.33	226	107.77	288	142.22
41	5.00	103	39.44	165	73.88	227	108.33	289	142.77
42	5.55	104	40.00	166	74.44	228	108.88	290	143.33
43	6.11	105	40.55	167	75.00	229	109.44	291	143.88
41	6 66	106	41.11	168	75.55	230	110.00	292	144.44
45 46	7.22 7.77	107	41.66 42.22	169 170	76.11	231	110.55	293	145.00
47	8,33	108 109	42.22	170	$76.66 \\ 77.22$	232 233	111.11	294 295	$\frac{145.55}{146.11}$
48	8.88	110	43.33	172	77.77	234	112.22	296	146.66
49	9.44	111	43.88	173	78.33	235	112.77	297	140.00
50	10.00	112	44.41	174	78.88	236	113.33	298	147.17
51	10.55	113	45.00	175	79.44	237	113.88	299	148.33
52	11.11	114	45.55	176	80.00	238	114.44	300	148.88
53	11.66	115	46.11	177	80.55	239	115.00	400	204.44
54	12.22	116	46.66	178	81.11	240	115.55	600	315.55
55	1277	117	47.22	179	81.66	241	116.11	800	433,33
56	13.33		47.77	180	82.22	242	116.66	1000	537.77
							1		

Comparison of Centigrade and Fahrenheit Thermometers.

	Comparison of Centigrade and Fahrennett Thermometers.									
Cent.	Fahr.	Cent.	Fahr.	Cent.	Fahr.	Cent.	Fahr.	Cent.	Fahr.	
276*	461*	16	60.8	330	626	950	1742	1570	2858	
-260	436	17	62.6	340	644	9 0	1760	1580	2876	
-250	-418	18	64.4	350	662	970	. 1778	1590	2894	
-240 -230	-400 -382	19 20	66.2	360	680	980	1796	1600	2912	
-230 -220	-364	21	68.0 69.8	370 380	698 716	990 1000	1814 1832	1610 1620	2930 2948	
-210	— 346	22	71.6	390	734	1010	1850	1630	2966	
-200	-328	23	73.4	400	752	1020	1868	1640	2934	
-190	310	24	75.2	410	770	1030	1886	1650	3002	
-180	298	25	77.0	420	788	1040	1904	16:0	3020	
-170	-274	26	78.8	430	806	1050	1922	1670	3038	
—160	-256	27	80.6	440	824	1060	1940	1680	3056	
-150 -140	-238 -220	28 29	82.4 84.2	450 460 •	842 860	1070	1958 1976	1690 170J	3074 3092	
-130	202	30	86.0	470	878 .	1090	1994	1710	3110	
-120	-184	31	87.8	480	836	1100	2012	1720	3128	
-:10	-166	32	89.6	490	914	1110	2030	1730	3146	
-100	-148	33	91.4	500	932	1120	2048	1740	3164	
- 90	— 130	34	93.2	510	950	1130	2065	1750	3182	
— 80	-112	35	95.0	520	968	1140	2084	1760	3200	
- 70	-94	36	96.8	530	986	1150	2102	1770	3218	
-60 -50	$-76 \\ -58$	3 7 3 8	98.6 100.4	540	1004 1022	1169 1170	2120 2138	1780 1790	$3236 \\ 3254$	
- 40	-40	39	102.2	560	1040	1180	2156	1800	3272	
- 30	$-\frac{10}{22}$	40	104.0	570	1058	1190	2174	1810	3290	
- 20	$-\frac{7}{4}$	41	105.8	580	1076	1200	2192	1820	3308	
- 19	_ 2.2	42	107.6	590	1094	1210	2210	1830	3326	
- 18	- 0.4	43	109.4	600	1112	1220	2228	1840	3344	
17.77	Zero.	44	111.2	610	1130	1230	2246	1850	3362	
→ 17	+ 1.4	45	113.0 114.8	620	1148	1240 1250	$\frac{2264}{2282}$	1860 1870	3380	
$\begin{vmatrix} -16 \\ -15 \end{vmatrix}$	$\begin{array}{c c} + 3.2 \\ + 5.0 \end{array}$	46	116.6	630 640	1166 1184	1260	2300	1880	$\frac{3398}{3416}$	
— 13 — 14	+6.8	48	118.4	650	1202	1270	2318	1890	3434	
- 13	+ 8.6	49	120.2	660	1220	1280	2336	1900	3452	
- 12	+10.4	50	122.0	670	1238	1290	2354	1910	3470	
- 11	+12.2	60	140	680	1256	1300	2372	1920	3488	
- 10	+14.0	70	158	690	1274	1310	2390	1930	3506	
- 9 	+15.8	80	176 194	700	1292 1310	1320 133)	$2408 \\ 2426$	1940 1950	$3524 \\ 3542$	
- 8 - 7	$+17.6 \\ +19.4$	100	212	720	1328	1340	24-14	1960	3560	
- 6	+21.2	110	230	730	1346	1350	2462	1970	3578	
- 5	+23.0	120	248	740	1364	1360	2480	1980	3596	
_ 4	+24.8	130	266	750	1382	1370	2498	1990	3614	
- 3	+26.6	140	284	760	1400	1330	2516	2000	3632	
- 2	+28.4	150	302	770	1418	1390	$2534 \ 2552$	2010	3650	
<u>1</u>	$+30.2 \\ +32.$	160 170	320 338	780 700	$1436 \\ 1454$	1400 1410	$-\frac{2552}{2570}$	2020	3668 3686	
Zer . +1	+32. $+33.8$	180	356	800	1472	1420	$\frac{2570}{2583}$	2 40	3704	
1 2	35.6	190	374	810	1490	1430	2606	2050	3722	
3	37.4	200	392	820	1508	1440	2624	2060	3740	
4	39.2	210	410	830	1526	1450	2642	2070	3758	
5	41.0	220	428	840	1544	1460	2660	2080	3776	
6	42.8	230	446	850	1562	1470	2678	2090	3794	
7	44.6	$\begin{vmatrix} 240 \\ 250 \end{vmatrix}$	464 482	860 870	1580 1698	1480 1490	$\begin{array}{c} 2 \delta 96 \\ 2714 \end{array}$	2100	3812	
8 9	46.4 48.2	260	500	880	1616	1500	2732	2110 2120	3830 3848	
10	50.0	270	518	890	1634	1510	2750	2130	4166	
ii	51.8	280	536	900	1652	1520	2768	2140	4184	
12	53.6	290	551	910	1670	1530	2786	2150	4162	
13	52.4	300	572	920	1688	1540	2804	2:0	4180	
14	57.2	310	590	930	1706	1550	2822	2180	4216	
15	59.0	320	608	940	1724	1560	2840	2200	4252	
									1	

Number of Degrees Cent. = Number of Degrees Fahr.

Degrees		Tenths of a Degree—Centigrade Scale.											
Cent.	.0	.1	.2	.3	.4	.5	.6	.7	.8	.9			
	Fahr.	Fahr.	Fahr.	Fahr.	Fahr.	Fahr.	Fahr.	Fahr.	Fahr.	Fahr.			
0	0.00	0.18	0.36	0.54	0.72	0.90	1.08	1.26	1.44	1.62			
1	1.80	1.98	2.16	2.34	2.55	2.70	2.88	3.06	3.24	3.42			
2	3.60	3.78	3.96	4.14	4.32	4.50	4.68	4.86	5.04	5.22			
3	5.40	5.58	5.76	5.94	6.12	6.30	6.48	6.66	6.84	7.02			
4 5	7.20	7.38	7.56	7.74	7.92	8.10	8.28	8.46	8.64	8.82			
5	9.00	9.18	9.36	9.54	9.72	9.90	10.08	10.26	10.44	10.62			
. 6	10.80	.10.98	11.16	11.34	11.52	11.70	11.88	12.06	12.24	12.42			
7	12.60	12.78	12 96	13.14	13.32	13.50	13.68	13.86	14.01	14.22			
8	14.40	14.58	14.76	14.94	15.12	15.30	15.48	15.66	15.84	16.02			
9	16.20	16.38	16.56	16.74	16.92	17.10	17.28	17.46	17.64	17.82			

Number of Degrees Fahr. = Number of Degrees Cent.

Degrees			Tentl	ns of a l	Degree-	–Falirei	nheit Sc	cale.		
Fahr.	.0	.1	.2	.3	.4	.5	.6	7.	.8	.9
	Cent.	Cent.	Cent.	Cent.	Cent.	Cent.	Cent.	Cent.	Cent.	Cent
0	0.00	0.06	0.11	0.17	0.22	0.28	0.33	0.39	0.41	0.55
1	0.56	0.61	0.67	0.72	0.78	0.83	0.89	0.94	1.00	1.06
2	1.11	1.17	1.22	1.28	1.33	1.39	1.44	1.50	1.56	1.51
3	1.67	1.72	1.78	1.83	1.89	1 94	2.00	2.06	2.11	2.17
-1	2.22	2.28	233	-2.39	2.44	2.50	2.56	2.61	2.67	27_
5	2.78	2 83 $ $	-2.89	2.94	3.00	3.06	3.11	3.17	3.22	3.28
6	3,33	3,39	3.44	3.50	3.56	3.61	3.67	3.72	3.78	3.8
7	3 89	3.94	4.00	4.06	4.11	4.17	4.22	4.28	4.33	4.39
8	4.41	4.50	4 56	4.61	4.67	4.72	4.78	4.83	4.8)	4.94
9	5.00	5.06	5.11	5.17	5.22	5.28	5 33	5.39	5.44	5.5 0

LATENT HEAT.

Latent heat is the number of units of heat required to change the aggregate form of a body, whilst the temperature remains constant—that is, the heat required to melt a body from solid to liquid, and to evaporate a liquid. In the one case it is called the latent heat of fusion, and in the other, the latent heat of evaporation.

Latent Units of Heat per Pound of Substance.

Solids smelted to liquid.	Latent heat.	Liquids converted to vapor.	Latent heat.
Ice to water,	141	Water to steam,	966
Tin,	$25.6 \\ 50.6$	Amnionia,	$895 \\ 372$
Zinc, Sulphur,	17.0	Alcohol, pure,	298
Lead,	9.72	Bisulphide of carbon,	212
Mercury,	5.00	Ether, sulphuric	174
Beeswax,	175	Essence of turpentine,	137
Bismuth,	550	Oil of turpentine,	184
Cast iron,	233	Mercury,	157
Spermaceti,	46.4	Chymogene,	175

Fusion.

L = latent heat (units) per pound of liquid at smelting-point.

C = specific heat of the liquid.

c = specific heat of solid.

t =temperature of fusion, Fahr.

$$L = (C - c)(t + 256).$$

Evaporation.

l = latent units of heat per pound of vapor at boiling-point.

T= temperature of boiling-point, Fahr.

(Regnault.)

 $l = 1091.7 - 0.695(T - 32) - 0.000000103(T - 39.1)^3$.

Temperature of Boiling or Evaporation under Atmospheric Pressure.

Liquids.	Fahr.	Cent.	Liquids.	Fahr.	Cent.
Wrought iron,	5000°	27600	Alcohol,	173	78
Cast iron,	3 300	1815	Ether,	96	35
Mercury,	6 65	352	Carbon, bisulphuretted,	116	47
Whale oil,	630	332	Water, distilled,	212	100
Oil of linseed,	600	316	Salt sea water,	213	101
Oil of turpentine, .	357	180	Water 20 per cent. salt,	218	103
Sulphuric acid,	593	312	" 30 " " .	222	105
Sulphur,	570	300	" 40 " saturated,	227	108
Phosphorus,	557	292	Ammonia, liquid,	140	60
Sweet oil,	412	211	Water in vacuo,	98	36
Naplitha,	320	160	Chymogene,	+ 38	3.3
Nitric acid,	220	104	Carbonic acid,	-112	80
Milk of cows,	213	101	Ammonia,	- 30	- 34
Rectified petroleum, .	316	158			1

Distillation Temperatures of Coal-oils.—(Tissandier.)

LIGHT OILS.	Fahr.	Cent.	HEAVY OILS.	Fahr.	Cent.	HEAVY OILS.	Fahr.	Cent.
Amylène, Benziue, Toluène, Xylène, Pyridine,	102° 187° 226° 271° 302°	86.1° 108° 133°	Cumène, Lutidine, Eupione, Cymène, Aniline,	304° 311° 338° 347° 359°	155° 170° 175°	Carbolic acid Nephthline, Quilonèine, Anthracene, Chrysène,	370° 422° 462° 500° 572°	188° 217° 239° 260° 300°

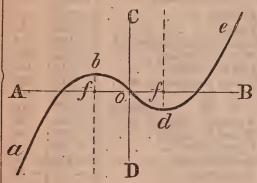
The temperature of distillation of vapors is equal to that of the boiling-point of the liquid of which the vapor is formed.

Temperature of Fusion, Freezing or Smelting-Point.

Solids.		Fahr.	Cont	Solids.	Fahr	Cent.
SULIDS.		ram.			rall.	cent.
Platinum, .		30800	16930	Puddle slag,	26060	1430°
Wrought iron, .		2912	1600	Sulphur,	228	169
Cast iron, gray.		2012	1100	Beeswax, white,	155	68
Cast iron, white, .		1922	1050	" yellow, .	142	61
Steel,		2500	1371	Spermaceti,	142	61
Gold, pure,		2300	1260	Potassium,	136	58
Gold, money, .		2192	1200	Sodium,	104	90
Copper,		2160	1232	Olive oil,	92	33
Brass, common,		1900	1038	Tallow,	36	2.2
Silver,		1850	1021	Ice of water,	32	0.000
Litharge, .		1739	954	" milk,	30	1.1
Antimony,		800	427	" sea water,	28	-2.2
Zinc,		740	393	" Vinegar	28	- 2.2
Lead,	. L	600	316	" strong wine, " brandy,	20	6.6
Bismuth,	. B	470	254	" " brandy, .	7	13.9
Tin,		420	215	" oil of turpentine,	14	10
2 Tin, 1 Lead, .		360	181	1 snow, 1 salt,	0.00	-17.8
1 Tin, 3 Lead, .		500	260	1 alcohol, 1 water, .	- 7	-21.6
1 Tin. 1 Bismuth,		283	140	Cyangen,	— 30	-34.4
3T + 2L + 5B, .		212	100			-40
1T + 1L + 4B,		200	93	Sulphuric ether,	- 47	- 43.9
2T + 3L + 2B, .		199	92	Sulphurous acid,	-105	-76
Slag of copper,		2462	1350	Nitrous oxide,	-150	- 101
Slag of tin,		2402	1318	Nitric acid,		
			-			

EXPANSION OF BODIES BY HEAT.

All bodies in nature expand when heated, and contract when cooled. Solids vary but little by the difference in temperature; liquids vary more, but gases are extremely susceptible to the impression of heat and cold.



There is a very singular fact connected with the expansion and contraction of substances at and near the temperature of fusion, which may be illustrated in the accompanying figure.

Let A B represent the absciss-axis of temperature, C D the ordinate axis of expansion or contraction, and the origin O the temperature of fusion, O A the femperature of the solid, and O B that of the liquid.

Let a solid of volume and temperature at a be heated, it will expand until it reaches a maximum volume at b, after

which it contracts toward the temperature of fusion O. The temperature still increasing, the liquid will continue to contract until it reaches a minimum volume or maximum density at d, after which it will expand toward e. The lines a b 0 and 0 d e are parabolas, of which the absciss-axis A B passes through the focuses f. The formula for the parabola is $y = x^n$, in which the exponent n depends

upon the nature of the substance operated upon, and also whether it is linear or volume expansion, x representing the temperature and y the volume.

Ice melts at 32° Fahr., and the water reaches its maximum density at $d=39^{\circ}$ (as now accepted, but d is nearer 40°). Ice reaches its maximum volume at $b=24^{\circ}$. Ice and water are of equal density at the temperatures 16°, 32° and 48°. Ice generally floats in water, because the difference in temperature is less than 32°, but if ice of less than 16° is put into water of more than 48°, it will sink. The same phenomenon takes place with other substances; for instance, solid cast iron put into molten cast iron will float, but if the fluid cast iron is at a white heat, like that in a pneumatic furnace (Bessemer), the solid iron will sink.

The following formulas are deduced from experiments which have not extended through the temperatures of fusion, except that for water, page 392.

Notation of Letters.

- L = linear expansion of solids and liquids, per degree Fahr., between any temperatures.
- l= linear expansion per degree between 32° and 212°, as contained in the accompanying table.
- D and d = absolute temperature in degrees Fahr.
- n = exponent of expansion, which varies inversely with the rate of expansion of bodies.

Exponent n for	1.04 · Water.	2.5 Glass.	2.6 Iron.	2.77 Copper.	14.1 Platinum.	15.6 Mercury.
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Linear expansion per degree from 32° to T° will be

$$L = \frac{l}{10580000} \sqrt[n]{D}.$$

Linear expansion per degree between any temperature is

$$L = \frac{l}{10580000} \left(\sqrt[n]{D} - \sqrt[n]{d} \right)$$

The linear expansion per degree multiplied by 2 will be the surface expansion. The linear expansion per degree multiplied by 3 will be the volume expansion.

Dilatation or Expansion of Substances,

Per Degree of Fahrenheit Scale.

Tempera-	Solids.	Linear, l.	Surface, a.	Volume, v.
32° to 212°		0.00000478	0.00000956	0.00001434
212 " 392	Glass,	0.00000546	0.00001093	0.00001434
392 " 572	Curaos,	0.00000040	0.00001093	0.00001039
	{	0.000000656	0.00001320	0.00001980
	Wrought iron,			
32 " 572	Soft mood iman	0.00000895	0.00001790	0.00002686
32 " 212	Cost inch	0.00000680	0.00001360	0.00002040
32 " 212	Cast fron,	0.00000618	0.00001236	0.00001854
32 " 212	Soft, good iron,	0.00000600	0.00001200	0.00001800
32 " 212	hardened steer,	0.00000689	0.00001378	0.00002067
32 " 212	Copper,	0.00000955	0.00001910	0.00002865
32 " 572		0.00001092	0.00002184	0.00003276
32 " 212	Lead,	0.00001580	0.00003160	0.00004740
32 " 212	Gold, pure,	0.00000815	0.00001630	0.00002445
32 " 212	Gold, hammered,	0.00000830	0.00001660	0.00002490
.33 " 212	Silver, pure, Silver, hammered,	0.00001060	0.00002120	0.00003180
32 " 212	Silver, hammered,	0.00001116	0.00002232	0.00003348
32 " 212	Brass, common cast,	0.00001043	0.00002086	0.00003129
32 " 212	Brass, wire or sheet, .	0.00001075		0.00003225
32 " 212	Platinum, pure,	0.00000191	0.00000982	0.00001473
32 " 572)	0.00000520	0.00001040	0.00001560
32 " 212	Palladium,	0.00000555	0.00001110	0.00001665
32 " 212	Palladium,	0.00000797	0.00001594	0.00002391
32 " 212	Platinum, hammered, .	0.00000530	0.00001060	0.00001590
32 " 212	Zinc, pure or cast,	0.00001633	0.00003266	0.00004899
32 " 212	Zinc, hammered, .	0.00001722	0.00003414	0.00005166
32 " 212	Tin, cast,	0.00001207	0.00002414	0.00003621
32 " 212	Zinc, pure or cast, Zinc, hammered, Tin, cast, Tin, hammered, Fire brick, Good red brick, Marble, Granite; Bismuth, Antimony,	0.00001500	0.00003000	0.00004500
32 " 212	Fire brick,	0.00000275	0.00000470	0.00000705
32 " 212	Good red brick,	0.00000305	0.00000610	0.00000915
32 " 212	Marble,	0.00000613	0.00001226	0.00001839
32 " 212	Granite;	0.00000438	0.00000876	0.00001314
32 " 212	Bismuth,	0.00000773	0.00001546	0.00002319
32 " 212	Antimony,	0.00000602	0.00001204	0.00001806
32 " 212	Palladium,	0.00000555	0.00001110	0.00001665
32 " 212		0.00003333	0.00006666	0.00010000
212 " 392	≻Mercury,	0.00003416	0.00006833	0.00010250
392 " 572		0.00003500	0.00007000	0.00010500
32 " 212		0.00008806	0.00017612	0.00026420
212 " 392	Water, · · ·	0.00017066	0.00034133	0.00051020
392 " 572		0.00018904	0.00037808	0.00056713
32 " 212	Salt, dissolved,	0.00009250	0.00018500	0.00027780
32 " 212	Sulphuric acid,	0.00011111	0.00022222	0.00033333
32 " 212	Turpentine and ether, .	0.00012966	0.00025933	0.00038900
32 " 212	Oil, common,	0.00014814	0.00029629	0.00044444
32 " 212	Alcohol and Nitric Acid,	0.00015151	0.00030302	0.00055555
32 " 212	All permanent gases, .	0.00069416	0.00138832	0.00208250

Force of Temperature.

It is the force of temperature which expands the bodies, and not the quantity of heat. See pages 379 and 392. Temperature is convertible into force. Let P denote the force of pressure in pounds per square inch, and T temperature Fahr.

Then,
$$P = \left(\frac{T + 105.1}{202.8}\right)^6$$
, and $T = 202.8 \sqrt[6]{P} - 105.1$.

This force, multiplied by the space of expansion, is the work done by the heat.

Conducting Power of Different Substances for Heat and Electricity.

		22200110103			
Metals.		Quartz sand, 3	5.56	Liquids.	
Silver, fine, .	100	Limestone, 19	9.8 V	Vater,	1.000
Gold, "	98			Iercury,	2.80
Gold, .991, .	84			Proof spirit,	0.847
Copper, ham'd,	85			Alcohol, pure,	0.931
Copper, cast,	81			Vitric acid,	1.5
Mercury,	68			ulphur. acid,	1.7
Aluminium, .	66		.026 S	ulphur. ether,	2.1
Zinc, hammered	64	Roman cement, 2.		Surpentine,	3.1
Zinc, cast ver-			.52	Gases.	
tical,	63	Chalk, 5.	$.853 _{A}$	Lir,	0.9855
Zinc, cast hori-		Woods.		Radiating Power.	
zontal,	60		.10 V	Vutar	100
Lead, cast, .	20		.10 L	Vater,	100
Cadmium,	57			Paper, writing,	98
Wrought iron,	43	Oak with the films 2	.30 R	Rosin,	96
Tin,	42	Elm " " 3		ealing-wax,	95
Steel,	40	Ash " " 3		lass, common, .	90
Platinum,	40	Apple " " 2		ndia ink,	88
Cast iron,	36	Elm, " " . 3. Ash, " " . 3. Apple, " " . 2. Ebony, " " . 2.	2 11	ce,	85
Antimony, cast	04	Lampblack, 0.	.112 R	Red lead,	80
vertical,	21	Cross: with fibre=1:3,		raphite,	75
Antimony, cast	40			ead, tempered, .	45
horizontal,	19	Black oak, 3.		Iercury,	20
German silver,	10	Chestnut, 3.		ead, polished,	19
Bismuth,	6	Spanish mahogany, 2.	.8 I	ron, polished,	15
Stone & Crystals.		Walnut, 3.	.3 T	'in and silver,	12
Marble,	12.21	Fur.	C	topper and gold, .	12
Glass,	9.65	Hare's fur, 0.0	0946	Reflecting Powers.	
Common brick,	8.422	Eider down, 0.0	0668 B	Brass,	100
Fire-brick, .	6.05	Beaver's fur 0.0	0675 S	ilver	90
Fire-clay,	6.61	Raw silk, 0.0	069 2 T	infoil,	85
Porcelain, .	7.55	Wool, sheep, 0.0	$0778 \mathrm{T}$	in,	80
Wood-ashes, .	0.8359			teel,	70
				lead,	60
Coal, bitum., .)955 G	llass,	10
Coal, charred,	0.738	Flannel, 0.3	395 G	lass, oiled or waxed,	5
Coke,	19.80	Horse-hair,	304 II	ampblack,	0

Miscellaneous Temperatures.

	Fahr.		Fahr.
In the Bessemer furnace, .	40000	1 alcohol, 1 water freezes, .	_ 70
Puddling-furnace,	3500	Mean temp. of the poles, .	 13
Cupola,	3000	Temp. outside atmosphere, . -	58
Heat of common fire,	1100		 56
Red heat in daylight,	1070	,	65
Iron red in dark,	752	, , , , , , , , , , , , , , , , , , , ,	 78
Mean temp. of the earth,	50		 88
" " torrid zone, " " temp. " " " polar region,	75	The state of the s	 43
temp. "	50		166
polar region,	20	At 50°, Mixtures of—	Prod.
Temp, of ignition,	636		46
Highest temp. of wind,	117	Water,	10
Temp. of the human blood,	98	Sulphate of soda, 8]	5 0
A comfortable room,	70	Muriatic acid, 5	•
Mean temp. of ocean,	6 2	Dilate sulphuric acid, . 5	23
	1	Snow, 45	

ON AIR AND HEAT.

Dry air expands or contracts uniformly 0.0020825 its volume per degree Fahr. in difference of temperature, or 0.0037485 per degree Centigrade under constant pressure. Assuming the expansion per degree Fahr. as unit, the primitive volume will be—

$$\frac{1}{0.0020825} = 480.$$

V and v = volumes of dry air of temperatures t and T Fahr., and pressure p and P above vacuum. The volumes and pressures in the following formulas may be expressed in any units of measures.

Volume and Temperature Variable under Constant Pressure.

$$V = v \left(\frac{T - t}{480} + 1 \right)$$
, and $(T - t) = \frac{480 (V - 1)}{v}$, 1.

Example 1. v = 18 cubic feet of air, of $t = 36^{\circ}$, is to be heated to $T = 84^{\circ}$ under constant pressure. Required, the volume V?

$$V = 18\left(\frac{84 - 36}{480} + 1\right) = 19.8$$
 cubic feet, the answer.

Volume and Pressure variable under Constant Temperature.

$$(T-t)=0$$
, the pressures will be—

$$\frac{P}{p} = \frac{V}{v}$$
, and $\frac{p}{P} = \frac{v}{V}$, 2.

$$P = p \frac{V}{v}$$
, and $v = V \frac{p}{P}$, 3.

Example 2. V=150 cubic feet of air, of pressure p=1475 pounds to the square inch, is to be compressed to 50 cubic feet. The heat generated in the compression to radiate through the vessel until the temperature of the compressed air is equal to that in V. Required, the pressure P?

Formula 3.
$$P = p \frac{V}{v} = 14.75 \times \frac{150}{50} = 44.25 \text{ lbs.}$$

When the Temperature, Volume and Pressure

are all variable, we have-

$$P = p \frac{V}{v} \left(\frac{T - t}{480} + 1 \right)$$
, and $(T - t) = 480 \left(\frac{Pv}{pV} - 1 \right)$, 4.

It must be distinctly understood in all these formulas that the volume v belongs to the pressure P and temperature T, and the volume V to p and t. The primitive quantities are v, P, T. It may happen in the Formula 4 that v > V, t > T, and p > P.

Example 3. V=1000 cubic inches of air of p=14.75 and $t=59^{\circ}$, is to be reduced to v=320 cubic inches, and the temperature increased to $T=369^{\circ}$. Required, the pressure P per square inch?

Formula 4.
$$P = 14.75 \frac{1000}{320} \left(\frac{369 - 59}{480} - 1 \right) = 75.8 \text{ lbs.}$$

Example 4. v=290, P=88.5 to be increased to V=838, and p=18.4. Required, the difference of temperature (T-t)?

Formula 4.
$$(T-t) = 480 \left(\frac{88.5 \times 290}{18.4 \times 838} - 1 \right) = 320^{\circ}$$
.

On the Compression and Expansion

of a definite weight of air enclosed in a vessel.

In this treatment no heat must be lost or gained by radiation from the sides of the vessel in which the air is enclosed. Let D and d represent the degrees of absolute temperatures of volumes v and V of the air to be experimented upon.

The absolute zero is 461° below Fahr. zero, and 274° Cent. below the freezing-point of water. D=461+T, d=461+t, and D-d=T-t, Fahr. scale.

Volume and Temperature.

$$\frac{V}{v} = \left(\frac{D}{d}\right)^{2.45}$$
, and $\frac{v}{V} = \left(\frac{d}{D}\right)^{2.45}$ 5.

Expansion
$$V = v \left(\frac{D}{d}\right)^{2.45}$$
, Compression $u = \left(\frac{d}{D}\right)^{2.45}$ 6.

Compression
$$D = d \sqrt[2.45]{\frac{\overline{V}}{v}}$$
, Expansion $d = D \sqrt[2.45]{\frac{\overline{v}}{V}}$ 7.

Example 5. To what fraction must air of $t=65^{\circ}$ be compressed, in order to fire tinder at a temperature of $T=550^{\circ}$, $d=461+65=526^{\circ}$, $D=550+461=1011^{\circ}$?

Formula 5.
$$\frac{v}{V} = \left(\frac{526}{1011}\right)^{2.45} = 0.20$$
, the answer.

Example 6. How much must air of $T=80^{\circ}$ be expanded to reduce the temperature to $t=32^{\circ}$, or freezing-point of water?

Formula 5.
$$\frac{V}{v} = \left(\frac{541}{493}\right)^{2.45} = 1.3308$$
 times, the answer.

Example 7. v=360 cubic inches of air of temperature $T=380^{\circ}$, or $D=841^{\circ}$, is to be expanded until the temperature becomes $t=80^{\circ}$ or $d=541^{\circ}$. Required, the volume V, corresponding to that temperature?

Formula 6.
$$V = 360 \left(\frac{821}{541}\right)^{2.45} = 1025.9$$
 cubic feet.

Example 8. V=20 cubic feet of air of $t=32^{\circ}$, or d=493, is to be compressed to v=12 cubic feet. Required, the temperature T of compression?

Formula 7.
$$D = 493 \sqrt[2.45]{\frac{20}{12}} = 60729^{\circ}$$
, or $T = 146.29^{\circ}$.

Pressure and Temperature.

$$\frac{P}{p} = \left(\frac{D}{d}\right)^{3.42}, \quad \text{and} \quad \frac{p}{P} = \left(\frac{D}{d}\right)^{3.42} \quad 8.$$

Compression
$$P = p\left(\frac{D}{d}\right)^{3.42}$$
, Expansion $p = P\left(\frac{d}{D}\right)^{3.42}$ 9.

Compression
$$D = d \sqrt[3.42]{\frac{\overline{P}}{p}}$$
, Expansion $d = D \sqrt[3.42]{\frac{\overline{p}}{P}}$ 10.

Example 9. A volume of air of pressure p=15 pounds to the square inch, and of temperature $t=62^{\circ}$, is to be compressed until the temperature becomes $T=120^{\circ}$. Required, the pressure P per square inch at $T=120^{\circ}$?

$$d = 461 + 62 = 523$$
, and $D = 461 + 120 = 581$.

Formula 9.
$$P = 15 \left(\frac{581}{523}\right)^{3.42} = 21.49$$
 lbs. pr. sq. inch.

Example 10. A volume of air of pressure P=45 pounds to the square inch, and of temperature $T=250^{\circ}$, or $D=711^{\circ}$, is to be expanded to a pressure of p=25 pounds. Required, the temperature t of the expanded air?

Formula 10.
$$d = 711 \sqrt[3.42]{\frac{25}{45}} = 598.72^{\circ}$$
, and

 $t = 598.72 - 461 = 137.72^{\circ}$, the temperature required.

Pressure and Volume.

$$\sqrt[2.45]{\frac{\overline{V}}{v}} = \sqrt[3.42]{\frac{\overline{p}}{P}} \quad \text{and} \quad \sqrt[2.45]{\frac{\overline{v}}{V}} = \sqrt[3.42]{\frac{\overline{p}}{P}} \quad . \quad 11.$$

Expansion
$$V=v\sqrt[1.4]{\frac{P}{p}}$$
, Compression $v=V\sqrt[1.4]{\frac{P}{P}}$. 12.

Compression
$$P = p\left(\frac{V}{v}\right)^{1.4}$$
, Expansion $p = P\left(\frac{v}{V}\right)^{1.4}$. 13.

Example 11. A volume v = 50 cubic inches, and of pressure P = 80 pounds per square inch, is to be expanded until the pressure becomes p = 15 pounds. Required, the expanded volume V?

Formula 12.
$$V = 50 \sqrt[1.4]{\frac{80}{15}} = 165$$
 cubic inches.

Example 12. What will be the pressure of a volume of air expanded 1.3308 times?

Formula 13.
$$p = \left(\frac{1}{1.3308}\right)^{1.4} = 0.5324$$
 of the primitive pressure.

Volume and Weight of Dry Air

At different Temperatures, under a constant Atmospheric Pressure of 29.92 inches in the Barometer, the Volume at 32° Fahr. being the unit.

Temp.	Volume.	Wt. per Cub. ft. Pounds.	Temp.	Volume.	Wt. per Cub. ft. Pounds.	Temp.	Volume.	Wt. per. Cub. ft. Pounds.
00	.935	.0864	1620	1.265	.0368	5500	2.056	.0384
12	.960	.0842	172	1.425	.0628	600	2.150	.0376
22	.980	.0824	182	1.306	.0618	650	2.260	.0357
32	1.000	.0807	192	1.326	.0609	700	2.362	.0338
42	1.020	.0791	202	1.347	.0600	800	2.566	.0315
52	1.041	.0776	212	1.367	.0591	900	2.770	.0292
62	1.061	.0761	230	1.404	.0575	1000	2.974	.0268
72	1.082	.0747	250	1.444	.0559	1100	3.177	.0254
82	1.102	.0733	275	1.495	.0540	1200	3.381	.0239
9.3	1.122	.0720	300	1.546	.0522	1500	3.993	.0202
102	1.143	.0707	325	1.597	.0506	1800	4.605	.0175
112	1.163	.0694	350	1.648	.0490	2000	5.012	.0161
122	1.184	.0682	375	1.689	.0477	2200	5.420	.0149
132	1.204	.0671	400	1.750	.0461	2500	6.032	.0133
142	1.224	.0619	450	1.852	.0436	2800	6.644	.0121
152	1.245	.0649	500	1.954	.0413	3000	7.051	.0114

For Weight and Volume of air at Low Temperature, see Hygrometry, page 357.

SPECIFIC HEAT OR CALORIC.

Different bodies require different quantities of heat for equal difference in temperature. This difference is called specific heat. The specific heat of bodies varies nearly inverse as the specific gravity. The specific heat in all bodies increases slightly with the elevation of temperature. One pound of water elevated from 32° to 212° requires 180.9 units of heat instead of 180. The specific heat increases nearly in the same ratio for all solid and liquid bodies. The specific heat of water from 32° to T° will be—

$$S = 1 + \frac{(T - 32)^{1.67}}{1167713}.$$

The specific heat of water between any temperatures T and t will be—

$$S = 1 + \frac{(T - 32)^{1 \cdot 67} - (t - 32)^{1 \cdot 67}}{1167713}.$$

The following table gives the specific heat of different substances between the temperature 32° and 212°, compared with water as unit. When the specific heat of a body is required between high temperatures, it is necessary to calculate first the specific heat of water between such temperatures, which multiplied by the number in the table will give the required specific heat of the body.

Specific Heat or Caloric of Substances.

					
Water,	1.000	Lead,	0.030	Sweet oil,	0.310
Ice of water, .	0.513	Steel,	0.118	Cil of turpentine,	0.472
Cast iron,	0.140	Diamond,	0.147	Gases of constant	
Wrought iron, .	0.110	Arsenic,	0.081	volume and under	
Cobalt,	0.150	Iodine,	0.054	atmospheric pres-	
Nickel,	0.103	Sulphur,	0.200	sure.	
Copper,	0.094	Lime, burned, .	0.217	Atmospheric air, .	0.250
Zinc,	0.093	Glass-crystals,	0.193	Oxygen,	0.230
Tin,	0.047	Glass, common,	0.177	Hydrogen,	3,30
Autimony,	0.051		0.500	Nitrogen,	0.275
Bismuth,	0.030	Brick, common,	0.200	Carbonic acid,	0.221
Tellurium,	0.091	Firebrick,	0.220		0.288
Gold,	0.029	Coal,	0.261	Olefiant gas,	0,421
Silver,	0.057	Beeswax,	0.450	Nitro-oxide,	0.237
Platinum,	0.034	Alcohol, s. g. 0.81,	0.700	Gas of oils,	0.421
	0.094		0.335	Sulp. hydrogen, .	0.242
Mercury,	0.030	Nitric acid,	0.661	Steam of atm. pr.,	0.475
	1	U	- 1	* ′	

Let two different substances of known weight or volume and temperature be mixed together; the temperature of the mixture will dissolve the relative quantity of caloric in the ingredients.

Mixture of the same Substances.

W= weight or volume of a substance of temperature T. w= weight or volume of a similar substance of temperature t. t= temperature of the mixture W+w. We shall have—

$$t'(W+w) = WT+wt, \quad 3. \qquad t' = \frac{WT+wt}{W+w}, \quad 5.$$

$$W = \frac{w(t'-t)}{T-t'},$$
 4. $T = \frac{w(t'-t)}{W} + t'.$ 6.

Example 1. Let W = 4.62 cubic feet of water at $T = 150^{\circ}$ be mixed with w = 5.43cubic feet at t = 46. Required, the temperature of the mixture t' = ?

$$t' = \frac{4.62 \times 150^{\circ} + 5.43 \times 46^{\circ}}{4.62 + 5.43} = 97.6^{\circ}$$
, the answer.

Example 2. How much water of $T=107^{\circ}$ must be mixed with w=27.3 gallon of $t = 58^{\circ}$, the mixture of the water to be 75°?

$$W = \frac{27.3(75 - 58)}{107 - 75} = 14.5$$
 gallons.

Mixture of Different Substances.

Wand w expressed by weights only. S and s = specific caloric as given in theaccompanying table. We shall have-

$$WS(T-t') = w s(t'-t), \quad 7. \quad t' = \frac{WST + wst}{WS + ws}.$$
 9.
$$T = \frac{t'(WS + ws) - wst}{WS}. \quad 8. \quad W = \frac{ws(t'-t)}{S(T-t)},$$
 10.

Example 3. To what temperature must W=20 pounds of cast iron be heated to raise w = 131 pounds of water of $t = 54^{\circ}$ to a temperature $t' = 64^{\circ}$? T = ?From the table we have s = 1, and S = 0.14.

$$T = \frac{64(20 \times 0.14 + 131) - 131 \times 1 \times 54}{20 \times 0.14} = 532^{\circ},$$

the required temperature, supposing no vapor escapes from the water.

If any chemical action takes place in the mixture, these formulas will not answer, because part of the sensible caloric may become latent, or latent caloric may be set free.

Example 4. The temperature of 5 pounds of copper is to be elevated from 60°

to 80°. How many calorics will be required?

See table for copper 0.094 (80 - 60) = 1.88 calories, the answer.

Specific Heat of Gases.

When heat is applied to a constant volume of gas enclosed in a vessel, the specific heat of that gas increases as the square root of the pressure generated by the heat.

$$S = \frac{0.9585}{\sqrt{P}}$$
. 11.

When the volume, pressure and temperature are all variable, the specific heat of air will be-

$$S = \frac{0.9585}{\sqrt{\frac{VP}{v} \left(\frac{T-t}{493} + 1\right)}}.$$
 12.

For any permanent gas of s = specific heat under atmospheric pressure, the specific heat under any other pressure and volume will be—

$$S = \frac{3.834 \,s}{\sqrt{\frac{VP}{v} \left(\frac{T-t}{493} + 1\right)}}.$$

The weight of 320 cubic reet of air at 59° is (see table) $0.076 \times 320 = 24.32$ pounds. The calorics consumed in the operation will be-

Formula 13.
$$h = 1.08 \times 24.32 (369 - 59) = 1050.625$$
 units.

The specific heat of any other gas, under different volumes, pressures and temperatures, is equal to that of air multiplied by the specific heat in the table and divided by 0.25.

The number of calories h required to elevate the temperature of W pounds of

gas from to to To, will be-

$$h = SW(T-t)$$
. 13.

When the pressure is constant, and the volume is increased by heat, and S = specific heat of the primitive volume of air, then the calorics will be—

$$h = S W(T-t) + \frac{P}{5.36} \left(\frac{V}{v} - v\right),$$
 . 14.

in which the last term expresses the calorics expended in expanding the volume

under the pressure P.

Example 6. One cubic foot of air of $t=32^{\circ}$ is enclosed in a cylinder of one square foot area of piston, and under atmospheric pressure P=14.75 pounds to the square inch. Let heat be applied to the air until $T=511^{\circ}$, when the volume will be about double, the piston being well balanced to move with the constant pressure. Required, the number of calorics imparted to the air, and the heat expected in a cylinder of the piston with the constant pressure. pended in moving the piston with the pressure 14.75 pounds.

Formula 14.
$$h = 0.25 \times 0.0807 \times (511 - 32) + \frac{14.75}{5.36} \left(\frac{2}{1} - 1\right) = 9.65 + 2.75 =$$

12.4 calories, of which 2.75 was expended in moving the piston one foot.

DYNAMICS AND UNITS OF HEAT AND WORK.

The ordinary English unit of heat is that required to elevate the temperature of one pound of distilled water one degree Fahr. from 39° to 40° (Fahr. lb.), and called one caloric.

The German unit of heat is that required to elevate the temperature of one pound (German pfund) of water one degree Centigrade, from 4° to 5° (Cent. fb.)

The French unit of heat (called calorie) is that required to elevate the temperature of one kilogramme (2.2047 lbs.) of water one degree Centigrade from 4° to 5° (Cent. kilo.).

A combination of French and English units of heat is sometimes expressed by

Fahr. scale and French weight (Fahr. kilo.).

Heat is dynamic work, or the product of the three simple elements, force, velocity and time, in which the temperature of the heat represents force, and the cubic contents of the units of heat represent the product of time and velocity, which is space.

The English unit of dynamic work is one pound raised one foot, called footpound

(Ft. 1b.). One caloric = 772 ft. 1bs.

The French unit of dynamic work is one kilogramme raised one metre, called kilomet.

One horse-power will consume or generate 2564 calorics per hour.

Comparison of Different Units of Heat and Work.

ork.
lomet.
6.51
3.066
6.52 3.66
3825
1.7 3.0 6.5 3.6

Performance. Weight and Dimensions of Heavy Ordnance.

DESCRIPTION.	Diam	length	Weigh	in Poun			
990 13 3 2 200 1 mile 2	Rore.	Gun	Gun	Proj'tile	Powd.	Velocity	Fore.
	Inches	17. in.	simus 1	Pounds.	Pounds	F.1' 3.612 186.	
American riche.	47	· +	2, 61.19				Ritle.
** ** **	6	3 6	2.620				Ritte.
gotter missifty insi.	0110	6,2 6	14.14)	130	229	1:574	Smooth.
A servan cast iron,	3	19,	3.62.5				**
8 x 335 .	10	11.	4.63271	7(1)	153	1298	44
American, "	11	11 6	16,511				93
Brestr. "	11	11 6	11/2.77	496	52.3	1862	Ni.
" desta Co	12	13,	19:27	69.63	67	1150	44
American,	13	13 5"	16,511				**
64 40	1,5	13. 8	(1) [2]				11
65 66	20	71. 3	High	378	120	1181	**
" moriar, .	13	2 10	17.198	0.00		0.3004	**
RYK BYKK MAKEN II.	(16.	2/5	6111111	1419.			66

Effect of Gunpowder.

$$V = S\sqrt{\frac{K}{W}}$$
, $W = \frac{64K}{V^2}$, and $K = \frac{WV^2}{64}$.

The length of the gun for these formulas should be at least 12 times the bore.

Force of Gunpowder.

The force of gunpowder depends much upon its quickness of burning and resistance to its expansion. Gunpowder enclosed in a strong vessel, and burned in its primitive volume, may reach a pressure of 100 tons to the square inch; but when the gas of powder is subjected to an excessive pressure, it gets cracked, as it were, and less the property of expansion due to a permanent gas less strained. This is a very important fact in the use of heavy ordinance, where the gan may be double strained with a loss of effect in the projectile.

Quick powder may strain a gun over 30 tons to the square inch, whilst slower powder will strain it only 15 tons, and give a greater velocity to the projectile.

It appears that the charge ought to be so arranged in a gun that a slow powder is first ignited, and then a quicker and quicker until the quickest at last, by which the gun need not be strained to more than 15 tons to the square inch, with full benefit of the expansion property of the gas, greater velocity of the propertie and less risk in bursting the gun. The work done by the gas of powder in a gun should be treated under the same laws as that of stemm in a steam cylinder.

This special subject is too extensive for proper treatment in this Pocket-book.

Composition of Gunpowder,

The composition of gnupowder varies in all proportions between the limits of 70 and 78 parts of saltpetre (nitrate of potash, KO, NO_N), 18 and 15 parts of charcoal, 9 and 20 parts of sulphur in 100 parts of the powder.

Chinese powder, 62 saltpetre, 28 charcoal, 15 sulphur,

The different proportions depend much upon the purpose for which the powder is used, and also upon the ideas and experience of the manufacturers and users of the powder. The quickest powder requires the highest proportions of sultpotre.

Size of Gunpowder-grains.

USE OF POWDER.	SUR OF SUNE	Size in Inches,	Companie
Sporting	No. 1 to 2.	30,0 or 20,0	44.18.10
Mortar,	No. 2 to &	0,(भी कि धरी	11,333,57
Cannon,	No. 4 to 5.	0,25 to 0.35	\$1,81.67
Mammoth,	No. 6 to 7.	(74 to (75)	74.11.13

Fine grupowder is also moulded into lumps to fit the chamber of the gun, The Enssians mould fine powder into hexagon blocks for heavy ordnance,

PROPERTIES OF WATER AND STEAM,

In Relation to Heat.

The following six pages of tables for water and steam have been calculated by the author whilst stationed in the Bureau of Steam Engineering of the United States Navy Department, under the direction of Chief Engineer Isherwood. The tables have been improved for this Pocket-book.

Properties of Water.

Column h' contains the calorics required to raise each cubic foot of distilled water from 32° to temperature T, under the pressure P.

Column h contains the calorics required to raise each pound of water from 32° to To. This column is calculated from the formula deduced from Regnault's experiments, namely:

$$h = T^{\circ} - 32^{\circ} + \frac{(T^{\circ} - 32)^n}{p'}$$
, or $h' = T - t' + \frac{(T - 32)^n - (t' - 32)^n}{p'}$. 1.

in which the last term is a parabola of exponent n = 2.67, and parameter p'1167713. log. p' = 6.0673350. h' = calorics required per pound of water of temperature t', and raised to To.

Column c contains the fractional cubic feet per pound of water of temperature T. Column w contains the weight in pounds per cubic foot of water of temperature Water of the maximum density at 39° weighs 62.388055 pounds per cubic foot.

Column v contains the volume of water of temperature T, that at 39° being unit. This column is calculated from the Formula 2, deduced from Kopp's experiments.

$$v = 1 + \frac{(T - 39)^2}{2000000 [0.23 + 0.0007 (T - 39)]}$$
. 2.

Column t contains the temperature of the steam and water, Celsius' scale. Columns i and p give the steam-pressure indicated on the safety-valve or mercury-gauge.

+ means pressure above the atmosphere. - means vacuum under the atmosphere.

Properties of Steam.

Column P contains the total stcam-pressure in pounds per square inch, in-

cluding the pressure of the atmosphere.

Column I is the same pressure in inches of mercury, The specific gravity of mercury at 32° Fahr, is 13.5959, compared with water of maximum density at 39°. One cubic inch of mercury weighs 0.49086 pounds, of which a column of 29.9218 inches is a mean balance of the atmosphere, or 14.68757 lbs. per sq. in.

Column T contains the temperature of the steam on Fahr.'s scale, deduced from

Regnault's experiments.

Column V contains the volume of steam of the corresponding temperature T, compared with that of water of maximum density at 39° Fahr. This column is calculated from the formula of Fairbairn and Tate, namely:

$$V = 25.62 + \frac{49513}{I + 0.72} \cdot \dots 3.$$

Column W contains the weight per cubic foot in fractions of a pound; and Column C the cubic feet per pound of saturated steam under the pressure P and temperature T.

Column H contains the calories per pound of steam from 32° to temperature T and pressure P, calculated from the formula—

$$H = 1081.91 + 0.305 T.$$
 . . . 4.

Column H' contains the calorics per cubic foot of steam from 32° to temperature T.

The columns H and H' give the calories required to heat the water from 32° to the boiling-point and evaporate the same to steam under the pressure P and of

temperature T.

Column L contains the latent units of heat per pound in steam of temperature T and pressure P. The latent heat expresses the work done in the evaporation, or the difference between the calories per pound in the steam and in the water of the same temperature.

Column L' contains the latent heat per cubic foot of steam.

Latent heat L = H - h, the calorics required to evaporate each pound of water from the boiling-point into steam.

The maximum work K, which can be realized per caloric in steam without

expansion, is-

$$K = \frac{144 \ P(V-1)}{H' \ V}$$
. . . 5.

Example 1. Required, the maximum work K = ? that can be realized per caloric in steam of P = 50 lbs. per sq. in.? V = 508.29 and H' = 143.3.

$$K = \frac{144 \times 50 (508.29 - 1)}{143.3 \times 508.29} = 50.14$$
 footpounds,

or, 50.14:772 = 0.0649 of the natural effect.

The maximum work which can be realized per caloric in steam with expansion will be—

$$K = \frac{144 P(V-1)(2.3 \log_{\cdot} \frac{S}{l} + 1)}{H'V}, \qquad . \qquad 6.$$

in which S = stroke of piston, and l = part of the stroke with full steam.

The natural effect of a steam-engine in horse-power is
$$=\frac{NK}{\tau 550}$$
, 7.

of which from 50 to 75 per cent. is realized in ordinary practice. N = number of

calorics passed through the engine in the time τ in seconds.

Example 2. Let the steam in Example 1 be expanded S: l=3 times. We have $\log.3=0.47712$, and $2.09737\times50.14=105.16$ footpounds per caloric. Suppose each stroke of the piston to use 4 cubic feet of steam expanded 3 times, and making 90 strokes per minute.

Then
$$\frac{90 \times 4 \times 143.3}{60} = 439.8 \text{ calorics per second,}$$

and the power will be
$$\frac{439.8 \times 105.16}{1 \times 550}$$
 = 84 horses.

This is the effect of steam when raised from water of 32° , but when the feedwater is of higher temperature, calculate the calorics from the Formula 1, h', and add the latent heat per pound of the steam; the sum will be the calorics required in generating the steam.

The late Professor Alexander, of Baltimore, gave a very simple and clear formula for temperature and pressure of steam, which may be as reliable as the experiments of Regnault, from which it differs very little, namely:

$$I = \left(\frac{T}{180} + \frac{990}{1695}\right)^6$$
, and $T = 180 \sqrt[6]{I} - 105.13$.

The inches of mercury $I \times 0.48875 =$ pressure in pounds per square inch. T = temperature of the steam, Fahr.

The pressure in atmospheres A will be—

$$A = \left(\frac{T}{317.13} + \frac{561.91}{169.5}\right)^{6}$$
, and $T = 317.13 \sqrt[6]{A} - 105.13$.

000						
Temp.	Volume	Units of	f heat.	Pounds	Cubic ft.	Temp.
Fahr.	1 at 39°	pr. lb.	pr. cub. ft.	pr. cub. ft.	pr. lb.	Celsius.
T°	v	h h	<i>h'</i>	⁻ w	- c	t
32	1.000109	0.000000000	0.00000	62.387	0.01603046	0.000
33	1.000103	1.000000867	62:383	62:383	0.01602994	0.555
34	1.000055	2.000000545	124.77	62.384	0.01602956	1.111
35	1.000035	3.00001609	187.16	62.385871	0.01602927	1.666
36	1.000020	4.00003468	249.55	62:386791	0.01602904	2.222
37	1.000020	5.00006294	311.99	62.387493	0.01602886	2.777
38	1.000003	6.00010241	374.33	62:387930	0.01602874	3.333
39	1.000000	7.00015455	436.72	62.388055	0.01602871	3.888
40	1.000002	8.00022076	499.12	62.387930	0.01602874	4.444
41	1.000009	9.00030234	561.51	62:387493	0.01602886	5.000
42	1.000019	10.00040056	623.89	62.386869	0.01602902	5.555
43	1.000034	11.00051663	686.28	62.385933	0.01602926	6.111
44	1.000053	12.00065175	748.66	62:384748	0.01602956	6.666
45	1.000077	13.00080704	811.03	62.383251	0.01602994	7.222
46	1.000104	14.00098362	873.40	62:381567	0.01603038	7.777
47	1.000136	15.001326	935.70	62:379571	0.01603088	8.333
48	1.000171	16.0014050	997.77	62.377388	0.01603146	8.888
49	1.000211	17.0016518	1060.0	62:374893	0.01603210	9.444
50	1.000254	18.0019242	1122.8	62.372212	0.01603278	10.000
51	1.000302	19.0022230	1185.1	62.369219	0.01603355	10.555
52	1.000353	20.0025493	1248.0	62.366039	0.01603437	11.111
53	1.000408	21.0029241	1310·1	62:362611	0.01603525	11.666
54	1.000468	22.0032880	1372.3	62:358871	0.01603621	12.222
55	1.000531	23.0037024	1434.3	62.354944	0.01603723	12.777
56	1.000597	24.0041479	1496.4	62:350831	0.01603828	13.333
57	1.000668	25.0046256	1558.6	62:346407	0.01603942	13.888
58	1.000740	26.0051362	1620.9	62.341921	0.01604057	14.444
59	1.000819	27.0056808	1683.2	62:337000	0.01604184	15.000
60	1.000901	28.0062600	1745.5	62.331893	0.01604316	15.555
61	1.000986	29.0068749	1807.8	62.326620	0.01604451	16.111
62	1.001075	30.0075263	1870.1	62.321059	0.01604594	16.666
63 64	1.001167 1.001262	31·0082149 32·0089416	1932·4 1994·4	62:315333 62:309420	0·01604741 0·01604894	$17.222 \\ 17.777$
65	1.001262	33.0097073	2056.6	62.303198	0.01605054	18.333
		34.010513	2118.7	62.296852	0.01605218	18.888
66 67	1.001464 1.001570	35.011359	2180.8	62.290259	0.01605388	19.444
68	1.001680	36.012246	2242.9	62.283418	0.01605564	20.000
69	1.001793	37.013175	2305.0	62.276293	0.01605748	20.555
70	1.001909	38.014148	2367.1	62.269183	0.01605921	21.111
71	1.002028	39.015164	2429.2	62.261788	0.01606122	21.666
72	1.002020	40.016224	2491.2	62.254146	0.01606318	22.222
73	1.002277	41.017330	2553.2	62.246320	0.01606521	22.777
74	1.002406	42.018482	2615.2	62.238309	0.01606728	23.333
75	1.002539	43.019680	2677.1	62.230052	0.01606941	23.888
76	1.002675	44.020926	2739.2	62.221612	0.01607158	24.444
77	1.002814	45.022220	2801.0	62.212987	0.01607382	25.000
78	1.002956	46.023563	2862.8	62.204179	0.01607610	25.555
79	1.003101	47.024956	2924.6	62:195187	0.01607841	26.111
80	1.003249	48.026398	2985.4	62.186012	0.01608078	26.666
81	1.003400	49.027893	3048.2	62.176654	0.01608321	27.222
82	1.003554	50.029438	3111.0	62:167113	0.01608567	27.777
83	1.003711	51.031039	3172.8	62:157388	0.01608820	28.333
84 85	1.003872 1.004035	52·032688 53·034394	$3234.4 \\ 3296.2$	62·147420 62·137330	0·01609077 0·01609338	28·888 29·444
86	1.004199	54.036154	3358.2	62.127182	0.01609601	30.000
87 88	1.004370 1.004542	55·037969 56·039841	3418·7 3480·4	62·116605 62·105969	0·01609875 0·01610151	30·555 31·111
89	1.004542	57.041769	3542.1	62.095152	0.01610432	31.666
90	1.004894	58.043754	3603.8	62.084214	0.01610715	32:222
}	T OO TOO T			02 001211	0 01010110 1	

,						JOHNAN TOINT.	
ĺ	Temp.	Volume	Units of	heat.	Pounds	Cubic ft.	Temp.
ı	Fahr.	1 at 39°	pr. lb.	pr. cub. ft.	pr. cub. ft.	pr. lb.	Celsius.
i	T°	$oldsymbol{v}$	h	h'	w	c	t
ı	91	1.005094	59.045797	3665.0	62.071860	0.01611036	32.777
ı	92	1.005258	60.047899	3726.6	62.061734	0.01611298	33.333
ı	93	1.005414	61.050061	3788.2	62.050252	0.01611597	33·88 8
ł	94	1.005633	62.052282	3849.8	62.038591	0.01611900	34.444
ı	95	1.005825	63.054564	3911.2	62.026749	0.01612208	35.000
Į	96	1.006019.	64.056907	3972.6	62:014787	0.01612519	35.555
Į	97	1.006216	65.059312	4033.9	62.002646	0.01612834	36·11 1
ı	98	1.006415	66.061780	4035.2	61.990386	0.01613153	36.666
	99 10 0	1.006618 1.006822	67 · 964311 68·066906	4156.5	61-977885	0.01613478	37.222
I				4217.7	61.965322	0.01613806	37.777
ı	$\begin{array}{c c} 101 \\ 102 \end{array}$	1.007030 1.007240	69.069565	4278.9	61.952528	0.01614140	38.333
ı	102	1.007553	70.072290 71.075080	4340·1 4401·3	61.939612	$\begin{bmatrix} 0.01614475 \\ 0.01614977 \end{bmatrix}$	38·888 39·444
ľ	104	1.007668	72.077937	4462.5	61.913303	0.01615161	40.000
ı	105	1.007905	73.080861	4523.0	61.898745	0.01615541	40.555
I	106	1.008106	74.083852	4585.0	61.886403	0.01615863	41.111
ı	107	1.008328	75.086912	4645.9	61.872778	0.01616220	41.666
	108	1.008554	76.090014	4706.8	61.858913	0.01616581	42.222
	109	1.008781	77.093239	4767.7	61.844994	0.01616946	42.777
	110	1.009032	78.096509	4828.6	61.829609	0.01617348	43.333
	111	1.009244	79.099846	4889.5	61.816622	0.01617677	43.888
	112	1.009479	80.103255	4950.4	61.802231	0.01618064	44.144
	113	1.009718	81.10674	5011.3	61.787602	0.01618447	45.000
	114 115	1·009956 1·010197	82·11029 83·11392	5072·2 5133·0	61.773042	0.01618829 0.01619216	45·55 5 46·11 1
					61.758305		
	116	1·010442 1·010688	84·11762 85·12140	5193·7 5254·3	61.743331 61.728302	0.01619608 0.01620003	46.666 47.222
	117 118	1.010038	86.12525	5314.9	61.713037	0.01620403	47.777
	119	1.011189	87.12918	5375.5	61.697719	0.01620806	48.333
	120	1.011442	88.13318	5436.1	61.682286	0.01621211	48.888
	121	1.011698	89.13726	5496.6	61.666678	0.01621621	49.444
	122	1.011956	90.14141	5557.1	61.650956	0.01622034	50.000
	123	1.012216	91.14565	5617.6	61.635123	0.01622451	50·55 5
	124	1.012478	92.14996	5678.1	61.619170	0.01622871 0.01623296	51.111
	125	1.012743	93.15435	5738.6	61.603047	0.01623724	51.666
	$egin{array}{c} 126 \ 127 \ \end{array}$	1·013010 1·013278	94·15882 95·16338	5798·9 5859·2	61.586810 61.580516	0.01624153	52·222 52·777
	128	1.013550	96.16801	5919.5	61.553998	0.01624590	53.333
	129	1.013823	97.17272	5979.7	61.537423	0.01625027	53.888
	130	1.014098	98.17752	6040.0	61.520735	0.01625468	54.444
	131	1.014358	99.18239	6100.2	61.504966	0.01625884	55.000
	135	1.015505	103.20274	6340.3	61.435497	0.01627724	57.222
	140	1.016962	108.23009	6639.6	61.347282	0.01630064	60.000
	145	1.018468	113·25965 118·29147	6937·9 7215· 1	61.256765	0.01632473	62·777 65·555
	150	1.020021		1	1	0.01637523	6S·333
	155	1·021619 1·023262	123·32562 128·36217	7531·2 7826·2	61.067829	0.01640156	71.111
	160 165	1.025202 1.024947	133.40119	8098.1	60.869542	0.01642857	73.888
	170	1.026672	138.44273	8412.8	60.767270	0.01645623	76.666
	175	1.028438	143.48687	8704.2	60.662047	0.01648477	79.444
	180	1.030242	148.53666	8994.9	60.556699	0.01651345	82.222
	185	1.032083	153.58316	9281.9	60.448679	0.01654296	85.000
	190	1.033960	158.63545	9571.6	60.338944	0.01657305	87.777
	195	1.035873	163.69057	9858.5	60.227513	0.01660370	90·5 55 93·333
	200	1.037819	168.74858	10318			96.111
	205	1.039798	173.80956	10428 10712	60.000168	0.01666662	98.888
	210 212	1.041809 1.042622	178·87355 180·90000	18824	59.837654	0.01679883	100.000
	م الم	1 0 120 22	100 00000		00 00,001		

ر	20								
-	1			W	ater.			Indic.	_
1	Temp.	Units	of heat.	Bulk	Weight	Volume	Temp.	Atmos. ex	cluded
ı	Fahr.	per	per	cub. ft.	lbs. pr.	wat.=1	Celsius	inches	lbs. pr.
ı	Scale.	cub. ft.	pound.	per lb.	cub. it.	at 39°	Scale.	mercury	sq. in.
ľ	T	11'	h	c	w	v	t	i	p
ı	101.36	4301	69.430	.01617	61.848	1.0071	30.83	-28.52	-14
I	126.21	5631	94.369	.01624	61.583	1.0130	41.87	-26.48	 13
I	141.67	6583	109.91	.01630	61.317	1.0174	48.74	-24.44	- 12
i	153.27	7331	121.58	.01637	61:101	1.0210	53.90	22.41	— 11
	162.51	7974	130.89	.01638	60.920	1.0241	58.00 -		 10
ļ	170.25	8421	138.69	.01644	60.762	1.0267	61.44	—18.33	— 9
	176.97	8812	145.46	.01647	60.657	1.0288	64.43	-16.29	→ 8
	182.96	9203	151.52	.01652	60.514	1.0309	67.09	-14.26	— 7
	188.36	9531	156.97	.01656	60.372	1.0333	69.49	-12.22	- 6
	193.20	9755	161.87	.01659	60.282	1.0359	71.64	-10.18	- 5
	197.60	9975	166.32	.01663	60.169	1.0369	73.60	-8.149	→ 4
	201.90	10183	170.67	.01666	60.072	1.0385	75.51	- 6.111	— 3
	205.77	10398	174.59	.01669	59.973	1.0401	77.23	4.074	$\frac{-2}{-1}$
	209.55	10613	178.42	.01672	59.896	1.0416	78.91	-2.037	_
	212.00	10824	180.9	.01674	59.838	1.0426	100.00	0.0000 0.6365	0 2105
	213.04	10883	181.95	.01675	59.814	1.0430	100.53		0.3125
	216.33	11047 11225	185.29 188.45	.01677 .01679	59.735 59.659	$1.0444 \\ 1.0457$	102.45 104.36	+2.037 + 4.074	+ 1 + 2
	219.45	$11225 \\ 11389$	191.44	.01680	59.592	1.0469		+6.111	
	222.40 225.25	11559	194.33	.01681	59.523	1.0481	105.78 107.35	+8.149	+3 $+4$
	$\frac{225.25}{227.95}$	11718	197.08	.01684	59.459	1.0492	108.86	+10.18	+ 5
	230.60	11868	199.77	.01686	53.389	1.0503	110.33	+12.22	$\begin{array}{ccc} + & 5 \\ + & 6 \end{array}$
	233.10	12012	202.40	.01688	59.329	1.0514	111.50	+14.26	+ 7
	235.49	12150	204.73	.01690	59.270	1.0524	113.05	+16.29	+ 7 + 8
	237.81	12282	207.10	.01692	59.212	1.0534	114.00	+18.33	+ 9
	240.07	12408	209.39	.01693	59.154	1.0545	115.59	+20.37	+10
	242.24	12528	211.57	.01695	59.007	1.0555	116.90	+22.41	+11
	244.32	12642	213.72	.01696	59.057	1.0564	117.95	+21.41	+12
	246.35	12750	215.78	.01697	59.006	1.0573	119.08	+26.48	+13
	248.33	12852	217.80	.01698	58.953	1.0589	120.18	+28.52	+ 14
	25.0.26	12946	219.76	.01699	58.901	1.0590	121.25	+30.55	+ 15
	252.13	13053	221.67	.01700	58.851	1.0599	122.20	+32.59	+ 16
	253.98	13157	223.55	.01701	58.803	1.0607	123.32	+ 34.63	+ 17
	255 77	13258	225.28	.01702	58.757	1.0615	124.32	+ 36.67	+18
	257.52	13336	227.16	.01703	59.713	1.0623	125.29	+38.71	+19
	259.22	13430	228.89 230.59	.01704	58.671 58.631	1.0631	126.23	+40.74	+ 20
	260.88	13520 13608	232.24	.01705 .01707	58.592	1.0639 1.0646	127.15 128.05	+42.78 + 44.82	$+21 \\ +22$
	262.50 264.09	13694	233.86	.01708	58.550	1.0654	128.05 128.94	+46.85	+23 + 23
	265.65	15778	235.45	.01709	58.517	1.0661	128.94	+40.89 $+48.89$	$+23 \\ +24$
	267.17	13860	237.00	.01710	58.481	1.0668	130.65	+50.93	$+25 \\ +25$
	268.66	13940	238.52	.01711	58.435	1.0675	131.48	+50.95	$+26 \\ +26$
	270.12	14018	240.02	.01712	58.400	1.0684	132.29	+55.00	+27
	271.55	14094	241.48	.01713	58.366	1.0688	133.05	+57.04	$+\frac{1}{2}$ S
	272.96	14168	242.92	.01714	58.332	1.0695	133.86	+59.08	$+\frac{1}{2}$
	274.33	14241	244.32	.01715	58.298	1.0701	134.63	+61.11	+30
	275.68	14314	245.70	.01716	58.26 4	1.0708	135.38	+63.15	+31
	277.01	14385	247.06	.01717	58.230	1.0714	136.12	+65.19	+ 32
	278.32	14454	248.40	.01718	58.197	1.0720	136.84	+67.23	+33
	279.62	14522	249.73	.01719	58.164	1.0726	137.56	+69.20	+34
	280.89	14592	251.03	.01720	58.131	1.0732	138.27	+71.30	+35
	282.14	14659	252.30	.01721	58.098	1.0738	138.96	+73.34	+36
	283.39	14725	253.58 25 4 .80	.01722	58,066	1.0744	139.66	+75.38	+37
	284.58 285.76	14852	256.01	.01723 .01724	58,035	1.0750	140.33	+77.41	+ 38
	286.96	14913	257.24	.01724	58.004 57.972	1.0756	140.98	+79.45	+ 39
	238.06	14973	258.38	.01726	57.941	1.0761 1.0767	141.64	+ \$1.49	+40
	259.24	15032	259.67	.01727	57.910	1.0773	$142.27 \\ 142.91$	+83.52 +85.56	$+41 \\ +42$
	290.37	15091	260.71	.01728	57.879	1.0778	143.54	+87.61	+42 + 43
	.91.48	15149	261.87	.01729	57.848	1.0783	144.15	+89.64	+ 44
	292.58	15203	262.99	.01730	57.817	1.0789	144.76	+91.67	
									10

	Water. Indic. press.										
Temp.	Units o	of heat	Bulk	Weight	Volume	Temp.					
Fahr.	per	per	cub. ft.	lbs. pr.	wat.=1	Celsius	Atmos. en	lbs. pr.			
Scale.	cub. ft.	pound.	per lb.	cub. ft.	at 39°	Scale.	mercury	sq. in.			
T	h'	h	c	w	v	t	i	-			
293.66	15265	264.10	.01731	57.786	1.0794	145.37	+93.71	+ 46			
294.73	15321	265.20	.01732	57.769	1.0799	145.96	+95.75	+ 47			
295.78	15377	266.27	.01733	57.742	1.0804	146.54	+ 97.78	+ 48			
296.82	15432	267.34	.01734	57.714	1.0809	147.12	+ 99.82	+ 49			
297.84	15485	268.39	.01735	57.687	1.0814	147.69	+ 101.8	+ 50			
238.85	15536	269.42	.01735	57.650	1.0820	148.25	+103.9	+ 51			
299.85	15588	270.45	.01736	57.633	1.0825	148.80	+105.9	+ 52			
300.84 301.81	15639 15690	271.46 272.46	.01737	57.606	1.0830	149.34	+105.0	+ 53			
302.77	15739	273.44	.01738	57.580 57.554	1.0835 1.0840	149.89 150.43	+110.0 + 112.0	+ 54 + 55			
303.72	15789	274.42	.01739	57.529	1.0844	150.45	+ 114.1	$+55 \\ +56$			
304.69	15839	275.40	.01739	57.504	1.0849	151.48	+ 116.1	+ 57			
305.60	15888	276.35	.01740	57.480	1.0854	152.00	+ 118.1	+ 58			
306.52	15936	277.30	.01741	57.456	1.0859	152.51	+120.2	+ 59			
307.42	15983	278.22	.01741	57.432	1.0863	153.01	+ 122.2	+ 60			
308.38	16029	279.14	.01742	57.410	1.0867	153.51	+124.3	+ 61			
309.22	16075	280.07	.01743	57.388	1.0871	154.01	+126.3	+ 62			
310.11	16120	280.98	.01743	57.364	1.0875	154.50	+128.3	+ 63			
310.99 311.86	16165 16209	$281.87 \\ 282.78$	$\begin{bmatrix} .01744 \\ .01745 \end{bmatrix}$	57.344 57.322	1.0880 1.0884	154.99 155.48	$+130.4 \\ +132.4$	+ 64			
312.72	16254	283.66	.01745	57.300	1.0888	155.95	+ 132.4 + 134.4	$\begin{array}{c c} + & 65 \\ + & 66 \end{array}$			
313.57	16298	284.54	.01746	57.278	1.0892	156.42	+136.5	+67			
314.42	16342	285.41	.01746	57.254	1.0897	156.90	+138.5	+ 68			
315.25	16384	286.27	.01747	57.232	1.0901	157.36	+140.5	+ 69			
316.08	16426	287.12	.01748	57.210	1.0905	157.82	+142.6	+ 70			
316.90	16467	287.96	.01748	57.188	1.0909	158.28	+ 144.6	+ 71			
317.71	16507	288.80	.01749	57.166	1.0913	158.73	+146.7	+ 72			
318.51	16547	289.62	.01750	57.144	1.0918	159.17	+148.7	+ 73			
319.31 320.10	16587 16637	290.44 291.26	0.01751 0.01752	57.122 57.101	1.0921 1.0926	159.62 160.05	$+150.7 \\ +152.8$	$\begin{array}{ c c c c c c c c c c c c c c c c c c c$			
320.88	16677	292.06	.01752	57.080	1.0929	160.49	+154.8	$\begin{array}{c} + 76 \\ + 76 \end{array}$			
321.66	16717	292.85	.01753	57.059	1.0935	160.92	+156.8	+ 77			
322.42	16756	293.65	.01753	57.038	1.0937	161.34	+158.9	+ 78			
323.18	16795	294.43	.01754	57.017	1.0941	161.76	+160.9	+ 79			
323.94	16834	295.21	.01755	56.996	1.0945	162.17	+163.0	+ 80			
324.67	16872	295.96	.01756	56.975	1.0949	162.59	+165.0	+ 81			
325.43	16910	296.75	.01756	56.954	1.0953	163.02	+167.0	+ 82			
326.17 326.90	16947	297.51	.01757	56.933	1.0956 1.0960	163.43	$+169.1 \\ +171.1$	+ 83			
327.63	16984 17020	298.26 299.01	.01757	56.912	1.0964	163.83 164.24	+171.1 + 173.1	+ 84 + 85			
328.35	17056	299.75	.01759	56.871	1.0968	164.64	+175.2	+ 86			
329.07	17092	300.50	.01759	56 862	1.0972	165.04	+177.2	+ 87			
329.78	17127	301.23	.01760	56.844	1.0975	165.43	+179.2	+ 88			
330.48	17162	301.95	.01761	56.826	1.0979	165.82	+ 181.3	+ 89			
331.18	17197	302.67	.01761	56.808	1.0982	166.21	+183.3	+ 80			
331.87	17231	303.38	.01762	56.790	1.0986	166.59	+185.4	+ 91			
332.56	17265	304.10	.01763	56.772	1.0989 1.0993	166.98 167.35	+ 187.4	+ 92			
333.24 333.92	17299 17333	304.80	.01763	56.754	1.0996	167.77	$+189.4 \\ +191.5$	+ 93 + 94			
334 59	17366	306.19	.01765	56.716	1.0999	168.10	+193.5	+ 95			
335.26	17399	306.88	.01765	56.699	1.1003	168.47	+195.5	+ 96			
336.58	17465	308.34	.01767	56.664	1.1010	169.21	+ 199.6	+ 98			
3 7.23	17497	308.91	.01768	56.647	1.1013	169 57	+201.6	+ 99			
337.89	17529	309.60	.01769	56.629	1.1017	169.94	+203.7	+100			
341.0	17688	312.87	.01772	56.549	1.1035	171.70	+213.9	+ 105			
344.1	17840	316,04	.01775	56.469	1.1050	173.40	+ 224.1	+ 110			
347.1	17993	319.12	.01778	56.389	1.1065 1.1090	175.06 176.68	$+234.2 \\ +244.4$	+115			
350.0	18136 18278	322.13 325.06	.01781	56.220	1.1095	178.25	+244.4 + 254.6	$\begin{vmatrix} +120 \\ +125 \end{vmatrix}$			
355.6	18413	327.91	.01786	56.146	1.1100		+264.8	+ 130			
358.4	18549	330.75	.01788	56.073	1.1124	181.35	+275.0	$+\frac{135}{135}$			
						Name of the last o					

1										
i					eam.					Press
Total p	ressure	Temp.	Volume	Weight	Bulk			, from 32		ob. at.
lbs. pr.		Fahr.	wat.=1		cub. ft.	Tota	d pr.		nt pr.	lbs. pr.
sq. in.	mer.	Scale.	at 39°	cub. ft.	pr. lb.	pound.	cub. ft.	pound.	cub. ft.	sq. in.
P	I	T	V	W	C	H	H	L	L'	p
1	2.037	101.36	17983	.00347	288.24	1112.8	3.8614	1043.4	3.6337	- 14
2	4.074	126.21	10353	.00602	165.94	1120.4	6.7449		6.1165	- 13
3	6.111	141.67	7283.8	.00856	116.75	1125.1	9.6308	1015.2	8.6901	- 12
4	8.149	153.27	5608.4	.01112	89.895	1128.7	12.551	1007.1	11.199	-11
5	10.18	162.51	4565.6	.01366	73.180	1131.5	15.456		13.714	10
6	12.22	170.25	3851.0		61.742	1133.8	18.156		16.113	— 9
7	14.26	176.97	3330.8		53.388	1135.9	20.846		18.194	8
8	16.29	182.96	2935.1		47.046	1137.7	24.176		20.957	- 7
9	18.33	188.36	2624.0	.02377	42.059	1139.4	27.083		23.352	- 6
10	20.37	193.20	2373.0	.02628	38.037	1140.8	29.980	978.99	25.728	5
11	22.41	197.60	2166.3	.02880	34.723	1142.2	32.895	975.88	28.099	- 4
12	24.44	201.90	1993.0		31.945	1143.5	35.791		30.450	— 3
13	26.48	205.77	1845.7	.03380	29.584	1144.7	38.691	970.11	32.789	- 2
14	28.52	209.55	1718.9	.03629	27.551	1145.8	41.581	967.43	35.435	- 1
14.7	29.92	212.00	1641.5		26.311	1146.6	43.571	965.70	36.706	0 2105
15 16	30.55	213.04	1608.6 1511.7	.03878	25.784 24.230	1146.9	44.476	964.96 962.63	37.421	0.3125
17	32.59 34.63	216.33 219.45	1426.2	.04123	22.859	1147.9	50.248	960.49	39.690	$+ 1 \\ + 2$
18	36.67	222.40	1349.8	.01622	21.636	1149.7	53.138	958.32	$\begin{vmatrix} 42.012 \\ 44.393 \end{vmatrix}$	
19	38.71	225.25	1281.1	.04868	20.539	1150.6	56.011	958,30	46.698	+ 3 + 4
20	40.74	227.95	1219.7	.05119	19.550	1151.4	58.894	954.38	48.655	+ 5
21	42.78	230.60	1163.8	.05363	18.654		61.758	952.50	51.924	$\begin{array}{cccc} + & 6 \\ + & 6 \end{array}$
$\frac{1}{22}$	44.82	233.10	1112.9	.05605	17.838	1153.0	64.637	950.62	53.282	+ 7
23	46.85	235.49	1066.3	.05851	17.092	1153.7	67.503	949.03	55.529	+ 8
24	48.89	237.81	1023.6	.06095	16.407	1154.5	70.367	947.37	57.743	+ 9
25	50.93	240.07	984.23	.06338	15.776	1155.1	73.410	945.76	59.942	+10
26	52.97	242.24	947.86	.06582	15.193	1155.8	76.074	944.25	62.161	+11
27	55.00	244.32	914.14	.06824	14.652	1156.4	78.913	942.74	64.423	+12
28	57.04	246.35	882.80	.07067	14.150	1157.1	81.772	941.29	66.521	<u>+</u> 13
29	59.08	248.33	853.60	.07308	13.682	1157.7	84.604	939.88	68.686	+14
30	61.11	250.26	826.32	.07550	13.245	1158.2	87.444	938.50	70.857	+ 15
31	63.15	252.13	800.79	.07791	12.835	1158.8	90.166	937.17	73.015	+16
32	65.19	253.98	766.83	.08031	12.451	1159.4	93.121	935.45	75.126	+ 17
33	67.23	255.77	754.31	.08271	12.090	1159.9	95.861	934.57	77.298	+18
34	69.26	257.52	733.09	.08510	11.750	1160.5	98.782	933.32	79.425	+ 19
35	71.30 73.34	259.22 260.88	713.08	.08749	11.429	1161.0	101.48	932.10	81.549	+ 20
37	75.38	262.50	694.17 676.27	.09225	11.127 10.840	1161.5	104.38	930.92	83.662	+ 21
38	77.41	264.09	659.31	.09462	10.568	1162.0 1162.5	107.19 109.98	$ \begin{array}{c c} 929.76 \\ 928.62 \end{array} $	85.770	+ 22
39	79.45	265.65	643.21	.09700	10.310	1162.9	112.79	C	87.866	+ 23
40	81.49	267.17	627.91	.09936	10.064	1163.4	115.59	$927.51 \\ 926.42$	\$9.968 92.059	+24
41	83.52	268.66	613.34			1163.9	118.39	925.35	94.126	$+25 \\ +26$
42	85.56	270.12	599.46	.10407	9.6086	1164.3	121.17	924.30	96.192	+20 + 27
43	87.60	271.55	586.23	.10642	9.3963	1164.7	123.95	923.28	98.255	$\frac{7}{+}\frac{21}{28}$
41	89.64	272.96	5 73.58	.10877	9.1938	1165.2	126.74	922.27	100.32	+29
45	91.67	274,33	561.50	.11111		1165.6	129.51	921.29	102.36	+30
46	93.71	275.68	549.94	.11344	8.8149	1165.0	132.29	920.32	104.40	+31
47	95.75	277.01	538.87	.11577			135.07	919.36	106.43	+32
48	97.78	278.32	528.25	.11810			137.83	918.43	108.46	+33
49	99.82	279.62	518.07	.12042		1167.2	140.69	917.49	110.48	+34
50	101.86	280.89	508.29	.12273	8.1472	1167.6	143.30	916.58	112.49	+35
51	103.90	282.14	498.89	.12505	7.9966		146.03	915.68	114.50	+36
52 53	105.93	283.39	489.85	.12736	7.8517	1168.4	148.85	914.79	116.51	+37
54	107.97 110.01	284.58 285.76	481.15 472.77	.12966 .13196	7.7122		151.63	913.93	118.50	+38
55	112.04	286.96	464.69	.13428	7.5779 7.1468		154.48	913.08	120.49	+ 39
55	114.08	238.09	456.90		7.3236		157.02 159.74	912,22	122.47	+40
57	116.12	289.24	430.30	.13883	7.2030		162.45	911.42 910.48	124.43	+41
58	118.16	290.37		.14111		1170.5	165.15	909.78	126.40 128.38	+42 + 43
59		291.48	435.10	.14338	6.9741		167.84	908.97	130.33	+44
60		292.58	428.32		6.8654		170.58	908.18	132.28	+45
										1 20

	Steam. P									*0.
Matal -		Manan	137 - 1		0	Press				
lbs. pr.	ressure inches	Temp. Fahr.	Volume wat.=1	Weight	Bulk cub. ft.	Units	of heat,	from 32		ob. at.
sq. in.	mer.	Scale.	at 39°	lbs. pr. cub. ft.	pr. lb.	pound.	l pr.	pound.	it pr.	lbs. pr. sq. in.
P	I	T	V	10	C	H H	H'	L pound.	L'	
61	124.27	293.66	421.75	.14792	6.7601	1171.5	173.27	907.40	134.22	+ 46
62	126.30	294.73	415.40	.15018	6.6583	1171.8	175.96	906.63	136.16	+ 47
63	128.34	295.78	409.25	.15244	6.5597	1172.1	178.65	905.87	138.09	+ 48
61	130.38	2∂6.82	403.29	.15469	6.4642	1172.5	181.34	905.13	140.01	+ 49
65	132.42	297.84	397.51	.15694	6.3715	1172.8	184.03	904.39	141.93	+ 50
66	134.45	238.85 299.85	391.90 386.47	.15919	6.2817 6.1994	1173.1 1173.4	186.72	903.66	143.85	+ 51
68	138.53	300.84	381.18	.16366	6.1099	1173.4	189.40 192.97	902.94 902.23	145.64 147.66	+52 + 53
69	140.36	301.81	376.06		6.0277	1174.0	194.74	901.53	149.56	+ 54
70	142.60	302.77	371.07	.16812	5.9478	1174.3	197.42	900 84	151.45	+ 55
71	144.64	303.72	366.24		5.8702	1174.6	200.08	900.15	153.34	+ 56
72	146.68	304.69	361.53		5.7948	1174.9	202.74	899.46	155.21	+ 57
73	148.72	305.60	356.95	.17478	5.7214	1175.1	205.40	898.79	157.09	+ 58
74 75	150.75 152.79	306.52 307.42	352,49 348.15	.17690 .17919	5.6500 5.5805	1175.4 1175.8	208.04 210.67	893.13 897.57	158.88 160.83	$+59 \\ +60$
76	154.83	308.32	343.93		5.5129	1176.0	213.30	896.83	162.67	$\begin{array}{cccc} + & 60 \\ + & 61 \end{array}$
77	156.86	309.22	339.81	.18359	5.4468	1176.2	215.93	896.18	164.56	+62
78	158.90	310.11	335 80	.18578	5.3825	1176.5	218.56	895.54	166.37	+ 63
79	160.94	310.99	331.89	.18797	5.3190	1176.8	221.19	894.92	168.22	+ 64
80	162.98	311.86	328.08	.19015	5.2588	1177.0	223.82	894.27	170.04	+ 65
81	165.01	312.72 313.57	324.37	.19233	5.1992	1177.3	226.44	895.65	171.87	+ 66
82 83	167.05 169.09	314.42	320.74 317.20	.19451	5.1410 5.0843	1177.6 1177.9	229.06 231.68	893.03 892.51	173.70 175.52	+ 67 + 68
84	171.12	315.25	313.74	.19885	5.0289	1178.1	234.28	891.82	177.33	+ 69
85		316.08	310.36	.20101	4.9748	1178.3	236.89	891.22	179.14	+ 70
86	175.20	316.90	307.07	.20317	4.9219	1178.6	239.50	890.63	180.95	+ 71
87	177.24	317.71	303.85	.20532	4.8703	1178.8	242.10	890.04	182.75	+ 72
88	179.27	318.51	300.70	.20747	4.8198	1179.1	244.69	889.46	184.53	+ 73
89	181.31	319.31	297.62	.20962	4.7704	1179.3	247.29	888.88	186.33	+ 74
90 91	183.35 185.38	320.10 320.88	294.61 291.66	.21185 .21390	4.7222 4.6750	1179.6 1179.8	249.88 252.45	888.31 887.74	188.12 189.88	+75 + 76
92	187.42	321.66	288.78	.21603	4.6288	1180.0	255.02	887.19	191.66	+ 77
93	189.46	322.42	285.96	.21816	4.5836	1180.3	257.58	886.63	193.43	+ 78
94	191.50	323.18	283.21	.22029	4.5394	1180.5	260.14	886.08	195.19	+ 79
95	193.53	323.94	280.50	.22241	4.4961	1180.7	262.69	885.53	196.94	+ 80
96	195.57	324.67	277.86	.22453	4.4537	1180.9	265.23	885.00	198.71	+ 81
97	197.61	325.43 326.17	275.27 272.73	.22672	4.4106	1181.2	267.77	884.45	200 49 202.18	$\begin{array}{ c c c c c } + & 82 \\ + & 83 \\ \end{array}$
98	199.65 201.68	326.90	270.24	.23085	4.3715 4.3316	1181.4 1181.6	270.30	883.91 883.38	203.92	+ 83 + 84
100	203.72	327.63	267.80	.23296	4.2926	1181.9	275.52	882.85	205.67	+ 85
101	205.76	328.35	265.41	.23505	4.2543	1182.1	277.85		207 39	+ 86
102	207.79	329.07	263.07	.23715	4.2167	1182.3	280.38	881.81	209,12	+ 87
103	209.83	329.78	260.77		4.1799	1182.5	282.90	881.29	210 84	+ 88
104	211.87	330.48	258.52		4.1438	1182.7	285.42 287.93	880.78	212.55	+ 89 + 90
105 106	213.91 215.94	331.18 331.87	256.31 251.14		4.1083 4.0736	1182.9 1183.2.	287.93	880.27 879.77	214.26 215.96	+ 90 + 91
107	217.98	332.56		.24750	4.0394	1183.4	292.94	879.27	217.66	$\begin{array}{c c} $
108	220.02	333.24	249.92		4.0058	1183.6	295.41	879.79	219.36	+ 93
109	222.05	333.92	247.87		3.9731	1183.8	297.91	878.28	221.05	+ 94
110	224.10	334.59	245.86		3.9408	1183.9	300.44	877.80	222.74	+ 95
111	226.13	335.26		.25581	3.9091	1184.2	302.93	877.31	224.42	+ 96
113	230.20	336.58	240.03		3.8474	1184.6	307.90	876.25	227.74	+ 98
114 115	232.24° 234.28	337.23 337.89	238.15	.26204	3.8100 3.7578	1184.8 1185.0	$310.36 \\ 312.86$	875.88 875.40	229.51 231.10	+99 + 100
120	244.4	341.0	227.56		3.6475	1185.9	325.20	873.09	239.41	+ 105
125	254.6	344.1	219.50		3.5184		337.39	870.85	247.51	+110
130	264.8	347.1	212.07		3.3991	1187.8	349.44	868.68	255.55	+115
135	275.0	350.0	205.18	.30406	3.2880	1188.7	361.42	866.56	263.48	+120
140	285.2	352.8		.31385	3.1862	1189.5		864.49	271.32	+125
145	295.4	355.6		.32354		1190.4		862.48	278.97	
150	305.6	358.4	187.20	.33315	3.0001	1191.2	390.86	860.45	286.66	+ 135

EXPANSION OF STEAM.

In order to save steam, or more correctly to employ its effect to a higher degree, the admittance of steam to the cylinder is shut off when the piston has moved a part of the stroke; from the cut-off point the steam acts expansively with a decreased pressure on the piston, as represented by the accompanying figure.



Let the steam be cut off at \frac{1}{2} of the stroke, and Aa represent the total pressure, say 20 pounds per square inch which will continue to the point E where the admittance of steam is shut off at one-third the stroke S. The steam Aa eE, is now acting expansively on the piston, and the pressure decreases as the volume increases, when the piston has attained Cc or two-thirds of S, the pressure C'c=10 pounds, only half the pressure Aa=20 because the volume $Aa\ eE$ is only half of Aa cC, and so on until the piston has attained B b the pressure $B'b = \frac{1}{3} \times 20 = 6.66$ pounds.

The mean pressure, or the effectual pressure, throughout the stroke, will be about 13.33 pounds per square inch, or 66 per cent., but the quantity b of steam used is only 33 per cent., hence 33 per cent. is gained by using the steam expansively.

l = part of the stroke S in feet, at which the steam is cut off.

P=pressure per square inch under full admittance of steam. F = mean pressure per square inch throughout the stroke S.

f = mean pressure per square inch during the expansion, which in double expansion cylinder engines will be the average pressure per square inch on the large piston A.

p = end pressure per square inch after expansion.

S = stroke of the cylinder Piston in feet.

$$F' = \frac{Pl}{S} \left[2.3 (\log S - \log l) + 1 \right]$$
 $f = \frac{FS - Pl}{S - l}$, $p = \frac{Pl}{S}$

The following Tables are calculated from these formulas.

Example 1. Required from the Table I. the mean pressure F for P=32lbs. at five-eights expansion.

Add { For 30 lbs. $F=22\cdot252$ $F=1\cdot483$ from the Table I.

Mean pressure of 32 lbs. F=23.735 the answer.

Example 2. Required from Table II. the mean pressure f, per square inch during the expansion, or on the large piston A in double cylinder engines, when the initial pressure P=75 lbs. and under two-thirds expansion? f=40.75 Table II. Example 3. Required the

Required the mean pressure f=? for an initial pressure

P=43 lbs. under 3/4 expansion?

For
$$P = 40$$
 lbs. $f = 18.48$
 $P = 30$ or 3 lbs. $f = 1.38$ Table II.

P=43 lbs. f=19.86 the answer.

The effect gained or fuel saved by expansion and high steam is calculated from the following formulæ, in which it is supposed as a unit the work of an engine with P=30 pounds per square inch, or an indicated pressure of 15 lbs. without expansion. c= per cent on 100 and c=

c = per cent on 100, of effect gained or fuel saved.

For expansion
$$c = 100 (1 - \frac{lP}{SF})$$
. For high steam $c = 100 (1 - \frac{26490}{VP})$.

The following Table III. is calculated from these formulæ, in which the first line from 30 contains the economy per cent. from expansion alone, and the column o contains the economy per cent. from high steam above P=30 lbs. The balance of the table contains the jointed economy of expansion and high steam. Required the jointed economy of P=90bs. under \(\frac{1}{2} \) expansion? 50.5 per cent. the answer.

			Grade	e of Ex	pansion	•		
Press.	1	1 3	3 8	$\frac{1}{2}$	5 8	2 3	3 4	7 8
1	0.9637	0.9333	0.9187	0.8465	1 0.7417	0.6991	0.5965	0 3848
\hat{z}	1.9275			1.6930	1.4835	1.3982		
2 3	2.8912	2.7999		2.5395	2.2252	2.0873	1.7895	
4	3.8550	3.7333		3.3860	2.9670	2.7964	2.3860	
5	4.8185	4.6666	4.5935	4.2325	3.7085	3.4955	2.9825	1.9240
6	5.7822			5.0790	4.4502	4.1946	3.5790	2.2008
7	6.7469	i		5.9255	5.2419	4.8937	4.1755	2.6946
8	7.7106	4		6.7720	5.9346	5.5928	4.7720	3.0784
9	8.6733		1 -	7.6185	6.6753	6.2919	5.3685	3.4632
10 11	9.6370	1		8.4656	7.4170	6.9912	5.9650	3.8480
12	10.601			9.3115	8.1597	7.7001	6.5615	4.2333
13	11.565 12.528	1		10.158	8.9014	3.3892	7.1580	4.6186
14	13.492	1		11.004	9.6421	9·0783 9·7874	7·7545 8·5310	5.0034
15	13.492	1		11.851 12.698	11.126	10.486	8.9475	5.7730
16	15.420		1	13.544	11.268	11.185	9.5440	6.1582
17	16.383			14.390	12.609		10.140	6.5426
18	17.347			15.237	13.531	12.483	10.737	6.9274
19	18.311			16 803	14.093	13.183	11.333	7.3122
20	19.275	18.666		16.930	14.835	13.902	11.930	7.6970
21	20.238	19.599	19.293	17.776	15.576	14.501	12.526	8.0818
22	21.201			18.623	16.318	15.300	13.123	8.4667
23	22.166			19.469	17.060	15.989	13.720	8.8516
24	23.030		22.050	20:316	17.802	16.698	14.316	9.4365
25	24.093			21.162	18.573	17.477	14.912	9.6210
26	25.057	24.266	23.887	22.009	19.285	18.046	15.509	9.8978
28	26.985	26.233	25.714	23.702	20.769	19.495	16.702	10.775
30 35	28·912 33·731	27.999	27.562	25.395	22.252	20.873	17.895	11.546
40	38.550	32.666 37.333	32·156 36·750	29·627 33·860	$\begin{vmatrix} 25.961 \\ 29.670 \end{vmatrix}$	24·368 27·964	20·877 23·860	13·470 15·395
45	43.368	42.000	41.341	38.092	33.378	31.459	26.842	17.319
50	48.187	46.666	45.937	42.325	37.067	34.955	29.825	19.243
55	53.005	51.333	50.530	46.557	40.775	38.450	32.807	21.167
60	57.822	55.999		50.790	44.520	41.946	35.790	23.090
65	62.640	60.666	59.715	55.022	48.228	45.441	38.772	24.924
70	67.460	65.333	64.300	59.255	52.419	48.937	41.755	26.694
75	72.278	69.999	68.893	63.487	56.127	52.432	44.737	28.626
80	77.096		73.500	67.720	59.340	55.928	47.720	30.790
85	81.914	80.333	78.093	71.952	63.048	59.423	50.702	32.714
90	86.730	83.999	82.680	76.180	66.750	62.919	53.680	34.638
95	91.548	88.666	87·273 91·870	80.412	70.458	66.414	56.662	36.554
100 105		93.333	96.463	88.882	74.170	73.405	59.650 62.632	38·480 40·404
110	101.18	101.66	101.05	93.120	81.586	76.900	66.614	40.404
115			105.64	97.352	85.294	80-395	69.596	44.252
125			114.83	105.81	102.83	87.387	74.562	48.101
140	134.92		128.62	118.51	103 84	97.874	85.310	53.882
150		139.33		126.47	111.26	104.86	89.470	57.730
200		186.66		169.30	148.35	139.02	119.30	76.970
250		233.33	229.68	211.62	185.43	174.77	149.12	96.210
300	289.12	279.99	275.62	253.95	222.52	208.73	178.95	115.46

	N	Iean	Pressur	e f duri	ng the I	Expansi	on.	
Pres. P.	1 1	$\frac{1}{3}$	3/8	$\frac{1}{2}$	5/8	$\frac{2}{3}$	34	8
-30	28.549	24	23.50	20.79	17.60	16.31	13.86	8.9097
35	33.308	28	27.41	24.25	20.54	19.02	16.17	10.394
40	38.066	32	31.83	27.72	23.47	21.73	18.48	11.879
45	42.824	36	35.25	31.18	26.40	24.46	20.79	13.364
50	47.582	40	39.16	34.65	29.33	27.16	23.10	14.849
55	52.340	44	43.08	38.11	32.24	30.17	25.41	16.334
60	57.098	48	47.00	41.58	35.20	32.62	27.72	17.819
65	61.853	52	50.91	45.04	38.14	35.33	30.03	19.303
70	66.616	56	54.83	48.51	41.07	38.04	32.34	20.788
75	71.371	60	58.75	51.90	44.00	40.75	34.65	22.263
80	76.128	64	62.66	55.44	46.94	43.47	36.96	23.758
85	80.885	68	66.18	58.90	49.87	46.19	39.27	25.243
90	86.448	72	70.50	62.37	52.80	48.93	41.58	26.729
95	90.391	76	74.41	65.73	55.73	51.62	43.89	28.213
100	95.160	80	78.33	69.30	58.66	54.33	46.20	29.699
105	99.910	84	82.24	72.76	61.57	57.33	48.51	31.183
110	104.68	88	86.16	76.23	64.48	60.35	50.82	32.669
115	109.40	92	90.08	79.69	67.44	62.79	53.13	34.153
125	118.95	100	97.91	97.02	73.34	67.95	57.75	37.122
140	133.23	112	109.6	97.02	82.14	76.08	64.68	41.576
150	142.74	120	117.5	103.9	88.00	81.50	69.30	44.548
200	190.32	160	156.6	138.6	117.3	108.6	92.40	59.398
250	237.07	200	195.7	173.2	146.6	135.8	115.5	74.247
300	288.16	240	235.0	207.9	176.0	163.1	138.6	89.097

Table III. Economy of Expansion and high Steam. Fuel saved or effect gained per cent.

Pres.	0	4	1/3	3/8	$\left \begin{array}{c} \frac{1}{2} \end{array}\right $	<u>5</u> 8	<u>2</u>	$\frac{3}{4}$	78	
30	0	12	29.5	32	41	49.3	52	58	67.5	
35	1.6	13.6	31	33.6	42.6	51	53.6	59.6	69.1	
40	2.5	14.5	32	34.5	43.5	51.8	54.5	60.5	70	
45	3.4	15.4	33	35.4	44.4	52.7	55.4	61.4	71	
50	4.3	16.3	33.8	36.3	45.3	53.6	56.3	62.3	71.8	
55	5.2	17.2	34.7	37.2	46.2	54.5	57.2	63.2	72.7	
60	6	18	35.7	38	47.	55.3	58	64	73.5	
65	6.7	18.7	36.2	38.7	47.7	56	58.7	64.7	74.2	
70	7.3	19.3	36.8	39.3	48.3	56.6	59.3	65.3	74.8	
75	7.8	19.8	37.3	39.8	48.8	57.1	59.8	65.8	75.3	
80	8.5	20.5	38	40.5	49.5	57.8	60.5	66.5	76	
85	9	21	38.5	41	50	58.3	61	67	76.5	
90	9.5	21.5	39	41.5	50.5	58.8	61.5	67.5	77	
95	10	22	39.5	42	51	59.3	62	68	77.5	
100	10.4	22.4	40	42.4	51.4	59.7	62.4	68.4	78	
105	10.7	22.7	40.2	42.7	51.7	60.	62.7	68.7	78.2	
115	11	23	40.5	43	52	60.3	63	69	78.5	
125	11.7	23.7	41.2	43.7	52.7	61	63.7	69.7	79.2	
150	14	26	43.5	46	55	63.3	66	72	81.5	
200	16	28	45.5	48	57	65.3	68	74	83.5	
250	17.7	29.7	46.2	49.7	58.7	67	69.7	75.7	85.2	
300	19	31	48.5	51	60	68.3	71	77	86.5	
	1		1		i			!		

				Fable T					
Consumption	of	Coal	in	pounds	per	horse	power	per	hour.
		~		0.10			_		

1	consumption of coal in pounds per norse power per nour,											
1	_			G	trade of	i Expai	asion.					
	Pres.	0	1	$\frac{1}{3}$	1. 3	$\frac{1}{2}$	58	$\frac{2}{3}$	$\frac{3}{4}$	7 8		
-	P.	_	~		· ·		-		<u>*</u>	8		
1	lbs,	lbs,	lbs,	lbs,	lbs,	lbs,	lbs,	lbs,	lbs,	lbs,		
1	30	5.6	4.93	3.95	3.81	3.30	2.84	2.69	2.35	1.82		
1	35	5.21	4.84	3.86	3 72	3.21	2.74	2.60	2.26	1.73		
	4.0	5.46	4.79	3.81	3.67	3.16	2.70	2.55	2.21	1.68		
1	45	5.41	4.73	3.75	3.62	3.11	2.65	2.50	2.16	1.62		
1	50	5.36	4.68	3.71	3.57	3.06	2.60	2.45	2.11	1.58		
	55	5.31	4.63	3.66	3.51	3.01	2.55	2.40	2.06	1.53		
	60	5.26	4.59	3.60	3.47	2.97	2.50	2.35	2.02	1.49		
ı	65	5.20	4.55	3.57	3.43	2.93	2.46	2.31	1.98	1.45		
ł	70	5.19	4.52	3.54	3.40	2.90	2.43	2.28	1.94	1.41		
	75	5.16	4.49	3.51	3.37	2.87	2.40	2.25	1.91	1.39		
١	80	5.12	4.45	3.47	3.33	2.83	2.36	2.21	1.88	1.35		
	85	5.09	4.42	1		1		1				
1	1			3.44	3.30	2.80	2.33	2.18	1.85	1.32		
	90	5.07	4.39	3.41	3.28	2.77	2.31	2.16	1.82	1.29		
1	95	5.04	4.37	3.39	3.25	2.74	2.28	2.13	1.79	1.26		
ı	100	5.01	4.34	3.36	3.23	2.72	2.26	2.10	1.77	1.23		
	105	5.00	4.32	3.35	3.21	2.70	2.24	2.09	1.75	1.22		
ĺ	115	4.98	4.31	3.33	3.19	2.69	2.22	2.07	1.73	1.20		
-	125	4.94	4.27	3.29	3.15	2.65	2.19	2.03	1.70	1.17		
ı	150	4.81	4.14	3.16	3.02	2.52	2.05	1.90	1.57	1.04		
	200	4.70	4.03	3.05	2.91	2 41	1.94	1.79	1.46	0.92		
-	250	4.60	3.93	3.01	2.81	2.31	1.85	1.70	1.36	0.83		
	300	4.54	3.87	2.89	2.75	2.24	1.78	1.62	1.29	0.75		
	000	201	00.		_ , ,							

Table V.

Consumption of Coal in tons per 100 horses in 24 hours.

	Cons	umpuo	H 01 C0	ai in to	tons per 100 norses in 24 nours.						
Pres.	0	14	1 3	38	$\frac{1}{2}$	5 8	$\frac{2}{3}$	34	1 3		
P.			!			· · · · · · · · · · · · · · · · · · ·					
lbs.		tons,	tons,	tons,	tons,	tons,	tons,	tons,	tons,		
30	6.00	5.29	4.23	4.09	3.54	3.04	2.88	2.52	1.95		
35	5.90	5.19	4.13	3.99	3.44	2.94	2.79	2.42	1.86		
40	5.85	5.13	4.08	3.93	3.39	2.90	2.73	2 37	1.80		
45	5.80	5.07	4.02	3.88	3.34	2.84	2.68	2.31	1.73		
50	5.75	5 01	3.97	3.83	3.28	2.79	2.63	2.26	1.69		
55	5.70	4.96	3.92	3.77	3.22	2.73	2.57	2.21	1.64		
60	5.64	4.92	3.87	3.72	3.18	2.68	2.52	2.17	1.60		
65	5.28	4.88	3.82	3.68	3.14	2.63	2.48	2.12	1.55		
70	5.56	4.84	3.79	3.64	3.11	2.60	2.44	2.08	1.51		
75	5.53	4.81	3.76	3.61	3.07	2.57	2.41	2.05	1.49		
80	5.49	4.77	3.72	3.57	3.03	2.53	2.37	2.01	1.44		
85	5.46	4.74	3.69	3.54	3.00	2.50	2.33	1.98	1.41		
90	5.43	4.70	3.66	3.51	3.97	2.47	2.31	1.95	1.38		
95	5.40	4.68	3.63	3.48	2.94	2.44	2.28	1.92	1.35		
100	5.37	4.65	3.60	3.46	2.91	2.42	2.26	1.90	1.32		
105	5.36	4.63	3.59	3.44	2.89	2.40	2.24	1.88	1.31		
115	5.34	4.61	3.57	3.42	2.88	2-38	2.22	1.85	1.29		
125	5.30	4.58	3.53	3.38	2.84	2.34	2.18	1.82	1.25		
150	5.16	4.44	3.39	3.34	2.81	2.30	2.04	1.68	1.11		
200	5.04	4.32	3.27	3.12	2.59	2.19	1.92	1.56	0.99		
250	4.93	4.21	3.22	3.01	2.47	2.09	1.82	1.46	0.89		
300	4.87	4.15	3.10	2 95	2.40	2.01	1.74	1.38	0.83		
1 300	1 01	1 10									

Force or Feed Pumps.

Letters denote,

d = diameter of the force-pump, single acting.

D = diameter of the steam-cylinder piston, in inches, double acting,

V = volume of steam given in the table at the given pressure.

The stroke of the steam-piston is only that under which steam is fully admitted to the cylinder.

$$d = 2D\sqrt{\frac{S}{Vs}},$$
 $s = 4\frac{D^2 S}{Vd^2},$. . . 4, 5.

Slip-water included in the formulas,

Example. Required, the diameter of a force-pump having the same stroke as the cylinder piston s = 38 inches, diameter of cylinder D = 30 inches. The steam is cut off at $\frac{1}{2}$ the stroke, and the steam pressure + 50 pounds per square inch. Here V = 437, and S = 19 inches, because steam is cut off at $\frac{1}{2}$ the stroke.

$$d = 2 \times 30 \sqrt{\frac{19}{437 \times 38}} = 2.03$$
 inches.

To find the Quantity of Condensing Water.

q= condensing water of temp. t in cubic feet. $q=\frac{1.4\,Q(990+T-t')}{V(t'-t)}$, 6. t' =temperature in the condenser.

Dimensions of the Air-Pump.

Assume $t' = 100^{\circ}$, and $t = 50^{\circ}$, we shall have—

Double acting air-pumps. Single acting air-pumps. 10.

$$d = 0.326D\sqrt{\frac{S(940 + T)}{Vs}},$$

$$s = 0.106D^2 \frac{S(940 + T)}{Vd^2},$$

$$s = 0.053D^2 \frac{S(940 + T)}{Vd^2},$$
10.

Example. A single acting air-pump is to be constructed for an engine D=38 inches, S=45 inches stroke of the cylinder; the stroke of the air-pump can be 32 inches, and the exhaust steam is 261°. Required, the diameter of the air-pump? V=767.

$$d = 0.326 \times 38 \sqrt{\frac{45(940 + 261)}{767 \times 32}} = 18.25$$
 inches.

Slip-water included. T and V must be taken for the exhaust steam, as the steam may have worked expansively; the area of the foot valve must be calculated from the following formulas.

Foot Valve in the Air-Pump.

To enable an air-pump to work well and with the greatest advantage, it is necessary to pay particular attention to the following formulas. The force by which the water is driven from the condenser through the foot valve into the air-pump is limited by the pressure in the condenser; this pressure is the vacuum subtracted from 14.7 pounds; it is noted in the third column, where the temperature in the condenser is opposite, in the first column. Every pound of this pressure per square inch balances a column of water 27 inches high, which is the head that presses the water from the condenser.

Foot-Valves in Air-Pumps.

 $\mathfrak{A} = \text{area of the air-pump piston.} \qquad \mathfrak{a} = \text{area of the foot-valve, or bucket-valve.} \qquad \mathfrak{a} = \frac{D^2 S n (890 + T)}{23000 m V \sqrt{\mathfrak{p}}}$

 $\mathbf{m} = \text{diameter of the air-pump-piston.}$ m = 0.6 to 0.8

n = diameter of the foot-valve, when round.

≅ = stroke of air-pump piston, in feet.

3 = pressure in the condenser at the temperature T.

n = number of strokes of the air-pump piston per minute.

$$\mathfrak{a} = \frac{\mathfrak{A} \leq n}{100\sqrt{\mathfrak{P}}}, \qquad 12, \qquad \mathfrak{d} = \frac{\mathfrak{P}\sqrt{\leq n}}{10\sqrt[4]{\mathfrak{P}}}, \qquad 15,$$

$$\mathfrak{S} = \frac{100\pi\sqrt{3}}{n\,\mathfrak{A}}, \qquad 13, \qquad \mathfrak{S} = \frac{100\mathfrak{d}^2\sqrt{3}}{n\,\mathfrak{D}^2}, \qquad 16,$$

$$n = \frac{100\pi\sqrt{3}}{3}, \qquad 14, \qquad n = \frac{100\pi^2\sqrt{3}}{10^2}, \qquad 17.$$

Example. The area \mathfrak{A} of an air-pump-piston is 2.35 square feet, stroke of piston $\mathfrak{A} = 3.6$ feet, to make n = 40 strokes per minute, and the pressure to be $\mathfrak{P} = 3.2$ pounds. Required the area of the foot-valve.

$$\mathfrak{A} = \frac{2.35 \times 3.6 \times 40}{100 \sqrt{3.2}} = 1.85 \text{ square feet.}$$

To Find the Velocity and Quantity of the Injection Water through the Adjustage into the Condenser.

Letters denote.

v =velocity in feet per second.

h = head of the press water; + when above, and — below the adjustage.

F= vacuum, noted — or negative in the last column, but is positive in the formulas.

q = quantity of water discharged in cubic feet, per second. a = area of all the holes in the adjustage in square feet.

 $d = ext{diameter}$ of the injection pipe, in feet.

n = double strokes of cylinder-piston, or revolutions per minute.

A, D, and S, dimensions of the steam cylinder, in feet.

T = temperature, and v = volume coefficient of the exhaust steam.

$$a = \frac{q}{5\sqrt{2F \pm h}},$$
 18, $q = 5a \sqrt{2F \pm h},$ 21

$$v = 8\sqrt{2F \pm h}$$
 19, $d = 0.35\sqrt{\frac{L q^2}{2F \pm h}}$, 22,

$$q = \frac{n S D^{2}(940+T)}{55 V}$$
, 20, $a = \frac{n S D^{2}(940+T)}{275 V \sqrt{2F+h}}$, 23,

Example. Required the diameter of an injection pipe L=10 feet long, which shall supply q=1.3 cubic feet of water per second into a vacuum of 12 pounds per square inch, the head of press water h = 2 feet?

$$d = 0.35 \sqrt{\frac{10 \times 1.3}{2 \times 12 + 2}} = 0.3055 \text{ feet} = 3\frac{1}{16} \text{ inches.}$$

Area of Steam Passages.

= area of the steam pipe, sq. in. A = area of the cylinder piston, sq. in. d =diameter of the pipe, in inches.

D = diameter, S = stroke of cylinder, in inches.

$$a = \frac{A S n}{35000},$$
 $d = \frac{D\sqrt{S n}}{186},$ - 24, 25.

Example. Required the diameter of a steam-pipe for a cylinder D = 40inches. Stroke of piston S=48 inches, and n=38 revolutions per minute?

$$d = \frac{40\sqrt{48\times38}}{186} = 9.2$$
 inches, nearly.

Steam Ports to the Cylinder.

$$\mathbf{a} = \frac{A S n}{30600}, \qquad \bullet \qquad \bullet \qquad \bullet \qquad \mathbf{26},$$

Safety Valve.

Three-fourths of the fire grate in square feet is a good proportion for the safety valve in square inches.

Notation of Letters corresponds with Figure 3, Plate V.

a = area of safety valve in square inches.

P = pressure per square inch in the boiler W = weight on the safety valve lever Q = weight of the safety valve and lever Q =

Q = weight of Q Q = weight of Q Q = weight of Q Q = weight of Q Q = weight of Qin inches.

Balance the lever over a sharp edge, and the centre of gravity Q is found; measure the distance x from the fulcrum C.

$$\mathbf{a} \ P \ e = W \ l + Q \ x$$
 27, $W = \frac{\mathbf{a} \ P \ e - Q \ x}{l}$, 29, $P = \frac{W \ l + Q \ x}{2}$, 28, $l = \frac{\mathbf{a} \ P \ e - Q \ x}{W}$, 30,

Example. Area of the safety valve $\mathbf{a}=9$ square inches, $\mathbf{c}=4\frac{1}{4}$ inches, W=50 pounds, weight of the lever and safety valve Q=15 pounds, and x=1? inches. Required at what distances l, l' and l'' will the weight W indicate pressures of P=30, P'=40, and P''=50 pounds?

$$l = \frac{9 \times 30 \times 4.5 - 15 \times 17}{50} = 19.2$$
 inches,

from the fulcrum C the weight W will indicate P = 30 pounds l' = 37.9 inches, when P' = 40 pounds. l'' = 45.8 " P' = 50 "

and thus the lever can be graduated.

Linear Expansion or Contraction in Inches of Cast Iron, Lengths in Feet.

Length.			Differen	ce in To	emperati	ure.—Fa	hrenheit		
nength.	1000	1500	2000		3000			6000	8000
Feet.	Inch.	Inch.	Inch.	Inch.	Inch.	Inch.	Inch.	Inch.	Inch.
1	0.0072	0.0110	0.0159	0.0192	0.0237	0.0336	0.0444	0.0561	0.0787
2	0.0144	0.0220	0.0300	0.0384	0.0474	0.0632	0.0885	0.1123	0.1574
5 4	0.0216	0.0330	0.0450	0.0576	0.0711	0.1008	0.1332	0.1684	0.2361
4	0.0288	0.0440	0.0600	0.0768	0.0948	0.1344	0.1776	0.2246	0.3148
5 6	0.0360	0.0550	0.0750	0.0960	0.1185	0.1680	0.2220	0 2805	0.3935
6	0.0432	0.0660	0.0900	0.1152	0.1422	0.2016	0.2664	0.3368	0.4722
7	0.0504	0.0770	0.1050	0.1344	0.1659	0.2552	0.3108	0.3929	0.3509
8	0.0576	0.0880	0.1200	0.1536	0.1896	0.2688	0.3552	0.4496	0.6396
9	0.0648	0.0990	0.1350	0.1728	0.2133	0.3024	0.3996	0.5052	0.7083
10 11	0.0720	0.1102	0.1502	0.1926	0.2376	0.3360	0.4440	0.5616	0.7872
12	0.0792	0.1214	0.1652	0.2125	0.2615	0.3696	0.4884	0.6177	0.8659
13	0.0936	0.1316	$0.1802 \\ 0.1952$	0.2318	0.2853 0.3090	0.4032	0.5328	0.6739	0.9446
14	0.1008	0.1417	0.1332	0.2510 0.2703	0.3030	0.4368	0.5772 0.6216	0.7300	1.0233 1.1020
15	0.1080	0.1620	0.2102	0.2895	0.3565	0.5040	0.6660	0.7862 0.8423	1.1808
16	0.1152	0.1722	0.2403	0.308	0.3803	0.5376	0.7104	0.8985	1.2595
17	0.1224	0.1823	0.2553	0.3280	0.4040	0.5712	0.7548	0.9546	1.3382
18	0.1296	0.1925	0.2703	0.3472	0.4278	0.6048	0.7992	1.0108	1.4169
19	0.1368	0.2026	0.2853	0.3665	0.4515	0.6384	0.8436	1.0669	1.4956
20	0.1440	0.2203	0.3005	0.3852	0.4752	0.6720	0.8880	1.1232	1.5744
21	0.1512	0.2305	0.3155	0.4045	0.4995	0.7056	0.9324	1.1793	1.6531
22	0.1584	0.2407	0.3275	0.4238	0.5228	0.7392	0.9768	1.2394	1.7318
23	0.1656	0.2508	0.3425	0.3430	0.5465	0.7728	1.0212	1.2915	1.8105
24	0.1728	0.2610	0 3575	0.3623	0.5703	0.8064	1.0656	1.3477	1.8892
25	0.1800	0.2711	0.3725	0.3815	0.5940	0.8400	1.1100	1.4038	1.9679
26	0.1872	0.2813	0.3876	0.4008	0.6179	0.8736	1.1544	1.4600	2.0467
27	0.1944	0.2914	0.4026	0.4200	0.6415	0.9072	1.1988	1.5161	2 1254
28	0.2016	0.3016	0.4176	0.4393	0.6553	0.9408	1.2432	1.5723	2.2041
29 30	0.2088	0.3117	0.4326	0.4585	0.6890	0.9744	1.2876 1.3320	1.6284	2 2 29 2.3616
31	$0.2160 \\ 0.2232$	0.3304 0.3405	0.4507 0.4657	0.5778 0.5970	0.7128 0.7365	1.0080 1.0416	1.3764	1.6848 1.7409	2.4403
32	0.2304	0.3507	0.4807	0.6163	0.7603	1.0410	1.4208	1.7971	2.5190
33	0.2376	0.3608	0.4957	0.6355	0.7841	1.1088	1.4652	1.8533	2.5977
34	0.2448	0.3710	0.5107	0.6548	0.8078	1.1424	1.5096	1.9094	2.6764
35	0.2520	0.3811	0.5258	0.6740	0.8316	1.1760	1.5540	1.9656	2.7552
36	0.2592	0.3913	0.5408	0.6933	0.8553	1.2096	1.5984	2.0217	2.8339
37	0.2664	0.4014	0.5558	0.7125	0.8791	1.2432	1.6428	2.0779	2.9126
38	0.2736	0.4116	0.5708	0.7298	0.9028	1.2768	1.6872	2.1340	2.9913
39	0.2808	0.4217	0.5858	0.7490	0.9266	1.3104	1.7316	2.1902	3.0701
40	0.2880	0.4406	0.6009	0.7704	0.9504	1.3440	1.7760	2.2464	3.1488
45	0.3240	0.4957	0.6760	0.8667	1.0692	1.5120	1.9980	2.5272	3.5424
50	0.3600	0.5508	0.7512	0.9630	1.1880	1.6800	2.2200	2.8080	3.9360
55	0.3960	0.6059	0.8263	1.0593	1.3068	1.8480	2.4420	3.0888	4.3296
60	0.4230	0.6610	0.9014	1.1556	1.4256	2.0160	2.6640	3.3696	4.7132
65	0.4680	0.6665	0.9765 1.0517	1.2519 1.3482	1.5444 1.6632	2.1840 2.3520	2.8860 3.1080	$\frac{3.6540}{3.9312}$	5.1068 5.5104
70 75	0.5040	$0.7711 \\ 0.8262$	1.1268	1.3482	1.7820	$\frac{2.5320}{2.5200}$	3.3300	4.2120	5.9040
80	$0.5400 \\ 0.5760$	0.8202	1.2019	1.5408	1.9008	2.6880	3.5520	4.2120	6.2976
85	0.6120	0.9364	1.2770	1.6371	2.0196	2.7560	3.7740	4.7756	6.6912
90,	0.6120	0.9914	1.3521	1.7334	2.1384	3.0240	3.9960	5.0544	7.0848
95	0.6840	1.0465	1.4272	1.8297	2.2572	3.1920	4.2180	5.3352	7.4784
100	0.7200	1.1016	1.5024	1.9260	2.3760	3.3600	4.4400	5.6160	7.8720
	000600	612	626	642	660	700	740	780	820
		Ex	pansion	per Deg	ree.—Fa	hrenheit	•		

Multiply by 1.1 for wrought iron, 1.5 for copper, 1.6 for brass and 2.6 for zinc.

Table of Pressure and Temperature of Steam,

calculated by the Alexander formula, with a slight modification to accommodate the volumes of the component gases, oxygen and hydrogen.

Pressure per sq. in.	Temp. Fahr.	Pressure per sq.in.	Temp. Fahr.	Pressure per sq. in.	Temp. Fahr.	Pressure per sq. in.	Temp. Fahr.
P.	T.	P.	T.	P.	T.	P.	T.
100	328.2	700	503.0	4500	714.1	30,000	1019
150	358.6	800	508.4	5000	728.3	35,000	1048
200	381.5	900	520.6	6000	754.0	40,000	1074
250	400.0	1000	531.8	7000	776.5	45,000	1098
300	415.6	1500	576.4	8000	796.4	50,000	1119
350	429.2	2000	610.0	9000	814.3	60,000	1157
400	441.1	2500	637.2	10,000	830.6	70,000	1190
450	452.2	3000	651.3	15,000	896.2	80,000	1219
500	462.1	3500	680.1	20,000	945.4	90,000	1245
600	479.6	4000	697.8	25,000	987.7	100,000	1285

In the above table it is supposed that the steam is superheated from an indefinite volume of water. The formulas on pages 394 and 395 are not reliable above

a pressure of 500 pounds to the square inch.

The formula of Messrs. Fairbairn and Tate, for the volume of steam, is inconsistent with the physical laws involved. The steam in Fairbairn and Tate's experiments has evidently been moist with globes of water, which made the steam-volume too small and the formula wrong.

For low pressure and temperatures of aqueous vapor, see Hygrometry, page 357.

HORSE-POWER IN STEAM-ENGINES.

Horse-power in machinery is assumed to be about the effect a horse is able to produce, and has been estimated and established by Mr. Watt to be 33,000 lbs. raised one foot per minute for one horse, which will be the same as 550 lbs. raised one foot per second. Mr. Watt adopted a standard steam-pressure of 7 lbs. per square inch, established a simple rule for the nominal horse-power of engines, which is, "The square of the diameter of the cylinder in inches multiplied by the cube root of the stroke in feet, and divided by the constant number 47, is the nominal horse-power. This rule agreed very near to the actual performance of engines in those days, but as the improvements advanced we found that the steam-piston can move with a greater velocity, and the steam-pressure gradually increased—that our day's engines greatly exceed the above rule.

Nominal Horse-Power.

Assume a standard steam-pressure of 30 lbs. per square inch expanded two-thirds, the velocity of the steam-piston to be $200 \frac{3}{10} \frac{3$

minute
$$n = \frac{100}{\sqrt[3]{S^2}}$$
, we will arrive at a formula of nominal horse-power.

$$H=\frac{D^2\sqrt[3]{S}}{10}$$
 for condensing engines, which will agree very near with the actual performance of our present condensing engines. The following tables are calcu-

lated from this formula.

For high-pressure engines I will assume the steam-pressure to be 80 lbs. persquare inch, expanded one-half, which will give the nominal horse-power—

$$H = \frac{D^2 \sqrt[3]{S}}{4}$$
, high-pressure engines.

The horse-power in the accompanying table, divided by 0.4, gives the nominal power of high-pressure engines. The diameters D are contained in the first column in inches, and the stroke S in feet and inches on the top line.

Indicated Horse-Power

Is that imparted by the steam on the cylinder-piston, without friction and working the pumps.

ACTUAL HORSE POWER.

One actual horse power is 33000 lbs. raised one foot in one minute. This applied to steam engines will be the mean steam pressure on cylinder piston in pounds, multiplied by the velocity of piston in feet per minute, divided by 33,000, is the horse power imparted by the steam. From this we shall deduct 25 per cent. in condensing engines, and 13.1 per cent. in high pressure engines, for working friction and pumps, the balance

to be termed the actual horse power.

Example 1. Fig. and formulæ 318. Area of steam cylinder A = 1809 square inches, stroke of piston S=4 feet, indicated pressure of steam 30 lbs. to which add the atmospheric pressure 15 lbs. or P=45 lbs. expanded $\frac{2}{3}$, the mean pressure will be F=31.459 lbs. (see Expansion Table I.), vacuum v=12 lbs. the engine making n=45 revolutions or double stroke per minute. Required the actual horse power, $H=\frac{2}{3}$ W=31.459+12-14.7=28.759 lbs. $H = \frac{1809 \times 4 \times 28.759 \times 45}{45} = 425.6 \text{ horses.}$

In this example the actual horse power is 11.6 per cent. more than the

nominal power from the table.

Example 2. Fig. 318. A high pressure engine of cylinder piston A=314 square inches, stroke S=3 feet, steam pressure 80 lbs, per square inch, to which add 15 lbs. P=95 lbs. expanded $\frac{1}{2}$, the engine making n=56 revolutions per minute. Required the actual horse power? From the expansion table we have the mean pressure F = 80.412 lbs., from which subtract the atmospheric pressure 14.7 lbs. W=65.712 lbs.

$$H = \frac{314 \times 3 \times 65.12 \times 56}{19000} = 180.8 \text{ horses.}$$

Annular Expansion Double Cylinder, Fig. 319.

These kind of engines are now sometimes made in Europe with a view to economise fuel, and to extend the expansion of steam. The outer cylinder A, A, is annular, similar to that made by Mouslay, but in this case it is employed only for expansion, the inner cylinder A is used for high pressure only. It is so arranged by steam valves that the high steam is acting the whole stroke on the small piston a, after which it is conducted to the annular cylinder where it acts expansively on the large piston A, A. The two pistons being connected by rods to one common crosshead as shown by Fig. 319. This arrangement has been successfully carried out by Mr. Jägerfelt in Nyköping, Sweden. The inner cylinder can be considered an ordinary high pressure engine where the utilized steam is set free into the air at each stroke; but in this case the exhaust steam accomplishes a second engagement in the annular cylinder, which according

to the grade of expansion may greatly exceed the original effect imparted in the small cylinder during the first engagement.

Example 3. Fig. 319. Area of the high pressure cylinder piston a=254.4 square inches, the annular expansive piston A=763.2 square inches, stroke of pistons S=3 feet, the high steam pressure P=60 lbs. vacuum v=12 lbs., making n=65 revolutions per minute. Required the actual horse power of the engine H=? The grade of expansion will be

 $\frac{100.2}{254.4} = \frac{2}{5}$, for which the mean pressure on the annular piston will be

f=32.62 lbs. See Expansion Table II. The effective pressure on the two pistons will be V=763.2 (32.62+12-14.7) + 254.4 (60-32.62) = 29800 lbs.

$$H = \frac{29800 \times 3 \times 65}{22000} = 264 \text{ horses.}$$

Example 4. Now we will reject the annular expansion cylinder, and take the effect of the steam without expansion, when the effectual pressure will be 60-14.7=45.3 lbs. and the actual power,

$$H = \frac{254.4 \times 3 \times 45.3 \times 65}{19000} = 118 \text{ horses.}$$

If we consider the last result as unit we shall have 264_118=146 horses or nearly 124 per cent. gained by the expansion, omiting the loss of steam in the steam passages.

In the first case about 11 per cent. was gained by vacuum, but that advantage is rather in favour of the utility of expansion, because the high

steam cannot so well be introduced into the condenser.

The economy will be in the same proportion when the same grade of

expansion is used in one cylinder.

I do not mean to maintain that this high per centage of economy is always fully realized in practice, as I am well aware of cases where expansion is of little use, caused by misconception and carelessness in its employment. ployment. There are many circumstances about an engine which are in favour of expansion, for instance, the steam passages between the main valve and cylinder, and the clearance between the piston and cylinder heads, contains a great deal of steam which is a total loss, but when expansion is used, that steam expands into the cylinder, and is consequently utilized. The expanded exhaust require a smaller air pump than would be necessary for high steam introduced in the condenser.

Half Trunk Expansion Engines. Fig. 320.

This kind of engines has been introduced by Mr. Carlsund, and are extensively used in Sweden, they are well suited for Gunboats where the machinery is required to be below the water line. The high steam is employed throughout the stroke in the annular space around the trunk, after which it is conducted to act expansively on the large piston A Fig. 320.

Example 5. Fig. 320. Area of the annular piston a=562 square inches, and A=2248 square inches, stroke of piston S=4 feet, steam pressure P=90 lbs., making n=68 revolutions per minute. Required the actual

horse power?

Grade of expansion =
$$1 - \frac{562}{2248} = \frac{3}{4}$$
,

From the Expansion Table II. we have f=41.58 lbs. mean pressure on A. The effectual pressure will be V=2248 (41.58–14.7) + 562 (90–41.58) = 87639 lbs., high pressure $H = \frac{87639 \times 4 \times 68}{38000} = 627.3$ horses.

Double Cylinder Expansion Engines. Fig. 321.

This kind of engines are now made in England and are said to be very economical. The small cylinder is used for high pressure, from which the steam is conveyed to expand in the large cylinder. In the figure it is arranged so that the pistons follow one another in one direction, when the steam must be conveyed from the top of the small cylinder to the bottom of the large one, and vice-versa; but it is sometimes arranged so that the pistons move in opposite direction, when the steam is conveyed direct at the same ends from the small cylinder to the large one, which has the advantage of making the steam passages shorter, but is more complicated in concentrating the motion.

Example 6.

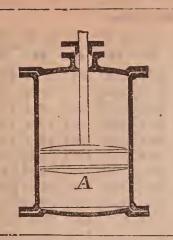
High pressure cylinder, $\begin{cases} a = 962 \text{. square inches.} \\ s = 5 \text{ feet.} \end{cases}$

A = 3848 square inches. Expansion cylinder, S = 10 feet.

Steam pressure in the small cylinder P=40 lbs., vacuum v=12 lbs., aking n=21 revolutions per minute. Required the actual horse making n=21 revolutions per minute. Grade of expansion = $1 - \frac{962 \times 5}{3848 \times 10} = \%$. power, H=?

From the Expansion Table II. we have f=11.879 lbs., mean pressure on A. $w=3848\times 10$ $(11.879+12-14:7)+962\times 5$ (40-11.879)=366767 lbs. of momentum.

 $H = \frac{366767 \times 21}{22000} = 350$ horses.

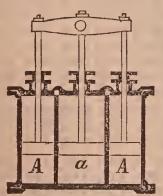


One double acting Cylinder.

Actual
$$H = \frac{A S W n}{22000}$$
, cond. engs.
horse power. $H = \frac{A S W n}{19000}$, high pr. engines.

W=F+v-14.7 for cond. engines.

W=F-14.7 for high pressure engines.

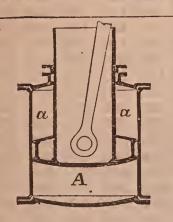


319. Annular expansion double Cylinder.

$$F = \frac{Pa}{A} [2 \cdot 3 (\log A - \log a) + 1].$$

$$f = \frac{FA - Pa}{A - a}, \quad V = A(f + v - 14.7) + a(P - f).$$

Actual $\int H = \frac{V S n}{22000}$, cond. engines. horse power. $H = \frac{V S n}{19000}$, high pr. engs.

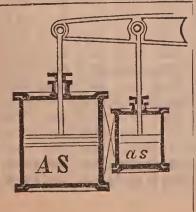


Halftrunk expansion Cylinder.

$$F = \frac{P \, a}{A} \, [2 \cdot 3(\log A - \log a) + 1].$$

$$f = \frac{Fa - Pa}{A - a}$$
, $V = A(f + v - 14.7) + a(P - f)$.

Actual f $H = \frac{V S n}{44000}$, cond. engines. horse power. $H = \frac{V S n}{38000}$, high pr. engs.



321. Double Cylinder expansion.

$$F = \frac{P \ a \ s}{A \ S} [2 \cdot 3(\log AS - \log as) + 1]$$

$$f = \frac{F \ A - P \ a}{A - a}, \quad w = \frac{AS(f + v - 14 \cdot 7)}{+a \ s(P - f)}.$$

$$J = \frac{1}{A-a}, +a s(P-J).$$

$$(m \quad w \quad n \quad \text{cond. engines.}$$

Actual $H = \frac{w n}{22000}$, cond. engines.

power. $H = \frac{w n}{10000}$, high pr. engines.

Diam			Str	- Alco	of Cy	- lind	or P	istan	Sin	foot			
Diam	1	:1/ 3/	1' 6"					" 2' 9		3' 6	•	4' 6'	1 51
in.	H	H	H	H	H	H	H	H	H	H	H	H	H
	n .			1			11	1	1				
6 7	$\begin{vmatrix} 3 & 0 \\ 4 \cdot 9 \end{vmatrix}$		1	5.90									1
8			I									_	
9		8.72	i	9.75									1
10	10	10.8		12.0					1				17.1
11	12.1	13.0	1										
12	14.4	15.5	16.5	17.4		18.9							
13	16.9	18.2	19.3			22.1							28.9
14	19.6	21.1	22.4	23.6		25.7			28:3	3 29.7			33.5
15	2.25	24.2	25.8	27.1	28.3	29.5	30.5			[34.]	35.7	37.1	38.5
16	25.6	27.4	29.3	30.8	32.2				37.0				43.8
17	28.9	31.1	33.1	34.8	36.4	37.9	39.2						49.4
18	32.4	34.9	37.1	39.0	40.8	42.5	44.0						55.4
	36.1	38.9	41.3		45.5	47.3	49.0			1		, ,	61.7
20	40.0	43.1	45.8	48.2	50.4	52.4	54.3						68.4
21	44.1	47.5	50.5	53.1	55.6	57.8	59.8					72.8	75.4
22	48.4	52.1	55.4	58.3	61.0	63.4	65.6)			82.8
23 24	52·9 57·6	57.0	$\begin{array}{c} 60.5 \\ 65.9 \end{array}$	63·7 69·4	$ \begin{array}{c} 66.7 \\ 72.6 \end{array} $	75.5	71.8 78.1		76·3 83·1			87·4 95·2	90.5
1	62.5	$62.0 \\ 67.3$	71.5	75.3	78.7	81.9	84.8		,			103	98.6
26	67.6	72.8	77.3	81.5	85.2	88.6	91.7		4			111	116
27	72.9	78.5	83.5	87.8	91.9	95.6	99.0	1	3	111	116	120	125
	78.4	84.4	89.8	94.5	98.8	102	106		113	119	124	129	134
1	84.1	90.5	96.2	101	106	110	114			128	133	139	144
30	90.0	96.9	103	108	113	118	122		130	137	143	149	154
	96.1	103	110	116	121	126	130	134	139	146	153	159	164
32	102	110	117	123	129	134	138	143	148	155	163	170	175
33	109	117	124	131	137	142	147	152	157	165	173	180	186
34	115	124	132	139	145	151	157	162	167	175	183	190	198
35	122	132	140	148	154	$\begin{array}{c c} 160 \\ 170 \end{array}$	166	172	177	186	194 205	202	210
36 37	$ \begin{array}{c c} 129 \\ 137 \end{array} $	$\begin{array}{c} 140 \\ 147 \end{array}$	$\begin{array}{c c} 148 \\ 156 \end{array}$	$\begin{array}{c} 156 \\ 165 \end{array}$	$\begin{array}{c c} 163 \\ 172 \end{array}$	180	$\begin{array}{c} 176 \\ 186 \end{array}$	$\begin{array}{c c} 182 \\ 192 \end{array}$	187 198	$\begin{array}{c} 197 \\ 208 \end{array}$	217	214 226	222 234
38	144	155	165	174	182	190	196	202	209	218	229	238	247
39		164	174	183	192	200	206		220	231	241	251	260
40	160	172	183	193	202	210	217	224	231	243	254	264	274
42	176	190	202	212	222	231	240	347	254	268	280	291	302
44	193	208	221	233	244	254	263	271	280	294	307	320	331
46	211	228	242	255	266	277	287	297	306	321	336	350	362
48	230	248	264	277	290	302	313	323	332	350	366	380	394
50	250	269	286	301	315	328	339	350	360	380	397		427
52	270	291	309	326	340	354	367	378	390	410	429		463
54	291	314	333	351	367	382	396	408	420	443	463	481	500
60 66	360 435	388 468	412 498	433 525	453 548	472 571	488 591	504 610	519 628	547 661	571 690		$\begin{array}{c c} 616 \\ 744 \end{array}$
72	518	558	593	626	653	679	704	726	748	787	822		886
78	608	655	696	734	766	784	825	852	877	924		003 1	
84	705	759	807	851	888	924	957		1015		1116		
90	810	872	927	975	1020 1	062	1100	1134	1168	1229	1284 1	336 1	385
	921			1110	1160 1	206	1249	1291	1327	1400	146011	505 1	575

			Stro	ke o	f Cyl	inde	r Pis	ton 5	s in	feet.			
D	6'	7'	8'	. 9'	10'		12'	13	14'	15'	16′	18′	201
in.	H	H	H	H	H	H	H	H	·H	H	H	H	H
30	163	172	180	187	194	200	206	1	217	222	226	236	244
32	186	196	204	213	220	227	252	1	246	1			278
34 36	210	221	231	240	249	257	264					303	313
38	235 262	248 276	$\begin{array}{ c c } 259 \\ 289 \end{array}$	269 299	273 311	288 321	296 330		312 348			$\begin{array}{c c} 339 \\ 378 \end{array}$	351 391
40	$\frac{202}{290}$	306	320	333	344	355	366			1	1		434
42	320	336	352						425			462	478
44	352	371	387		1	430	453		466	477		507	525
46	384		1		460	1	484					554	587
48	418	441	461		496	1 1	527		555	1	1	603	625
50	554	478			538		572			1		655	677
52	491	518		562	582		619		651	667		708	733
54	529 570	558			628 675		667		700 755	719 775	734 790	764 811	79 0 850
56 58	611	644	673	ě .	724				810	830		880	912
60	654	689	720		775				867	888		943	977
62	698				828		879			948			1043
64	744						938				1024		1101
66	791	834		906								1141	
68	840	885						1087					1254
70	890							1152				1283	
72 74	942 995	_	1037 1095		$1116 \\ 1179$			$\begin{array}{c} 1218 \\ 1287 \end{array}$				1358 1434	
76		11048				1216		1358			1	_	1567
78	1105		1219			1353						_	1649
80		1225		1331				1504				1	1737
84	1,282	1350		1467	1520	1569		1658					1914
88	1407	1	1549			1722		1820					2100
92	1538		1693			1882							2297
96 100	1674 1817		1843			2049						$2414 \begin{vmatrix} 2620 \end{vmatrix}$	2474
						$\begin{array}{c c} 2224 \\ 2405 \end{array}$						2833	
	2119		2333	2426	2512	2594	$\frac{24}{2671}$				2939		
$\overline{112}$	2279	2399	2509	2609	2702	2790	2871	2949	3023	3092	3161	3286	3404
116	2445	2574	2691	2799	2898	2992	3081	3163	3243	3315	3391	3525 3	3651
											3628		
											3874		
											4128 4390		
136	3380	2520	3499	3024	3084	4113	4235	4348	4150	4557	4654	1846 5	019
140	3561	3749	3920	4077	4222	4359	4488	4608	4716	4832	4939	5135	319
											5225		
148	3980	4190	4381	1556	4718	4871	5016	5179	5279	5399	5519	5739 5	944
152	4198	4402	4621	4805	4976	5138	5291	5431	5568	5696	5821	6053 6	270
											6132		
162	1768	5020	5249	5458	5653	5836	5010	6170	6324	6469	6613	7004	122
174	5404	5701	6055	6207	6521	6727	6022	7117	7206	7464	7112 7629	7039 9	218
180	5887	6199	6480	6530	6979	7205	7419	7817	7809	7989	8164 8	3488 8	793
	,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,	3200	3 200]	3000,	3010	. = 00]]	, 110	. 02.6]				20010	

Approximate Horse-Power

of small high-pressure engines. $H = 0.1 D^2 \sqrt[3]{S}$. Steam pressure not less than 60 pounds to the square inch.

Diam.					Stroke	e S of	pisto	n in ii	nches.				
D Inches.	3	4	5	6	7	8	9	10	12	14	15	16	18
2	.577	.634	.684	.727	.765	.800	.832	.862	.915	.964	.985	1.00	1.05
$2\frac{1}{2}$.900	.990	1.07	1.13	1.20	1.25	1.30	1.34	1.42	1.50	1.54	1.57	1.63
3	1.30	1.43	1.54	1.64	1.72	1.80	1.87	1.94	2.06	2.17	2.22	2.27	2.36
$3\frac{1}{2}$	1.77	1.94	2.10	2.22	2.34	2.45	2.55	2.64	2.80	2.95	3.00	3.69	3.21
4 i	2.31	2.54	2.74	2.90	3.06	3.20	3.33	3.44	3.66	3.85	3.94	4.05	4.19
41/2	2.92	3.21	3.47	3.68	3.87	4.05	4.42	4.36	4.64	4.88	5.00	5.10	5.0
5	3.60	3.96	4.27	4.54	4.78	5.00	5.20	5.38	5.72	6.02	6.16	6.30	6.55
6	5.19	5.70	6.15	6.53	6.89	7.20	7.55	7.82	8.31	8.75	8.95	9.15	9.50
7	7.08	7.78	8.40	8.92	9.40	9.80	10.2	10.6	11.2	11.8	12.1	12.3	12.9
8	9.25	10.1	11.0	11.6	12.2	12.8	13.3	13.8	14.6	15.4	15.7	16.1	16.8
9	11.7	12.9	13.9	14.7	15.5	16.2	16.8	17.4	18.5	19.5	20.0	20.4	21.2
10	14.4	15.9	17.1	18.2	19.1	20.0	20.8	21.5	22.9	24.1	24.6	25.2	26.2
11	17.5	19.2	20.8	22.0	23.2	24.2	25.2	26.1	27.7	29.2	29.9	30.5	31.6
12	20.8	22.9	24.7	26.2	27.6	23.8	30.0	31.0	33.0	34.8	კ 5.5	36.3	37.8

The horse-power of small engines, as counted by the English, is only 0.4 of that in this table for the same size cylinders.

To Approximate the Size of Steam-Engines.

Example 1. It is required to build a river steamer of displacement T=1000 tons to run M=16 nautical miles per hour. Required, the size of the cylinder for an ordinary overbeam engine? From the table of steamship performance will be found the required actual power H=1798 horses.

From the table of Nominal horse-power select the approximate size of cylinder, which may be D=88 inches, diameter of cylinder by S=14 feet stroke, which answers to H=1866 horses nominal. In this case the nominal horse-power can be considered the same as the actual.

Example 2. A propeller steamer is to run M = 10 nautical miles per hour, with a displacement T = 3400 tons. Required, the size of the cylinders?

From table of steamship performance H=992 horses, to be divided into two cylinders of 496 each. Select from table of Nominal horse-power D=60 inches diameter of cylinders and S=2' 19" stroke of piston, which answers to H=504, or $504\times 2=1008$ horses of the two cylinders. After these approximations are made, make a careful calculation from the original formulas.

Example 3. Suppose the propeller for the steamer in the preceding Example 2 makes n=60 revolutions per minute. Required, the diameter of the propeller-shaft? See Table, page 418, for wrought-iron shafts, for 1000 horses and 60 revolutions, the shaft should be 12.8 inches.

Example 4. A steamer of T=2500 tons is to run M=9 nautical miles per hour with an indicated steam-pressure of 20 lbs., or P=35 lbs. per square inch, expanded $\frac{1}{2}$. Required, the consumption of fuel in tons per 24 hours?

Table of steamship performance H = 585 horses.

Table V., page 409, consumption of fuel, 3.44 tons.

The required consumption will be $5.85 \times 3.44 = 20.124$ tons per 24 hours' steaming.

SOUND.

Velocity of Sound through Air.

v = velocity in feet per second.

t =temperature of the air, Fahr. scale.

D =distance in feet the sound travels in the time T.

$$v = 1089.42\sqrt{1 + 0.00208(t - 32)}$$
.

Velocity of sound in water is about 4 times that in air, and 8 times that through solids.

Intensity of sound is inversely as the square of the distance.

$$D = 1089.42 T_{V} \sqrt{1 + 0.00208(t - 32)},$$

$$T = \frac{D}{v}.$$

Example. A ship at sea was seen to fire a cannon, and 6.5 seconds afterward the report was heard; the temperature in the air was 60°. Required, the distance to the ship.

$$D = 1089.42 \times 6.5 \sqrt{1 + .00208(60^{\circ} - 32)} = 7300$$
 feet, or 1.38 miles.

Descriptions of Sound	Audible at	a distance of
Descriptions of Sound.	Feet.	Miles.
A powerful human voice in the open air, no wind,	460	0.087
Report of a musket,	16 ,000	3.02
Drum,	10,500	2
Music, strong brass band,	15,840	3
Cannonading, very strong,	575,000	90
In a barely observable breeze a strong human voice		
with the wind can be heard,	15,840	3

Ringing Bells-Weight, Dimension and Key-note.

8 8						
Place, and when cast.	Weight.	Diameter.	Soun S.	d-bow.	Key- note.	Vibrat.
Moscow, 1726,		inches. 272 185 151.25	inches. 23 14.750 12.125	S: D. 0.084 0.080 0.080	note. D G# B	vib. 18.21 25.1 30.58
Olmutz, Bohemia, Vienna, Austria, Westminster, Eng., 1856. Erfurt, 1487,	40,320 40,200 35,625 30,800	121 118 113.5 103.5	9.125 9.500 9.375 7.75	0.075 0.080 0.083 0.075	D# D# E F	39.4 38. 6 40.3 42
Paris, 1680, Montreal, 1847, York, Eng., 1845. New York, City Hall,	23,672 28,560 24,080 22,300	103 103 100 108	7.5 7.8 8 8,3	0.073 0.082 0.080 0.077	E F E	40 42 46 4 41
St. Peter's, Rome, Oxford, Great Tom, 1680, Cologne, 1447, Brussels, Belgium,	18,600 17,024 16,016 15.848	97.25 84 95 81	7.5 6.125 7.2 5.75	0.077 0.073 0.076 0.071	G G H	46 50 49 51
Lincoln, Eng., 1834, St. Paul's, Eng., 1716, Exeter, 1675,	12,096 11.500 10,080 9,856	82.5 81 76 75.5	6 6.08 5 5.93	0.073 0.075 0.066 0.078	G# A G#	51 54 50
Old Lincoln, 1610, Westminster, 1857,	8,960	72	5.75	0.079	B	60.4

Diameters in Inches of Wrought-Iron Shafts.

Horse, Number of revolutions per minute of wrought-iron shafts.													
power.	10	15	20	25	30	35	40	45	50	55	60	70	80
Н.	In.	In.	In.	In.	In.	In.	In.	In.	In.	In.	In.	In.	In.
1	2.32	2.07	1.84	1.71	1.61	1.53	1.46	1.41	1.36	1.31	1.28	1.22	1.16
2	2.92	2.55	2.32	2.16	2.03	1.92	1.84	1.72	1.71	1.66	1.61	1.53	1.46
3	3.40	2.72	2.66	2.47	2.33	2.21	2.11	2.03	1.91	1.90	1.71	1.75	1.67
4	3.68	3.22	2.92	2.72	2.55	2.43	2.32	2.23	2.16	2.09	1.80	.1.93	1.84
5	3.97	3.48	3.15	2.92	2.75	2.61	2.50	2.41	2.33	2.25	1.88	2.08	1.99
6	4.22	3.68	3.35	3.11	2.92	2.78	2.66	2.56	2.47	2.39	2.06	2.21	2.11
7	4.44	3.88	3.52	3.27	3.06	2.92	2.80	2.69	2.60	2.52	2.12	2.33	2.22
8 9	4.64	4.05	3.69	3.42	3.22 3.35	3.06	$\frac{2.92}{3.04}$	$2.82 \\ 2.93$	$\begin{vmatrix} 2.72 \\ 2.82 \end{vmatrix}$	$2.63 \\ 2.74$	2.27	2.43	2.33
10	4.82 5.00	4.22 4.36	3.83 3.98	$3.56 \\ 3.69$	3.47	$\begin{vmatrix} 3.18 \\ 3.29 \end{vmatrix}$	3.15	$\frac{2.35}{3.03}$	$\begin{vmatrix} 2.82 \\ 2.92 \end{vmatrix}$	2.83	$\begin{array}{c} 2.40 \\ 2.75 \end{array}$	$\begin{bmatrix} 2.52 \\ 1.61 \end{bmatrix}$	$2.42 \\ 2.50$
12	5.34	4.64	4.22	3.92	3.68	3.50	3.35	3.22	3.11	3.01	2.73	$\frac{1.01}{2.78}$	$\begin{bmatrix} 2.50 \\ 2.61 \end{bmatrix}$
15	5.72	5.00	4.54	4.22	3.97	3.76	3.60	3.47	3.35	3.24	3.15	3.00	2.86
20	6.30	5.50	5.00	4.64		4.14	3.97	3.82	3.96	3.57		3.29	3.15
25	6.79	5.93	5.39	5.00	4.71	4.46	4.28	4.11	3.97	3.84	3.74	3.55	3.40
30	7.21	6.30	5.72	5.32	5.00	5.74		4.37	4.22	4.08	3.97	3.77	3.61
35	7.59	6.63	6.03	5.60	5.26	5.00	4.78		4.44	4.30	4.18	3.97	3.80
40	7.94	6.93	6.30	5.85	5.50	5.22	5.00	4.81	4.65	4.50	4.37	4.15	3.98
45	8.25	7.20	6.55	6.09	5.73	5.43	5.20	5.00	4.83	4.67	4.54	4.31	4.13
50	8.55	7.47	6.79	6.30	5.93	5.62	5.38	5.18		4.84		4.47	4.28
60	9.08	7.93		6.70	6.30	5.98	5.72	5.50	5.32	5.15	5.08		4.55
70	9.57	8.36		7.05	6.64	6.30	6.03	5.80	5.60	5.42	5.27	i	4.79
80	10.0	8.75	7.94	7.37	6.94	6.58	6.30	6.07	5.85	5.67	5.51	5.23	5.00
90	10.4		8.25	7.67	7.22	6.84	6.55	6.30		5.90	5.73	5.44	5.20
100	10.8	9.41		7.94	7.47	7.09	6.78	6.53		6.10	5.93	5.63	5.39
$\begin{array}{c} 120 \\ 140 \end{array}$	$\begin{array}{ c c }\hline 11.4\\12.0\\\hline\end{array}$	$10.0 \\ 11.5$	$9.09 \\ 9.57$	8.44	7.95 8.37	7.53 7.93	7.21 7.59	$6.94 \\ 7.31$	$6.70 \\ 7.06$	6.49 6.83	6.31 6.64	6.00 6.30	5.73
160	12.6		10.0	9.29	8.74	8.29	7.94	7.64		7.14	6.94	t t	6.03 6.31
180	13.1	11.4		9.67	9.09		8.26	7.95	7.67	7.42	7.21	- 1	6.55
200	13.6			10.0	9.42		8.55	8.23	7.94	- 4	7.48		6.79
2:0	14.6	12.8		10.8	10.1	9.63	9.22	8.87	8.56		8.06	7.65	7.32
300	15.5	13.6	12.3	11.5	10.8	10.2	9.80	9.43	9.10		8.57	8.12	7.77
350	16.3	14.3	13.0	12.0	11.3	10.8	10.3	9.92	9.58	9.27	9.00	8.55	8.18
400	17.1	15.0	13.6	12.6	11.9	11.2	10.8	10.4	_	9.69	9.42	8.94	8.55
450	17.8	15.5	14.1	13.1	12.3	11.7	11.2	10.8		10.1	9.80	9.30	8.89
500	18.4		14.6		12.8				10.8			9.64	
550	19.0		15.1	14.0		12.5		11.5		10.8		9.94	_
600 700	$ 19.6 \\ 20.7 $		15.5 16.4	$14.4 \\ 15.2$		12.9 13.6		$\frac{11.9}{12.5}$		11.1			
800	$\begin{vmatrix} 20.7 \\ 21.5 \end{vmatrix}$		17.1	15.2		14.2		13.1		$11.7 \\ 12.2$	$\frac{11.4}{11.9}$		10.3
1000	23.3		18.5	17.1		15.3		14.1	13.6		12.8		
1200	24.7		19.6			16.3		14.9		14.0		12.9	
1500	26.6			19.6		17.5		16.1		15.1		13.9	
2000	29.3		23.5		20.3	19.3		17.7		16.6		15.3	
2500	31.5	27.5			21.9	20.8		19.1		17.9		16.5	
3000	33.5	29.3			23.3	22.1	21.1	20.3	19.6	19.0		17.5	
3500	35.2		28.0		24.4	23.3	22.2	21.4	20.7	20.0		18.4	
4000	36.8				25.6	24.3		22.3	21.6			19.3	
4500	38.4		30.4		26.6			23.3	22.4	21.7	21.1	20.0	19.2
v000	39.6	34.7	[31.5]	29.3	27.2	26.1	25.0	24.1	23.3	[22.5]	21.9	20.8	19.91

Diameters in Inches of Wrought-Iron Shafts.

House	Number of revolutions per minute of wrought-iron shafts.												
Horse power.	1001		1501		200	-	300		400	-	600		1000
power.	100	120	100	11.	200	200		000	400		000		1000
H.	In.	In.	In.	In.	ln.	In.	In.	ln.	In.	In.	In.	In.	In.
1	1.08	1.00	0.94	0.90	0.85	0.80	0.75	0.71	0.68	0.63	0.59	0.54	0.5
2	1.35		1.19		1.08	1.00		0.90	0.86	0.80		0.68	0.63
3	1.55	1.44	1.36	1.29	1.24	1.15	1.08	1.03	0.98	0.91		0.78	0.72
4	1.71	1.59		1.42		1.26		1.13		_	0.94	0.86	0.80
5	1.84	1.71	1.61		1.46	1.36			1.16	1.08		0.92	0.86
6	1.96	1.82	1.71	1	1.56	1.44			1.24	1.15		0.98	0.91
7	2.06	1.92	1.80	1.71	1.64	1.52	1.43	_	1.30	1.21		1.03	0.96
8	2.15	2.00	1.88	1.79	1.71	1.59			1.36	1.26	1.19	1.08	1.00
9	2.24	2.08	1.96	1.86		1.65	1.55		1.41	1.31	1.24	1.12	1.04
10	2.22	2.16	2.03	1.93	1.85	1.71	1.61		1.47	1.36		1.16	1.08
12	2.47	2.29	2.15	$\frac{2.05}{2.00}$	1.96	1.82	1.71		1.56	1.44		1.24	1.15
15	2.66	2.47	2.32	2.20	2.11	1.96	1.85		1.67	1.55	1.46	1.33	1.24
20	2.92	2.71	2.56	2.43	2.33	2.15	2.03		1.84	1.71		1.46	1.36
25	3.15	2.92	2.75	2.61	2.5	2.33	2.19		1.98	1.84		1.57	1.46
30	3.34	3.11	2.92	2.78	2.66	2.47	2.33	2.21	2.11	1.96		1.68	1.55
35	3.52	3.27	3.08	2.93	2.80	$\frac{2.60}{2.71}$	2.44	$\begin{bmatrix} 2.33 \\ 2.43 \end{bmatrix}$			1.94 2.03	1.76	1.64
40	3.68	3.42 3.56	3.22	3.06 3.18	2.92 3.04	$\begin{bmatrix} 2.71 \\ 2.82 \end{bmatrix}$	2.56 2.66	2.53		$2.15 \\ 2.24$		$\begin{bmatrix} 1.85 \\ 1.92 \end{bmatrix}$	1.71
45	3.83		3.34	3.29	3.15	$\frac{2.02}{2.92}$	$\frac{2.00}{2.75}$	$\frac{2.33}{2.62}$		2.33	$\frac{2.11}{2.19}$		1.78
50	$\begin{vmatrix} 3.97 \\ 4.21 \end{vmatrix}$	3.69 3.91	3.47 3.68	3.50	3.35	3.11	$\begin{bmatrix} 2.73 \\ 2.93 \end{bmatrix}$	$\frac{2.02}{2.78}$		2.47	2.13	1.99 2.11	1.84
1	4.44		3.88	3.69	3.53	3.27	3.06	$\frac{2.73}{2.93}$		$\begin{bmatrix} 2.47 \\ 2.60 \end{bmatrix}$	2.44	$\frac{2.11}{2.22}$	2.06
70 80	4.64	4.12 4.31	4.05	3.86	3.63	3.42	3.22	3.06		$\frac{2.00}{2.71}$	2.55	2.33	$\frac{2.00}{2.15}$
90	4.82	4.48	4.22	4.01	3.83	3.56		3.18		2.82	2.61	2.42	$\frac{2.15}{2.24}$
100	5.00	4.64		4.15	3.97		3.47	3.29		$\begin{vmatrix} 2.02 \\ 2.92 \end{vmatrix}$	$\frac{2.01}{2.75}$	2.50	2.31
120	5.31	4.94	4.64	4.41	4.22	3.92	3.68	3.50		3.11	2.92	2.66	2.46
140	5.59	5.20	4.89		4.44	4.12		3.68		3.27		2.80	$\frac{2.40}{2.59}$
160	5.85	5.43		1	4.64	4.31	4.05	3.85		3.42		2.92	2.71
180	6.08	5.65	5.31	5.05		4.48	4.22	4.01		3.56		3.04	2.82
200	6.30	5.85	5.50	5.23	1	4.64	,	4.15	3.97	3.68		3.15	2.92
250	6.78	6.30	5.93	5.51	5.39	5.00	4.70	4.47		3.97	3.73	3.39	3.15
300	7.21	6.69	6.30	6.00	5.73	5.31	5.00	4.75	4.54	4.11	3.97	3.61	3.35
350	7.59	7.05	6.63	6.30	6.03	5.59	5.41	5.00		4.44		3.80	3.52
400	7.94	7.37			6.30	5.85		p.	5.00			3.92	3.68
450	8.26		7.21	6.85	6.55	6.08	5.72	5.44	5.20	4.83	4.54		
500	8.55	7.94			6.79	6.30	5.93	5.63	5.39		4.71	4.27	3.97
550	8.82	8.19	7.71	7.32	7.01	6.50	6.12	5.81	5.56	5.16	4.86	4.41	4.10
600	9.08	8.43	7.92	7.54	7.21	6.69	6.30	6.00		5.32	5.00	4.54	4.22
700	9.56	8.88	8.35	7.94		7.05			6.03	5.59		4.78	4.44
800	10.0	9.28	8.74		7.94	7.37			6.30	5.85		5.00	4.64
1000	10.8	10.0	9.41		8.55	7.94			6.79	6.30		5.39	5.00
1200	11.5		10.0		9.09		7.94		7.21	6.69		5.72	5.31
1500	12.3		10.7		9.79		8.55		7.77	7.21		6.17	5.72
2000	13.5		11.8		10.8	10.0			8.55	7.94			6.30
2500	14.6		12.8		11.6		10.2	9.63		8.55		7.31	6.73
3000	15.5		13.5		12.3	11.4			9.79	9.09		7.77	7.41
3500	16.4		14.3		13.0	12.1			10.3	9.56		8.18	7.59
4000	17.1	L.	15.0		13.6		11.8		10.8			8.55	7.94
4500	17.8		15.5		14.1		12.3				9.79		8.25
5000	118.4	17.1	16.1	115.3	14.6	13.5	12.8	12.1	11.6	11.8	10.1	9.21	8.55

SLIDE VALVES.

THE slide valve motion is one of the most important features in causing a steam engine to work well, and to employ the effect of steam economically. The author of this book being well acquainted with disarrangements on this point, has here endeavoured to give a good working-drawing of the proper proportions and arrangements of slide-valve motion. (See Plate IV.)

Main Valve.

It will be best to assume a certain size cylinder, and at the same time give the proportions for any size.

D=34 inches, diameter of the cylinder.

S = 18 inches stroke of piston.* n = 56 double strokes per minute.

We have the area of the steamports m, from Formula 26, page 252.

$$\mathbf{a} = \frac{342 \times 0.785 \times 18 \times 56}{30600} = 30 \text{ square inches, nearly.}$$

$$m = \frac{D+S}{26} = \frac{34+18}{26} = 2$$
 inches,

the width of the steamport; if the quotient gives a fraction take the nearest quarter or eighth.

$$\frac{\mathbf{a}}{m} = \frac{30}{2} = 15$$
 inches, breadth of steamport.

 $r=\frac{1}{6}m$ about = 1 inch, the exhaust port $o=2m-\frac{1}{6}r=3\frac{1}{6}$ inches, and $f=o+2r=5\frac{1}{2}$ inches, $h=f-\frac{1}{4}r=5\frac{1}{4}$ inches, $k=1\frac{1}{2}m=3$ inches, and $i=h+2k=11\frac{1}{4}$ inches, e=m=2 inches.

* The stroke and diameter is here rather out of proportion, but we will maintain them in the calculations as they suit the drawing, which is purposely made to show the *slide valves* on a large scale. The rules will however suit any proportions of diameter and stroke.

To Find the Stroke of the Eccentric.

s = stroke of the eccentric in inches.

The $lap L = \frac{1}{6}(i - f - 2m) = \frac{7}{8}$ inches.

The lead of the valve, or opening of the steamport when the crank pin stands on the centre should be about

$$l = \frac{m\sqrt{n}}{80} = \frac{2\sqrt{56}}{80} = \frac{1}{4}$$
 inches, nearly.

Having finished the main valve and ascertained the stroke of the eccentric, it is now required to find the position of the centre b, (Plate V.,) of the eccentric, to the crank-pin. Suppose the crank pin of the engine stands at an on the centre nearest to the cylinder, and the eccentric rods are attached direct to the valve rods; draw the line dd, at right-angle to the centre-line aa'' of the engine, then

the angle,
$$\sin W = \frac{2(L+l)}{s} = \frac{2(\frac{7}{6} + \frac{1}{4})}{5\frac{1}{6}} = 0.409$$
, or $W = 24^{\circ} 10'$.

See Plates IV. and V.

To Find the position of the Crank-Pin at the moment the Main Valve opens.

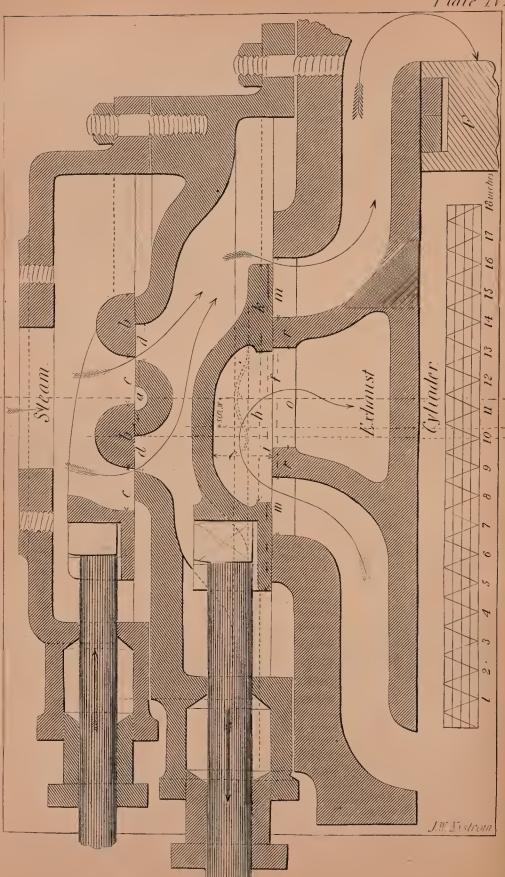
$$y = \frac{Sl}{s \cos W} = \frac{18 \times 0.25}{5.5 \times 0.9123} = 0.9$$
 inches, nearly,

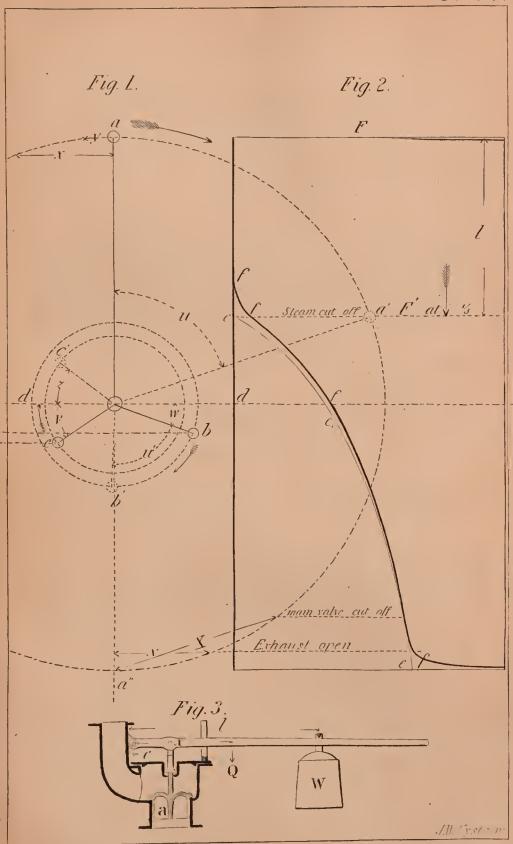
from the centre line.



Stide Valves.

Plate IV.







To Find the position of the Crank at the moment the Exhaust opens.

$$x = \frac{S}{2} \left(\sin W - \frac{1}{s} (f - h) \right) = \frac{18}{2} \left(0.409 - \frac{1}{5.5} (5.5 - 5.25) \right) = 3.27 \text{ inches}$$

from the centre line.

To Find the position of the Crank Pin when the Main Valve cuts off the Steam.

$$X = \frac{2SL}{s} = \frac{2 \times 18 \times \frac{7}{8}}{5.5} = 5.727$$
 inches.

To Find at what part of the Stroke the Main Valve Cuts off the Steam,

Will cut off at =
$$1 - \frac{4L^3}{s^2} = 1 - \left(\frac{2 \times \frac{7}{8}}{5 \cdot 5}\right)^2 = 0.899$$
 of the stroke.

The greater the lap is, the sooner will the main-valve cut off, but if the lap is increased the stroke of the eccentric must also be equally increased. It does not work well to cut off much by the main-valve, especially when the engine works fast; for very slow motion it may answer to cut off at \(\frac{1}{2} \) the stroke.

It will be noticed that the centre of the eccentric is always ahead of the crank

It will be noticed that the centre of the eccentric is always ahead of the crank pin with an angle $90^{\circ}+w$. Hence when the engine is to be reversed, the centre b must have the same position on the opposite side of the centre-line, or the eccentric must be moved forwards an angle of $90^{\circ}-2w$.

Cut=off Valve.

The width of the cut off ports should be about $d = \{m = 1\}$ inch, and their

breadth
$$\frac{\mathbf{a}}{2d} = \frac{30}{2 \times 1\frac{1}{4}} = 12$$
 inches, when two ports are used.

Proportions of the Valve.

a-b=c-d, a+d=b+c, and a=2d, and the stroke of the cut-off valve eccentric s=2b, we shall have $a=2\frac{1}{2}$, $b=2\frac{1}{4}$, $c=1\frac{1}{2}$, $c=1\frac{1}{3}$, and $s=4\frac{1}{3}$ inches.

Let us assume the steam to be cut off at $\frac{1}{2} = l$ of the stroke S, the position of the crank-pin a' will then be $\sin u = 2l = 0.666$, or $u = 70^{\circ}$ 30'; at the same time the position of the centre c' of the cut off eccentric will be

$$\sin z = \frac{d+c}{s} = \frac{1\frac{1}{4}+1\frac{1}{2}}{4\frac{1}{2}} = 0.612$$
, or $z = 37^{\circ} 50'$,

and $V = u - z = 70^{\circ} 30' - 37^{\circ} 50' = 32^{\circ} 40'$, the position of the centre c when the crank-pin a is on the centre. This Table will show the positions of the centre a and c, at different cut offs. Letters correspond with Figure 1, Plate VI.

Cut off at i.	v	sin.v	stroke of eccen.s.	z	u	F.	p.
	22° 10′ 32° 40′ 31° 55′ 42° 35′ 46° 30′ 50° 30′	0·377 0·539 0·527 0·675 0·7193 0·7933	2b 2b c+a b+c a+b-c a+b-c	37° 50′ 37° 50′ 43° 35′ 47° 25′ 58° 58° 30′	60° 70° 30' 75° 30' 90° 104° 30' 109° 30'	0.5880 0.6914 0.7332 0.8350 0.910 0.985	0·250 0·333 0·375 0·500 0·625 0·666

It will now be observed that the effectual pressure F in this Table is less than in the Table on page 239, owing to the valve not cutting off the steam instantly, but gradually, so that the density of the steam in the cylinder is already diminished at the cut off point. The valve will cut off quicker the less the angle z is.

Sec Figure 2, Plate VIII. The actual pressure will not form a sharp corner at e, or follow the line e, e, e, as would be due when cut off at $\frac{1}{3}$ the stroke, but the line ff'ff will be the true diagram. Including the steam in the ports and steamchest, the density at the end of the stroke will correspond nearly with the **Ta**ble.

STEAM BOILERS.

The accompanying proportions are averages of a great number of good marine boilers.

Letters denote.

D = diameter of the steam-cylinder in inches.

S = stroke of piston under which steam is fully admitted, in inches.

n = number of double strokes, or revolutions per minute. w = pounds of water evaporated per pound of coal, per hour.

V = volum coefficient from the steam table.

= fire grate in square feet, for each cylinder, and with natural draft.

To Find the Area of Fire Grate.

$$= \frac{D^2 S n}{4.66 wV} \qquad n = \frac{4.66 wV}{D^2 S} \qquad -1, 2.$$

Example 1. A steam engine of D=54 inches diameter of the cylinder, and stroke of piston 96 inches, cut off at $\frac{1}{2}$, S=48 inches; is to make 22 revolutions per minute. Anthracite coal to be used, that evaporates w = 7 pounds of water per pound of coal, and to carry 27 pounds of steam per square inch, V = 649. Required the area of fire grate = 2? in square feet.

$$= \frac{54^2 \times 48 \times 22}{4 \cdot 66 \times 7 \times 649} = 145 \cdot 34 \text{ square feet.}$$

Example 2. A steamboiler of = 128 square feet, is to be used for an engine of D=36 inches diameter, and 64 inches stroke,—cut off the steam at $\frac{3}{2}$ then S=42.66 inches. Steam pressure to be kept at 25 pounds per square inch V=679. w=6.5. Required for how many revolutions per minutes can the steam be kept at 25 pounds?

$$n = \frac{4.66 \times 6.5 \times 679 \times 128}{36^2 \times 42.66} = 47.6$$
 revolutions.

Horse Power of the Fire Grate.

H = horse power of the fire grate.

P = pressure in the boiler in pounds per square inch, excluding the atmosphere.

p == vacuum in the condensor in pounds per square inch.

$$= \frac{Hx}{Vw (P+0.8 p)}, \quad H = \frac{Vw (P+0.8 p)}{x}. \quad 3 \quad 4.$$
(\frac{1}{5} \text{ the stroke. } x = \frac{27700. \text{ saves } 55}{40}

Cut off the stroke. x = 27700. saves 55 $\frac{1}{3}$, , , x = 31400. , 49 per cent steam at $\begin{cases} \frac{1}{3} & \text{the stroke.} & x = 31400 & \text{stand} & 49 \\ \frac{1}{3} & \text{the stroke.} & x = 38400 & \text{stand} & 38 \\ \frac{1}{3} & \text{the stroke.} & x = 45500 & \text{stand} & 20 \\ \frac{3}{4} & \text{the stroke.} & x = 49100 & \text{stand} & 20 \end{cases}$ Steam admitted throughout the stroke x = 61700. , 0 per cent.

Example 3. Steamboilers are to be constructed for an engine of 650 horses, the steam to be cut off at $\frac{1}{3}$ the stroke, and P = 36 pounds per square inch, V=544, w=7.5 pounds of water evaporated per pound of coal. Required the fire grate in the boilers = ? in square feet.

$$= \frac{650 \times 38400}{554 \times 7.5 (36 + 0.8 \times 11)} = 136 \text{ square feet.}$$

Example 4. Required, the horse-power of a fire grate = 112 square feet, to carry 18 pounds steam, and cut off at $\frac{2}{3}$ the stroke? V = 810, w = 7 pounds.

$$H = \frac{112 \times 18 \times 810 \times 7}{45500} = 251.2$$
 horses.

Consumption of Coal.

C =coal consumed in pounds per hour.

$$C = \frac{3D^2 S n}{w V}$$
, $C = \frac{14H x}{V w (P + 0.8p)}$. 5, 6.

Example 5. A steam-engine of D=42 inches diameter, and 48 inches stroke, cut off the steam at $\frac{1}{3}S=16$ inches, is to make n=65 revolutions per minute with a pressure of 34 pounds per square inch, V=564, and w=6 pounds. Required, the consumption of coal in pounds per hour C=?

$$C = \frac{3 \times 42^2 \times 16 \times 65}{6 \times 564} = 1625$$
 pounds per hour.

Example 6. A pair of steam-engines of H=260 horses are to be worked with P=28 pounds per square inch, cut off at $\frac{1}{3}$ the stroke, V=635, the coal to evaporate w=6.5 pounds of water per pound of coal. Required, the consumption of coal in pounds per hour C=?

$$C = \frac{14 \times 260 \times 31400}{630 \times 6.5(28 + 0.8 \times 10)} = 775$$
 pounds per hour.

It will be observed in the Formulas 4 and 6 that the higher steam used, the less fuel and fire-grate is required for the same power—the proportion of fuel will be nearly as the square root of the steam pressure, and still more fuel is saved by cutting off the steam at an early part of the stroke.

Heating Surface O Compared with Grate.

In common stationary boilers, . . . $\bigcirc = 20$ $\boxed{=}$. Returning flue boilers, . . . $\bigcirc = 25$ $\boxed{=}$. Tubular boilers (marine), . . . $\bigcirc = 30$ $\boxed{=}$. With vertical tubes (Martin), . . . $\bigcirc = 35$ $\boxed{=}$.

Cross-area of Flues (Calorimeter).

In the common single returning flue boilers, the cross-section area of the first row should be, 0.18 Returning row, flues or tubes, . . 0.13 Cross-section area of chimney at the top A = 0.16 .

Height of Chimney.

$$h = \frac{C^2}{4 | \Box|^2} - 2, \qquad h = \frac{H^2}{2.1A}, \qquad C = 2 | \Box| \sqrt{h+2},$$
 $H = 1.45A\sqrt{h}, \qquad A = \frac{H}{1.45\sqrt{h}}, \qquad \Box = \frac{C}{2\sqrt{h+2}}.$

Example. Area of fire-grate $\boxed{}$ = 140 sq. ft., to consume C = 2100 pounds of ccal per hour. Required, the height h of the chimney?

$$h = \frac{2100^2}{4 \times 140^2} = 56.3$$
 feet, the answer.

Standard Horse-Power of Steam-Boilers.

The power of a steam-boiler ought to be graded by the dimensions of the areas of the fire grate and heating surface, like that of a steam-engine is graded by the diameter and stroke of the steam-piston, without taking into consideration the evaporative power of the fuel, expansion of the steam, etc., which are independent of the size of the boiler, as well as that of the engine.

Let denote the area of the fire grate.

O = the area of the heating surface in square feet. P = pressure of steam in pounds per square inch above vacuum.

Then the standard nominal horse-power H of a steam boiler can be expressed

$$H = \sqrt{\frac{10 \sqrt{P}}{10}} \cdot \bigcirc = \frac{10 H^2}{\sqrt{P}} \cdot \bigcirc = \frac{10 H^2}{\sqrt{P}} \cdot P = \left(\frac{10 H^2}{\boxed{\Box}}\right)^2$$

Example. Suppose = 100, $\bigcirc = 3000$ and P = 75,

Then,
$$H = \sqrt{\frac{100 \times 3000 \sqrt{75}}{10}} = 510$$
, the standard nominal

horse-power.

Ordinary Performance of Steam-Boilers.

Natural draft consumes about 12 to 15 pounds of coal per square foot of grate

per hour, and generates about 4 to 5 horse-power per square foot of grate.

The heating surface should be about 4 to 5 square feet per horse-power, and evaporate 4 to 5 pounds, or 92.5 to 115.5 cubic inches, of sea water per hour, at the above-mentioned rate of combustion.

Good coal evaporates about 6 to 8 pounds of water per pound of coal.

Each horse-power requires the consumption of about 3 to 4 pounds of coal per hour.

To find the Ultimate Bursting Strength

of a steam-boiler-shell, tube or flue.

Notation of Letters.

W=ultimate tensile strength in pounds per square inch of the boiler iron.

t = thickness of the plate iron in decimals of an inch. D = diameter of the boiler in inches.

P = bursting pressure (internal) in pounds per square inch.

$$P = \frac{Wt}{D}$$
, for single-riveted, and

$$P = \frac{1.3 Wt}{D}$$
, for double-riveted boilers.

Example 1. The diameter of a single-riveted boiler being D=72 inches, thickness of plates t = 0.375 inches, and the ultimate strength of the iron W = 45000. pounds to the square inch. Required, the bursting pressure of the boiler?

$$P = \frac{45000 \times 0.375}{72} = 234.4$$
 pounds to the square inch.

A double-riveted boiler of the same dimensions will burst with $1.3 \times 234.4 =$ 304.72 pounds to the square inch.

The Thickness of Boiler-Plates required for Bursting Pressure.

$$t = \frac{PD}{W}$$
, for single-riveted, and

$$t = \frac{PD}{1.3 W}$$
, for double-riveted boilers.

Ultimate Strength of Tubes and Flues

for External Pressure to Collapse.

Notation of Letters.

D =diameter of tube or flue in inches. L =length of the tube or flue in feet.

t =thickness of iron in decimals of an inch.

P = external collapsing pressure in pounds per square inch.

$$P = \frac{200.000 \, t^2}{D \, \sqrt{L}},$$
 and $t = \sqrt{\frac{P \, D \, \sqrt{L}}{447.2}}.$

Example 1. A flue of D=15 inches diameter, and L=12 feet long, thickness of iron t=0.25. Required, the collapsing pressure?

$$P = \frac{200,000 \times 0.25^2}{15 \times \sqrt{12}} = 241$$
 pounds to the square inch.

Example 2. D = 9, L = 10 and t = 0.2.

$$P = \frac{200,000 \times 0.04}{9\sqrt{10}} = 282$$
 pounds.

Example 3. D=6, L=6, and t=0.2. Required the pressure P?

$$P = \frac{200,000 \times 0.04}{6 \times \sqrt{6}} = 504$$
 pounds.

Staying Steam-Boilers.

$$d = \text{diameter of good iron stay-bolts in inches.}$$
 $d = \frac{D\sqrt{P}}{74}$.

D= distance apart in inches in salt water on flat surfaces. $D=\frac{74 d}{2}$

$$P$$
= pressure of steam in pounds per square inch. $P = \frac{5476 d^2}{D^2}$.

The following table is given by Mr. Fairbairn, as exhibiting the strongest form and best proportions of rivet joints, as deduced from experiments and actual practice:

								4		
Thickness of plate.				om head. Distance from centre to cent.			Quantity of lap in single riveted. double riveted			riveted.
in. 16ths.	in.	Ratio.	in.	Ratio.	in.	Ratio.	in.	Ratio.	in.	Ratio.
0.19 = 3	0.38	2	0.88	4.5	1.25	6	1.25	· 6	2.10	10
0.25 = 4	0.50	2	1.13	4.5	1.50	6	1.50	6	2.50	10
0.31 = 5	0.63	2	1.38	4.5	1.63	5	1.88	6	3.15	10
0.38 = 6	0.75	2	1.63	4.5	1.75	5	2.00	5.5	3.33	9.2
0.50 = 8	0.81	1.5	2.25	4.5	2.00	4	2.25	4.5	3.75	7.5
0.63 = 10	0.94	1.5	2.75	4.5	2.50	4	2.75	4.5	4.58	7.5
0.75 = 12	1.13	1.5	3.25	4.5	3.00	4	3.25	4.5	5.42	7.5

WOOD FOR COMBUSTION.

A cord of wood is 8 feet wide by 4 feet high and 4 feet deep, or the wood is 4 feet long. The cord contains $8 \times 4 \times 4 = 128$ cubic feet, of which only 74 cubic feet is solid wood and 54 cubic feet of space.

Two cords of wood evaporate about the same quantity of water as one ton of

anthracite coal.

The best pine wood evaporates 5 pounds of water per pound of wood consumed in a steam-boiler furnace. One cord of wood can be consumed per hour on 60 square feet of grate.

Weight in Pounds per Cord of Different Woods.

Woods, Seasoned.	lbs.	Woods, Seasoned.	lbs.	Woods, Seasoned.	lbs.
White Oak Red-heart Hickory . Southern Pine	3821 3705 3375	Beech	2875 2870 2689	Cedar Yellow Pine White Pine Spruce Hemlock	1904 1868 1685

Wood requires 32 per cent. more fire grate than mineral coal, for equal generation of steam. The furnace should be 60 per cent. of cubical space more for wood than for coal, or about 4.5 cubic feet per square foot of grate.

Properties of Fuel.

Kind of Fuel.	Units of heat per pound of fuel.	Pounds of water evaporated per 1b. of coal.	Per cent. of carbon.	Cubic feet of air requ. for one lb. of coal.	Weight per cubic foot.	Cubic feet to stow a ton.
Bituminous coal	_11600	7 to 9	80	265	50	44
Anthracite coal	13340	8 to 10	92	282	54	40
Coke	12420	8 to 10	86	245	31	72
Coke, nat. Virginia	11600	8 to 9	80	260	48	48
Coke, Cumberland	11600	8 to 10	80	250	32	70
Charcoal	13920	5 to 6	96	265	24	104
Dry wood	6380	4 to 5	44	147	20	100
Wood with 20 per ct. water	4930	4	34	115	25	100
Turf, dry	7395	6	51	165	28	80
Turf, 20 per ct. water .	5800	5	40	132	30	75
Oil, Wax, Tallow	11165	14	77	200	59	37
Alcohol (from market) .	8410	9.56	58	154	52	4 2
Obanically one nound of ac	whom hamme	to ourhonia	bion	nograinog	4ha	· · · · · · · · · · · · · · · · · · ·

Chemically, one pound of carbon burnt to carbonic acid requires the oxygen of 153 cubic feet of atmospheric air.

Timber, Green and Seasoned.

Timber.			Green.	Seasoned.	
American Pine. Ash Beech Cedar English Oak Riga Fir	•	•	44.75 58.19 60.00 32.00 71.62 48.75	30.69 50.00 53.37 28.25 43.50 35.50	Com bi

Comparative weight per cubic foot in pounds of green and seasoned timber.

Board Measure.

Multiply together the three dimensions, width and thickness in inches and the length of the lumber in feet; divide the product by 12, and the quotient will be the board measure.

Combustion is the rapid chemical combination of substances with oxygen. Carbon C and hydrogen H, are the substances most generally employed for generating heat. Carbon is fully consumed when combined with oxygen O, to form carbonic acid gas CO_2 , and partly consumed when in the form of carbonic oxide gas CO or smoke. h=units of heat generated of one pound of fuel. The heat necessary to raise one pound of water one degree Fah. is one unit of heat. w=pounds of water at 212° evaporated per pound of fuel. A=volume in cubic feet and a=weight in pounds of atmospheric air required for the perfect combustion of one pound of fuel. C, C, and C0, and C1 are in the four first formulas, fractions in one pound of the compound fuel.

one pound of the compound fuel.

Perfect Combustion.

$$A=149[C+3(H-\frac{o}{8})], -1$$
 $a=12[C+3(H-\frac{o}{8})], -2$
 $b=14500[C+4\cdot28(H-\frac{o}{8})], 3$
 $w=\frac{h}{966}=15[C+4\cdot28(H-\frac{o}{8})]$
 $m=\frac{h}{966}=15[C+4\cdot28(H-\frac{o}{8})]$
 $m=\frac{h}{966}=15[C+4\cdot28(H-\frac{o}{8})]$
 $m=\frac{h}{966}=15[C+4\cdot28(H-\frac{o}{8})]$
 $m=\frac{h}{966}=15[C+4\cdot28(H-\frac{o}{8})]$

When oxygen is supplied to carbon in a proportion between CO and CO_2 , both the gases will be formed separately in the proportion of the formulas 5 and 6, when the heat generated will be as formulas 7 and 8, in which C, C, CO and CO_2 are expressed in pounds, for instance: C=20 lbs. of oxygen united with C=12 lbs. of carbon will form

$$(CO) = \frac{56 \times 12 - 21 \times 20}{12} = 21 \text{ lbs. carbonic oxide.}$$

$$(CO_2) = \frac{33 \times 20 - 44 \times 12}{12} = 11$$
 lbs. carbonic acid, and will

generate $h=8002.5\times20-6820\times12=78210$ units of heat.

One unit of heat=772 foot pounds, if generated per second will be H= 1.4 horses, of which we in our days practice utilizes about one-twentieth. The following table will show how important it is to fully consume the combustibles to acid. One pound of carbon consumed to oxide will generate only 1.72 horses, instead of 5.66 when consumed to acid.

Properties of Combustion, per Hour.

C	CO	CO_2	0	α	A	h	w	H
lbs.	lbs.	lbs.	lbs.	lbs.	cub. ft.	heat.	lbs.	horses.
1		3.666	2.666		149	14500	15	5.660
. 1	2.666		1.333	6	74.50	4400	4.55	1.720
0.433	1		0.566	2.550	31.65	1650	5.633	1.200
0.272		1	0.727	3.275	40.56	3960	4.100	1.545
	1.750	1.375	1	3.500	43.33	5440	5.633	2.125
	0.445	0.392	0.222	A	1.2.38	1210	1.250	0.472
	.0358	.0246	·0 2 31	.0808	1	97.3	0.100	0.038
	0.584	0.244	0.170	0.800	9.920	966	1	0.378
	1.550	0.651	0.470	2.120	26.30	2558	2.645	1

RADIATION OF HEAT FROM STEAM-PIPES,

Boilers or Steam Cylinders.

Notation of Letters.

D = outside diameter of steam-pipe, without casing, and limited to not more than 12 inches.

T = temperature of the steam, Fahr. scale.

t = temperature of the external air.

h = calorics radiated per square foot per hour, on uncovered pipe.

A = outside area in square feet of steam-pipe.

H = horse-power lost by radiation of heat.

n = exponent of the wind, which varies with the current of air or draft about the steam-pipe, as in the following table:

Wind.	Exp. n.
Calm.	1.20
Gentle.	1.22
Brisk.	1.24
Storm.	1.26

The loss of heat will then be per hour-

One horse-power consumes or generates 2564 calorics per hour. By logarithms the Formula 1 is reduced to—

The log. k is contained in the second column of the accompanying table for different diameters of pipes.

For any uncovered plane or cylindrical surface above 12 inches in diameter the radiation in units of heat per square foot per hour will be—

The effect of thickness of metal is inappreciable for practical purposes.

Example 1. The California S. N. Co.'s steamer Julia has a steam-pipe 40 feet long by D=9 inches in diameter, and two branch-pipes 12 feet long by D=4 inches each, all uncovered. Pressure of steam, 100 fbs. $T=337^{\circ}$. Temperature of the external air $t=70^{\circ}$. Required, the loss of heat and power by radiation? In calm wind n = 1.2. See table for n.

 $h = 0.001122[450 + (12 - 9)^{2}](337^{\circ} - 70^{\circ})^{1.2} = 420.34,$ the units of heat lost per square foot per hour.

Area of pipe, $A = 0.75 \times 3.14 \times 40 = 94.24$ square feet. Power lost, $H = \frac{94.24 \times 420.34}{1000} = 15.5$ horses.

2564

The branch-pipes lose

4.6 horses.

The total loss of power

20.1 horses.

The same pipes covered with 2-inch-thick felt would gain $20.1 \times 0.93 = 18.7$ horse-power.

In the factory of Bellavista, Peru, are 150 feet of uncovered steam-Example 2. pipes D=3 inches in diameter. Steam-pressure, 45 fbs. $T=292^{\circ}$ Fahr. Temperature of external air t=68, and wind gentle, n=1.22. Required, the horse-power and fuel lost?

Formula 3. $\log h = 0.77408 - 1 + 1.22 \log_{10} (292 - 68) = 2.32805$

or 173 units of heat lost per hour.

Area of steam-pipes, $A = 0.785 \times 150 = 117.8$ square feet.

Formula 2. $H = \frac{117.8 \times 173}{2564} = 8$ horse-power nearly, which is lost by radiation.

The same pipes covered with one-inch felt will gain 8×0.89 (see table) = 7.12 horse-power. The steam-engine in Bellavista works without expansion, and consumes about 10 fbs. of coal per horse-power per hour = $7.12 \times 10 = 71.2$ pounds,

and for 8 hours' working = 569.6 lbs. of coal lost per day.

The radiation of heat from steam-pipes causes a condensation of steam to water, and the weight in pounds of water so condensed is equal to the units of heat radiated, divided by the latent heat of the steam in the pipe. The Formula 1 will also answer for calculating the quantity of heat radiated from steam or water-pipes for heating rooms.

Percentage of Heat or Power Gained

by covering steam-pipes with felt and canvas outside.

Diam	Logarithm			Thick	ness o	f felt,	coverii	ng in i	nches.		
. D	k	1 4	<u>3</u> 8	$\frac{1}{2}$	$\frac{3}{4}$	1	$1\frac{1}{2}$	2	3	4	6
1	0.80663—1	65	76	81	86	92	94	96	98	99	100
2	0.79561-1	63.	74	80	85	90	93	. 95	97	98	99
3	0.77408—1	61	72	79	84	89	92	95	96	98	99
4	0.76096-1	59	71	77	83	83	92	94	96	97	99
5	0.74809—1	57	69	76	82	87	91	. 94	96	97	99
6	0.73670—1	54	67	74	81	86	91	94	95	97	69
7	0.72668—1	52	66	73	81	85	90	93	95	97	99
8	0.71838—1	50	64	71	80	85	90	. 93	95	97	99
9	0.71179—1	47	62	70	79	85	89	93	95	97	99
10	0.70705 - 1	45	61	69	78	84	89	92	95	96	99
11	0.70417—1	42	59	67	78	83	88	92	94	96	98
12	0.70321—1	40	58	66	77	83	88	92	94	96	98

Lap-welded American Charcoal Iron Boiler Tubes.

Pascal Iron Works
Philadelphia.

Tasker Iron Works, New Castle, Del.

Diameter of the tube. Outside Inside.		Heating surface per foot of length. Outside Inside.		Thickness of metal.	Length of per square Outside.		Area of cross- section. Outside Inside.		Weight per foot of length.
Inches.	Inches.	Sq. ft.	Sq. ft.	Wg. inches.	Feet.	Feet.	Sq. in.	Sq. in.	Pounds.
1	0.856	0.2618	0.2241	15 0.072	3.819	4.460	0.785	0.575	0.708
1.25	1.106	0.3272	0.2895	15 0.072	3.056	3.455	1.227	0.960	0.9
1.50	1.334	0.3926	0.3492	14 0.083	2.547	2.863	1.767	1.396	1.250
1.75	1.560	0.4580	0.4084	13 0.095	2.183	2.448	2.405	1.911	1.665
2	1.804	0.5236	0.4723	13 0 098	1.909	2.118	3.142	2.556	1.981
2.25	2.054	0.5890	0.5377	13 0.098	1.698	1.850	3.976	3.314	2.238
2.50	2.283	0.6545	0.5977	12 0.109	1.528	1.673	4.909	4.094	2.755
2.75	2.533	0.7200	0.6631	12 0.109	1.390	1.508	5.940	5.039	3.045
3	2.783	0.7853	0 7285	12 0.109	1.273	1.373	7.069	6 083	3.333
3.25	3.012	0.8508	0.7885	11 0.119	1.175	1.268	8.296	7 125	3.958
3.50	3.262	0.9163	0.8430	11 0.119	1.091	1.171	9.621	8.357	4.272
3.75	3.512	0.9817	0.9194	11 0.119	1.018	1.088	11.045	9.687	4.590
4	3.741	1.0472	0.9794	10 0.130	0.955	1.023	12.566	10.992	5.320
4.50	4.241	1.1781	1.1105	10 0.130	0.849	0.901	15.904	14.126	6.010
5	4.720	1.3680	1.2357	9.5 0.140	0.764	0.809	19.635	17.497	7.226
6	5.699	1.5708	1.4920	9 0.151	0.637	0.670	28.274	25.509	9.346
7	6.657	1.8326	1.7428	7.5 0.172	0.545	0.574	38.484	34.805	12.435
8	7.636	2.0944	1.9991	7 0.182	0.478	0.500	50,265	45.795	15.109
9	8.615	2.3562	2.2553	6.5 0.193	0.424	0.444	63.617	58.291	18.002
10	9.573	2.5347	2.5022	5.5 0.214	0.382	0 399	78.540	71,975	22.19

The length of tube and thickness of metal can be varied to suit orders.

The heating surface of a boiler tube is that exposed to the fire.

Safe ends of thicker metal welded on the ends of tubes as may be required.

BLOWING OFF. SALT WATER. INCRUSTATION.

Sea water contains about 0.03 its weight of salt. When salt water boils, fresh water evaporates and the salt remains in the boiler; consequently the proportion of salt increases as the water evaporates, until it has reached 0.36 weight to the water; the salt will then commence to saturate in the boiler, and the water in so-

lution will hold 0.36 weight of salt to 1 of water.

To prevent deposit in the boiler, it is necessary to keep the salt below this proportion, which is overcome by withdrawing (blowing off) part of the supersalted water, while less salted (feed) water is replaced. It is found in practice that when the proportions are kept 0.12 of salt to 1 weight of water, the deposit will be very slight. To obtain this it will be necessary to blow off—

$$\frac{0.03}{0.12}$$
 = 0.25 parts of the feed water, or,

if a brine-pump is used, it should be at least 0.25 of the feed-pump. W = cubic feet of supersalted water to be blown off per minute. $W = \frac{D^2 S n}{3000 V}$. $W = \frac{D^2 S n}{3000 V}$.

Example. D=30 inches, stroke of piston 36 inches, cut off at half stroke S=18, making 14 revolutions per minute, with a pressure of 30 pounds per square inch, V=610. How much water must be blown off per minute?

$$W = \frac{30^2 \times 18 \times 14}{3000 \times 610} = 0.124$$
 cubic feet.

Heat Wasted by Blowing Off.

Letters denote,

w = water evaporated and W = water blown off in cubic feet per unit of time.

t =temperature of the feed water. T = " blowing off.

H= heat wasted, per cent.

$$H = \frac{W(T-t)}{w(990 + T-t)}$$

Example. Let the quantity of water blown off be $\frac{1}{3}$ of the feed water, we have W=1, and w=2; the boiling-point of the water will then be $T=215.5^{\circ}$; let the feed water taken from the hot-well be $t=100^{\circ}$. Required, the quantity of heat lost?

$$H = \frac{1(215.5^{\circ} - 100)}{2(990 + 215.5 - 100)} = 0.052$$
 or 5.2 per cent.

This is a very trifling quantity of heat lost.

Heat Wasted by Incrustation.

The conducting power of iron for heat is about 30 times that of saturated scales, hence a considerable portion of heat is lost when the scales become thick in a boiler.

t = thickness of the scale in 16ths of an inch. H = per cent, of heat wasted.

$$H = \frac{t^2}{32 + t^2}.$$

Example. The scale in a boiler is 5-sixteenths of an inch thick. How much heat is lost by it?

 $H = \frac{5^2}{32 + 5^2} = 0.438$, or 44 per cent., nearly,

which goes out through the chimney.

This is merely to show that the heat lost by blowing off is but trifling compared with the heat lost by saturation of scales, which additionally injures the boiler by softening and fracturing the iron, and final explosions.

When boilers are taken good care of by cleaning and blowing off at short inter-

vals, the scales need not exceed 1-sixteenth of an inch.

Proportions of Salt in Water:

its boiling-point and weight per cubic foot.

Salt in 100	Boiling temp.	Weight per	Spe- cific	Salt in 100	Boiling temp.	Weight per	Spe- cific		
Weights.	Fahr.	cub. ft.	grav.	weights.	Fahr.	cub. ft.	grav.		
				weighter.	ran.		5100		
	07.00	pounds.	71.00	0.74	040 001	pounds.			
0 1	2120	59.837	1.00	21	218.304	72.224	1.21		
1 1	212.205	60.431	1.01	22	218.690	72.728	1.22		
2	212.422	61.024	1.02	23	219.082	73.395	1.23		
3	212.649	61.617	1.03	24	219.483	73.980	1.24		
4	212.887	62.209	1.04	25	219.887	74.565	1.25		
5	213.136	62 801	1.05	26	220.296	75.148	1.26		
. 6	213.394	63.393	1.06	27	220.713	75.732	1.27		
7	213.664	63.984	1.07	28	221.131	76.316	1.28		
8	213.942	64.575	1.08	29	221.558	76.899	1.29		
9	214.229	65.166	1.09	30	221.984	77.482	1.30		
10	214.526	65.756	1.10	31	222.419	78.064	1.31		
11	214.801	66.346	1.11	32	222.857	78.646	1.32		
12	215.145	66.935	1.12	33	223 302	79.228	1.33		
13	215.446	67.524	1.13	34	223.733	79.810	1.34		
14	215.797	68.113	1.14	35	221.208	80.390	1.35		
15	216.132	69.701	1.15	36	224.668	80.970	1.36		
16	216.477	69.289	1.16	37	225.139	81,550	1.37		
17	216.826	69.877	1.17	38	225.611	82,130	1.38		
18	217.186	70.464	1.18	39	226.087	82.709	1.39		
19	217.550	71 051	1.19	40	226.572	83.288	1.40		
20	217.924	71.377	1.20	Saturates with 40 parts of salt.					

Water does not increase in volume by addition of the above proportions of salt.

To Command the Engineer how to Manœuvre the Engine in a Steamboat.

·	
Go ahead,	one stroke.
Back,	two strokes.
Stop,	one stroke.
Slowly,	two short.
Full speed,	three short.
Go ahead slowly,	one long, two short.
Back slowly,	two long, two short.
Go ahead, full speed,	one long, three short.
Back fast,	two long, three short.
Hurry,	three short repeated.

It is also customary to have two bells in the engine-room—a large bell for the long strokes, and a smaller for the short strokes.

Weight, Size, Price and Surface of Copper and Brass Tubes, 10 feet long.

Outside	Bir.W.	Weight	of tube.	Price	Whole		Bir.W.	Weight	of tube.	Price	Whole
Diam- eter.	Gauge	Brass.	Cop.	per tube.	Sur- face.	Diam- cter.	Gauge	Brass.	Cop.	per tube.	Sur- face.
Inches.	No.	Lbs.	Lbs.	\$ cts.	Sq. Ft.	Inches.	No.	Lbs.	Lbs.	\$ cts.	Sq. Ft.
0.625	18	3.478	3.681	2 30	1.636	2.	14	18.84	19.95	8 00	5.236
0.75	17	4.950	5.241	2 97	1.963	2.125	14	19.07	20.18	8 20	5.563
.8125	17	5.372	5.679	3 00	2.127	2.25	14	21.18	22.42	8 90	5.890
0.875	17	5.775	6.114	3 40	2.290	3.375	14	22.32	23.65	9 45	6.217
.9375	16	6.954	7.362	3 60	2.454	2.5	14	23.53	24.89	9 95	6.544
1.	16	7.418	5.854	3 92	2.618	2.625	14	24.67	26.12	10 45	6.872
1.125	16	8.354	8.835	4 40	2.945	2.75	14	25.83	27.35	11 00	7.200
1.25	15	10.21	10.83	4 70	3.272	3.	13	37.00	39.17	13 70	7.854
1.375	15	11.23	11.91	4 95	3.600	3.25	13	40.00	42.34	14 85	8.508
1.5	15	12.28	13.00	5 20	3.927	3.5	13	43.10	45.61	16 00	9.163
1.625	15	13.30	14.08	5 65	4.254	4.	12	49.39	52.30	17 00	10.47
1.75	14	16.5	17.45	7 00	4.581	4.5	12	55.55	58.8	19 10	11.78
1.812	14	17.08	18.08	7 20	4.745	5.	12	61.44	65.00	21 00	13.08
1.875	14	17.72	18.75	7 50	4.908	6.	11	81.58	86.35	26 00	15.71
1.937	14	18.26	19.32	7 75	5.072	8.	11	108.8	115.0	34 50	20.95

Scamless-Drawn Brass Tubes for Plumbing,

In lengths of 10 feet. Screw-coupling on one end of each length. Price per tube.

Diameters, inches.	<u>5</u> 8	3/4	7/8	1	$1\frac{1}{4}$	$1\frac{1}{2}$
Plain tubes, Tinned tubes,	\$ cts.	\$ cts.	\$ cts.	\$ cts.	\$ cts.	\$ cts.
	2 50	3 00	4 50	6 00	7 00	8 00
	3 00	3 50	5 00	7 00	8 00	9 00

Price of Taps, Dies and Stocks.

Diameters, inches.	<u>5</u>	3/4	7 8	1	$1\frac{1}{4}$	$1\frac{1}{2}$
Taps, Solid dies,	\$ cts. 2 50 3 50 St	\$ cts. 2 75 3 50 ocks, \$8,	\$ cts. 3 00 3 50 net.	\$ cts. 3 50 3 50	\$ cts. 4 50 3 50	\$ cts. 6 00 4 00

Price for Each Extra Coupling.

Diameters, inches.	° <u>5</u>	3 [*]	7 8	'1'	11.	$1\frac{1}{2}$
Straight couplings, Elbows, Tees, Cross couplings,	\$ cts. 20 26 30 45	\$ cts. 25 35 40 60	\$ cts. 35 48 55 85	\$ cts. 40 53 60	\$ cts. 45 65 85 1 50	\$ cts. 50 80 1 00 2 20

The prices are only approximate. The price of copper tubes is 12 to 13 per cent. more than of brass.

Brass and copper tubes are manufactured at the American Tube Works, Boston, Mass.; Merchant & Co., 507 Market street, Philadelphia, agents.

Proportionate Tensile Strength of Rolled Iron and Copper, In pounds per square inch, at different temperatures, Fahr. and Centigrade.

Fahr.	Cent.	Iron	Copper.	Fahr.	Cent.	Iron.	Copper.
32	0.	55,000	32,800	800	427	51,800	17,200
100	37.7	58,200	32,300	900	483	45,000	14,000
200	93.3	62,800	31,000	1000	540	37,000	11,000
300	149.	65,750	29,500	1200	650	25,000	7,000
400	205.	67,000	27,400	1500	820	16,500	3,000
500	260.	66,000	25,300 $23,000$	2000	1090	7,000	0.0000
600	316.	62,700		2500	1370	2,500	Fused to
700	370.	57,800	20,100	3000	1650	Fused.	liquid.

	Composition Nails, Copper and Iron Rivets.													
ose.	Comp	osition N	ails.	Braziers	Copper	Rivets.		Ire	on Rivets.					
Gange.	Thick.	Length.	In 1	Diameter.	Length.	In 10 lbs.	Gan	Diameter.	Length.	In 10 fbs.				
No.	Inches.	Inches.	Num	Inches.	Inches.	Num.	No.	Inches.	Inches.	Num.				
1	0.04	3/4	290	3,116	1f2	2384	0	3f16	1,52	3280				
2	0.05	7 7 5 8	260	1 1 4	1f2	1018	1	1f4	1,72	1276				
3	3 0.06 1 inch. 212 1/4 9/16 983 2 1/4 9/16 1130													
4	0.07	1.1 <i>f</i> 8	201	5 f 16	9 f 16	573	3	5 f 16	9 f 16	654				
5	0.08	1.1 / 4	199	5 f 16	5 f 8	516	4	5 f 16	5 f 8	589				
6	0.09	1 inch.	190	3 78	7 / 8	357	5	3 f 8	7, 18	407				
7	0.10	1.1 f 8	184	3 78	15 / 16	334	6	3 f 8	15 f 16	380				
8	0.10	1.1 f 4	168	7 f 16	1 inch.	210	7	7 / 16	1 inch.	239				
9	0.11	1.1 / 2	110	1/2	1.3 f 16	141	8	1f2	1.3 f 16	160				
10	0.11	1.5 f8	101	9 / 16	1.5 f 16	99.5	9	9 f 16	1.5 f 16	112				
11	0.12	1.3 f 4	74	5 f 8	1.7 f 16	71.9	10	5 <i>f</i> 8	1.7 f 16	81.7				
12	0.12	2 inches	64	11/16	1.9 f 16	53.8	11	11 f 16	1.9 f 16	61.3				
13	0.13	2.1 f 4	59	3 / 4	1.3f4	41.6	12	3f4	1.3 f4	47.3				
14	0.14	2.1 / 2	51	13 / 16	1.13 / 16	32.8	13	13 f 16	1.13 / 16	37.3				
15	0.15	2.3 f 4	43	7 f 8	2.1 f 16	26.3	14	7 <i>f</i> 8	2.1 f 16	30.				
16	0.16	3 inches	35	1 inch.		16.7	15	1 inch.	2.3f.8.	19.				
		T	engi	th in I	nches o	f Pen	nv	Nails.						

	1.5 1.75 4 d. 5 d.									
--	--------------------	--	--	--	--	--	--	--	--	--

Sheet Zinc and Iron.

SHEET ZINC .. RUSSIA SHEET IRON. Size 84 in. by 24, 28, 32, 36 and 40 inches. Size 28×56 in. = 10.88 sq. feet.

Zinc	Wi	dth of Sh	eet.	Bir. W.	Russian	Weigl	Weight per		
gauge.	24	32	40	gauge.	gauge.	Sheet.	Sq. Ft.	gauge.	
No.	Pounds.	Pounds.	Pounds.	No.	No.	Pounds.	Pounds.	No.	
8	6.23	9.68	12.1	28	7	6.25	0.574	29	
9	7.20	11.2	14.0	27	8	7.25	0.666	28	
10	8.00	124	15.6	26	9	8.	0.735	27	
11	8.90	13.8	17.3	25	10	9.	0.827	26	
12	10.1	15.7	19.7	$24\frac{1}{2}$	11	10.	0.918	25	
13	11.1	17.3	21.6	23	12	10.75	0.987	$24\frac{1}{2}$	
14	12.4	19.3	24.1	22	13	11.75	1.08	24	
15	16.2	25.2	31.6	21	14	12.5	1.15	231/4	
16	17.4	27.1	33.9	20	15	13.5	1.24	$22\frac{3}{8}$	
18	21.9	34.0	42.6	18	16	14.5	1.33	$21\frac{1}{2}$	

To find the Weight of Castings, by the Weight of Pine Patterns. RULE.

Multiply the weight of the Pattern by

12 for Cast Iron, for Brass, 13 19 for Lead, 12.2 for Tin, 11.4 for Zinc,

and the product is the weight of the Castings.

Reductions for Round Cores and Core-prints.

Rule. Multiply the square of the diameter by the length of the Core in inches, and the product by 0.017, is the weight of the pine core, to be deducted from the weight of the pattern.

Shrinking of Castings.

Pattern-Makers' Rule should be for

Cast Iron, . Brass. Lead, . Zinc, .

of an inch longer per linear foot.

To Approximate the Weight of Steam Boilers.

The area of fire grate gives a nearer approximation to the weight of Marine boilers, than the heating surface.

Letters denote.

= total fire grate in square feet.

W = weight of the boiler in pounds, including fire bars, doors, smoke pipe, fire tools and appendages, but without water. W=800 = .

Example. Required the weight W=? of a steam boiler of ==250 square feet, grate surface.

W=800×250=200,000 lbs.

Weight of the water is about three-fourths of W or of the total weight of boilers.

Weight of rivets, braces or stays, doors and fire bars, is about one quarter of W or of the total weight of boilers.

To Approximate the Weight of Engines. .

Letters denote

D = diameter of cylinder in inches. S = stroke

W=weight of engine in pounds, including engine room tools, oil and tallow tanks, wheels, propeller and shafts.

	coemcient w.
Trunk and oscillating engines, Direct action paddle wheel engines,	4 4·25 4·5
Geared propeller engines,	5·5
Side lever engines,	6.
$W \equiv k D^2 \sqrt{S_c}$. 11

Example. Require the weight W=? of a pair of Horizontal direct action propeller engines of D=72, S=36 inches, k=4.5.

 $W = 4.5 \times 72^{2} / 36 = 139968$ lbs. for one cylinder, multiplied by 2=279936 lbs. the weight required.

For trunk engines must be taken the largest diameter.

Practical Thickness in Decimals of an Inch of Good Plate Iron in Steam-boilers, Single Riveted.

P = steam pressure in pounds per square inch above atmosphere.

Press.	Diameter of Boiler in Inches.															
P.	10	15	20	25	30	35	40	50	60	70	80	90	100	120	150	200
										_						
10	.10	.10	.11	.11	.12	.12	.13	.13	.14	.14	.15	.15	.15	.16	.17	.20
15	.10	.10	.11	.12	.13	.13	.13	.14	.15	.15	.16	.18	.19	.19	.22	.25
20	.11	.11	.12	.12	.13	.14	.14	.15	.16	.17	.18	.20	.20	.22	.26	.30
25	.11	.12	.12	.13	.14	.15	.15	.16	.18	.19	.20	.22	.23	.25	.30	.35
30	.12	.13	.13	.14	.14	.15	.16	.18	.19	.20	.22	.24	.25	.28	.33	.40
40	.12	.13	.14	.15	.16	.16	.18	.20	.22	.24	.26	.28	.30	.34	.40	.50
50	.13	.14	.15	.16	.18	.18	.20	.22	.25	.28	.30	.33	.35	.40	.47	.60
60	.14	.14	.16	.17	.19	.20	.22	.25	.28	.32	.34	.37	.40	.46	.55	.70
70	.14	.15	.17	.18	.20	.22	.24	.28	.31	.35	.38	.42	.45	.52	.60	.80
80	.15	.16	.18	.20	.22	.23	.26	.30	.34	.38	.42	.46	.50	.58	.70	.90
90	.15	.17	.19	.21	.24	.25	.28	.32	.37	.42	.46	.50	.55	.60	.77	1.0
100	.15	1.18	.20	.22	.25	.27	.30	.35	.40	.45	1.50	.55	.60	.70	.85	1.1
$120 \\ 150$.16	.19	.22	.25	.28	.31	.34	.40 .47	.46	.52	.58	.60	.70	1.0	1.0 1.2	1.3 1.6
200	1.11	.22	$\begin{bmatrix} .26 \\ .30 \end{bmatrix}$.30	.30	.45	.50		.70	.60	$\begin{bmatrix} .70 \\ .90 \end{bmatrix}$	3 0	1 7	1.3	1.6	2.1
200	11.20	1.20	1.50	.55	1.40	1.40	1.00	1.00	1.10	.80	1.50	1.0	1 1.1	1,0	1.0	4.1

Punching Iron Plates.

To punch iron plates of from $\frac{1}{4}$ to 1 inch thick requires 24 tons per square inch of metal cut; that is, the circumference of the hole multiplied by the thickness of the plate is the area cut through.

Letters denote.

d = diameter of the punch or hole. D = diameter of the hole in the die.

t =thickness of the iron plate. All dimensions in 16ths of an inch.

W = weight or force in pounds required to punch the hole.

 $W=660 \ t \ d$. $D=d+0.2 \ t$. Example 1. An iron plate of t=6 sixteenths of an inch thick, and the hole to be d=12 sixteenths in diameter. Required the force W=?

 $W=660\times6\times12=47520$ lbs., the answer. Example 2. Under the same conditions require the diameter D=? of

the die.

 $D=12+0.2\times6=13.2$ sixteenths.

Example 3. Required the diameter of piston for a direction action steam punch, for the plate and hole as in example 1, pressure of steam to be 50 lbs. per square inch.

Force $47520=A \times 50$ of which area of piston will be $A = \frac{47520}{50} = 950.4$ square inches, which answers to a diameter of 34.8, say 36 inches.

Shearing Iron Plates.

It requires the same force per section cut, for shearing as for punching, namely, 20 to 24 tons per square inch. If the shears are good, sharp, and

well adjusted, 16 tons may be sufficient.

When the cutters in the shears are inclined to one another, the area cut, will be the square of the thickness of the plate multiplied by half the cotagent for the angle of the shears. Let v=angle of the shears, Wand t same as for punching. $W = 88 t^2 \cot v$.

Example 4. What force is required to cut a half inch plate t=8 sixteenths with a pair of shears forming an angle of $v = 12^{\circ}$? Cot. 12° = 4.7.

 $W = 88 \times 8^2 \times 4.7 = 26470$ lbs.

Atmospheric Columns.

Water=33.95 feet. 2.3 feet for 1 lbs. per square inch. Seawater=33.05 ft. 2.23 Mercury at 60°=30 inches. 2.05 inches, Atm. air=28183 feet. 1912 feet,

Atmospheric air Required for each.

Blacksmith's forge, - - 100 to 200 Charcoal forge, - - - 400 to 500 Finery forge, - - - 800 to 1000 Charcoal furnace, - - 1000 to 3000 Anthracite furnace - - 2000 to 5000

Cubic feet per minute.

Cupola.

In a cupola of 3 feet 4 inches diameter, and 10 feet high, can be melted down 1000 lbs. of cast iron, 200 lbs. of bitumninous coal per hour, with a blowing machine of 4.5 horses making 1700 cubic feet of air per minute into a pressure of 2.25 inches of mercury at which the temperature of the blast will be about 70° Fah.

Steam-boiler Explosions.

The steam-boiler is a reservoir of work. Each unit of heat in the steam and

water is equivalent to a work of 772 footpounds.

The steam-table gives the units of heat per cubic foot, or per pound, in the steam and water at different temperatures and pressures. Work is the product of the three simple elements force F, velocity V, and time T, or K = FVT,

when the force of the work will be $F = \frac{K}{VT}$. When the pressure in any part

of a steam-boiler is suddenly removed, the entire work in the steam and water is at the same time started with a velocity proportionate to the removed pressure. The steam and water, in the form of a foam, strike the sides of the boiler, by which the work is suddenly arrested. If the time of arresting the work is infinitely small, we see from the above formula that the force of the work will be infinitely great, and thus the boiler explodes.

Steam-boiler explosions are caused in various ways, namely:

1st. By long use boilers become corroded and, from neglect, give way in some

unexpected place.

2d. The general construction with staying and bracing of steam-boilers is often very carelessly executed and results in explosion. This kind of explosion is often indicated, long before the accident occurs, by leakage of the boiler; when the engineer, not suspecting the approaching danger, limits its remedies generally to efforts to stop the leak. The leakage from bad calking, or packing, is easily distinguished from that of bad or insufficient bracing. In the latter case the fire ought to be hauled out, the steam blown off, and the boiler secured with proper bracing.

3d. Explosion is sometimes caused from low water in the boiler, but more rarely than generally supposed. When the fire-crown and tubes, subjected to a strong heat and not covered with water, the steam does not absorb the heat fast enough to prevent the iron from becoming so hot that it cannot withstand

the pressure, but collapses from weakness.

4th. Steam-boilers often burst by strain in uneven expansion or shrinkage,

occasioned by the fire being too quickly lighted or extinguished.

5th. It is a very bad practice to make boiler-ends of cast-iron, composed of a flat disc of from two to three inches thick, with a flange of from one to two inches thick, with cast rivet-holes. The first shrinkage in the cooling of such a plate causes a great strain, which is increased by riveting the boiler to it. Any sudden change of temperature, therefore, either in starting or putting out the fire, might crack the plate and thus occasion an explosion. Such accident may be avoided by making the cast-iron ends concave and of even thickness.

6th. In cold weather, when the boilers have been at rest for some time, they

may be frozen full of ice: then, when fire is made in them, some parts are suddealy heated and expand, whilst other parts still remain cold, causing an undue strain, which may also burst the boilers. Such accident can be avoided by a

slow and cautious firing.

7th. Sometimes a great many boilers are joined together by solid connections of cast-iron steam-pipes, which expand when heated, whilst the masonry enclosing the boilers contracts. Should such a steam pipe burst from expansion or shrinkage, explosion will likely follow in all the connected boilers, of which numerous examples have occurred. Such accident may be avoided by making the connection elastic, or free to expand or contract without moving the boilers.

Steam-boiler explosion is thus not always caused by the pressure of steam alone, but often by the expansion and contraction of the materials of the boiler. A steam-boiler which is perfectly safe with a working pressure of 200 lbs. may

explode with a pressure of 20 lbs. to the square inch.

The bursting of a boiler is a preliminary process to explosion. A boiler may burst without exploding. A boiler full of steam may burst, but never explode.

It is the work in the heated water which makes the explosion.

The sudden disturbance in the water by the forming of foam generates a high heat, and consequently a corresponding high steam-pressure is formed over the original pressure, and thus causes a disastrous explosion.

It is evident from the results of explosions that a much higher pressure had

been acting than the normal working pressure.

2

Destructive Work of Steam-boiler Explosion.

When a steam-boiler explosion takes place, the enclosed water is resolved into one volume of boiling hot water, and one volume of stcam, as follows:-

Notation of letters prior to explosion.

W' = weight in pounds of the water under full steam pressure in the boiler.

w'= pounds of water evaporated in the explosion. h = units of heat per pound in the water W'.

H = units of heat per pound in the steam of pressure P.

H'= units of heat per cubic foot in the steam P

P =pressure of steam in pounds per sq. in. V =volume coefficient of steam.

Then

$$w' = \frac{W' H (h - 180.9)}{824.8}.$$

The destructive work K will be in footpounds.

$$K = \frac{W' H P}{5.728 H' V} (h - 180.9)(V - 1)(2.3 \log P - 1.6848298).$$

The number which expresses the destructive work of an ordinary steamboiler explosion in footpounds is so large as to be inconceivable to the mind; for which it is proposed to express explosions by a larger unit, as workmandays, of 1980000 footpounds each, or 2564.75 units of heat. (See page 262.)

The workmandays of explosion will be

$$k = \frac{W' H P (h - 180.9)(V - 1)(23 \log P - 1.6848298)}{11341440 H' V}.$$

Example.—In the explosion at CORNELIUS & BAKER'S, Philadelphia, April 25, 1864, the boilers contained about W' = 14750 lbs. of water; the steampressure P = 80 lbs., H = 1177.05, H' = 223.82, V = 328.08, and h = 282.78. Required the workmandays of the explosion.

$$k = \frac{14750 \times 1177 \cdot 05 \times 80(282 \cdot 78 - 180 \cdot 9)(328 \cdot 08 - 1)(2 \cdot 3 \times \log \cdot 80 - 1 \cdot 6848298)}{11341440 \times 223 \cdot 82 \times 328 \cdot 08} =$$

149.63 workmandays; or 150 men in one day could do the work of the explosion. The destructiveness of an explosion is thus proportioned to the quantity of water and units of heat in the boiler. The steam in a boiler, prior to the explosion, does very little or no damage in the explosion. The work concentrated in a given volume of steam expanded into the atmosphere is

$$K = CH'$$
 (0.1518 log. $P - 0.1771987$). 4
 $C = \text{cubic feet of steam in the boiler}$.

Precaution against Fire on Steamboats.

Each steamer should have three buckets for every 100 tons measurement. plus 10 buckets. That is, a steamer of 800 tons should have $8 \times 3 + 10 = 34$ buckets. Also one axe for every 5 buckets.

U. S. Steam-boilers Inspector's Rule for Strength of Boilers.

Multiply one-sixth (1/6) of the lowest tensit strength found stamped on any plate in the cylindrical shell, by the thickness expressed in parts of an inch of the thinnest plate in the same cylindrical shell, and divide the product by the radius or half the diameter of the shell expressed in inches, and the quotient will be the steam pressure in pounds per square inch allowable in single riveted boilers, to which add twenty per centum for double riveting.

S = breaking.strain in pounds per square inch stamped on the plate.

t =thickness of the plate in fraction of an inch.

D = diameter of the boiler in inches.

P = steam pressure in pounds per square inch.

$$P = \frac{St}{3D} \qquad D = \frac{St}{3P} \qquad t = \frac{3DP}{S} \qquad S = \frac{3DP}{t}$$

SUPERHEATED STEAM.

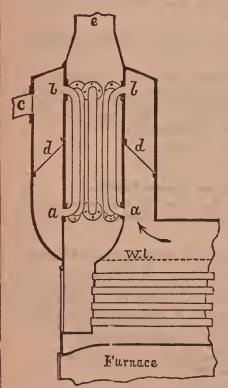
The Author's experience in superheated steam has been sufficient to convince him of its great importance. It appears that in order to utilize the maximum effect of steam or at least to attain the maximum quality of expansion, it is not necessary to overheat it after a pure steam is formed, that is, when all the small particles and bubbles of water are evaporated. Water which accompanies the steam in such a form has the same temperature as that due to the surrounding steam pressure, prevents it to vapories; but when it passes through the superheating apparatus the temperature is greatly increased while the pressure remains the same because it being in connection with the steamroom in

the boiler allows the water to vaporise and a pure steam may be formed. If steam with particles of water is admitted into the cylinder part of the stroke and then allowed to expand, it is generally found that the end pressure does not come up to that due by theory, from which it has been pronounced that the expansive quality of steam does not follow that of a presser and that steam has condensed during the stroke: but if we perfect gas, and that steam has condensed during the stroke; but if we knew the cubic containt of all the particles of water and subtracted that from the cubic containt of the steam it might be found that its expansive

quality is not so far from that of a perfect gas. It appears also that the expansive quality is diminished by overheating pure steam.

The small particles of water contain a great deal more caloric per volume than the surrounding steam, consequently when admitted into the condenser a good vacuum cannot be formed so well as with pure It is therefore of great importance to pay particular attention to the superheating of steam, otherwise economy by expansion will not be realized to the extent herein given by formulas and tables. It is also of great importance for expansion that the piston and steam valves are perfectly tight.

SUPERHEATING APPARATUS.

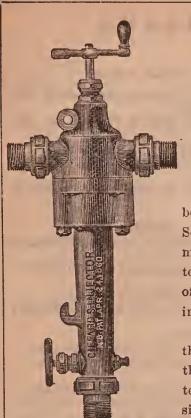


The accompanying figure represents a superheating apparatus such as the Author has built it in Russia, and is found to answer exceedingly well. The figure is a section of the forend of an ordinary tubular boiler with steamdrum and uptake. The chimney is made a great deal wider in the steamdrum and contracted to the usual size at e, of 0·16 times the area of the firegrate; if a strong fan blast is applied it may be better to contract it to 0·11. In the inside of the chimney are placed a number of copper tubes a, a, b, with flanges screwed to the side; the area of these tubes should be about four times that of the steamning c. In four times that of the steampipe c. In the steamdrum is riveted steamtight a conical plate d, d, so that the steam cannot pass to the top without passing the superheating pipes. This superheating apparatus is in successful operation in three first class passenger steamers on the River Volga in Russia, each of 500 actual horses, and one in a steamer of 100 actual horses on the Black Sea.

The steamdrum can be placed around the chimney separately from the boiler and the steam led either above or below the plate d, d, by pipes from the steam-

room, as may suit the circumstances.

This superheating apparatus may also be well suited for locomotives.

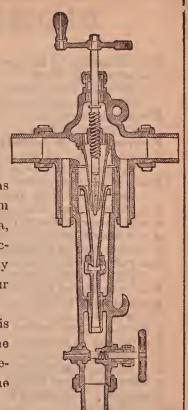


THE GIFFARD INJECTOR,

Sellers' Patent.

The following table has been furnished by William Sellers & Co., Philadelphia, manufacturers of this injector. It gives the quantity of water injected per hour in cubic feet.

The first column No. is the size or diameter of the throat in French millimeters. The last column is the size in 16ths of an inch.



Capacity and Size of Giffard's Injector.

Size	Size Pressure of steam in pounds per square inch above atmosphere. S														Size
No.	10	20	30	40	50	60	70	80	90	100	110	120	130	150	_
	_														
2	8.3	9	9.7	10.4	11.1	11.8	12.5	13.2	13.9	14.6		16.0	16.7	18.1	1.26
3	19.3	21.0	22.8	24.6	26.3	28.1		31.6			37.0	38.7	40.5	44.1	1.89
4	36.6	39.6	42.7	45.9	49.0	52.1	55.3	58.4	61.6	64.7	67.8	71.0	74.1	80.4	2.5
5	57.6	62.5	67.4	72.3	77.2	82.2	87.1	92.0	96.9	_	107	112	116	126	3.6
6	83.5	90.6	97.7	105		119	126	133		147	155	162	169	183	3.78
7	114	124	133	143	153	162	172	182	192	201	211	221	231	250	4.41
8	149	162	174	187	200	213		239	251	264	277	290	303	328	5.04
9	189	205	221	237	254	270.		302	318	334	351	367	383	415	5.67
10	234	254	274	294	313	333	353		393	413	433	453	473	513	6.30
12	337	366	395	423	452	481	510		567	596	625	654	682	740	7.56
14	451	491	531	571	611	651	691	731		811	851	891		1011	8.80
16	600	651	703	78±		857	908			1062		1164		1318	10.1
18	760	825	890							1344		1474		1669	11.3
20	939	1019	1099	1179	1259	1339	1420	1500	1590	1660	1740	1820	1900	2061	12.6

Method of Working the Injector.

FIRST.—See that the steam-plug is closed down, and waste-valve stem is raised. Second.—Admit steam from boiler to Injector, which should cause the water to flow from the waste pipe.

THIRD.—Turn up the steam-plug until the waste valve can be closed without

causing the Injector to cease working.

FOURTH.—Turn up the steam-plug to increase the delivery, and down to decrease it. When this Injector has to lift its supply water, the steam valve between the Injector and boiler must be opened very slowly, until the water flows out of the waste pipe.

N. B.-A failure to work will always be indicated by an escape of steam and

water from the waste check attached to check valve in water-supply pipe.

BLOWING MACHINES.

Letters denote.

D = diameter in inches, of blowing cylinder double acting.

S =stroke in feet, t = part of the stroke S under which the air compresses from the atmospheric density to that in the reservoir.
 F = mean resistance in pounds per square inch of the air on the

cylinder piston. P =pressure in pounds per square inch of the blast in the reservoir. C = cubic feet of air of atmospheric density, delivered from the blow-

ing cylinder to the reservoir per minute.

H = actual horse power required to work the blowing engine, including 13 per cent. for friction.

d = diameter of blast pipe in inches.

n = number of revolutions or double stroke per minute.

A = area of supply valve to the blowing cylinder in square inches, at each end of cylinder.

p =vacuum in pounds per square inch, on the supply side of the cylinder

piston, which should not exceed 0.1 lbs.

V =velocity of the blast through the tuyeres in feet per second. v =velocity of the air through the supply valve A, in feet per second, which should not exceed 100 feet.

a =area of the orifice or tuyeres in square inches. h =height of mercury in inches, in the gauge on the blast reservoir. L =length of the blast pipe in feet from the receiver to the tuyeres.

k =volume coefficient, see Table. t =temperature Fah. of the blast caused by compression or heating. Example 1. Formulæ 8. For an Anthracite blast furnace is required 4000 cubic feet of air per minute, under a pressure of 6 inches mercury. Required the horse power necessary for the blowing machine? The effectual resistance F=2.365 lbs. see Table. Assume the vacuum to be v = 0.09 lbs.

We have
$$H = \frac{4000 (2.365 + 0.09)}{198} = 49.6$$
 horses.

Example 2. Formulæ 10. Suppose the blast cylinder to be D=144 inches diameter with S=15 feet stroke. Required the number of double strokes per minute n=?

$$n = \frac{96 \times 4000}{144^2 \times 15} = 12.3$$
 the answer.

Example 3. Formulæ 9. Under the above conditions, require the area of the supply valves A=? when the velocity v=105 feet, per second.

$$A = \frac{144^2 \times 15 \times 12 \cdot 3}{40 \times 105} = 911$$
 square inches.

Capacity of Blast Reservoir should not be less than the following proportions, but more is better.

For one single acting cylinder, 20 For one double acting cylinder, 10 times the capacity of one cylind'r. Two double act. cyl. cranks at 90° 5 One double acting cylinder, same as two single acting. The more

cylinders the less capacity required for blast reservoir.

$$V = 246\sqrt{h(1+0.00208t)},$$

$$P = 14.7(k-1),$$

$$t = 32+493(k-1),$$

$$t = 33.55 P+32,$$

$$k = \frac{P}{14.7},$$

Formulas for Blowing Machines.

$$l = \frac{Sh}{30+h}, -1$$

$$P = 0.49h, -2$$

$$C = \frac{D^2 Sn}{96}, -3$$

$$H = \frac{C(F+p)}{19000}, 7$$

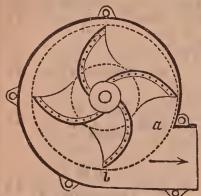
$$U = 350 \sqrt{p} - 12$$

$$U = \frac{D^2 Sn}{40 A}, -13$$

Table for Blast and Blowing Machines.

	d temperat.		in inches.	Pressure I	os. sq inch.	Stroke.	Velocity.				
k	t	water.	. h	P	F		V				
1.002	330	1	0.073	0.036	0.032	0.0024	72				
1.005	34.2	2	0.147	0.079	0.063	0.0049	102				
1.007	35.2	3	0.220	0.108	0.095	0.0073	125				
1.010	37	4	0.294	0.144	0.128	0.0097	144				
1.012	38	5	0.368	0.180	0.159	0.0121	161				
1.015	39.5	6	0.441	0.216	0.191	0.0145	176				
1.020	42	8	0.588	0.288	0.253	0.0192	204				
1.025	44.5	10	0.736	0.360	0.309 "	0.0239	228				
1.030	47	12	0.884	0.432	0.379	0.0287	249				
1.035	49.5	14	1.030	0.503	0.437	0.0334	269				
1.043	53.5	17	1.250	0:612	0.531	0.0400	297				
1:051	57.5	20	1.470	0.719	0.623	0.0467	322				
1.062	63	24	1.766	0.863	0.745	0.0556	352				
1.074	69	28	2.060	1.008	0.865	0.0643	381				
1.082 -	73	31	2.281.	1.116	0.955	0.0706	401				
1.091	77.3	34	2.501	1.223	1.043	0.0769	420.				
1.100	82	37	2.720	1.332	1.130	0.0833	438				
1.109	86.5	46	3.000	1.470	1.205	0.0908	460				
1.116	90	47.5	3.500	1.715	1.431	0.1045	496				
1.132	98	54.3	4.000	1.961	1.636	0.1178	530				
1.165	.114.5	67.7	5.000	2.450	2.010	0.1431	593				
1.200	132	81.4	6.000	2.941	2.365	0.1667	650				
1.265	164.5	108.5	8.000	3.925	3.088	0.2105	751				
1.400	232	163	12.00	5.900	4.389	0.2859	918				
1.500	282	203.7	15.00	7.375	6.875	0.3333	1077				
1.625	344.5	254.6	18.75	9.217	8.831	0.3846	1393				
1.750	407	305.5	22.49	11.06	10.67	0.4285	1590				
1.875	469.5	356.4	26.24	13.90	11.64	0.4666	1760				
2.000	532	407.4	30.00	14.75	12.50	0.5000	1955				
			i								

FAN OR VENTILATOR.



Fans constructed as the accompanying figure have been found by the Author who has made several of them, to be the most effective.

The vanes are each one quarter of an arithmetical spiral with a pitch twice the diameter of the fan, that is, each vane should be constructed in an angle of 90° from centre to tip. Length of fan to be from to to the diameter. Inlet to be half the diameter of the fan. Number of vanes to be not more than six, and not less than four. Six vanes work softer and better, but they give no better effect than four.

The housing should be an arithmetical spiral with sufficient clearing for the fan at a, and leaving a space at b about $\frac{1}{8}$ of the diameter. Fans of this construction make no noise.

Letters denote.

d = diameter of fan in inches. l = length

A = area in sq. in. of blast pipe, to be as straight as possible.

L =length in feet, cond =length in feet

C = cubic feet of air delivered per minute.

h = inches of mercury.

v =velocity in feet per second through a. k =volume coefficient, see Table, page 441.

n = revolutions of fan per minute.

H= actual horse power required to drive the fan.

Formulas for Fans.

$$h = \frac{d n^{2}}{50000000} \sqrt{\frac{d l}{25 a + d l}}, \qquad 1 \qquad v = \frac{n \sqrt{d}}{28 \cdot 86} \sqrt{\frac{d l}{25 a + d l}}, \qquad \bullet$$

$$H = \frac{d l h n}{24000}, \qquad 2 \qquad n = \frac{24000 H}{d l h}, \qquad 7$$

$$h = \frac{24000 H}{d l n}, \qquad 3 \qquad C = \frac{v a k}{2 \cdot 6}, \qquad 8$$

$$v = 244 \sqrt{h} \qquad 6$$

$$A = a \sqrt{L} \qquad 6$$

Example 1. A fan of d=36 inches diameter, l=12 inches, making n=725revolutions per minute, area of tuyere being a=25 square inches. Required the density of the blast in inches of mercury h=1

Formulæ 1.
$$h = \frac{36 \times 725^{\circ}}{50000000} \sqrt{\frac{36 \times 12}{25 \times 25 + 36 \times 12}} = 0.242 \text{ inches.}$$

Example 2. Under the same conditions require the cubic containt of air delivered per minute, C=1 k=1.01 the nearest in the Table.

Formulæ 9. $C=94\times25\times1.01/0.242=1167.7$ cubic feet. Required the horse power H=?

Formulæ 2.
$$H = \frac{36 \times 12 \times 0.242 \times 725}{24000} = 3.16 \text{ horses.}$$

BLAST OR IRON FURNACES.

It is almost impossible to set up the many variable circumstances connected with the performance of Blast Furnaces, into a table form. The datas herein given are deduced to an average from the performances of a great many furnaces both in America and Europe.

The accompanying Tables are so arranged that the numbers in Table I., multiplied by the numbers in Table II., gives the corresponding charge of Iron ore, lime stone, coal, and the produce of pig iron in pounds per 24 hours, with the consumption of air in cubic feet per minute.

Table II. contains the effective capacity of blast furnaces in cubic yards.

Example. It is required to construct a blowing machine for an Anthracite blast furnace of 12 feet diameter of boshes, height of stack 45 feet to

cite blast furnace of 12 feet diameter of boshes, height of stack 45 feet, to be worked with hot blast. Required the produce of pig iron per 24 hours, cubic feet of air per minute and actual horse power of the blowing engine?

Produce of pig iron 155 Table I.×123 Table II.=19065 lbs. or 8.5 tons per

24 hours.

Consumption of air $20 \times 123 = 2460$ cubic feet per minute. Suppose the blast to be blown into the furnace at a pressure of P=2.94 lbs., vacuum in the supply side in cylinder to be p=0.07 lbs. we shall have the required actual power.

 $H = \frac{2460 (2.36 + 0.07)}{2400 (2.36 + 0.07)} = 30.2$ horses. Forumlæ 8, p. 287.

Table I. Iron or Blast Furnaces.

The unit bein	g the capacity	Charge and produce per 24 hours. Ai						
of the F	ŭrnace in yards.	Iron Ore.	Pig Iron.	Pig Lime		per minute.		
	•	Ibs.	lbs.	lbs.	lbs.	cub, feet.		
Soft charcoal	{Cold blast,	535	215	196	400	24		
	Warm blast,	700	292	256	350	19		
Hard charcoal	{Cold blast,	670	270	245	400	24		
	Warm blast,	875	365	320	350	19		
Goke	{Cold blast, Warm blast,	26 8 3 50	108 146	98 128	515 397	26 20		
Bituminous	{Gold blast,	252	101	92	515	24		
	Warm blast,	327	136	120	397	19		
Authracite	{Gold blast,	287	115	105	515	26		
	Warm blast,	373	155	137	597	20		

Capacity and Dimensions of Iron Furnaces. Table II.

Diameter of			Height of stack in feet.							
Bashes in ft.	25	30	35	40	45	50	55	60		
8	40	44	47	51	54	58	62	65		
. 9	50	55	60	64	69	73	78	83		
10	62	68	74	79	75	91	96	102		
11	75	82	89	96	103	110	117	123		
12	90	98	106	114	123	130	139	147		
13	105	115	125	134	144	153	163	172		
14	121	133	145	155	167	178	189	200		
15	140	153	166	178	191	204	217	230		
16	160	174	189	203	217	232	247	261		
17	280	197	213	229	245	262	279	295		
18	202	220	239	257	275	293	312	330		

ON THE PARABOLIC CONSTRUCTION OF SHIPS.

The water-lines, frames, areas of frames and water-lines, and the displacement of a vessel, are all parabolas of different orders and power, with the vertex in the greatest cross-section or dead flat frame.

The accompanying tables contain ordinates for different parabolas, with the corresponding areas, displacement, centre of gravity, meta-centre, tangent for the

angles of resistance and inflection.

The lengths from \mathfrak{M} to the stem and stern, and the draft from the water-line to the keel, are each divided into eight equal parts, at which the ordinates are

calculated.

The first column in the tables contains the exponent n for the parabolas. higher the exponent is, the fuller will the vessel be. The power q of the parabolas makes hollow lines when greater than 1, and the higher the power is, the hollower will the lines be. The power of the water-lines should never be less than 1.

The top-line contains the number of the ordinates, which are counted from the

stem or stern to M, or from the keel to load-water line.

The half breadth of the beam is the unit for the ordinates of the load-water

line, and for the frame M.

It requires some experience in selecting the proper exponents and powers, but let us suppose, for example, the exponent n=2 and the power q=1, for the forward load-water line of a vessel of length l=100 feet from \mathfrak{M} to stem, and the beam B=30 feet. Then multiply 15 feet by the ordinates in the table, and the products will be the corresponding ordinates for the water-line, the whole area of which will be (see column a), $a = 100 \times 30 \times 0.6666 = 1999.99$, or 2000 square feet. The centre of gravity of that area will be (see column e)—

$$e = 100 \times 0.3750 = 37.5$$
 feet from **22.**

Now let us select the exponent n=5 and the power q=1 for the frame \mathfrak{A} , and let d=12 feet depth from the water-line to keel. Then multiply 15 by the ordinates of that exponent and power, and the products will be the corresponding ordinates for the frame M. The area of the frame M will be (see column a),

$$X = 30 \times 12 \times 0.8333 = 299.988$$
, or 300 square feet.

The depth of the centre of gravity of \mathfrak{M} will be (see column e)—

$$e = 12 \times 0.4286 = 5.14$$
 feet under the load-water line.

Let us select the exponent n=2.25, and power q=1 for the forward displacement. Then multiply $\mathfrak{M}=300$ square feet by the ordinates for that exponent and power, and the products will be the corresponding areas at each frame. The forward displacement will then be (see column a)-

$$D = 300 \times 100 \times 0.6923 = 20769$$
 cubic feet.

The distance from \mathfrak{W} to the centre of gravity of the forward displacement will be (see column e), $e = 100 \times 0.3823 = 3823$ feet.

The operation is precisely the same for the after-body of the vessel, only that

fuller exponents are generally selected.

After the lines are laid out as described, the divisions of the frames are made as

required in the building of the vessel.

For simplicity in our illustration, let us suppose that the exponents and powers are respectively the same for the after-body of our vessel, and 100 feet from M to stern; then the displacement will be $D = 20769 \times 2 = 41538$ cubic feet, the whole length $L = 100 \times 2 = 200$ feet. The height of the meta-centrum will be—

$$m' = \frac{L b^3 m}{D} = \frac{200 \times 15^3 \times 0.3021}{41358} = 4.9305$$
 feet.

The coefficient m = 0.3021 is taken for the exponent and power of the load-water line in column m.

The tangent for the mean angle of resistance to the vessel in motion in water will be-

tang.
$$v = \frac{\mathcal{X} t}{2 l' d} = \frac{300 \times 1.447}{2 \times 100 \times 12} = 0.18087 =$$

tang. 10° 15′, the mean angle of resistance.

The coefficient t = 1.447 is taken for the exponent and power of the displacement in column t.

The whole area of the load-water line is $\mathbf{a} = 2000 \times 2 = 4000$ square feet. The depth of the centre of gravity of the whole displacement will be—

$$e = \frac{d}{2\left(2 - \frac{D}{a \, d}\right)} = \frac{12}{2\left(2 - \frac{41358}{4000 \times 12}\right)} = 5.28 \text{ feet, under the wa-}$$
 [ter-line.]

To Calculate the Ordinates for the Frames.

Having given the half area of the frame, the ordinate of the load-water line and the depth d, multiply the ordinate by the depth, and divide the given area by the product, which will give a decimal fraction. Find this fraction in the columns a, or area in the tables for frames, multiply the ordinates of that area by the given ordinate for the load-water line, and the products will be the corresponding ordinates for the frame,

Example. The given area = 64.5 square feet, the ordinates of the water-line = 6 feet, and the depth = 18 feet. Then $\frac{64.5}{18 \times 6} = 0.599$. Find this area in table

q=1 for frames, and it will be found to correspond nearly with the ordinates of exponent n=1.5, which will give a full line; but if it is desired that the frame should be a reverse curve, then select the area of higher power—for instance, in table q=1.25, the area 0.599 corresponds nearly with the ordinates of the exponent n=1.75, in which case the frame will reverse at $18 \times 0.77 = 13.86$ feet from the water-line.

To lay down the Ordinates of all the Water-lines

and frames on the drawing direct from the tables without calculation.

Construct a scale or diagram like that on Plate VII., divided into 100 equal parts

each way.

Set off half the beam b of the same scale as the drawing, from B toward C, say at a, join a with A, then the line a A, measured from the base A B, is the scale for all the ordinates in the load-water line and greatest cross-section M. Let us select the exponent n=2.5 and power q=1.5 for the forward load-water line, which will be slightly hollow and reverse at $0.782 \times l'$ from M. Measure off the ordinates from the corresponding number on the base A B to the line a A, and set them down on the drawing.

Set off the ordinates from B toward a, and join them with A; then each line forms a scale for the ordinates of the corresponding frames. The fourth ordinate $\sqrt{7469}$ will be the line g h, and the incline line 4 is the scale for the fourth frame.

Turn the scale round, and set off the half beam b from D toward A; join it with C, and proceed in the same way for the after-body of the ship, only select higher exponent for the aft load-water line.

Scales or diagrams like that on Plate VII., but of larger size, have been printed,

and can be had in Philadelphia.

To find the Exponents and Powers

from the lines of a vessel constructed without regard to the parabolic method.

Divide the lengths from \mathcal{W} to the stem and stern, and the depth from the loadwater line to the keel, each into eight equal parts, as before stated. Suppose half the beam of the vessel is b=20 feet. Measure the 2nd and 4th ordinates in the load-water line, say 6.68 feet and 15.31 feet, respectively. Divide those ordinates by the half beam 20 feet, which will give 0.334 and 0.765. Find these ordinates in the tables, which will be found to correspond with exponent n=3 and power q=2. The area of the water-line will be, supposing the length to be 130 feet from \mathcal{W} to stern, $130 \times 40 \times 0.6428 = 3342.56$ square feet.

All the other exponents and powers are found in the same way. For the displacement, divide the ordinate areas of the frames by W and find the corresponding ordinates in the tables, and thus all the properties of the displacement a e

found by the parabolic method.

Recording Formula.

The form of any vessel may be recorded by one general formula, as follows-

$$\frac{W.n.q.}{D.n.q.} l\left(\frac{L.B.d.}{\cancel{x}}\right) l'\left\{\frac{W.n.q.}{D.n.q.}\right\}$$

The first part, $\frac{W.n.q.}{D.n.q.}$ l, represents the form of the after-body of the displacement.

W.n.q. = exponent and power of the load-water line, D.n.q. = exponent of the

displacement, and l = length from M to stern-post.

The middle part, $\left(\frac{L.B.d.}{\cancel{\cancel{M}} n.q.}\right)$, represents the length, beam and depth of the displacement, $\cancel{\cancel{M}} n.q.$ the exponent and power of the frame $\cancel{\cancel{M}}$.

The last part, $l' \left\{ \frac{W.n.q.}{D.n.q.} \right\}$, represents the fore-body of the displacement. The recording formula is not intended for arithmetical operation.

Recording Formula of the Ironclad "Dictator."

$$\frac{W5.5 \times 1.75}{D4.75 \times 2.25} 96 \left(\frac{240 \times 42 \times 16}{20 \times 2.75 \times 0.5}\right) 144 \left\{\frac{W2.75 \times 1.5}{D3 \times 2}\right\}$$

From these data a similar vessel to the hull of the "Dictator" can be constructed by any one familiar with the parabolic method.

Sailing-Yacht.

A well-proportioned sailing-yacht may be set up as follows:

$$\frac{W3\times2}{D2\times2}\right\}30\left(\frac{80\times16\times8}{203\times4}\right)50\left\{\frac{W2.75\times2}{D2\times2}\right.$$

The Formula for the Steam-Propeller on Plate X. is-

Angles of the Lines.

The angle of entrance in the stem, or delivery in the stern, of any water line, is-

$$\tan v = \frac{b \, n}{l \, q}.$$

The angle of the line, at any distance y from \mathfrak{M} , is—

$$\tan v = \frac{b \, n \, q \, y^{n-1}}{l^n} \left(1 - \frac{y^n}{l^n} \right)^{q-1}.$$

The mean angle of resistance or delivery of the displacement is-

$$\tan v = q^2 b \ n^2 \int \left(1 - \frac{y^n}{l^n}\right)^{2q-2} \frac{y^{2n-2}}{l^{2n}} dy.$$

The column t' in the tables is calculated from this formula.

The distance y from \mathfrak{M} , to the point of inflection, is—

$$y = \sqrt[n]{\frac{n-1}{n \, q - 1}}.$$

Explanation of Tables.

Table I. gives the greatest buoyancy and stability of the displacement with the

least proportionate resistance.

Tables II. to IX., inclusive, give hollow lines of which those with high power and low exponents are too hollow for the load-water line, but the high exponents with high power will suit for the aft load-water line.

Tables X. to XIII. should not be used for water-lines, but for frames.

Tables XIV. to XIX. are for frames exclusively. Table XX. for elliptic stern and sheer of vessels.

Table XXI. contains the coefficient of displacement, or the fraction it occupies in the parallelopipedon, length, breadth and depth. For light draft and high speed the coefficient should be selected toward the corner .490, and for freight and light draft toward the corner .797. The first column \mathfrak{M} n contains the exponent for \mathfrak{M} , and the tope-line that for the displacement, supposing q=1 in both cases.

Table XXII. The first column C contains the coefficient of the vessel, for which the tabular number, multiplied by the cube root of the displacement in tons, will

give the length of the vessel in feet.

Explanation of the Plates VII., VIII., IX. and X.

Plate VII. is a scale for laying down the parabolic lines directly from the tables without calculation, as before described.

Plate VIII. illustrates the sharpness of water-lines and cross-sections. The numbers on the figures correspond with the exponent n in the first column of the

Plate IX. Fig. 1 illustrates the sharpness of full lines from Table I. Fig. 2 are cross-sections from the same Table I. Fig. 3 is a scale of displacement and draft

of water, referred to Table I., in which the exponent n (or ratio r) is taken for the areas of the water-lines. This scale also corresponds with the Formulas 6 to 9, for finding the displacement \triangleright and draft δ .

Fig. 4 is a scale for laying out the frames.

Fig. 5 is the spring or rise of beams, for which the ordinates should always be taken from the exponent 2, Table 1.

Plate X. illustrates a propeller steamer constructed on the parabolic method.

Steamship Performance.

For similar proportioned vessels the resistance is a function of \mathcal{M} M^2 , and the horse power a function of \mathcal{M} M^3 . The displacement of a vessel is a function of the cube of any linear dimension of the same, and the greatest immersed section \mathcal{M} a function of the square of any linear dimension of the displacement; consequently the $\sqrt[3]{T}$ is a function of any linear dimension, and $(\sqrt[3]{T})^2 = \sqrt[3]{T^2}$ is a function of \mathfrak{M} ; therefore, the resistance is a function of $M^2\sqrt[3]{T^2}$, and the horse power a function of $M^3 \chi^3 / T^2$.

The tables of steamship performance are calculated by this last formula, in which it is assumed that the displacement of the vessel is about one-half of the parallelo-

pipedon, and the length about eight times the beam.

$$M = \sqrt[3]{\frac{228H}{\sqrt[3]{T^2}}}$$
 $H = \frac{M^3\sqrt[3]{T^2}}{228}$ $T = \sqrt{\left(\frac{228H}{M^3}\right)^3}$

On the Form Waves, or the Wave-line.

v = velocity of the wave in feet per second. l = length of wave in feet from top to top.

h = total height in feet of the wave from top to bottom.

	Ab.	Ordinates.	Ab.	Ordinates.
$v = 1.82\sqrt{t}$, $l = 3.14h$, $h = 0.3183l$.	1	.009607	9	.59755
,	2	.03806	10	.69134
The accompanying table shows the ordinates	3	.08426	11 .	.77778
for the wave line, the abscissa or base of the line	4	.14644	12	.85355
from the lowest part to the highest, or half the	5	.22221	13	.91573
length of the wave being divided into 16 equal	6	.30866	14	.96194
parts. The ordinates are expressed in parts of	7	.40245	15	.99039
the height h.	8	.50000	16	1.0000

Notation of Letters for the Formulas.

All dimensions are in feet, square feet or cubic feet.

The Vessel.

A =area of the immersed hull.

a =area to load water-line. a =area of water-line at the draft δ .

B =breadth of beam.

b = half breadth of beam B.

d = draft of water, omitting depth of keel.

 δ = any draft less than d.

 $\delta =$ difference of draft of water, which should not be taken more than 0.25 feet for the largest, and only 0.1 for vessels of 100 tons.

d = differential.

L = length of vessel in load-water line. l = length from X to stern-post. l' = length from X to stem.

m = area of greatest immersed section.

 \widetilde{D} = displacement, cubic feet.

 $\mathbf{D} = \text{displacement forward of } \mathfrak{D}.$

 $\mathbf{q} = \text{displacement aft of } \mathbf{X}.$

 \triangleright = displacement at the draft δ .

T = displacement in tons.

 $\delta \Delta =$ differential of displacement.

Centres of Gravity.

S =distance of centre of gravity of displacement from the stern-post.

= distance of centre of gravity of q

from \mathfrak{M} . s' =distance of centre of gravity of Dfrom M.

e = centre of gravity in the tables.
e' = depth of centre of gravity of displacement under the load-water

Parabolas.

n and q =exponent and power.

 $\beta =$ any ordinate at distance y from M. r = exponent of the displacement from

load-water line to keel, supposing q=1.

Stability of the Vessel.

m = meta-centre for load-water line inthe tables.

m' = height of meta-centre above centre of gravity of displacement.

P = the real stability of a ship.

Q = momentum of stability in foot-tons.

g = height between centres of gravityof vessel and displacement when in equilibrium.

o = horizontal distance between the two centres of gravity when out of equilibrium.

o' = horizontal distance between centre of gravity of displacement when in and out of equilibrium.

z = careen-angle of the vessel.

C = coefficient of displacement, Table XXI.

Performance.

H =horse-power required to move the vessel.

M = speed in knots per hour.

R = resistance to the vessel in pounds.

t =tangent in the tables.

v = mean angle of resistance to the vessel moving in water.

V = mean angle of delivery of the aft displacement.

k = coefficient of friction in pounds persquare foot of the immersed surface of the vessel.

Surface. Coefficient, k.

For polished metallic surface, Ordinary copper sheeting, . . . 0.005 Wood, smooth-planed, . . . 0.007 Rough castings of iron or brass, . 0.009 Fouled with barnacles and sea-

Fouled with barnacles and oyster-

shells, . . .

$A = [\mathbf{a} + 2(\mathfrak{M} + dL)] \sqrt{\frac{D}{BLd}}.$

Explanation of the Formulas, with Examples.

The whole method of the Parabolic Construction of Ships is based upon the Formula 1. The formula looks very simple, but when developed into its combinations with the form of a ship, it becomes a very complicated affair, which requires a separate treatise on ship-building for proper explanation.

Example for Formula 5. The length of a vessel is L=250 feet, of which l=100 feet from \mathfrak{M} to stern-post, and l'=150 feet from \mathfrak{M} to stern. The centres of gravity of the fore and after body of the displacement have been found, as before described, to be s=48 feet aft of \mathfrak{M} , and s'=68 feet fore of \mathfrak{M} . Required, the centre of gravity of the whole displacement from the stern-post?

Formula 5.
$$S = \frac{100 (100 - 68) + 150 (100 + 48)}{250} = 116$$
 feet.

Formulas for the Parabolic Construction of Ships,

Stability and Performance.

$$R = 2.858M^{2} \left[\mathcal{Z}(0.9\sqrt{\sin^{3}v} + 0.1\sqrt{\sin^{3}V}) + \frac{A k}{\sqrt[4]{L}} \right]. \qquad 16$$

$$\tan v = \frac{\mathcal{Z}t}{l'd}. \qquad 17 \left| H = \frac{RM}{22450}. \qquad 19 \left| R = \frac{22450H}{M}. \qquad 21$$

$$\tan v = \frac{\mathcal{Z}t}{ld}. \qquad 18 \left| M = \frac{22450H}{R}. \qquad 20 \right| \text{Friction} = \frac{A k}{\sqrt[4]{L}}. \qquad 22$$

Example for Formula 8. A vessel of D=150000 cubic feet of displacement, a=10000 square feet area of load-water line at d=20 feet draft. Required, the exponent r? and how much $\delta \triangleright$ can the vessel be loaded per inch of difference of draft at $\delta=15$ feet draft?

Formula 2.
$$r = \frac{15000}{10000 \times 20 - 150000} = 3$$
, the exponent.
Formula 8. $\delta \rhd = \frac{10000 \times 1}{12} \sqrt[3]{\frac{15}{20}} = 728$ cubic feet,

which in salt water will be 728:35=20.8 tons per inch of draft at $\delta=15$ feet.

Example for Formula 10. A vessel of D=150000 cubic feet, half beam b=20 feet, l'=170 feet, n=3.5, q=2, for which meta-centre in the table is m=0.350, and l=180, n=2.5, q=2, for which m=0.277. Required, the height of the meta-centre above the cent. gr. of the displacement?

Formula 10.
$$m' = \frac{20^3}{150000} (0.350 \times 170 + 0.277 \times 180) = 5.832$$
 feet.

The momentum of stability will be, when T=150000:35=4288.8 tons, careen angle $z=10^{\circ}$, and the height between the two centres of gravity g=-1 foot, or the cent. gr. of the vessel is one foot above the cent. gr. of displacement.

Formula 11.
$$Q = 4288.8 \sin 10^{\circ} (5.832 - 1) = 3591.9 \text{ foot-tons.}$$

Divide the momentum of stability by the length of the lever upon which the force is applied to careen the vessel, and the quotient will be the force required in tons.

400	Table I. Power q = 1. Full lines.											
Exp.	1			Ordina		, ,				Meta.		Inflec
71	1	2	3	4		6	17	a WD		m	t	tion.
2.	.2344		.6094	.7500		.9375	.9814	.6666	.3750	.3021	1.333	
$\begin{bmatrix} 2.125 \end{bmatrix}$.4574	.6317	.7707	8756		.9879	.6800	.3788	.3162		The lines for these ordinates have no inflection.
2.25		.4765	.6527	.7898	.8899		.9907	.6923	.3823	.3288	1.447) cti
2.375	.2716	.4950	.6725	.8072	.9026		.9928	.7047	.3857	.3394	1.500	ıffe
2.5		.5129	.6912	.8232		.9687	.9945	.7142	.3888	.3502	1.562	o ii
2.625	.2954	.5300	.7088		.9238		.9957	.7241	.3919	.3612	1.622	n
2.75	.3073	.5466	.7254			.9779	.9967	.7333	.3948	.3688	1.682	ave
2.875		.5627 .5781	.7411 .7558			.9814	.9975	.7419 .7500	.3974	.3776 .3857	1.738	s h
3.25		.6074	.7829	.8750 .8949	.9587		.9980	.7647	.4000 .4047	.4010	1.922	ate
3.5		.6346	.8070		.9677		.9993	.7777	.4091	.4144	2.040	iii
3.75		.6600	.S284			.9945	.9996	.7894	.4130	.4263	2.166	orc
±.		.6836	.8474		.9802		.9997	.8000	.4166	.4376	2.285	S. S.
1.5	.4517	.7260	.8794	.9559		.9980	.9998	.8181	.4230	.4570	2.534	the
jā.	.4871	.7627	.9046	.9687	.9926		.9999	.8333	.4286	.4734	2.775	or
6.	.5512		.9404		.9972		.9999	.8571	.4375	.5000	3.270	88
8.		.8999	.9767	.9961		.9999	.9999	.8888	4500	.5354	4.272	ine
10. 12.		9437	.99.19	.9990		1.000	1.000 1.000	.9090	.4583 .4643	.5585 .5768	$5.265 \\ 6.275$	le]
16.		.9900	10001	9398			1.000	.9412	.4720		8.273	E
		ble I			owei					ow li		
2.		.3558		.6979			.9805		.3528	.2778	1.28	.8165
2.125		.3761	.5631	7222	.8470		.9850	.6399	.3572	.2911	1.333	.8335
2.25	.1852		.5866	.7445	.8644		.9884	.6538	.3623	.3040	1.380	.8478
2.375		.4152	.6090	.7651	.8793		.9910	.6666	.3660	.3154	1.428	.8510
2.5		.4340		.7841	.8948	.9611	.9 931	.6788	.3700	.3262	1.476	.8728
2.6 15	.2178	.4523		.8006	.9057	.9673	.9947	.6900	.3739	.3462	1.524	.8832
2.75		.4700	.6695		.9165	.9725		.7000	.3777	.3558	1.573	.8922
2.575	2595	.4837	.6876 .7048		.9260 .9350	.9768 .9805	.9968 .9976	.7094	.3814 .3850	.3548	1.622	.8993 .9055
3.25		.5362	.7365	.8704	.9487	.9862	.9985		3904	.3794	1.765	.9148
3.5		.5665	.7649	.8908	.9598	.9902	.9991	.7485	.3950	.3945	1.863	.9212
3.75		.5949	.7903	.9080	.9685	.9931	.9995		.4010	.4065	1.975	.9260
4.	.3319		.8130		.9753	.9951	.9997		.4040	.4183	2.092	.9306
4.5	.3703		.8516		.9349	.9975	.9999	.7940	.4111	.4390	2.298	.9384
5.		.7127	.8823		.9307		.9999		.4183	.4563	2.492	.9450
6. 8.	.4749	.7827 .8765	.9260		0.9965 0.9995		1.000 1.000		.4283 .4397	.4845	2.873	.9555
10.			.9710		.9999	.9999 1.000	1.000		.4502		3.635 4.515	.9694 .9787
12.	.7550			.9993			1.000		.4593		5.150	.9815
16.	.547	.9875	.9934	.9999	1.000	1.000	1.000	.9323	.4684	.5965	7.225	.9858
		le II			owe					w li	-	
2.		.2391		.6495			.9766		.3395 [1.250	.7071
2.125	.1227	.3093	.5020	.6766	.8193	.9222	.9820	.6057	.3443	.2706	1.291	.7285
2.25		.3289	.5273		.8396			.6205	.3489	.2834	1.330	.7484
2 375		.3483	.5515		.8576	.9448			.35:34		1.370	.7666
2.5	.1606	.3573	.5746		.8751	.9535			.3576	.3065	1.410	.7820
2.625		4042	.5967		.8879	.9670			.3619 .3654		1.450	.7958
2.575	.1797		.6380		.9119	.9722			.3689			.8080 .8192
3.	.1896		.6571		.9225	.9766			.3723			.8300
3.25	.2099	.4734	.6928	.8465	.9387	.9834	.9982	.7068	.3781			.8473
3.5	.2281		.7249	.8704	.9519	.9883		.7231	.3836	.3760		.8612
3.75		.5352	.7540		.9623	.9917			.3888		1.853	.8732
4.		.5652			.9705	.9941			.3932			.8838
4.5	3400	.6661	.8246		.9889	.9971			4018			.8980
6.	.4092		.9119		.9358	.9596						.9072 .9247
18.		.8536	.9653		.9994	.9999						.9451
11.		.9115				1.000						.9585
12.	.7136	.9530	.9947	.9997	.9999	1.000	1.0001					.9666
16.	.8232	.9850	.9992	.9999	1.000	1.000	1.000		4649			9735
											100	

Table IV. Power q = 1.75. Hollow lines.												10.
Exp.	1		C	rdina				Prod.	°C. gr.	Meta.	Res.	Inflec-
77	1	2	3	4	5	6	7	a WD	e	m	t	tion.
2.	.0780	.2353	.4203	.6044	.7670	.8932	.9728	.5592	.3252	.2412	1.228	.6345
2.125	.0865	.2544	.4476	.634)	.7926	.9098		.5761	.3308	.2538	1.260	.6600
2.25	.094	.2733	.4739		.8154	.9240	.9838	.5919	.3358	.2665	1.294	.6822
2.325	.1022	.2921	.4994		.8359	.9359	.9875	.6065	.34()()	.2786	1.329	.7018
2.5		.3108		.7115	.8559	.9460		.6200	.3446	.2900	1.363	.7200
2.625		.3218	.5 175		.8705	.9545	.9925	.6320	.3487	.3000	1.400	.7364
2.75 2.875	1.1269	.3476		.7545 .7738	.8851 .8989	.9617 .96 7 7	.9943 .9956	.6431	.3529	.3105	1.438	.7514
3.	.1437	.3833		.7916	.9102	.9728	.9966	.6542	.3604	.3200	1.475 1.511	.7650 .7777
3.25	.1609	.4179	.6517	.8234	.9289	.9807	.9980	.6833	.3670	.3464	1.591	.7987
3.5	.1825	.4513		.8505	.9442	.9864		.7000	.3736	.3618	1.591	.8175
3.75		.4833		.8736	.9562	.9904		.7158	.3782	.3758	1.673	
4.	.2135	.5139	.7484		.9657	.9932	.9996	.7293	.3834	.3883	1.850	.8430
4.5		.5710	.7985		.9789	.9966		.7521	.3922	.4108	2.010	.8613
5.		.6225	.8391	.9460	.9870	.9983		.7732	.4006	.4300	2.171	.8754
6.		.7096		.9728	.9951	.9996	1.000	.8050	.4129	.4610	2.500	.8989
8.		.8314		.9932	.9903		1.000	.8475	.4296	.5041	3.175	.9258
10. 12.		.9009	.9938	.9983	.9998 .9999		$1.000 \\ 1.000$.8734	.4420	.5313	3.878	.9431
16.		.9825	9930	0000	1 000	1.000	1.000	0185	.4503 .4615	5528 5821	4.550 6.050	.9533
10.		able			Powe				ollov			.0010
$\frac{1}{2}$.		.1914	.3713				.9630	.5333	.3125	.2273	1,219	.5773
$\begin{vmatrix} 2.125 \\ 2.125 \end{vmatrix}$.0610		.3990		.7667	.8976		.5504	.3160	.2415	1.242	.6038
3.25		.2271	.4260		.7920	.9136		.5664	.3189	.2541	1.273	.6292
2.375	.0738		.4523		8147	.9271	.9857	.5813	.3278	.2662	1.301	.6517
2.5	.0806	2630	.4777	.6777	.8371	.9385	.9800	.5952	.3333	.2770	1.355	.6723
2.625	.0873	.2310	.5024	.7020	.8534	.9481	.9915	.6083	.3388	.2875	1.666	.6904
2.75.	11944	.2988	.5262	.7248	.8698	.9563	.9934	.6205	.3418	.2979	1.402	.7066
2.875	.1014		.5492		.8843	.9632		.6320	.3450	.3974	1.436	.7222
3.	.1000		.5713	.7656	.8980		.9961	.6428	.35)()	.3164	1.472	.7:68
3.25	.1240	.3689	.6130		.9192	.9779 9841	.9977	.6627 .6°05	.3571	.3255	1.545	.79°8 .8175
3.5	.1394	.4028	.6512 $.6862$.8310 .8569	.9365	.9830	99.12	.6966	.3636 .3695	.3500 .3638	1.620 1.697	.8319
4.	.1712	.4673	.7181	.8789	.9608		,9395	.7111	.3750	.3765	1.773	.8013
4.5	.2045		.7733		.9759	.9961		.7363	.3816	1000	1.929	.8315
5.	.2373	.5804	.8184		.9852	.9980	.9999	.7576	.3929	.4196	2.088	.8488
6.	.3038		.8843	.9690	.9945	.9995	9939	.7912	.4062	.4517	2.407	.8767
8.		.8098		.9922	.9992	.9991	1.000		.4250	.4962	3.060	
10.	.5431	.8905	.9819	.9980	.9399		1.000		.1:.75	.5249	3.643	.9279
12.	.6377	.9379		.9995	.9999		1.000	.8861	.4464	.5463	4.390	.9418
16.								.9126				.9556
2.		le V .1557					2.25.	.5109	1.2815	0 v 1	1.226	5328
$\begin{vmatrix} 2. \\ 2.125 \end{vmatrix}$.1721	3557	.5566	7416		.9731		.2861	.2300	1.248	.5657
2.25		.1887		.5880	.7693		.97.12	.5450	2.)28	.2425	1.272	.5923
2.375		.2055		.6176	.7942		.9810	.5600	.2598	.2545	1.298	.6164
2.5		.2226	.4356	.6455	.8187	.9 311	.9876	.5742	.3046	.2657	1.325	.6363
2.625		.2398		.6716	.8367		.9904		.3115	.2762	1.354	.6547
2.75		.2570		.6962	.8547		.9926	.6005	.3158	.2863	1.385	.6722
2.875	4	.2742		.7191	.8703		.9943	.6124	.3207	.2.360		.6885
3.	.0826			.7405	.8937		.9956	.6235	.3:250	.3053	1.453	.7035
3.25	.0955			.7789	.9095		.9974	.6443	.3333 .3415	.3228	1.524 1.596	.7294 .7490
3.5 3.75	1090	.3595 .3926	6547	.8120 .8405	.9 140		.9991		.3480	.3535	1.663	.7658
4.		.4219		.8648	.9560		9994		.3543	.3665	1.725	.7800
4.5	.1673			.9035	.9730		.9998	.7213	.3659	.3920	1.883	.8048
ð.		.5436		.9311	.9834	.9.178		.7435	.3753	.4105	2.038	.8258
6.		.6434	. 624	.9652	.9938	.9995		.7794	.3907	.4437	2.:52	.8622
8.	.3878			.9 +12	.99 1		1.000	.8271	.4128	.4895	2.988	.8950
10.		.8777		.9978	.999+		1.000		.4270	.5192	3.623	.9144
12.	.6029	.9304	.9920	.9995	.4999	1.000	1.000	.8791	.4373	.5413	4.270	.9315
16.	1.1558	1.9776	.9988	9993	1.000	1.000	1 000	.9072	-404±	19114	5.500	.9485

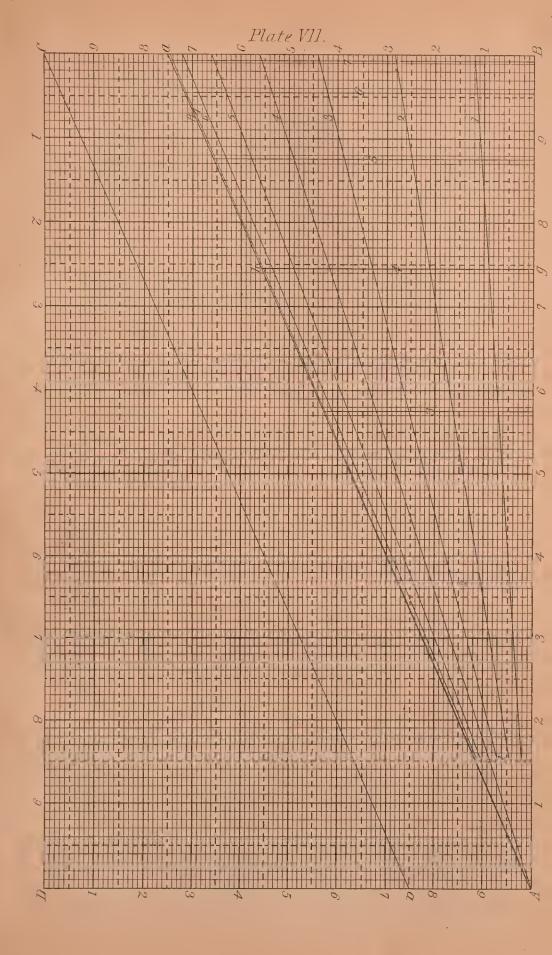
PARABOLIC CONSTRUCTION OF SHIPS. Table VII. Power q = 2.5. Hollow Lines.												
	Tabl	e VI	I.	I	owe	r q =	2.5.		Holl	ow I	ines	•
Exp.	11		0	rdinat	es.			Prod.	C. gr.	Meta	Res.	Inflec-
n.	1	2	3	4	5	6	17	a WD	e	m	t	tion.
.2.	.0266	.1266	.28.09	.4871	.6846	.8510	.9614	.4913	.2912	.2053	1.248	.5000
2.125		.1415	.3171	.5215		.8737	.9702	.5092	.2)54	.2182	1.266	.5300
2.25		.1568	3442	.5543	.7472	.8932	.9769	.5260	.3003	.2310	1.287	.5568
2.375		.1724	.3709	.5854		.9097	.8922	.5414	.3084	.2480	1.309	.5807
2.5		.1884	.3972	.6149		.9237	.9862	.5558	.3134	.2545	1.333	.6008
2.625		.2046	.4230	.6426		.9356	.9894	.5695	.3198	.2655	1.360	.6227
$\begin{vmatrix} 2.75 \\ 2.875 \end{vmatrix}$.2210	$\begin{bmatrix} .4482 \\ .4728 \end{bmatrix}$.6688		.9497	.9918	.5825	.3235	.2762 .2861	1.389 1.420	.6605
3.		.2541	.4967	.7162	.8742	.9614	.9051	.6068	.3325	.2954	1.452	.6767
3.25	.0735	2875	.5424		.9000		.9974	.6282	.3405	.3138	1.520	.7044
3.5	.0852		.5850	.7935	.9212	.9806	.9983	.6476	.3480	.3296	1.530	.7254
3.75	.0974		.6246	.8244	.9380	.9863	.9990	.6650	.3540	.3441	1.653	.7432
4.		.3864	.6610	.8510		.9903	.9994	.6806	.3605	.3577	1.710	.7582
4.5	.1371	.4501	.7252	8913	.9700		.9998	.7077	.3715	3820	1.861	.7846
5.	1656	.5080	.7784			.9976	.9999	.7311	.3806	.4027	2.014	.8070
S. 8.	.2255	$ 6126 \\ .7682$.8576	.9614		.9994	1.000 1.000	.7692	3955 4166	.4365 .4835	2.312 2.935	.8472 .8827
10.	.4662	.8651	.9774		.9998		1.000	.8496	.4303	.5145	3.554	.9029
12.	.5699	.9229		.9995		1.000	1.000	.9732	.4403	.5368	4.180	.9223
16.		.9751			1.000		1.000	.9026	.4558	.5738		
	Tab	le V				er q			Holle	w L	ines.	
2.	.0129			1.4219	1.6347	.8240	.9539	4571	1.2739	.1894	1.330	.4472
2.125	.0151	.9567	.2520		.6713	.8505	.9643	.4758	.2787	.2030	1 341	.4771
2.25	.0175		.2781	.4927	.7049		.9724	.4933	.2862	.2151	1.357	.5037
2.375	0200	.1213	.3042	.5260	.7355	.8926	.9787	.5097	.2927	.2274	1.379	.5286
2.5	0229		.3302		.765	.9092	.9835	.5252	.2970	.2387	1.400	.5508
$\begin{bmatrix} 2.625 \\ 2.75 \end{bmatrix}$	$\begin{array}{c c} .0258 \\ .0290 \end{array}$.3561	.5882	.7885 .8112	.9232	.9873 .9902	.5397	$\begin{bmatrix} .3042 \\ .3090 \end{bmatrix}$.2498	$1.424 \\ 1.450$.5723 .5926
2.875	0.0230		.4070	.6171 $.6443$.8316	.9453	.9324	.5663	.3135	.2702	1.476	.6117
3.	.0359		4318	.66 33		.9538	.9941	.5785	.3180	.2798	1.504	.6290
3.25	.0136		.4799	.7166	.8812		.9965	.6011	.3267	.2973	1.583	.6591
3.5		.2556	.5255		.9062	.9767	.9979	.6213	.3350	.3136	1.625	.6832
3.75	.0611	.2875	.5684		.9261	.9835	.9988	.6397	.3420	.3290	1.705	.7039
4.	.0709		.6085	.8240	.9419	.9883	.9993	.6564	.3482	.3427	1.755	.7227
4.5 5.	.0921	.3826	.6800	0.8734 0.9092	.9641	.9941	.99.7	.6355 .7102	.3603 .3700	.3682 .3893	1.890 2.025	.7514 .7750
6.	.1674		.7403	9539	.9779	.9971	.9999 1.000	.7514	.3860	.4244	2.312	.8155
8.	2828	.7287	9318	.9883	.9988		1.000	.8042	.4030	.4734	2.888	.8635
10.		.8404	.973.)	9971	.9799		1.000	.8378	.4233	.5060	3.476	.8845
12.	.5093	.9083	.9894	.9993	.9999		1.000	.8622	.4345	.5293	4.065	.9082
16.	1.6868	.9702	.9384	.9939	1.000	1.000	1.000	.8940	.4490	.5062	5.260	.9310
		ble I				r q =			lollo	w Li	nes.	
2.	11.0302		.1379	.3164		.7725		.4063	.2461		1.455	.3778
2.125		.0438	.1592	.3529		.8058	.9527	.4257	.2534	.1810	1.461	.4107
$\begin{vmatrix} 2.25 \\ 2.375 \end{vmatrix}$.0516	.1815				.9634	.4440	.2607	.1930	1.469	.4400
2.5		.0692	.2045		.7003	.8594 $.8807$.9717 .9781	.4612	.2572 $.2735$.2047 $.2160$	1.478	.4648
2.625	.0762	.0789	.2524		.7284		.9831	.4928	2796	.2270	1.505	.5078
2.75		.0893		.5253		.9145	.9869	.5073	.2852	.2374	1.522	.5282
2.875	.0130	1024		.5564	.7820	.9275	.9899	.5210	.2906	.2475	1.556	.5477
3.		.1117	.3264		.8065		.9922	.5340	.2955	.2570	1.569	.5665
3.25		.1361	.3757		.8449		.9054	.5581	.3046	2747	1.618	.5985
$\begin{vmatrix} 3.5 \\ 3.75 \end{vmatrix}$.1622		.6906	.8770		.9972	.5799	.3131 .3211	.2908	1.670	.6261
4.		.2184	.4709 .5157	.7725	.9027 .9232		.933 9990	.5997	.3288	.3056	1.725 1.787	.6488
4.5		.2778	.5981		.9524		.9996	.6494	.3415	.3458	1.906	.6687
ā.		.3384	.6697		.9707		.9999	.6764	.3529	.3607	2.036	.7275
6.5	.0923	.4566	.7821	.9390	.9889	.9990	1.000	.7196	.3711	.4057	2.309	.7754
8.		.6558	.9101		.9984		1.000	.7788	.3966	.4575	2845	.8304
10. 12.		7931	.9641		.9.195		1.000	.8174	.4138	.4924	3.403	.8637
16.	6030	.8796	.9859	9999	.9999	1.000	1.000	.8445	.4260	.5174	3.987	.8859
10.	1 .0000	.0000	0100	ן פפספ.	1.000	1.000	1.000	.0000	.4424 [.5507	0.087	.9142

								Prod. Area.				
Exp.	1		0	rdinat	es		1	Prod	1 C 0:1:	1	1	1
n.		1 2	ı 3 Ğ	4	1 5	6	7	Area.	0.81.			
0.25	1957	5052	5770	6916	6000	7257	7 .7979	.6126	.4164			
0.25	4607	5655	.6196	.0310	7449	7070	.1919	.6524	.4210			
0.5	5041	6046	6765	7357	7890	8408	.8967	.7011	.4249			
0.625	5315	6224	.6765 .7103	7700	8228	8725	.9235	.7317	.4277			
0.75	.5556	.6637	.7383	7979	.8495	.8967	.9422	.7540	4304			
0.875	.5757	.6868	.7620	.8202	.8712	.9155	.9567	7721	.4328			
1.	.5946	.7071	.7825	.8409	.8891	.9306	.9672	.7885	.4351			
1.125			.8005				.9750		.4323			
1.25	.6262	.7413	.8164	.8725	.9172	.9525	.9809	.8128	.4393			
1.375							.9853	.8224	.4412			
1.5	.6527	.7694	.8429	.8967	.9368	.9672	.9887	.8313	.4428			
1.75	.6756	.7930	.8653	.9156	.9517	.9771	.9933	.8463	.4455			
2.	.6955	.8133	.8835	.9306	.9628	.9840	.9961	.8586	.4478			
2.25	.7137	.8308	.8988	.9427	.9413	.9887	.9977	.8678	.4499			
2.5	7440	.8462	.9118	.9525	.9780	.9921	.9986	.8760	.4519			•
2.75	7500	.8099	.9229	9000	.9827	0001	.9992	.8830	4554			
0.	7917	.8720	.9292	.9072	9800	1006	.9999	0.6902	45094	1		
1.0	8020	0003	9594	9840	9950	9920	0000	01.01	4606	1		
5	8354	9345	9752	9921	9981	9997	9999	.8586 .8678 .8760 .8836 .8902 .9023 .9121 .9203	4634			
	Tal	le X	T.	F	Owe	r a -	- 0.37	5.	H'n	11 T	ines.	
0.5	1 3579	4702	1 5564	6310	6693	7709	.8491	.6031	.4003	LAA AA	IIICS.	
0.625	3874	4478	.5986	6757	.7463	.8150	.8875	.6410	.4090			
0.75	4141	.5407	.6343	.7128	.7830	.8491	.8840	.6722	.4150			
0.875	.4368	.5692	.6652	.7441	.8132	.8761	.9358	.6993	.4182			
1.	.4585	.5946	.6922	.7711	.8384	.8977	.9511	.7203	.4215			1
1.125	.6014	.6147	.7162	.7945	.8593	.9142	.9626	.7388	.4240			
1.25	.4955	.6383	.7377	.8150	.8781	.9296	.9714	.7537	.4262			
1.375	.5118	.6573	.7564	.8331	.8934	.9414	.9781	.7673	.4281			
1.5		.6749		.8491			.9832	.7797	.4298			
1.75	.5541	.7062	.9049	.9761	.9284	.9659	.9900	.8000	.4330			
2.	.5802	.7334	.8305	.8977	.9448	.9761	.9941	.8172	.4355		[
2.25	.6236	7755	.8921	.9195	.9072	.9852	.9965 .9979	.8312	.4381 .4405			
$\begin{bmatrix} 2.5 \\ 2.75 \end{bmatrix}$	6495	7079	9888	0414	0749	9016	0000	.8534	.4427			
3.	6500	8142	8957	9511	9800	9941	.9992 .9995	.8620	4448			
3.25	5934	7794	8848	9460	.9791	.9944	.9994	.8693	.4458			
3.5	6611	8432	.9227	.9659	.9878	.9971	.9997	.8759	.4486			
4.	.7183	.8671	.9398	.9761	.9925	.9985	.9999		.4523			
4.5	.7423	.8868	.9529	.9832	.9954	.9993	1.000	.8960	.4553			
5.	.7636	.9034	.9633	.9881	.9972	.9.396	1.000	.9033	.4582			
		ble 2					=0.5	j		ll Li	nes.	
1.		.5000		1.7071		0883.	.9354	.6666	.3966			
1.125	.3734	.5258	.6408			.8873	.9506	.6860	.4023			
1.25		.5496		.7613		.9073	.9621	.7048	.4050			
1.375		.5716	.6892		.8605		.9709	.7218	.4076			
1.5		.5020		.8040	.8777 .8927	.9354	.9776 .9827	.7382	.4002 .4125			
1.625		.6111	.7488		.9057	.9548	.9868	.7646	.4148			
1.75 1.875		.6457	7653		.9171	.9621	.9898	.7755	.4170			
2.		.6614		.8660	.9270		.9921	.7854	.4192			
2.25		.6903	.8079		.9434		.9953	.8013	.4234			
2.5	.5327		.8314		.9565	.9842	.9972	.8147	.4270		}	
2.75	.5544	.7394	.8517	.9227		.9889	.9984	.8262	.4302			
3.	.5745	.7603		.9354		.9921	.9990	.8376	.4331			
3.25	.5934	.7794		.9460		.9944	.9994	.8465	.4357			
3.5		.7966		.9526	.9837		.9996	.8554	.4383			
3.75		.8124		9621		.9972	.9998	.8630	.4407			
4.		.82(8		.9682	.9900		.9999	.8701	.4430			
4.5		5520		.9777	.9939		.9999	.8819	.4474			
5.	.0979	.8733	1.9511 1.9697	.9842	.9963		1.000	.8910	.4512			
6.	1.7424	1.9001	1.8087	.5787.21	0000	.5555	1.0001	.9004	.4562			

Tabl	e XII	I.		Pow	er q =	= 0.75	j.		Full	Line	S.
Exp.				Ordin	otos			L i	C.gr.		
n	1	2	3	4	5	6	7	Area.	e'	Infl.	
1.5	.2781	.4555		.7209	.8223	.9047	.9666	.6594			
1.625	.2932	.4777	.6247	.7284	.8434	.9201	.9742	.6788	.3853		
1.75	.3070	.4988	.6479	.7675	.8619	.9329	.9802		.3893		
1.875	.3225	.5188		.7876	.8782	.9437	.9348	.7028	.3929	22	
2.	.3367	.5379	.6897	.8059	.8925	.9527	.9853	.7175	.3963	The lines for these ordinates have no inflections.	
2.125	.3504	.5562	.7085	.8226	.9051	.9603		.7282	.3993	din ns.	
2.25 2.375	$\begin{array}{c} .3636 \\ .3762 \end{array}$.5735 .5902	.7261 .7426	.8378	.9163	.9667	.9930 .9946	.7400 .7504	.4020 .4050	tion	
2.5	.3888	.6060		.8446		.9765	.9958	.7604	.4071	ese	
2.75	.4128	.6353		.8863	.9490	.9834	.9975		.4128	th it	
3	.4355	.6630	.8023	.9047	.9605	.9882	.9985	.7910	.4168	roi no	
3.25	.4570	.6880		.9201	.9689	.9917	.9991	.8032	.4207	es ve	
3.5	.4776	.7110		.9329	.9757	.9941	.9995	.8142	.4238	lin ha	
3.75	.4972	.7322		.9437	.9675		.9997		.4268	he	
4	.5159	.7518		.9527	.9851	.9971	.9998 .9999	.8341 .852 5	.4292 .4333	H	
4.5 5	.5510	.7865	.9081	9765	.9944		.9939	.8652			
6	.7178	.8633	.9120	.9882	.9979		1.000	.8835	.4451		
8	.7292		.9825	.9971			1.000		.4562		
10	.7954	.9575	.9932	1.9993	.9938	.9999	1.000		.4623		
Tabl	e XI	v.		Pow	ver q	=1.			Fı	came	3.
.125	.0165	1.0353	.0517	.0830	.1154	.1591	1.2289	.1111	1.2647	y, l	1
.25	.0320	.0691		.1591		.2989	.4054		.2777	rve	
.375	.0187	.1023		.2289	.3077	.4054	.5415	.2727	.2849	ca	
.5	.0646		.2094		.3876	.5000	.6464	.3333	.3000	Concave curves.	
.625	.0798		.2545	.3516	.4583	.5795	.7274	.3816	.3095	nca	
.75 .875	.0953	$0.1941 \\ 0.2225$.2971 .3372	.4054 $.4547$.5208 5761	.6464	.7898 .8379	.4286	$\begin{bmatrix} .3182 \\ .3261 \end{bmatrix}$	ပိ	
1.	.1250	.2500		.5000	.6250	7500	.8750	.5000	.3333	strai't	· ·
1.125	.1394	.2764		.5415	.6683	.7873	.9036	.5294	.3400		
1.25	.1537	.3020		.5795	.7065	.8232	.9257	.5555	.3461	es.	
1.375	.1676		.4 50	.6144	·740 t	.8513	.9427	.5789	.3518	ırv	
1.5	.1815		.5059	.6464			.9558	.6000	.3571	ເວ	
1.625	.1948	.3734		.6758		8949	.9657	.6190	3621	Vež	
1.75 1.875	.2084	4169	5857	7027	8203	.9116	.9737 .9797	.6363	.3666 .3710	Convex curves.	
1.010		1.1.00	1.0001		-0110	.0401	1.010.	1 .0022	1.01.20	0 1	
Tabl	e XV	•		Pov	ver q	=1.2	5.		Fr	ames	·
	0 = 0		0.070	LOAAC	L OCETI	1.1005	.1583	0765	[.2120]	4	
.125	.(059	.0137	.0279	.0446	.0671					a pred	
.255	.0140	.0329	.0640	.1005	.1485	.2155	.3235	.1500	.2421	s win.	ł
.255 .375	.0140	.0329 .0578	.0640	1005 1582	.1485	.2155 $.3242$.3235 .4645	.1500	.2421 .2555	nes wi	
.255 .375 .5	.0140 .0229 .0326	.0329 .0578 .0808	.0640 .1024 .1417	.1005 .1582 .2155	.1485 .2292 .3059	.2155 .3242 .4201	.3235 .4645 .5796	.1500 .2222 .2755	.2421 .2555 .2687	lines wi	
.255 .375 .5 .625	.0140 .0229 .0326 .0424	.0329 .0578 .0808 .1048	.0640 .1024 .1417 .1808	.1005 .1582 .2155 .2707	.1485 .2292 .3059 .3771	.2155 .3242 .4201 .5054	.3235 .4645 .5796 .6717	.1500 .2222 .2755 .3254	.2421 .2555 .2687 .2800	ave lines wi	
.255 .375 .5	.0140 .0229 .0326	.0329 .0578 .0808 .1048 .1288	.0640 .1024 .1417 .1808 .2193	.1005 .1582 .2155	.1485 .2292 .3059 .3771 .4424	.2155 .3242 .4201 .5054 .5797	.3235 .4645 .5796 .6717 .7445	.1500 .2222 .2755 .3254 .3691	.2421 .2555 .2687 .2800 .2895	ancave lines wil	
.255 .375 .5 .625 75 .875	.0140 .0229 .0326 .0424 .0530 .0633 .0743	.0329 .0578 .0808 .1048 .1288 .1528 .1768	.0640 .1024 .1417 .1808 .2193 .2569 .2J34	.1005 .1582 .2155 .2707 .3235	.1485 .2292 .3059 .3771	.2155 .3242 .4201 .5054	.3235 .4645 .5796 .6717 .7445 .8095 .8163	.1500 .2222 .2755 .3254	.2421 .2555 .2687 .2800	Concave lines with no inflection.	
.255 .375 .5 .625 73 .875 .1	.0140 .0229 .0326 .0424 .0530 .0633 .0743 .0852	.0329 .0578 .0808 .1048 .1288 .1528 .1768 .2004	.0640 .1024 .1417 .1808 .2193 .2569 .2J34 .3287	.1005 .1582 .2155 .2707 .3235 .3734 .4204 .4645	.1485 .2292 .3059 .3771 .4424 .5019 .5557 .6033	.2155 .3242 .4201 .5054 .5797 .6434 .6980 .7417	.3235 .4645 .5796 .6717 .7445 .8095 .8463 .8810	.1500 .2222 .2755 .3254 .3691 .4080 .4432 .4755	.2421 .2555 .2687 .2800 .2895 .2991 .3073	.3332	
.255 .375 .5 .625 75 .875 .1 1.125 1.125	.0140 .0229 .0326 .0424 .0530 .0633 .0743 .0852 .0963	.0329 .0578 .0808 .1048 .1288 .1528 .1768 .2004 .2239	.0640 .1024 .1417 .1808 .2193 .2569 .2J34 .3287 .3627	.1005 .1582 .2155 .2707 .3235 .3734 .4204 .4645 .5056	.1485 .2292 .3059 .3771 .4424 .5019 .5557 .6033 .6478	.2155 .3242 .4201 .5054 .5797 .6434 .6980 .7417 .7841	.3235 .4645 .5796 .6717 .7445 .8095 .8463 .8810	.1500 .2222 .2755 .3254 .3691 .4080 .4432 .4755 .5040	.2421 .2555 .2687 .2800 .2895 .2991 .3073 .3145	.3332 .5135	
.255 .375 .5 .625 75 .875 .1 1.125 1.125 1.375	.0140 .0229 .0326 .0424 .0530 .0633 .0743 .0852 .0963 .1072	.0329 .0578 .0808 .1048 .1288 .1528 .1768 .2004 .2239 .2470	.0640 .1024 .1417 .1808 .2193 .2569 .2J34 .3287 .3627 .3943	.1005 .1582 .2155 .2707 .3235 .3734 .4204 .4645 .5056 .5440	.1485 .2292 .3059 .3771 .4424 .5019 .5557 .6033 .6478 .6868	.2155 .3242 .4201 .5054 .5797 .6434 .6980 .7417 .7841 .8178	.3235 .4645 .5796 .6717 .7445 .8095 .8463 .8810 .9080	.1500 .2222 .2755 .3254 .3691 .4080 .4432 .4755 .5040 .5299	.2421 .2555 .2687 .2890 .2895 .2991 .3073 .3145 .3212 .3273	.3332 .5135 .6175	
.255 .375 .5 .625 75 .875 .1 1.125 1.125 1.375	.0140 .0229 .0326 .0424 .0530 .0633 .0743 .0852 .0963 .1072 .1185	.0329 .0578 .0808 .1048 .1288 .1528 .1768 .2004 .2239 .2470 .2697	.0640 .1024 .1417 .1808 .2193 .2569 .2J34 .3287 .3627 .3943 .4254	.1005 .1582 .2155 .2707 .3235 .3734 .4204 .4645 .5056 .5440 .5796	.1485 .2292 .3059 .3771 .4424 .5019 .5557 .6033 .6478 .6868 .7217	.2155 .3242 .4201 .5054 .5797 .6434 .6980 .7417 .7841 .8178 .8463	.3235 .4645 .5796 .6717 .7445 .8095 .8463 .8810 .9080 .9289 .9451	.1500 .2222 .2755 .3254 .3691 .4080 .4432 .4755 .5040 .5299 .5523	.2421 .2555 .2687 .2800 .2895 .2991 .3073 .3145 .3212 .3273 .3333	.3332 .5135 .6175 .6886	
.255 .375 .5 .625 .75 .875 .1 1.125 1.125 1.375 1.5 1.625	.0140 .0229 .0326 .0424 .0530 .0633 .0743 .0852 .0963 .1072 .1185 .1294	.0329 .0578 .0808 .1048 .1288 .1528 .1768 .2004 .2239 .2470 .2697 .2919	.0640 .1024 .1417 .1808 .2193 .2569 .2334 .3287 .3627 .3943 .4254 .4566	.1005 .1582 .2155 .2707 .3235 .3734 .4204 .4645 .5056 .5440 .5796 .6127	.1485 .2292 .3059 .3771 .4424 .5019 .5557 .6033 .6478 .6868 .7217 .7529	.2155 .3242 .4201 .5054 .5797 .6434 .6980 .7417 .7841 .8178 .8463 .8708	.3235 .4645 .5796 .6717 .7445 .8095 .8463 .8810 .9080 .9289 .9451 .9574	.1500 .2222 .2755 .3254 .3691 .4080 .4432 .4755 .5040 .5299 .5523 .5726	.2421 .2555 .2687 .2800 .2895 .2991 .3073 .3145 .3212 .3273 .3333 .3386	.3332 .5135 .6175 .6886 .7382	
.255 .375 .5 .625 75 .875 .1 1.125 1.125 1.375	.0140 .0229 .0326 .0424 .0530 .0633 .0743 .0852 .0963 .1072 .1185	.0329 .0578 .0808 .1048 .1288 .1528 .1768 .2004 .2239 .2470 .2697 .2919 .3137	.0640 .1024 .1417 .1808 .2193 .2569 .2J34 .3287 .3627 .3943 .4254	.1005 .1582 .2155 .2707 .3235 .3734 .4204 .4645 .5056 .5440 .5796	.1485 .2292 .3059 .3771 .4424 .5019 .5557 .6033 .6478 .6868 .7217	.2155 .3242 .4201 .5054 .5797 .6434 .6980 .7417 .7841 .8178 .8463 .8708 .8908	.3235 .4645 .5796 .6717 .7445 .8095 .8463 .8810 .9080 .9289 .9451	.1500 .2222 .2755 .3254 .3691 .4080 .4432 .4755 .5040 .5299 .5523 .5726 .5910	.2421 .2555 .2687 .2800 .2895 .2991 .3073 .3145 .3212 .3273 .3333 .3386 .3435	.3332 .5135 .6175 .6886	

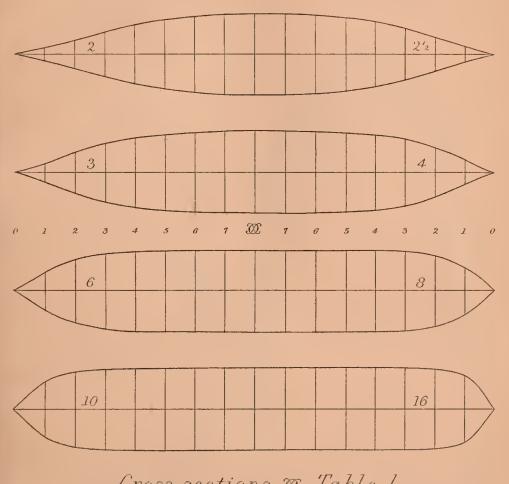
Tabl	Table XVI. Power q = 1.5. Frames.												
Exp.				Ordina	ites.			11	C. gr.	(1	
n	1	2	3_	4	5	6	7	Area.	e	Infl.		_	
.125			.0136	.0239	.039T	.0635	1.1095	.0650	.1915	th th			
.25		.0166		.0635		.1585	.2581	.1252	.2125	wi n.			
.375	.0107	.0327		.1094		.2581	.3385	1810	.2290	nes			
.5	.0164	.0668		.1585			.5197	.2313	.2423	Concave lines with no inflection.			
.75		.0955	.1619	.2581		.5197		.3238	.2658	av ir			
.875	.0364	.1050		.3067		.5890			.2763	000			
1.	.0442	.1250	.2296	.3535	.4940	.6489	.8185	.4000	.285)	1			
1.125		.1453		.3985			.8590		.2937	.2068			
1.25 1.375		.1660 .1867		.4412	.5939	7855	.8906	.4626	.3015	.3333 .4444			
1.5			.3586	.5197		8185	1.9344	.5131	.3160				
	.0860		.3903	.5555	.7113	.8455	.9491	.5348	.3224				
1.75	.0951	.2 488	.4198	.5890	.7429	.8704	.9608	.5545 .5727	.3285	.6534			
									1.3342	.6838			
	le XV									mes.		·	
.125	.0008	.0025	1.0067	.0128	.0228	.0401	.0758	.0500					
.25				.0401 $.0767$.0693	.2060		.1000 .1482	.1876 .2058	s w			
.375	.0050	0.0185 0.0296		.1166		.3039			.2200	ine			
.625	.0120	.0425		.1605					.2337	nfl(
.75	.0164	.0767		.2060		.4660	.6617	.2860	.2456	cav io i			
.875	.0210	.0721	.1492	.2518		.5 393	1.7338	.3272	.2563	Jon n			
1.	.0263	.0894		.2973			.7916		,2663				
1.125		.1054		.3418					.2757	.1 61 9			
1.25 1.375	.03:7	.1231	2118	.3850		.7115 .7545							
1.5	.0505	.1596	3022	.4660	.6334	.7916			.3008	.4575			
1.625		.1784		.5037	.6721	.8234	.9409	.5015	.3072	.5193			
1.75	.0643	.1973	1.3633	.5393	.7070	.8505	.9545	.5222	.3137	.5676			
1.875	1.0713	1.1718	1.3922	.5729	.7386	1.8736	.9648	.5414		mes.			
												1	
	.0003	.0011	1.0933	.0069	.0133	.0253	.0524 .1643	.0222	.1470	Concave lines with no inflection.			
.25	.0011	0105	.0113	.0523		.0858		.1168	.1842	ss v			
.5	.0042	.0179		.0858		.2497		.1666	.2000	les lin			
.625	.0064	.0271	.0648	.1236	.2100	.3359	.5323	.2136	.2145	ve inf			
.75	.0091	.0377	.0652	.1643	.2712		.6237	.2571	.2273	nca no			
.875	.0121	.0495	.1137	.2068			.7021		.2395	Con			
1. 1.125	.0156	.0625	.1406 .1686	.2500		.5625 .6199	.7656 .8165	.3665	.2600	.1291			
1.125	.0236	.0912	.1974	.3359		.6777	.8569	.3968	.2691	.2350			
1.375	.0281	.1067	.2256	.3775		1.7248	.8887	.4245	.2780	.3244			
1.5	.0330	.1128	.2547	.4179	.5934	.7656	.9136		.2860	.3968			
1.625	.0380	.1394	.2853	.4557	.6350	.8008	.9317	.4734	.2930	.4587			
1.75	.0434	.1565	.3144				.9481		.3000 .3062	5473			
1.875	.0489 e XX		4.9 1 91		er q		.9593 25	1017E	Fra				
.375		1.0059	1.0166				.2515	1022	.1237		1	Ī	
.5	.0021			.0631		.2099	.3747		.1546	ine			
.625	.0060	.0172	.0460	.0952	.1728	.2931	.4886	.1863	.1629	Concove lines, no inflection.			
.75	11 .	.0251	.0481	.1342		.3747	.5881	.2270	.1855	inf			
.875	0069			.1698		.4521	.6717	.2675	.1990	Con			
1. 195	00∂5	.0442	.1100 .1350	.2102		.5235	.7405 .7961	.3412	.2216	.1078			
1.125 1.25		.0676		.2931		.6455	.8405	.3717	.2331	.2015			
1.375			1830	.3343			.8757	.4000	.2422	.2833			
1.5	.0215	.0945	.2147	.3747	.5560	.7405	.9033	.4251	.2512	.3515			
1.625	.0252	[.1090	1.2439	.4141	.6000	1.7789	.9246	.4:89	.2590	.4032			

Table XX.—For Elliptic Stern of Vessels.													
Ex-		Ord	linates	of Ellip	ses of 1	Differen	t Order		Area	Index			
nent		Ord				DINCECH			$\begin{vmatrix} \mathbf{a} = \\ bl \times \end{vmatrix}$	i			
$\frac{n}{n}$	1/2	1	2	3	4	5	6	3					
2.	.3398	.4840					.9682		.7854	1.603			
2.25	.4108	.5490	1		9004.		9801		.8154	1.544			
2.5	.4670	,						.9978	.8382	1.495			
2.75	.5174	.6514		1	9434.			- 1	.8564	1.453			
3.		.6911						9994		1.418			
3.25	.5991	.7252 .					9973			1.388			
3.5		.7548				- 1	9978.	[]		1.362			
4.		.8021 .								1.318			
Arc.	30° 45°	.0149 .							Sh				
41		.0157 .								of sels.			
	-00	.0100].	04/4].	1000	13:44	0130 .	1104	0940)	7 65	seis.			
Ta	ble X	XI.—T							f Vess	els.			
	D		Ex	ponent	for d	lisplac	ement	n.	q=2.				
$\frac{d}{-}$	n'	2	2.5	3	3.5	4	5	6	8	10			
ů.	. (2.	$\ .356$.397	.429	.453	.474	.500	.528	.558	.577			
er. Deep.	$\langle 2. \rangle$	5 .381	.425	.459	.486	.508	.541	.566	.597	.620			
ate	1 5	.400	.447	.482	.510	.533	.563	.594	.627	.650			
Draft of water. ht. Middling. Dee	3.8	.414	.462	.500	.528	.552	.589	.616	.650	.673.			
of	$\frac{1}{4}$.427	.476	.514	.544	.569	.606	.635	.668	.693			
ft	(5	.444		.535	.567	.592	.631	.660	.696	.722			
ra t.	(6	.458	.509	.550	.583	.610	.649	.679	.717	.750			
Dra Light.	$\left\{\begin{array}{c}8\\1\end{array}\right\}$	1.474	.529	571	.605	.632	.673	.704	.743	.770			
H	(10	.490	.547	1.590	.625	.654	.696	.720	.759	.797			
Purp	ose.		peed a		Fr	eight	and		eight a				
Lar	, OBC.	ll pa	asseng	ers.	pa	ssenge	ers.	slo	ow spe	ed.			
Tal	ble X	XII.—I	lengtl	ı of V	essels=	=Tabı	ılar N	umb	$\operatorname{er} X_{\mathfrak{d}}^3$	\overline{T} .			
Conff	ient C.		Propo	ortion	of dra	ft and	lengt	h of v	ressels				
	ent C.	8	12	18	26	36	48	64	82	102			
Sailing yachts.	.356	14.9	19.0	23.7	28.9	34.0	38.9	43.6	47.2	48.0			
act	.425	13.9	17.7.	22.1	$\frac{26.9}{2}$	31.7	36.2	40.6	43.9	44.5			
	.482	13.3	17.0	21.2	25.8	30.3	34.7	38.9	42.1	42.7			
ar.	.528	12.9	16.5	20.5	25.0	29.4	33.7	37.7	40.8	41.3			
Ordinary vessels.	.569	12.5	16.0	20.0	24.4	28.7	30.8	36.8	39.8	40.3			
0 > (.631	12.1	15.5	19.4	23.5	27.6	31.6	35.4	38.3	38.8			
14.5	.679	11.8	15.1	18.8	22.9	26.9	30.8	34.6	37.4	38.0			
Heavy Freight.	.723	11.6	14.8	18.5	22.5	26.5	30.3	34.0	36.8	37.2			
田岩(.797	$\parallel 11.2$	14.3	17.9	21.8	25.6	29.3	32.9	35.6	36.0			
Cons	litian	V	essels	for		rdina		Riv	er stea	mers,			
Cono	lition.	de	ep wa	ter.	na	vigati	on.		ght dra				

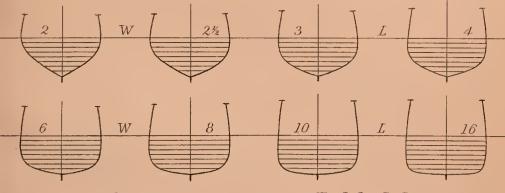




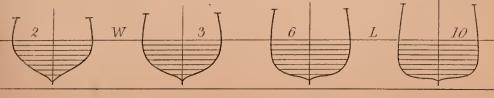
Hollow Waterlines Table IV



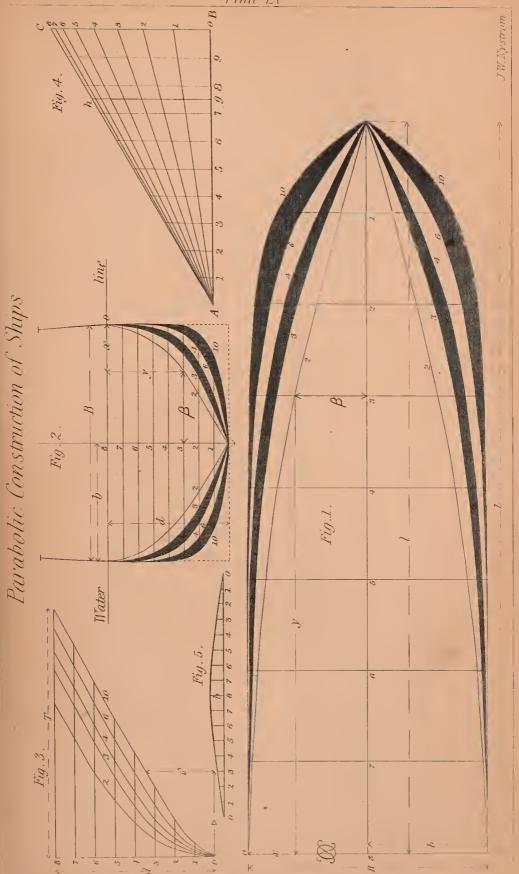
Cross-sections & Table 1



Cross-sections & Table IV

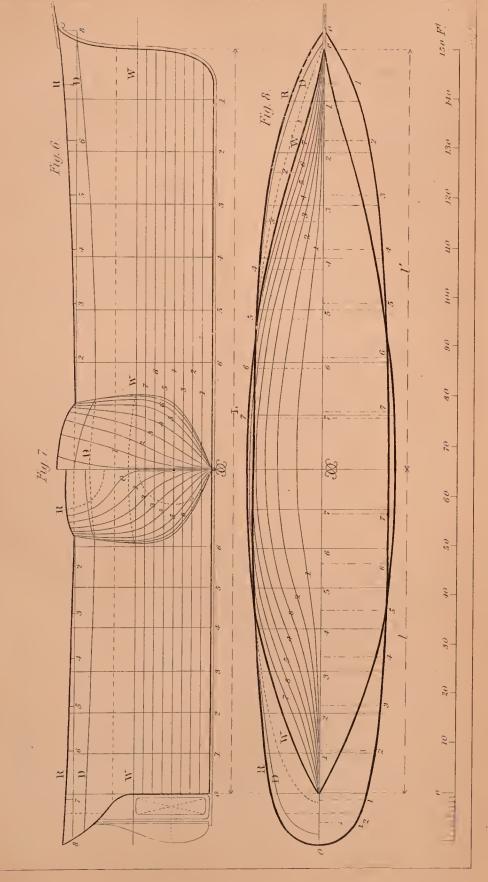








Astronus Parabolic Construction of Ships.





TO CONSTRUCT A DISPLACEMENT SCALE.

D =displacement of the vessel in cubic feet.

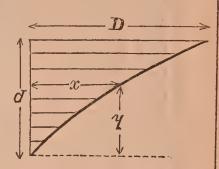
 $\delta =$ displacement in cubic feet per inch of difference of draft.

 \mathbf{a} = area of load water line in square feet. d = draft of water in feet. a = area of any water line at draft y and displacement x. n = exponent of the displacement scale.

$$n = \frac{\mathbf{a} d}{D}.$$

$$x = \frac{y^n}{d^n} D. \qquad y = \sqrt[n]{\frac{x}{D}}.$$

$$a = \frac{D y^{n-1}}{d^n}. \quad \delta = \frac{D y^{n-1}}{12 d^n}.$$



Example. The area of the load water line of a vessel is a = 6400 square feet; draft of water d = 17 feet, and the load draft displacement D = 80,500 cubic feet. Required the draft exponent n=? and at what draft y the displacement is x=45,000 cubic feet?

$$n = \frac{6400 \times 17}{80500} = 1.35$$
, $y = 17$ $\sqrt[1.35]{\frac{45000}{80500}} = 11.05$ feet, the draft required.

Construct a scale as shown by the accompanying figure, and draw the ordinates x; the draft d being divided into eight equal parts.

Assuming the displacement as unit, the ordinates x are found in the following

table, opposite the given exponent n.

After the exponent is known, the displacement can be expressed in tons, and the load draft displacement multiplied by the tabular number gives the displacement x at the corresponding draft y.

Rule. Multiply the load draft displacement, expressed either in tons or cubic feet, by the tabular number for the given exponent and water line, and the product is the corresponding displacement.

Displacement Scale.

$n = \frac{\mathbf{a} d}{\mathbf{b}}$	41		Ordina	ate Wat	terlines.			Dood size					
$N = \overline{D}$	1	2	3	4	5	6	7	Dead rise.					
1.00	.1250	.2500	.3750	.5000	.6250	.7500	.8750	Flat bottom.					
1.05	.1127	.2333	.3571	.4830	.6105	.7393	.8692						
1.10	.1015	.2176	.3300	.4665	.5963	.7287	.8634						
1.15	.0915	.2031	.3237	.4506	.5824	.7183	.8577.	76.					
1.20	.0825	.1895	.3082	.4353	.5689	.7080	.8512	nt is,					
1.25	.0743	.1768	.2935	.4205	.5557	.6980	.8463	ri					
1.30	.0669	.1649	.2794	.4061	.5428	.6880	.8407	exponen					
1.35	.0604	.1539	.2660	.3923	.5302	.6782	.8351	2 2					
1.40	.0544	.1436	.2533	.3789	.5179	.6685	.8295	[X o					
1.45	.0490	.1340	.2303	.3660	.5047	.6589	.8240	- - =					
1.50	.0447	.1250	.2297	.3535	.4941	.6495	.8185	th is					
1.55	.0398	.1166	.2187	.3415	.4826	.6402	.8130						
1.60	.0359	.1088	.2082	.3299	.4714	.6311	.8076	higher higher					
1.65	.0323	.1015	.1982	.3186	.4605	.6221	.8023	බුල් බුල්					
1.70	.0291	.0947	.1887	.3078	.4498	.6132	.7969	22					
1.75	.0257	.0884	.1797	.2985	.4393	.6044 ·	.7916	The					
1.80	.0233	.0824	.1711	.2872	.4291	.5958	.7864	문관					
1.85	.0213	.0769	.1629	.2774	.4129	.5873	.7811						
1.90	.0192	.0718	.1551	.2680	.4094	.5789	.7759						
1.95	.0173	.0670	.1477	.2588	.4008	.5706	.7708	Highest					
2.00	.0156	.0625	.1406	.2500	.3905	.5625	.7656	dead rise.					

APPROXIMATE LENGTHS OF VESSELS.													
Displacem'nt in tons.							s. $X =$			_			
plac n t	•				L=	L = 1					L DAR	L=	L==
Dis	L = 5B	L = 6B	7B	$\frac{L}{8B}$	9B	10B	Displace ment.	L= 5B	$^{11}_{6B}$	7B	8B	9B	10B
T	L	L	L	L	L	L	T	L	L	L	L	L	L
1	16.6	18.3	20.3	22.2	24.0	25.8	1000	166	183	203	222	240	2:8
2	21.0	22.9	25.6	28.0	30.3	32.5	1100	171	189	210	230	248	267
3	24.0	26.4	29.3	32.0	34.6	37.2	1200	177	194	216	236	255	274
4	26.4	29:0	323	35.3	38.2	41·0 44·2	1300 1400	181	199	222	242	262	251
5 6	28.4	31·4 33·3	$\frac{34.8}{37.0}$	38·0 40·4	42.0 43.8	47.0	1500	186 190	$204 \\ 210$	$\begin{bmatrix} 2.6 \\ 233 \end{bmatrix}$	$\frac{249}{255}$	$\begin{vmatrix} 269 \\ 275 \end{vmatrix}$	288
7	31.7	34.9	38.8	42.4	46.0	49.3	1600	195	214	238	260	281	302
8	33.2	36.6	40.6	44.4	48.0	51.4	1700	199	218	243	265	286	:05
9	34.6	38 0	42.2	46.2	50.0	53.7	1800	202	223	248	270	292	314
10	35.7	39.3	43.7	47.8	51.7	55.5	1900	206	227	252	275	298	320
11 12	$36.9 \ 38.0$	40.6 41.9	45·1 46·6	49·3 50·9	53·4 55·0	57·3 59·1	$\begin{bmatrix} 2000 \\ 2100 \end{bmatrix}$	210 212	$\begin{array}{c} 230 \\ 234 \end{array}$	$\frac{256}{260}$	280 2×5	302 307	525 330
13	39 0	43.0	47.8	52.2	56.5	60.6	2200	216	238	265	290	312	335
14	40.0	44.0		53.6	58.0	62.2	2300	220	242	269	295	317	341
15	40.9	45.0	50.0	54.7	59.0	63.5	2400	223	245	272	300	322	346
16	41.8	460	51.2	56.0	60.6	65.0	2500	226	248	276	304	326	351
17	42·7 43·6	$\frac{46.9}{47.8}$	52·2 53·2	57 0 58·0	61·8 63 0	66·3 67·7	2600 2700	$\begin{array}{c} 229 \\ 232 \end{array}$	$\begin{array}{c} 252 \\ 255 \end{array}$	$\frac{280}{283}$	308	330	355
18 19	44.4	48.6	54.2	59.0	64.2	69.0	$\begin{vmatrix} \tilde{2}800 \\ 2 \end{vmatrix}$	235	$\begin{array}{c} 259 \\ 259 \end{array}$	287	311 315	334 338	360
20	45.0	49.5	55.1	60 0	65.2	70.0	2900	238	261	290	318	342	369
25	48.5	53.4	59.2	64.8	70.2	75.4	3000	240	264	294	321	347	373
30	51.6	57.0	63.3	69.0	74.7	80.2	3100	243	267	297	324	350	377
35	54.3	59.6	66.4	72.7	78 6	84.3	3200	246	270	300	327	354	381
40 45	$56.8 \ 59.2$	62·6 65·0	69.5 72.3	$76.0 \\ 79.0$	82·2 85·5	88·3 92·0	$\begin{bmatrix} 3300 \\ 3400 \end{bmatrix}$	248 250	272 275	303 306	330 333	358 362	385 389
50	61.2	67.2	74.8	81.8	88.4	95.0	3500	253	278	309	337	365	393
55	63.1	69.4	77.3	84.4	91.4	98.0	3600	255	281	312	340	369	396
60	64.9	71.4	79.4	86.8	93.9	101	3700	257	283	314	344	372	399
65	668	73.5	81.7	89.3	96.6	104	3800	260	285	317	347	375	403
70 75	68.4	75·3 77·1	83·7 85·8	91.6	98·0 101	107 109	$\begin{array}{ c c c c }\hline 3900 \\ 4000 \\ \end{array}$	$\begin{bmatrix} 262 \\ 265 \end{bmatrix}$	288 291	$\begin{bmatrix} 320 \\ 323 \end{bmatrix}$	350 353	378 380	406
80	71.6	78.9	87.6	95.7	103	111	4100	268	293	$\frac{325}{325}$	356	3:3	413
85	73.0	80.5	89.5	97.7	106	114	4200	270	296	328	359	386	417
90	74.5	81.9	91.1	996	108	116	4300	272	298	331	362	389	420
95	75.8	83.4	92.7	111	100	118	4400	273	300	334	365	392	423
100	77·0 79·7	84·7 87·6	94·4 97·4	103 107	112 115	$\begin{array}{c} 120 \\ 124 \end{array}$	4500 4600	275 277	302 304	337 339	368 370	395 398	426
125	83 0		100	111	120	129	4700	279	306	331	372	401	402
150	88.3	97.0	108	113	128	137	4800	281	308	343	374	404	435
175	93.0	102	114	124	134	144	4900	283	310	345	376	407	438
200	97.3	107	119	130	140	151	5000	286	312	348	378	411	441
225	101 105	111	124 128	135 140	146 152	157 163	5250 5500	289 • 294	318 323	354 359	$\frac{386}{392}$	418 424	450 457
275	108	119	132	145	156	168	5750	298	331	364	398	430	463
300	111	122	136	149	161	173	6000	303	336	370	404	437	469
325	114	126	140	153	165	178	6250	307	340	375	409	443	476
350	117	129	143	157	170	182	6500	310	345	380	414	448	4.82
375	120 122	130 135	147 150	161 164	173 177	186 191	6750 7000	315 319	349 354	384 389	420 425	454 460	488 494
450	128	140	156	170	184	198	7250	$\frac{313}{322}$	358	394	430	465	500
500	132	145	161	176	191	205	7500	326	361	398	435	470	506
550	136	150	166	182	197	211	7750	330	365	402	440	475	512
660	140	154	171	188	202	217	8000	333	370	407	445	480	517
650	144 148	$\begin{array}{ c c }\hline 158 \\ 162 \\ \end{array}$	176 180	193 197	$\frac{208}{213}$	223 229	8250 8500	337 340	374 377	410 415	449 453	485 490	522 527
750	151	166	185	202	218	235	8750	343	380	419	457	495	532
800	154	170	189	206	223	240	9600	347	354	423	461	500	537
850	158	173	193	210	227	245	9250	350	388	427	466	504	542
900	160	176		215	232	250	9500	353	392	430	470	509	547
950	163	1 0	200	219	236	254	10000	359	399	438	478	517	556

APPROXIMATE LENGTHS OF VESSELS. 40:															
Displacem'nt	e l			'au I	V	esso	els.		$\mathfrak{M}n =$	16.	Dno	q = 0	6×1	1.	
acei	in tons.	:							 id draf			-			
ldsi	in	L=	L=		L =	L=	L=		Displace-	L = 1	L=	L=1	L =	L =	L =
		5B	6B	7B.	8B	9B	10B	-	ment.	5B	6B	7B	8B	9B	10B
,	r 1	L 10.9	L 14·6	16·2	L 17.8	L 19·2	L 20.6		T 1000	L 109	L 146	$f L \\ 162$	178	L 192	206
	2	13.7	18:3	20.4	22.4	24.2	26.0		1100	112	151	166	184	192	213
	3	15.7	21.0	23.4	25.7	27.7	29.7		1200	116	155	173	190	205	219
	4 . 5	17.3	23.2	25.8	28.3	30.5	32.8		1300 1400	119	160	177	195	210	225
	6	18.7 19.8	25·0 26·6	27.7	30·4 32· 4	$\frac{32.8}{34.9}$	35·2 37·6		1500	122 125	164 167	180 184	199 204	$\begin{array}{c c} 216 \\ 221 \end{array}$	$\begin{vmatrix} 230 \\ 235 \end{vmatrix}$
	7	20.8	28.0	31.0	34.0	36.7	39.4	II.	1600	127	171	188	208	226	240
	8	21.8	29.2	32.4	35 6	38.4	41.2	ł	1700	130	174	193	212	230	245
	9 10	22·7 23·5	30·4 31·4	33·7 34·9	37.0	40.0	42·8 44·3	Н	1800 1900	132 135	177	198	217 220	235 239	250 255
	11	24.2	32.4	36.0	39.5	42.6	45.7	Ш	2000	137	184	205	224	243	260
	12	25.0	33.3	37.1	40.7	44.0	47.2	Н	2100	139	188	208	228	247	264
	13 14	25·6 26·3	34·3 35·2	38.1	41·8 42·9	45·1 46·2	48.4		2300 2300	141	190 193	211 214	231 234	251 254	$ \begin{array}{c c} 268 \\ 272 \\ \end{array} $
	15	26.8	36:0	39 9	43.8	47.2	507		2400	146	195	214	238	258	276
	16	27.5	36.8	40.9	44 8	48.4	51.8		2500	148	198	220	242	261	280
	17 18	28·0 28·5	37 5	41.8	45·7 46·6	49·4 50·3	52·9 54·0		2600 2700	$\frac{150}{152}$	200	223 226	245 248	264 267	284 287
	19	$\frac{28.0}{29.0}$	$\frac{38.3}{39.0}$	43.4	17.4	51.3	56.0		2800	154	205	228	251	270	290
	20	29.5	39.6	44.2	48.2	52.0	58.0	Н	2900	155	208	231	254	274	294
	25	31.8	42.6	45.4	52.0	56.1	60.0	Ш	3000	157	211	234	257	277	297
	30 35	33·9 35·6	45.5 47.8	50.5	55·3 58·1	59.9	64.0	H	3100 3200	159 160	213	$\frac{237}{240}$	260	280 284	300 304
	40	37.3	500	55.6	60.8	65.7	70.4		3300	162	218	242	264	287	307
	45	38.8	52.0	57.8	63.3	68.4	73.3	П	3400	164	220	245	267	290	310
	50 55	40.1	53.8 55.5	59.8	65·5 67·7	70.7	75·7 78·2	11	3500 3600	166 167	222 225	248 250	$\frac{270}{272}$	292	313
	60	42.6	57.1	63.5	69.5	75.2	80.4	Н	3700	169	226	252	275	297	319
	65	43.8	58.7	65.2	71.5	77:4	82.7	Н	3800	171	228	254	278	299	322
	70 75	45·0 46·0	60.2	66.9	73.4	79·2 81·2	85.0	I	3900 4000	172 173	230 232	255	280 283	302	325 327
	80	47.0	63.0		77.0	82.9	88.8		4100	174	234	261	285	308	330
	85	47.9	64.2		78.2	84.6	90.5		4200	175	236	263	287	310	333
	90 95	48 8	65.5		79·7 81·3	86.3	92.3		4300 4400	177	238 240	265 267	$\begin{vmatrix} 289 \\ 291 \end{vmatrix}$	312 314	336
1 1	.00	50.5	67.8	75.4	82.7	89.2	95.6	П	4500	179	242	269	294	317	340
	10	52.2	70.0	78.0	85.3	92.2	98.5		4600	181	244	271	296	320	343
	25	55.0	73.0		89.0	95.0			4700 4800	182	246	273	298	322	345
	50 175	57.8	77:5 81:6		94.5	102	110 115		4900	184 185	248 249	275 276	300	324 326	347 350
2	000	63.6	85.4	95.2	104	113	120		5000	187	250	277	304	329	352
	225 250	66 2	88.9			117	125 130		5250 5500	190	254 258	278 287	309	334	354 356
	30 275	68.7	92 0 95·0			121 125	134		5750	196	262	291	315	345	369
3	800	72 8	97.8	109	119	129	138	Н	6000	198	266	295	324	350	374
	325	74.0				132		1	6250	200	269	300	328	354	383
	350 375	76.8 78.7	106		$\begin{vmatrix} 126 \\ 129 \end{vmatrix}$	136 139	146		6500 6750	203 206	273 276	303	332	359 364	384
4	600	80.3	108		132	142			7000	209	280	311	340	368	394
	£50	85.5			137	148	158		7250	211	283	314	344	372	399
	500 550	86.4				153 158	164 169		7500	213 216	286 289	318	348	376	404
- €	600	91 9	123	136			174		8000	218	292	325	356	384	412
	350	94.4		140	154	167	178		8250	220	296	328	360	388	417
	700 750	98.9				170 173	183 187		8500 8750	222 224	299	331 334	364 367	392	421 425
1 8	800	101				177	191		9000	226	304	337	370	400	429
	350	103	139	154	169	182	195		9250	229	307	340	374	404	432
	900	105 197				$\begin{array}{c} 186 \\ 189 \end{array}$		1	9580 10000	231 235	310	314 350	$\begin{vmatrix} 377 \\ 381 \end{vmatrix}$	408	$\begin{array}{c} 437 \\ 446 \end{array}$
1	UCC	1 777	144	109	119	199	400		10000	• 200	. 919	990	100 £	414	440

Horsepower in Steamship Performance.												
Displace-			Na	utical r	niles or	knots p	er hou	r.				
ment in tons.	1	2	3	4	5	6	7	8.	9	10		
T	H	H	H	H	H	H	H	H	H	H		
1	0.004	0.035	0.118	0.280	0.550	0.949	1.50	2.24	3.20	4.38		
2 3	0.007	0.055	0.190	0.444	0.870 1.14	1.51	2.40	3.55	5.08	6 96		
4	0.010	0.084	0.300	0.673	1.40	1.98 2.40	3·12 3·80	4·79 5·39	6·91 8 06	9.12		
5	0.012	0.102	0.348	0.818	1.52	2.78	4.40	6.55	9.36	12.2		
6	0.014	0.115	0.390	0.924	1.81	3.12	4.96	7.39	106	14.5		
8	0.016	0·128 0·138	0.435	1.025 1.125	2.01	3.48	5.50	8.20	11.7	16.1		
9.	0.019	0.151	0.501	1.211	2 20 2·38	3·80 4·12	6.01	8.96	12·8 13·8	17·5 19·0		
10	0.020	0.161	0.552	1.30	2.54	4.42	6.98	10.4	14.9	20.3		
11	0.022	0.175	0.590	1.40	2.72	4.70	7.46	11.1	15.9	21.8		
12 13	0.023	0.185	0 624	1.48	2.88	4.99	7.90	11.8	16.8	23.0		
14	0.024	0.198	0.654	1·56 1·62	3·04 3·18	5·25 5·52	8·33 8·75	12·5 13·0	17·7 18·6	24.3		
15	0.026	0.213	0.725	1.70	3.32	5.80	9.20	13.6	19.5	25·4 26·6		
16	0.028	0.223	0.780	1.78	3.49	6.04	9.55	14.2	20.4	27.9		
17	0.029	0.236	0.785	1.89	3.64	6.58	9.95	15.0	21.2	29.1		
19	0·030 0·03 1	0.242	0.815	1.94 2.00	3·78 3·90	6·52 6·80	10·3 10·7	15.5	22.0	30.2		
20	0.032	0.258	0.875	2.06	4.02	7.00	11.1	16·0 16·5	22 8 23·0	31·2 32·2		
25	0 038	0.300	1.015	2.40	4.14	8.12	12.9	19.2	$24 \cdot 2$	33.1		
30 35	0.042	0.333	1.14	2.70	5.30	9.18	14.6	21.6	31.0	42.4		
40	0·047 0·050	0·375 0·409	1·26 1·39	3.00	5.89	10.1	16.2	24.0	34.2	47.1		
45	0.056	0.445	1 50	3.21	6·41 6·95	11·1 12·0	17·6 19·0	26·2 28·5	37·5 40·5	51·3 55·6		
50	0.056	0.474	1.61	3.79	7.44	129	20.5	30.3	43.2	59.5		
55	0.062	0.501	1.72	4.06	7.95	13.8	21.8	32.5	46.2	63.6		
60 65	0·067 0·071	0·538 0·570	1.80 1.90	4·30 4·56	8:41	14.4	23.1	34.4	49.1	67.3		
70	0.074	0.597	2.02	4.77	8·88 9·36	15·1 16·2	24·4 25·5	36·5 38·2	51·8 54·4	71·0 74·9		
75	0.078	0.625	2.12	5.00	9 77	16.9	26.8	40.0	56.8	78.0		
80	0.081	0.620	2.20	5.50	10.2	176	28 0	41.6	58.1	81.6		
85 90	0·085 0·088	0 680	2.30	5.44	10.6	184	29.2	43.5	62 0	85.0		
95	0.088	0.710	2.49	5 64 5 68	11·0 11·4	19·1 19·9	30·5 31·3	45·2 47·0	64·5 66·6	88.4		
100	0.094	0.755	2.56	6.04	11.8	20.5	32.4	48.4	68 5	91·5 94·5		
110	0.101	0 810	2.73	6.48	12.6	21.9	34.6	51.8	73.2	101		
125 150	0·109 0·124	0.877	2.98	7.02	13.7	23.8	37.5	56.2	80.0	110		
175	0.138	1.10	3.38	7·72 8·81	15 5 17·2	27·0 29·8	42·8 47·2	61·7 70·5	90.5	124		
200	0.150	1.20	4.06	9.60	18.8	32.5	51.5	76.9	100 110	138 150		
225 250	0.162	1 30	4.39	10.4	20.2	35.1	56.0	83.3	118	162		
275	0·175 0·188	1·40 1·50	4·70 5·04	11·2 11·9	21.9	37 6	59.8	89 2	127	175		
300	0.196	1.57	5.31	12 6	23·2 24·5	$\begin{array}{c c} 40.3 \\ 42.5 \end{array}$	63·8 67·5	95·2 100	$\begin{array}{c} 136 \\ 142 \end{array}$	186		
325	0.201	1.66	5.63	13.3	26.0	45.0	$71 \cdot 2$	106	152	196 208		
350 375	0 220	1.75	5.91	14 0	27 4	47.3	75.0	112	159	219		
400	0·228 0·240	1·82 1·91	6.12	14·6 15·3	28.6	49.0	78.4	117	166	229		
450	0.250	2.06	6.98	16.5	29·8 32·2	51·4 55·8	81·7 88·5	$\begin{array}{c c} 122 \\ 132 \end{array}$	172	238		
500	0.276	2.21	7.45	17.7	34.6	59.6	94.3	132	188 200	258 276		
550 600	0.295	2:36	7 98	18.9	36.9	63.8	101	151	215	295		
650	0·312 0·330	2·50 2·64	8.40	$20.0 \\ 21.1$	39.0	67.2	107	160	226	313		
700	0.348	2.78	9.32	22.2	41·2 43·3	71·2 74·6	113 119	169 177	240 250	329		
750	0.362	2.90	9.80	23.2	45.2	78.4	119	186	264	337 352		
800 850	0.380	3.03	10.2	24.2	47.3	81.5	150	194	274	378		
900	0·394 0·410	3·15 3·28	10 6 11·0	$25\cdot2$ $26\cdot2$	49.2	85.0	135	202	288	394		
950	0.422		11.4	27.3	51·1 53·1	88·1 91·8	140 146	210	296	409		
					.,,,,	010	110	218	310	445		

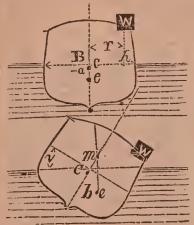
Horsepower in Steamship Performance.

701 2	Nautical miles or knots per hour.												
Displace- ment in				Nautic	al miles	or knot	ts per he	our.					
tons.	11	12	13	14	15	16	17	18	19	20			
\mathbf{T}	H	H	H	H	H	H	H	H	H	H			
1	5 85	7.59	9.63	12.0	14.8	17.9	21.6	25.6	30.1	35.1			
2	9.28	1:0	153	191	23.5	28.4	34 2	40 6	47.8	54.7			
3	12.2	15.8	20 0	25.0	30.8	38.3	44.8	53.3	62.6	73.0			
4	14.8	19 2	24 4	3(.3	37.4	43.1	54.3	64.5	75.9	88.4			
5	17.2	22.2	28 3	35.2	4:5:4	52.4	€30	74.9	88.0	97.8			
6	19.4	25·1 27·8	31.9	39 7	49.0	59.1	71.1	84.5	99.2	116			
8	21.4	30.4	35·3 £8·6	44.0	54.0	65.5	79.0	93.7	110	128			
9	25.3	32.9	418	48·1 52·1	59·3 64·0	68·7 77·5	86·2 93·2	102	121	140			
10	27 2	35.3	44.8	55.8	68.8	83.2	100	110 119	130 140	152 163			
11	29.0	37.6	47.8	59.7	73.5	89.0	107	127	150	174			
12	307	39.9	5 0 6	63 2	77.7	94 4	113	134	158	184			
13	32.4	42.0	53 3	66.6	82.0	99.6	120	142	167	194			
14	34 0	44.2	£6·0	70.0	86.0	105	126	149	176	203			
15	35.6	46.3	58.7	73.5	90.0	109	131	156	183	213			
16	37.2	48.3	61.3	76.5	94.0	114	137	163	192	223			
17	38.7	50.2	63.8	79.6	· 98·0	120	143	170	200	233			
18 19	40·2 41·7	52.2	66·2 68·7	82·7 85·8	102 106	124	148	176	207	242			
20	43.2	56.0	71 0	88.9	111	128 132	154 159	182 189	215 222	250 258			
25	50.0	65.0	52.5	103	127	154	184	194	258	265			
30	56.5	73.4	93.2	117	143	173	208	248	291	339			
35	62.6	81.3	103	130	159	192	2:0	274	322	377			
40	68.4	88.8	113	141	173	209	252	300	350	410			
45	74.0	962	122	152	188	228	273	324	382	445			
50	79.4	103	131	164	201	242	293	346	410	476			
55 60	84.6	110	140	174 185	215 226	$\frac{200}{285}$	312 330	370 393	437 464	509 538			
65	94.7	123	156	195	240	292	\$ 4 9	414	488	568			
70	99.6	130	164	206	252	306	367	437	512	599			
75	104	135	171	214	264	320	383	455	536	624			
80	109	141	180	224	276	333	400	467	561	€53			
85	113	147	187	234	287	₹48	417	496	584	680			
90	118	153	194	243	298	362	433	516	607	707			
100	122 126	158 164	201 207	251 259	309 318	376 387	448 464	533 551	629 648	732 756			
110	135	175	222	277	340	414	495	588	693	807			
125	146	190	241	300	370	450	539	640	753	878			
150	165	215	273	342	420	494	669	724	852	992			
175	183	238	302	378	464	564	675	862	946	1100			
200	200	260	330	412	506	615	737	875	1027	1201			
225 250	217 232	281 301	358	447 478	548	666 714	800 855	947 1016	1118 1200	1300			
275	248	322	409	510	627	762	912	1010	1286	1490			
300	262	340	432	540	662	806	966	1146	1347	1573			
325	277	360	457	570	700	852	1010	1213	1428	1665			
350	290	378	480	600	737	896	1073	1276	1500	1750			
375	305	395	502	627	770	936	1122	1332	1570	1830			
400	317	412	522	654	803	976	1170	1402	1632	1907			
450 500	343 368	446	567	708 7£9	870 932	1060 1131	1265 1358	1500 1611	1770 1896	$2065 \\ 2213$			
550	393	510	648	810	995	1210	1450	1720	2025	2362			
600	415	540	684	856	1036	1280	1532	1820	2140	2500			
650		570	724	905	11111	1350	1618	1923	2265	2636			
700	460	599	759	938	1166	1417	1700	2016	2373	2770			
750	483	6:7	797	995	1220	1485	1780	2113	2490	2900			
800	503	654	830 866	1038	1274 1330	1548 1620	1857 1935	$2206 \\ 2300$	2593 2710	3026 3152			
900	1 545	708	895	1123	1380	1675	209	2385	2803	3274			
950	- ECF	73	632	1170	1430	1740	2080	2478	2920	3400			
,													

Horsepower in Steamship Performance.												
Displace- ment in						knots p						
tons.	1	$\frac{2}{2}$	3	4	5	6	7	8	9	10		
T	H	H	H	丑丑	H	H	H	11	H	H		
1000	0.438	3.50	11.8	28.0	54.9	94.6	150	225	318	439		
1100 1200	0.456	3·75 4·00	12·5 13·4	30.0	58·4 62·0	100 107	160 170	239 254	338 359	467		
1300	0.515	4.12	14.0	33.0	65.3	112	179	267	378	523		
1100	0.548	4.38	14.9	35.0	68.7	119	189	281	398	549		
1500	0.562	4.50	15.5	36.0	71.9	124	197	295	417	575		
1600 1700	0.578 0.594	$4.62 \\ 4.75$	16·2 16·9	37·0 38·0	75·0 78·1	130 135	206 215	307 320	$\frac{435}{453}$	600		
1800	0.625	5.00	17.5	40.0	81.2	140	224	332	470	649		
1900	0.634	5.25	18.1	42.0	84.2	145	231	345	488	673		
2000	0.700	5.60	18.8	44.0	87.0	150	239	356	504	696		
2100 2200	0.719	5·75 5·88	19.4	$\frac{460}{47.0}$	90.0	155 160	$\frac{247}{255}$	2'69 380	52 1 537	720 741		
2300	0.765	6.12	20.6	49.0	95.6	165	262	391	554	764		
2400	0.788	6.28	21.1	50 2	98.4	170	170	462	569	786		
2500	0.805	6.44	21.8	51.5	101	174	277	414	585	808		
2600 2700	0.828	6 62 6 81	22·4 23·0	53.0 54·5	104 . 106	179 184	$\begin{array}{c} 285 \\ 292 \end{array}$	4:4	$600 \\ 616$	826 850		
2800	0.872	6.98	23.5	55.8	109	188	299	446	631	871		
2900	0.876	7.12	24.0	57.1	111	192	306	457	646	893		
3000	0.909 0.931	7.35	24.6	58.8	114	197	313	467	660	913		
3100 3200	0.951	7.45 7.62	25·1 25·6	59·8 61·0	117 119	$\frac{201}{205}$	$\frac{320}{327}$	478 488	676 690	933 952		
3300	0 972	7.78	26.1	62.2	121	209	334	498	704	972		
3400	0.992	7.94	26.8	63.5	124	214	340	508	718	992		
3500	1.01	8.10	27.2	64.8	127	218	347	518	733	1010		
3600	1·03 1·05	8·25 8·39	27·8 28·2	66·0 67·1	129 131	$\begin{array}{c} 222 \\ 226 \end{array}$	$\frac{354}{360}$	528 538	746 759	1025 1049		
3800	1.08	8.60	27.8	68.5	133	230	367	548	774	1070		
3900	1.09	8.70	28.9	69.6	135	234	373	558	787	1087		
4000	1·11 1·13	8.85	29.9	70.8	138	238	380	567	801	1105		
4200	1.14	9·01 9·14	30·4 30·9	71·1 73·1	140 142	242 246	386 392	577 586	814 827	1122 1141		
4300	1.16	9:30	31.4	74.4	145	250	398	595	840	1160		
4400	1.18	9.42	31.9	75.5	147	254	404	604	853	1179		
4500	$1.19 \\ 1.22$	9.56	32·4 32·8	76·5 77·7	150	258	410	613	816	1198		
4700	1.23	$9.72 \\ 9.86$	33.4	78.9	152 154	$\begin{array}{c c} 261 \\ 266 \end{array}$	416	622 631	879 881	1216 1232		
4800	1.25	10.0	33.9	80.0	156	270	428	640	904	1248		
4900	1.28	10.1	34.4	81.1	158	274	434	649	916	1265		
5000	1·30 1·32	10·3 10·6	34.8 35.6	82·7 85·0	160 165	277	440	658	929	1282 1324		
5500	1.36	10.9	36 4	87.5	171	283 290	$\begin{array}{c} 455 \\ 469 \end{array}$	670 700	959 990	1524		
5750	1.40	11.2	37.5	90.0	176	298	483	721	1024	1408		
6000	1.42	11.4	38.0	92.8	181	303	497	742	1050	1448		
6250 6500	1·47 1·52	11·9 12·2	$40.2 \\ 41.2$	95.2	188 191	322	512	762	1065	1488 1526		
6750	1.56	12.5	42.4	97.8	196	330 339	526 540	782 802	$\begin{array}{c c} 1078 \\ 1123 \end{array}$	1557		
7000	1.60	12.9	43.2	103	202	346	554	822	1174	1616		
7250	1 64	13 1	44.4	105	205	355	566	842	1198	1644		
7500	1.68 1.72	13·5 13·8	45.5	108	210 215	364 372	579 599	861 879	$1226 \\ 1253$	1682 1719		
8000	1.75	14.0	47.4	112	$\begin{array}{c} 213 \\ 220 \end{array}$	379	603	899	$\begin{array}{c c} 1235 \\ 1280 \end{array}$	1757		
8250	1.78	14.2	48.4	115	224	387	615	918	1306	1793		
8500	1.81	14.5	49.4	116	229	395	628	929	1333	1829		
9000	1.84 1.88	14·9 15·2	50·0 51·1	$119 \\ 122$	233 238	403 411	640 653	955 973	1354 1385	1865 1902		
9250	1.92	15 4	52.2	124	242	418	668	991	1411	1937		
9560	1.95	15.6	53.2	126	246	426	683	1008	1437	1972		
10000	2.05	16.4	55.1	131	255	441	714	1044	1488	2042		

Horsepower in Steamship Performance.										
Displace	1		Na	autical	miles o	r knot	s per ho	ur.		
ment in tons.	11	12	13	14	15	16	17	18	19	20
T	Н	H	H	H	H	H	H	H	H	H
1000	585 622	759 806	$963 \\ 1024$	1206	1480	1798	2157	2560	3008	3514
1200	660	858	1024	$1284 \\ 1360$	1574 1670	1913 2030	2295 2435	2723 2890	3203 3400	3736 3967
1300	696	903	1147	1432	1758	2136	2564	3043	3576	4178
1400	732	950	1204	1508	1850	2248	2697	3200	3762	4394
1500	766	995	1264	1580	1938	2355	2825	3252	3943	4605
1600	800 833	1038 1083	1317 1374	1648 1718	$2020 \\ 2107$	$2458 \\ 2561$	2948 3072	3500 3646	4113	4803 5006
1800	864	1123	1422	1784	2188	2660	3140	3785	4448	5195
1900	897	1166	1479	1850	2270	2760	3310	3928	4615	5390
2000	927	1205	1527	1913	2345	2854	3420	4060	4770	5570
2100 2200	958 988	1247 1284	1582 1628	$\begin{vmatrix} 1979 \\ 2037 \end{vmatrix}$	2382	2948	3535	4195	4935	5762
2300	1017	1324	1680	2102	$2500 \\ 2578$	3038 3134	3642 3755	4325 4460	5084 5241	5935 6120
2400	1047	1360	1723	2160	2646	3220	3860	4580	5386	6290
2500	1077	1400	1777	2222	2725	3313	3970	4715	5542	6470
2600	1102	1435	1820	2280	2796	3400	4075	4835	5655	6637
2700 2800	1131 1160	1473 1508	1870 1911	2338 2395	$2868 \\ 2935$	3486 3568	4180 4280	4960 5076	5832 5970	6813 6970
2900	1189	1545	1960.	2452	3010	3655	4385	5200	6115	7142
3000	1215	1582	2000	2508	3075	3740	4485	5318	6255	7300
3100		1614	2048	2565	3145	3822 -	4585	5440	6394	7470
$\frac{3200}{3300}$	1268 1296	1648 1683	$2092 \\ 2134$	2616	3210	3905	4680	5550	6525	7622
3400		1717	2178	$2671 \\ 2725$	3280 3343	3985 4063	4775 4870	5670 5784	6666	7781 7936
3500		1750	2220	2779	3408	4143	4965	5893	6936	8090
3600		1783	2264	2830	3475	4222	5060	6010	7061	8250
3700		1815	2303	2881	3534	4300	5155	6115	7184	8400
$\frac{3800}{3900}$	1422 1446	1848 1880	$2348 \\ 2385$	2941 2986	3606 3660	4385 4453	5250 53 4 0	6238 6336	7333 7444	8563 8696
4000		1912	2427	3038	3725	4530	5430	6444	7580	8847
4100	1497	1944	2468	3086	3785	4610	5520	6550	7700	8988
4200		1975	2507	3137	3850	4680	5610	6655	7830	9141
4300 4400		2008	2546 2585	3186 3238	3910 3970	4750 4825	5700 5790	6761 6865	7950 8072	9285 9432
4500		2070	2624	3286	4025	4900	5875	6970	8195	9572
4600	1614	2100	2664	3333	4087	4935	5960	7070	8320	9710
4700		2130	2702	3382	4145	4970	6045	7172	8437	9850
4800		$2160 \\ 2190$	$\begin{vmatrix} 2740 \\ 2779 \end{vmatrix}$	3431 3478	4202 4260	5112 5193	6130 6215	7275 7375	8555	9990
5000		2220	2817	3525	4321	5253	6300	7475	8673 8792	10120
5250	1760	2293	2909	3640	4414	5426	6507	7723	9081	10601
5500		2365	3000	3755	4608	5600	6715	7972	9370	10953
$\begin{array}{c c} & 5750 \\ \hline & 6000 \end{array}$		2436 2507	3090 3180	3868	4744	5767 5935	6917 7120	8204	9652	11269
6250		2574	3261	3981 4094	4880 5013	6096	7313	8436 8519	9935	11586
6500	2035	2642	3352	4207	5146	6258	7505	8603	10472	12218
6750		2710	3438	4320	5281	6419	7698	8986	10741	12534
$\frac{17000}{7250}$		2778 2842	3524	4434	5417	6580	7892	9370	11010	12851
7500		2907	3606 3688	$4531 \\ 4629$	$5542 \\ 5668$	6733 6886	8076 8260	9587 9805	11265 11521	13152 13453
7750	2290	2971	3770	4276	5794	7039	8445	10022	11776	13754
8000		3036	3852	4824	5920	7192	8628	10240	12032	14056
8250 8500		3098	3931	4923	6042	7340	8806	10451	12280	14345
8750		3223	4011	5023 5123	6164	7488 7637	8984 9162	10662 10823	12528 12776	14634 14922
9000	2933	3286	4170	5222	6408	7785	9340	11084	13024	15211
9250		3346	4247	5343	6516	7926	9512	11289	13364	15493
$\begin{array}{ c c c }\hline 9500\\ 10000 \end{array}$		3407	4324	5465	6645	8068	9685	11494	13505.	15775
10000	2720	3529	1 4478	5708	6882	8351	10030	11904	13987	16340

To find the Momentum of Stability of a Vessel by Experiments.



W= weight in tons placed on deck at a distance r from the contre-line and h feet above the loadwater line, when the vessel is in equilibrium; v= careen angle, d= depth in feet of the centre of gravity of the vessel under meta-centre, Q= momentum of stability in foot-tons.

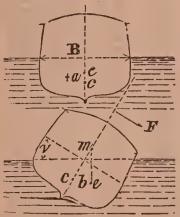
$$Q = W(r \cos v + h \sin v),$$

$$d = \frac{Q}{T \sin v}, \quad \sin v = \frac{Q}{T d}.$$

Example. The weight W=15 tons, the centre of gravity of which is placed at r=12 feet from centre on deck and h=8 feet above the water, which careens the vessel to an angle $v=2^{\circ}$. The displacement T=4288.8 tons. Required, the momentum of stability Q, and depth centre of gravity d?

$$Q = 15(12 \times \cos. 2^{\circ} + 8 \times \sin. 2^{\circ}) = 183.08$$
 foot-tons, and $d = \frac{183.08}{4288.8 \times 0.0349} = 1.223$ feet, the depth of the centre of gravity of the vessel, under meta-centre.

Momentum of Wind on Sails Careening a Vessel in Sailing.



Let F denote the force of wind in tons, acting at right angle to the vessel on the centre of gravity of all the sails, =l feet above the centre of gravity of the displacement. Then the momentum of the wind will be $=Q=Fl=Td\sin v$.

Example. The centre of gravity of all the sails being l=35 feet above the centre of gravity of the displacement of a vessel of T=4288.3 tons. The force of wind on all the sails F=7 tons. The depth of the centre of gravity of the vessel, under metacentre d=1.223 feet, as found by experiments. Required, the momentum Q of the wind, and to what angle the vessel will be careened?

$$Q = 7 \times 35 = 245$$
 foot-tons,
and, $\sin v = \frac{Q}{T d} = \frac{245}{4288.8 \times 1.223} = 0.04671$
= $\sin 2^{\circ} 40' 40''$, the careen angle required.

Tonnage of Vessels .- Old U.S. Measurement.

T= townage of vessel. L= length of the vessel in feet, from the fore part of the stem to the after part of the stern-post, measured on the upper deck. B= greatest beam in feet, measured above the main-walls. d= depth of the vessel in feet. For double-decked vessels, half the beam B is taken as the depth d. For single-decked vessels, the depth is taken from the underside of deck plank to the ceiling of the hold.

Example. L = 186 feet, B = 30 and d = 15, for a double-decked vessel. Re-

quired, the tonnage?

$$T = \frac{B d}{95} (L - 0.6B) = \frac{30 \times 15}{95} (180 - 0.6 \times 30) = 795.77 \text{ tons.}$$

Custom-House New Tonnage Law, May 6, 1864.

An Act to regulate the admeasurement of tonnage of ships and vessels of the U. S.

Be it enacted by the Senate and House of Representatives of the United States of America in Congress assembled. That every ship or vessel built within the United States, or that may be owned by a citizen or citizens thereof, on or after the first day of January, eighteen hundred and sixty-five, shall be measured and registered in the manner hereinafter provided; also every ship or vessel that is, now owned by a citizen or citizens of the United States, and shall be remeasured and reregistered upon her arrival after said day at a port of entry in the United States, and prior to her departure therefrom, in the same manner as hereinafter described: Provided, That any ship or vessel built within the United States after the passage of this Act may be measured and registered in the manner herein provided.

SEC. 2. And be it further enacted, That the register of every vessel shall express her length and breadth, together with her depth, and the height under third or spar deck, which shall be ascertained in the following manner: The tounage deck, in vessels having three or more decks to the hull, shall be the second deck from below; in all other cases the upper deck of the hull is to be the tonnage deck. The length from the forepart of the outer planking, on the side of the stem, to the after part of the main sternpost of screw steamers, and to the after part of the rudder-post of all other vessels measured on the top of the tonnage deck, shall be accounted the vessel's length. The breadth of the broadest part on the outside of the vessel shall be accounted the vessel's breadth of beam. A measure from the under side of tonnage deck plank, amidships, to the ceiling of the hold (average thickness) shall be accounted the depth of hold. If the vessel has a third deck, then the height from the top of the tonnage-deck plank to the under side of the upperdeck plank shall be accounted as the height under the spar deck. All measurements to be taken in feet and fractions of feet; and all fractions of feet shall be expressed in decimals.

SEC. 3. And be it further enacted, That the register tonnage of a vessel shall be her entire internal cubic capacity in tons of one hundred cubic feet each, to be ascertained as follows: Measure the length of the vessel in a straight line along the upper side of the tonnage deck, from the inside of the inner plank (average thickness) at the side of the stem to the inside of the plank on the sterntimbers (average thickness), deducting from this length what is due to the rake of the bow in the thickness of the deck, and what is due to the rake of the stern timber in the thickness of the deck, and also what is due to the rake of the stern timber in one-third of the round of the beam; divide the length so taken into the number of equal parts required by the following table according to the class in such table to

which the vessel belongs:

Table of Classes.

Class 1.—Vessels of which the tonnage length according to the above measurement is fifty feet or under, into six equal parts.

Class 2.—Vessels of which the tonnage length according to the above measurement is above fifty feet, and not exceeding one hundred feet long, into eight equal parts.

Class 3.—Vessels of which the tonnage length according to the above measurement is above one hundred feet long, and not exceeding one hundred and fifty feet long, into ten equal parts.

Class 4.—Vessels of which the tonnage length according to the above measurement is above one hundred and fifty feet, and not exceeding two hundred feet long,

into twelve equal parts.

Class 5.—Vessels of which the tonnage length according to the above measurement is above two hundred feet, and not exceeding two hundred and fifty feet long, into fourteen equal parts.

Class 6.—Vessels of which the tonnage length according to the above measurement is above two hundred and fifty feet long, into sixteen equal parts.

Then, the hold being sufficiently cleared to admit of the required depths and breadths being properly taken, find the transverse area of such vessel at each point

of division of the length as follows:

* Measure the depth at each point of division from a point at a distance of one-third of the round of the beam below such deck, or, in case of a break below a line stretched in continuation thereof, to the upper side of the floor timber, the inside of the limber strake, after deducting the average thickness of the ceiling, which is between the bilge planks and limber strake; then, if the depth at the midship division of the length do not exceed sixteen feet, divide each depth into four equal parts: then measure the inside horizontal breadth, at each of the three points of division, and also at the upper and lower points of the depth, extending each measurement to the average thickness of that part of the ceiling which is between the points of measurement; number these breadths from above (numbering the upper breadth one, and so on down to the lowest breadth); multiply the second and fourth by four, and the third by two; add these products together, and to the sum add the first breadth and the last, or fifth; multiply the quantity thus obtained by one-third of the common interval between the breadths, and the product shall be deemed the transverse area; but if the midship depth exceed sixteen feet, divide each depth into six equal parts, instead of four, and measure as before directed, the horizontal breadths at the five points of division, also at the upper and lower points of the depth; number them from above as before; multiply the second, fourth and sixth by four, and the third and fifth by two; add these products together, and to the sum add the first breadth and the last, or seventh; multiply the quantities. thus obtained by one-third of the common inte[r]val between the breadths, and the product shall be deemed the transverse area.

Having thus ascertained the transverse area at each point of division of the vessel, as required above, proceed to ascertain the register tonnage of the vessel in

the following manner:

Number the areas successively one, two, three, etc., number one being at the extreme limit of the length at the bow, and the last number at the extreme limit of the length at the stern; then whether the length be divided, according to table, into six or sixteen parts, as in classes one and six, or any intermediate number, as in classes two, three, four and five, multiply the second and every even-numbered area by four, and the third and every odd-numbered area (except the first and last) by two; add these products together, and to the sum add the first and last if they yield anything; multiply the quantities thus obtained by one-third of the common interval between the areas, and the product will be the cubical contents of the space under the tonnage deck; divide this product by one hundred, and the quotient, being the tonnage under the tonnage deck, shall be deemed to be the register tonnage of the vessel, subject to the additions hereinafter mentioned.

If there be a break, a poop, or any other permanent closed-in space on the upper decks, on the spar deck available for cargo or stores, or for the berthing or accommodation of passengers or crew, the tonnage of such space shall be ascertained as

follows:

Measure the internal mean length of such space in feet, and divide it into an even number of equal parts, of which the distance asunder shall be most nearly equal to those into which the length of the tonnage deck has been divided; measure at the middle of its height the inside breadths—namely, one at each end and at each of the points of division, numbering them successively, one, two, three, etc.; then to the sum of the end breadths, add four times the sum of the even-numbered breadths and twice the sum of the odd-numbered breadths, except the first and last, and multiply the whole sum by one-third of the common interval between the breadths; the product will give the mean horizontal area of such space; then measure the mean height between the plank of the decks, and multiply by it the mean horizontal area; divide the product by one hundred, and the quotient shall be deemed to be the tonnage of such space, and shall be added to the tonnage nuder the tonnage decks, ascertained as aforesaid.

If a vessel has a third deck, or spar deck, the tonnage of the space between it

and the tonnage deck shall be ascertained as follows:

Measure in feet the inside length of the space, at the middle of its height, from the plank at the side of the stem to the plank on the timbers at the stern, and divide the length into the same number of equal parts into which the length of the tonnage deck is divided; measure (also at the middle of its height) the in-

side breadth of the space at each of the points of division, also the breadth of the stem and the breadth at the stern; number them successively one, two, three and so forth, commencing at the stem; multiply the second and all other even-numbered breadths by four, and the third and all the other odd-numbered breadths (except the first and last) by two; to the sum of these products add the first and last breadths, multiply the whole sum by one-third of the common interval between the breadths, and the result will give, in superficial feet, the mean horizontal area of such space; measure the mean height between the plank of the two decks, and multiply by it the mean horizontal area; and the product will be the cubical contents of the space; divide this product by one hundred, and the quotient shall be deemed to be the tonnage of such space, and shall be added to the other tonnage of the vessel, ascertained as aforesaid. And if the vessel has more than three decks, the tonnage of each space between decks, above the tonnage deck, shall be severally ascertained in manner above described and shall be added to the tonnage of the vessel, ascertained as aforesaid.

In ascertaining the tonnage of open vessels the upper edge of the upper strake is to form the boundary line of measurement, and the depth shall be taken from an athwartship line, extending from edge of said strake at each division of the length.

The register of a vessel shall express the number of decks, the tonnage under the tonnage deck, that of the between decks, above the tonnage deck; also that of the poop or other enclosed spaces above the deck, each separately. In every registered United States ship or vessel the number denoting the total registered tonnage shall be deeply carved or otherwise permanently marked on her main beam, and shall be so continued; and if at any time it cease to be so continued, such vessel shall no longer be recognized as a registered United States vessel.

SEC. 4. And be it further enacted, That the charge for the measurement of tonnage and certifying the same shall not exceed the sum of one dollar and fifty cents for each transverse section under the tonnage deck; and the sum of three dollars for measuring each between decks above the tonnage deck; and the sum of one dollar and fifty cents for each poop, or closed-if space available for cargo or stores, or for the berthing or accommodation of passengers, or officers and crew, above the

upper or spar deck.

Sec. 5. And be it further enacted, That the provisions of this act shall not be deemed to apply to any vessel not required by law to be registered, or enrolled, or licensed, and all acts and parts of acts inconsistent with the provisions of this act are hereby repealed.

English Tonnage Measurement.

Divide the length of the upper deck between the after part of the stem and the fore part of the stern-post into 6 equal parts, and note the foremost, middle and aftermost points of division. Measure the depths at these three points in feet and tenths of a foot, also the depths from the under side of the upper deck to the ceiling at the limber strake; or in case of a break in the upper deck, from a line stretched in continuation of the deck. For the breadths, divide each depth into 5 equal parts, and measure the inside breadths at the following points, viz.: at .2 and .8 from the upper deck of the foremost and aftermost depths, and at .4 and .8 from the upper deck of the amidship depth. Take the length, at half the amidship depth, from the after part of the stem to the fore part of the stern-post.

Then, to twice the amidship depth, add the foremost and aftermost depths for the sum of the depths; and add together the foremost upper and lower breadths, 3 times the upper breadth with the lower breadth at the midship, and the upper and

twice the lower breadth at the after division for the sum of the breadths.

Multiply together the sum of the depths, the sum of the breadths, and the length,

and divide the product by 3500, which will give the number of tons, or register.

If the vessel has a poop or half deck, or a break in the upper deck, measure the inside mean length, breadth and height of such part thereof as may be included within the bulkhead; multiply these three measurements together, and divide the product by 92.4. The quotient will be the number of tons to be added to the result as above ascertained.

For Open Vessels.—The depths are to be taken from the upper edge of the upper

strake.

For Steam Vessels.—The timnage due to the engine-room is deducted from the

total tonnage computed by the above rule.

To determine this, measure the inside length of the engine-room from the foremast to the aftermost bulkhead; then multiply this length by the midship depth of the vessel, and the product by the inside amidship breadth at 4 of the depth from the deck, and divide the final product by 92.4.

CENTRIPETAL PROPELLER.

THE Centripetal Propeller has, since the year 1851, faught its way through the usual obstructions to success, and is now approved and adopted by the most advanced engineers in Europe and America. From the course of progress, it appears that the form of propeller now in use has not been reached through scientific investigations, but through the usual and expensive course of trials and errors, by which it has gradually approached the form represented on Plate XI., and according to the present rate of progress that shape will no doubt be reached and finally adopted within a few years more.

The propellers constructed by John Roach for the Pacific Mail Steamship Company are upon the centripetal principle, a full description of which is given in a work entitled "Education and Shipbuilding," published in the year 1866, by H. C.

Baird, Philadelphia.

The helicoidal or propelling surface in the common propeller is formed by a straight generatrix at right angle to the axis; whilst in the centripetal propeller that surface is formed by a spiral generatrix constructed in an angle w, Formula 7. In practice this angle can be assumed to be,

 $w=30^{\circ}$ for the fore-edge, and $w'=45^{\circ}$ for the after-edge of the propeller.

The difference between the angles w and w' makes the pitch expanding from the centre to the periphery.

Ilaving given the spirals a and e, the spirals b, e and d are obtained by dividing

the angles into four equal parts, as will be understood by the illustration.

A straight generatrix inclined to the axis will give the same helicoidal surface as that of the curved generatrix at right angles to the axis; but the inclination of the straight generatrix must be according to Formula 8.

The dotted lines fghi represent a centripetal propeller with straight inclined generatrix. Propellers constructed either as the dotted or drawn lines, or between the two cases, will produce the same propelling effect in the water. When the propeller is constructed between the two cases represented on the drawing, the

propeller is constructed between the two cases represented on the grawing, the blades will appear curved in both views.

The length L of the propeller should be from 0·2D to 0·25D, and the pitch from 1·5D to 2D. For very sharp vessels constructed for speed, and when the draft of water is over one-half the beam, the pitch may be made 2·5D.

One quarter of the pitch is set off on the centre line from 0 to 8, and the helix constructed in the ordinary way. The outer edge of the blades should not follow the true helix, but be made slightly concave, as shown in the drawing, which makes the pitch expanding in the direction of the axis.

The mean pitch of the propeller should be calculated by Formula 3, making

The mean pitch of the propeller should be calculated by Formula 3, making r = 0.7R.

Example 1. The diameter of a propeller is 10 feet 6 inches, and the angle $W=58^{\circ}$ at the periphery. Required the pitch P= in feet?

$$P = \cot.58^{\circ} \times 3.14 \times 10.5 = 20.6$$
 feet.

Example 2. The propeller on Plate XI. is of dimensions D=15 feet, L=5 feet, $W=57^{\circ}$ 30', the slip is 38 per cent. or S=0.38. What power is required to drive it 40 revolutions per minute, H=?

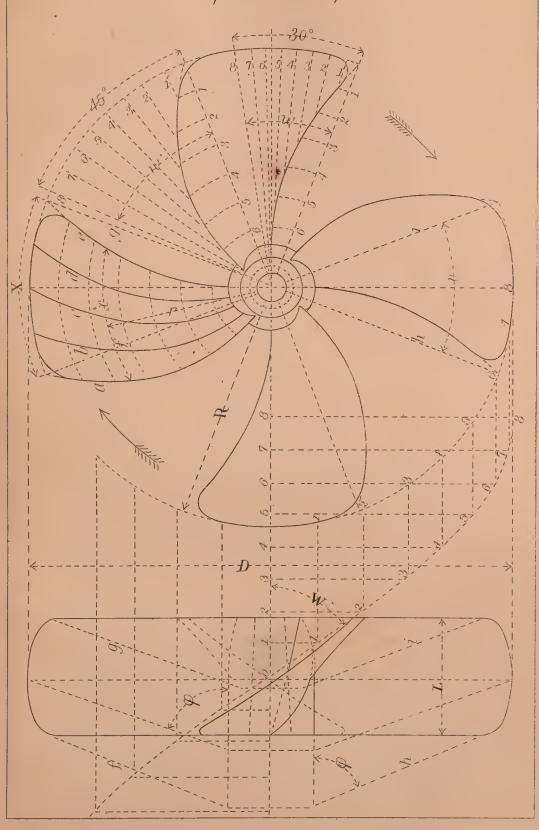
$$H = \frac{15^3 \times 40^3}{480000} \left(5 \times 0.38 \times \cos.57^{\circ} 30' + 0.11 \right) = 509 \text{ horses, nearly.}$$

Example 3. A propeller of diameter D=12 feet, angle $W=64^{\circ}$, and length L=3 feet 6 inches, is to be driven by a steam engine of 450 horses, the slip S = 0.28. How many revolutions will it make per minute, n = ?

$$n = \frac{78}{12} \sqrt[3]{\frac{450}{(3.5 \times 0.28 \times \cos.64^{\circ} + 0.11)}} = 61 \text{ revolutions}$$

per minute.

Centripital Propeller.





Pitch.

P=
$$\pi D \cot W 1$$

Cot. $W = \frac{P}{\pi D}$, 5

 $a = \frac{D^2 L m}{P}$, - 9

 $P = \frac{360 L}{v}$, - 2

 $v = \frac{360 L}{P}$, - 6

 $A = \frac{D m}{3.5} (L + X)$, - 10

 $A = \frac{2 \pi r}{\sqrt{x^2 - L^2}}$, 3

 $A = \frac{D m^2 S^2}{102.4}$, - 7

 $A = \frac{D}{2.75} (P + \sqrt{\pi^2 D^2 + P^2})$, 11

 $A = \frac{D^2 L m}{4}$, - 4

 $A = \frac{D m}{2.75} (L + X)$, - 10

Horsepower and Revolutions.

$$H = \frac{D^2 n^3}{480000} \left(L S \cos W + 0.11 \right), 13 \left| n = \frac{78}{D} \sqrt[3]{\frac{H}{L S \cos W + 0.11}}, 14 \right|$$

Horsepower of Frietion.

$$h = \frac{R L k m n^3}{59,400,000 P} \left(311.7 R^4 + 26.42 R^2 P^2 + P^4\right), - - 15$$

D = diameter, R = radius, L = length, and P = pitch of the propeller in feet.

W = angle of the blades to the centre line.

v = projecting angle of each blade.

w = centripetal angle for the curved generatrix.

 $\phi = \text{angle of inclination of the straight generatrix.}$ $\mathbf{a} = \text{projecting area of all the blades.}$

A =helicoidal surface of the propelling side of all the blades. a =helicoidal surface of one whole convolution.

O = acting area at right angles to the axis. All areas in square feet.

x = length of any helix at radius r, and m = number of blades.

X = length of external helix of the blade.

n = number of revolutions per minute.

H =horsepower required to drive the propeller.

h =horsepower required for friction in the water.

k = friction coefficient. See page 448.

The pitch of the propeller is equal to the tabular number opposite the year angle W multiplied by the diameter.

given angle 17, muruphed by the diameter.											
W	Pitch.	W	Pitch.	W	Pitch.	w	Pitch.	w	Pitch.	w	Pitch.
30	5.45	40	3.74	50	2.63	60	1.81	70	1.14	80	0.55
31	5.23	41	3.62	51	2.54	61	1.74	71	1.11	81	0.50
32	5.03	42	3.20	52	2.45	62	1.67	72	1.02	82	0.44
33	4.85	43	3.27	53	2.37	63	1.60	73	0.96	83	0.37
34	4.66	44	3.20	54	2.28	64	1.53	74	0.90	84	0.33
35	4.50	45	3.14	55	2.20	65	1.46	75	0.84	85	0.27
36	4.33	46	3.09	56	2.12	66	1.40	76	0.78	86	0.22
37	4.17	47	2.93	57	2.04	67	1.33	77	0.72	87	0.16
38	4.02	48	2.83	58	1.96	68	1.27	78	0.67	88	0.11
39	3.88	49	2.73	59	1.89	69	1.20	79	0.61	89	0.06

470 Simple Elements with Old and New Equivalents (Chemistry),

NAME OF ELEMENTS.	Sym-	Old	New	Sp. gr.	REMARKS ON THE ELEMENTS.
	bol.	eqvlt.	eqvlt.		
Aluminium	Al.	13.7	27.5	2.50	Light metal. Like zinc.
Antimony	Sb.	129.0	122.	6.70	White metal used in types.
Arsenicum	As.	75.	75.	5.80	Metal, steel-gray lustre.
Barium	Ba.	68.5	137.2	4.70	White metal, fuses at red heat.
Bismuth	Bi.	210.30		9.80	Hard brittle reddish metal.
Boron	Bo.	10.9	11.	2.00	Combination with potassium.
Bromine	Br.	80.	80.	3.187	Deep red volatile liquid.
Cadmium	Cd.	56.	111.6	8.60	Very soft and ductile metal.
	Cs.	132.4	132.15		Two strong blue lines in spectr.
Cæsium				1 57	Tight well as his most all as his most all
Calcium	Ca.	20.	39.9	1.57	Light yellow malleable metal.
Carbon	C.	6.	12.	3.52	Diamond. Graphite. Coal.
Cerium	Ce.	46.	141.3	5.5	Little known and less used.
Chlorine	Cl.	35.5	35.5	2.44	Gas, greenish-yellow color.
Chromium	Cr.	26.3	52.4	6.8	Dark-gray metal, strong affinity
Cobalt	Co.	29.5	58.6	8.9	Reddish-gray, magnetic metal.
Copper	Cu.	31.7	63.3	8.9	Yellowish-red ductile metal.
Didymium	D.	48.	147?		Little known and less used.
Erbium	E.		170.6		Classed as a metal.
Fluorine	F.	19.	19.1	1.31	Found in fluor spar.
Gallium	G.		69.9		Silver-white metal.
Glusium.	Ğİ.	4.7	9.25		Its salt has a sweet taste.
Gold (Aurum)	Au.	196.44		19.34	Standard of value.
	H.				Lightest of gases.
Hydrogen		1.	1.	7 9	Dowly blue lines in anacture
Indium	In.	74.	113.4	7.2	Dark-blue lines in spectrum.
Iodine	I.	127.	127.	4.94	Metallic bluish solid.
Iridium	Ir.	98.6	169.7	18.68	Hard white metal.
Iron (Ferrum)	Fe.	28.	55.9	7.8	The most useful metal.
Lanthanum		46.	92.	*****	Little known and less used.
Lead (Plumbum)	Pb.	103.6	206.4	11.44	Soft and malleable metal.
Lithium	L.	7.	7.022	0.593	White metal, burns brilliantly.
Magnesium	Mg.	12.16	24.	1.7	Burns brilliantly.
Manganese		27.40	54.8	8.	Grayish-white metal.
Mercury		100.	200.	13.59	White liquid metal.
Molybdenum		48.	95.8	8.6	White brittle metal.
Nickel		29.5	58.6	8.8	White, hard, ductile metal.
Niobium		48.8	94.		Not generally known.
Nitrogen		14.	14.044		Gas without color or taste.
Osmium	Ōs.	99.4	198.6	10.	White and brittle metal.
	_	8.	16.		Gas, supports life and combus'n.
Oxygen		53.2		11.5	Hard ductile white metal.
Palladium	ru.		106.2		Translucent solid socile imited
Phosphorus	P	31.	31.	1.83	Translucent solid easily ignited.
Platinum		98.6	196.7	21.5	Heaviest of all metals.
Potassium	K.	39.	39.137		Brittle metal, melts at 130°.
Rhodium	Ro.	52.2	104.2	11.	White, hard metal.
Rubidium	Rb.	85.36		1.52	Metal little known.
Ruthenium			103.5	8.6	Most infusible of metals.
Selenium	Se.	39.7	78.	4.8	A semi-metallic solid.
Silicon	Si.	14.	28.	2.49	Flint, quartz, glass, and clay.
Silver (Argentum)	Ag.	108.	108.	10.5	Metal of standard value.
Sodium (Natron)	Na.	23.	23.043	0.972	Bluish-white and soft metal.
Strontium		43.8	87.2	2.54	White metal like barium.
Sulphur		16.	32.	2.	Brimstone, widely used.
Tantalum		68.8	182.	10.7	Little used.
Tellurium	Te.	64.5	128.	6.6	Lustre of metal like sulphur.
Thallium	Tl.	204.	203.6	11.8	Green line in spectrum.
Thorium	Th.	59.5	_		
			233.9	7.7	Not used in the arts.
Tin (Stannum)	Sn.	59.	117.8	7.3	White and malleable metal.
Titanium		25.	48.	5.28	Its oxide used for painting.
Tungsten (Wolfram).	W.	92.	184.	17.	An iron-gray metal.
Uranium		60.	120.	10.15	A steel-white metal.
Vanadium	V.	68.5	51.2	5.5	A metal little used.
Yttrium	Y.	32.2	89.6		Found in Sweden in 1843.
Zinc	Zn.	32.6	64.9	7.	A bluish-white metal.
Zirconium	Zr.	44.8	90.	4.15	In nature as silicate.

Solids and Salts.	FORMULAS.	COMMERCIAL NAMES AND USE.
Aluminium sulphate	A1.(SO.).	
Aluminium sulphate Ammonium chloride	$Al_2(SO_4)_3$. NH_4Cl .	For preparing salts of aluminium. Sal ammoniac, for soldering.
Arsenious acid		
Barium oxide		White arsenic, poisonous.
		Baryta, a gray powder.
Barium sulphate		Heavy Spar. Fr. adult. wt. lead.
Calcium oxide		Quick or caustic lime.
Camphor	$C_{10}H_{16}O.$	Used for making celluloid.
Carbolic acid	C_6H_6O .	Used as a disinfectant.
Carbonate of lime	CaO,CO ₂ .	Common limestone, marble.
Chloride of lime	$CaCl_{\mathfrak{g}}O_{\mathfrak{g}}.$	Bleaching powder.
Chloride of sodium	ClNa.	Common salt,
Copper sulphate	CuSO ₄ .	Blue stone or vitriol.
Copper pyrites	Cu ₂ S.Fe ₂ S ₂ .	Pyramidal and tetrahedral crys-
Cuprous oxide	Cu ₂ O.	Red oxide of copper, [tals.]
Gold manager	AuCl ₃ .	Used in photography.
Gold mercury	Au ₂ Hg.	Gold amalgam.
Gun-cotton	$C_6H_7(\overline{NO}_2)_3O_5.$	Used as an explosive.
Hydrogen sodium carb'te.	HNaCO ₃ .	Baking powder, artificial yeast.
Hydrogen potass, carb'te.	HKCO ₃ .	Yeast for raising bread.
Iron, ferric oxide	$\operatorname{Fe}_{2}O_{3}$.	Red hematite, iron ore.
Iron, ferric hydrate	$\text{Fe}_{2}\text{H}_{6}\text{O}_{6}.$	Yellow ochre, iron orc.
Iron, magnetic oxide	Fe ₃ O ₄ .	Loadstone, iron ore.
Iron, bisulphate	FeS ₂ .	Pyrites, cube crystals.
Iron, ferric sulphate	$FeSO_4 + 7H_2O$.	Green vitriol, copperas.
Indigo blue	$C_8H_5NO.$	Used in dyeing.
Lead chromate	PbO,CrO ₃ .	Chrome-yellow.
Lead protoxide	PbO.	Litharge, dryer for oils.
Lead chloride and oxide	(PbCl ₂ ,7PbO).	Pigment, Turner's yellow.
Lead carbonate	Pbo,co ₂ .	White lead, paint.
Lead sequi-oxide	Pb_3O_4 .	Minium, rcd lead.
Lead sulphate	PbS.	Galena, lead ore.
Lapis lazuli	2AlPO ₄ .MgH ₂ O ₂ .	Blue precious stone.
Malachite	$CuCO_3$. CuH_2O_2 .	Green precious stone.
Manganese binoxide	MnO ₂ .	For making chlorine and oxygen.
Mercury chloride	HgCl_{2} .	Corrosive sublimate.
Mercury sulphide	HgS.	Cinnabar, ore of mercury.
Oxalic acid	$C_2H_2O_4$.	A powerful poison.
Paraffin	$C_{27}H_{54}$.	For making candles.
Potassium carbonate		Used for making glass.
Potassium chlorate	KClO ₃ .	For making oxygen in medicine.
Potassium chromate		Used for bleaching. Calico print-
Potassium cyanide	KCN.	Used in photography. [ing.]
Potassium liydrogen	HKCO ₃ .	Cream of tartar.
Potassium nitrate	KNO ₃ .	Saltpetre, prismatic crystals.
Saccharose	$C_{12}H_{22}O_{11}$.	Cane-sugar, gum-arabic.
Silver chloride	AgCl.	Horn-silver, in photography.
Silver nitrate	AgNO ₃ .	Lunar caustic.
Silver cyanide	AgCN.	Used in electro-plating.
Sodium biborate	Na ₂ B ₄ O ₇ .10H ₂ O.	Borax, used as a flux.
Sodium nitrate	NaNO ₃ .	Soda saltpetre, cubic crystals.
Sodium carbonate	Na ₂ CO ₃ .	Soda, used for making soap.
Sodium oxide	NaO.	Soda, oxide of natrium.
Stannous chloride	SnCl ₂ .	Tin-salt, used in dycing.
Stannic oxide	SnO_2 .	Tin-stone, cassiterite.
Starch	$C_6H_{10}O_5$.	Used in washing.
Stearic acid	$C_{18}H_{36}O_{2}$.	Solid fat, candles.
Strychnine	$C_{20}H_{24}N_{2}O_{2}$.	Strong poison.
Sulphate of soda	NaU,SU3+10H20.	
Sulphate of lime		Alabaster, gypsum, plaster Paris.
Tannic acid		For tanning leather.
Zinc chloride	ZnCl_2 .	For preserving timber.
Zinc sulphate	ZnSO ₄ .	White vitriol, used in medicine.
Equal proportions of d	ifferent atoms may	y be formed into different orders
and make different subst	ances, as cane-suc	ar and gum-arabic; also, strych-
nine and quinine, which	have the same for	rmula.
mine and quinine, which	marc one same to	A AA - C-3CC3

Liquids.	FORMULAS.	COMMERCIAL NAMES OR USE.
Water	H ₂ O.	The most abundant liquid.
WaterAlcohol. Ethyl	$C_2 \tilde{H}_6 O$.	Spirit of wine, intoxicating.
Methyl alcohol	CH_4O .	Proof spirit.
Ether	$(C_2H_5)_2O.$	Used as a solvent, anæsthetie.
Chloroform	$CHCl_3$.	Used as an anæsthetic.
Clyporino		Much used in the arts.
Glycerine	$(C_3H_5)H_3O_3$.	
Nitro-glyeerine	$C_3H_5N_3O_9$.	The most powerful explosive.
Oil of turpentine	$C_{10}H_{16}$.	Spirit of turpentine.
Benzol	C_6H_6 .	Constituent of eoal-tar.
Nitro-benzol	$C_6H_5(NO_2)$.	Forms the main portion of ani-
Aniline	C_6H_7N .	For aniline colors. [line.]
Carbon bisulphide	CS_2 .	A solvent for India-rubber
Nitrie acid	$\mathrm{HN} \circlearrowleft_3$.	Aqua-fortis, oxidizing agent.
Sulphuric acid	$\mathrm{H}_{2}\mathrm{SO}_{4}.$	Oil of vitriol, much used.
Hydroehloric acid	$\mathbf{HCl}.^{-}$	Muriatic acid.
Nitro-muriatie acid	$HNO_3 + 2HCl.$	Aqua-regia, dissolves gold.
Citric acid	$C_6H_8O_7$.	Juice of lemons.
Oxalie acid	$C_2H_2O_42H_2O_4$	A powerful poison.
Quinie acid	$C_7H_{12}O_6$.	From Peruvian bark.
Quinine	$C_{20}H_{24}N_2O_2$.	For ehills and fever.
Gases.	20 27 2 2	
Atmospheric air	$N_{4}O.$	Not chemically combined.
Nitrous oxide	N_2^{40} .	Laughing-gas.
Nitrie oxide	N_2 0.	Extinguishes fire.
Carbonie aeid		. 91.
Carbonie oxide	CO_2 .	Perfectly consumes coal.
	CO.	Suffocating, poisonous.
Carburetted hydrogen	$_{\mathrm{C}}^{\mathrm{CH}_{4}}$.	Marsh-gas, fire-damp.
Olefiant gas	C_2H_4 .	Illuminating gas.
Cyanogen	NC.	Produces blue color.
Ammonia	NH ₃ .	Hartshorn, volatile alkali.
Cyanhydric acid	HCN.	Prussie acid, poisonous.
Hydrogen sulphide	$_{\rm S2}^{\rm H_2S.}$	Used as a reagent in laboratory.
Sulphurous anhydride	· SO ₂ .	Used for bleaching straw.

Proportion of Compounds by Weight or Volume.

Names.	Carbon. C.	Hydrogen. H.	Oxygen. O.	Nitrogen.
Olive oil, by weight	772 780 740	133 118 103	95 102 157	
Linseed oil, "	760 527 432	113 129 68	127 344 500	
Atmosp. air		1	230 210 8	770 790
" " volume India-rubber by weight	853	147	1	-

To Transform Atomic Formulas into Weights.

Rule. Multiply together the equivalent (equiv.) and the exponent (exp.) of each substance, and the product is the proportion in the compound by weight. Divide each weight by its specific gravity, gives the proportions by bulk or volume.

Example 1. The chemical formula for common alcohol is C₂H₆O. Required its proportioned parts by weight in 1000?

Carbon C₂ = $12 \times 2 = 24$ Hydrogen H₆ = $1 \times 6 = 6$ Oxygen O = $16 \times 1 = 16$ $\times 1000 : 46 = 21.74$ $\times 1000.04$ $\times 1000.04$ by weight.

NITRO-GLYCERINE, C₃H₅N₃O₉.

Nitro-glycerine is an oily liquid of the above composition, which is highly explosive under peculiar circumstances, but can be set fire to and burned like alcohol without explosion. It explodes by concussion or pressure of about 2000 pounds to the square inch, or by the corresponding temperature of about 630° Fahr, suddenly applied.

The explosion of nitro-glycerine is **instantaneous**, like that of electricity passing between two points, decomposes a small portion of the air and explodes the nitrogen by concussion, which makes the electric spark. Thunder and lightning are explosions of a kind of nitro-glycerine formed by electricity in the air.

Small portions of nitro-glycerine, say half an ounce each, placed (any number) within a few feet of one another, if one of them is exploded, all the rest will explode simul-instantaneously. Therefore, when a charge is to be exploded, care must be taken that no more of it is in the neighborhood.

It may appear strange that nitro-glycerine can be so dangerous to handle, when it requires the enormous pressure of 2000 pounds to the square inch to explode it; but the fluid may be squeezed between surfaces of only one 10,000th part of one

square inch, when the pressure need be only 3 ounces to explode it.

The charge of nitro-glycerine in blasting is exploded by a percussion cap placed on the end of a fuse and dipped into the liquid. The fuse explodes the fulminant in the cap, the concussion of which explodes the charge. On account of the action of nitro-glycerine being instantaneous, no tamping is required in the blast-hole, except water or loose sand, but even that is not necessary. This explosive is therefore entirely unfit for use in firearms, which would be blown to pieces without discharge through the muzzle.

The many and very serious accidents which have happened by unexpected explosions of nitro-glycerine have caused it to be forbidden transportation on railroads and steamboats, for which a new form of the explosive has been invented, which consists in mixing sawdust and some other solid substances with nitro-glycerine, to the form of a moist brown powder, of nearly the same specific gravity

as that of water.

Dynamite.

This powder is called dynamite, and is now manufactured by the nitro-glycerine inventor, Alfred Nobel, in Hamburg, and also by the Giant Powder Company, in

San Francisco, California.

The strength and instantaneous action of dynamite are precisely the same as those of nitro-glycerine, but it is much safer to handle, it is said—more so than common gunpowder. The dynamite powder is made up into cartridges of different sizes to snit the blast-hole, and is exploded by percussion caps like nitro-glycerine, and requires no tamping. It has been employed with great success in blasting immense masses of rock in the Andes, Peru.

The price of dynamite is higher than that of gunpowder per weight, but its execution per price is much greater. The blast-holes for dynamite need be only one-

half the size of those for gunpowder, with equal execution.

The instantaneous action of dynamite makes it far superior to gunpowder in

blasting, but it is unfit for use in firearms.

Any number of cartridges of dynamite placed in a deep blast-hole with tampings of sand between, if one of them is exploded, all the rest will explode simultaneously. Small cartridges are made for the percussion cap, and called primers, by which the principal charge is exploded. Should a charge fail to explode, put in a new fuse and primer.

Blasting under Water.

For this purpose the cartridges should be made of strong oiled paper and perfectly water-tight, to save the dynamite from moisture. The cartridges should also be ballasted, so as to sink easy in water, which can be done by placing a lead ball in the bottom and pack the dynamite on the top, after which the cartridge is hermetically sealed with some varnish insoluble in water. The cartridges (any number) are guided into the blast-hole through a tube, and finally the primer with the fuse, by which the whole charge is exploded.

Dynamite is insoluble in water, but will not explode if moist with water. It freezes to a snowy mass at 40° Fahr., but its explosive quality is not impaired

thereby. At 212° the nitrogen evaporates and spoils the powder.

CEMENT, CONCRETE AND MORTAR.

Roman Cement. Parker's analysis.

One part of common clay to $2\frac{1}{2}$ parts of chalk, set very quick.

Concrete. Eight parts of pebble or pieces of brick about the size of an egg, to 4 parts of scrap river-sand, and 1 part of good lime, mixed with water and grouted in, makes a good concrete.

Lime Mortar. One part of river-sand to two parts of powdered lime, mixed

with fresh water.

Hydraulic Mortar. One part of pounded brick powder to two parts of powdered lime mixed with fresh water. This mortar must be laid very thick between the bricks, and the latter well soaked in water before laid.

No. 1. Hydraulic Concrete, by Treussart.

30 parts of hydraulic lime, measured in bulk before slacked.

30 66 20 gravel.

40 66 broken stone, a hard limestonc.

This concrete diminishes one-fifth in volume after manipulation. The mortar is made first, and then mixed with gravel and stone.

No. 2. Another Concrete, by Treussart.

33 volumes hydranlic lime unslacked. 45 Puzzolano (Pozzulano).

22 sand.

60 broken stone and gravel.

Asphalte Composition for street pavement, by Colonel Emy. $2\frac{1}{2}$ pints (wine measure) of pure mineral pitch.

11 lbs. of Gaugeac bitumen.

17 pints of powdered stone-dust, wood-ashes or minion.

Cements for Cast Iron.

No. 1 should be put in place immediately after mixed, whilst No. 2 ought to rest 12 hours.

Two ounces sal-ammoniac, one ounce sulphur and sixteen ounces of borings or filings of cast iron, to be mixed well in a mortar and kept dry. When required for use, take one part of this powder to twenty parts of clear iron borings or filings, mixed thoroughly in a mortar, make the mixture into a stiff paste with a little water and then it is ready for use. A little fine grindstone sand improves the cement.

Or, one ounce of sal-ammoniac to one hundred weight of iron borings. No heat

allowed to it.

The cubic contents of the joint in inches, divided by 5, is the weight of dry borings in pounds Avoir, required to make cement to fill the joint nearly.

Cement for Stone and Brick Work.

Two parts ashes, three of clay and one of sand, mixed with oil, will resist weather equal to marble.

Brown Mortar.

One part Thomaston lime, two of sand and a small quantity of hair.

Hydraulic Mortar.

Three parts of lime, four Puzzolano, one smithy aslies, two of sand and four parts of rolled stone or shingle.

Crushing Weight in Pounds per Square Inch

on Portland cement, mixed with different proportions of sand, and at different age of the mixture in months.

Age in		P	arts of san	d to one of	cement.		
mouths.	0	11	2	3	4	5	6
3	3800	2490	1900	1500	1200	950	780
6	5280	3550	2750	2190	1800	1500	1200
9	5980	4450	3350	2700	2280	1800	1440
12	6160	5150	3850	3010	2450	2050	1600

About 1/3 of this weight should be depended upon in practice.

Some iron filings in a very weak solution of sal-ammoniac, mixed with Portland cement, increases its strength to double or more.

BRICKS.

Dimensions.

Common brick, $8 \times 4\frac{1}{9} \times 2\frac{1}{9}$ inches = 85 cubic inches. Front brick, $8\frac{1}{4} \times 4\frac{1}{2} \times 2\frac{1}{2}$ " = 92.8 "

When laid in a wall with cement, it occupies a space of— Common brick, $8\frac{1}{4} \times 4\frac{1}{2} \times 2\frac{3}{4}$ inches = 102 cubic inches. Front brick, $8\frac{1}{2} \times 4\frac{3}{4} \times 2\frac{3}{4}$ " = 111 " " Front brick,

Weight and Bulk of Bricks.

			Number of bricks.						
			by it	self.	in wall with cement.				
Tons.	Pounds.	Cub. ft.	C. brick.	F. brick.	C. brick.	F. brick.			
1	2240	22.4	448	416.6	381	347			
0.04464	100	1	20	18.6	17	$15\frac{1}{2}$			
2.23	5000	50.00	1000	930	850	772			
2.4	5376	53.76	1075	1000	914	834			
2.62 .	5872	58.72	1130	1100	1000	913			
2.88	6451	64.51	1240	1200	1100	1000			

One perch of stone is 24.75 cubic feet.

Acids for Soldering or Tinning.

TIN. One part of muriatic acid, with as much zinc as it will dissolve, then add two parts of water and some sal-ammoniac.

BRASS and COPPER. One pound of muriatic acid, four ounces of zinc and

five ounces of sal-ammoniac.

ZINC. One pound of muriatic acid, two onness of sal-ammoniac with all the zinc it will dissolve, then add three pints of water.

IRON. One pound of muriatic acid, six ounces sperm tallow and four ounces of

sal-ammoniac.

GOLD and SILVER. One pound muriatic acid, eight ounces sperm tallow and eight ounces of sal-ammoniac.

Silvering Metals.

Ten parts of nitrate of silver, ten parts common salt, thirty parts cream of tartar. Moisten the powder with water when ready to apply.

Glues.

Rice glue. Rice flour mixed in cold water and boiled in china or clay pot; stir it well during the boiling. This makes an excellent white glue.

Houseblose glue. Dissolve the houseblose in strong alcohol, and apply it hot on the articles to be glued. This makes a very strong glue which is not soluble in water or moisture.

Barrel Measure.

A barrel of flour weighs 196 pounds.

A barrel of pork, 200 pounds.

A barrel of rice, 600 pounds.

A barrel of powder, 25 pounds.

A firkin of butter, 56 pounds.

A tub of butter, 84 pounds.

14 pounds, . 1 stone.

28 pounds, . 1 quarter.

1 cwt. 4 quarters, .

Bushel Measure.

The following are sold by weight per bushel:

Wheat, beans and clover-seed, 60 pounds to the bushel.

Corn, rye and flax-seed, 56 pounds.

Buckwheat, 52 pounds.

Barley, 48 pounds. Oats, 35 pounds.

Bran, 20 pounds.

Timothy-seed, 45 pounds.

Coarse salt, 85 pounds.

Acre.

A square of 208.75 feet each way is one acre. A circle of 235.5 feet in diameter is one acre.

LIGHT AND COLORS.

Light is the sensation transmitted to the eye, and produces the sense of seeing. Light is a component part of heat, and a compound imponderable substance whose ingredients depend upon the composition of the burning substance; or, burning substances can be analyzed by decomposition of its light in a spectrum.

Decomposition of Light in the Spectrum.

Colors.	Maximum ray.	Combination of Colors.				
Violet.	Chemical.	Primary.	Secondary.	Tertiary.		
Indigo. Blue.	Electrical.	Blue. Yellow.	Green.	Dark		
Green. Yellow.	Light.	Blue. Red.	Purple.	Green.		
Orange. Red.	Heat,	Yellow, Red.	Orange.	Brown.		

All the colors of the spectrum mixed together make white, which is proved by the decomposition of white light, which makes the seven colors.

The velocity of light in planetary space is 192500 miles per second. The velocity of light through transparent bodies is not known, but probably varies inverse as the square root of the specific gravity of the transparent substance.

Light passes from the sun to the earth, 95000000 miles, in eight minutes, at which rate of velocity light can pass around the earth in one-eighth of a second.

The intensity of light is inverse as the square of the distance from the luminous body.

The standard unit for measuring the intensity of light is assumed to be that produced by a sperm candle, "short 6," burning 120 grains per hour.

A spermatic candle 0.85 in diameter burns about 1 inch per hour.

MOTION OF GAS IN PIPES.

Letters denote,

Q = cubic feet of gas passed through the gas-pipe per hour.

L = length in feet, D = diameter in inches, of the pipe. H = head of water in inches which presses the gas through the pipe.

s = specific gravity of the gas, air being 1.

n = number of candles required for giving the same light as Q cubic feet of gas

$$Q = 780D^2 \sqrt{\frac{HD}{SL}}, \qquad Q = \sqrt{n} \\ n = Q^2 \qquad D = \frac{1}{14.35} \sqrt[5]{\frac{SL Q^2}{H}}.$$

Example. At a distance of L=6450 feet from the gas-work is required Q=940 cubic feet of gas per hour. Head of water being H=1 inch, specific gravity s=0.5. Required, the diameter of the pipe D=?

$$D = \frac{1}{14.35} \sqrt[5]{\frac{0.5 \times 6450 \times 940^2}{1}} = 5.396 \text{ inches.}$$

Each light in a room consumes about 4 cubic feet of gas per hour, and ordinary street-lights 5 cubic feet.

ELECTRICITY.

Electro-Chemical Order of

and

arranged in their order of positive The substance is positive to either

chemical formulas the electro-positive substance is placed first, and the negative last

The substances are

Oxygen, being the substance most electro-negative, combines with the most electro-positive substance in the couple, and the force liberated by the oxidation, or that which kept the oxidated

The exciting fluid to

be diluted sulphuric acid. Other fluids cause some difference in

No electricity can

solid, forms the electricity.

substance

negative electricity. The substance is below it, and negative to any one above.

the order, depending upon the different chemical affinity between

the fluid and the substances in the

galvanic couple.

Simple Substances.

ELECTRO-POSITIVE. Potassium. Sodium.

Lithium. Barium.

Strontium. Calcium.

Magnesium. Aluminium.

Uranium. Manganese.

Zinc.

Iron. Nickel.

Cobalt.

Cadmium.

Lead. Tin.

Bismuth.

Copper. Silver.

Mercury.

Palladium.

Platinum.

Gold.

Hydrogen. Silicon.

Titanium.

Tellurium.

Antimony.

Carbon.

Borou.

Tungsten.

Molybdenum.

Vanadium.

Chromium.

Arsenicum. Phosphorus.

Iodine.

Bromine.

Chlorine.

Fluorine.

Nitrogen.

Seleninm.

Sulphur.

Oxygen.

ELECTRO-NEGATIV ..

Order of Compounds. ELECTRO-POSITIVE.

Smooth glass.

Woollen cloth.

Featners.

Wood.

Paper.

Silk.

Rough glass.

anlphur.

Cofton.

ELECTRO-NEGATIVE.

Order of Conducting Power

for Electricity. Metals, best conductors.

Well-burnt charcoal.

Plumbago.

Concentrated acids. Powdered charcoal.

Diluted acids.

Saline solutions.

Metallic ores.

Animal fluids.

Sea water.

Spring water.

Rain water. Ice above 13° Fahr.

Snow.

Living vegetables.

Living animals.

Steam.

Salts soluble in water. Rarefied air.

Vapor of alcohol.

Moist earth and stones. Powdered glass.

Flower of sulphur.

Dry metallic oxides.

Oils, the heaviest the

Ashes.

·Transparent crystals. Ice below 13° Fahr.

Phosphorus.

Lime.

Dry chalk.

Caoutchouc.

Camphor.

Silicious stones.

Drv marble.

Porcelain.

Baked wood.

Dry gases and air. Leather.

Parchment.

Dry paper.

Feathers.

Hair.

Wool.

Dyed silk.

Bleached silk.

Raw silk.

Diamond.

Mica.

All vitrifications. Glass.

Jet.

Wax. Sulphur.

Resins.

Amber.

Shellac.

Gutta-percha, the worst

conductor of all.

page 386.) The poor conductors for electricity are called insulators, and employed between good conductors to stop the flow The substances are set up in their order of conducting power r electricity. The conducting power of substances for heat appears to be in the same proportion as that for electricity. for electricity. or passage

that of light through planetary space—about 200,000 miles per. When the conductor is insulated with a solid nonconducting substance, like gutta-percha, and immersed in water as a submarine cable, the velocity may be reduced to only 20,000 Velocity of electricity through the best conductors is equal

miles ler second, or less. second.

FIRE-ASSAY OF SILVER AND GOLD ORES.

From actual practice by the author in California and South America.

Assay Composition.

Gold or silver ores,	400	grains.
Litharge (oxide of lead),	500	"
Carbonate of soda,	240	66
Borax,	110	46
Charcoal,	20	66
Total.	1270	66

All the ingredients to be well powdered and mixed before placed in the crucible. Should the ore contain much sulphur, stick a 3-inch nail in the assay. The more galena in the ore, the less litharge is required. Smelt the assay, cupel the lead and weigh the remaining button of precious metal.

Should the button be pure silver, multiply the weight in grains by 100, and the product is the value of silver in dollars per ton of ore; if pure gold, multiply by

1500, and the product is the value in dollars per ton of ore.

When the button contains both gold and silver, the latter metal must be dissolved in nitric acid, for which the alloy must contain at least 3 silver to 1 of gold, otherwise the acid will not dissolve it. In case the alloyed button does not contain sufficient silver, it is necessary to add what is required, and melt it into one button by blowpipe and charcoal. Hammer the button to a thin leaf and boil it in nitric acid; when all the silver is dissolved, the pure gold remains solid. Wash the gold in clean water, dry and weigh it.

the gold in clean water, dry and weigh it.

Suppose the alloyed button to weigh 2.156 grains, and its color being between that of gold and silver, so as to suspect too little of the latter metal; then add, say, 2 grains of pure silver, and dissolve the button, weigh the remaining gold, which, for example, may be 1.162 grains. Then 2.156—1.162=1.994 grains of

silver in the assay.

Silver,
$$1.994 + 100 = 199.40$$
 dollars per ton.
Gold, $1.162 + 1500 = 1743$ "

Value of the ore, $= 1942.40$ "

About one per cent. of the precious metal is lost in the cupelling. This rule is sufficiently correct for practical purposes.

North American Standard.

Pure { Gold, 387 ounces, 8000 dollars. Silver, 99 ounces, 128 dollars.

Peruvian Standard.

Pure ${
m Gold, 1 \ ounce, 24.29 \ pesos = 19.43 \ soles.}$ One peso = 4 francs; one sole = 5 francs.

Assay Table I.—North and South American Measures.

The table will answer for any system of assaying weights.

Percentage of metal in the ore.	Value of Metal per ton of Ore. Gold. Silver.		Value of Me tal of Gold.	Silver per cajon.	
Per ct.	Dollars.	Dollars.	Soles.	Soles.	Marcs.
0.1	602.924	39.709	31,090	2.053	12
0.2	1205.85	79.418	62.179	4.106	24
0.3	1808.77	119.127	93.269	6.158	36
0.4	2411.69	158.836	124.359	8.211	48
0.5	3014.62	198.545	155.448	10.264	60
0.6	3617.54	238.254	186.538	12.317	72
0.7	4220.45	277.963	217.627	14.370	84
0.8	4823.39	317.672	248.717	16.422	96
0.9	5426.31	357.381	279 807	18.473	108
i per cent.	6029.24	397.090	310.896	20.528	120
1	North Ame	erican.	ll So	uth American	1.

Suppose the assay to be 112 grammes, and the cupelled button weighs 0.657 of a gramme of silver, then $0.657 \times 100:112 = 0.586$ per cent.

See Table
$$\begin{cases} 0.5 &= 10.264 \\ 0.08 &= 1.642 \\ 0.006 &= 0.012 \\ \hline 0.586 &= 11.918 \end{cases}$$
 Soles per quintal.
$$\begin{cases} 0.5 &= 198.545 \\ 0.08 &= 31.767 \\ 0.006 &= 2.382 \\ \hline 0.586 &= 232.694 \end{cases}$$
 Dollars per ton of ore.

Table II. For Gold and Silver.

	Wei		lue		Bu	ılk.				
Avoir	dupois.	Troy.		in do	llars.	Go	ld.	Silv	Silver.	
Tons.	Pounds.	Ounces.	Grains.	Gold.	Silver.	Cub. ft.	Cub. in.	Cub. ft.	Cub. in.	
1.	2000	29166.6	14 millions.	602924	39709	1.6643	2875.91	3.060	5287.48	
0.0005	1	14.5833	7000	301.46	18.854		1.43795		2.64284	
	0.06857	1	480	20.6718	1.2929		0.09859		0.18129	
	0.0002	0.00283	1	0.04306	0.00269		0.00020		0.00038	
	0.00332	0.04837	23.2202	1	1.000		0.0524			
	0.05304	0.77346	371.264	1.0000	1			:	0.1401	
0.60085	1201.7	17524.8	8411900	362267		1	1728	1.0000	1728	
	0.69543	10.1416	4867.99	209.645		0.00058	1	0.00058		
0.32679	653.577	9531.34	4 575043		12976.4		1728	1	1728	
	0.378227	5.51581	2647.59			0.00058		0.00058		

Table III. Gold, Silver and Platinum.

Weight in grains per square inch of sheet, thickness by Birmingham gauge for those metals, and in inches.

		1	1						
Bir. G.	Thick.	Gold.	Silver.	Platin.	Bir. G.	Thick.	Gold.	Silver.	Platin.
No.	inches.	grains.	grains.	grains.	No.	inches.	grains.	grains.	grains.
1	0.004	20.68	11.52	25.50	19	0.063	339.5	184.7	397.5
2	0.005	26.93	14.40	31.26	20	0.069	371.8	201.9	435.0
3	0.006	32.19	17.28	38.00	21	0.075	404.0	220.0	471.8
4	0.008	42.80	23.52	50.43	22	0.081	436.1	237.2	509.2
5	0.010	53.85	2 9.28	58.14	23	0.087	468.8	255.0	548.6
6	0.012	64.46	35.04	75.45	24	0.093	500.0	272.6	586.0
7	0.014	75.42	40.80	87.88	25	0.099	533,3	290.0	625.0
8	0.016	86.58	46.56	100.1	26	0.105	566,6	307.8	663.0
9	0.018	97.07	52.00	113.2	27	0.111	596.1	325.5	697.3
10	0.022	118.9	64.32	138.5	28	0.117	630.0	342.6	735.6
11	0.025	134.6	72.96	157.7	29	0.124	673.3	363 5	783.1
12	0.029	156.3	84.96	182.3	30	0.130	701.5	380.3	817.0
13	0.033	178.2	96.48	207.4	31	0.136	730.0	398.4	855.0
14	0.038	204.6	111.3	239.5	32	0.142	769.5	416.3	892.0
15	0.043	231.5	125.8	270.5	33	0.148	798.5	433.3	932.0
16	0.048	258.8	140.8	302.6	34	0.152	837.6	451.6	970.0
17	0.053	285.6	155.3	323.8	35	0.160	865.7	470.5	1007
18	0.058	312.6	170.0	365.3	36	0.166	894.0	486.0	1047

California Rule for Silver and Gold.

It is an established custom in California to allow one per cent, for base metal in all gold and silver bars from the mines. The fineness is always stamped in parts of 1000; that is, if a gold bar is stamped 900 fine, it is understood to contain—

900 parts of pure gold, 90 parts of pure silver, 10 parts of base metal,

in 1000 parts of the bar.

To Find the Value of Gold and Silver Bars.

Example 1. Required, the value of the pure gold in a bar weighing 989 ounces and stamped 797 fine?

From table
$${790 \text{ fine} = 16.33.07 } {7 \text{ fine} = .14.47}$$
 dollars.

Required value of the bar, $989 \times 16.47.54 = 16294.17$ dollars.

Example 2. A gold bar weighing 366 ounces has been assayed and stamped to 860 fine. Required, its total value?

Metals. Bul. Fine. Ounces. per Ounce. Value. Gold,
$$366 \times 860 = 314.76 \times 20.67.18 = \$6506.65.57$$
. Silver, $366 \times 130 = 47.58 \times 1.27.29 = 61.51.61$. Base metal, $366 \times 10 = 3.66$ no value.

Total amount $1000 = 366$ Answer, $\$6568.17.18$.

The last two figures in the columns of Table IV. are decimals of a cent. The fineness of gold is also expressed in *carats*, 24 for pure gold; that is, a piece of gold 18 carats fine is $18 \times 1000: 24 = 750$ fine.

Table IV.—Value of Gold and Silver, per ounce Troy, of Different Fineness.

To Refine Silver.

Dissolve the impure silver in nitric acid, add chloride of sodium (salt) sufficient to precipitate all the silver in form of chloride; then all the impurities will remain in solution.

Filter, wash and dry the chloride of silver. Fuse in a crucible two weights of carbonate of potash, add gradually one weight of chloride of silver, raise the heat, and the pure silver will melt and collect on the bottom.

Tests for Metals in Solution with Acids.

The reagents are placed in the liquid, which precipitates the metal in solution.

Zito rougous are present	,	
REAGENTS.	PRECIPITATES.	SOLUTIONS.
Sulphate of iron, Oxalic acid, Potash or soda,	Gold, as brown powder, Gold in large flakes, Gold, yellow,	Gold in aqua-regia.
Potash or soda, Plate of copper, Muriatic acid, Common salt, Tincture of nutgall,	Silver, dark olive, Metallic silver, White crudy silver, White crudy silver, Brown silver,	Silver in nitric acid.
Potash or soda, Ferro-prussiate of potash, Carbonate of potash,	Blue cobalt, Green " Red "	Cobalt in nitric acid.
Pure water, Gallic acid, Potash or soda,	White bismuth, Greenish yellow, White bismuth,	Bismuth in nitric acid.
Sulphate of soda, Sulphuric acid, Infusion of nutgall,	White lead,	Lead in nitric acid.
Plate of iron or zinc, Potash, Ammonia, Infusion of nutgall,	Metallic copper, Green copper, Azure-blue copper, Brown copper,	Copper in nitric acid.
Pure water, Plate of iron,	White autimony, Black antimony,	Antimony in 4 muriatic acid, 1 nitric acid.
Plate of copper, " iron, Gallic acid,	Metallic mercury, Dark powder, Orange yellow,	Mercury in muriatic or nitric acid.
Infusion of nutgall, Ferro-prussiate of potash, Ammonia,	Black iron, Blue iron, Dark-red iron,	Iron in muriatic acid.

Acid Test for Strength and Quality of Iron and Steel.

This is a subject well worthy of attention by workers in iron and steel. The sample to be tested is filed smooth, or polished on all sides, and placed in dilute nitric or sulphuric acid for 12 to 24 hours; then wash the sample and dry it. The action of the acid has revealed the structure of the sample, from which its

quality can be decided with great precision.

The best steel presents a frosty appearance; ordinary steel, honeycombed. Iron presents a fibrous structure in the direction in which it has been worked; the best iron shows the finest fibres. Should the iron be uneven, or made from a pile of different kinds of iron, all are exposed by the action of the acid. Hammered blooms show slag and iron; gray cast iron shows crystals of graphic carbon; other cast irons show different figures, all with marked characteristics.

Iron Pyrites, Sulphurets.

There are two kinds of iron pyrites—namely, protosulphuret and bisulphuret, of which the latter is generally richest in gold. All iron pyrites are slightly magnetic, but the gold seems to destroy the magnetism. The protosulphuret acts sensibly on the magnetic needle, whilst the bisulphuret does not, and may therefore be distinguished for gold.

The presence of arseniuret of iron in sulphurets indicates richness in gold.

Roasting of Sulphurets.

When sulphurets contain magnesia, lime or arsenic, sufficient salt should be added to chlorize those substances, which then evaporate and go out through the chimney. The amount of those impurities should be ascertained beforehand. The salt should be well mixed with the ore before put into the furnace. Ten pounds of salt contain six pounds of chlorine and four pounds of sodium.

	Ten pounds	of			Pounds red Chlorine.	quired.
Those impurities are very injurious to chlorination of		•		•	3.58 5.78	6 9.65
	Arsenic,	•		•	10.64	17.6

Chlorination of Gold in Roasted Sulphurets.

Free gold is attacked and dissolved by chlorine gas, and forms two chlorides, namely,

An. 844 parts of gold.
Cl. 156 "chlorine.
Au. Cl. 1000 protochloride of gold.

Au. 648.5 parts of gold. Clz. 351.5 " chlorine. Au. Clz. 1000 terchloride.of gold.

Gold-bearing sulphurets are roasted for the purpose of obtaining the gold free for the action of chlorine gas. The combination is very slow, and requires the gold to be very fine for the prompt formation of chloride. In some ores, the gold is too coarse for chlorination, when it must be extracted by amalgamation.

Composition for Making Chlorine Gas.

For each ton of reasted ore in the vat are required 14 pounds of salt, 10 pounds of peroxide of manganese and 5 quarts of sulphuric acid. The composition should be constantly stirred in the gasometer, and kept to a uniform temperature of about 180° Fahr. The chlorine gas thus formed is led into the vat containing the ore.

On account of chlorine gas being much heavier than air, the gasometer ought to be placed at a considerable height above the vat, to facilitate the chlorination of the gold. In California they place the gasometer below the vat, which is decidedly wrong.

Chloride of gold is soluble in water, and can be washed out from the vat simply by pouring water on the top of the ore and running it into another vessel, where

the gold is precipitated with sulphate of iron.

Chloride of silver is not soluble in water, and remains in the ore in the vat. There is always some silver in gold sulphurets.

Quartz Mills.

Each stamp, weighing about 800 pounds, lifted one foot 60 times per minute, can crush one ton of quartz per 24 hours with a dynamic effect of two horse-power. This is the average performance. The custom-mill in Grass Valley, California, crushes quartz for about four dollars per ton.

The stamps are generally divided into sets of four or five, working in one mortar, and called a battery. The shoes and dies in the battery are made of chilled

cast iron.

Most of the gold is collected by amalgamation in the battery. The pulp from the battery contains much gold, which is often allowed to run away, but generally the sulphuret in the pulp is concentrated and roasted for chlorination; the rest of the pulp is ground in pans and the gold amalgamated.

Amalgams.

GOLD. One weight of mercury amalgamates with two weights of gold. SILVER. 10 silver to 19 mercury.

TIN. 1 tin to 3 mercury, for looking-glasses.

1 tin, 1 lead, 2 bismuth, 10 mercury, for glass-globes.

1 fin. 1 zinc. 3 mercury, for rubbers in electric machines.

OPTICS.

Optics is that branch of philosophy which treats of the property and motion of light.

Mirrors.

Example 1. Fig. 307. Before a concave mirror of r=6 feet radius, is placed an object 0=1, at d=1.75 feet from the vertex. Required the size of the image I=?

image
$$I = \frac{O \ r}{r-2 \ d} = \frac{1 \times 6}{6-2 \times 1.75} = 2.4$$

* Example 2. Fig. 308. Before a concave mirror of r = 5.25 feet radius, is placed an object O = 1, at D = 4.5 feet from the vertex. Required the size of the inverted image I = ?

image
$$I = \frac{O \ r}{2 \ D - r} = \frac{1 \times 5.25}{2 \times 4.5 - 5.25} = 1.4$$

Example 3. Fig. 309. Before a convex mirror of r = 1.8 feet radius, is placed an object 0 = 1, at D = 3.15 feet from the vertex. Required the size of the image I = ?, and the distance in the mirror d = ?

image
$$I = \frac{1 \times 1.8}{2 \times 3.15 + 1.8} = 0.222$$
 distance $d = \frac{3.15 \times 1.8}{2 \times 3.15 + 1.8} = 0.699$ ft.

Example 4. Fig. 310. A parabolic mirror is h = 1.31 feet high, and d = 2.15 feet in diameter. Required the focal distance f = ? from the vertex.

focal distance
$$f = \frac{d^2}{16 h} \cdot \frac{2 \cdot 15^2 \times 12}{16 \times 1 \cdot 31} = 2 \cdot 646$$
 inches.

Optical Lenses.

Example 5. Fig. 316. A double convex lens, of crown glass, having its radii R = r = 6 inches. Required its principal focal distance f = ?For crown glass the index of refraction is m = 1.52. See table.

$$f = \frac{6}{2(1.52-1)} = 5.768$$
 inches

Microscope

Letters aenoie.

n = magnifying power of a lens.

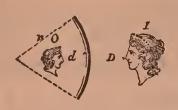
13 = limit of distinct vision.

a = limit of distinct sight, which for long-sighted eyes is about 10 or 12 inches, and near-sighted 6 to 8 inches. For common eyes take
 a = 10 inches.

n = limit distance of the object from the optical centre at distinct vision.

Example 6. Fig. 322. Required the magnifying power of a single microscope with principal focal distance, f=4.3 inches?

Mag. power
$$p = \frac{a + f}{f} = \frac{10 + 4.3}{4.3} = 3.325$$
 times.

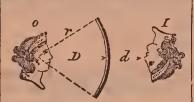


307 Spherical Concave Mirror.

r = radius, and $f = \frac{1}{2}r$, focal distance of the mirror.

$$I = \underbrace{\frac{O \, r}{r - 2 \, d}}_{} \cdot D = \underbrace{\frac{d \, r}{r - 2 \, d}}_{} \cdot$$

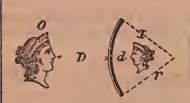
The image disappears when $d = f = \frac{1}{2}r$.



308 Spherical Concave Mirror.

$$I = \underbrace{\frac{O \, r}{2 \, D - r}}, \qquad d = \underbrace{\frac{D \, r}{2 \, D - r}}.$$

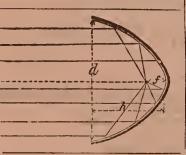
When the object is beyond the focal distance the image will be inverted.



309

Spherical Convex Mirror.

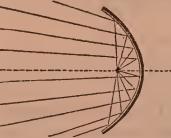
$$I = \frac{O r}{2 D + r} \qquad d = \frac{D r}{2 D + r}$$



310

Parabolic Concave Mirror.

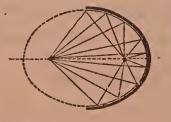
$$f = \frac{d^2}{16 h} \cdot h = \frac{d^2}{16 f} \cdot$$



311

Hyperbolic Concave Mirror.

Heat, Light, or Sound emanating from the foci of a hyperbola will be reflected diverged, from the concave surface.



312

Eliptic Concave Mirror.

Emanating rays from either of the two foci in an elipse, will be refracted by the convex surface to the other foci.

Astronomical Telescopes and Opera Glasses.

Example 7. Fig. 325. The principal focal distance f=0.65 inches of the ocular or eye-lens. F=58 inches the principal focal distance of the objective-lens. Required the magnifying power of the telescope I=?

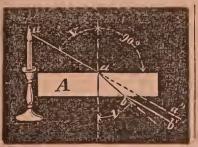
image
$$I = \frac{O F}{f} = \frac{1 \times 58}{0.65} = 89.23$$
 times the object.

The telescope is to be used at the limited distance D=1380 feet and $D=\infty$. Required the proper lengths l=? and micrometrical motion of the ocular or eye-lens? when the limit of distinct sight $\mathfrak{a}=10$ in. F=58:12=4.833 feet. f=0.65:12=0.05416 feet.

$$l = \frac{1380 \times 4.833}{1380 - 4.833} + \frac{10 \times 0.05416}{10 + 0.05416} = \frac{4.89035}{0.05386}$$
When $D = 1380$ feet, the length $l = \overline{4.94421}$ feet.
When $D = \infty$, $l = 4.8333 + 0.05386 = 4.88719$
Micrometrical motion of eye lens
$$\begin{cases} 0.05702 & \text{,} \\ 0.68424 & \text{inches.} \\ \frac{11}{16} & \text{nearly.} \end{cases}$$

Table of Refractive Indices.

Substances.	Index. m.	Substances.	Index. m.
Cromate of Lead Realgar Diamond Glass, flint Glass, crown Oil of Cassia Oil of Olives	2·97 {2·50 2·55 2·45 1·57 1·52 1·63 1·47	Quartz	1.54 1.40 1.33 1.30 1.000138 1.000272 1.000294



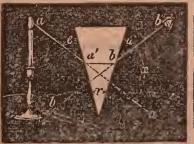
314

Prism.

An emergent rays of light a a' falling upon a transparent medium A (say a glass prism) will be transmitted through in the direction a b, and de livered in the direction b b', parallel to a a' a''.

V = angle of incident, v = angle of refraction.

Indix of refraction
$$m = \frac{\sin \cdot V}{\sin \cdot v}$$
.



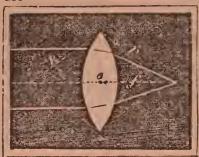
315 Given the direction of the emergent rays a a', angles e and r—to find the angles u and x—or the direction of the rays b b'.

$$\cos z = \frac{\cos e}{m}, \cos u = m \cos (180 - z - r).$$

$$x = 180 - (e+r+u)$$
.

When e = u, the angle x is smallest.

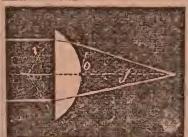
An eye in b' will see the candle in the direction b' b b''.



316 Double Convex Lens.

$$f = + \frac{Rr}{(m-1)(R+r)}$$
 the principal focal distance.
 $f = \frac{r}{2(m-1)}$ when $R = r$

o = optical centre of the lens.

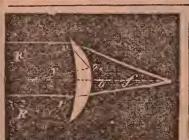


317

Plano Convex Lens.

$$f = + \frac{r}{m-1}.$$

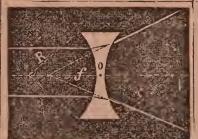
The optical centre is in the convex surface.



318 Convex-concave Lens (Meniscus.)

$$f = + \frac{R r}{(m-1)(R-r)}$$

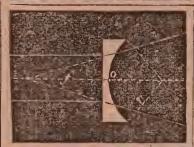
Draw the radii R' and r' parallel to one another.—Draw n o, then o is the optical centre.



319

Double Concave Lens.

$$f = -\frac{R r}{(m-1)(R+r)}$$

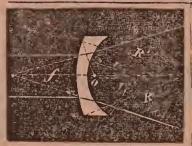


320

Plano Concave Lens.

$$f = -\frac{r}{m-1}.$$

The optical centre is in the concave surface.



321

Concavo-convex Lens.

$$f = -\frac{R r}{(m-1)(R-r)}$$

Draw R and r' parallel to one another. Draw n o, then o is the optical centre.



322

Single Microscope.

$$I: O = f: f - d, \quad I = \frac{Of}{f - d}, \quad D = \frac{df}{f - d},$$

$$\mathfrak{P} = \frac{\mathfrak{A} + f}{f}, \quad \mathfrak{P} = \frac{\mathfrak{A} f}{f - \mathfrak{A}}, \quad \mathfrak{d} = \frac{\mathfrak{A} f}{\mathfrak{A} + f}.$$



323

When the object O is beyond the focal distance the image I will be inverted.

$$I: O = f: D - f, \quad I = \frac{Of}{d - f}, \quad d = \frac{Df}{D - f}.$$



324 Diminishing Power of a Double Concave Lens.

$$I: O = f: f + D \qquad I = \frac{Of}{f + D},$$

$$D = \frac{f(O - I)}{I}, \qquad d = \frac{Df}{D + f}.$$

325

Astronomical Telescope.



Z



 $I\colon O=F\colon f,$

 $I = \frac{OF}{f}, \qquad d = \frac{Df}{F}.$

$$l = \frac{D F}{D - F} + \frac{a f}{a + f}.$$

(if $D = \infty$, $l = F + \frac{a}{a} f$)

* + for astronomical telescope,

- for opera-glasses.

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Opera Glass.



D



Formulas are the same as for Astronomical Telescope.

GEOGRAPHY.



The Earth on which we live is a round ball or sphere, with a mean diameter of 7914 statute miles. The whole surface of the earth is 196,800,000 square miles, of which only one-fourth or nearly 50,000,000 square miles is land, and about 150,000,000 square miles water.

Table of Area and Population of the Whole Earth, 1883.

Division	ns o	f th	e Ea	rth.		Area in Square Miles.	Population.	Proportion to Square Mile.
America,						14.491,000	100,466,000	7
Europe, .						3,760,000	327,743,400	87
Asia, .						16,313,000	795,591,000	49
Africa, .		,				10,936,000	205,823,260	20
Oceanica,	•		•	1	•	4,500,000	31,619,000	7
Total,			•	•		50,000,000	1,461,242,660	30

About $\frac{1}{30}$ th of the whole population are born every year, and nearly an equal number die in the same time; making about one born and one dead per second.

The annual increase of population per 1000 is about 6 in Europe and 19 in America. Europe loses and America gains by emigration. The annual increase of population in the whole world is about 6 per 1000.

The Earth is not a perfect sphere, it is flatted at the Poles. The following are her true dimensions in statute miles of 5280 feet.

Dimensions of the Earth.

Diameter, . . {7898.8809 miles at the Poles. 7911.92 miles mean, or in 45° lat. 7924.911 miles at the Equator.

Difference, . . 26.0302 miles Poles and Equator.

Flatted, . . . 13.015 miles at each Pole.

Circumference, {24802.486 miles round the Poles. 24851.640 miles mean, or in 45° lat. 24884.22 miles round the Equator.

To Find the Radius of the Earth in Any Given Latitude.

 $R = 3955.96(1 + 0.00164 \cos 2l)$, statute miles.

Distribution of Population in the World.

	ISTIDUU	on or Lobur	ation in	the world.	
Br. Amer.,	5,800,000	Denmark,	2,700.000	Puebla,	75,500
78.47 1 2	102,000	Copenhagen,	180,000		63,000
Montreal, .				Guanajuato,	
Quebec,	62,000	Russia,	70,000.000	Cuba,	1,420,000
Toronto,	45,000	St. Petersb'rg,	680,000	Havana,	209,000
St. John, N.B.	37,000	Moscow,	400,000	St. Jago Cuba,	100,000
Halifax, N.S.	28,000	England,	22,703,000	Porto Rico	616,000
		London		C. America	
Ottawa, Ont.,	15,000	London,	3,883,000		2,665,000
U.S. Amer.,		Scotland,	3,359,000	Whites,	133,000
N.York &Brk.	1,338,600	Edinburgh,.	180.000	Indians.	1,500,000
Philadelphia,	675,000	Glasgow, .	468,000	Negroes,	30,000
Chicago,	209,000	Ireland, .	6,000,000	Mixed,	1,000,000
St. Louis, .	311,000	Dublin,	322,000	Guatemala	1,180,000
		Duomi, .			
Baltimore, .	268,000	France, Rp.,	36,595,000	Guatemala, A	40,000
Boston,	251,000	Paris,	1,830,000	St Salvador	600,000
Cincinnati, .	216,000	Germ. Emp	41,000,000	St. Salvador, A	20,000
S'n Francisco,		Berlin,	702,000	Nicaragua,	400,000
Washington,	120.000	Austria, .	20,400,000	Managua, .	10,000
				managua, .	
Buffalo,	118,000	Vienna,	607,500	Honduras,	350,000
Newark,	105,000	Hungary,	15,509,000	Comayagua,	8,000
Louisville, .	101,000	Pesth,	202,000	Costa Rica,	135.000
Cleveland, .	93,000	Holland, .	3,688,500	San Jose, .	25,000
Pittsburg, .	87,000	Amsterdam,	281,800	S. America,	31.369,000
Jersey City,	82,500	Bavaria, .	4,825,000	Wild Indians,	3,500,000
Detroit	80,000	Munich, .	171,000	Whites,	10.000,000
Milwaukee,.	71,500	Switzerl'd,	2,670,000	Negroes,	600,000
Providence,	69,000	Berne,	29,500	Mixed,	14,569,000
Albany,	69,500	Belgium,	5,022,000	U.S.Colom.	3,000,000
Dock auton		Brussels,			50.000
Rochester, .	62,500		287,000	Bogota,	
Alleghany, .	53,200	Spain,	16,642,000	Panama,	20,000
Richmond,	51,000	Madrid,	317,000	Venezuela,	1,565,000
New Haven,	51,000	Italy,	26,000.000	Caraccas, .	48,000
Charleston, .	49,000	Rome,	240,000	Equador,	1,110,000
Troy,	46,500	Greece,	1,458,000	Quito,	76.000
Syracuse, .	43,000	Athens,	42,000	Guiana, .	221,000
	41,500	Turkey, E.,	15,487.000	Georgetown,	26,000
Indianapolis,					11,780,000
Worcester, .	41,100	Const'tinople,	1,075.000	Brazil,	
Lowell,	41,000	Turkey, A.,	16,463.000	Rio Janeiro,	420,000
Memphis, .	40,200	Smyrna, .	150,000	Bahia,	152,000
Cambridge,	4 0,000	Arabia,	8,000,000	Slaves,	1,400,000
Hartford, .	37,200	Mecca,	60,000	Peru,	3,100,000
Scranton, .	35,100	Persia,	9,000,000	Lima,	130 000
Reading,	34,000	Tabreez, .	110,000	Callao,	40,000
Reading,	20,200	Afgh'nist'n			1,990,000
Kansas City,	32,300		4,000,000	Bolivia,	
Mobile,	32,000	Candabar, .	100,000	La Paz,	22,000
Portland, .	31,500	Beloochs'n	1,500 000	Chili,	1,909,000
Wilmington,	31,000	Kelat,	15,000	Santiago, .	115,380
Toledo,	31,600	Turkistan,	6,500.000	Valparaiso, .	70,500
Columbus, .	31,300	Bokhara, .	100,000	Argentine,	1.750,000
	30,500	India,	172,000,000	Buenos Ayres	177,800
Dayton,		Bombay,			1,330,000
Lawrence, .	29,000		817,000	Paraguay,	
Utica,	28,800	Calcutta,	61 6,000	Asuncion,	15,000
Savannah, .	28,300	China,	446,500,000	Uruguay,	2,614,800
Nashville, .	26,000	Peking,	1,800,000	Montevideo,	128.000
Alaska,	54,000	Canton,	1,000,000	Patagonia,	1,200,000
Sitka,	?	Hong-Kong,	40,000	Antonio,	? '
		Japan, .	35,000,000	Australia,	1,900,000
RACES IN U. S.	33,570,000	Yeddo,	2,000.000	Melbourne,	193.700
White,					
Colored,	4,890,000	Miaco	500,000	Wellington,	3,300
Chinese,	64,000	Barbary, .	2,800.000	Jamaica,	444,000
Indians,	25,500	Tunis,	130.000	Kingston, .	36 ,500 j
		Egypt,	5,195,000	Hayti,	572.000
Sweden, .	4.106,000	Cairo,	313.400	P't-au-Prince	21 000
Stockholm,	136,000	Jerusalem, .	25,000	Sandwich I	73.000
Norway, .	1,650,000	Mexico,	9,200.000	Honolulu, .	13 530
Christiana,	63,500	Mexico City,	200,000 1	W. Indies,	4,000,000

Latitude and Longitude of Places (from Greenwich.)

	Latitude.	Longitude.		Latitude.	Longitude.
America	D. M. S.	D M. S.	France.	D. M. S.	D. M. S.
Atl. Coast.				48.50.13 N.	0.09.21 E.
Quebec	46.49. N		Paris, Obs	49.38.	
Halifax	XI.00.	00.00.	Cherbourg	43.18.	Tiot.
Chicago	42.00. "	01.00.	Marseilles	40.10.	0.44.
Boston	42.21. "	(1.Ut.	Calais	00.00.	1.01.
New York	40.42. "	74.00.42 "	Brussels	90.91.	4.24.
Philadelphia .	39.57. "	75.10. "	Antwerp	5 1 .13. "	4.24.
Cincinnati	39.06. "	04.00	Italy.	45.04.06 45	
St. Louis	38.36. "	89.36. "	Turin	任9.0年.00	7.42. "
Washington .	38.53. "	77.00.18 "	Florence	30.XU.	11.10.
Charleston	32.42. "	79.54. "	Leghorn	40.04.	10.18.
New Orleans .	29.57.30 "	90.00. "	Rome	ましひま	14.44.
Georgetown, Br.	32.22.12 "	46.37.06 "	Malta	35.54. "	14.30. "
Nassau	25.05.12 "	77.21.12 "	Naples	40.50. "	14.16. "
Port-au-Prince	19.46.24 "	72.11.12 "	Palermo	38.08. "	13.22. "
Porto Rico	18.29. "	66.07.06 "	Venice	45.26. "	12.21. "
Kingston, Jam.	17.58. "	76.46. "	Austria.		
Havana	23.09. "	82.22. "	Vienna	48.13. "	16.23. "
Vera Cruz	19.12. "	96.09. "	Trieste	45.39. "	13.46. "
Mexico, City .	19.26. "	99.05. "	Pestli	47.28. "	19.13. "
Colon, N. G.	9.22. "	79.55. "	Germany.		
Para	1.28. S.	48.29. "	Berlin	52.31. "	13.24. "
Rio Janeiro	22.56. "	43.09. "	Hamburg	53.33. "	9.56. "
Buenos Ayres	34.36. "	58.22. "	Cologne	50.56. "	6.58. "
Cape Horn.	55.59. "	67.16. "	Amsterdam .	52.22. "	4.51. "
Pac. Coast.			Bremen	53.05. "	8.49. "
Valparaiso	33.02. "	71.41. "	Berne	46.57. "	7.25. "
Callao	12.04.	79.13. "	Turkey.		
Lima*	12.02.34 "	79.06. "	Constantinople	41.01. "	28.59. "
Cuzco*	13.31.45 "	74.15.50 "	Ragusa	42.38. "	18.07. "
Payta	5.05. "	81.10. "	Salonica	40.39. "	22.57. "
Guayaquil.	2.13. "	79.53. "	Athens	37.53. "	23.44. "
Panama	8.57. N	1	Smyrna	38.26. "	27.07. "
Acapulco	16.55. "	99.48. "	Cairo	30.03. "	31.18. "
San Francisco	37.47. "	122.21. "	Jerusalem, Pal.	31.48. "	37.20. "
Alaska	58.	158	Russia.		
Beliring's Strait		170	St. Petersburg	59.56. "	30.19. "
China. Ind.			Moscow	55.46. "	35.33. "
Peking	39.54. "	116.23. E.	Nish Novgorod	56.20. "	43.43. "
Canton	23.07. "	113.14. "	Cazan	55.48. "	48.50. "
TT 1	22.15. "	114.12. "	Archangel	64.32. "	40.14. "
1 "1 1	21.19. "	157.52. "	Jecatherinburg	56.50. "	60.21. "
	35.40, "	139.43. "	Astracan	46.21. "	47.46. "
Jeddo	20.23. "	155.54. W.	Odessa	46.27. "	30.42. "
Calcutta	22.34. "	88.20. E.	Warsaw	52.13.05 "	21.02.9 "
Batavia	6.08. "	106.50. "	Sweden.		
	34.00. S		Stockholm	59.21. "	18.04. "
Sydney	37.48.36 "	144.57.45 "	Gothenburg .	57.42. "	11.57. "
347 319 4	41.14. "	174.44. "	Wisby, Gotland		18.17. "
Africa.	TI.IT.		Christiania .	59.55. "	10 52. "
	34.22. "	18.30. "	Bergen	60.24. "	5.20. "
Cp. of G. Hope.	39.34. N	1	Ystad	55.25. "	13.50. "
Morocco Algiers	36.47.	3.04. "	Haparanda .	65.49. "	24.11. "
Aigiers	30.47.	5.0x.	Copenhagen .	55.41. "	12.34. "
England.	51.31. "	0.06. W.		00.11.	12.0x.
London, Tower	01.01.	0.00.	1 m r 3 3 3 3	40.25. "	3.42. W.
Greenwich .	01.20.00	2.52. "	70 1	41.23. "	2.11. E.
Liverpool	00.44.	4.04.	C1.1. 14	36.06. "	5.20. W.
Glasgow	00.02.	7.10.	0 11	37.36. "	1.01. "
Edinburgh	00.01.	2.35. "	1 - 1	38.42.	9.09. "
Bristol	51.27. "	1.19. E.	Disboil	41.11. "	8.38. "
Dover	01.00.			Tr.II.	0.00.
Dublin	5 3.23.	# Measured by		MI.TI.	17.56. "
		1.0000000000000000000000000000000000000	, , ,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,		

Difference of Longitude in Time Between Places.

	San Francisco.	New York.	London. Greenwich.	St. Peters- burg.	Canton, China.
	H. M. S.	H. M. S.	н. м. s.	H. M. S.	н. м. s.
Amsterdam	8 29 19	5 15 32	0 19 32	1 41 44	7 13 24
Antwerp	8 27 17	5 13 30	0 17 36	1 43 40	7 15 20
Batavia	8 42 50	11 56 37	7 07 20	5 6 4	0 25 36
Berlin	9 3 22	5 49 35	0 53 35	1 7 41	6 39 21
Boston	3 25 33	0 11 46	4 44 14	6 45 30	11 4 2 <i>5</i> 0
Buenos Ayres	4 16 19	1 2 32	3 53 28	5 54 44	11 26 24
Canton	8 17 17	11 31 4	7 32 56	5 31 40	0 0 0
Calcutta	9 56 53	10 49 20	5 53 20	3 52 4	1 39 36
Cairo	10 14 59	7 1 12	2 5 12	0 3 56	5 27 44
Copenhagen	9 0 3	5 46 16	0 50 16	1 11 0	6 42 40
Constantinople Dublin	10 5 43 7 44 25	6 51 56 4 30 38	$\begin{array}{ c c c c c c c c c c c c c c c c c c c$	0 5 20	5 37 0
731	7 44 25 8 54 51	4 30 38 5 41 4		2 26 38	8 18 18
Gibraltar	7 47 56	4 34 32	$\begin{bmatrix} 0 & 45 & 4 \\ 0 & 21 & 28 \end{bmatrix}$	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	6 47 52 7 54 24
Gothenburg.	8 57 38	5 43 51	0 47 48	1 13 28	7 54 24 6 45 08
Halifax	3 54 27	0 41 40	4 14 20	6 15 36	11 47 16
Hamburg	8 49 39	5 35 52	0 39 52	1 21 24	6 53 04
Jecatherinburg	11 48 57	7 25 20	4 1 16	2 0 0	3 31 40
Jerusalem	10 39 7	7 25 20	2 23 20	0 22 4	5 09 36
Lima	1 43 2	0 12 24	5 08 24	7 9 40	11 18 40
London	8 9 50	4 56 3	0 0 24	2 1 40	7 33 20
Lisbon	7 33 11	4 19 24	0 36 36	2 37 52	8 08 32
Madrid	7 55 39	4 41 52	0 14 8	2 15 24	7 47 04
Melbourne	4 2 24	7 16 11	9 39 51	11 41 31	2 7 0
Naples	9 6 51	5 53 4	0 57 4	1 04 12	6 35 52
New Orleans	2 9 37	1 04 10	6 0 10	8 01 26	10 26 54
New York	3 13 47	0 0 0	4 56 3	6 57 19	11 31 01
Paris	8 19 7	5 5 20	0 9 20	1 51 50	7 23 36
Peking	8 4 21	12 41 52	7 45 52	5 44 36	0 12 56
Quebec	3 2 36	0 11 11	4 44 49	6 46 5	11 19 53
Rome	8 59 35	5 45 48	0 49 48	1 11 28	6 43 08
San Francisco	0 0 0	3 13 47	8 9 47	10 11 3	8 17 17
St. Louis	2 8 46	1 5 1	6 1 1	8 2 17	10 26 03
St. Petersburg	10 11 3 9 22 11	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	$\left \begin{array}{cccc} 2 & 1 & 16 \\ 1 & 12 & 24 \end{array} \right $	$\begin{bmatrix} 0 & 0 & 0 \\ 0 & 58 & 52 \end{bmatrix}$	5 31 40
Stockholm	8 40 38	5 26 51	0 30 48	1 30 28	6 20 32
XX7 1 1 4	3 1 46	0 12 1	5 8 1	7 9 17	7 02 08 11 19 53
Wellington, N. Z	5 30 22	8 44 09	11 38 56	10 19 48	2 46 52
Tollington, It. Z	0 00 22	0 11 03	1 71 00 00 1	10 10 10	40 04

To Reduce Longitude in Degrees into Time, and vice versa.

RULE 1. Divide the number of degrees by 15, and the quotient is the corre sponding hours. Should the degrees be less than 15, multiply them by 4, and the product will be minutes in time. The minutes of degrees multiplied by 4 will be seconds in time. The seconds of degrees divided by 15 will be seconds in time.

RULE 2. The time in hours, minutes and seconds, multiplied by 15, will be the corresponding angle in degrees, minutes and seconds. The trigonometrical table contains the conversion of time and angle.

Example 1. Required, the difference in time between Philadelphia and Paris?

Longitude of Philadelphia, 75° 10' W.

" Paris, 2 20 E.

770 30' Difference in longitude divided by 15 will be 5h 10m, the difference in time. When it is 12 o'clock in Philadelphia, it is 5h 10mo'clock in Paris.

Example 2. A vessel sails from New York to Liverpool; after she has been at sea about one week, her difference in time with New York is found to be 2h7m 45s. Required, her longitude from New York?

 $15(2h\ 7\ 45) = 31^{\circ}\ 58'\ 15''$ from New York.

The time is ahead in the east, from where the sun rises. The time is behind in the west, toward sunset.

San Francisco 5820

Distances by Sca

100 9780	800 17400	380 16980	936 15796	731 15591	236 15096	147 15007	076 14836	848 14628	790 1457	740 14520	500 14280	254 13020	640 13080	658 14091	680 15000	9780 7680	7860 2580	6480 4620
Cape Horn. 6100	Orleans 7620 13800 17400	2129 7200 13380 16980	6076 8837 15936 15796	5871 8632 15731	5376 8137 15236 15096	5287 8047 15147 15007	5136 7896 14076 14836	4908 7668 13848 14628	4850 7610 13790 14570	4800 7560 13740 14520	4560 7320 13500 14280	4300 6460 1254 13020	4500 6460 12640 13080	5518 7578 13658 14091	6540 8460 14680 15000	7380 3600 9		
	New Or	York.	4516	4311	3816	3727	3576	3348	3290	3240	3000	2980	3220	4238	5260	0069	20801	23001
		New	sburg.	377	200	839	1188	1421	1686	1407	1986	2336	2606	3624	4716	9908	3244 1	42361
			St. Petersburg.	Stockholm.	495	634	983	1216	1481	1201	1841	2131	2405	3419	4511	1984	30391	40311
			St	Stock	Copenhagen.	139	488	721	986	904	1286	1636	1906	2924	4016	1386 7861	125441	1353611
					Copen	Gottenburg.	360	582	897	617	1197	1547	1817	2835	3927	7277	12457	113471
	ci :					Gotte	Hamburg.	348	726	451	1256	1370	1680	2698	3720	0804	12260	13296
	places on the earth: in	മ്					Har	Antwerp.	518	258	818	1168	1438	2456	3548	6838	12018	13068
	n the	degre						ΨD	Paris.	410	160	1110	1380	2398	3490	6840	12060	1301
	o sees	ou per degree.		mole	99					London-	710	1060	1400	2418	3440	6840	12020	12960
				ich Tele	TOT TOT					Ä	Liverpool.	006	1200	2218	3240	0099	11780	12720
	porta	ilm 1	obe.	Sanda	33						Liv	Lisbon.	330	1348	23.40	5340	10520	11460
	st im	puice	H poor	n. 1980 to	4500								Gibraltar. 330	Rome, 1018 1348	2040	5400	10580	11520
	between the most important	Geographical miles,	* Round Cape of Good Hope.	TRound Cape Horn. From San Francisco 1980 to Sandwich Telands	,								Gil	Rome.	Constantinople. 1150 2040 2340 3	Care Good Hope. 7320 6418 5400 5340 6600	11598	12538
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Milles.	Nearest travelling distances	between Cities in Europe.
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Nearest travelling distances Nadrid 625	1295 625 1250 625 1295 650 625 885 442 630 445	002 790 267 1055 544 332 936 724 984 772 951 739
Antwerp 1142 877 Hamburg 391 1560 1295 Berlin 175 509 1515 1250 Berne 608 605 541 1150 885 Turin 193 803 901 736 895 630	265 890 1 877 252 1295 670 1250 625 885 442 630 445	<u> </u>
Antwerp 1142 877 Hamburg 391 1560 1295 Berlin 175 509 1515 1250 Berne 608 605 541 1150 885 Turin 193 803 901 736 895 630 Viennal 669 574 500 679 751 1794 1459	877 252 1295 670 1250 625 885 442 630 445	
Hamburg 391 1560 1295 Berlin 175 509 1515 1250 Berne 608 605 541 1150 885 urin 193 803 901 736 895 630 689 574 500 679 751 1794 1459	625 442 445	
Berne 608 605 541 1150 885 urin 193 803 901 736 895 630 689 554 1794 1459	625 442 445	
Berne 608 605 541 1150 885 urin 193 803 901 736 895 630 669 659 751 1794 1459	442	
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669 574 500 679 751 1794 1459	400	954 742
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Munich 270 508 281 454 600 513 1431 1166 551	551	1045 833
Rome 507 745 328 521 9631109 1022 1223 958 773	958 773	1373 1161
Triest 407 342 338 456 584 796 942 855 1351 1086 1107	1086 1107	1399 1187
Warsaw 798,1069 563 460,1034 836 536 711,1045,2051,1786,1297	1786 1297 1589	589 1377
Constantinople 1200 1000 1050 1679 1409 1456 1584 1909 2084 2160 2350 2086 2412	2086 2412 2704	704 2492
Odessa 750 805 1400 1907 1369 1099 1856 2000 1336 1511 1836 2750 2485 1900	2485 1900 2450	450 2238
792 2751 3158 2683 2413 3191 2964 2489 2664 3173 4004 3739	3739 3114 3717	212 3505
969 1144 1478 2484 2219	2219 1594 1953	953 1741
1148 1633 1928 1291 1370 1799 1606 866 691 1082 2251 1986	1986 1334 1626	626 1413
967 1198 1493 856 935 1364 1171 431 256 647 1816 1551	899	1191 979
Lubeck 234 669 1109 1504 1514 2123 709 748 1146 639 718 849 643 214 39 352 1599 1334 710	710	896 634

Halifax.

Boston. 390

Nantucket light, 107 | 360

Sailing distances

between the most important seaports in the United States, in Geographical miles, 60 per Degree.

		IO2	LLLL		D 10											_
648	999	650	753	765	416	923	795	865	984	1065	1162	1930	1900	2685	2800	2635
284	302	380	483	508	661	299	539	609	624	905	1000	1768	1738	2413	2638	2738
 193	211	274	377	403	555	199	433	503	426	202	802	1570	1540	2215	2440	2640
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Sandy	New York.	149	252	276	428	434	306	375	340	621	912	1484	1454	2129	2354	2554
	New	Cape Henlopen.	103	135	287	293	165	235	218	499	594	1362	1332	2007	2232	2432
		pe Her	Philadelphia.	238	390	396	268	338	321	602	269	1465	1435	2110	2335	2535
		Ca	Philad	Cape Henry, 238	152	158	30	100	114	395	490	1258	1228	1903	2128	2328
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						Washi	Norfolk, 178	06	144	425	520	2288	1258	1933	1158	2358
							Z	Richmond.	214	495	290	1348	1328	2003	2228	2428
								Rich	Cape Hatteras.	281	928	202	738	1413	1638	1838
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ğ	pany.	231	329	368	499	746	308	1088	1333	1508	2004	1143	806	693	545	289	325	508
	All	87	185	224	355	602	864	926	1221	1396	1892	1293	1048	84.7	470	194	470	636
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ASTRONOMY.

The matter constituting the heavenly bodies has probably been evenly distributed in space from the beginning; the force of attraction gradually formed bodies, which accumulated into groups or nebulæ, each of which finally became a planetary system with the largest body in the centre, now seen as stars. This operation of forming or creating bodies and planetary systems is still and will for ever be continued in parts of the infinite space. Each star has a planetary system, and astronomers have even been able to observe some planets of the star Sirius.

The magnitude of this operation, with the enormous dimensions, even within a single group, can hardly be conceived by any human mind; for the long row of figures expressing a number of conceivable units of length or weight does not

bring the real magnitude within conception.

The Sun.

The sun is a dark body surrounded by a luminous substance in which spots are frequently seen. The spots are caused by meteors or other heavenly bodies falling into it.

Mean distance from the earth to the sun, 95,000,000 miles, or 11,992 diameters of the earth.

Inclination of the ecliptic to the equinoctial, 23° 28′ 40″.

The sun subtends an angle from the earth of 32' 3".

Horizontal parallax of the sun, 8.6".

The Moon.

Distance from the Earth to the Moon, 273,000 miles, = 30 diameters of Earth, or about 0.25 diameters of the Sun, or the diameter of the Sun is twice the diameter of the Moon's orbit around the Earth.

Diameter of the Moon, 2160 miles, or about 0.2729 of the diameter of the Earth.

Volume of the Moon, 0.02024 of that of the Earth.

Density of the Moon, 0.5657 of that of the Earth.

Mass of the Moon, 0.0114 of that of the Earth. .

Inclination of the Moon's orbit to the ecliptic, 5° 8′ 48″.

The Moon subtends an angle from the Earth of 31' 7".

Mean sidereal revolution of the Moon, 27.32166 solar days.

Mean synodical revolution of the Moon, 29.5305887 solar days.

The Moon passes the meridian in periods of 24.814 hours, or 48m. 50s. later every day.

Moon's Age is the number of days from the last new moon.

Epact of the Year is the Moon's age on the 1st of January of each year. See Almanac for the 19th Century.

The sum of the epact of the year and that of the month is the moon's age on the first of the month.

Epact of the Month.

Jan.	Feb.	March	April.	May.	June.	July.	Aug.	Sept.	Oct.	Nov.	Dec.
0	2	1	2	3	4	5	6	8	8	10	10

To Find the Moon's Age on Any Given Day.

Add together the epacts of the year and month and the date of the month; the sum will be the moon's age. If it exceeds 30, reject that much, and the remainder is the moon's age.

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Almanac for the 19th Century.

Yrs.	Days.	Dom. let-	Epact.	Yrs.	Days.	Dom.	Epact.	Yrs.	Days.	Dom.	Epact.
7000	0-41-2	ter.		1001	G - 4 3	ter.	1 6	1000	G3	ter.	1
1800	Saturd.*	FE	4	1834	Saturd.	E	20	1868	Sunday*	ED	6
1801	Sunday.	D	15	1835	Sunday.	D	. 1	1869	Monday.	C	17
1802	Monday.		26	1836	Tuesd.*	CB	12	1870	Tuesday.	В	28
1803	Tuesday.	B	7	1837	Wednes.	A	23	1871	Wednes.	A	9
1804	Thursd.*	AG	18	1838	Thursd.	G	4	1872	Friday.*	GF	20
1805	Friday.	F	29	1839	Friday.	F	15	1873	Saturd.	E	1
1806	Saturd.	E	11	1840	Sunday*	ED	26	1874	Sunday.	D	12
1807	Snuday.	D	22	1841	Monday.	C	7	1875	Monday.	C	23
1808	Tuesd.*	CB	3	1842	Tuesday.	P	18	1876	Wedns.*	BA	4
1809	Wednes.	A	14	1843	Wednes.	A	29	1877	Thursd.	G	15
1810	Thursd.	G	25	1844	Friday.*	GF	11	1878	Friday.	E	26
1811	Friday.	F	6	1845	Saturd.	E	22	1879	Saturd.	E	7
1812	Sunday.*	ED	17	1846	Sunday.	D	3	1880	Monday*	DC	18
1813	Monday.	C	28	1847	Monday.	C	14	1881	Tuesday.	B	29
1814	Tuesday.	В	9	1848	Wedns.*	BA	25	1882	Wednes.	A	11
1815	Wednes.	A	20	1849	Thursd.	G	6	1883	Thursd.	G	22
1816	Friday.*	GF	1	1850	Friday.	F	17	1884	Saturd.*	FE	,
1817	Saturd.	E	12	1851	Saturd.	E	28	1885	Sunday.	D	14
1818	Sunday.	D	23	1852	Moud.*	DC	9	1886	Monday.	C	25
1819	Monday.	C	4	1853	Tuesday.	В	20	1887	Tuesday.	В	6
1820	Wedns.*	BA	15	1854	Wednes.	A	1	1888	Thursd.*	AG	17
1821	Thursd.	G	26	1855	Thursd.	G	12	1889	Friday.	F	28
1822	Friday.	\mathbf{F}	7	1856	Saturd.*	FE	23	1890	Saturd.	E	9
1823	Saturd.	E	18	1857	Sunday.	D	4	1891	Sunday.	D	20
1824	Monda.*	DC	29	1858	Monday.	C	15	1892	Tuesd.*	CB	1
1825	Tuesday.	B	11	1859	Tuesday.	В	26	1893	Wednes.	A	12
1826	Wednes.	A	22	1860	Thurs.*	AG	7	1894	Thursd.	G	23
1827	Thursd.	G	3	1861	Friday.	\mathbf{F}	18	1895	Friday.	F	4
1828	Saturd.*	FE	14	1862	Saturd.	E	29	1896	Sunday*	ED	15
1829	Sunday.	D	25	1863	Sunday.	D	11	1897	Monday.	C	26
1830	Monday.	C	6	1864	Tuesd.*	CB	22	1898	Tuesday.	В	7
1831	I Tuesday.	В	17	1865	Wednes.	A	3	1899	Wednes.	A	18
1832	Thursd.*	AG	28	1866	Thursd.	G	14	1900	Friday.*	GF	29
1833	Friday.	F	9	1867	Friday.	F	25	1901	Saturd.	E	11

The day of the week opposite the year in the &'manac falls on the dates in this table.

February, March, November.	February,* August.	May.	January, October.	January,* April, July.	September, December.	June.
1 8 15 22 29	2 9 16 23 30	3 10 17 24 31	4 11 18 25	5 12 19 26	6 13 20 27	7 14 21 28

In leap years take January,* February.*

Example 1. On what day of the week will the 4th of July fall in the year 1880? See table 1890 = Monday, which answers to the 5th in the date table, consequently the 4th of July is on Sunday.

Example 2. It is known to be Saturday in the middle of August, 1875. Required.

the date of that day?

The year 1875 = Monday (see almanac), then August the 16th falls on Monday, and Saturday on the 14th.

Example 3. A gentleman was born on the 8th of February, 1824. Required,

the day of the week?

1824 = Monday, which fell on the 9th. The gentleman was consequently born on a Sunday.

CHRONOLOGY.

Our unit of time, year, is the period in which the earth makes one revolution

around the sun, in reference to a fixed star.

The unit day is the period in which the earth makes one revolution around its axis, in reference to the sun; but as the earth moves in an ellipse in which the sun is in one focus, the apparent solar day is not a constant period—that one hundred solar days in the winter are about half an hour longer than one hundred solar days in summer, for which a mean day is assumed in reference to an imaginary sun which falls in with the real sun about the 15th of April and 24th of December, when the mean time and apparent time are alike. The mean solar day is divided into twenty-four hours, of which the clock indicates twelve hours twice.

Sidereal Time.

The Sidereal Day is the interval of time in which any fixed star passes the meridian. The sidereal day is only 23h. 56m. 4.09s. mean solar time, or the fixed stars

pass the meridian, rise or set, 3m. 55.909s. earlier every day.

A Sidereal Clock in an astronomical observatory marks twenty-four hours in the interval of time in which any fixed star passes the meridian. The Right Ascension of the heavenly bodies is the time when the body passes the meridian by the sidereal clock. The dial of a sidereal clock is divided into twenty-four hours, and the hours are numbered from one up to twenty-four.

Years.

The tropical year, or the periodical return of seasons, is 365,24224 days = 365d.

5h. 48m. 49.536s. mean solar time.

The civil year is 365 days, or nearly one-fourth of a day too short, for which one day is added every four years, called leap year. But this addition makes one day too much in every 128.866 years, which error is corrected every fourth century which can be divided by 4 without a remainder.

Leap years of the Christian era are those that can be divided by 4 without a

remainder.

In some countries these important corrections are not properly attended to, as in Russia and Greece, where the dates are now twelve days behind our Gregorian reckoning.

The wild Indians of South America reckon their time by new moons, when all

their festivals are celebrated.

Dates.

The civil date of the month commences at midnight. The astronomical date commences at noon. The mariner's date (sea account) commences twelve hours before the civil date, and twenty-four hours before the astronomical date, or the mariner's date is one day ahead of the astronomical date.

Cycle of the Sun is the period of twenty-eight years, at which the days of the

week return to the same days of the month.

Lunar Cycle or Golden Number is the period of nineteen years, at which the changes of the moon fall on the same days of the month.

To Find the Golden Number.

Add 1 to the given year, divide the sum by 19, and the remainder will be the golden number. If 0 remains, the golden number is 19.

The age of the Julian period on the 1st of January, 1872, is 2,404,794 days.

Creation of the World.

Creation of the world, 4000 before Christ. Julius Africanus says 5508: Samaritan Pentateuch, 4700; Septnagint, 5872; Josephus, 4658; Talmudists, 5344; and others give different times; but the Chinese tradition and history claim an antiquity of 100,000 years before Christ. From geological formations, and from the working of rivers like that of Niagara, and the Danube cutting through the Alps at the Iron Gate, it can be estimated an age of millions of years. The creation itself, or the accumulation of the enormous quantities of matter in the larger planets, must have required millions of years. No body, however small, has been instantly created. Creation is work which consists of the three physical elements—force, motion and time—by which bodies grow like a tree, or by gradual accumulation of matter. These three physical elements constitute the trinity which governs the material universe. All creation, or action of whatever kind, whether mechanical, chemical or derived from light, heat, electricity or magnetism—all that has been and is to be done or undone—is accomplished by this triune function. It is omnipotent, ubiquitous and eternal.

Chronological Notes.

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Before Christ. B. C.	YEARS.	After Christ. A.D.	YEARS.
Deluge, 2348 (Hales), .	. 3154	Beginning of Christian Era, .	0
Tower of Babel finished, .		Christ crucified,	37
Chinese Monarchy,	2203	Destruction of Jerusalem	69
Egyptian Pyramids,	. 2090	Arabic numbers introduced,	991
Moses born,		Mohanimedan Era,	622
Troy destroyed,	. 1180	New Style in England,	1752
The compass discovered,		America discovered,	1492
Foundation of Rome,		Pizarro conquered Inca, Peru,	1530
Maps and Geometry introduce	ed, 605	Lutheran religion,	1527
Money coined at Rome,	576	New South Wales discovered,	1606
Hannibal crossed the Alps,		Australia discovered,	1622
Time first measured by water,		American great Republic, .	1775
Carthage destroyed,		Slaves free in West Indies,	1834
Casar invaded Britain, .	. 51	Slaves free in Russia,	1861
Cæsarean era,	. 48	Slaves free in America,	1866

ASTRONOMICAL ALMANAC.

From the English Nautical Almanac.

The following tables show the sun's right ascension and declination; also, the equation of time at Greenwich, apparent noon, for the year 1873:

In leap years at 6 h. A. M. First year after leap year at noon. Second year after leap year. at 6 h. P. M. In the year before leap year, at midnight following the date.

By the aid of the tables of correction the data can be found for any time and for any meridian.

Example 1. Required, the sun's R. A. on the 10th of April, 1874, at Greenwich, apparent noon?

1874 is the second year after leap year, when the tabular data is for 6 o'clock in the evening. The daily variation of the sun's R. A. is 3 m. 40 s. for the 10th of April, which for 6 hours will be 55 s.

The sun's R. A. on the 10th of April,
Correction for 6 hours, subtract

The required R. A. will be

1 h. 16 m. 24 s.

55 s.

1 h. 15 m. 29 s.

Example 2. Required, the sun's declination on the 20th of September, in the leap year 1876, at 3 o'clock P. M., in longitude 75°, or 5 hours west of Greenwich?

The tabular data for leap years is at 6 o'clock A. M. 3 P. M. and 5 hours difference in longitude make 14 hours of correction.

The daily variation in the sun's declination is 23'.

Sun's declination 20th September, . . . 0° 58′ Subtract correction, 13' 25″ The required declination, 0° 44′ 35″

In leap years take the tabular data one day earlier in January and February.

1	January.	Febru	larv.	March.	11
Date	Rt. As. Declin. Eq. t	n. Rt. As. Dec	lin. Eq. tm.	Rt. As. Declin. Eq. ti	n. Date
	h. m. s. ' m.	h. m. s. 0	m. s.	h. m. s. o m. s. 22 4) 58 S 7 16 +12	3.
1 2	$\begin{vmatrix} 18 & 48 & 49 & 8 & 22 & 59 & + & 3 \\ 18 & 53 & 14 & 8 & 22 & 54 & + & 4 \end{vmatrix}$		$\begin{bmatrix} 6 & 59 & +13 & 54 \\ 6 & 42 & +14 & 2 \end{bmatrix}$	22 47 58 S 7 10 +12 22 53 42 S 7 3 +12	18 2
3	185738 82248 +4	55 21 9 6 S 16	624 + 148	$ 22\ 57\ 26 S 6\ 40 + 12$	5 3
4	$\begin{vmatrix} 19 & 2 & 2 & 8 & 22 & 41 & + & 5 \\ 19 & 6 & 26 & 8 & 22 & 35 & + & 5 \end{vmatrix}$			$\begin{bmatrix} 23 & 1 & 9 & 8 & 6 & 17 & +11 \\ 23 & 4 & 52 & 8 & 5 & 54 & +11 \end{bmatrix}$	
5 6			548 + 1418 = 530 + 1422	23 8 35 S 5 31 +11 3	
7	$ 19 \ 15 \ 11 \ S \ 22 \ 20 + 6$	2 21 25 9 S 18	511 + 1425	$23\ 12\ 17\ S$ 5 8 $+11$	10 7
8.	$\begin{vmatrix} 19 & 19 & 33 & 8 & 22 & 12 & + & 7 \\ 19 & 23 & 55 & 8 & 22 & 3 & + & 7 \end{vmatrix}$		$\begin{vmatrix} 4.52 & +14.28 \\ 4.33 & +14.29 \end{vmatrix}$	$\begin{vmatrix} 23 & 15 & 58 & 8 & 4 & 44 & +10 & 8 \\ 23 & 19 & 39 & 8 & 4 & 21 & +10 & 8 \end{vmatrix}$	
10	$\begin{vmatrix} 19 & 23 & 55 & 8 & 22 & 3 & + & 7 \\ 19 & 28 & 16 & 8 & 21 & 54 & + & 7 \end{vmatrix}$		4 13 +14 29 4 13 +14 30	$\begin{vmatrix} 23 & 19 & 59 & 5 & 4 & 21 & +10 & 5 \\ 23 & 23 & 20 & 5 & 3 & 57 & +10 & 5 \end{vmatrix}$	
11	193236 S $ 2145 $ + 8	0 2141 0 8 13	353 + 1430	23 27 1 S 3 34 +10	7 11
12 13	$\begin{vmatrix} 19 & 36 & 56 & 8 & 21 & 35 & + & 8 \\ 19 & 41 & 15 & 8 & 21 & 25 & + & 9 \end{vmatrix}$		$\begin{vmatrix} 33 \\ +14 \\ 29 \\ +14 \\ 27 \end{vmatrix}$	$egin{bmatrix} 23\ 20\ 41\ S & 3\ 10\ +\ 9\ 3\ 23\ 34\ 21\ S & 2\ 47\ +\ 9\ 3 \end{bmatrix}$	
14	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$			$\begin{bmatrix} 23 & 34 & 21 & 3 & 247 & 7 & 37 \\ 23 & 38 & 0 & S & 2 & 23 & 7 & 9 \end{bmatrix}$	
15	19 49 51 S 21 3 + 9	8 21 56 38 S 12	232 + 1422	234139 S $ 159 + 9$	0 15
16	19 54 8 S 20 52 +10 19 58 24 S 20 40 +10		$212 + 1418 \\ 51 + 1413$	$egin{bmatrix} 23\ 45\ 19\ 8 & 1\ 36\ +\ 84\ 23\ 48\ 57\ 8 & 1\ 12\ +\ 85 \end{bmatrix}$	
18	20 240 S 20 28 +10	S 22 814 S 11	30 +14 8	235236 S 048 + 8	8 18
19	20 655 S 2015 +11	6 22 12 5 S 11		235615 S $ 024 + 75$	
20 21	20 11 9 S 20 2 +11 20 15 23 S 19 49 +11	4 22 15 55 S 10 0 22 19 44 S 10	$\begin{vmatrix} 47 & +13 & 56 \\ 25 & +13 & 49 \end{vmatrix}$	$egin{bmatrix} 23\ 59\ 53\ S & 0\ 1\ +\ 7\ 3\ 0 & 3\ 32\ N & 0\ 23\ +\ 7\ 1 \end{bmatrix}$	
22	20 19 35 S 19 35 +11	7 22 23 33 S 10	3 +1341	0.710 N 047 + 65	5 22
23	20 23 47 8 19 21 +12	2 22 27 31 S 9	41 + 13 32	0.1048 N 1.10 + 6.3	
24 25	20 27 59 S 19 7 +12 20 32 9 S 18 52 +12		19 + 13 23 57 + 13 14	$\begin{bmatrix} 0.14.26 & N & 1.34 & + 6.1 \\ 0.18 & 4 & N & 1.57 & + 6 \end{bmatrix}$	8 24 0 25
:26	20 36 19 S 18 37 +12	3 22 38 42 S 8	34 +13 4	0.2142 N 221 + 54	2 26
27 28	20 40 27 S 18 21 +13 20 44 35 S 18 6 +13	6 22 42 28 S	$312 + 1253 \\ 49 + 1242$	$\begin{array}{ c c c c c c c c c c c c c c c c c c c$	
23	20 48 43 8 17 49 +13		49 + 1242	$oxed{ \hspace{0.6cm} } 02859 oxed{ \hspace{0.6cm}N} 3 8 + 5 \\ oxed{ \hspace{0.6cm} } 03237 oxed{ \hspace{0.6cm}N} 331 + 44$	
30	20 52 49 S 17 33 +13 3			$0.3615 \mathrm{N} \cdot 3.55 + 4.2$	all out
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Date:	20 56 54 S 17 16 +13 April.	6 Ma		03953 N 418 + 41	0 31 Date
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3		N 22 57	+355		N 17 26	+ 554	10 49 55		-0.50	3		
5		N 22 52 N 22 47	+45 +416		N 17 11 N 16 54	+549 + 543	10 53 32 10 57 8			4 5		
6		N 22 41	+426	9 5 5 5	N 16 38	+536	11 0 45		-150	6		
7	7 642	N 2234	+ 436	9 9 49	N 16 21	+529	11 421		-210	7		
8		N 22 28	+445	9 13 38		+522	11 757	N 535		8		
9		N 22 20	+ 454	9 17 26		+ 514	11 11 33		-251	9		
10		N 22 13 N 22 5	+53 + 511	9 21 14 9 25 1	N 15 29 N 15 12	+555 +455	11 15 9 11 18 45		-312 -333	10		
12		N 21 57	+518	9 28 47	N 1454	+ 446	11 22 20		_ 354	12		
13	7 31 11	N 21 48	+526	93234	N 14 35	+ 435	11 25 56	N 341	- 415	13		
14		N 21 39	+532	9 36 19	N 14 17	+ 421	11 29 31		- 4:16	14		
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17		N 21 20 N 21 10	+544 $+550$	$94349 \\ 94733$	N 13 39 N 13 20	+41 + 348	11 36 42 11 40 17		- 5 39	17		
18		N 20 59				+335	11 43 53	N 145	- 6 0	18		
19		N 20 49	+559	9 54 59	N 1241	+ 322	11 47 28	N 122	— 6 21	19		
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Corrections in Minutes and Seconds of Right Ascension, Declination and Equation of Time for Hours up to 18.

Degrees.
Deg
15 30
45
60 75
90
105
135
150
180
195
210 225
240
$\begin{bmatrix} 255 \\ 270 \end{bmatrix}$

irs.	VARIATION IN MINUTES FOR 24 HOURS.												
Hours	1	2	3	4	5	6	7	8 9		10	20	Degrees.	
	,	1 11	1 11	' '/	1 11	1 11	, ,,	1 11	1 11	1 11	1 11		
1	2	5	7	10	12	15	17	20	22	25	50	15	
2	5	10	15	20	25	50	35	40	45	50	1 40	30	
3	7	15	22	30	37	45	52	1	1 7	1 15	2 30	45	
4	10	20	30	40	50	1	1 10	1 20	1 30	1 40	3 20	60	
5	12	25	37	50	1 2	1 15	1 27	1 40	1 52	2 5	4 10	75	
6	15	30	45	1	1 15	1 30	1 45	2	2 15	2 30	5	90	
7	17	35	52	1 10	1 27	1 45	2 2	2 20	2 37	2 55	5 50	105	
8	20	40	1	1 20	1 40	2	2 20	2 40	3	3 20	6 40	120	
9	22	45	1 7	1 30	1 52	2 15	2 37	3	3 22	3 45	7 30	135	
10	25	50	1 15	1 40	2 5	2 30	2 55	3 20	3 45	4 10	8 20	150	
11	27	55	1 22	1 50	2 17	2 45	3 12	3 40	4 7	4 35	9 10	165	
12	30	1	1 30	2	2 30	3	3 30	4	4 30	5	10	180	
13	32	1 5	1 37	2 10	2 42	3 15	3 47	4 20	4 52	5 25	10 50	195	
14	35	1 10	1 45	2 20	2 55	3 30	4 5	4 40	5 15	5 50	11 40	210	
15	37	1 15	1 52	,2 30	3 7	3 45	4 22	5	5 37	6 15	12 30	225	
16	40	1 20	2	2 40	3 20	4	4 40	5 20	6	6 40	13 20	240	
17	42	1 25	2 7	2 50	3 32	4 15	4 57	5 40	6 22	7 5	14 10	255	
18	45	1 30	2 15	3	3 45	4 30	5 15	6	6 45	7 30	15	270	

Explanation of the Sidereal and Solar Time Table.

The Sidereal Time = Mean Solar + Correction. Mean Solar Time = Sidereal — Correction.

To Find the True Sidereal Time.

The sun's Right Ascension + or — the Equation of time is the Sidereal time at Greenwich, mean noon.

The sign + or — must be used as noted in the Astronomical or Nautical Almanac for the given day. For any other meridian or longitude from Greenwich, correct the sun's R. A. and the equation of time, and perform the same operation.

	I.V.E. I	RACII	ON OF	I II II I I I	EA V E	ILL DO	CETTO	TIA TX	MILLOI	7780	908
Alt.	Refc.	Alt.	Refr.	Alt.	Refr.	Alt.	Refr.	Alt.	Refr.	Alt.	Refr.
D.M.	M.S.	D.M.	M. S.	D. M.	M.S.	D. M.	M.S.	D.	M.S.	D.	M. S.
0. 0	33. 0	2.30	16.23	6.30	7.52	12.20	4.16	30	1.38	60	0.33
0. 5	32.11	2.35	16. 4	6.40	7.41	12.40	4. 9	31	1.35	61	0 32
0.10	31.22	2.40	15.45	6.50	7.31	13. 0	4. 3	32	1.31	62	0.30
0.15	30.36	2.45	15.27	7. 0	7.21	13.20	3.57	33	1.28	63	0.29
0.20	29.50	2.50	15. 9	7.10	7.12	13.40	3.51	34	1.24	64	0.28
0.25	29. 6	2.55	14.52	7.20	7. 3	14. 0	3.46	35	1.21	65	0.27
0.30	28.23	3. 0	14.35	7.30	6.54	14.20	3.40	36	1.18	66	0.25
0.35	27.41	3, 5	14.19	7.40	6.46	14.40	3.35	37	1.16	67	0.24
0.40	27. 0	3.10	14.03	7.50	6.38	15. 0	3.30	38	1.13	68	0.23
0.45	26.20	3,15	13.48	8. 0	6.30	15.30	3.23	39	1.10	69	0.22
0.50	25.42	3.20	13.33	8.10	6.22	16. 0	3.17	40	1.8	70	0.21
0.55	25. 5	3.25	13.19	8,20	6.15	16.30	3.11	41	1. 5	71	0.20
1. 0	24.29	3.30	13.05	8.30	6. 8	17. 0	3. 5	42	1. 3	72	0.19
1. 5	23.54	3.40	12.39	8.40	6. 1	17.30	2.59	43	1. 1	73	0.17
1.10	23.20	3.50	12.14	8.50	5.55	18. 0	2.54	44	0.59	74	0.16
1.15	22.47	4. 0	11.50	9. 0	5.49	18.30	2.49	45	0.57	75	0.15
1.20	22.15	4.10	11.28	9.10	5.43	19. 0	2.44	46	0.55	76	0.14
1.25	21.44	4.20	11.07	9.20	5.37	19.30	2.40	47	0.53	77	0.13
1.30	21.15	4.30	10.47	9.30	5.31	20. 0	2.36	48	0.51	78	0.12
1.35	20.46	4.40	10.28	9.40	5.26	20.30	2.32	49	0.50	79	0.11
1.40	20.18	4.50	10.10	9.50	5.20	21. 0	2.28	50	0.48	80	0.10
1.45	19.51	5. 0	9.53	10. 0	5.15	21.30	2.24	51	0.46	81	0, 9
1.50	19.25	5.10	9.37	10.15	5. 8	22. 0	2.20	52	0.45	82	0.8
1.55	18.59	5.20	9.21	10.30	5. 0	23. 0	2.14	53	0.43	83	0. 7
2, 0	18.35	5 .30	9. 7	10.45	4.54	24. 0	2. 7	54	0.41	84	0. 6
2. 5	18.11	5.40	8.53	11. 0	4.47	25. 0	2. 2	55	0.40	85	0. 5
2.10	17.48	5.50	8 39	11.15	4 41	26. 0	1.56	56	0.38	86	0. 4
2.15	17.26	6. 0	8.27	11.30	4.35	27. 0	1.51	57	0.37	87	0. 3
2.20	17. 4	6.10	8.15	11.45	4.29	28. 0	1.47	58	0.36	88	0. 2
2.25	16.44	6.20	8. 3	12. 0	4.23	29. 0	1.43	59	0.34	89	0. 1

	2011									-
Con	versio	n oi	fSide	ereal			Sola			Π'
Hour.	Corr.	Min.	Corr.	Min.	Corr.	Sec.	Corr.	Sec.	Corr.	Н
H.	M.S.	M.	s.	M.	S.	S.	S.	S.	S.	П
1	0 9.8	1	0.2	31	5.1	1	0.0	31	0.1	Н
2	0 19.7	2	0.3	32	5.2	2	0.0	32	0.1	П
3	0 29.5	3	0.5	33	5.4	3	0.0	33	0.1	Ш
4	0 39.3	4	0.7	34	5.6	4	0.0	34	0.1	Н
5	0 49.1	5	0.8	35	5.7	5	0.0	35	0.1	ł
6	0 59.0	6	1.0	36	5.9	6	0.0	36	0.1	Ш
7	1 8.9	7	1.1	37	6.1	7	0,0	37	0.1	П
8	1 18.7	8	1.3	38	6.2	8	0.0	38	0.1	П
9	1 28.6	9	1.5	39	6.4	9	0.0	39	0.1	Н
10	1 38.4	10	1.6	40	6.6	10	0.0	40	0.1	Н
11	1 48.2	11	1.8	41	6.7	11	0.0	41	0.1	П
12	1 58.1	12	2.0	42	6.9	12	0.0	42	0.1	i
13	2 8.0	13	2.1	43	7.0	13	0.0	43	0.1	
14	2 17.8	14	2.3	44	7.2	14	0.0	44	0.1	
15	2 27.6	15	2.5	45	7.4	15	0,0	45	0.1	
16	2 37.5	16	2.6	46	7.5	16	0.0	46	0.1	Į.
17	2 47.3	17	2.8	47	7.7	17	0.0	47	0.1	П
18	257.1	18	2.9	48	7.9	18	0.0	48	0.1	Н
19	3 7.0	19	3.1	49	8.0	19	0.1	49	0.1	
20	3 16.9	2 0	3.3	50	8.2	20	0.1	50	0.1	
21	3 26.7	21	3.4	51	8.4	21	0.1	51	0.1	
22	3 36.5	22	3.6	52	8.5	22	0.1	52	0.1	
23	3 46.4	23	3.8	53	8.7	23	0.1	53	0.1	
24	3 56.3	24	3.9	54	8.8	24	0.1	54	0.1	
		25	4.1	55	9.0	25	0.1	55	0.2	
		26	4.3	56	9.2	26	0.1	56	0.2	1
		27	4.4	57	9.3	27	0.1	57	0.2	1
		28	4.6	58	9.5	28	0.1	58	0.2	1
		29	4.8	5 9	9.7	29	0.1	59	0.2	1
		30	4.9	60	9.8	30	011	60	0.2	1

The Sun's Parallax

in Alt	itude.
Altitude.	Parallax.
Ð.	S
0	9 9 8 8 7 6 5 4 4 3
10	9
20	8
30	8
40	7
50	6
55	5
60	4
65	4
70	3
75	2
80	. 2
85	1
90	0

Explanation.

The sun's parallax must be added to the observed altitude.

LATITUDE AND APPARENT TIME

By Altitude of the Heavenly Bodies.

Notation of Letters.

A = meridian altitude above horizon.

D = declination, to be found in the Astronomical Almanac.

l = latitude of the place of observation.

L =angle of apparent time from noon.

 $\alpha =$ any altitude of the heavenly body, before or after noon.

When the lutitude and declination are of

Equal Name.

Latitude. l = 90 + D - A. Altitude. A = 90 + D - l. Declination, D = A + l - 90.

Apparent Time.

When the latitude and declination are of

Different Names.

Latitude. l = 90 - A - D. A = 90 - l - D. Altitude. Declination, D = 90 - A - l.

Apparent Time.

 $\cos L = \sin a \sec l \sec D - \tan l \tan D$. $\cos L = \sin a \sec l \sec D + \tan l \tan D$.

At sea the altitude is observed from the visible horizon of the ocean, from which must be subtracted the dip of horizon. (See table, page 131.)

On land the horizon must be determined by a spirit-level, or more correctly by an artificial horizon of quicksilver, oil, syrup or some similar liquid.

The refraction of light through the atmosphere (see table, page 503) must also be subtracted from the observed altitude.

When the sun or moon is observed, the parallax must be added to the observed altitude.

Latitude.

Example 1. On the 7th of April, 1872, the sun's lower limb was observed to be 51° 42′ 50″ above the horizon at noon, in longitude about 45° west of Greenwich; the observation was made from the deck of a vessel 20 feet above the sea. Required. the sun's true altitude and latitude of observation?

The declination and latitude are both north or of equal name.

Dip of horizon for 20 feet, Refraction, 51°,	4' 24" 46
⊙'s scmi-diameter,	16 00
11.	21, 10
Sun's parallax, subtract.	6
Correction to be subtracted,	21 4
O's observed altitude, 51	42 50
O's true altitude, 51°	21' 46"

Declination Naut. Almanac, 7° 3′ 19" Correct. 45° W. long., add 2 48 True declination, . D = 7Add. . . 90 True altitude, subtract A = 51 21 46 The required latitude, $l = 45^{\circ} 44' 21''$

Artificial Horizon.

When the observation is made by a sextant through an artificial horizon, the observed angle must be divided by 2 for the altitude, and there will be no correction for dip of horizon, nor for semi-diameter, as the sun's discs are brought to cover one another. When a regular quicksilver horizon is not at hand, some slimy liquid, like oil or molasses, in an open vessel, may be used in calm weather.

In perfectly calm weather the altitude may be taken in a pool of water, which has been done by the author in South America.

Apparent Time.

Example. On the 8th of February, 1872, the sun's true altitude was found to be $a = 30^{\circ} 46' 29''$ in the afternoon, the latitude $l = 38^{\circ} 18' 38''$ N., and declination corrected $D = 15^{\circ} 5' 10''$ S. Required, the apparent and mean time of obser-

The latitude and declinations are of different names.

Cos. $L = \sin .30^{\circ} 46' 29'' \times \sec .38^{\circ} 18' 38'' \times \sec .15^{\circ} 5' 10'' = 0.68763 + \tan .38^{\circ} 18' 38'' \times \tan .15^{\circ} 5' 10'' = 0.21293$ $L = 1h. 49m. 13s. = \cos .29^{\circ} 18' 15'' = 0.88856$ Apparent time of obs., 14 Equation of time, add

> 2h. 3m. 39s., the time required. Mean time,

The calculation with logarithms is set up as follows:

 $Log. \sin 30^{\circ} 46' 29'' = 9.70898$ Tan. = 9.89765sec.38 18 38 = 0.10531 $5 \ 10 = 0.01529$ Tan. = 9.43067. . . 9.82958 9.32832 Logarithms, Natural numbers, . 0.67563 0.212930.21293 Add for different names,

 $L = 1h.49m.13s. = 27^{\circ} 18' 15'' = 0.88856 = cosino for hour angle.$ The hour angle in time can be read off directly for the cosine in the trigonometrical tables.

When the observation is made in the forenoon, subtract the cosine hour angle from 12 hours; or it can be read off directly from the tables by calling cosine for sine L.

To Find the Longitude.

Small differences in longitude can be obtained from actual measurement, as explained in Plane Sailing and Traverse Surveying.

For great distances, it is necessary to know the simultaneous times at the two

meridians between which the longitude is required.

At sea, the time at a distant meridian is kept by a chronometer, generally regulated for Greenwich mean time, and the difference in time between the two meridians is the difference in longitude.

The Greenwich mean time can also be found by astronomical observations and the Nautical Almanac. The common astronomical observations for Greenwich mean time are the moon culminating stars, lunar distances, eclipses of the sun and moon, all of which are too complicated to be introduced in this Pocket-book.

Eclipses of Jupiter's Satellites.

The most simple astronomical observations for Greenwich mean time are of the eclipses of Jupiter's satellites, but, unfortunately, the tables for those eclipses in the English Nautical Almanac are not yet reliable, as has been found by the author in using these tables in the interior of South America. The observation of several eclipses in one locality did not agree with the time given in the Nautical Almanac, from which I suspected the tables to be incorrect. On my arrival in London, in August, 1871, I called on the superintendent of the Nautical Almanac, Professor Hind, and explained my experience in relation to those eclipses and tables. The distinguished professor very kindly informed me that "there has not yet been sufficient accurate observations made of the time of eclipses of Jupiter's satellites to make the tables reliable—the actual time of eclipse may differ minutes from that in the tables."

The tables of eclipses of Jupiter's satellites are omitted in the American Nauti-

cal Almanac, perhaps for the same reason as given by Professor Hind.

It is strange that the elements of Jupiter's satellites are not yet better known;

there must be a screw loose somewhere.

This is a subject well worthy of attention at the National Observatory at Wash-The eclipses of Jupiter's satellites can be observed by an ordinary good spy-glass, even at sea, in calm weather, which would be of great importance over the whole world if accurate tables could be procured. Chronometers could then be corrected with great precision to Greenwich time in any part of the world, and by simple addition or subtraction of time the longitude could be determined correctly without the aid of complicated, bulky and expensive instruments, which few can afford to buy or know how to manage.

There are some 300 eclipses in Jupiter's satellites every year.

506				A	STRONO	MY.					
		E	lement	s of the	he Pla	netary	y Syst	em.			
The principal Planets.	Signs.	Mean distand fr. Sur	e period,	Eccent. part, sm. axis	eter in	Vel orbt Miles per sec.	Rota- tion in hours.	Dens-	Mass.	Vol	lume.
Sun,					882000	per neo.	H. M. 607 48	0.25	355000	137	'8000
Mercury,	ğ	0.3871		0.2055	3140	30.4	24 05	1.12	0.06966		6218
Venus, Earth,	O → → → → →	0.7233 1.	365.25	0.0068	7800	22.3	23 21	0.92	0.877	1	531
Mars, .	Pr	1.5236		$0.0168 \\ 0.0933$	7912 4100	18.9 15.33	$\begin{bmatrix} 24 & 0 \\ 24 & 37 \end{bmatrix}$	1. 0.95	1. 0.13 1 3	1.	384
Jupiter,	24	5.2028	3 4332.6	0.0482	87000	8.31	9 56	0.24	317.5		22.5
Saturn,	り出	9.5388		0.0561	79160	6.14	10 29	0.:4	139.5		96.2
Uranus,		19.182		0.0467	34500	4.33	9 30	0.21	198.		2.47
Neptune,	- 1	30.03	1	0.0087	41500	3.45	• •	0.14	20.	14	13.5
Positio 2d	m l M	of so: agnit	me Star tudes, d	rs of a Jan. 1	the 1st , 1874.	and	Tide	Tabl	le.		Rise feet.
NAME OF S	25.5	Mg.	Right	Ann.	Decli-	Ann.	Alban	y, N.		40	
NAMEOF	STAR	td.	As'sion.	Var.	nation.	Var.		a, Ger y. N.			
							Antw	erp, Be	$ Y_{.,} + 5$		
N Hamian	hana				North.		Baltin	nore,	_ 1	52	12
N. Hemisp			h. m. s.	s.	0 / //	"	Belfas	t, Ire.,	+ 8	36	
a Andron a Polaris,		$\begin{bmatrix} 2 \\ 1 \end{bmatrix}$	$\begin{bmatrix} 0 & 1 & 52 \\ 1 & 12 & 38 \end{bmatrix}$		28 23 41 88 28 15	+19.9 + 19.0	Berge	n, Noi		37	
a Arietis,		2	$\begin{array}{cccccccccccccccccccccccccccccccccccc$		22 51 55			anx, F n, Mas		34 20	12
a Persi,		2	3 15 20	+4.25	49 24 38	+13.1		gne, F		18	19
a Aldeba	ran,	1 1	4 28 41	+3.43	16 15 14		Bueno	s Ayre	es, + 6	6	
α Capella β Tanri,	,	$\frac{1}{2}$	5 7 23 5 18 20	+4.42 + 3.79	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	1	Breme	en,	+ 8		
a ² Castor,		2.1	7 26 33	+3.19 $+3.84$			Cadiz,	Spain		22 42	10
a Procyon	n,	1	7 32 42	+314	5 32 45	-8.97	Calc't	ta,Ben		23	19
β Pollux,		1.2	7 37 36	+3.68	28 19 42	-8.35	Charle	eston,	+ 5	44	5
α Regulu	s,	$\begin{vmatrix} 1.2 \\ 2 \end{vmatrix}$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	+3.20		- 17.4	Cherb	ourg, l	r. + 8	23	20
a Great B	Bear.	2	10 55 56	+3.76	62 25 50	-18.0		lenry, 3. Hop		$\begin{vmatrix} 3 \\ 29 \end{vmatrix}$	4
y Great E	Bear,	2.3	11 47 12	+3.19	54 23 42	-20.0		Hern,		9	9
η Great B	ear,	2 1	13 42 34	+2.37	49 56 33	- 18.1	C. Her	ilopen		41	5
a Arcturu a Coronæ		1 -	14 9 55 15 29 21	+2.73 +2.54	19 50 22 27 8 24	-18.8	Dublin	Bar,	+ 9	5	12
5 Herculi		1 ~ ~ !	16 36 32	+2.26		-12.3 -6.69	Glasse	tar, Sjow, Sco	$\frac{1}{100}$	$\begin{vmatrix} 13 \\ 42 \end{vmatrix}$	•
al Herculi	is,	Var.	17 8 54	+273	14 32 8	-4.39	Hamb	urg.		22	
a Vega,			18 32 40	+2.03			Halifa	x, N. A	1 + 5	42	8
a Altair,		1.2	19 44 38	+2.93	8 32 13	+9.22	Havar	ia <u>,</u> Cub		41	3
S. Hemisph	iere.				South.	5	Havre Ilull,	, Fr.,		44	12
β Ceti,		2	0 37 16	+3.01	18 40 43	+19.8		est,U.		$\begin{vmatrix} 22 \\ 22 \end{vmatrix}$	18 2
a Acherna	ar,	1	1 33 01	+2.23	57 52 38	+18.4	Lisbor	B. Por	rt. + 0	13	
β Rigel, δ Orionis,		$\begin{vmatrix} 1 \\ 2 \end{vmatrix}$	5 8 29 5 25 34		8 20 57 0 23 40		Liverp	ool,		16	25
a Canopus		ī	6 21 9	+1.33	52 37 39	+2.96 -1.85	New I	ork, Lavan	1 + 6	6	5
a Sirius,	Ť	1	6 39 36	+2.64	16 32 41	-4.69	Newca	stle, l	$\begin{vmatrix} A \cdot + 8 \\ -4 \cdot + 2 \end{vmatrix}$		17
€ Canis M	lajor		6 53 40			-4.67	Norfol	k, U.S	1., + 5	14	7
a Hydræ,		$\begin{vmatrix} 2\\2 \end{vmatrix}$	9 13 43 9 21 24	+1.603 +2.94	58 44 47	-14.9	Ostend				16
al Crucis,		11	12 19 36		62 23 58	-15.4 -19.9	Panan Philad		$+\frac{1}{0}$		24
a Spica,		1	13 18 33	+3.15	10 30 11	-18.9	Portsn			10	6
β Centaur	i,		13 54 57	+4.16	59 45 50	-17.6	Eng.	& U. Ś	1. + 9		10
a ¹ Centam β Libræ,	1,		14 31 4 15 10 14	+ 4.04	60 18 39 8 54 59		Provid		+ 5	25	
β¹ Scorpii,			15 58 7	+3.22 + 3.48		-13.5 -10.2	Quebe Queen				17
a Antares	3,	1.2	16 21 41	+ 3.67	26 9 1	- 8.37	Rio Ja				6
a Australi			16 35 21	+6.28	68 47 33	— 7.32	Rotter	dam,	+1		
α Pavonis β Aquarii.				+4.79		+11.1	Sandy	Hook	$, \mid +4 \mid$	58	6
a Cruis,	,			+3.16 + 3.81	6 7 28 47 34 11	+15.6 + 17.2	Valpar San Fr	caiso,	+ 7	2	5
a Fomalh	aut,	1.2		+3.33	30 17 23	+19.0	Washi	ancisc ngtan	0, + 89 + 18		6
-				-			,		T 1	00	

To Find the Meridian or True North by the North Star, Polaris.

Potaris is not in the true north, but revolves in a circle of radius 1° 22′ 24″ co-declination on the 1st of January, 1872, which diminishes 19″ every year; that on the 1st of January, 1873, its co-declination will be 1° 22′ 5″.

The position of Polaris is generally traced by the direction of the stars α and β , in the Great Bear, which point nearly to the North Star. See figure.

Polaris passes the meridian, or is true north when the star ϵ in the Great Bear is perpendicular either over or under Polaris. In low latitudes the Polaris is near the horizon, and the star ϵ cannot be seen when under, but must be observed at its upper transit. When the star ϵ is horizontal with Polaris, substract the radius of the circle, and the remainder will be the true north, from which the variation of the compass is ascertained. There is no star near the South Pole from which a similar observation can be made.

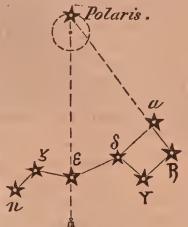


Table Showing how Much Earlier any Fixed Star Passes the Meridian, rises or sets, in number of days or nights up to 100.

•	1		1						
Nights.		ghts		Nights.		Nights.		Nights.	
e in	H.M. S.	Nig	H. M. S.	lig.	H. M. S.	118	H. M. S.	[Si	H.M. S.
F				~		4		. 4	
1	0.355.9	11	0 43 15.0	21	1 22 34.1	31	2 01 53.2	45	2 56 55.0
2	0 7 51.8	12	0 47 10.9	22	1 26 30.0	32	2 05 49.1	50	3 16 35.9
3	0 11 47.7	13	0 51 06.8	23	1 30 25.9	33	2 09 45.0	55	3 36 15.0
4	0 15 43.6	14	0 55 02.7	24	1 34 21.8	34	2 13 40.9	60	3 55 54.5
5	0 19 39.5	15	0 58 58.6	25	1 38 17.7	35	2 17 36.8	65	4 15 34.1
6	0 23 35.5	16	1 02 54.5	26	1 42 13.6	36	2 21 32.7	70	4 35 13.6
7	0 27 31.4	17	1 06 50.5	27	1 46 09.6	37	2 25 28.6	75	4 54 53.2
8	0 31 27.3	18	1 10 46.4	28	1 50 05.5	38	2 29 24.5	80	5 14 32.7
9	0 35 23.2	19	1 14 42.3	29	1 54 01.4	39	2 33 20.4	90	5 53 51.8
10	0 39 19.1	20	1 18 38.2	30	1 57 57.3	40	2 37 16.4	100	6 33 10.9
	5 5 5 7 7 7 7	1 -0	1 - 10 00:2	11 00	1 1 01 01 0	11 -20	20, 10,4	1100	0 55 10.9

The preceding table is for regulating a watch, clock or chronometer. The fixed stars set 3 m. 55.909 s. earlier every day, and by observing the time of setting over a sharp, distant object, as a hill, mountain or a house, the time-keeper can be regulated with great precision.

Example. A fixed star is observed to set at 9 h. 35 m. 51 s.

The time-keeper has lost 51 - 06.7 = 44.3 seconds in 25 days, or 1.772 seconds per day.

To Find the Time When Any Star or Planet Passes the Meridian.

Subtract the sun's right ascension from that of the star, increased by 24 f necessary, and the remainder will be the apparent time when the star passes the meridian. The sun's R. A. must be corrected for longitude from Greenwich, and for time of observation. This is the best mode of finding the meridian and variation of the compass, but the apparent time must be correctly known.

To Find Which Star Passes the Meridian Near a Desired Time.

Add the sun's R. A. to the desired hour, and the sum will be the nearest R. A. of the star passing the meridian at that time. Reject 24 hours if necessary. Find in the table of stars the one which comes nearest to that R. A.

TO APPROXIMATE THE TIME OF HIGH WATER.

On account of the Moon's orbit being an ellipse, in which the Earth is one of the focuses, and that the major axis of that ellipse does not point to the Sun, but to a fixed constellation of stars, the actual time of high water and also that of passing the meridian are not equal for equal age of the Moon, but may differ as much as 15 minutes from the average in the accompanying table. Also, the force and direction of winds cause a still greater variation.

Find first the Moon's age for the given day, as described on page 496. Opposite the age in the table is the time of the day when the Moon is south, or passes the meridian, and in the following columns are the times of high water at London Bridge in the morning and afternoon. Add or subtract the time in the tide table, page 506, for any other location, and the sum or difference is the time of high water

at that place.

]	Moon	•		High wat London B	er at ridge.
Quart'r	Face	Age d.	South. h. m.	Age.	Morning. h. m.	Afternoon h. m.
e e lst quarter. Ha 2d quarter.		0 1 2 3 4 5 6 7 8 9 10 11 12 13 14	12 0 p. m. 12 49 " 1 38 " 2 26 " 3 26 " 4 4 " 4 55 " 6 42 " 6 30 " 7 19 " 8 8 " 8 57 " 9 46 " 10 34 " 11 23 "	0 1 2 3 4 5 6 7 8 9 10 11 12 13 14	1 59 2 21 2 50 3 18 3 47 4 16 4 50 5 24 6 7 7 7 8 33 10 14 11 28 Noon. 0 40	2 7 2 36 3 3 3 33. 4 2 4 31 5 5 5 45 6 35 7 46 9 25 10 54 11 54 0 17 1 0
F 3d quarter. # 4th quarter.		15 16 17 18 19 20 21 23 24 25 26 27 28 29 29 ¹ / ₂	12 12 a. m 1 1 " 1 50 " 2 38 " 3 27 " 4 16 " 5 5 " 5 54 " 6 42 " 7 31 " 8 20 " 9 9 " 9 58 " 10 46 " 11 35 " 12 "	15 16 17 18 19 20 21 22 23 24 25 26 27 28 29 29 ¹ / ₂	1 20 2 1 2 42 3 26 4 10 4 55 5 44 6 44 7 59 9 31 10 52 11 49 0 11 0 48 1 23 1 51	1 40 2 22 3 5 3 48 4 34 5 19 6 12 7 21 8 43 10 15 11 23 M'night. 0 29 1 5 1 36 2 7

High Water.

Examples.

Required, the time of H. W. in Philadelphia on the 8th of Feb., 1874?

Epact, year, . 12 pg. 497. Epact, month, 2 pg. 496. Date, February, 8. Moon's age, . 22 days.

H.W.Lond., 6h.44m. Phila. subt., 0 49 pg. 506. H.W.Phila., 5h.55m. in the morn., Feb. 8, 1874.

Required, the time of H. W. in Panama on the 7th of October, 1873?

Epact, year, 1 pg. 497. Epact, month. 8 pg. 496. Date in October, 7

Moon's age, 16 days.

H.W. Lond., 2h. 1m. a.m. Panama add 1 24, pg. 506 3h. 25m. a.m.

in Panama.

Elements of Jupiter's Satellites.

Order	Radius of	Time in days		Mass,	Diameter	
of	orbit, that		ar. Jupiter	that of	of satellite	
satellite.	of Jupiter=1	revolution.	per year.	Jupiter=1	miles.	
1st.	6.0485	1.7691	206.457	0.000017		
2d.	9.6235	5.5512	65.7952	0.000028		
3d.	15.3502	7.1546	51.0499	0.000088		
4th.	26.9983	16.6888	21.8855	0.000043		

Number of Moons or Satellites to each Planet.

Earth, 1. Jupiter, 4. Saturn, with rings, 8. Uranus, 8 moons.

SOUNDINGS.

To Reduce Soundings to Low Water.

Letters denote—

T =time in hours between high and low water.

t = time in hours from low water to the time when the soundings are taken. R = vertical rise of tide in feet from high to low water.

r = reduction of the sounding taken at the time, t, in feet.

$$v = \frac{180t}{T}$$
, and $r = \frac{1}{2}R \ (1 = \cos v)$,

 $-\cos v$ when v < 90

 $+\cos v$ when v > 90vater at 10 h. 15 m. p. m. Example. High water at 3 h. 45 m. Low water at

Time T = 6 h. 30 m.

The sounding taken at 5 h. 30 m. was 16 feet 6 inches.

> Time t = 1 h. 45 m. Vertical rise R = 9.75 feet.

Required, the reduction r=? and true sounding at low water?

$$v = \frac{180 \times 1.75}{6.5} = 48^{\circ} 30',$$
 $cos.v = 0.66262.$

Reduction $r = \frac{1}{2} \times 9.75 (1 - 0.66262) = 1.6445$ feet.

Sounding taken at 5 h. 30 m. was 16.5 feet. Reduction subtract r = 1.6447

14.8553 feet. True sounding at low water,

Reduction for Soundings to Low Water.

This table will answer for any unit of measure of rise.													
Rise	Time	e of so	undin	g in h	rs. and	l min.	before	or af	ter tha	t of h	igh w	ater.	Rise
R.	0.30	1	1.30	$\tilde{2}$	2.30	3	3.30	4	4.30	5	5.30	6	R.
	0.00	0.04	0.57	0.70	0.05	0.55	0.49	0.91	0.00	0.10	0.05	TO O	
1 1	0.98	0.94	0.87	0.78	0.67	0.55	0.43	0.31	0.20	0.12	0.05	0.01	1
2	1.97	1.88	1.74	1.56	1.34	1.10	0.86	0.62	0.40	0.24	0.10	0.02	2
3	2.95	2.82	2.61	2.34	$\frac{2.01}{2.02}$	1.65	1.29	0.93	0.60	0.36	0.15	0.03	3
4	3.93	3.76	3.48	3.12	2.63	2.20	1.72	1.25	0.82	0.46	0.20	0.04	4
5	4.92	4.70	4.35	3.90	3.35	2.74	2.15	1.56	1.03	0.58	0.25	0.05	5
6	5.91	5.65	5.22	4.68	4.03	3.30	2.58	1.87	1.23	0.69	0.30	0.06	6
7	6.90	6.59	6 10	5.46	4.70	3.84	3.01	2.18	1.44	0.81	0.35	0.07	7
8	7.88	7.52	6.97	6.24	5.36	4.40	3.44	2.50	1.65	0 93	0.40	0.08	8
9	8.86	8.47	7.84	7.02	6.03	4.94	3.87	2.80	1.85	1.04	0.45	0.09	9
10	9.85	9.41	8.71	7.79	6.71	5.52	4.30	3.12	2.06	1.16	0.50	0.10	10
11	10.9	10.3	9.59	8.59	7.39	6.05	4.74	3.43	2.27	1.28	0.55	0.11	11
12	11.9	11.3	10.5	9.37	8.06	6.60	5.16	3.74	2.47	1.40	0.60	0.12	12
13	12.8	12.2	11.3	10.1	8.72	7.14	5.60	4.05	2.63	1.51	0.65	0.13	13
14	13.8	13.2	12.2	11.0	9.40	7.70	6.02	3.36	2.89	1.62	0.70	0.14	14
15	14.8	14.1	13.0	11.7	10.0	7.25	6.45	3.67	3.09	1.74	0.75	0.15	15
16	15.8	15.0	14.0	12.5	10.7	8.78	6.88	5.00	3.30	1.85	0.80	0.16	16
17	16.8	16.0	14.8	13.3	11.4	9.35	7.31	5.25	3.50	197	0.85	0.17	17
18	17.8	17.0	15.7	14.0	12.1	9.90	7.75	5.60	3.70	203	0.90	0.18	18
19	187	17.9	16.6	14.8	12.8	10.4	8.17	5.91	3.81	2.20	0.95	0.19	19
20	19.7	18.9	17.5	15.6	13.4	11.0	8.60	6.23	4.11	2.32	1.00	0.20	20
21	20.7	19.8	18.3	16.4	14.1	11.5	9.04	6.54	4.32	2.43	1.05	0.21	21
22	21 7	20.7	19.2	17.2	148	12.1	9.16	6.85	4.53	2.55	1.10	0.22	22
23	22.7	21.7	20.0	18.0	15.4	12.6	9.90	7.16	4.73	2.67	1.15	0.23	23
24	23.7	22.6	20.9	18.7	16.1	13.2	10.3	7.47	4.94	2.78	1.20	0.24	21
25	24.7	23.5	21.8	19.5	16.8	13.7	108	778	5.14	2.90	1.25	0.25	25
26	25.6	24.5	22 7	2).3	17.4	14.3	11.2	8.10	5 52	3.01	1.30	0.26	26
27	26.6	25.4	23.5	21.1	18.1	14.9	11.6	8.41	5.55	3.13	1.35	0.27	27
28	27.6	26.4	24.4	21.9	18.8	15.4	12.0	8.72	5.76	3,25	1.40	0.28	28
29	28 6	27.3	25.3	22.7	19.1	16.0	12.5	9.03	5.96	3.36	1.45	0 29	29
30	29.6	29.3	26.2	23.4	20.1	16.5	12.9	9.34	6.17	3.48	1.50	0.30	30
R.	5.45	5.15	4.45	4.15	3.45	3.15	2.45	2.15	1.45	1.15	0.45	0.15	R.
Rise	Tim	ne of s	oundi	ig in l	rs. an	d min	. befor	e or a	fter t h	at of	low wa	ater.	Rise

To Find at what Time the Sun Sets and Rises.

Let v denote the time angle from 6 o'clock to when the sun sets or rises, then-Sin.v = tan.l tan.D.

Example. What time does the sun set and rise on the 21st of June, in 60° latitude?

The declination on this day is about 23° 27'.

 $\sin v = \tan .60^{\circ} \times \tan .23^{\circ} 27' = 0.75131 = \sin .3h$. 14m. 48s.

The sun rises at 2h. 45m. 12s., and sets at 9h. 14m. 48s.

To Find the Length of Day and Night.

DAY.—Double the time of sunset, is the length of the day. NIGHT .- Double the time of sunrise, is the length of the night.

Amplitude.

The angle or bearing from east or west to where any heavenly body sets or rises, is called the amplitude of that body, which, denoted by x, will be-

$$\sin x = \sec l \sin D$$
.

The amplitude is used for finding the variation of the compass.

Example. The sun's declination being 18° 25′ south, required, his amplitude in latitude 48° 45' north?

 $\sin x = \sec .48^{\circ} 45' \times \sin .18^{\circ} 25' = \sin .28^{\circ} 38' \text{ south,}$

the amplitude required.

Azimuth.

l = latitude, D = declination, and a = altitude. z = angle of azimuth, or bearing of the heavenly body from meridian to the pole above horizon.

When the latitude and declination are of
Differen

Equal Names—
$$m = \frac{l+a-D+90}{2}$$
Different Names—
$$m = \frac{l+a+D+90}{2}$$

$$n = \pm m \mp \left(90 - D\right)$$
. Subtract the smallest, and the remainder is n .

Cos. $\frac{1}{2}z = \sqrt{\cos m \cos n \sec l \sec a}$.

auche fohlykumao porscuvumxyz

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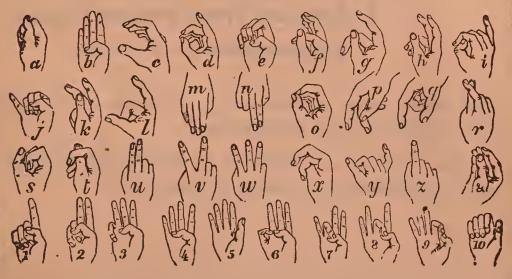


ABCDEFGHJRLMNDPDRSTUVWX Y3 abcdefghijklmnopgrsstuvwxyz

ABEDEFEHIJKLMYOPQRS IUUUXUZ. 1234567890 abcdefghijklmnopgrsfybbxyz.

DEAF AND DUMB ALPHABET.

Keep your hand horizontal for the letters a, g, h, r, s and t. For j and z describe the letter with the finger in the air. For x make a motion up and down with the index finger.



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